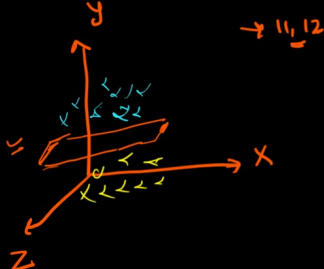
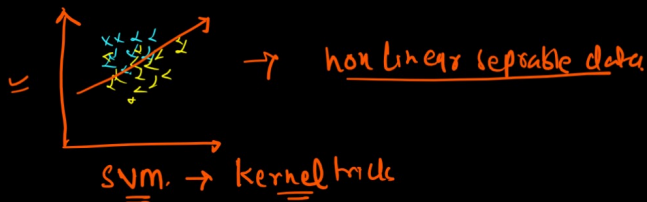
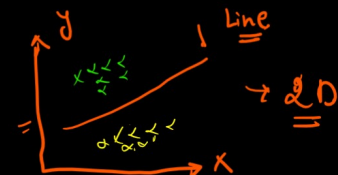
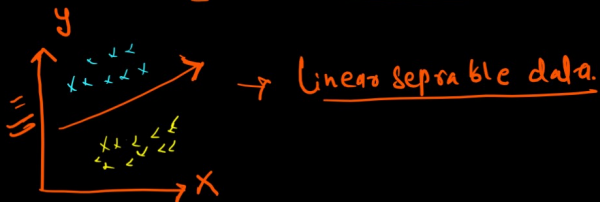


Log reg :- Prob → Line → Sigmoid fn. → (Prob) → Final out
0/1

(Line → $y = mx + c$)

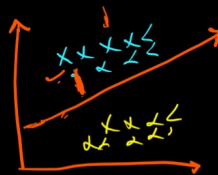
Log reg → (Linear separable)

Classification :- binary =
multiclass = (forest cover clm)

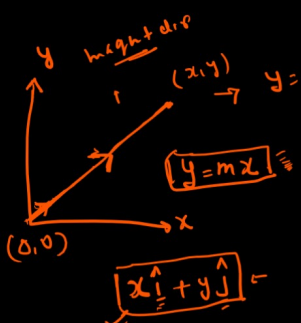


SVM → kernel trick

Linear Algebra



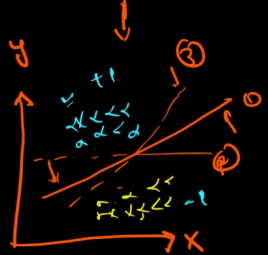
$y = mx + c \Rightarrow y = m_1x_1 + m_2x_2 + m_3x_3 + c$
 $y = w_0x + c \Rightarrow (m^T x) \rightarrow \begin{bmatrix} \end{bmatrix} \begin{bmatrix} \end{bmatrix} \rightarrow \text{Dot Product}$
 (Norms) → (distance blue)
 ML mathematics



Point and Plane
 $\text{Norm}_y = \frac{mx+c}{\|m\|} \rightarrow \text{value + direction}$

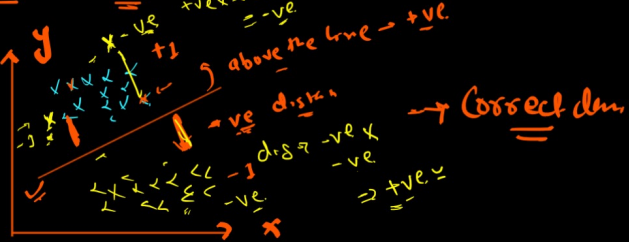
$\text{Norm}_y = \frac{w^T x + c}{\|w\|}$

$\text{Norm}_y = \frac{w^T x}{\|w\|} \rightarrow \text{unit vector} = 1$



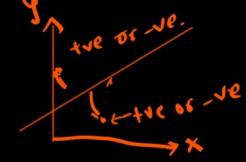
$\text{Norm}_y = w^T x = mx \Rightarrow mx + c$
 machine learning :- math → optimal lasat
 ① Cal.
 ② Cal.
 ③ Optimization

Binary class: 0, 1



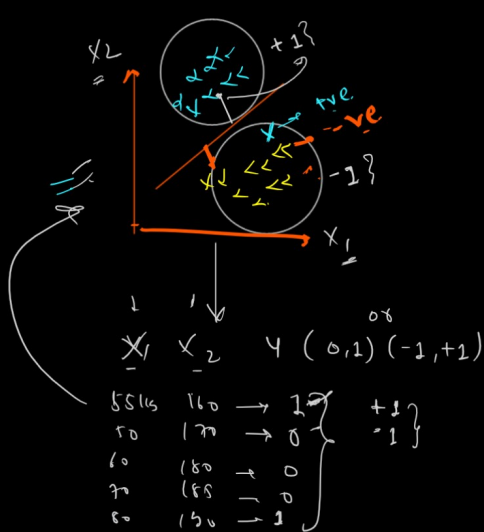
y actual	y pred.
0	0
0	0
1	1
1	0 x
1	1 x

distance
 $(+1, -1)$
 $(1, 0)$
 { above dis ⇒ +ve } → mathematically
 { below dis ⇒ -ve }



Case 1:- +ve x y;
 → +ve x +ve. blue
 ⇒ +ve = Correct class

Case 2 → +ve x -ve.
 ↓
 dis. Point iden.



→ -ve ≠ wrong

Case 3: $\boxed{-ve} \times \boxed{-ve}$

dist

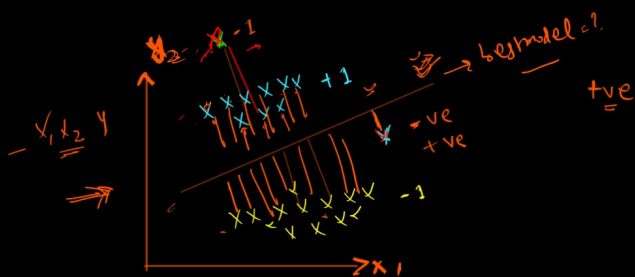
→ +ve → Correct

Case 4: $\boxed{-ve} \times \boxed{+ve}$

dis

ident point

→ -ve →



(correct classification)

$\Rightarrow +ve = 8$

distance (+ve) \times (+ve)

$\Rightarrow +ve$

Model
Line - 1

S point

$\left. \begin{aligned} 5x+1 &= 5 \\ 6x+1 &= 6 \\ 7x+1 &= 7 \\ 8x+1 &= 8 \\ 9x+1 &= 9 \end{aligned} \right\} = 35$

\Rightarrow S point + $\Rightarrow 70$

$\left. \begin{aligned} -5x-1 &= 5 \\ -6x-1 &= 6 \\ -7x-1 &= 7 \\ -8x-1 &= 8 \\ -9x-1 &= 9 \end{aligned} \right\} = 35 = \text{add (dis)}$

$\Rightarrow -ve \times -ve = \boxed{+ve}$

$\boxed{+ve \times -ve = -ve}$

Wrong classification

$\boxed{-ve \times +ve = -ve}$
Wrong classification

if my classifier is best classifier over here
distance addition max

Line 2

$\boxed{5x-1} = -5$

$\left. \begin{aligned} 6x+1 &= 6 \\ 7x+1 &= 7 \\ 8x+1 &= 8 \\ 9x+1 &= 9 \end{aligned} \right\} \Rightarrow 25$

$\boxed{-5x+1} = -5$

$\boxed{-6x+1} = -6$

$\left. \begin{aligned} -7x-1 &= 7 \\ -8x-1 &= 8 \\ -9x-1 &= 9 \end{aligned} \right\} \Rightarrow 19$

$\Rightarrow \max \left(\sum_{i=1}^n y_i \times w_i x_i \right)$

add (dis)

$\rightarrow \begin{cases} +ve \times +ve \\ +ve \\ -ve \times +ve \\ +ve \end{cases}$

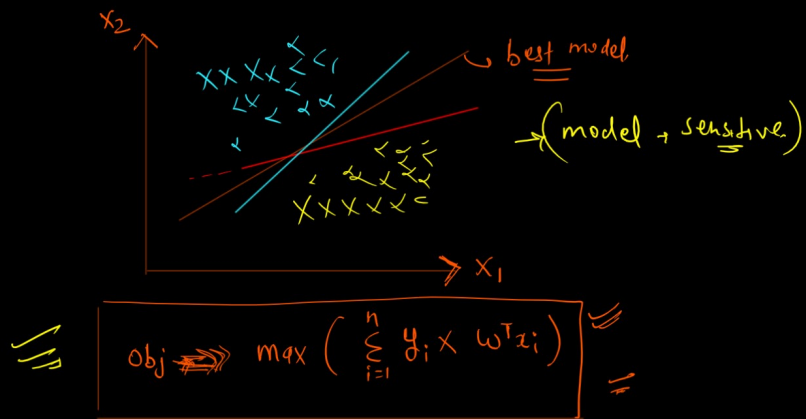
add

Line 3

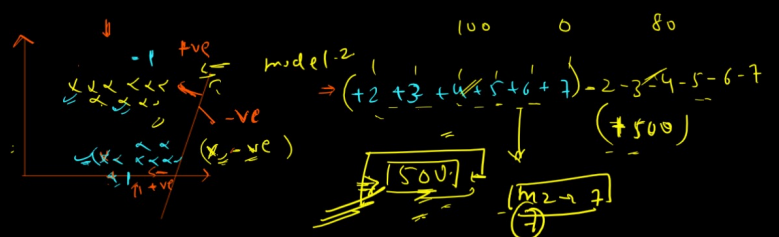
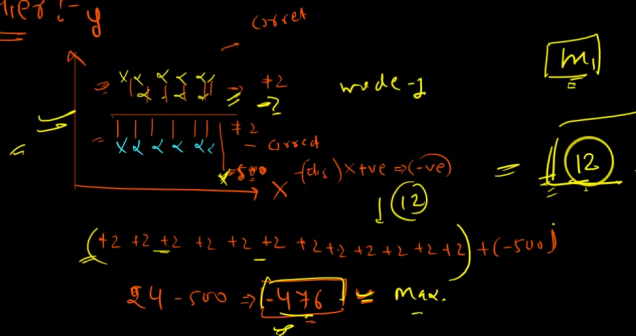
① Support vector → Max margin (Linear)

② Loss function →

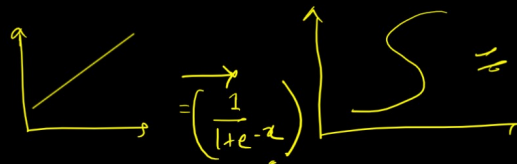
NLSD + ① Polynomial } kernel trick
② RBF



Outlier :- y



Sigmoid :- Squash



Mode 1 \rightarrow Correlated density $\Rightarrow (40)$

Obj sum $\Rightarrow 2000$

Mode 2 \rightarrow Correlated density $\Rightarrow (23)$

Obj sum $\Rightarrow 600$

(Outliers)

Sigmoid

max $\Rightarrow \frac{1}{1+e^{-x}} = \frac{1}{1+e^{-mx}}$

m

$(2x+2) = \checkmark$

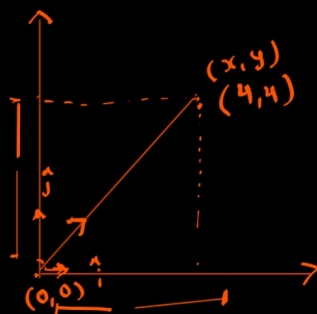
$(2x+3) = \checkmark$

$(2x500) = \checkmark$

$(0-1)$

$(\log 1)$

$(\log 1081)$



Vector = magnitude + direction

$$x\hat{i} + y\hat{j} = 0$$

general eq $ax + by + c = 0$

$$ax + by = 0$$

$$ax\hat{i} + by\hat{j} = 0$$

$$= \begin{bmatrix} a \\ b \end{bmatrix} \text{ or } \begin{bmatrix} x \\ y \end{bmatrix}$$

$$\sqrt{(4-0)^2 + (4-0)^2}$$

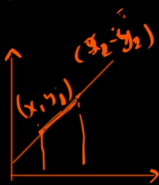
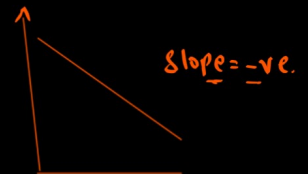
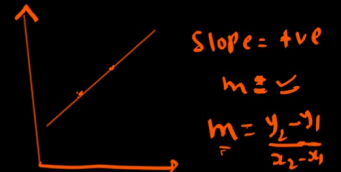
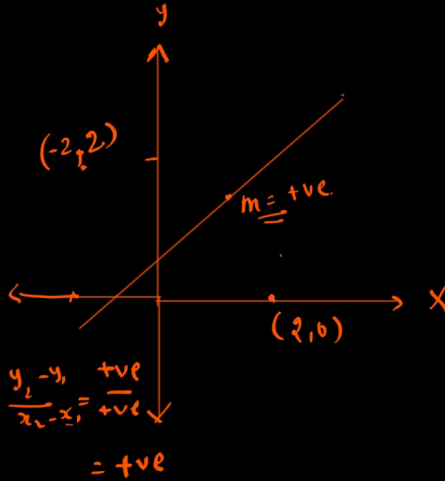
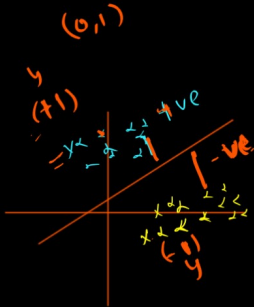
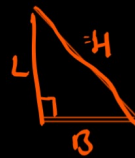
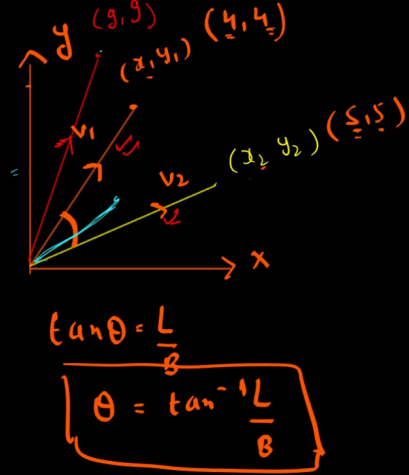
$$\sqrt{16+16} = \sqrt{32} + 0.14$$

distance

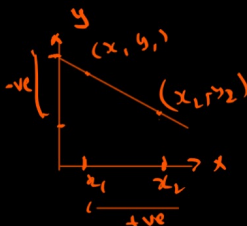
$$= \begin{bmatrix} x_1 & y_1 \\ x_2 & y_2 \end{bmatrix}$$

$$= (v_1 + v_2)$$

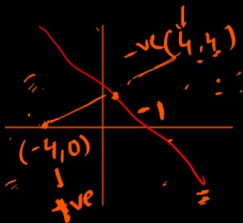
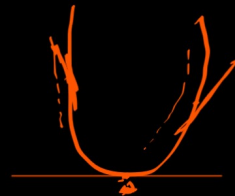
$$(w_1 - v_2)$$



$$m = \frac{y_2 - y_1}{x_2 - x_1} = +ve$$



$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-ve}{+ve} = -ve$$



\rightarrow $m = -1$

$$y = mx + c$$

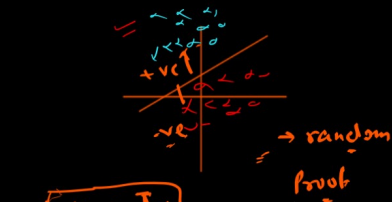
$$y = \omega_0 x + c$$

$$y = \omega^T x + c$$

$$y = m x \text{ or } y = \omega^T x$$

$$= -ve \times -ve = +ve \cdot c$$

$$= -ve \times +ve = -ve$$



$$y = m^T x$$

$$y = m_1 x_1 + m_2 x_2 + m_3 x_3 + c$$

$$= \begin{bmatrix} m_1 \\ m_2 \\ m_3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + c$$

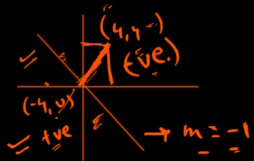
Dot product: $(m_1, m_2, m_3) \cdot (x_1, x_2, x_3)$

$$m_1 x_1 + m_2 x_2 + m_3 x_3$$

$$\begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix}^T \times \begin{pmatrix} y_1 \\ y_2 \\ y_3 \end{pmatrix}$$

$$\rightarrow x_1$$

Diagram showing a vector $(4,4)$.



$$y = \omega^T x + c - 0$$

$$= \begin{bmatrix} -1 \\ 0 \end{bmatrix} \begin{bmatrix} 4 \\ 4 \end{bmatrix}$$

$$= -4$$

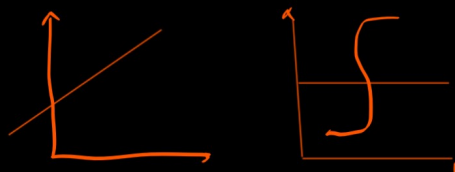
$$y = mx + c$$

$$= -1 \times 4 + 0$$

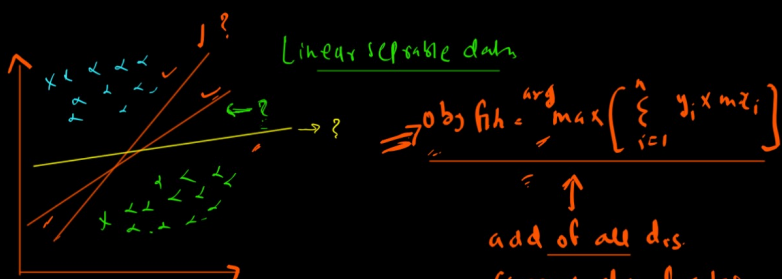
$$= -4$$

$$= \begin{bmatrix} m_1 & m_2 & m_3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}$$

$$= m_1 x_1 + m_2 x_2 + m_3 x_3$$



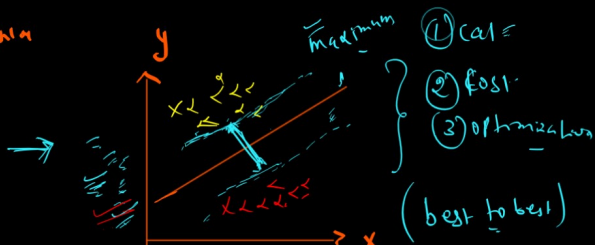
$(100, 20, 20) \rightarrow (50, 0, 0) \rightarrow (100, 20)$
 (soft) high - low



Linear separable data

$$\Rightarrow \text{Obj. fn.} = \arg \max \left[\sum_{i=1}^n y_i \cdot x \cdot m_i \right]$$

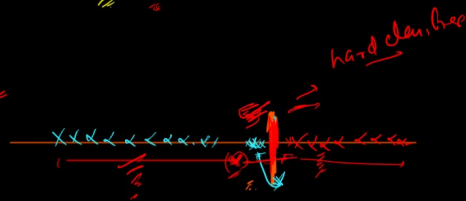
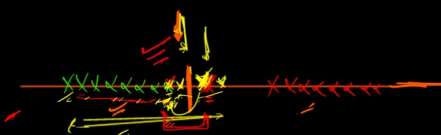
add of all d.s.
 correct classification
 +ve.



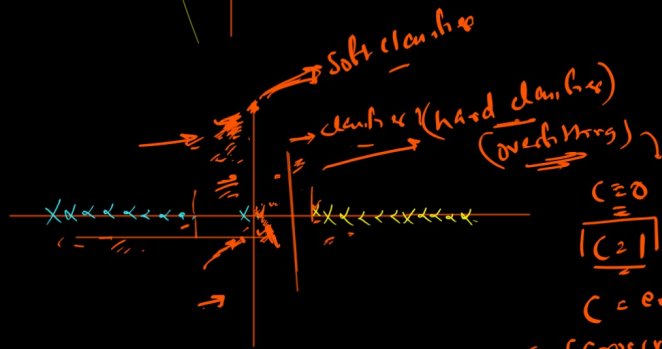
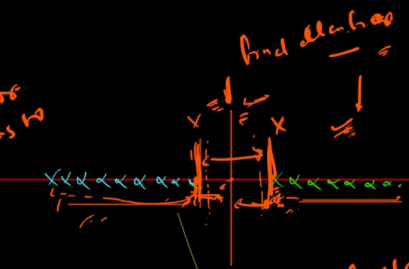
- ① cat
- ② post
- ③ optimization

(best to best)

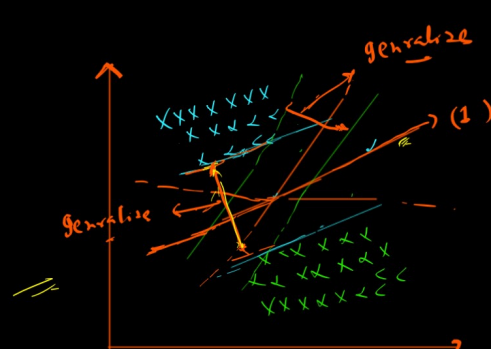
Squash
 turn softmax (sigmoid)
 log loss / obj function



SVM = loss
 how many errors
 before sums to
 consider

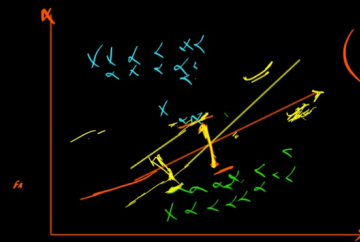


$C \geq 0$
 $\frac{C}{C+1}$ testings %
 $C = \text{conversion}$
 $= (C \text{ conversion rate})$

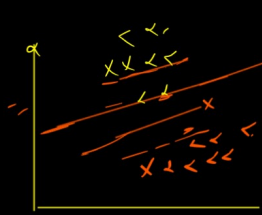


SVM \rightarrow max dist should be
 these.
 (maximum margin)

DATA

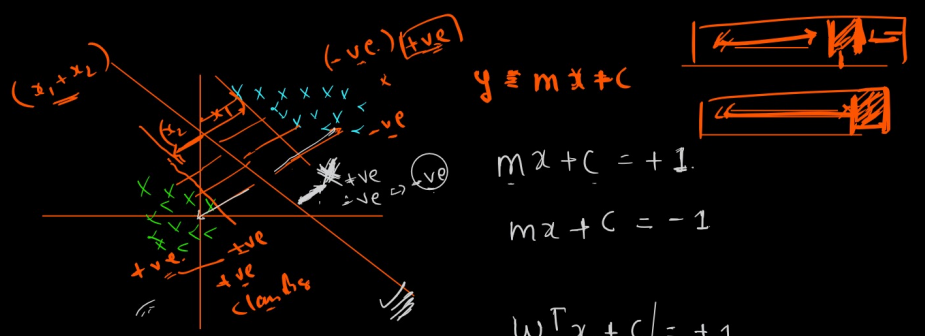


(SVM) \rightarrow good accuracy
 generalize model



conv \rightarrow 2, 3, 4, 5 ...
 (cross val d.)





$$\frac{w^T x + c}{\|w\|}$$

Distance

each and every

(obs.)

$$y_i x_i w^T x_i$$

$+ve \times +ve \Rightarrow +ve$
 $-ve \times -ve \Rightarrow +ve$

→ correct

error :- 2, 3, 4, 5 ... N

$\epsilon \times \text{distance}$

$(1 \times w^T x + c)$

$4 \times \text{distance}$

error → generalization

$$\frac{w^T (x_2 - x_1)}{\|w\|} = \frac{+2}{\|w\|}$$

max

distance

(min)

$$\frac{1}{w^T (x_2 - x_1)} = \frac{1}{2}$$

$f(x) = x$
 $f(1) = 1$
 $f(2) = 2$
 $f(3) = 3$

$f(x) = \frac{1}{x}$
 $f(1) = \frac{1}{1}$
 $f(2) = \frac{1}{2}$
 $f(3) = \frac{1}{3}$