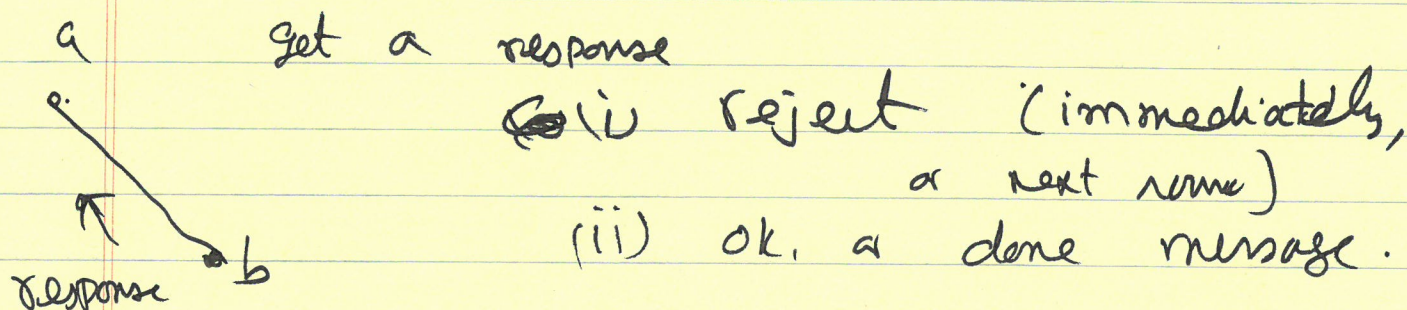
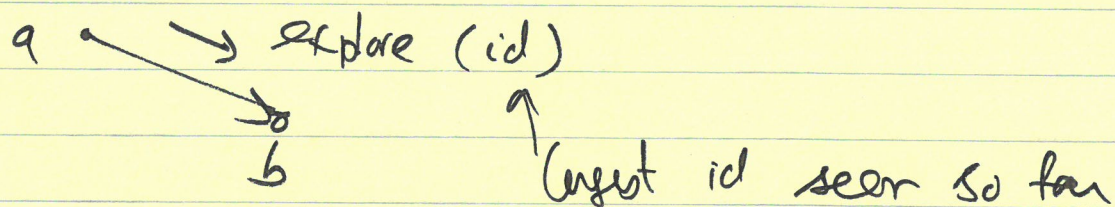


①

9-10-19

## Floodmax - termination



Node a is a leaf if all explore() messages sent by a get a reject as the response.

If a node is a leaf, send a Completed() message to the parent

If a node is a non-leaf,  
 { wait till all explore() messages get a response each;

(reject / completed)

Send a Completed() message to the parent

}



②

When a node (or a process)  $u$  receives a reply for each explore() message it had sent & if no explore() message with id larger than  $u$  has been received, the leader & it is  $u$  knows it is time to terminate

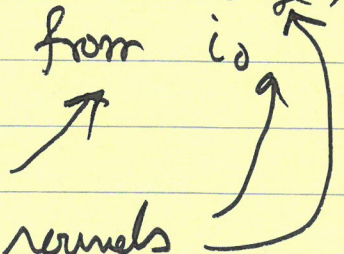
Exploration leader  $\rightarrow$  all (go down & create the tree)  
Replies  $\rightarrow$  Convergecast (go up)  
Termination  $\rightarrow$  go down the tree

### Breadth First Search

$i_0$  : root of the tree.

Build BFS tree rooted at  $i_0$ .

{ uses: broadcast a message, send a message from  $i_0$  to another process.  
Shortest path  
Smallest # of rounds

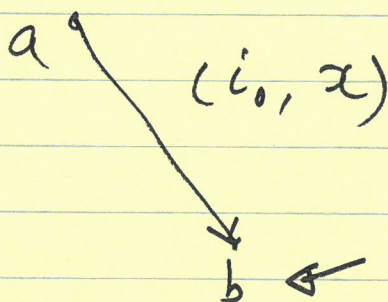




③

Initially,  $i_0$  sends a message containing  $(i_0, 0)$  to all neighbors

$\nearrow$  root id       $\uparrow$  # of hops between root & sender of this message.



if  $b$  is already part of the BFS tree rooted at  $i_0$  { ignore this message }

else { if this same message is received from  $> 1$  neighbor in this round {

Choose one of them to be the parent. // joined the tree  
 hopcount to the root =  $x+1$   
 forward message  $(i_0, x+1)$  to all neighbors as needed

} else {

join the tree;  
 forward  $(i_0, x+1)$  to all neighbors as needed }

Time:  $O(\text{diam})$   
 messages:  $O(|E|)$



④

We have a tree rooted at say  
 $x$ . ( $T_x$ )

Each process has a value, known  
only to itself (local value)

Want to find the max-value of all  
local values.

$x$  broadcasts a message (saying  
max-value is to be found)

On receiving this message {

using  
converge cast

if i'm a leaf, { send  
my local value to parent }

else {  
wait for a message  
containing a value from  
each child.

choose largest among values  
received from all children  
and its own local  
value & send this  
chosen value to parent

}  
messages:  $2(n-1)$

Time:  $2 \cdot (\text{depth of tree})$

min, sum, max, average. Can be  
done this way.



⑤

Read about BFS tree in ~~und~~ directed graphs. [not all edges/links are bidirectional] from the book.

Shortest ~~paths~~ paths.

Shortest paths tree.

$i_0$  = root.

(all) links have a non-negative costs.  
each  $\rightarrow$  cost

Bellman Ford algorithm

$dist_x$  = distance that  $x$  is from  $i_0$ .

initially,  $dist_x = \infty$  if  $x \neq i_0$   
&

$dist_x = 0$  if  $x = i_0$

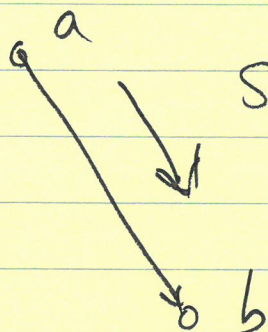
$i_0$  sends ~~dist~~ shortest-dist-  $(i_0, i_0, 0)$  to all neighbors.

root of tree  
sender of this message

Shortest distance from root to sender of this message as of now.



6



Shortest distance ( $x, a, d$ )

b receives message Shortest distance ( $x, a, d$ )

b performs "relaxation" step

if  $d + \text{cost}(a, b) < \text{dist}_b$  (for B shortest path tree ~~is~~ rooted at  $x$ )

// this message is "useful"

$\text{dist}_b(\text{SP tree rooted at } x) = d + \text{cost}(a, b)$

parent( $b$ ) =  $a$ ;

forward  $\text{dist}(x, b, \dots)$  to all other neighbors

}

else { discard message }

Time:

messages: