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EIG Stop.

## Byzantine Failures.

Behavior of a faulty process: any arbitrary behavior and in particular, all ~~the~~ faulty processes can collude among themselves.

Messages with authentication (digital signatures)  
- easier to solve.

No digital signatures for messages.

We need  $n > 3f$  processes for consensus despite Byzantine faults without message authentication.

$f$  = # of faulty processes.

Need  $n = \min$  of  $3f + 1$

→ Argue that  $f=1$ ,  $n=3$ , no solution to agreement problem.

1. Termination —

2. Validity: If all non-faulty processes start with  $v \in V$  as the input value, then  $v$  is the only possible solution.

Agreement 3. No two non-faulty processes decide on different values.



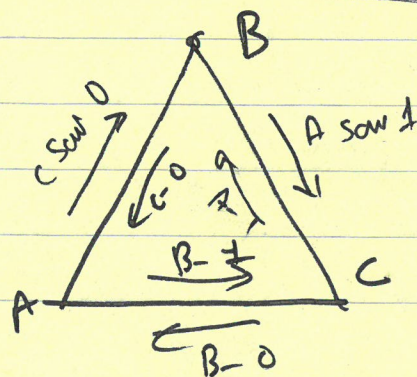
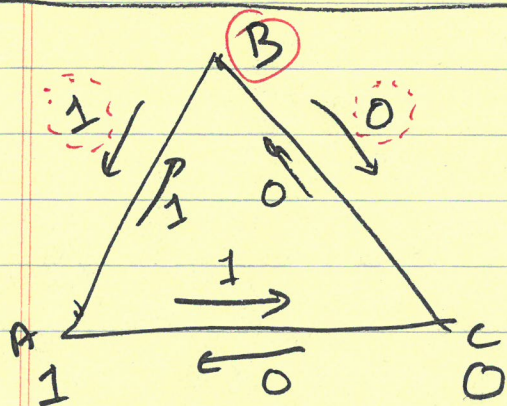
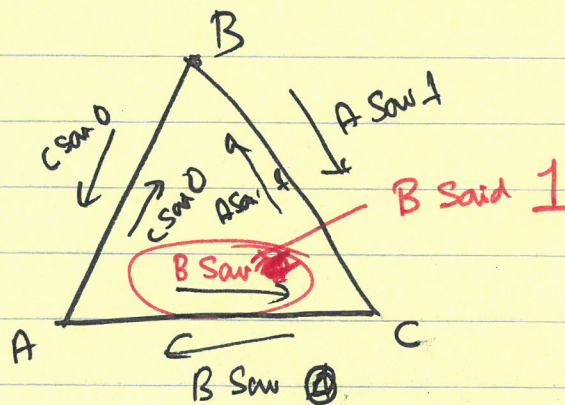
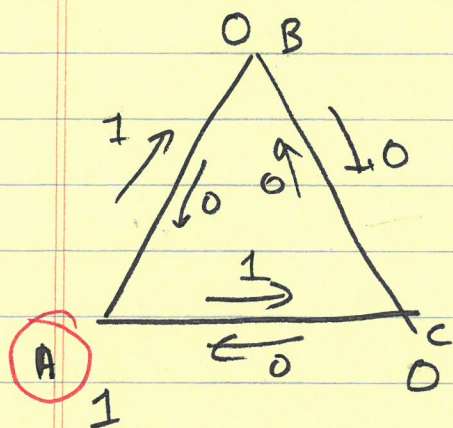
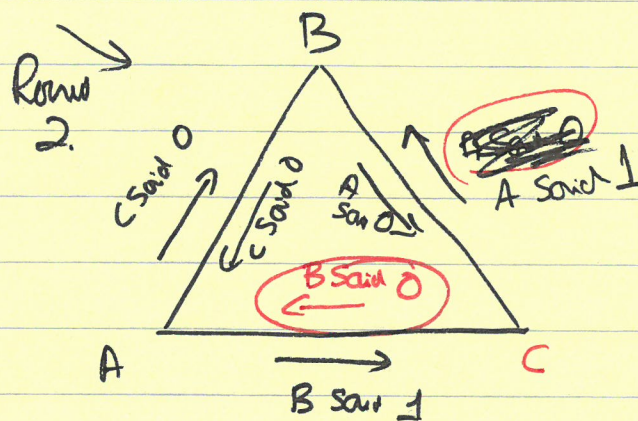
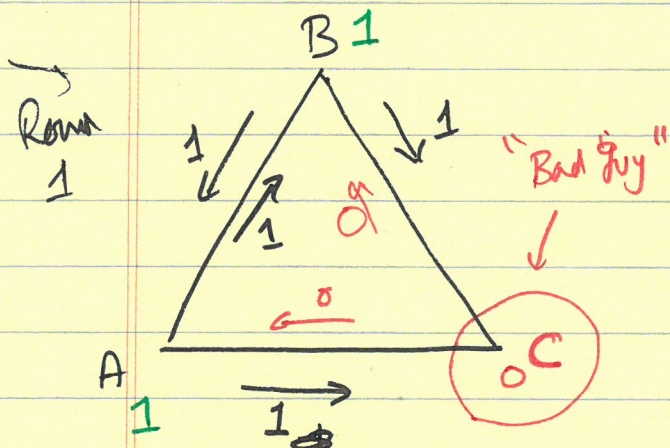
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The algorithms are of the form,

Power 1: Send local value to all.

Receive ... from others.

Round # > 1: Record received values.  
Send received values to others





③  $\alpha_1 \sim_A \alpha_3$  : From A's point of view  $\alpha_1$  &  $\alpha_3$  are indistinguishable

$\alpha_2 \sim_C \alpha_3$  : From C's point of view,  $\alpha_2$  &  $\alpha_3$  are identical.

A decides on 1 in  $\alpha_1$  [Both non-faulty processes start with 1]  
(Validity Condition)

C decides on 0 in  $\alpha_2$ .

in  $\alpha_3$ , C decides on 0 [ $\alpha_2$  &  $\alpha_3$  are same from C]

in  $\alpha_3$ , A decides on 1 ( $\alpha_1$ ,  $\alpha_3$  are same for A)

$\Rightarrow$  agreement is violated

$f=1$ ,  $n=3$  ~~so~~ no solution.

$f > 1$  ? Can show via simulation of  $> 1$  faulty process case.

$n = \min 3f + 1$  for consensus.



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## ELG Byz Algorithm

Run for  $t+1$  rounds (like in ELG STOP) and propagate  $\{val\}$  values with labels.

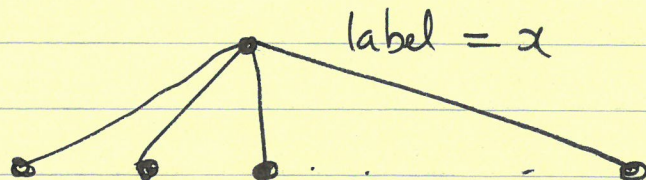
Every node of the ELG tree has label and val.

Associate another # to each node  $\rightarrow$  of the ELG tree in addition to val.

$newval()$ :

leaf  $newval(x) = val(x)$  if  $x$  is ~~to~~ a label of a leaf vertex

Interior vertex



$newval(x) =$  strict majority of the  $newval$  of its children if strict majority exists  
 else =  $v_0$ , default value.

$\nearrow$   
 All processes agree on what the new val is. before the algorithm starts.