

Question 1. Random Forests leverage randomization in two different ways. Name both.

There are two ways in which the trees in a random forest are randomized: by selecting the data points used to build a tree and by selecting the features in each split test.

Question 2. [20 points] Naive Bayes: Below is a simple medical dataset that gives details of symptoms that patients presented and whether they were suffering from meningitis. Included are three descriptive features which are common symptoms of the disease: HEADACHE, FEVER, AND VOMITING

ID	HEADACHE	FEVER	VOMITING	MENINGITIS
1	True	True	False	False
2	False	True	False	False
3	True	False	True	False
4	True	False	True	False
5	False	True	False	True
6	True	False	True	False
7	True	False	True	False
8	True	False	True	True
9	False	True	False	False
10	True	False	True	True

Using this dataset to determine if a patient presenting with the following symptoms would be classified by the model as having meningitis. HEADACHE = true & FEVER = true & VOMITING = true

Frequency Table:-

$$P(\text{meningitis} = T) = 3/10$$

$$P(\text{Meningitis} = F) = 7/10$$

$$P(\text{Headache} = Y \mid \text{Meningitis} = Y) = 2/3$$

$$P(\text{Headache} = Y \mid \text{Meningitis} = N) = 5/7$$

$$P(\text{Fever} = T \mid \text{Meningitis} = Y) = 1/3$$

$$P(\text{Fever} = T \mid \text{Meningitis} = N) = 3/7$$

$$P(\text{Vomit} = T \mid \text{Meningitis} = N) = 2/3$$

$$P(\text{Vomit} = N \mid \text{Meningitis} = N) = 4/7$$

$$P(\text{Meningitis} = Y \mid \text{Head} = T, \text{vomit} = T, \text{fever} = T) = 2/3 * 1/3 * 2/3 * 3/10 = 4/90 = 0.044$$

$$P(\text{Meningitis} = N \mid \text{Head} = T, \text{vomit} = T, \text{fever} = T) = 5/7 * 3/7 * 4/7 * 7/10 = 6/49 = 0.122449$$

$$P(M|T,H|T,F|T,V|T) = 0.044/(0.044 + 0.122) = 0.265$$

$$P(M|F,H|T,F|T,V|T) = 0.122/(0.044 + 0.122) = 0.735$$

$0.122 > 0.044$ or $.735 > .265$ hence when HEADACHE = true & FEVER = true & VOMITING = true then Meningitis = False

We can predict that the patient will not be diagnosed with Meningitis.

