

CS 569

Selected Topics in Software Engineering:  
Program Analysis & Evaluation

# **Symbolic and Concolic Testing**

Oregon State University, Winter 2024

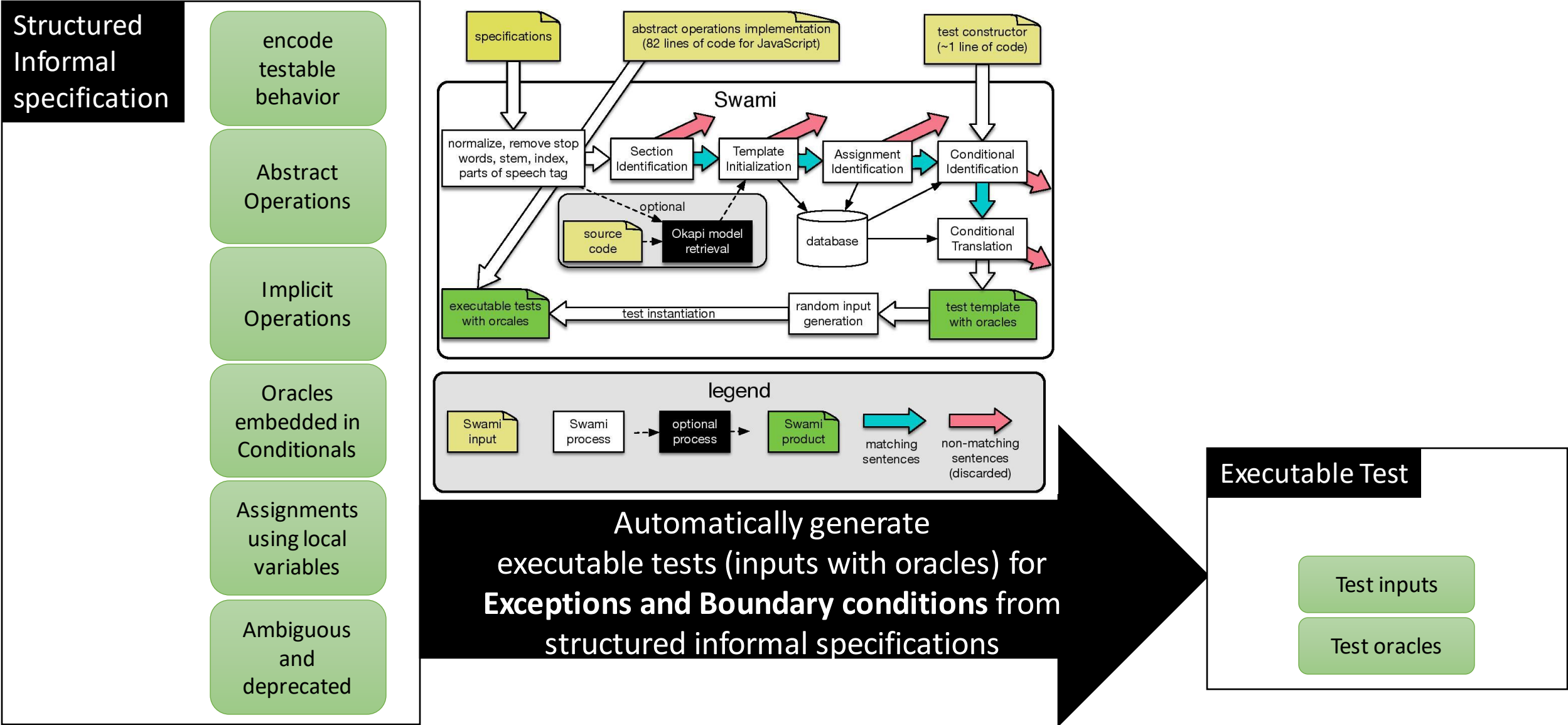
## DEMO for Paper Presentation

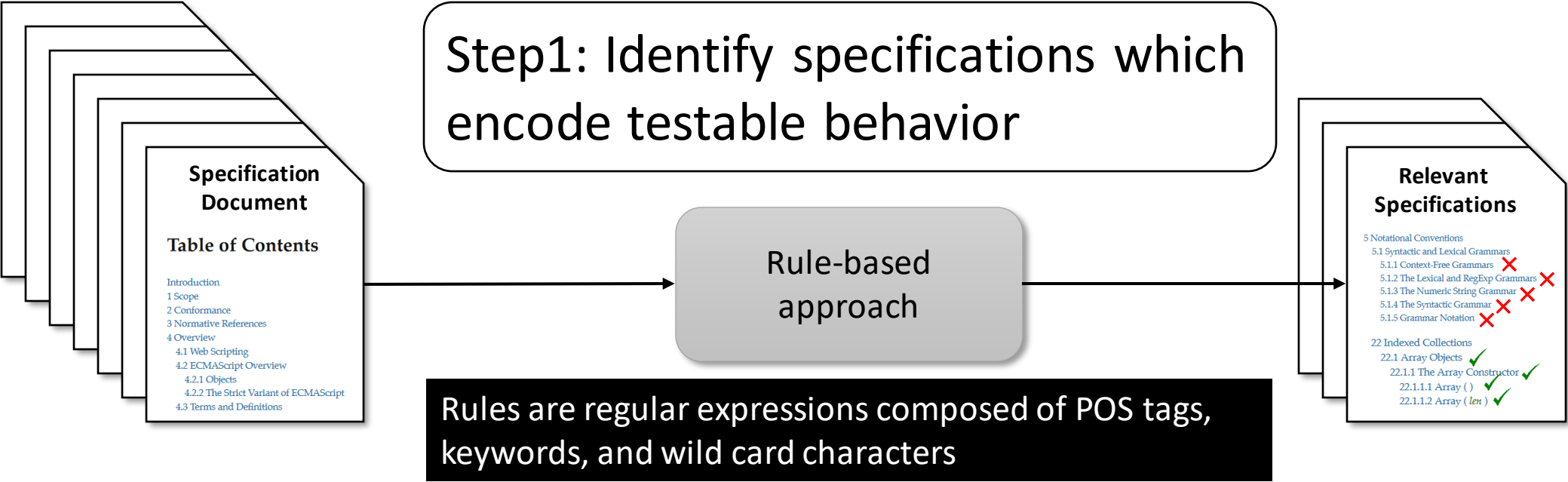
# Automatically Generating Precise Oracles from Structured Natural Language Specifications

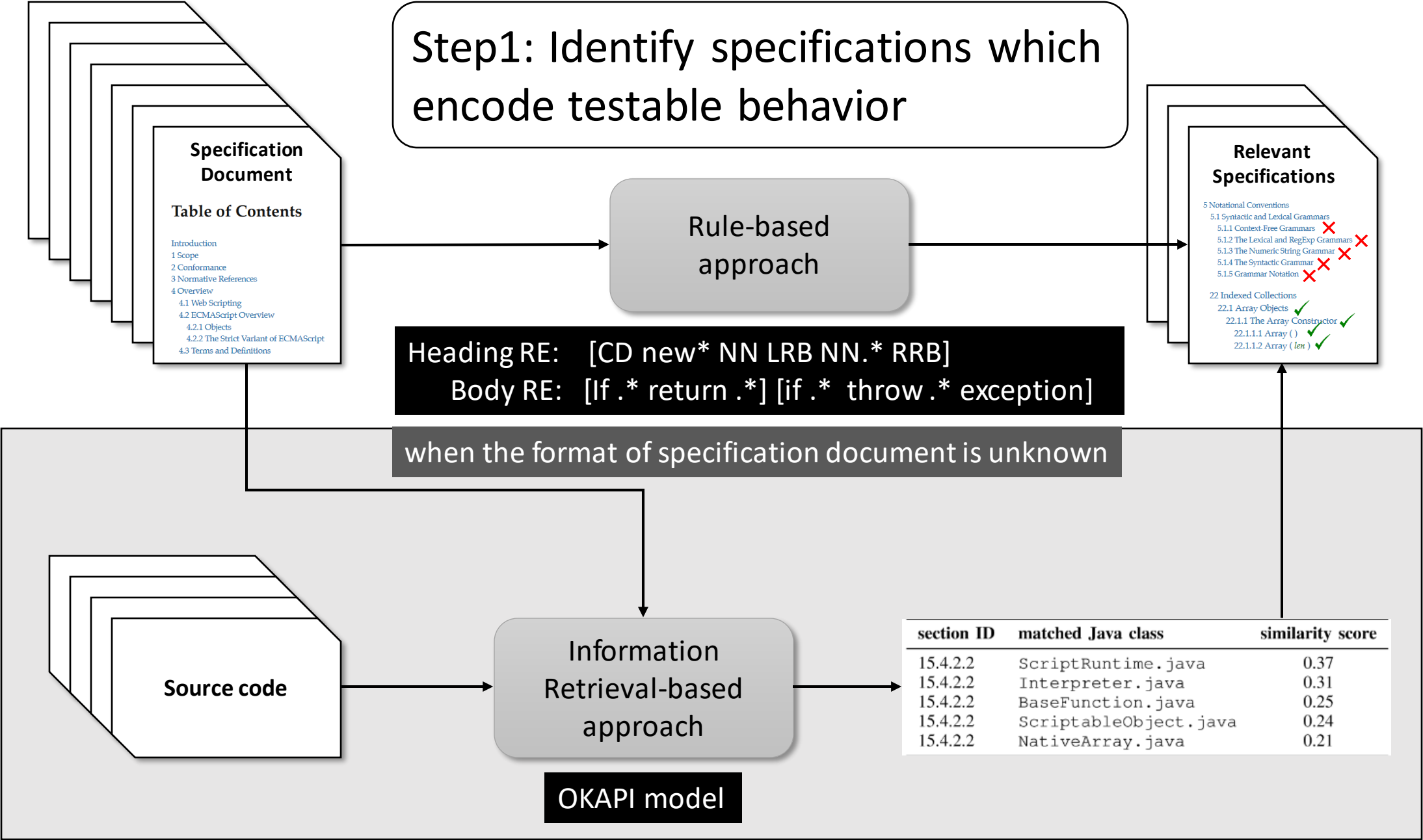
Manish Motwani and Yuriy Brun, ICSE' 2019

Practice your talk by recording your presentation  
See: <https://www.youtube.com/watch?v=GBwrvtrg1Ug>

# Swami







# Example specification encoding testable behavior

## Relevant Specifications

5 Notational Conventions	
5.1 Syntactic and Lexical Grammars	
5.1.1 Context-Free Grammars	✗
5.1.2 The Lexical and RegExp Grammars	✗
5.1.3 The Numeric String Grammar	✗
5.1.4 The Syntactic Grammar	✗
5.1.5 Grammar Notation	✗
22 Indexed Collections	
22.1 Array Objects	✓
22.1.1 The Array Constructor	✓
22.1.1.1 Array ( )	✓
22.1.1.2 Array ( len )	✓

### 21.1.3.20 String.prototype.startsWith ( *searchString* [ , *position* ] )

The following steps are taken:

1. Let *O* be ? RequireObjectCoercible(**this** value).
2. Let *S* be ? ToString(*O*).
3. Let *isRegExp* be ? IsRegExp(*searchString*).
4. If *isRegExp* is **true**, throw a **TypeError** exception.
5. Let *searchStr* be ? ToString(*searchString*).
6. Let *pos* be ? ToInteger(*position*). (If *position* is **undefined**, this step produces the value 0.)
7. Let *len* be the length of *S*.
8. Let *start* be min(max(*pos*, 0), *len*).
9. Let *searchLength* be the length of *searchStr*.
10. If *searchLength*+*start* is greater than *len*, return **false**.
11. If the sequence of elements of *S* starting at *start* of length *searchLength* is the same as the full element sequence of *searchStr*, return **true**.
12. Otherwise, return **false**.

Header RE:  
CD new\* NN LRB NN.\* RRB

Body RE:  
If .\* throw .\* exception

Body RE:  
If .\* return .\*

## Step2: Extract **method signature** from specification heading and initialize Test Template

### 21.1.3.20 String.prototype.startsWith ( *searchString* [, *position* ] )

The following steps are taken:

1. Let *O* be ? RequireObjectCoercible(this value).

**function** test\_< **method name** >(thisObj,<[ **method args** ]>) {}

3. Let *isRegExp* be ? IsRegExp(*searchString*).

4. If *isRegExp* is **true**, throw a **TypeError** exception.

5. Let *searchStr* be ? ToString(*searchString*).

6. Let *pos* be ? ToInteger(*position*). (If *position* is **undefined**, this step produces the value 0.)

7. Let *len* be the length of *S*.

**function** test\_string\_prototype\_startswith(thisObj,searchString,position) {}

Initialized  
Test Template

**new String(thisObj).startsWith(searchString, position);**

sequence of

12. Otherwise, return **false**.

Method  
invocation  
code

Step3: Identify and parse **Assignments** to store the local variables and their values

21.1.3.20 String.prototype.startsWith ( *searchString* [ , *position* ] )

The following steps are taken:

- 1. Let *O* be ? RequireObjectCoercible(**this** value).
- 2. Let *S* be ? ToString(*O*).
- 3. Let *isRegExp* be ? IsRegExp(*searchString*).
- 4. If *isRegExp* is **true**, throw a **TypeError** exception.
- 5. Let *searchStr* be ? ToString(*searchString*).
- 6. Let *pos* be ? ToInteger(*position*). (If *position* is **undefined**, this step produces the value 0.)
- 7. Let *len* be the length of *S*.
- 8. Let *start* be min(max(*pos*, 0), *len*).
- 9. Let *searchLength* be the length of *searchStr*.
- 10. If *searchLength*+*start* is greater than *len*, return **false**.
- 11. If the sequence of elements of *S* starting at *start* of length *searchLength* is the same as the full element sequence of *searchStr*, return **true**.
- 12. Otherwise, return **false**.

Variable	Value
O	RequireObjectCoercible(this value)
S	ToString(O)
isRegExp	IsRegExp(searchString)
searchStr	ToString(searchString)
pos	ToInteger(position)
len	length of S
start	min(max(pos,0),len)
searchLength	length of searchStr



## Step4: Identify and parse **Conditionals** to populate the conditional templates

### 21.1.3.20 String.prototype.startsWith ( *searchString* [ , *position* ] )

The following steps are taken:

1. Let *O* be ? RequireObjectCoercible(**this** value).
2. Let *S* be ? ToString(*O*).
3. Let *isRegExp* be ? IsRegExp(*searchString*).
4. If *isRegExp* is **true**, throw a **TypeError** exception.
5. Let *searchStr* be ? ToString(*searchString*).
6. Let *pos* be ? ToInteger(*position*). (If *position* is **undefined**, this step produces the value 0.)
7. Let *len* be the length of *S*.
8. Let *start* be min(max(*pos*, 0), *len*).
9. Let *searchLength* be the length of *searchStr*.
10. If *searchLength*+*start* is greater than *len*, return **false**.
11. If the sequence of elements of *S* starting at *start* of length *searchLength* is the same as the full element sequence of *searchStr*, return **true**.
12. Otherwise, return **false**.

# Step4: Identify and parse **Conditionals** to populate the conditional templates

```
if (<condition>) {
  try {
    var output = <method invocation>;
    return;
  } catch (e) {
    <test constructor>(true, (e instanceof <expected error>));
    return;
  }
}
```

Exception

```
if (<condition>) {
  var output = <method invocation>;
  <test constructor>(output, <expected output>);
  return;
}
```

Boundary Condition

3. Let *isRegExp* be ? *isRegExp*(*searchString*).

4. If *isRegExp* is **true**, throw a **TypeError** exception.

5. Let *searchStr* be ? *ToString*(*searchString*).

6. Let *pos* be ? *ToInteger*(*position*). (If *position* is **undefined**, this step produces the value 0.)

7. Let *len* be the length of *S*.

8. Let *start* be *min*(*max*(*pos*, 0), *len*).

9. Let *searchLength* be the length of *searchStr*.

10. If *searchLength*+*start* is greater than *len*, return **false**.

11. If the sequence of elements of *S* starting at *start* of length *searchLength* is the same as the full element sequence of *searchStr*, return **true**.

12. Otherwise, return **false**.

Step4: Identify and parse **Conditionals** to populate the conditional templates

```
if (<condition>) {  
  try {  
    var output = <method invocation>;  
    return;  
  } catch(e){  
    <test constructor>(true, (e instance of <expected error>));  
    return;  
  }  
}
```

Exception

```
if (<condition>) {  
  var output = <method invocation>;  
  <test constructor>(output, <expected output>);  
  return;  
}
```

Boundary Condition

- 3. Let *isRegExp* be ? *isRegExp*(*searchString*).
- 4. If *isRegExp* is **true**, throw a **TypeError** exception.
- 5. Let *searchStr* be ? *ToString*(*searchString*).
- 6. Let *pos* be ? *ToInteger*(*position*). (If *position* is **undefined**, this step produces **0**.)
- 7. Let *len* be the length of *S*.
- 8. Let *start* be *min*(*max*(*pos*, 0), *len*).
- 9. Let *searchLength* be the length of *searchStr*.
- 10. If *searchLength*+*start* is greater than *len*, return **false**.
- 11. If the sequence of elements of *S* starting at *start* of length *searchLength* is the same as the full element sequence of *searchStr*, return **true**.
- 12. Otherwise, return **false**.

Exception oracle

Boundary condition oracle

Step4: Identify and parse **Conditionals** to populate the conditional templates

```
if (<condition>) {  
  try {  
    var output = <method invocation>;  
    return;  
  } catch(e){  
    <test constructor>(true, (e instanceof <expected error>));  
    return;  
  }  
}
```

Exception

From step2

Input by developer

4. If *isRegExp* is true, throw a **TypeError** exception.

Exception oracle

```
if (isRegExp is true){  
  try{  
    var output = new String(thisObj).startsWith(searchString, position);  
    return;  
  } catch(e){  
    assert.StrictEqual(true, (e instanceof TypeError));  
    return;  
  }  
}
```



# Step4: Identify and parse **Conditionals** to populate the conditional templates

## 21.1.3.20 String.prototype.startsWith ( *searchString* [, *position*]

The following steps are taken:

- 1. Let *O* be ? RequireObjectCoercible(**this** value).
- 2. Let *S* be ? ToString(*O*).
- 3. Let *isRegExp* be ? IsRegExp(*searchString*).
- 4. If *isRegExp* is **true**, throw a **TypeError** exception.
- 5. Let *searchStr* be ? ToString(*searchString*).
- 6. Let *pos* be ? ToInteger(*position*). (If *position* is **undefined**, this step produces the value 0.)
- 7. Let *len* be the length of *S*.
- 8. Let *start* be min(max(*pos*, 0), *len*).
- 9. Let *searchLength* be the length of *searchStr*.
- 10. If *searchLength*+*start* is greater than *len*, return **false**.
- 11. If the sequence of elements of *S* starting at *start* length *searchLength* is the same as the full element sequence of *searchStr*, return **true**.
- 12. Otherwise, return **false**.

Boundary Condition

```
if (<condition>) {  
    var output = <method invocation>;  
    <test constructor>(output, <expected output>);  
    return;  
}
```

Boundary  
condition oracle

```
if (searchLength+start is greater than len){  
    var output = new String(thisObj).startsWith(searchString, position);  
    assert.strictEqual(output, false);  
    return;  
}
```



Step5: Recursively substitute **local variables** and **implicit operations**

```
if (isRegExp is true){
  try{
    var output = new String(thisObj).startsWith(searchString, position);
    return;
  }catch(e){
    assert.StrictEqual(true,(e instanceof TypeError));
    return;
  }
}
```

```
if (searchLength+start is greater than len){
  var output = new String(thisObj).startsWith(searchString, position);
  assert.strictEqual(output, false);
  return;
}
```

Variable	Value
O	RequireObjectCoercible(this value)
S	ToString(O)
isRegExp	IsRegExp(searchString)
searchStr	ToString(searchString)
pos	ToInteger(position)
len	length of S
start	min(max(pos,0),len)
searchLength	length of searchStr

**Method Arguments:**

thisObj  
searchString  
position

# Step5: Recursively substitute **local variables** and **implicit operations**

```
if (IsRegExp(searchString) === true) {
  try{
    var output = new String(thisObj).startsWith(searchString, position);
    return;
  }catch(e) {
    assert.StrictEqual(true, (e instanceof TypeError));
    return;
  }
}
```

```
if (ToString(searchString).length +
    Math.min(Math.max(ToInteger(position), 0),
    ToString(RequireObjectCoercible(thisObj)).length) >
    ToString(RequireObjectCoercible(thisObj)).length) {
  var output = new String(thisObj).startsWith(searchString, position);
  assert.strictEqual(output, false);
  return;
}
```

Variable	Value
O	RequireObjectCoercible(this value)
S	ToString(O)
isRegExp	IsRegExp(searchString)
searchStr	ToString(searchString)
pos	ToInteger(position)
len	length of S
start	min(max(pos,0),len)
searchLength	length of searchStr

**Method Arguments:**

thisObj  
searchString  
position

## Step6: Add conditionals to the initialized test template and check if it compiles

```
function test_string_prototype_startswith(thisObj, searchString, position) {  
  if (IsRegExp(searchString) === true) {  
    try {  
      var output = new String(thisObj).startsWith(searchString, position);  
      return;  
    } catch (e) {  
      assert.StrictEqual(true, (e instanceof TypeError));  
      return;  
    }  
  }  
}
```

}





## Implement **Abstract Operations** (100 lines JS code)

```
function IsRegExp(argument) {  
    return (argument instanceof RegExp);  
}  
...
```

```
function test_string_prototype_startswith(thisObj, searchString, position) {  
    if (IsRegExp(searchString) === true) {  
        try {  
            var output = new String(thisObj).startsWith(searchString, position);  
            return;  
        } catch (e) {  
            assert.StrictEqual(true, (e instanceof TypeError));  
            return;  
        }  
    }  
}
```

```
}
```



# Implement **Abstract Operations** (100 lines JS code)

```
function IsRegExp(argument) {
    return (argument instanceof RegExp);
}
...
```

Abstract Operations

```
function test_string_prototype_startswith(thisObj, searchString, position) {
```

```
    if (IsRegExp(searchString) === true) {
        try {
            var output = new String(thisObj).startsWith(searchString, position);
            return;
        } catch (e) {
            assert.StrictEqual(true, (e instanceof TypeError));
            return;
        }
    }
}
```

```
    if (ToString(searchString).length +
        Math.min(Math.max(ToInteger(position), 0),
            ToString(RequireObjectCoercible(thisObj)).length) >
        ToString(RequireObjectCoercible(thisObj)).length) {
        var output = new String(thisObj).startsWith(searchString, position);
        assert.strictEqual(output, false);
        return;
    }
}
```

```
}
```

Test Template encoding Oracles



# Step7: Instantiating test template by generating test inputs using random input generation

```
function IsRegExp(argument) {
    return (argument instanceof RegExp);
}
...
```

Abstract Operations

```
function test_string_prototype_startswith(thisObj, searchString, position) {
```

```
    if (IsRegExp(searchString) === true) {
        try {
            var output = new String(thisObj).startsWith(searchString, position);
            return;
        } catch (e) {
            assert.StrictEqual(true, (e instanceof TypeError));
            return;
        }
    }
}
```

```
    if (ToString(searchString).length +
        Math.min(Math.max(ToInteger(position), 0),
            ToString(RequireObjectCoercible(thisObj)).length) >
        ToString(RequireObjectCoercible(thisObj)).length) {
        var output = new String(thisObj).startsWith(searchString, position);
        assert.strictEqual(output, false);
        return;
    }
}
```

Test Template encoding Oracles

- Total number of inputs: 3
- Heuristic: String method => *thisObj* should be a valid string
- Number of test inputs to be generated: 1000



```
test_string_prototype_startswith("Y3I9", "E0RS6GU078", 894);
test_string_prototype_startswith("T82LL6", 572, false);
test_string_prototype_startswith("XU6W0", "J3A", Infinity);
test_string_prototype_startswith("W5E74X0R", null, NaN);
...
```



### 21.1.3.20 String.prototype.startsWith ( *searchString* [, *position*] )

The following steps are taken:

1. Let *O* be ? *RequireObjectCoercible*(**this** value).
2. Let *S* be ? *ToString*(*O*).
3. Let *isRegExp* be ? *IsRegExp*(*searchString*).
4. If *isRegExp* is **true**, throw a **TypeError** exception.
5. Let *searchStr* be ? *ToString*(*searchString*).
6. Let *pos* be ? *ToInteger*(*position*). (If *position* is **undefined**, let *pos* be 0.)
7. Let *len* be the length of *S*.
8. Let *start* be *min*(*max*(*pos*, 0), *len*).
9. Let *searchLength* be the length of *searchStr*.
10. If *searchLength*+*start* is greater than *len*, return **false**.
11. If the sequence of elements of *S* starting at *start* of length *searchLength*, return **true**.
12. Otherwise, return **false**.

#### Executable Test with Oracles

```
function IsRegExp (argument) {  
    return (argument instanceof RegExp);  
}
```

Abstract Operations

```
function test_string_prototype_startswith (thisObj, searchString, position) {  
    if (IsRegExp (searchString) === true) {  
        try {  
            var output = new String (thisObj).startsWith (searchString, position);  
            return;  
        } catch (e) {  
            assert.StrictEqual (true, (e instanceof TypeError));  
            return;  
        }  
    }  
}
```

```
    if (ToString (searchString).length +  
        Math.min (Math.max (ToInteger (position), 0),  
            ToString (RequireObjectCoercible (thisObj)).length) >  
        ToString (RequireObjectCoercible (thisObj)).length) {  
        var output = new String (thisObj).startsWith (searchString, position);  
        assert.strictEqual (output, false);  
        return;  
    }  
}
```

Test Template encoding Oracles

```
test_string_prototype_startswith ("Y3I9", "E0RS6GU078", 894);  
test_string_prototype_startswith ("T82LL6", 572, false);  
test_string_prototype_startswith ("XU6W0", "J3A", Infinity);  
test_string_prototype_startswith ("W5E74X0R", null, NaN);  
...
```

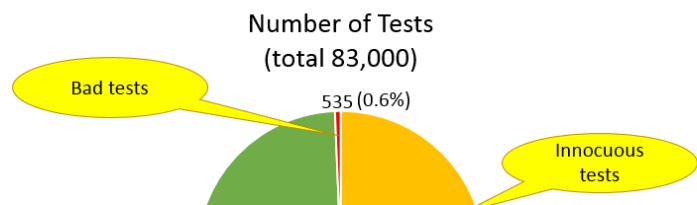
Test Inputs



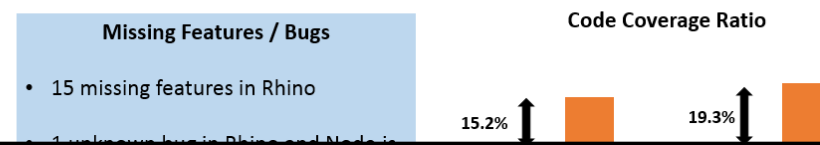
Swami

# Evaluation: A reminder

Swami-generated tests are precise to the specification



Swami covers more code and identifies features and bugs missed by developer-written tests



On JavaScript specification, Swami

- is 98.4% precise to the specification,
- improves developer-written and generated test suites, and
- Identifies 1 new bug and 15 missing features in Rhino, 1 new bug in Node.js, and 18 semantic ambiguities in the spec

bad tests  
■ EvoSuite ■ Swami

line coverage  
■ EvoSuite ■ EvoSuite+Swami

Swami tests complement EvoSuite-written tests









bad tests  
■ EvoSuite ■ Swami

line coverage  
■ EvoSuite ■ EvoSuite+Swami

Swami tests complement EvoSuite-written tests

# QUIZ: Randoop, Korat, and Swami

Which of the following statements are true for each test generation technique:

	Randoop	Korat	Swami
Uses type information to guide test generation.			
Each test is generated independently of the past test.			
Generates tests deterministically.			
Suited to test method sequences.			
Avoids generating redundant tests.			

# Symbolic Execution

- Reasoning about behavior of program by “executing” it using **symbolic values**
- Originally proposed by James King (1976, CASM) and Lori Clarke (1976, IEEE TSE)
- Became **practical** around 2005 because of **advances in constraint solving** (SMT solvers)

# Example

```
function f(a, b, c) {  
  var x = y = z = 0;  
  if (a) {  
    x = -2;  
  }  
  if (b > 5) {  
    if (!a && c) {  
      y = 1;  
    }  
    z = 2;  
  }  
  assert(x + y + z != 3);  
}
```

## Concrete Execution

Suppose  $a = b = c = 1$

$x = y = z = 0$

If(a) = true

$x = -2$

If ( $b > 5$ ) = false

$\text{assert}(-2 + 0 + 0 \neq 3) = \text{true}$



# Example

Symbolic values

**Symbolic Execution**

$a = a_0$     $b = b_0$     $c = c_0$

```
function f(a, b, c) {
  var x = y = z = 0;
  if (a) {
    x = -2;
  }
  if (b > 5) {
    if (!a && c) {
      y = 1;
    }
    z = 2;
  }
  assert(x + y + z != 3);
}
```

# Example

Symbolic values

## Symbolic Execution

$a = a_0$     $b = b_0$     $c = c_0$   
 $x = y = z = 0$

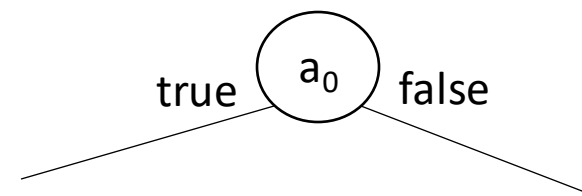
```
function f(a, b, c) {  
  var x = y = z = 0;  
  if (a) {  
    x = -2;  
  }  
  if (b > 5) {  
    if (!a && c) {  
      y = 1;  
    }  
    z = 2;  
  }  
  assert(x + y + z != 3);  
}
```

# Example

Symbolic values

Symbolic Execution

$a = a_0$     $b = b_0$     $c = c_0$   
 $x = y = z = 0$

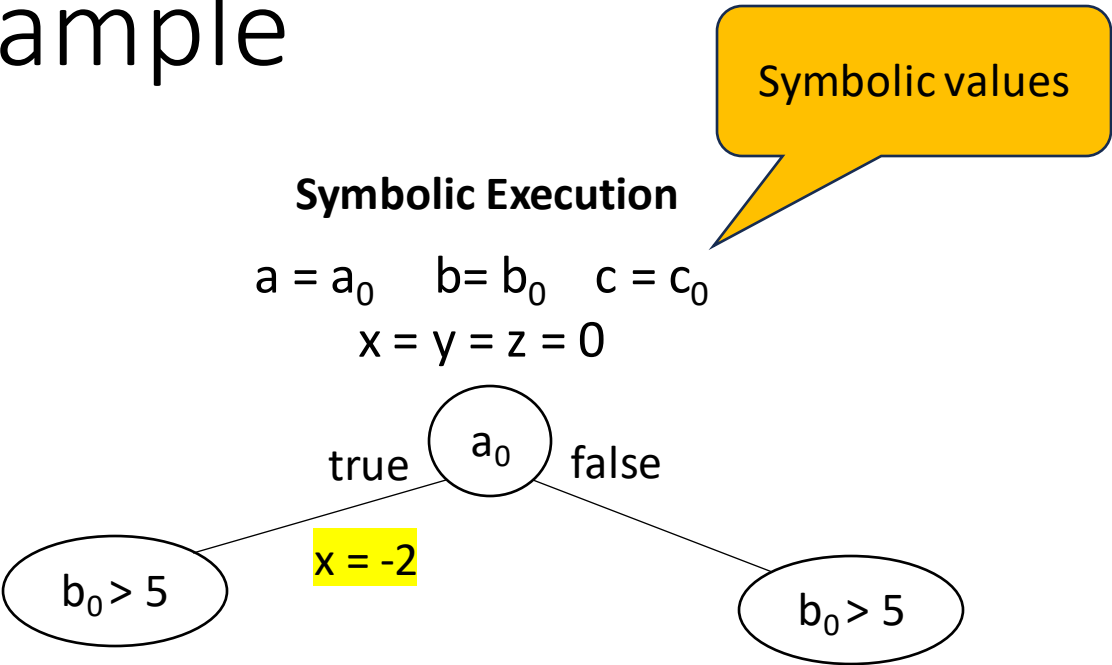


```

function f(a, b, c) {
  var x = y = z = 0;
  if (a) {
    x = -2;
  }
  if (b > 5) {
    if (!a && c) {
      y = 1;
    }
    z = 2;
  }
  assert(x + y + z != 3);
}
  
```

# Example

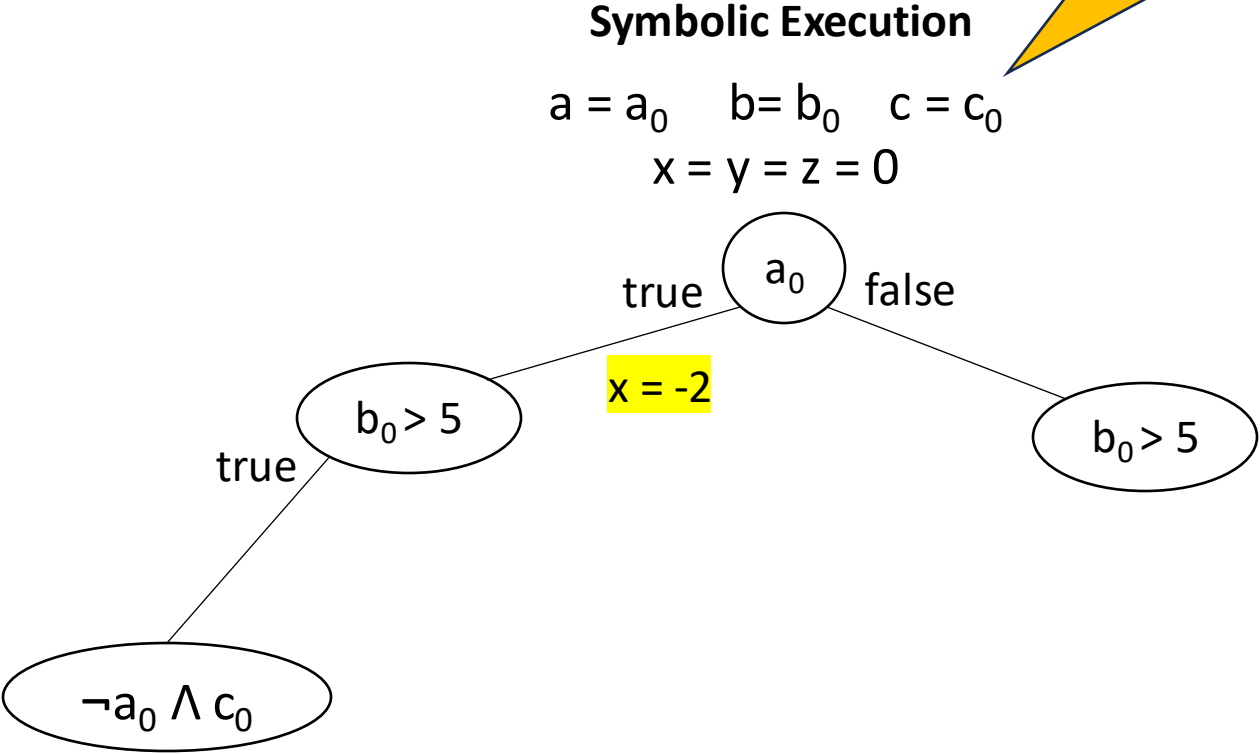
```
function f(a, b, c) {  
  var x = y = z = 0;  
  if (a) {  
    x = -2;  
  }  
  if (b > 5) {  
    if (!a && c) {  
      y = 1;  
    }  
    z = 2;  
  }  
  assert(x + y + z != 3);  
}
```



# Example

Symbolic values

```
function f(a, b, c) {  
  var x = y = z = 0;  
  if (a) {  
    x = -2;  
  }  
  if (b > 5) {  
    if (!a && c) {  
      y = 1;  
    }  
    z = 2;  
  }  
  assert(x + y + z != 3);  
}
```

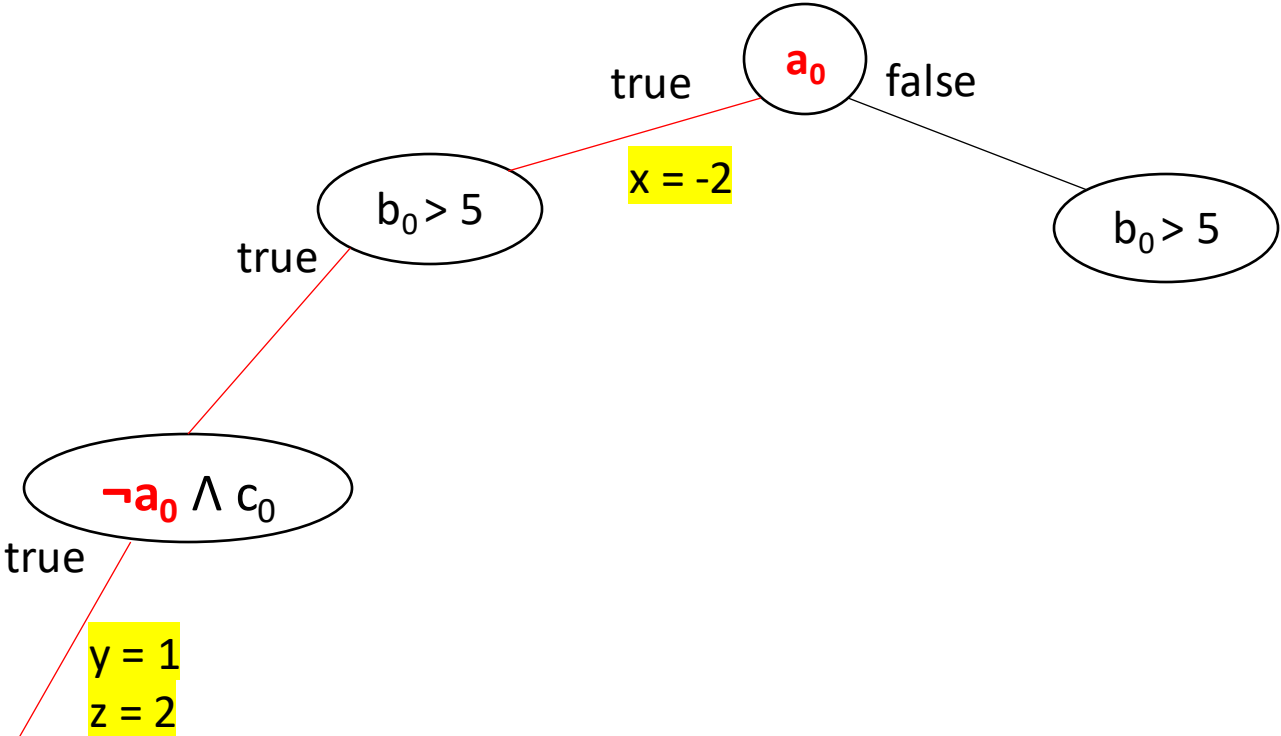


# Example

Symbolic values

## Symbolic Execution

$a = a_0 \quad b = b_0 \quad c = c_0$   
 $x = y = z = 0$



```
function f(a, b, c) {  
  var x = y = z = 0;  
  if (a) {  
    x = -2;  
  }  
  if (b > 5) {  
    if (!a && c) {  
      y = 1;  
    }  
    z = 2;  
  }  
  assert(x + y + z != 3);  
}
```

$a_0 \wedge (b_0 > 5) \wedge (\neg a_0 \wedge c_0)$

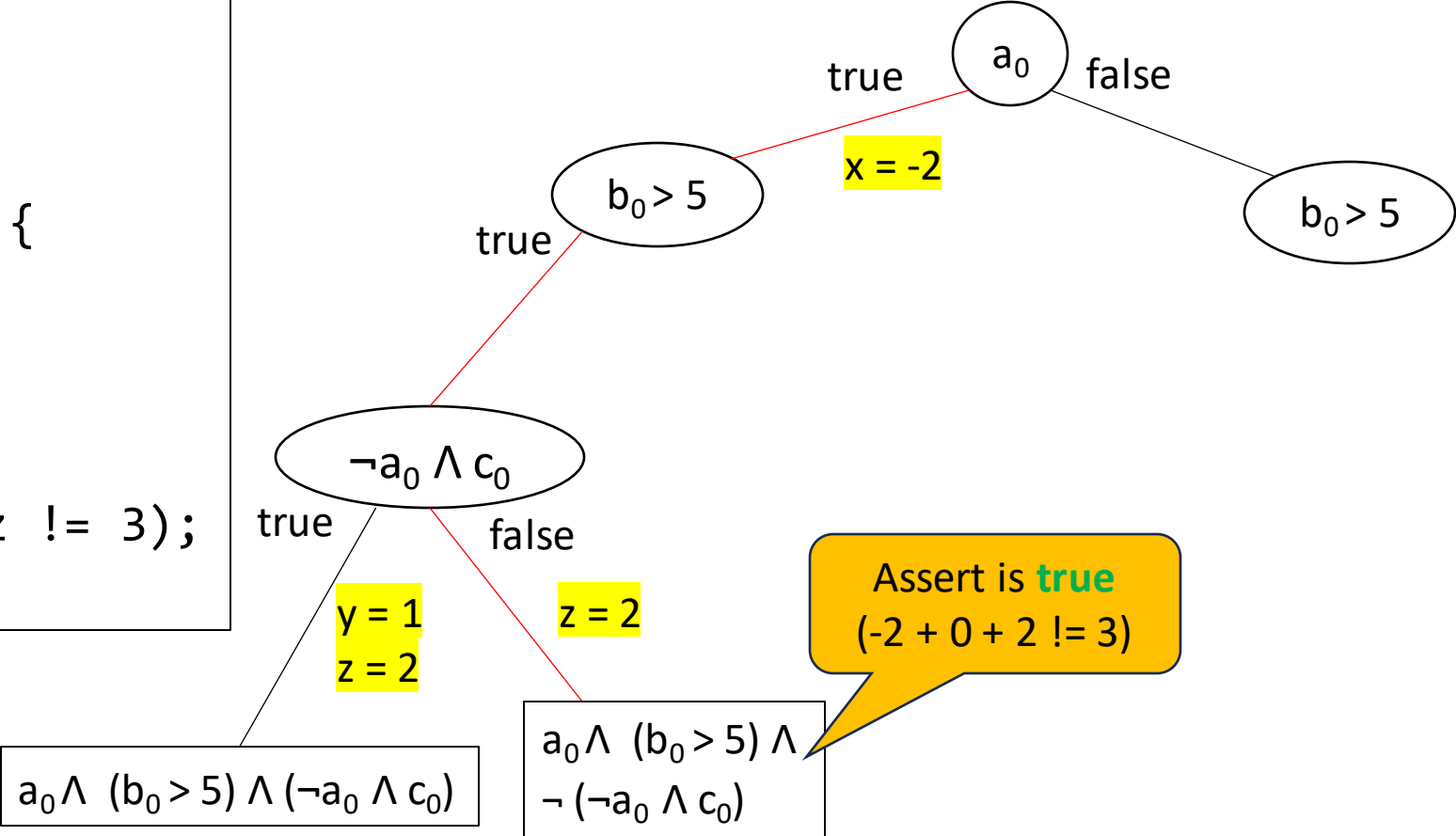
Infeasible path

# Example

```
function f(a, b, c) {  
  var x = y = z = 0;  
  if (a) {  
    x = -2;  
  }  
  if (b > 5) {  
    if (!a && c) {  
      y = 1;  
    }  
    z = 2;  
  }  
  assert(x + y + z != 3);  
}
```

Symbolic values

Symbolic Execution  
 $a = a_0 \quad b = b_0 \quad c = c_0$   
 $x = y = z = 0$



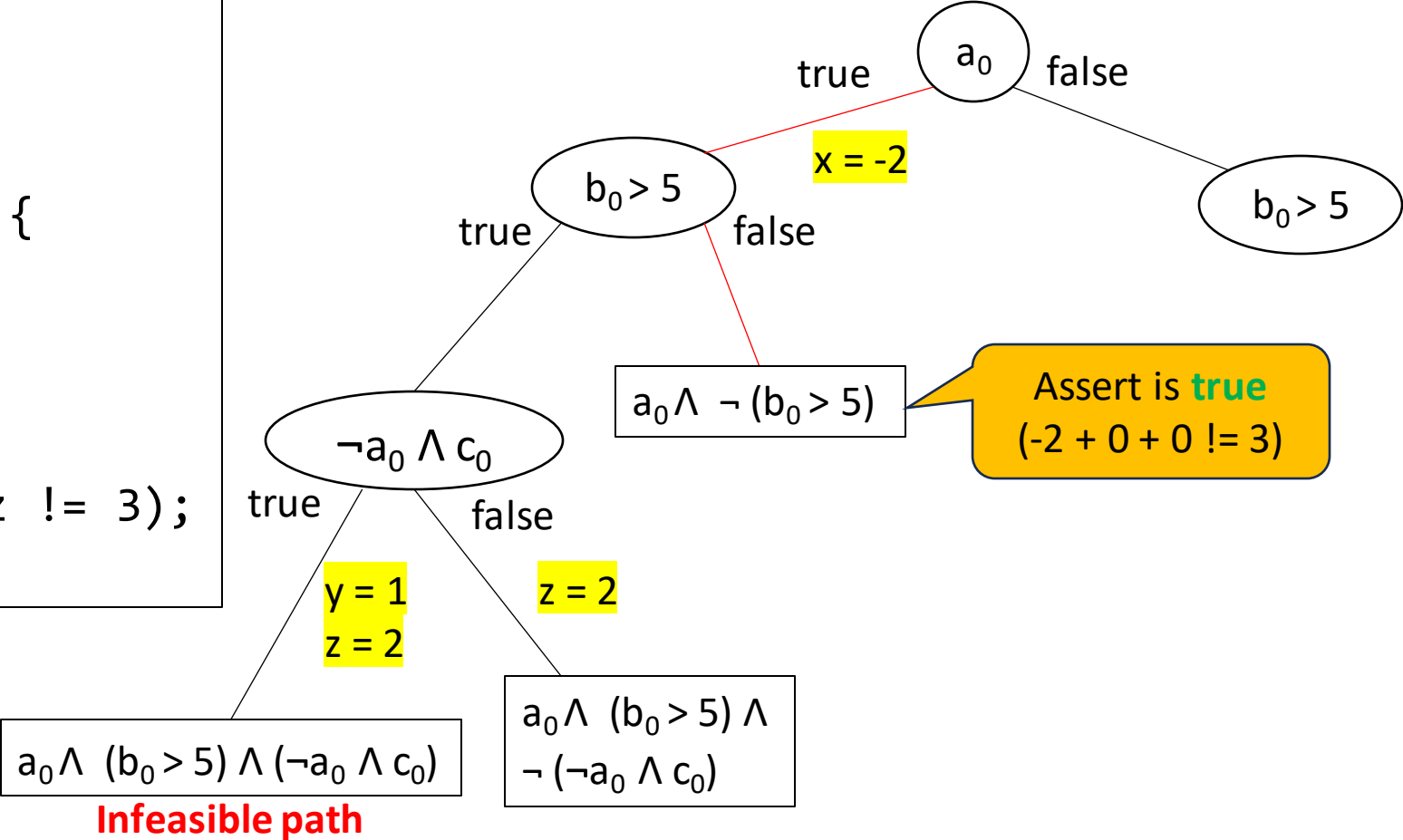
# Example

Symbolic values

## Symbolic Execution

$$\begin{aligned} a &= a_0 & b &= b_0 & c &= c_0 \\ x &= y = z = 0 \end{aligned}$$

```
function f(a, b, c) {  
  var x = y = z = 0;  
  if (a) {  
    x = -2;  
  }  
  if (b > 5) {  
    if (!a && c) {  
      y = 1;  
    }  
    z = 2;  
  }  
  assert(x + y + z != 3);  
}
```





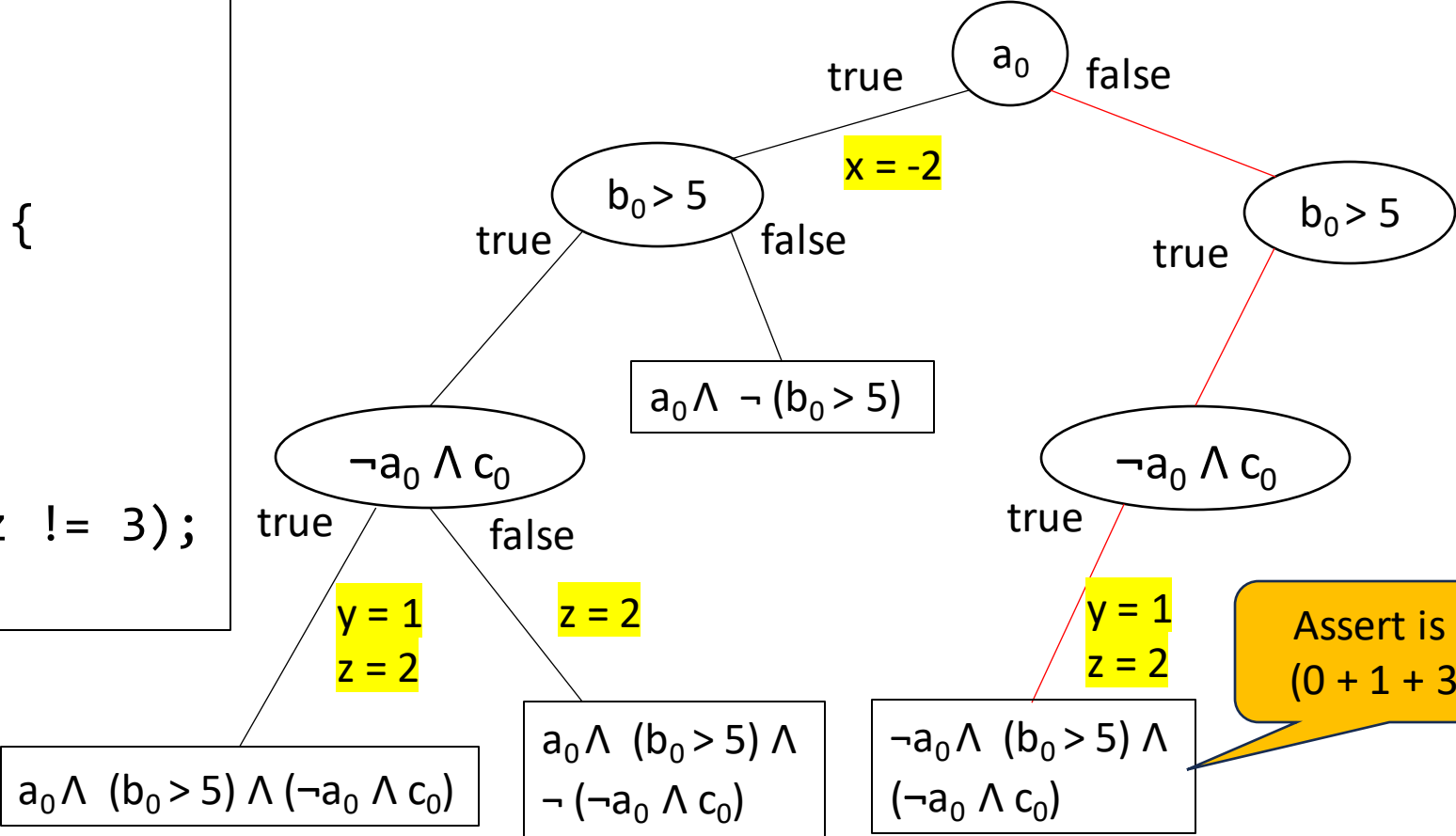
# Example

Symbolic values

## Symbolic Execution

$a = a_0 \quad b = b_0 \quad c = c_0$   
 $x = y = z = 0$

```
function f(a, b, c) {  
  var x = y = z = 0;  
  if (a) {  
    x = -2;  
  }  
  if (b > 5) {  
    if (!a && c) {  
      y = 1;  
    }  
    z = 2;  
  }  
  assert(x + y + z != 3);  
}
```



Infeasible path

Assert is **false**  
(0 + 1 + 3 != 3)

Symbolic values

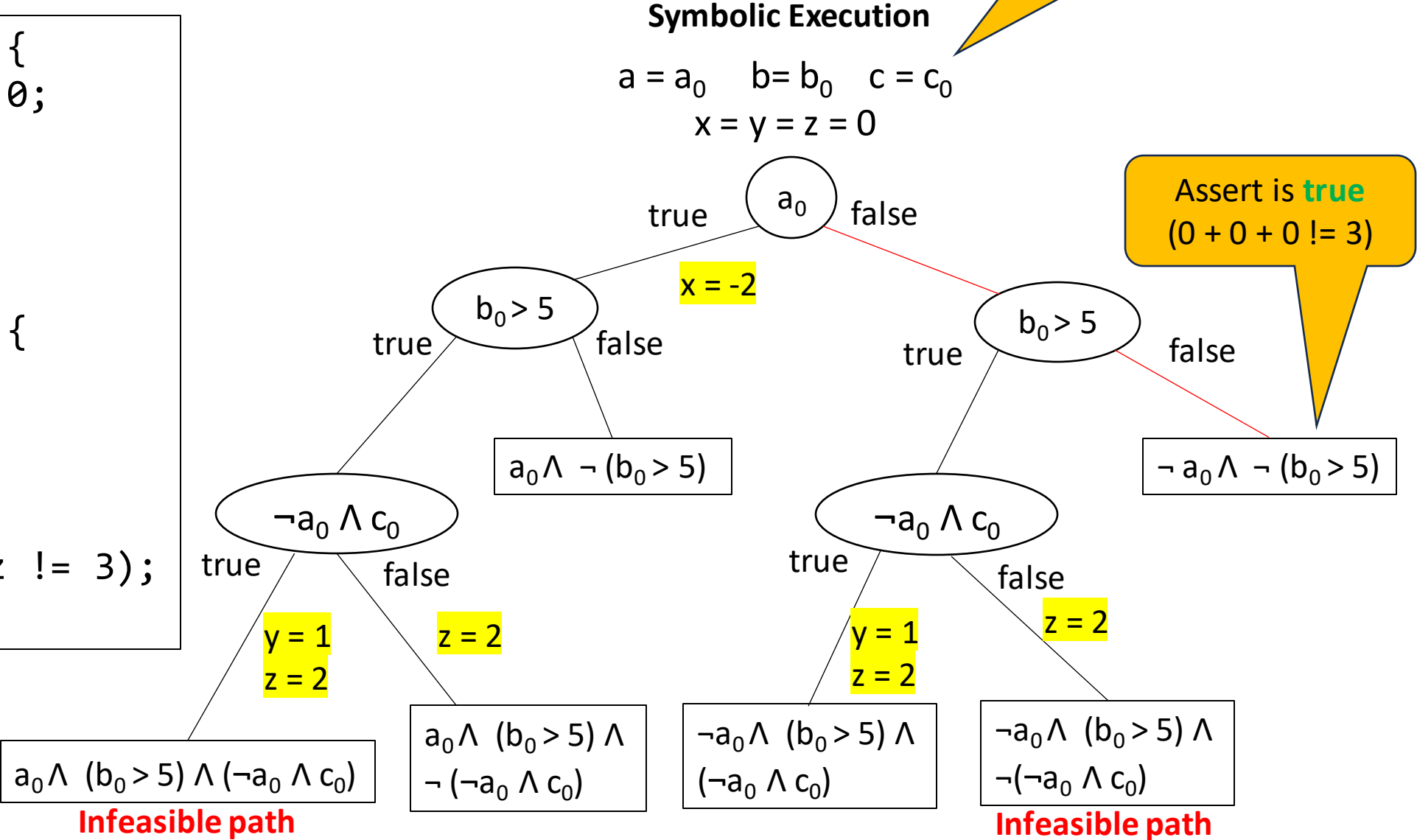
$$a = a_0 \quad b = b_0 \quad c = c_0$$

$$x = y = z = 0$$


## Infeasible path

# Example

```
function f(a, b, c) {  
  var x = y = z = 0;  
  if (a) {  
    x = -2;  
  }  
  if (b > 5) {  
    if (!a && c) {  
      y = 1;  
    }  
    z = 2;  
  }  
  assert(x + y + z != 3);  
}
```



# Example

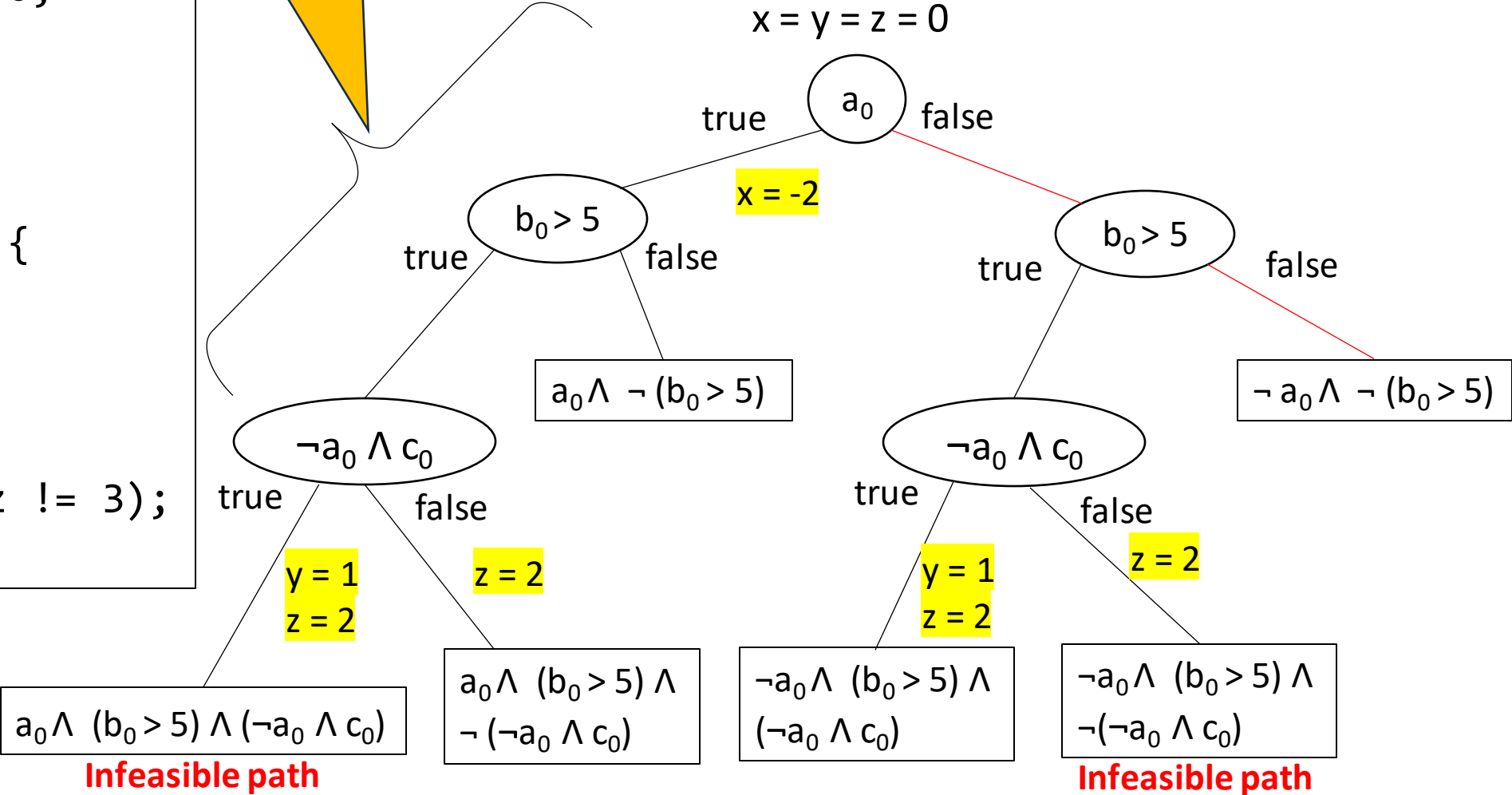
Symbolic values

```
function f(a, b, c) {  
  var x = y = z = 0;  
  if (a) {  
    x = -2;  
  }  
  if (b > 5) {  
    if (!a && c) {  
      y = 1;  
    }  
    z = 2;  
  }  
  assert(x + y + z != 3);  
}
```

Execution or Computation Tree

Symbolic Execution

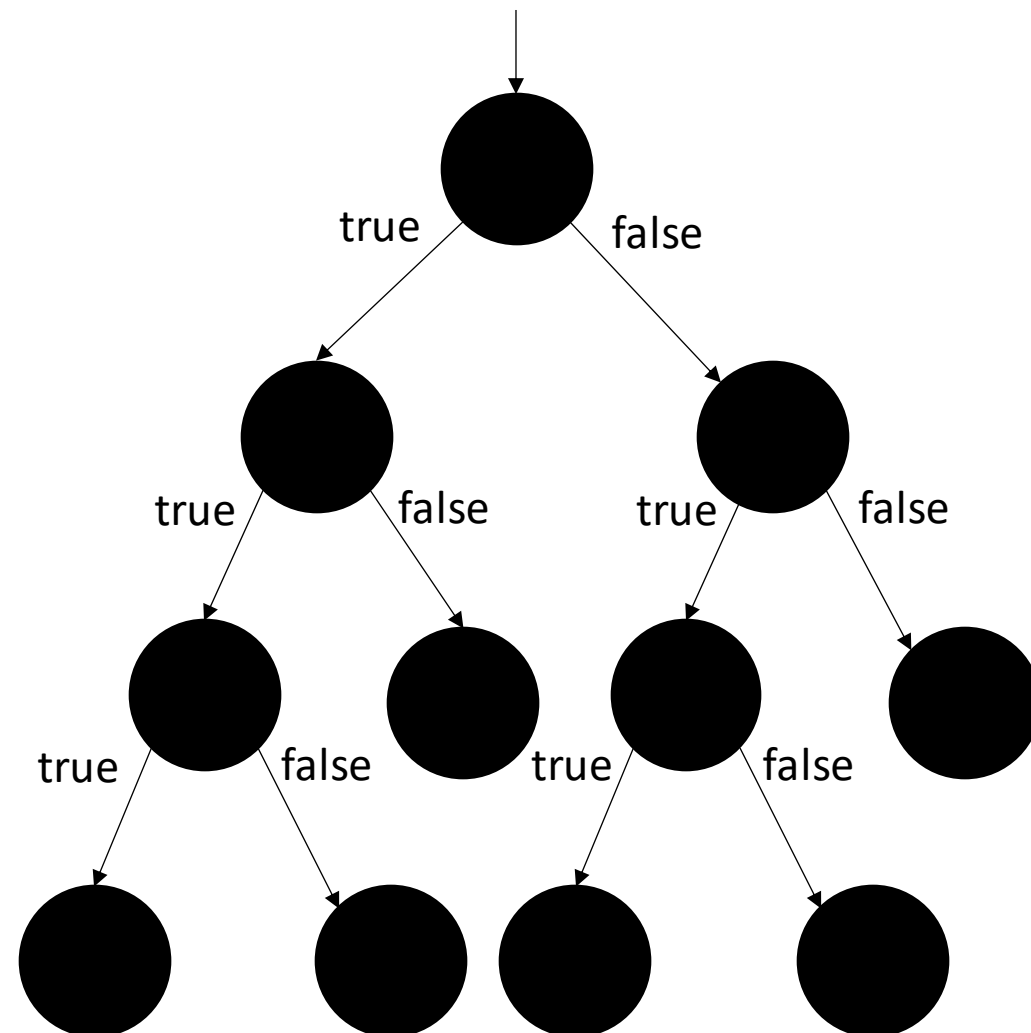
$a = a_0 \quad b = b_0 \quad c = c_0$   
 $x = y = z = 0$



# Execution Tree

All possible execution paths

- **Binary tree**
- **Nodes:** conditional statements
- **Edges:** execution of program on non-conditional statements
- Each **path** in tree represents equivalence class of inputs.



# QUIZ: Execution Tree

```
function f(x,y) {  
  var s = "foo";  
  if (x < y) {  
    s += "bar";  
    console.log(s);  
  }  
  if (y == 23) {  
    console.log(s);  
  }  
}
```

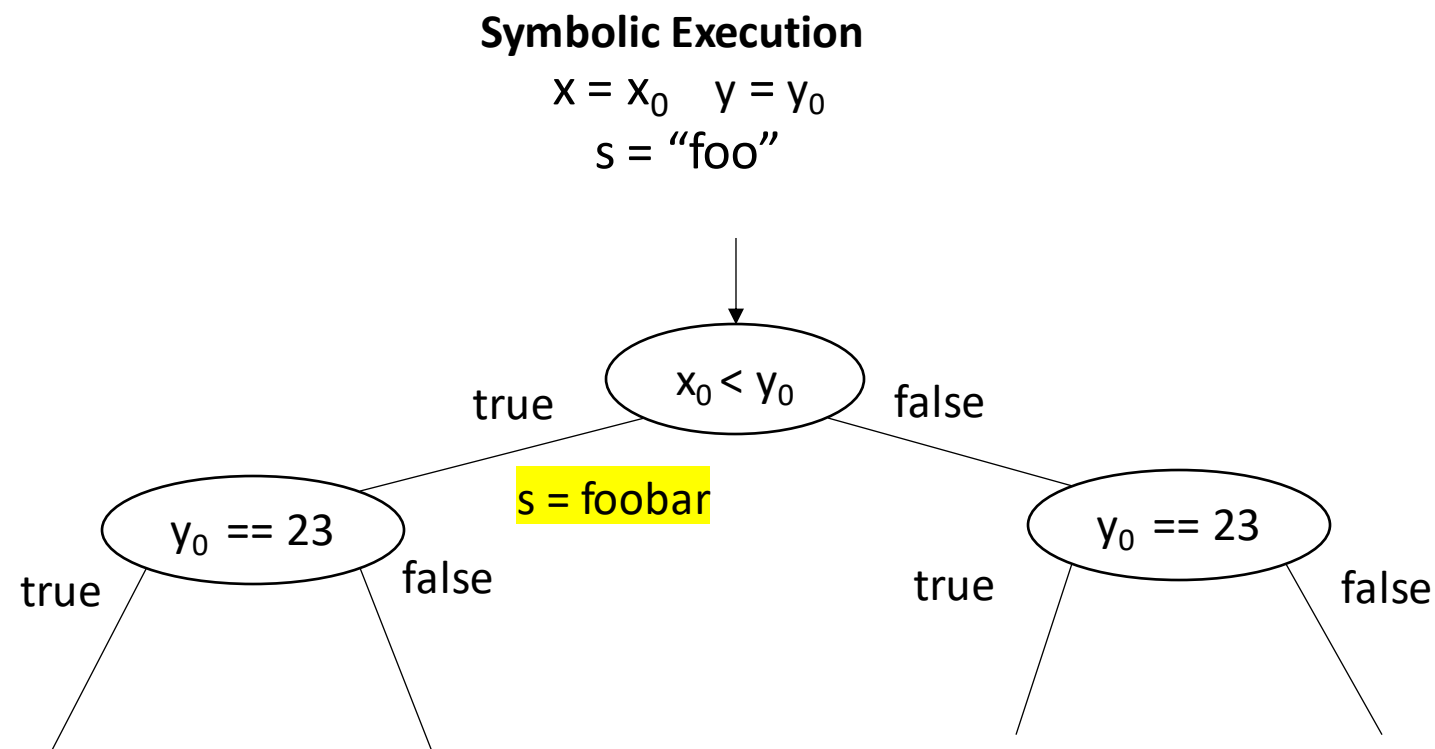
How many nodes and edges are there in the execution tree of the above function?

# QUIZ: Execution Tree

```
function f(x,y) {
  var s = "foo";
  if (x < y) {
    s += "bar";
    console.log(s);
  }
  if (y == 23) {
    console.log(s);
  }
}
```

How many nodes and edges are there in the execution tree of the above function?

3 Nodes and 7 Edges



# Symbolic Values and Symbolic States

- Unknown values of variables  
e.g., user inputs are kept  
**symbolically**
- **Symbolic State** maps program  
variables to their symbolic  
values

```
function f(x,y) {  
    var z = x + y;  
    if (z > 0) {...}  
}
```

$x = x_0 \quad y = y_0$

$z = x_0 + y_0$

Symbolic state  
of z





# Path Conditions

**Quantifier-free formula** over the symbolic inputs that encode all **branch decisions** taken so far

```
function f(x,y) {  
    var z = x + y;  
    if (z > 0) {...}  
}
```

$x = x_0 \quad y = y_0$

$z = x_0 + y_0$

$(x_0 + y_0) > 0$

Path condition



# Satisfiability of Formulas

- Determine whether a path is feasible
  - Check if the path condition is satisfiable
- Done by powerful SMT/SAT solvers
  - SAT = Satisfiability
  - SMT = Satisfiability Modulo Theory
  - E.g., Z2, Yices, STP
- For satisfiable formula, solvers also provide concrete solution
- Examples
  - $(x_0 + y_0) > 1$  : SAT  $x_0 = 1; y_0 = 1$
  - $(x_0 + y_0) < 0 \wedge (x_0 - 1) > 5 \wedge (y_0 > 0)$ : UNSAT

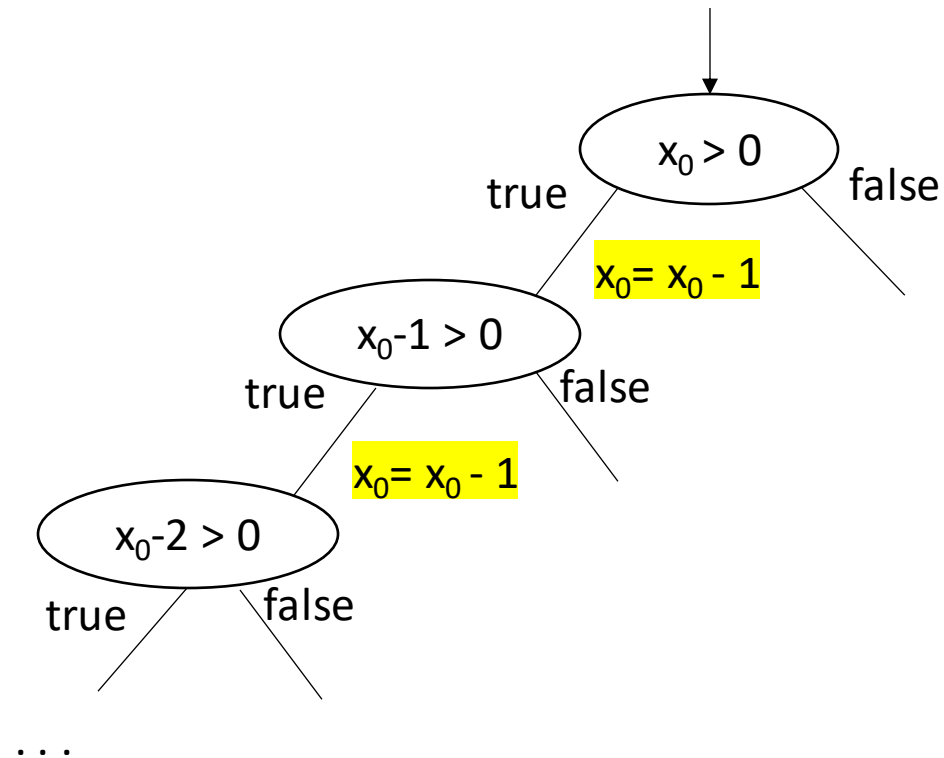
# Applications of Symbolic Execution

- General goal: **reason about the behavior of program**
- Basic applications
  - Detect infeasible paths
  - Generate test inputs
  - Find bugs and Vulnerabilities
- Advanced applications
  - Generate program invariants
  - Prove program equivalence
  - Debugging
  - Automatic Program Repair

# Problems of Symbolic Execution

- **Loops and Recursions:** infinite execution tree

```
function f(a) {
  var x = a;
  while (x > 0) {
    x--;
  }
}
```



# Problems of Symbolic Execution

- **Loops and Recursions:** infinite execution tree
- **Path explosion:** number of paths is exponential in the number of conditionals

```
function f(a) {  
    if (x) {...}  
    if (y) {...}  
    ...  
}
```

How many paths are there in the execution tree of this function?

# Problems of Symbolic Execution

- **Loops and Recursions:** infinite execution tree
- **Path explosion:** number of paths is exponential in the number of conditionals

```
function f(a) {  
    if (x) {...}  
    if (y) {...}  
    ...  
}
```

How many paths are there in the execution tree of this function?

$$2^2 = 4$$

1.  $x \wedge y$
2.  $x \wedge \neg y$
3.  $\neg x \wedge y$
4.  $\neg x \wedge \neg y$

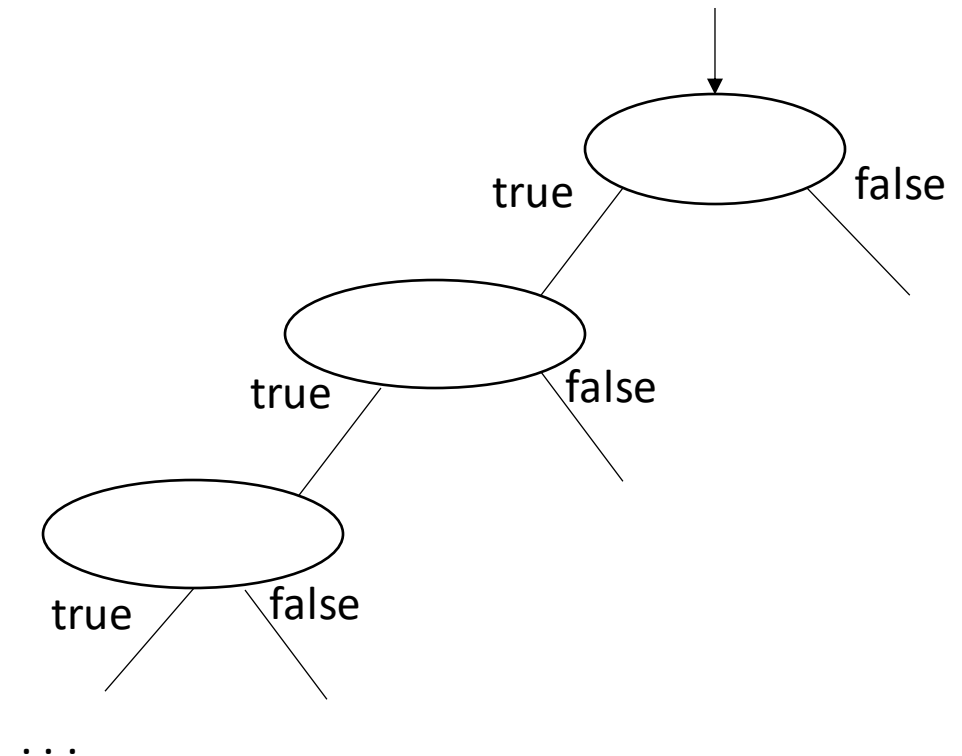
# Problems of Symbolic Execution

- **Loops and Recursions:** infinite execution tree
- **Path explosion:** number of paths is exponential in the number of conditionals
- **Environmental modeling:** dealing with native/system/library calls
- **Solver limitations:** dealing with complex path conditions
- **Heap modeling:** symbolic representation of data structures and pointers

# Dealing with Large Execution Trees

**Heuristically** select which branch to explore next

- Select at **random**
- Select based on **coverage**
- Prioritize based on distance to **“interesting”** program locations
- Interleaving **symbolic execution** with **random testing**





# Dealing with Environment

- Program behavior may depend on **parts of system not analyzed** by symbolic execution engine
- E.g., native APIs, interaction with network, file system access

```
var fs = require("fs");  
var content =  
fs.readFileSync("/tmp/foo.txt");  
if (content == "bar") {  
    ...  
}
```

How to reason  
about the  
environment?

# Dealing with Environment

- Program behavior may depend on **parts of system not analyzed** by symbolic execution engine
- E.g., native APIs, interaction with network, file system access
- Solution: **Model the file system (implemented by KLEE)**
  - If all arguments are concrete, forward to OS
  - Otherwise, provide **models that can handle symbolic files**
    - **Goal:** explore all possible legal interactions with the environment

```
var fs = require("fs");
var content =
fs.readFileSync("/tmp/foo.txt");
if (content == "bar") {
    ...
}
```

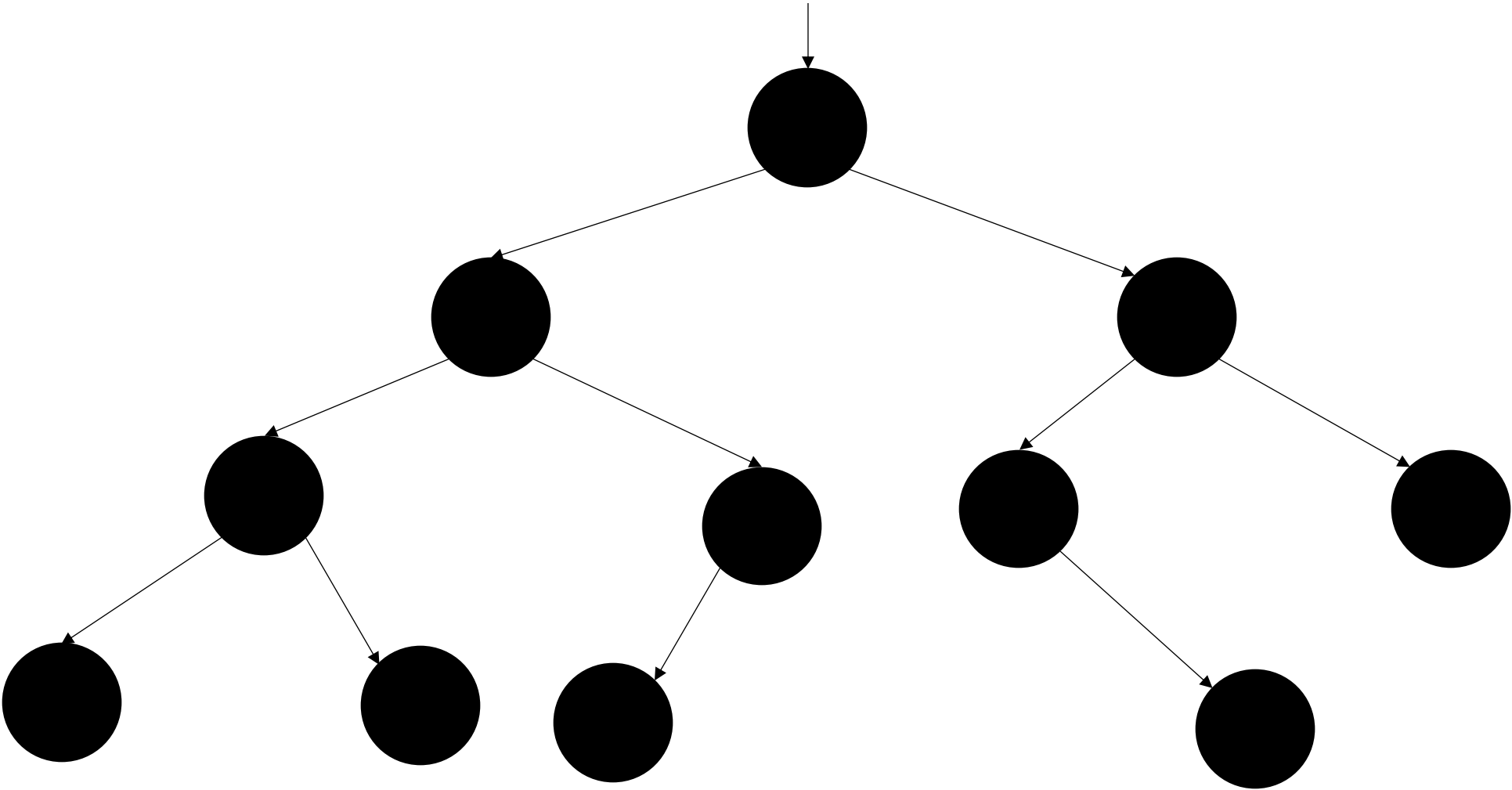
```
var fs = {
  readFileSync: function(file){
    // doesn't read actual file system, but
    // models its effect for symbolic file name
  }
}
```

# Combined Approach

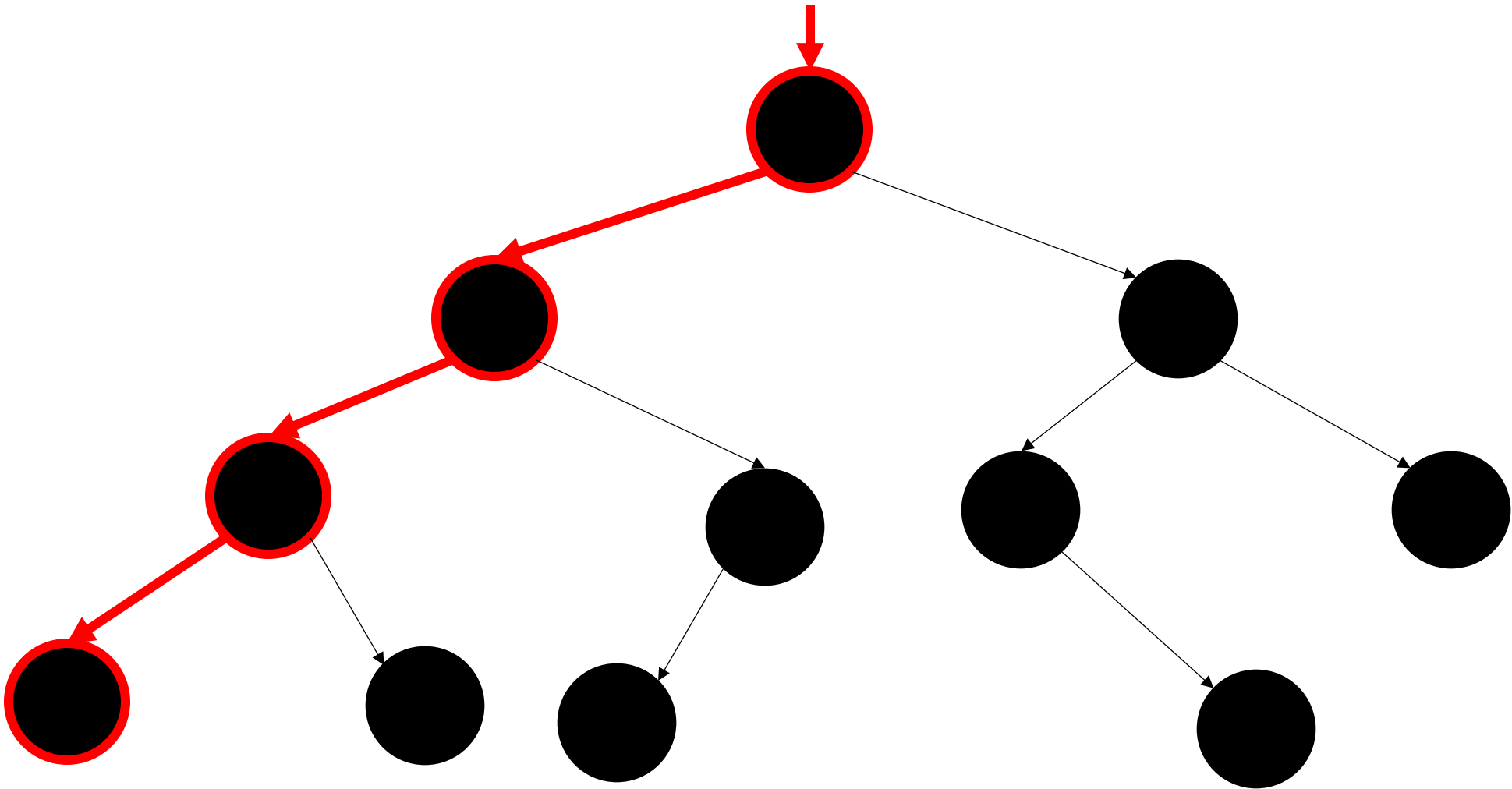
**Concrete + Symbolic = Concolic Testing** or  
Dynamic Symbolic Execution (DSE)

- Start with **random input values**
- Keep track of **both** concrete and symbolic values
- Use concrete values to **simplify** symbolic constraints to help solver

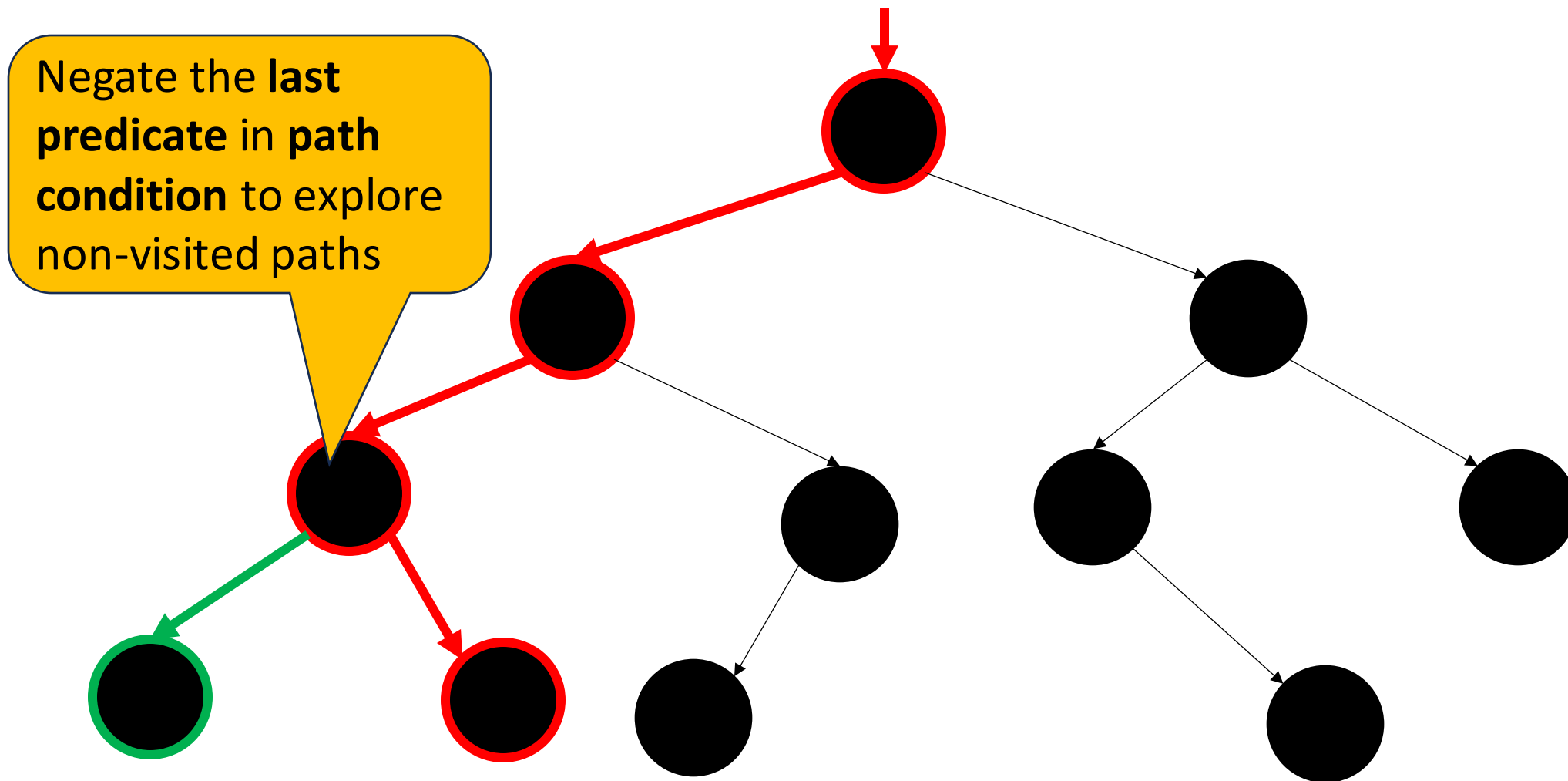
# Exploring the Execution Tree



# Exploring the Execution Tree

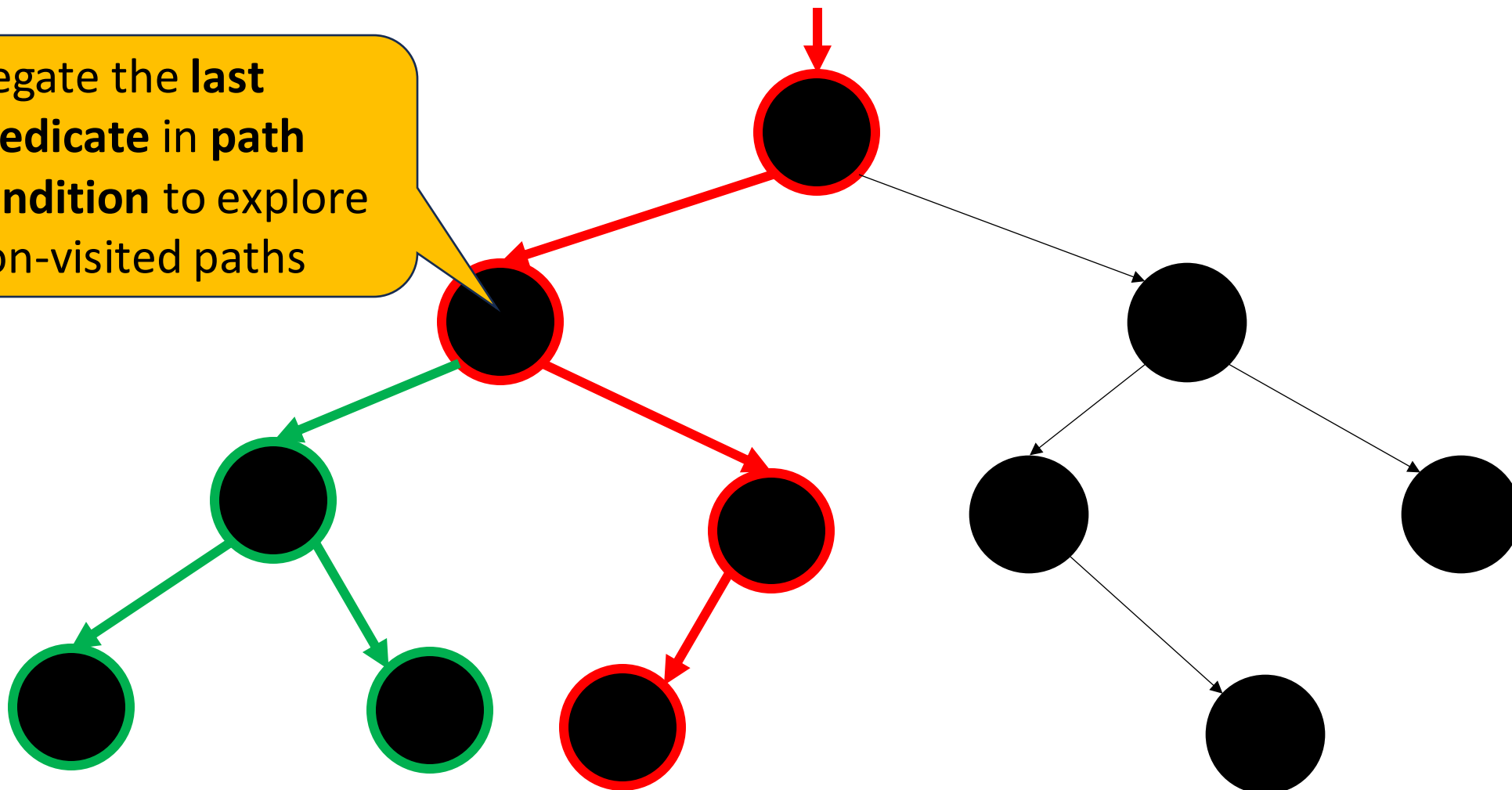


# Exploring the Execution Tree



# Exploring the Execution Tree

Negate the **last predicate in path condition** to explore non-visited paths



# DSE: An Illustrative Example

```
int foo(int v) {
    return 2*v;
}
```

```
void test_me(int x, int y) {
    int z = foo(y);
    if (z == x)
        if (x > y+10)
            ERROR;
}
```



Concrete  
Execution

Symbolic  
Execution

concrete  
state

symbolic  
state

path  
condition





# DSE: An Illustrative Example

```
int foo(int v) {
    return 2*v;
}
```

```
void test_me(int x, int y) {
    int z = foo(y);
    if (z == x)
        if (x > y+10)
            ERROR;
}
```

Concrete  
Execution

Symbolic  
Execution

concrete  
state

symbolic  
state

path  
condition

x = 22  
y = 7

x =  $x_0$   
y =  $y_0$



# DSE: An Illustrative Example

```
int foo(int v) {
    return 2*v;
}
```

```
void test_me(int x, int y) {
    int z = foo(y);
    if (z == x)
        if (x > y+10)
            ERROR;
}
```

Concrete  
Execution

Symbolic  
Execution

concrete  
state

symbolic  
state

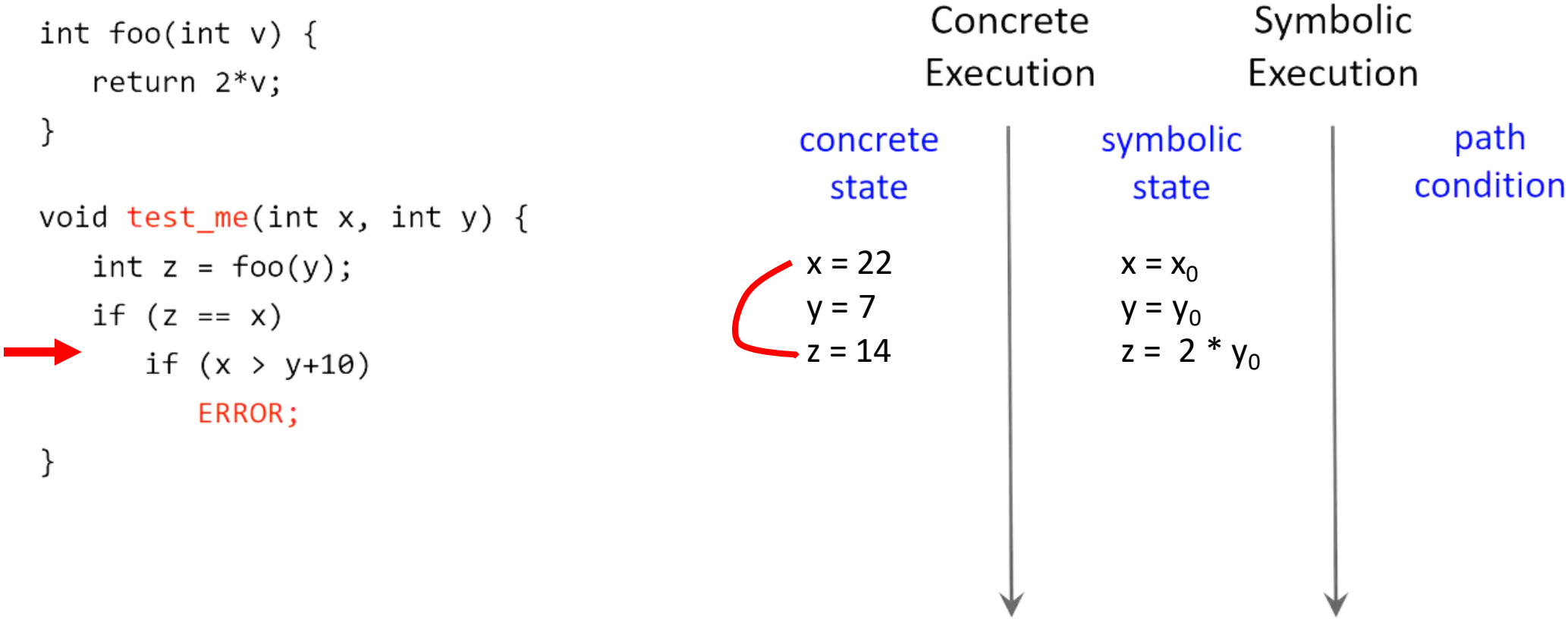
path  
condition

x = 22  
y = 7  
z = 14

x =  $x_0$   
y =  $y_0$   
z =  $2 * y_0$



# DSE: An Illustrative Example



# DSE: An Illustrative Example

```
int foo(int v) {
    return 2*v;
}
```

```
void test_me(int x, int y) {
    int z = foo(y);
    if (z == x)
        if (x > y+10)
            ERROR;
}
```



Concrete  
Execution

Symbolic  
Execution

concrete  
state

symbolic  
state

path  
condition

x = 22  
y = 7  
z = 14

$x = x_0$   
 $y = y_0$   
 $z = 2*y_0$

$x_0 \neq 2*y_0$



# DSE: An Illustrative Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
→ }  
}
```

Concrete  
Execution

concrete  
state

x = 22  
y = 7  
z = 14

Symbolic  
Execution

symbolic  
state

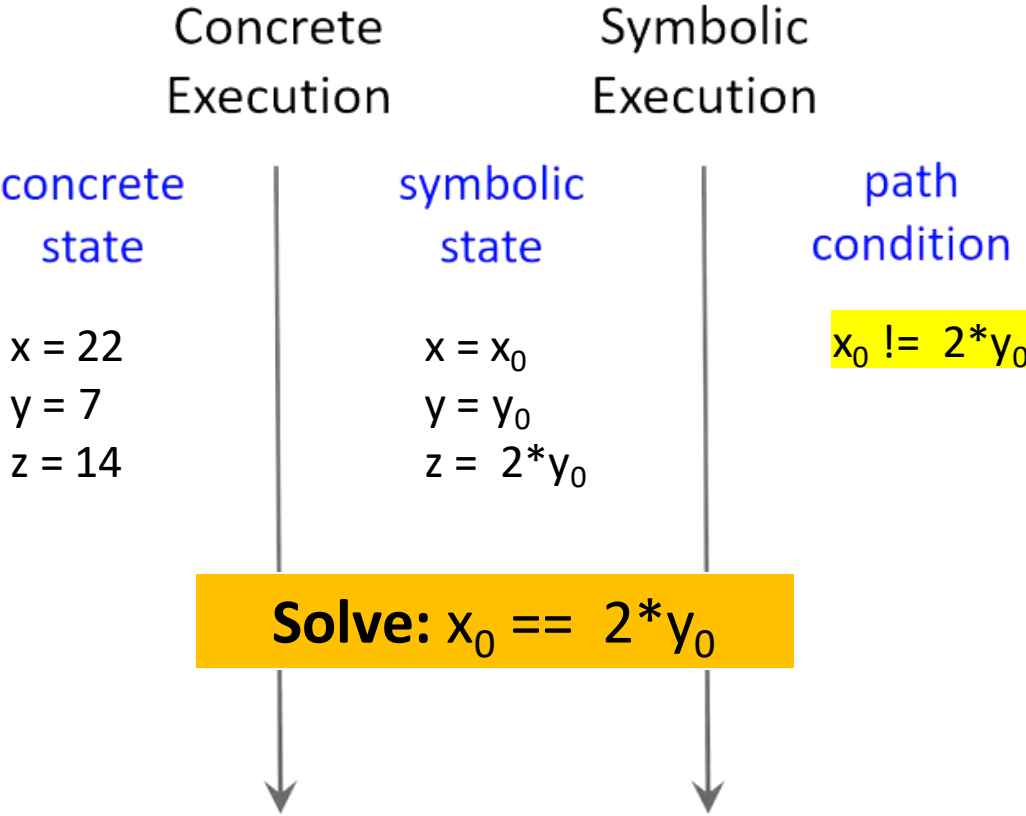
x = x<sub>0</sub>  
y = y<sub>0</sub>  
z = 2\*y<sub>0</sub>

path  
condition

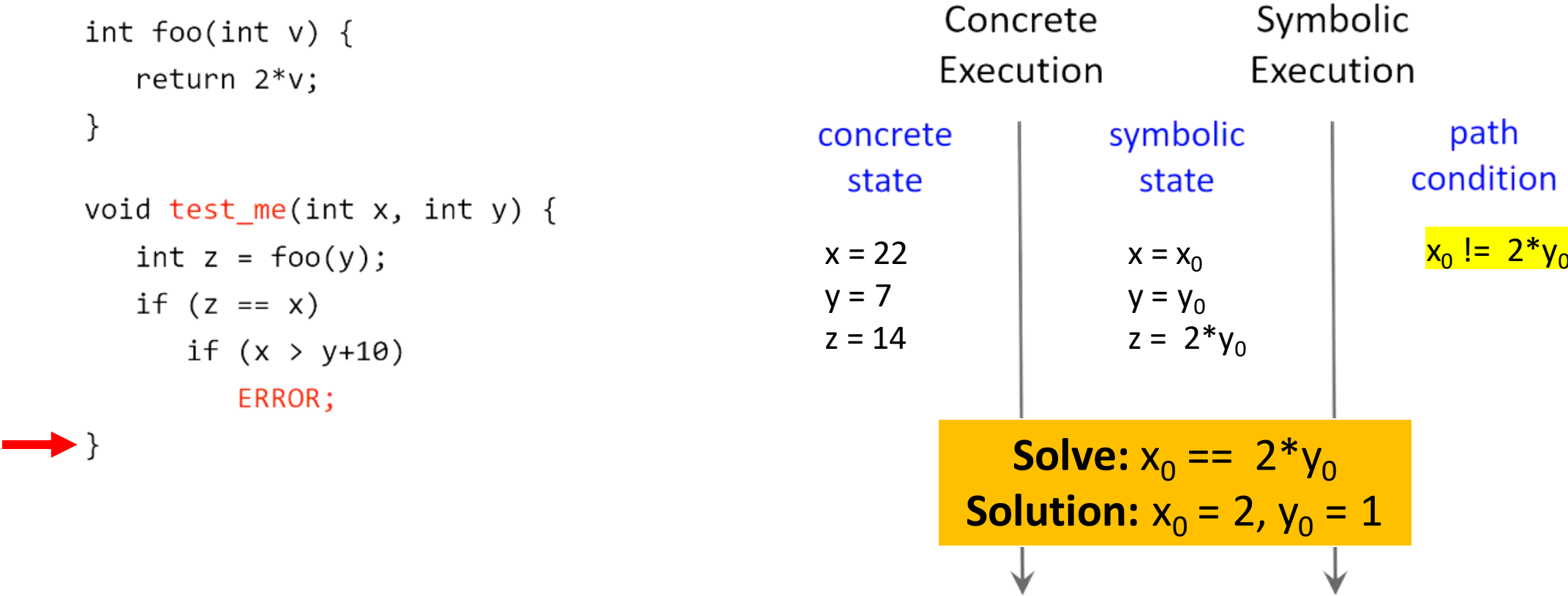
x<sub>0</sub> != 2\*y<sub>0</sub>

# DSE: An Illustrative Example

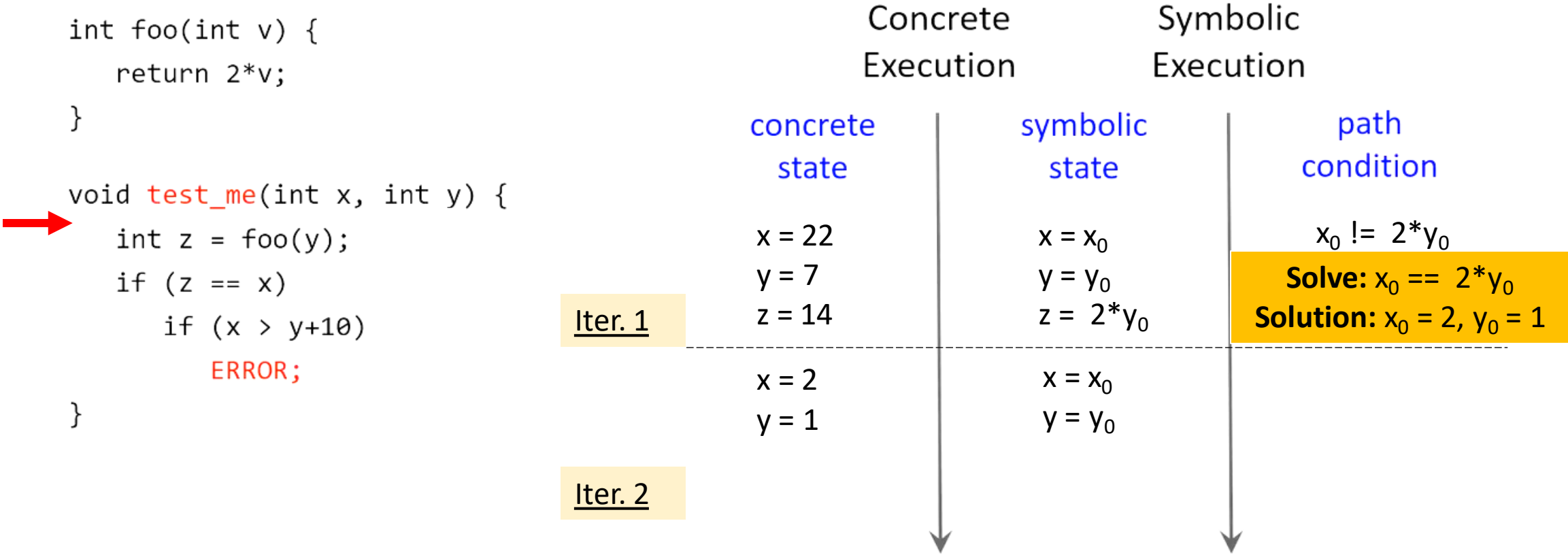
```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
→ }  
}
```



# DSE: An Illustrative Example

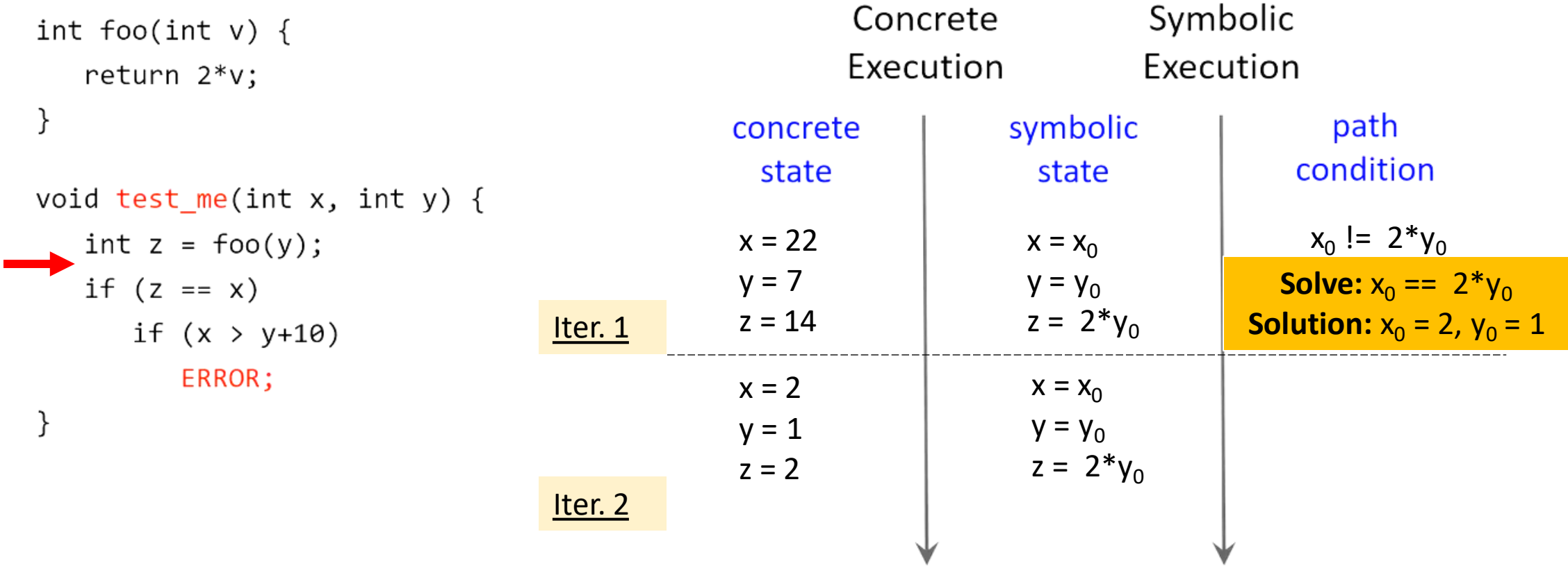


# DSE: An Illustrative Example

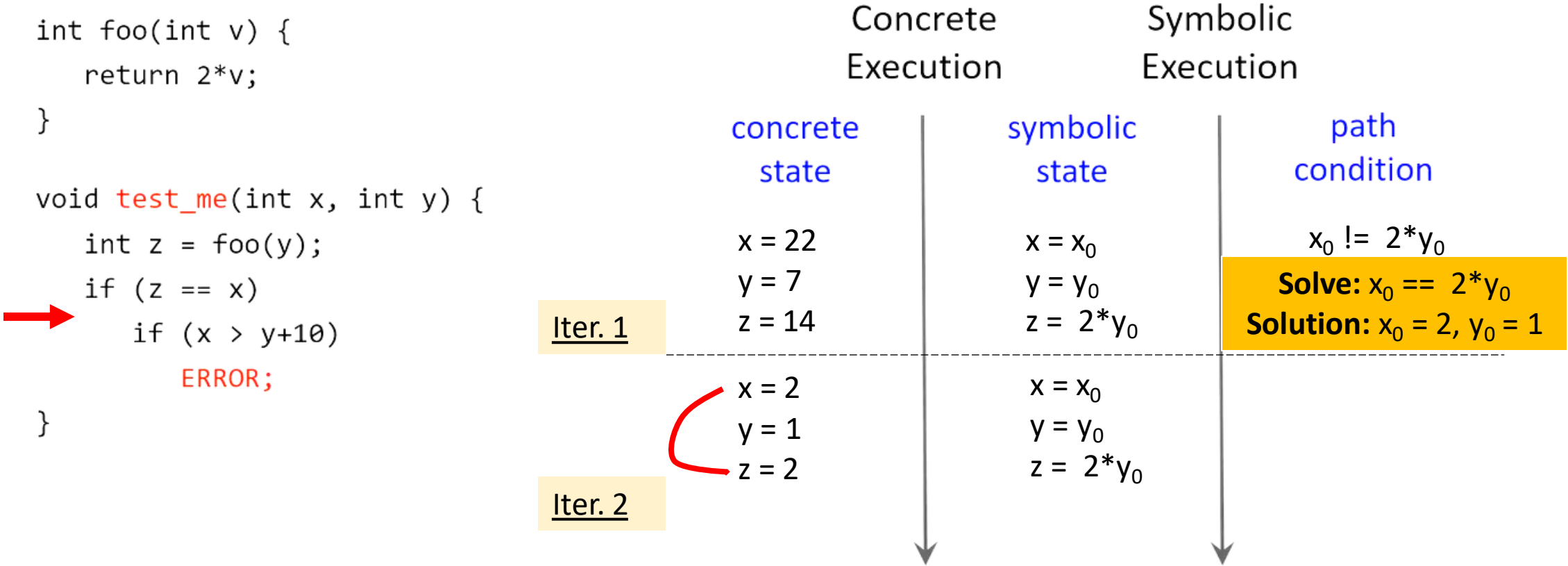




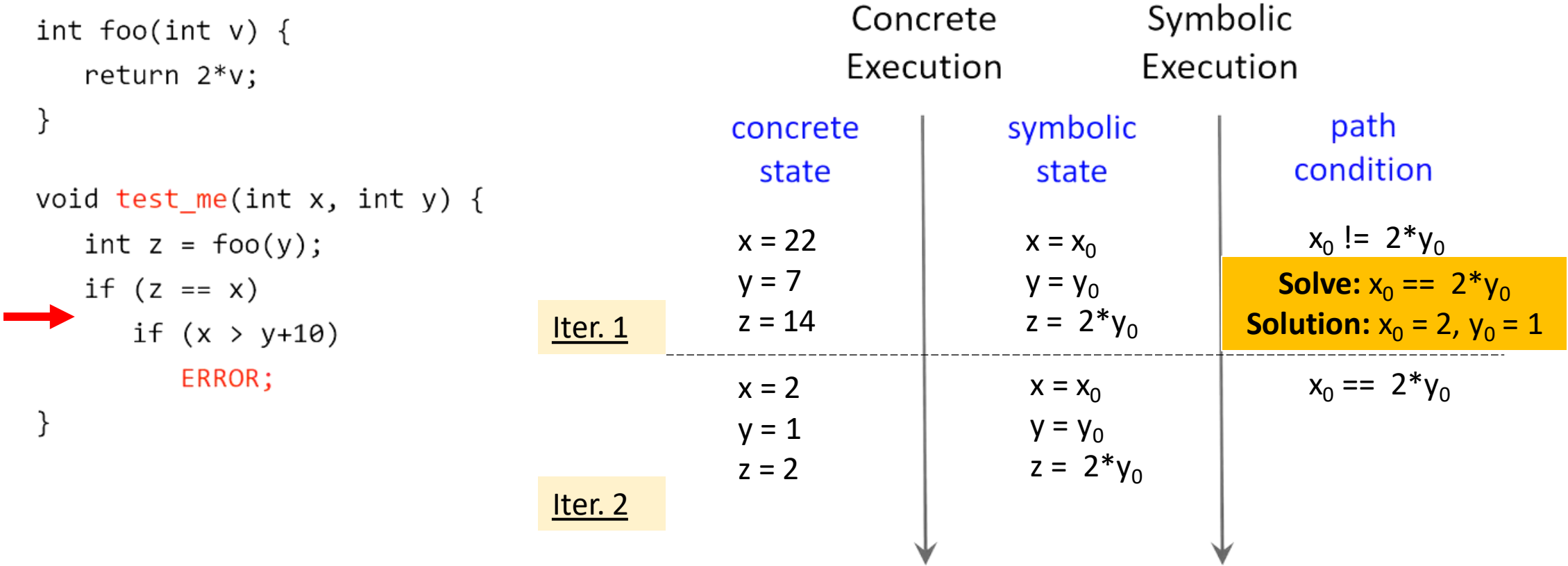
# DSE: An Illustrative Example



# DSE: An Illustrative Example



# DSE: An Illustrative Example



# DSE: An Illustrative Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
}
```




ERROR;

	Concrete Execution	Symbolic Execution	
	concrete state	symbolic state	path condition
Iter. 1	$x = 22$ $y = 7$ $z = 14$	$x = x_0$ $y = y_0$ $z = 2 * y_0$	$x_0 \neq 2 * y_0$ <b>Solve:</b> $x_0 == 2 * y_0$ <b>Solution:</b> $x_0 = 2, y_0 = 1$
Iter. 2	$x = 2$ $y = 1$ $z = 2$	$x = x_0$ $y = y_0$ $z = 2 * y_0$	$x_0 == 2 * y_0$

# DSE: An Illustrative Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
}
```



	Concrete Execution	Symbolic Execution	
	concrete state	symbolic state	path condition
Iter. 1	$x = 22$ $y = 7$ $z = 14$	$x = x_0$ $y = y_0$ $z = 2 * y_0$	$x_0 \neq 2 * y_0$ <b>Solve:</b> $x_0 == 2 * y_0$ <b>Solution:</b> $x_0 = 2, y_0 = 1$
Iter. 2	 $x = 2$ $y = 1$ $z = 2$	$x = x_0$ $y = y_0$ $z = 2 * y_0$	$x_0 == 2 * y_0$ $x_0 \leq y_0 + 10$

# DSE: An Illustrative Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
    }  
}
```



	Concrete Execution	Symbolic Execution	
	concrete state	symbolic state	path condition
Iter. 1	$x = 22$ $y = 7$ $z = 14$	$x = x_0$ $y = y_0$ $z = 2 * y_0$	$x_0 \neq 2 * y_0$ <b>Solve:</b> $x_0 == 2 * y_0$ <b>Solution:</b> $x_0 = 2, y_0 = 1$
Iter. 2	$x = 2$ $y = 1$ $z = 2$	$x = x_0$ $y = y_0$ $z = 2 * y_0$	$x_0 == 2 * y_0$ $x_0 \leq y_0 + 10$

# DSE: An Illustrative Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
    }  
}
```



	Concrete Execution		Symbolic Execution	
	concrete state		symbolic state	path condition
Iter. 1	x = 22 y = 7 z = 14		x = x <sub>0</sub> y = y <sub>0</sub> z = 2*y <sub>0</sub>	x <sub>0</sub> != 2*y <sub>0</sub> <b>Solve:</b> x <sub>0</sub> == 2*y <sub>0</sub> <b>Solution:</b> x <sub>0</sub> = 2, y <sub>0</sub> = 1
Iter. 2	x = 2 y = 1 z = 2		x = x <sub>0</sub> y = y <sub>0</sub> z = 2*y <sub>0</sub>	x <sub>0</sub> == 2*y <sub>0</sub> x <sub>0</sub> <= y <sub>0</sub> + 10 <b>Solve:</b> (x <sub>0</sub> == 2*y <sub>0</sub> ) ∧ (x <sub>0</sub> > y <sub>0</sub> + 10)

# DSE: An Illustrative Example

```
int foo(int v) {
    return 2*v;
}

void test_me(int x, int y) {
    int z = foo(y);
    if (z == x)
        if (x > y+10)
            ERROR;
    }
```



	Concrete Execution		Symbolic Execution	
	concrete state		symbolic state	path condition
Iter. 1	x = 22 y = 7 z = 14		x = x <sub>0</sub> y = y <sub>0</sub> z = 2*y <sub>0</sub>	x <sub>0</sub> != 2*y <sub>0</sub> <b>Solve:</b> x <sub>0</sub> == 2*y <sub>0</sub> <b>Solution:</b> x <sub>0</sub> = 2, y <sub>0</sub> = 1
Iter. 2	x = 2 y = 1 z = 2		x = x <sub>0</sub> y = y <sub>0</sub> z = 2*y <sub>0</sub>	x <sub>0</sub> == 2*y <sub>0</sub> x <sub>0</sub> <= y <sub>0</sub> + 10 <b>Solve:</b> (x <sub>0</sub> == 2*y <sub>0</sub> ) ∧ (x <sub>0</sub> > y <sub>0</sub> + 10) <b>Solution:</b> x <sub>0</sub> = 30, y <sub>0</sub> = 15



# DSE: An Illustrative Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
    }  
}
```



	Concrete Execution	Symbolic Execution	
	concrete state	symbolic state	path condition
Iter. 1	$x = 22$ $y = 7$ $z = 14$	$x = x_0$ $y = y_0$ $z = 2 * y_0$	$x_0 \neq 2 * y_0$ <b>Solve:</b> $x_0 == 2 * y_0$ <b>Solution:</b> $x_0 = 2, y_0 = 1$
Iter. 2	$x = 2$ $y = 1$ $z = 2$	$x = x_0$ $y = y_0$ $z = 2 * y_0$	$x_0 == 2 * y_0$ $x_0 \leq y_0 + 10$ <b>Solve:</b> $(x_0 == 2 * y_0) \wedge (x_0 > y_0 + 10)$ <b>Solution:</b> $x_0 = 30, y_0 = 15$

# DSE: An Illustrative Example

```
int foo(int v) {  
    return 2*v;  
}
```

```
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
}
```

Concrete  
Execution

Symbolic  
Execution

concrete  
state

symbolic  
state

path  
condition

x = 30  
y = 15

x = x<sub>0</sub>  
y = y<sub>0</sub>

Iter. 3

x = 2  
y = 1  
z = 2

x = x<sub>0</sub>  
y = y<sub>0</sub>  
z = 2\*y<sub>0</sub>

Iter. 2

x<sub>0</sub> == 2\*y<sub>0</sub>  
x<sub>0</sub> <= y<sub>0</sub> + 10

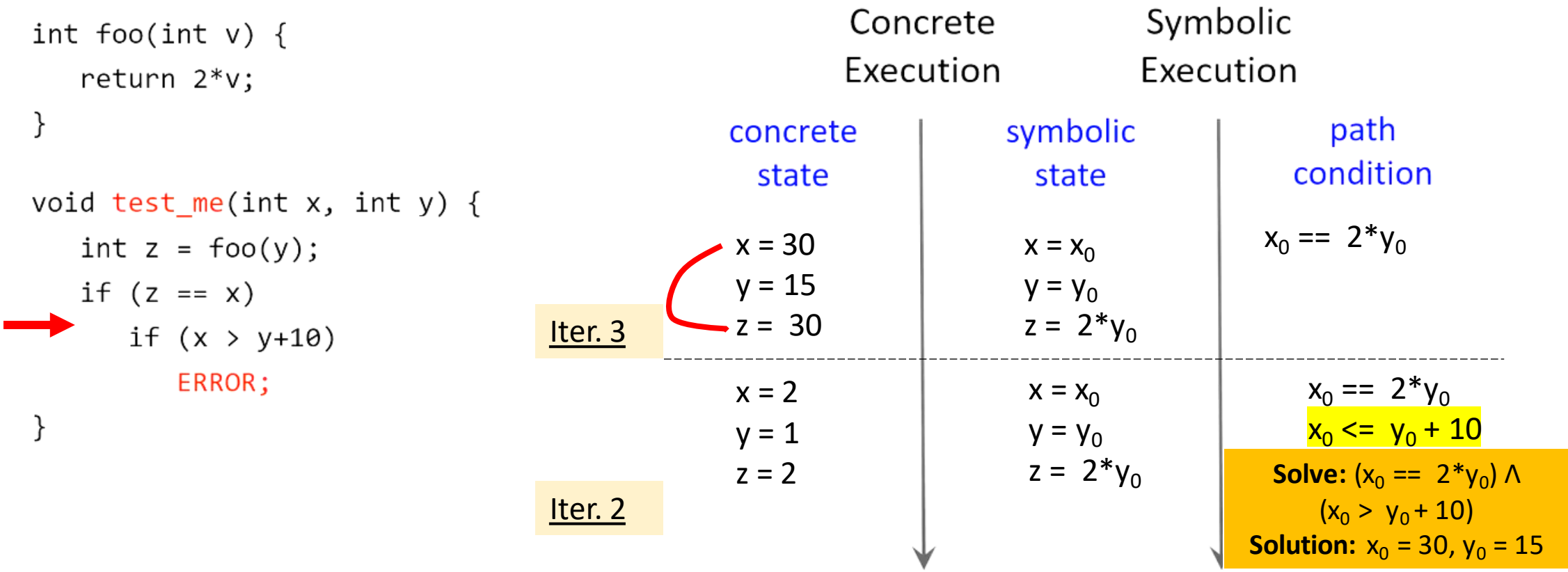
**Solve:** (x<sub>0</sub> == 2\*y<sub>0</sub>) ∧  
(x<sub>0</sub> > y<sub>0</sub> + 10)  
**Solution:** x<sub>0</sub> = 30, y<sub>0</sub> = 15

# DSE: An Illustrative Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
}
```


	Concrete Execution	Symbolic Execution	
	concrete state	symbolic state	path condition
Iter. 3	x = 30 y = 15 z = 30	x = x <sub>0</sub> y = y <sub>0</sub> z = 2*y <sub>0</sub>	
Iter. 2	x = 2 y = 1 z = 2	x = x <sub>0</sub> y = y <sub>0</sub> z = 2*y <sub>0</sub>	<div><math>x_0 == 2*y_0</math> <math>x_0 \leq y_0 + 10</math> Solve: <math>(x_0 == 2*y_0) \wedge (x_0 &gt; y_0 + 10)</math> Solution: <math>x_0 = 30, y_0 = 15</math></div>

# DSE: An Illustrative Example



# DSE: An Illustrative Example


```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
}
```

	Concrete Execution	Symbolic Execution	
	concrete state	symbolic state	path condition
	<div>x = 30 y = 15 z = 30</div>	<div>x = x<sub>0</sub> y = y<sub>0</sub> z = 2*y<sub>0</sub></div>	<div>x<sub>0</sub> == 2*y<sub>0</sub></div>
Iter. 3			
	<div>x = 2 y = 1 z = 2</div>	<div>x = x<sub>0</sub> y = y<sub>0</sub> z = 2*y<sub>0</sub></div>	<div>x<sub>0</sub> == 2*y<sub>0</sub> x<sub>0</sub> &lt;= y<sub>0</sub> + 10</div>
Iter. 2			<div>Solve: (x<sub>0</sub> == 2*y<sub>0</sub>) ∧ (x<sub>0</sub> &gt; y<sub>0</sub> + 10) Solution: x<sub>0</sub> = 30, y<sub>0</sub> = 15</div>

# DSE: An Illustrative Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
}
```



	Concrete Execution	Symbolic Execution	
	concrete state	symbolic state	path condition
	<div>x = 30 y = 15 z = 30</div>	<div>x = x<sub>0</sub> y = y<sub>0</sub> z = 2*y<sub>0</sub></div>	<div>x<sub>0</sub> == 2*y<sub>0</sub> x<sub>0</sub> &gt; y<sub>0</sub> + 10</div>
Iter. 3			
	<div>x = 2 y = 1 z = 2</div>	<div>x = x<sub>0</sub> y = y<sub>0</sub> z = 2*y<sub>0</sub></div>	<div>x<sub>0</sub> == 2*y<sub>0</sub> x<sub>0</sub> &lt;= y<sub>0</sub> + 10</div>
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# DSE Algorithm

## Repeat until all paths are covered

- **Execute** program with concrete input  $i$  and collect **symbolic constraints** at branch points:  $C$
- **Negate one constraint** to force taking an alternative branch  $b'$ :  
Constraint  $C'$
- Call constraint solver to **find solution** for  $C'$ : **new concrete input**  $i'$
- **Execute** program with input  $i'$  to take branch  $b'$
- Check at runtime that  $b'$  is indeed taken otherwise:  
“**divergent execution**”

# Divergent Execution Example

```
function f(a){
  if (Math.random() < 0.5){
    if (a > 1) {
      console.log
    }
  }
}
```

Concrete  
Execution

concrete  
state

$a = 0$

Symbolic  
Execution

symbolic  
state

$a = a_0$

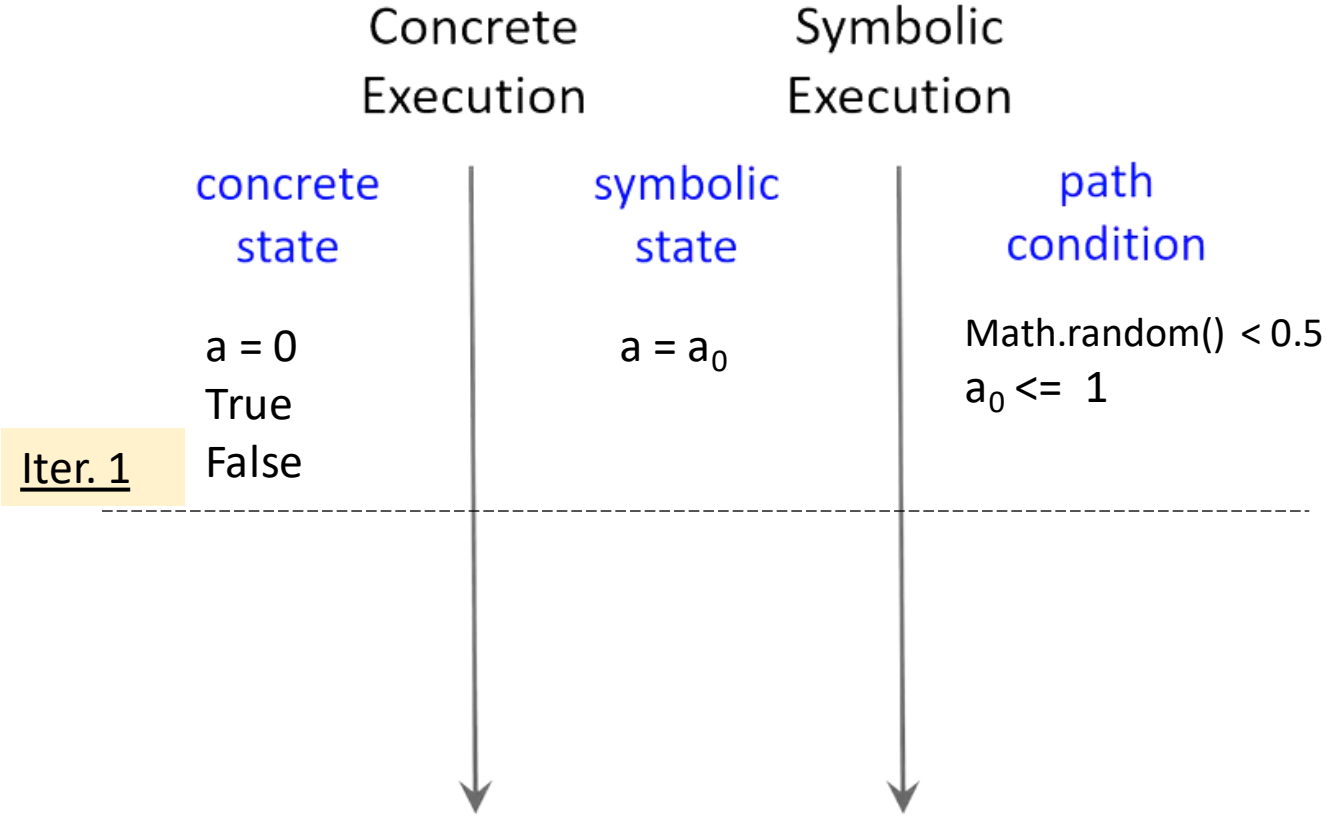
path  
condition





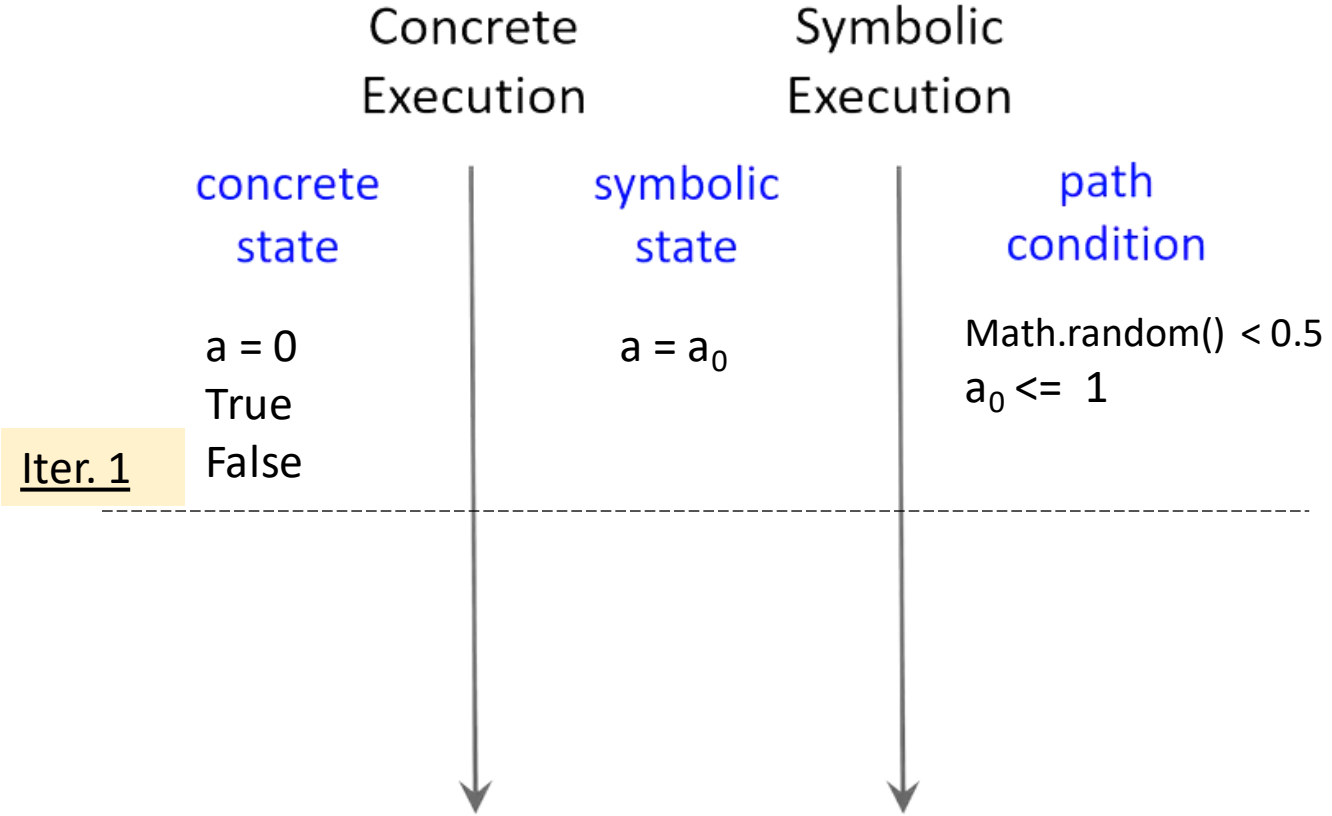

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    }  
  }  
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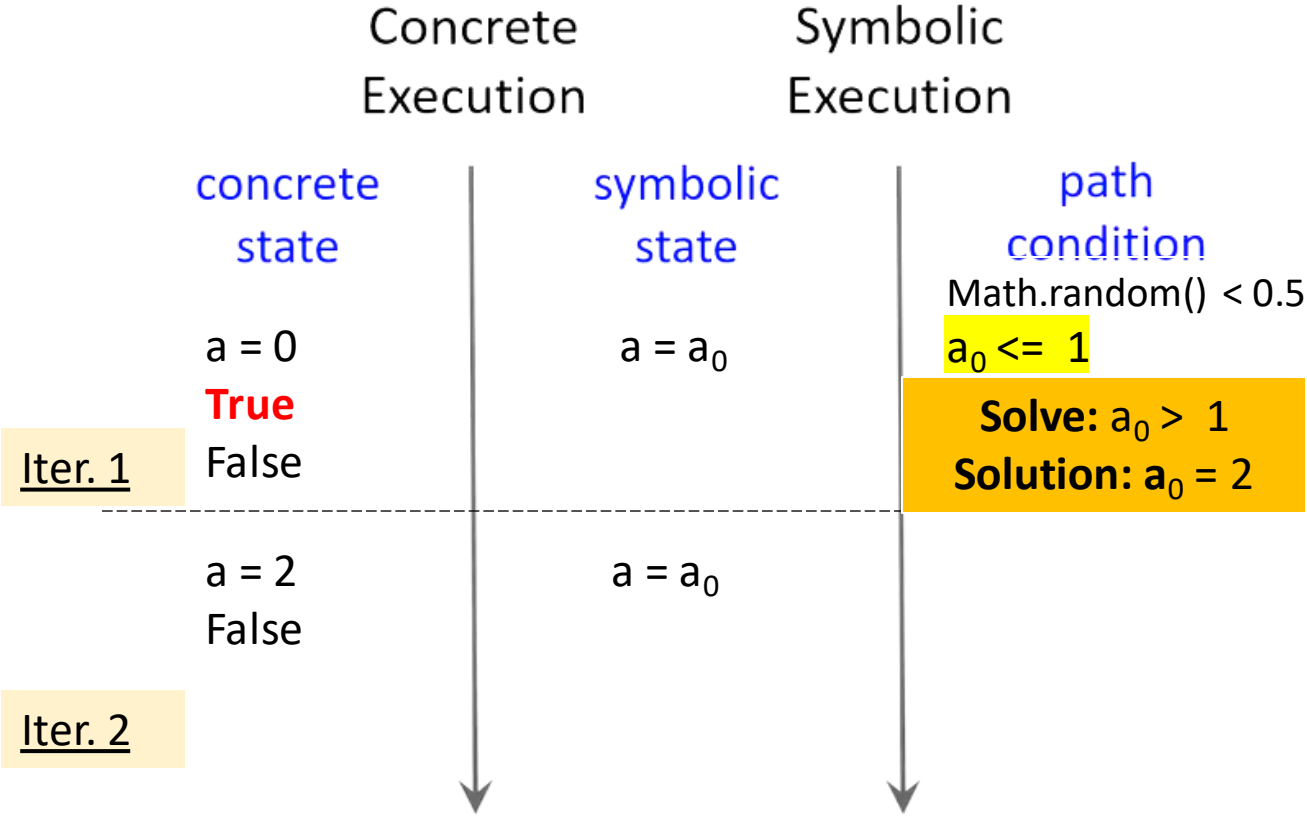
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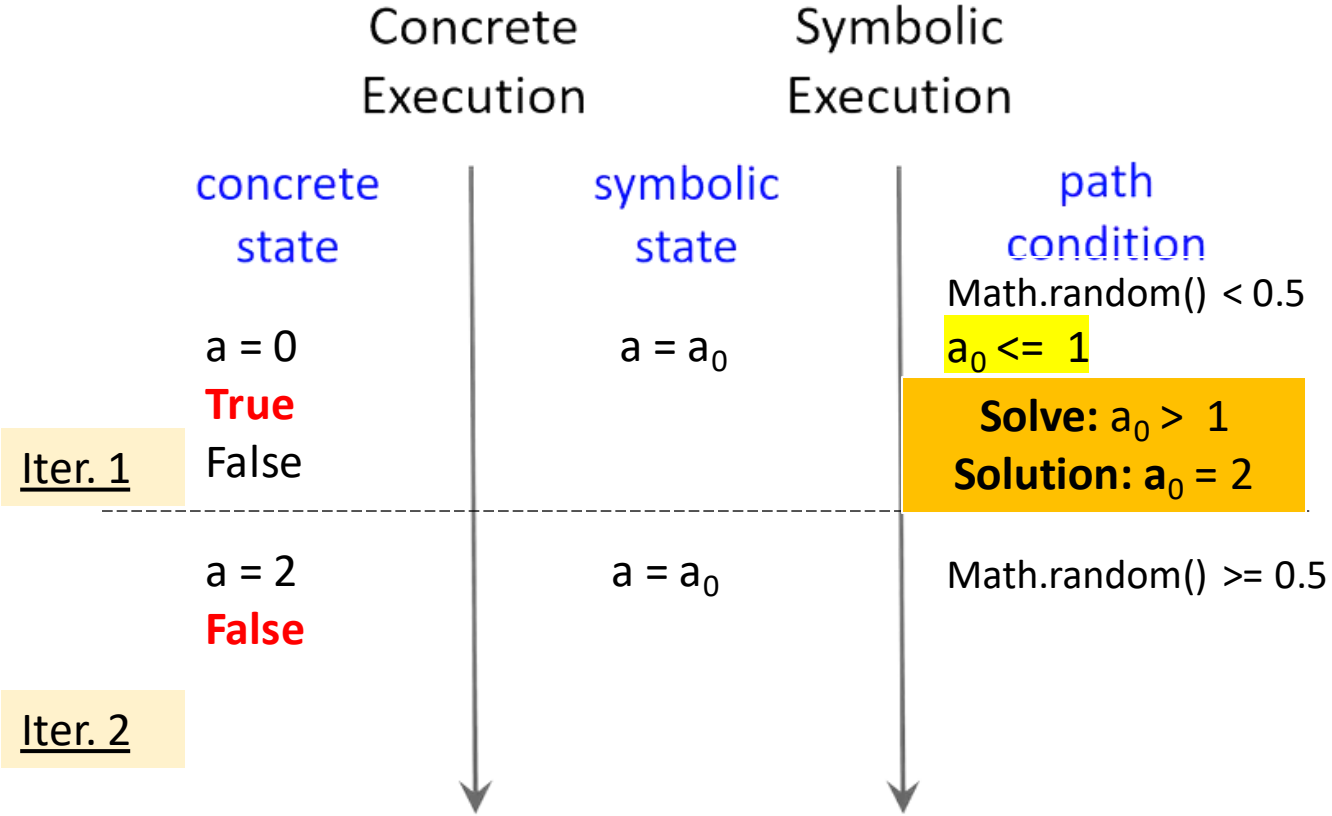
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# Divergent Execution Example

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    }  
  }  
}
```



# Benefits of Concolic Approach

**When symbolic reasoning is impossible or impractical, fall back to concrete values**

- Native/system API functions
- Operations not handled by solvers (e.g., floating point operations)

# Implementations of Concolic Approach

- **KLEE**: LLVM (C family of languages – C, C++, Objective C, and Objective C++)
- **PEX**: .NET framework
- **jCUTE**: Java programs
- **Jalangi**: JavaScript programs
- **SAGE** and **S2E**: binaries (x86, ARM, ...)

# Implementations of Concolic Approach

**SAGE**: binaries (x86, ARM, ...)

- Scalable Automated Guided Execution – developed at MSR
- Used by multiple product teams at Microsoft, run daily on cloud
- Found many security bugs in various Microsoft applications (MS Windows, MS Office, Media player, Bing, etc.)
- What makes it so useful?
  - **Works on large applications** => find bugs in multiple components
  - **Focuses on input file fuzzing** => makes it fully automated
  - **Works on binaries** => easy to deploy (does not depend on programming language or build process)

# QUIZ (1/2): Properties of DSE

Assume that programs can have infinite execution trees. Which of the following statements are true of DSE applied to such programs?

1. DSE is guaranteed to terminate
2. DSE is complete: if it ever found an error, the program can trigger that error in some concrete execution
3. DSE is sound: if it terminates and did not find an error, the program, cannot trigger an error in any concrete execution



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# QUIZ (2/2): Properties of DSE

1. The testing approach of DSE is:  
(a) Automated, black-box    (b) Automated, white-box  
(c) Manual, black-box        (d) Manual, white-box
  
2. The input search of DSE is:  
(a) Randomized                (b) Systematic
  
3. The static analysis of DSE is:  
(a) Flow-insensitive            (b) Flow-sensitive            (c) Path-sensitive

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# Test Generation: The Bigger Picture

Why didn't automatic test generation become popular decades ago?

- Weak-type systems
  - Test generation relies heavily on **type information**
  - **C, Lisp** just didn't provide the needed types
- Contemporary languages lend themselves better to test generation
  - **Java, UML**
- Lack of computational power required (e.g., modern NLP techniques, SMT solvers)

# What Have We Learned?

- Automatic test generation is a good idea
  - **Key:** avoid generating **illegal** and **redundant** tests and cover more parts of the program
  - Performs better for generating **unit tests** in **strongly-typed languages**
- Generating test oracles is harder than generating test inputs
- Being adopted in industry
  - Likely to become widespread in the future

# Announcements

- **Project Plan Presentation**

**Due next Wednesday, 02/14/2024 before class time**

- Describe **exactly** what you have decided to do in project

- **Paper Presentation**

**Starts in 1.5 weeks, Monday, 02/19/2024**

- Groups presenting papers 1 and 3 should get feedback from me next week Wednesday during my office hours
- In general, each group should get feedback on their presentation during my office hours in the week before you present.