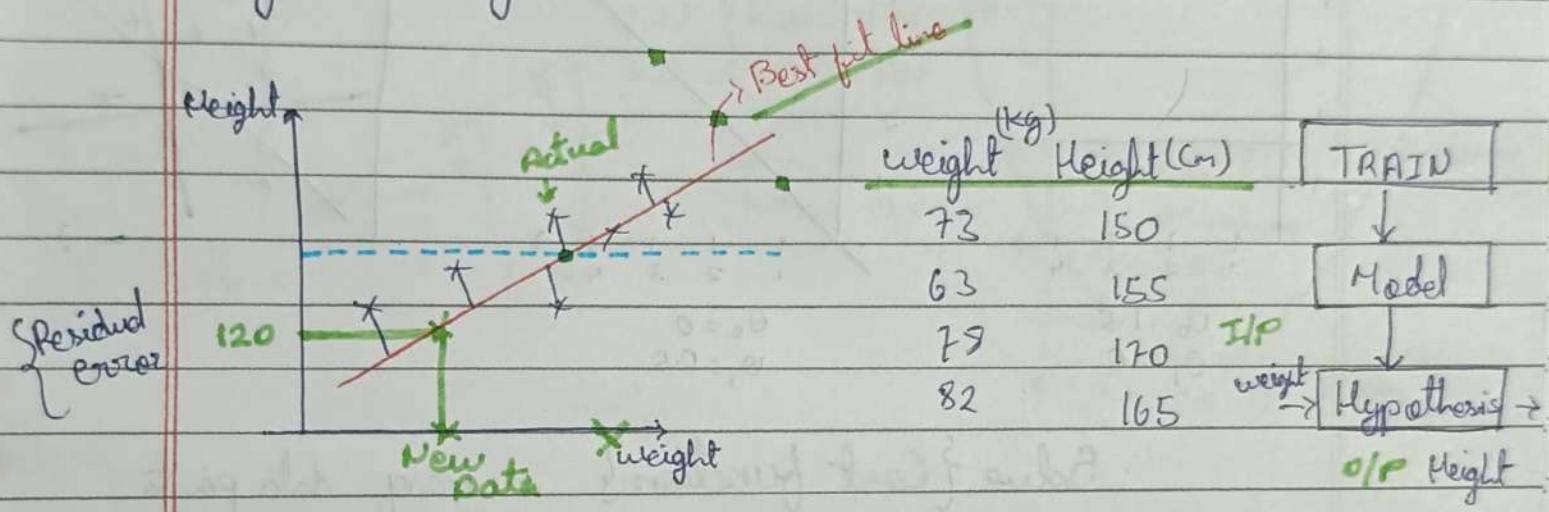


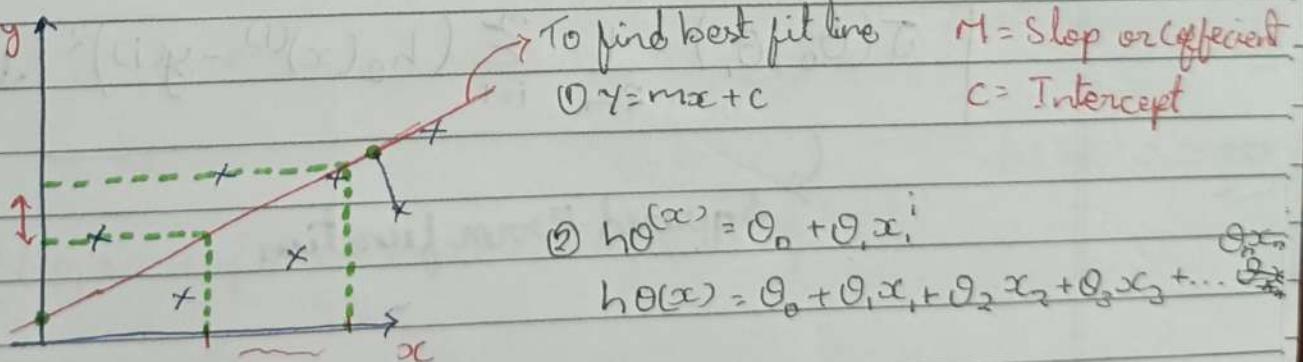
## Linear Regression Algorithm

Linear Regression is a way to predict a number by drawing the best straight line through data points.

It learns the relationship between input( $x$ ) and output( $y$ ) using a straight line.



Residual Error is difference between the actual value and predicted value



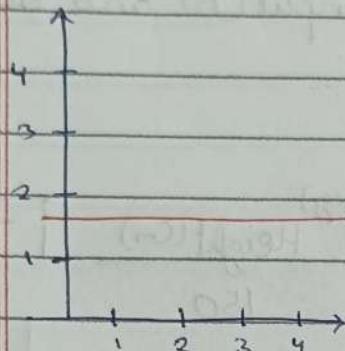
Hypothesis $\{y \text{ is a linear function of } x\}$ 

$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

↳ Intercept

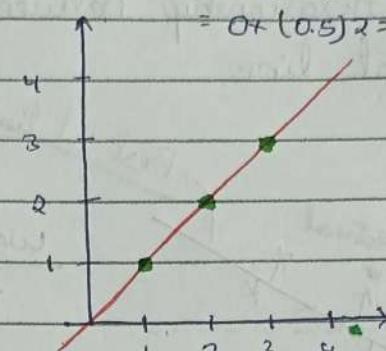
$$= \theta_0(0.5)1 = 0.5$$

$$= \theta_0(0.5)2 = 1$$



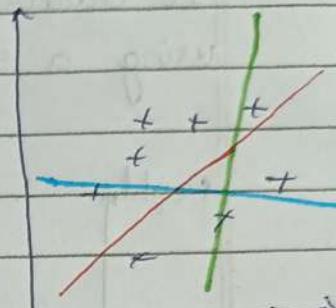
$$\theta_0 = 1.5$$

$$\theta_1 = 0$$



$$\theta_0 = 0$$

$$\theta_1 = 0.5$$

Solve {Cost function}  $m = \text{No. of data points}$ Minimize  
 $\theta_0, \theta_1$ 

$$\sum_{i=1}^m \frac{1}{2m} (h_{\theta}(x^{(i)}) - y^{(i)})^2 \downarrow \downarrow$$

$$\begin{aligned} \frac{\partial(x^2)}{\partial x} &= 2x^{2-1} \\ &= 2x \end{aligned}$$

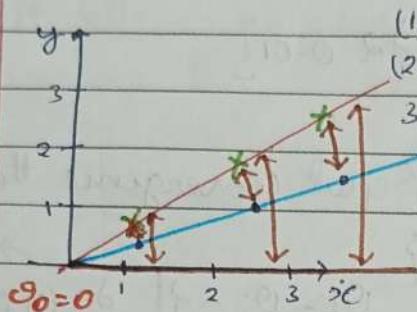
$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2 \quad \downarrow \downarrow \downarrow$$

↳ Squared Error function

## Hypothesis

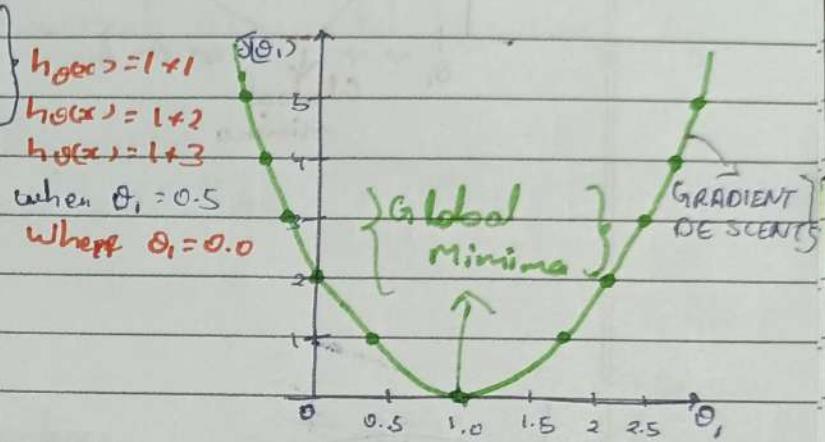
$$h_{\theta}(x) = \theta_0 + \theta_1 x, \quad \text{let } \theta_0 = 0$$

where  $\theta_1 = 1$



## Cost function

$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$



$$J(\theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2 \quad \text{when } \theta_1 = 1$$

$$= \frac{1}{6} [(0)^2 + (0)^2 + (0)^2]$$

$$= 0$$

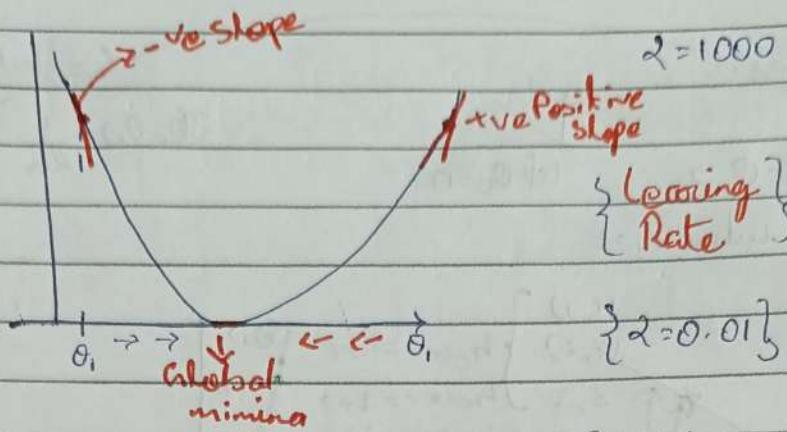
$$J(\theta_1) = \frac{1}{6} [(0.5-1)^2 + (1.2-1)^2 + (4.5-3)^2]$$

when  $\theta_1 = 0.5$

$$= \frac{1}{6} (3.5) = \approx 0.58$$

$$J(\theta_1) = \frac{1}{6} [(0-1)^2 + (0-2)^2 + (0-3)^2]$$

$$= \frac{14}{6} = \approx 2.3$$



Repeat convergence theorem

$$\theta_j := \theta_j - \eta \left[ \frac{\partial}{\partial \theta_j} J(\theta_j) \right]$$

↓ shape

$$\begin{cases} \theta_j := \theta_j - \eta (+ve) \} & \text{Decrement} \\ \theta_j := \theta_j - \eta (-ve) \} & \text{Increment} \\ \theta_j = \theta_j + \end{cases}$$

## Outline

- ① Start with  $\theta_0 \neq \theta$ .
- ② Keep changing  $\theta_0, \theta$ , to reduce  $J(\theta_0, \theta)$  until we reach near global minima.
- ③ Convergence Theorem

$$\theta_j := \theta_j - \eta \left[ \frac{\partial}{\partial \theta_j} J(\theta_0, \theta_j) \right]$$

$J = \theta$  and