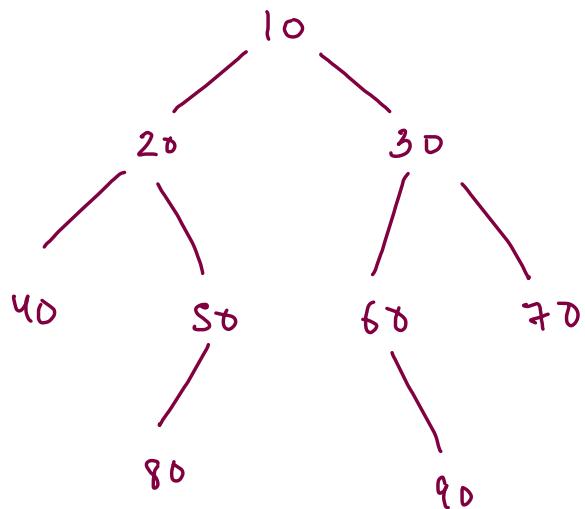
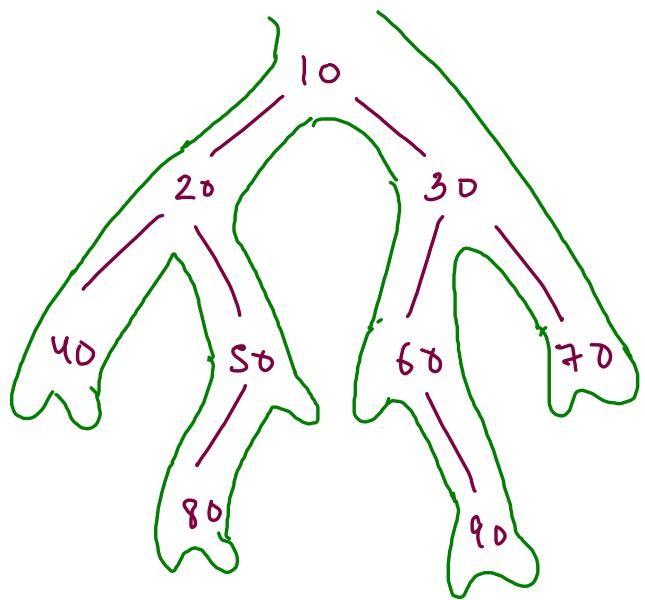


Binary Tree - Introduction And Data Members

↳ each node has atmost 2 child



Node {
 int data;
 Node left;
 Node right;
}



preorder

ans: 10 20 40 -1 -1 50 80 -1 -1
-1 30 60 -1 90 -1 -1 70 -1 -1

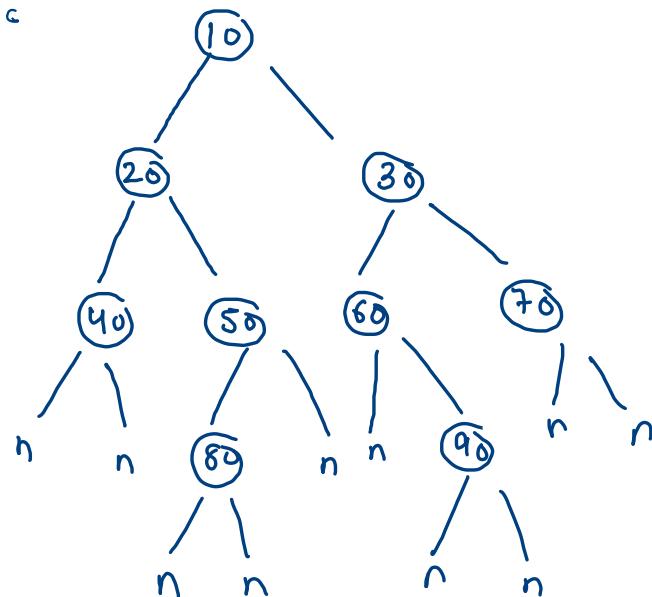
array: 10 20 40 -1 -1 50 80 -1 -1 -1 30 60 -1 90 -1 -1 70 -1 -1

0 → waiting for dc

1 → waiting for rc

2 → done, pop

root = 10



Pair 2

Node node;

int state;

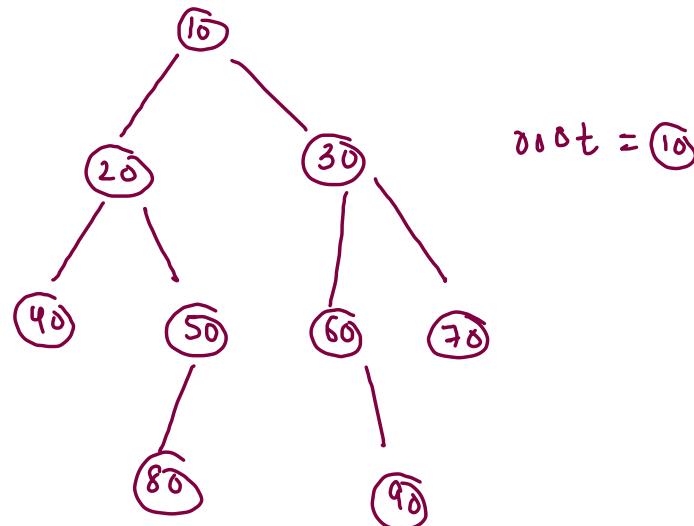
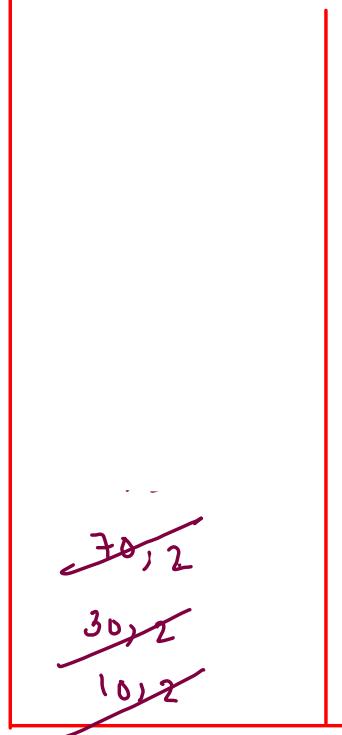
3

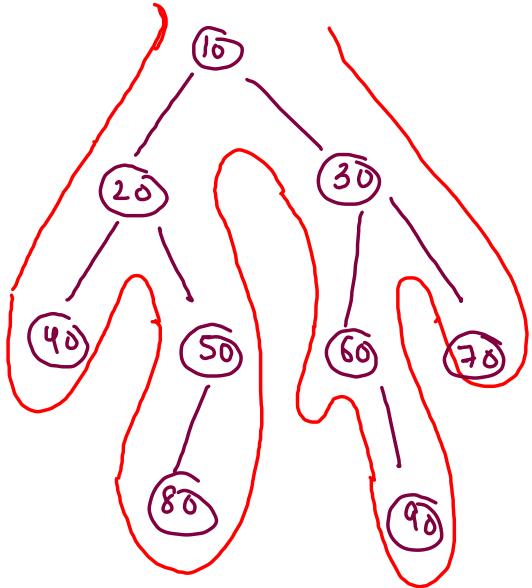
10 20 40 -1 -1 50 80 -1 -1 -1 30 60 -1 90 -1 -1 70 -1 -1

```

while(st.size() > 0) {
    Pair top = st.peek();
    if(top.st == 0) {
        //top's node is waiting lc
        if(arr[idx] == -1) {
            top.node.left = null;
        }
        else {
            Node node = new Node(arr[idx]);
            top.node.left = node;
            Pair lcp = new Pair(node,0);
            st.push(lcp);
        }
        top.st++;
        idx++;
    }
    else if(top.st == 1){
        //top's node is waiting rc
        if(arr[idx] == -1) {
            top.node.right = null;
        }
        else {
            Node node = new Node(arr[idx]);
            top.node.right = node;
            Pair rcp = new Pair(node,0);
            st.push(rcp);
        }
        top.st++;
        idx++;
    }
    else {
        //top's node is done
        st.pop();
    }
}

```





display(20)

20 ← 10 → 30

40 ← 20 → 50

. ← 40 → .

80 ← 50 → .

. ← 80 → .

60 ← 30 → 70

. ← 60 → 90

. ← 90 → .

. ← 70 → -

display(30)

```

public static void display(Node node) {
    if(node == null) {
        return;
    }

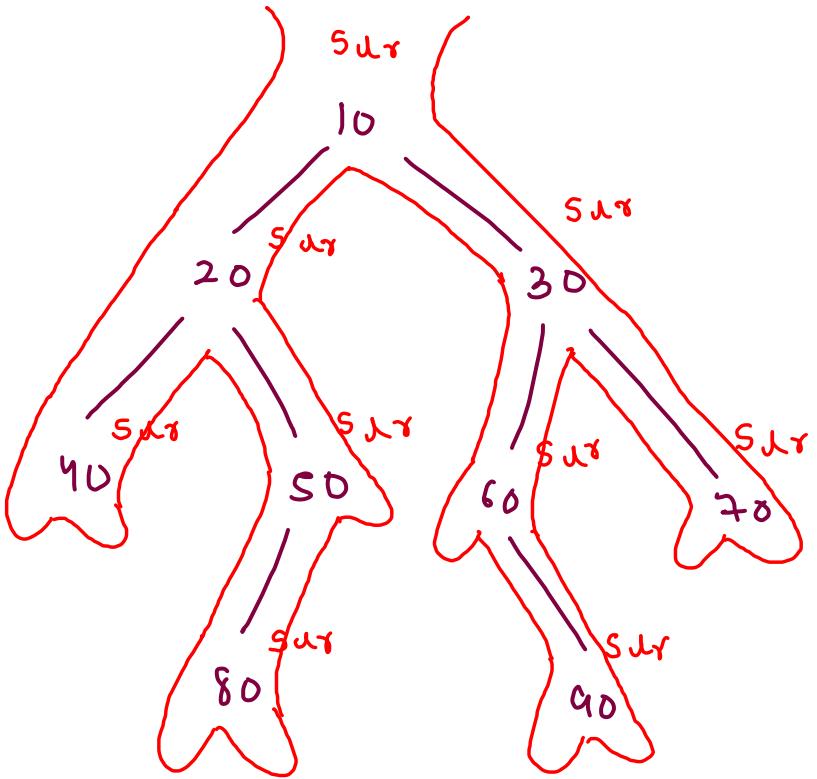
    String mp = " <- " + node.data + " -> ";
    String lp = (node.left == null) ? "." : (node.left.data + "");
    String rp = (node.right == null) ? "." : (node.right.data + "");

    System.out.println(lp + mp + rp);

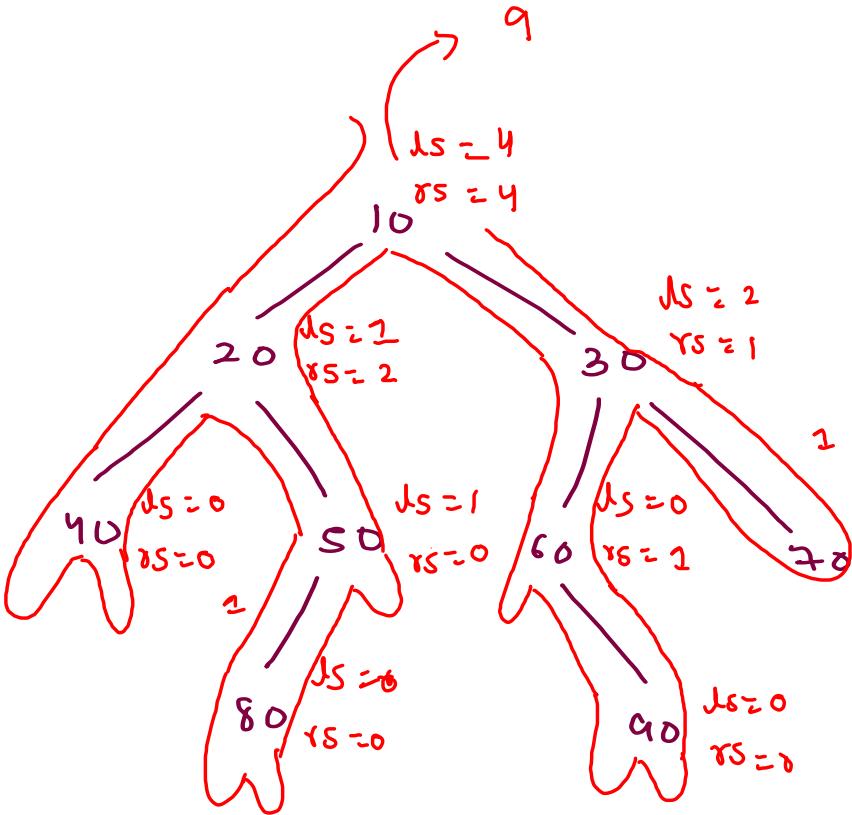
    display(node.left);
    display(node.right);
}

```

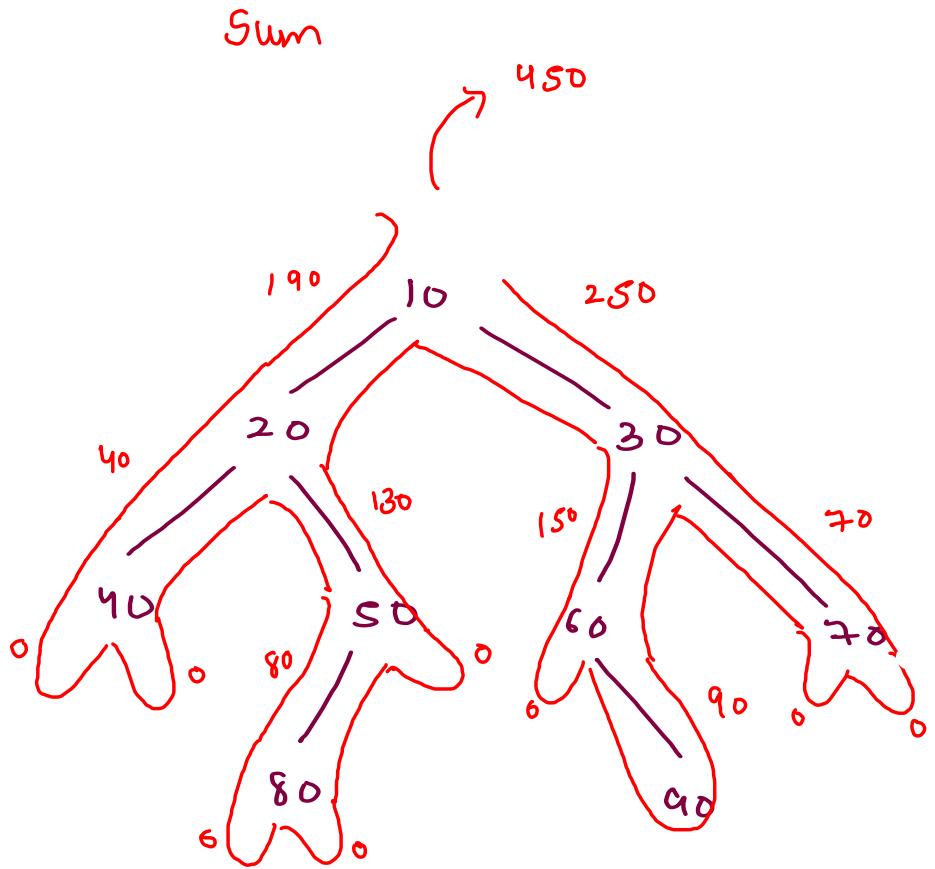
✓ 20 <- 10 -> 30
✓ 40 <- 20 -> 50
✓ <- 40 -> .
✓ 80 <- 50 -> .
✓ <- 80 -> .
✓ 60 <- 30 -> 70
✓ <- 60 -> 90
✓ <- 90 -> .
✓ <- 70 -> .



Size

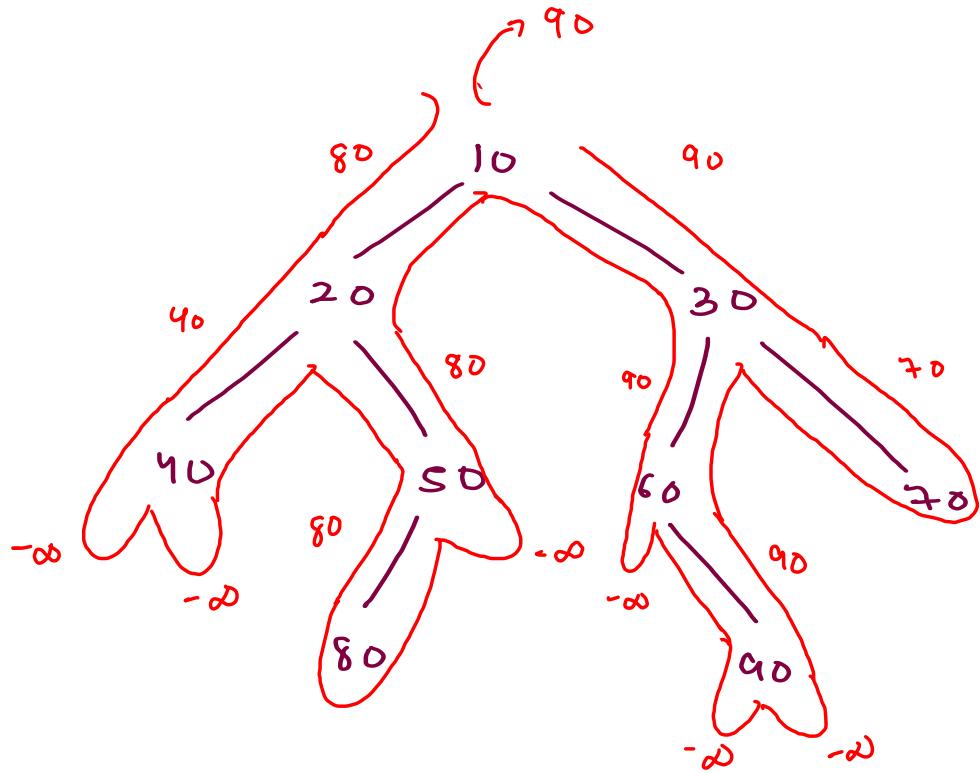


```
public static int size(Node node) {  
    if(node == null) {  
        return 0;  
    }  
  
    int ls = size(node.left); //Left subtree size  
    int rs = size(node.right); //right subtree size  
  
    return ls + rs + 1;  
}
```



```
public static int sum(Node node) {  
    if(node == null) {  
        return 0;  
    }  
  
    int ls = sum(node.left); //Left subtree sum  
    int rs = sum(node.right); //right subtree sum  
  
    return ls + rs + node.data;  
}
```

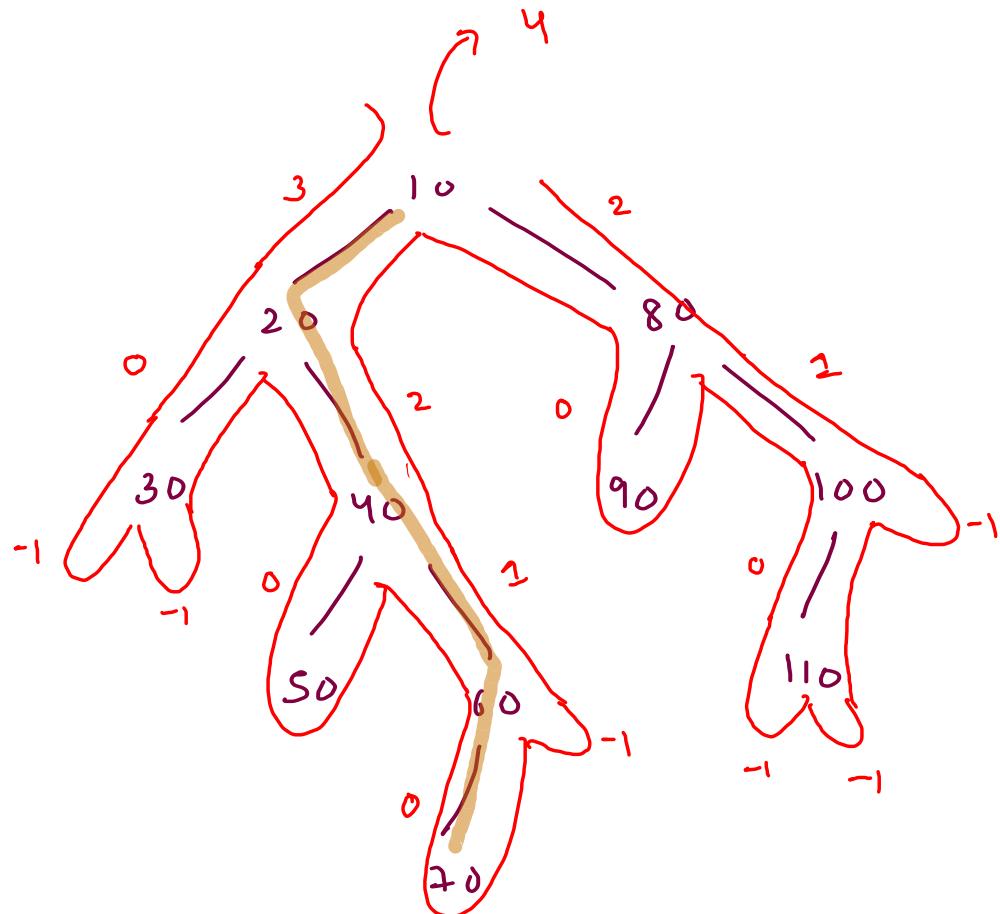
```
public static int max(Node node) {  
    if(node == null) {  
        return Integer.MIN_VALUE;  
    }  
  
    int lmax = max(node.left); //left subtree max  
    int rmax = max(node.right); //right subtree max  
  
    return Math.max(Math.max(lmax,rmax),node.data));  
}
```



```
public static int height(Node node) {
    if(node == null) {
        return -1;
    }

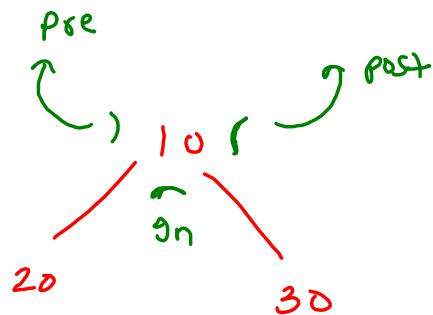
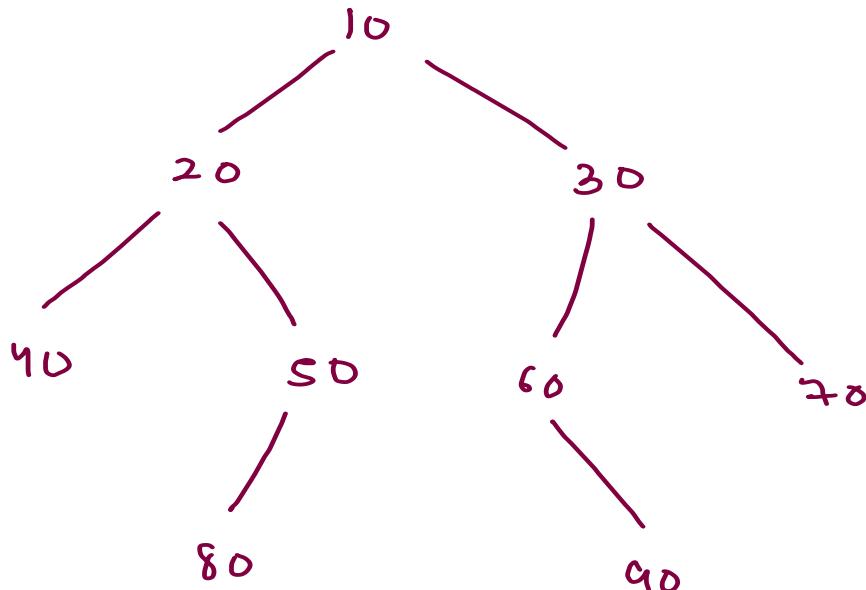
    int lht = height(node.left); //Left subtree height
    int rht = height(node.right); //right subtree height

    return Math.max(lht,rht) + 1;
}
```

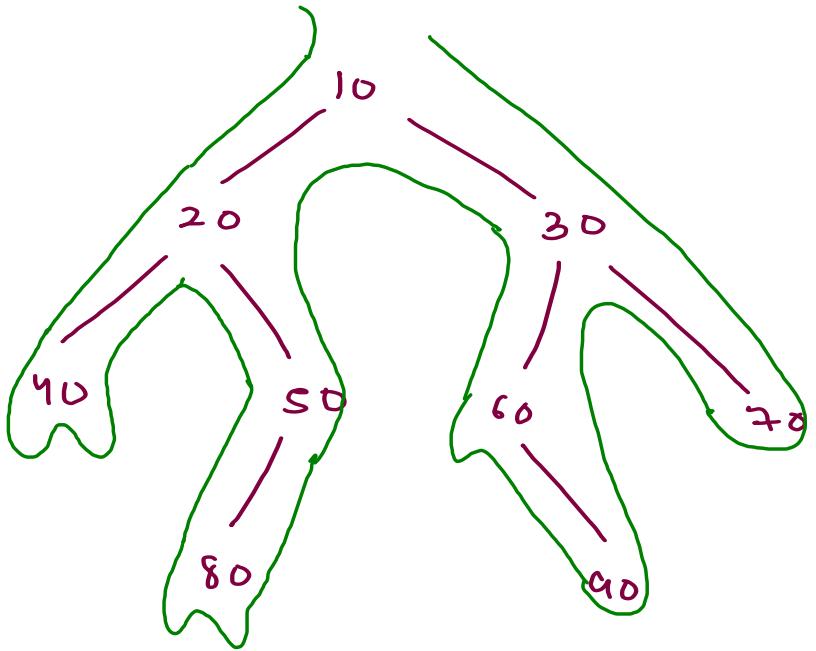




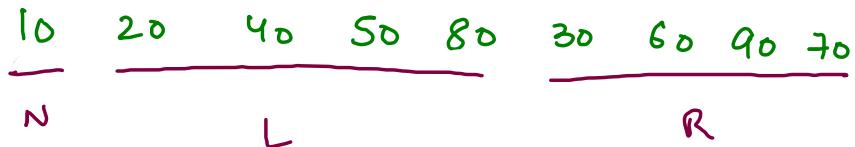
Traversals In A Binary Tree

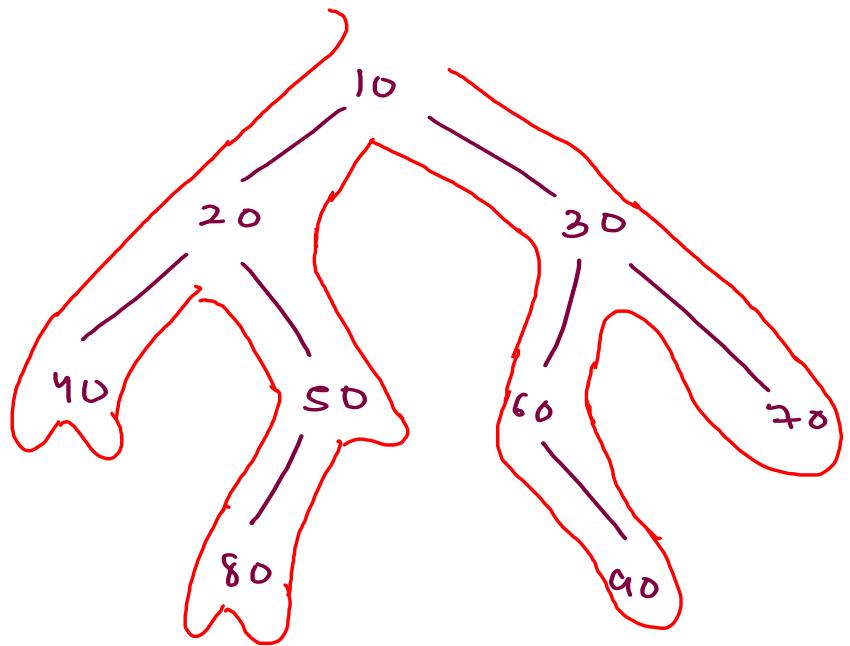


```
fun (node) {  
    if (node == null) return;  
    // pre  
    fun (node.left);  
    // gn  
    fun (node.right);  
    // post  
}
```



pre: NLR

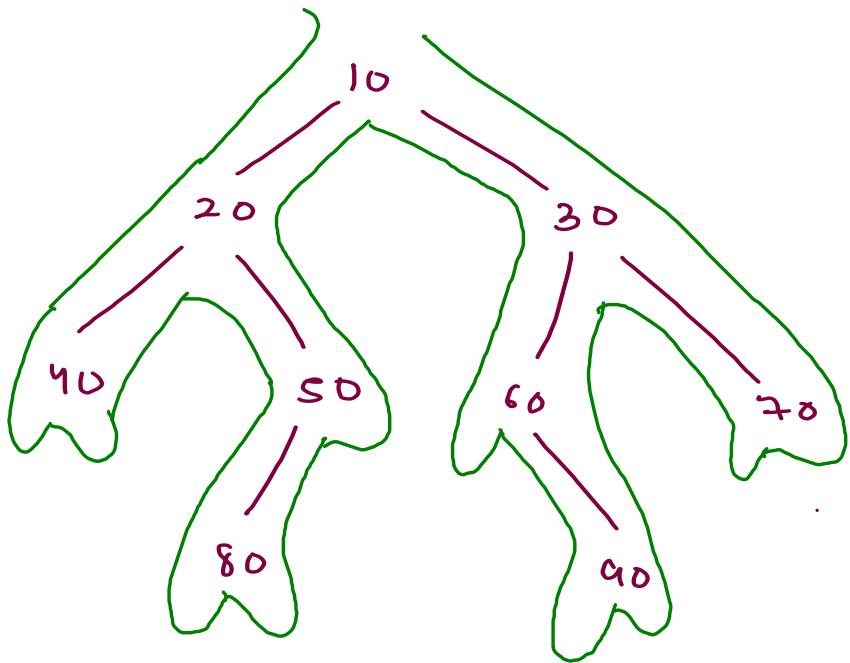




post : LRN

40 80 50 20 90 60 70 30 10

L R N



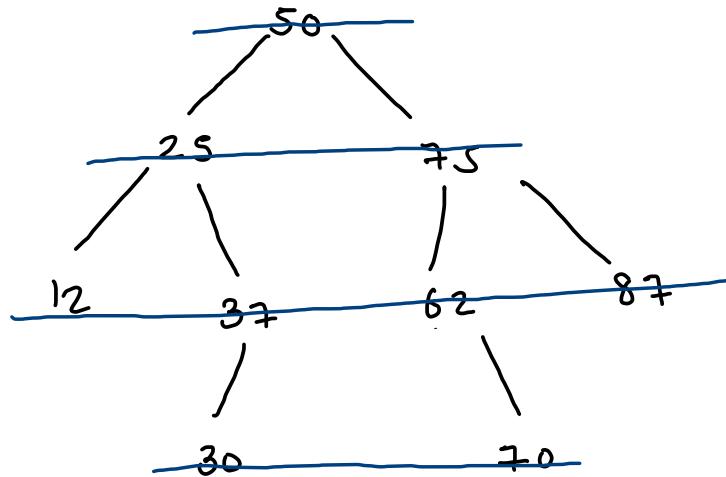
Grordan: LNR

40 20 80 50 10 60 90 30 70
L N R

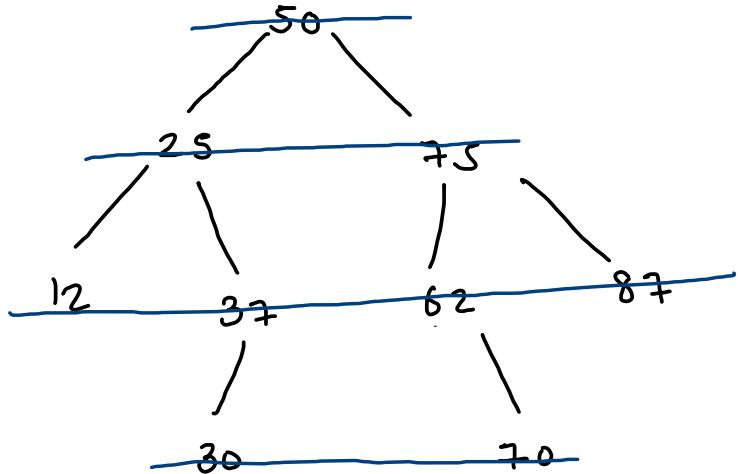
Levelorder Traversal Of Binary Tree

19
50 25 12 n n 37 30 n n n 75 62 n 70 n n 87 n n

50
25 75
12 37 62 87
30 70



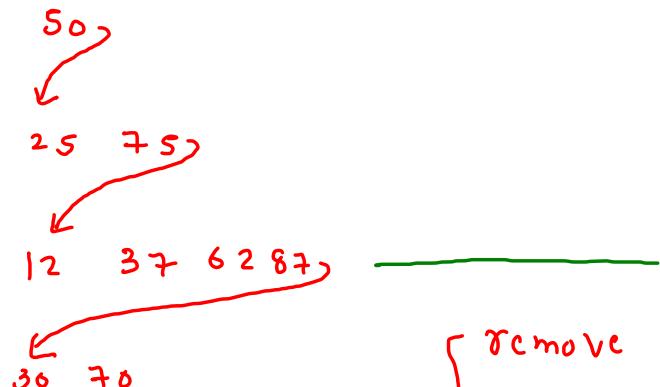
50
25 75
12 37 62 87
30 70



level order nine-wise

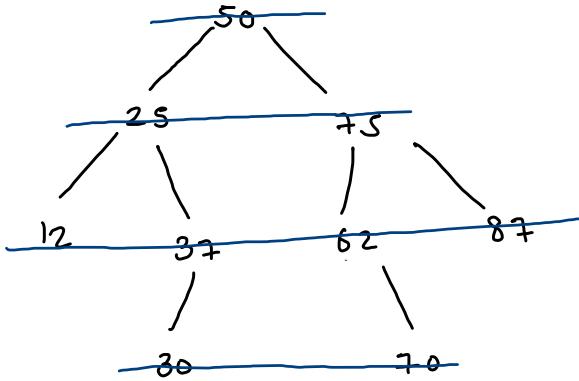
$$c = 2$$

~~50 | 25 | 75 | 12 | 37 | 62 | 87 | 30 | 70~~



count times
 remove work
 add children

Syso line



```

while(q.size() > 0) {
    int count = q.size();

    //-----k-----
    for(int i=0; i < count;i++) {
        //remove
        Node rem = q.remove();

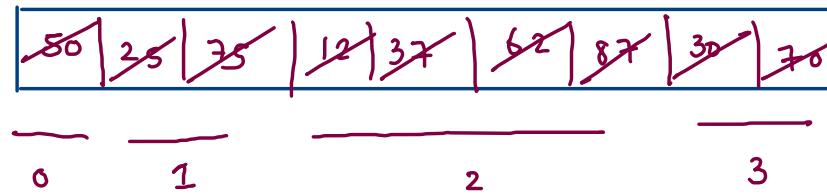
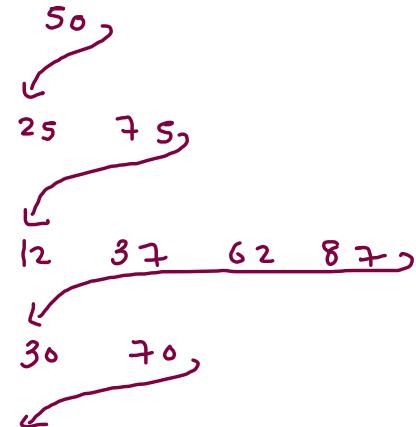
        //work
        System.out.print(rem.data + " ");

        //add children
        if(rem.left != null) {
            q.add(rem.left);
        }
        if(rem.right != null) {
            q.add(rem.right);
        }
    }

    //----- (k+1) -----
    System.out.println();
}

```

$$c = 2$$

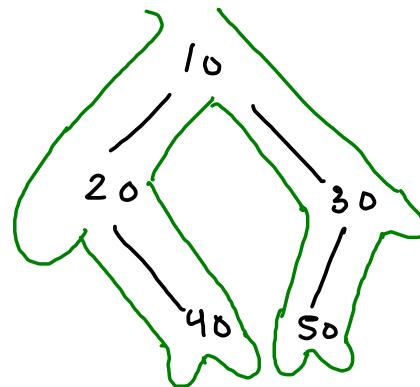


Iterative Pre, Post And Inorder Traversals Of Binary Tree

0 : pre, st++, go to left

1 : in, st++, go to right

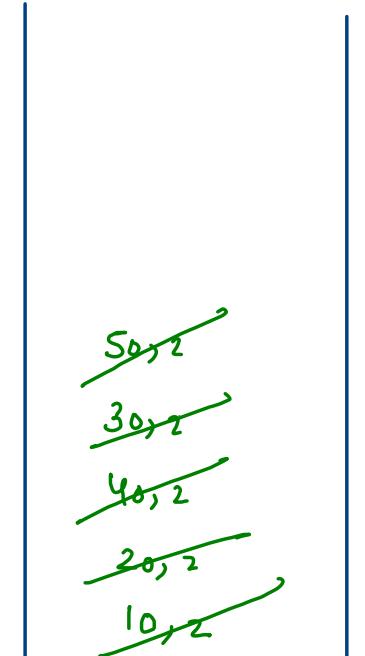
2 : post, pop



Pre : 10 20 40 30 50

In : 20 40 10 50 30

Post : 40 20 50 30 10



```

while(st.size() > 0) {
    Pair top = st.peek();

    if(top.state == 0) {
        //pre
        pre += (top.node.data + " ");
        top.state++;
    }

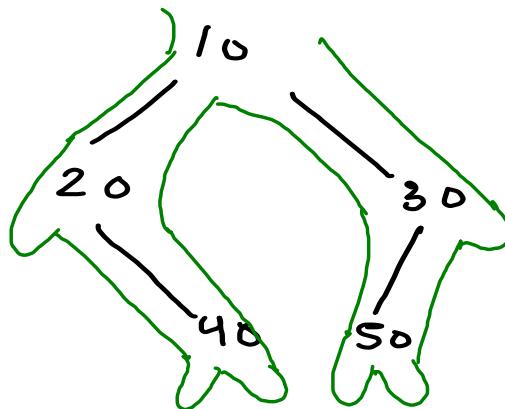
    if(top.node.left != null) {
        Pair lcp = new Pair(top.node.left,0);
        st.push(lcp);
    }
}

else if(top.state == 1) {
    //in
    in += (top.node.data + " ");
    top.state++;

    if(top.node.right != null) {
        Pair rcp = new Pair(top.node.right,0);
        st.push(rcp);
    }
}

else if(top.state == 2) {
    //post
    post += (top.node.data + " ");
    st.pop();
}
}

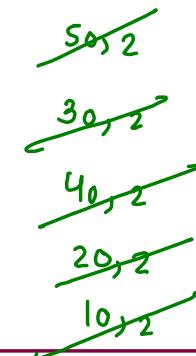
```



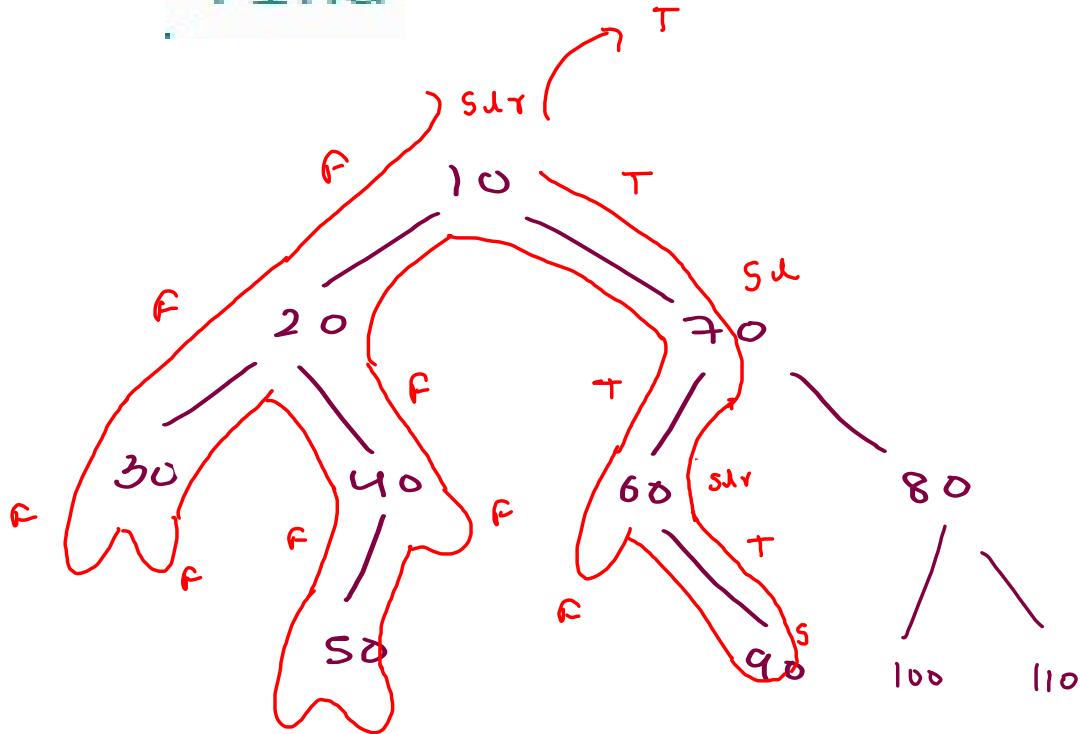
Pre : 10 20 40 30 50

In : 20 40 10 50 30

Post : 40 20 50 30 10

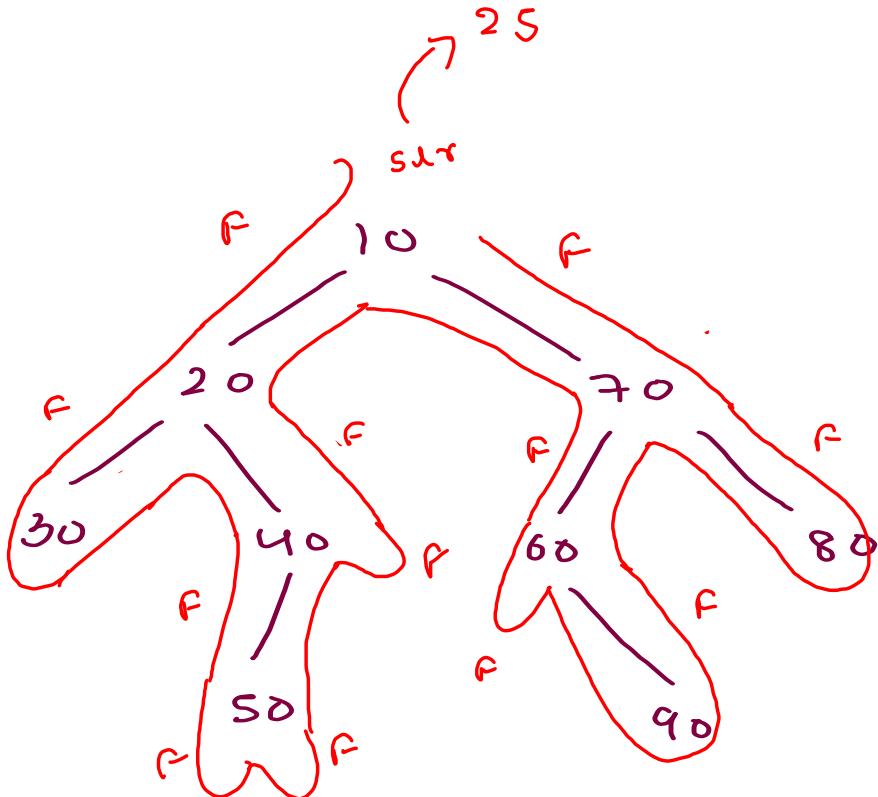


find



data = 90

```
public static boolean find(Node node, int data){  
    if(node == null) {  
        return false;  
    }  
  
    if(node.data == data) {  
        return true;  
    }  
  
    boolean fils = find(node.left,data); //found in left subtree  
    if(fils == true) {  
        return true;  
    }  
  
    boolean firs = find(node.right,data); //found in right subtree  
    if(firs == true) {  
        return true;  
    }  
  
    return false;  
}
```



$\text{data} \geq 25$

```

public static boolean find(Node node, int data){
    if(node == null) {
        return false;
    }

    if(node.data == data) {
        return true;
    }

    boolean fils = find(node.left,data); //found in left subtree

    if(fils == true) {
        return true;
    }

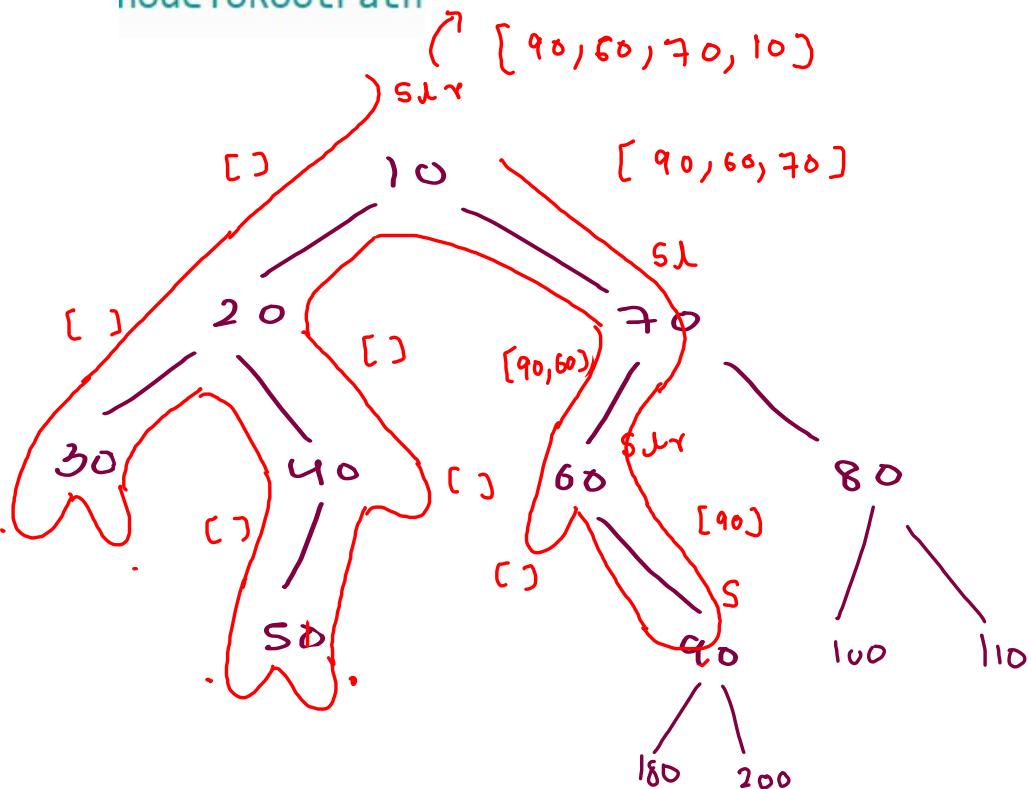
    boolean firs = find(node.right,data); //found in right subtree

    if(firs == true) {
        return true;
    }

    return false;
}

```

nodeToRootPath



data = 90

```
public static ArrayList<Integer> nodeToRootPath(Node node, int data){  
    if(node == null) {  
        return new ArrayList<>();  
    }  
  
    if(node.data == data) {  
        ArrayList<Integer>list = new ArrayList<>();  
        list.add(node.data);  
        return list;  
    }  
  
    ArrayList<Integer>n2lcp = nodeToRootPath(node.left,data);  
  
    if(n2lcp.size() > 0) {  
        n2lcp.add(node.data); //converting node to Left child path --> node to root path  
        return n2lcp;  
    }  
  
    ArrayList<Integer>n2rcp = nodeToRootPath(node.right,data);  
  
    if(n2rcp.size() > 0) {  
        n2rcp.add(node.data); //converting node to right child path --> node to root path  
        return n2rcp;  
    }  
  
    return new ArrayList<>();  
}
```