

CS 569

Selected Topics in Software Engineering:  
Program Analysis & Evaluation

# **Automated Test Generation**

Oregon State University, Winter 2024

# The Problem

- There are **infinitely** many tests
  - Which finite subset should we choose?
- And even **finite** subsets can be huge
- Need a subset which is:
  - **Concise**: avoids illegal and redundant tests
  - **Diverse**: gives good coverage

# Outline

- Previously: **Random Testing (Fuzzing)**
  - Security, mobile apps, concurrency
- **Feedback-directed random testing: Randoop**
  - Classes and libraries
- **Systematic testing: Korat**
  - Linked data structures
- **Test generation using natural language specification: Swami**
  - JavaScript compilers

# Key Idea

- Using **specifications** to guide test generation
  - Types
  - Invariants
  - Pre- and Post-Conditions
  - Natural language specifications

# Example: Using Types

```
void remove(BinaryTree bt, Node n) {  
    ... // remove node n from binary tree bt  
}
```

```
class BinaryTree {  
    Node root;  
    class Node {  
        Node left;  
        Node right;  
    }  
}
```

Helps to avoid testing the **remove** method on arbitrary byte inputs

# Example: Using Invariants

- Root may be null
- If Root is not null:
  - No cycles
  - Each node (except Root) must have one parent
  - Root has no parent

```
class BinaryTree {  
    Node root;  
    class Node {  
        Node left;  
        Node right;  
    }  
}
```

# Example: Using Invariants

```
public boolean repOK(BinaryTree bt) {  
    if (bt.root == null) return true;  
    Set visited = new HashSet();  
    List workList = new LinkedList();  
    visited.add(bt.root);  
    workList.add(bt.root);  
    while (!workList.isEmpty()) {  
        Node current = workList.removeFirst();  
        if (current.left != null) {  
            if (!visited.add(current.left)) return false;  
            workList.add(current.left);  
        }  
        ... // similarly for current.right  
    }  
    return true;  
}
```

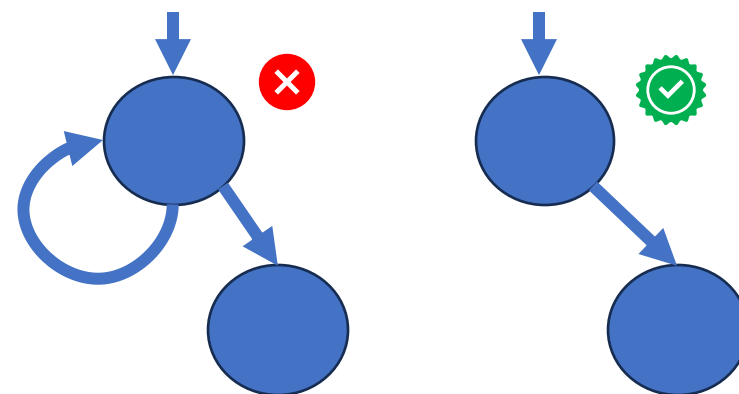
```
class BinaryTree {  
    Node root;  
    class Node {  
        Node left;  
        Node right;  
    }  
}
```

Checks if a binary tree object is valid (satisfies invariant)

# Example: Using Invariants

```
public boolean repOK(BinaryTree bt) {  
    if (bt.root == null) return true;  
    Set visited = new HashSet();  
    List workList = new LinkedList();  
    visited.add(bt.root);  
    workList.add(bt.root);  
    while (!workList.isEmpty()) {  
        Node current = workList.removeFirst();  
        if (current.left != null) {  
            if (!visited.add(current.left)) return false;  
            workList.add(current.left);  
        }  
        ... // similarly for current.right  
    }  
    return true;  
}
```

```
class BinaryTree {  
    Node root;  
    class Node {  
        Node left;  
        Node right;  
    }  
}
```





# Example: Using Invariants

```
@invariant repOk(bt)
```

```
void remove(BinaryTree bt, Node n) {  
    ... // remove node n from binary tree bt  
}
```

```
class BinaryTree {  
    Node root;  
    class Node {  
        Node left;  
        Node right;  
    }  
}
```

- Helps to avoid testing the **remove** method on tree structures that do not satisfy invariant
- Also serves as a contract to check that resultant tree at the end of **remove** method is valid binary tree

# Example: Using Pre- and Post-Conditions

```
@invariant repOk(bt)
@requires contains(bt, n) // pre condition
@ensures !contains(bt, n) // post condition

void remove(BinaryTree bt, Node n) {
    ... // remove node n from binary tree bt
}
```

```
class BinaryTree {
    Node root;
    class Node {
        Node left;
        Node right;
    }
}
```

- Helps to test even richer program execution states on entry and exit of **remove** method

# Example: Using Natural Language Specifications

## 15.4.2.2 new Array (len)

The `[[Prototype]]` internal property of the newly constructed object is set to the original Array prototype object, the one that is the initial value of `Array.prototype` (15.4.3.1). The `[[Class]]` internal property of the newly constructed object is set to "Array". The `[[Extensible]]` internal property of the newly constructed object is set to `true`.

If the argument `len` is a Number and `ToUint32(len)` is equal to `len`, then the `length` property of the newly constructed object is set to `ToUint32(len)`. If the argument `len` is a Number and `ToUint32(len)` is not equal to `len`, a `RangeError` exception is thrown.

If the argument `len` is not a Number, then the `length` property of the newly constructed object is set to 1 and the 0 property of the newly constructed object is set to `len` with attributes `[[Writable]]: true`, `[[Enumerable]]: true`, `[[Configurable]]: true`.

Describes how Array constructor should be implemented in JavaScript compiler

```
function test_array_len( len ){
    if ( ToUint32(len) != len ) {
        try{
            var output = new Array ( len );
            return;
        } catch(e) {
            assert.strictEqual(true, (e instanceof RangeError));
            return;
        }
    }
}

/*TEST INPUTS*/

test_array_len(1.1825863363010669e+308);
test_array_len(null);
test_array_len(-747);
test_array_len(368);
```

Test oracle

Test inputs

# Randoop: Feedback-Directed Random Testing

- Random test generation for object-oriented programs (Java, C#)
- Generates unit tests for methods of Java classes
- Motivating examples of generated tests

```
Set s = new HashSet();  
s.add("hi");  
assertTrue(s.equals(s));
```

Tests generated for  
Java HashSet class  
provided in Java Util  
library

```
Set s = new HashSet();  
s.add("hi");  
s.isEmpty();  
assertTrue(s.equals(s));
```

Only  
difference =>  
**redundant  
test**

# Motivating Examples

- Three randomly generated tests for Date class:

```
Date d = new Date(2006, 2, 14);  
assertTrue(d.equals(d));
```

```
Date d = new Date(2006, 2, 14);  
d.setMonth(-1);  
assertTrue(d.equals(d));
```

```
Date d = new Date(2006, 2, 14);  
d.setMonth(-1);  
d.setDay(5);  
assertTrue(d.equals(d));
```

Violates pre-  
condition

# Motivating Examples

- Three randomly generated tests for Date class:

```
Date d = new Date(2006, 2, 14);  
assertTrue(d.equals(d));
```

```
Date d = new Date(2006, 2, 14);  
d.setMonth(-1);  
assertTrue(d.equals(d));
```

```
Date d = new Date(2006, 2, 14);  
d.setMonth(-1);  
d.setDay(5);  
assertTrue(d.equals(d));
```



**Illegal tests**

# Randoop: Feedback-Directed Random Testing

## IDEA

- **Guide** randomized **creation** of new test inputs by **feedback** about **execution** of previous inputs
  - Avoid **redundant** inputs
  - Avoid **illegal** inputs
- Test input = **sequence of method calls**
- Software under test: Classes in Java-like programming languages

# Randoop: Feedback-Directed Random Testing

## EXAMPLE (from Randoop paper that exposed bug in Java Utils library)

No contracts  
are violated in  
all method calls

```
HashMap h = new HashMap();  
Collection c = h.values();  
Object[] a = c.toArray();  
LinkedList l = new LinkedList();  
l.addFirst(a);  
TreeSet t = new TreeSet(l);  
Set u = Collections.unmodifiableSet(t);  
assertTrue(u.equals(u));
```

Fails because of  
bug in JDK  
implementation



# Randoop: Feedback-Directed Random Testing

## APPROACH

- Build test inputs **incrementally**
  - New test inputs extend previous ones
- As soon as test input is created, **execute it**
- Use execution results to guide input generation
  - **Away from redundant or illegal** method sequences
  - **Toward** sequences that create **new object states**

# Randoop: Feedback-Directed Random Testing

## ALGORITHM

- Input:
  - Classes under test
  - Time limit
  - Set of contracts
    - Method contracts, e.g., `o.hashCode()` throws no exception
    - Class invariants, e.g., `o.equals(o) == true`
- Output:
  - Test cases with assertions

# Randoop: Feedback-Directed Random Testing

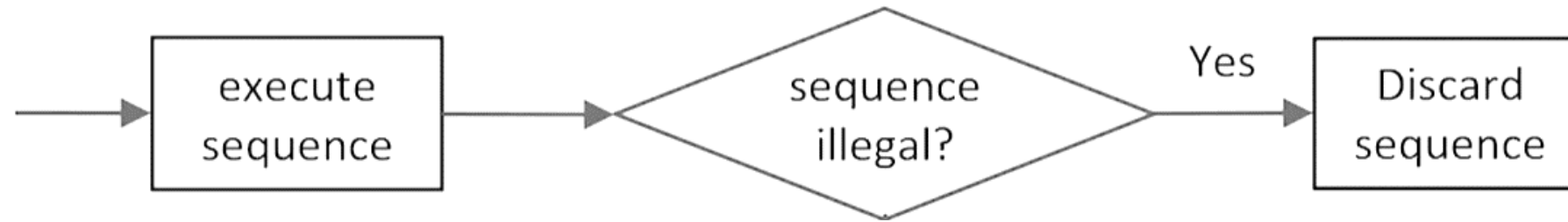
## ALGORITHM

- Initialize **seed components**:  $\text{int } i=0$ ; Boolean  $b=false$ ; ...
- Do until time expires:
  1. **Randomly pick a method to test**  
 $C.m(T_1, \dots, T_k)/T_{ret}$ , where  $C$  = class under test,  $m$  = method under test,  $(T_1, \dots, T_k)$  = method arguments' types, and  $T_{ret}$  = method return type
  2. For each argument of type  $T_i$ , randomly pick a sequence  $S_i$  from the components that **constructs a value  $v_i$  of type  $T_i$**
  3. Create **new sequence**  
 $S_{new} = S_1; \dots; S_k; T_{ret} \quad v_{new} = C.m(v_1, \dots, v_k)$
  4. If  $S_{new}$  was previously created (lexically), go to **step 1**
  5. **Else classify the sequence  $S_{new}$** 
    - May discard, output as test case, or add to components

New method call  
added to previously  
created sequence

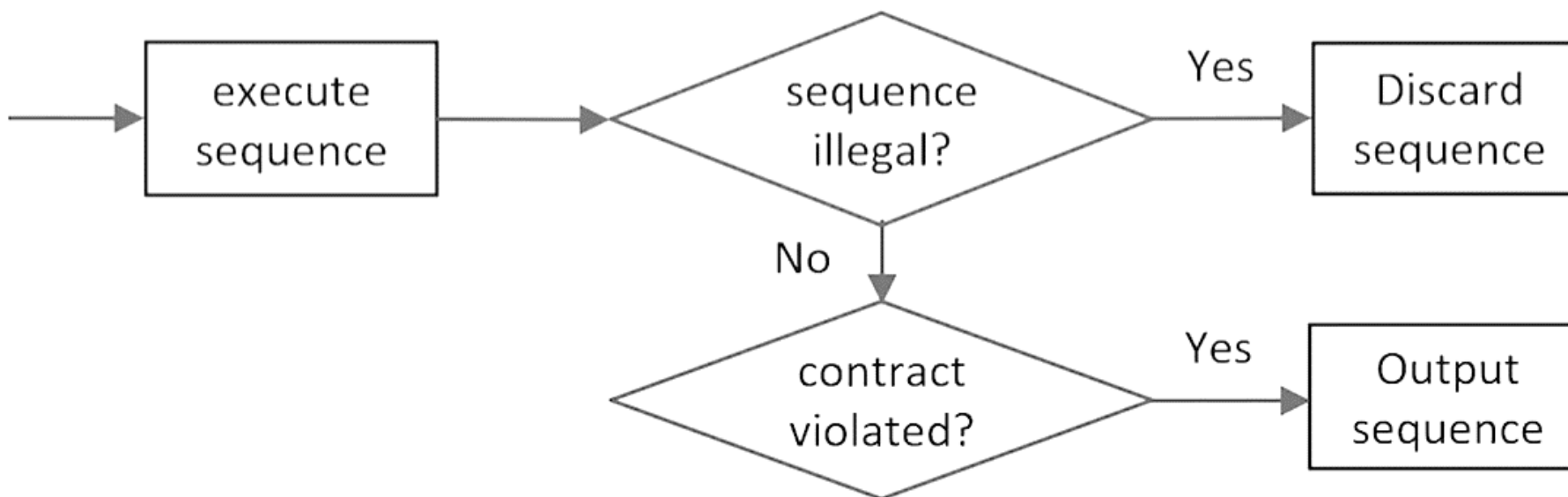
# Randoop: Feedback-Directed Random Testing

## Classify the sequence



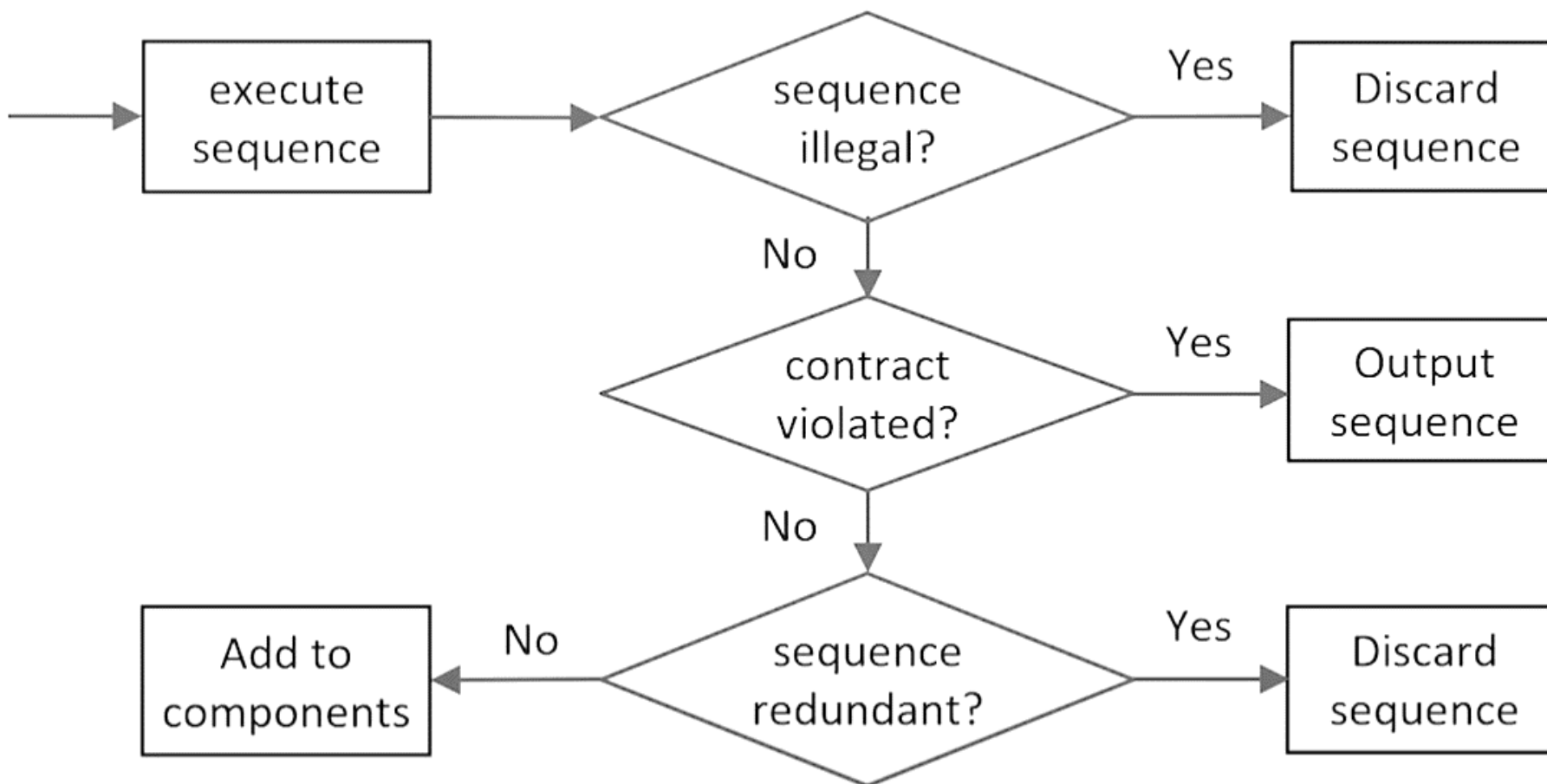
# Randoop: Feedback-Directed Random Testing

## Classify the sequence



# Randoop: Feedback-Directed Random Testing

## Classify the sequence



# Randoop: Feedback-Directed Random Testing

## How to detect Redundant Sequences?

- During sequence-generation and execution, maintain a **set of all objects created**
- **Sequence** is **redundant** if all objects created during its execution are in the maintained set
- Use `equals()` to compare objects for efficiency reasons.
- Could also use more sophisticated state equivalence methods that are more computationally expensive
  - E.g., heap canonicalization

# Some Errors Found by Randoop

- **JDK containers** have 4 methods that violate reflexivity property of `o.equals(o)` contract
- **Javax.xml** creates objects that cause `hashCode` and `toString` to crash, even though objects are well-formed XML constructs
- **Apache libraries** have constructors that leave fields unset, leading to NPE on calls of `equals`, `hashCode`, and `toString`
- **.Net framework** has at least 175 methods that throw an exception forbidden by the library specification (NPE, out-of-bounds, or illegal state exception)
- **.Net framework** has 8 methods that violate `o.equals(o)` contract



# QUIZ(1/2): Randoop Test Generation

Write the smallest sequence that Randoop can possibly generate to create a valid BinaryTree.

Once generated, how does Randoop classify it?

- ☐ Discards it as illegal
- ☐ Outputs it as a bug
- ☐ Adds to components for future extension

```
class BinaryTree {
    Node root;
    public BinaryTree(Node r) {
        root = r;
        assert(repOk(this));
    }
    public Node removeRoot() {
        assert(root != null);
        ...
    }
}
```

```
class Node {
    Node left;
    Node right;
    public Node(Node l, Node r) {
        left = l; right = r;
    }
}
```

# QUIZ(1/2): Randoop Test Generation

Write the smallest sequence that Randoop can possibly generate to create a valid BinaryTree.

```
Node n = null;
BinaryTree t = new BinaryTree(n);
```

Once generated, how does Randoop classify it?

- ☐ Discards it as illegal
- ☐ Outputs it as a bug
- ☒ Adds to components for future extension

```
class BinaryTree {
    Node root;
    public BinaryTree(Node r) {
        root = r;
        assert(repOk(this));
    }
    public Node removeRoot() {
        assert(root != null);
        ...
    }
}
```

```
class Node {
    Node left;
    Node right;
    public Node(Node l, Node r) {
        left = l; right = r;
    }
}
```

# QUIZ(2/2): Randoop Test Generation

Write the smallest sequence that Randoop can possibly generate that violates the assertion in `removeRoot()`.

```
class BinaryTree {
    Node root;
    public BinaryTree(Node r) {
        root = r;
        assert(repOk(this));
    }
    public Node removeRoot() {
        assert(root != null);
        ...
    }
}
```

Once generated, how does Randoop classify it?

- ☐ Discards it as illegal
- ☐ Outputs it as a bug
- ☐ Adds to components for future extension

```
class Node {
    Node left;
    Node right;
    public Node(Node l, Node r) {
        left = l; right = r;
    }
}
```

# QUIZ(2/2): Randoop Test Generation

Write the smallest sequence that Randoop can possibly generate that violates the assertion in `removeRoot()`.

```
Node n = null;
BinaryTree t = new BinaryTree(n);
t.removeRoot();
```

Once generated, how does Randoop classify it?

- ☒ Discards it as illegal
- ☐ Outputs it as a bug
- ☐ Adds to components for future extension

```
class BinaryTree {
    Node root;
    public BinaryTree(Node r) {
        root = r;
        assert(repOk(this));
    }
    public Node removeRoot() {
        assert(root != null);
        ...
    }
}
```

```
class Node {
    Node left;
    Node right;
    public Node(Node l, Node r) {
        left = l; right = r;
    }
}
```

# Korat

- Deterministic test-generation approach suitable for linked data-structures
- Idea
  - Use **pre-conditions** and **post-conditions** to generate tests automatically
- How?

# An Insight

- Often can do a good job by systematically testing **all inputs up to a small size**
- **Small Test Case Hypothesis:**
  - If there is any test that causes the program to fail, there is a small such test
- If a list function works for the lists of length 0 through 3, probably it will work for all list sizes
  - E.g., because the function is oblivious to length (recall bug depth for concurrency bugs – Cuzz)

# How Do We Generate All Test Inputs?

- Use the **types**
  - White-box testing
- The class declaration shows what values (or null) can fill each field
- Simply enumerate all possible shapes with a fixed set of **Nodes**

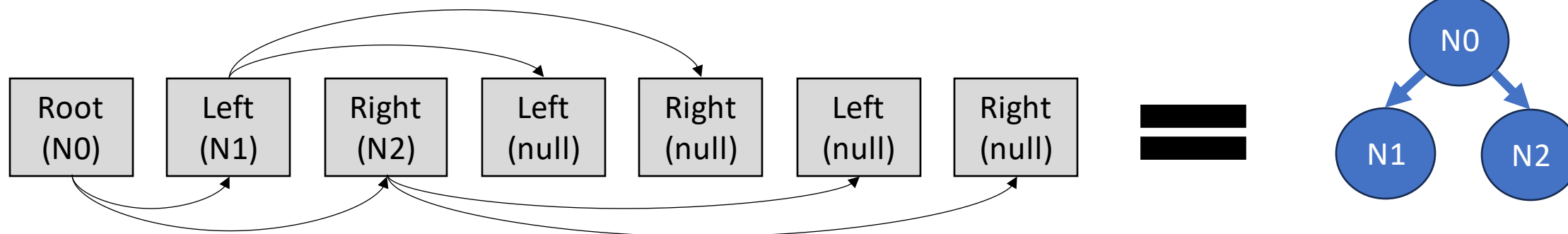
```
class BinaryTree {  
    Node root;  
    class Node {  
        Node left;  
        Node right;  
    }  
}
```

# Scheme for Representing Shapes

- Order all possible values of each field assigning each order a unique ID
- Order all fields into a vector
- Each shape == vector of field values

**Example:** BinaryTree of up to 3 Nodes:

```
class BinaryTree {
    Node root;
    class Node {
        Node left;
        Node right;
    }
}
```



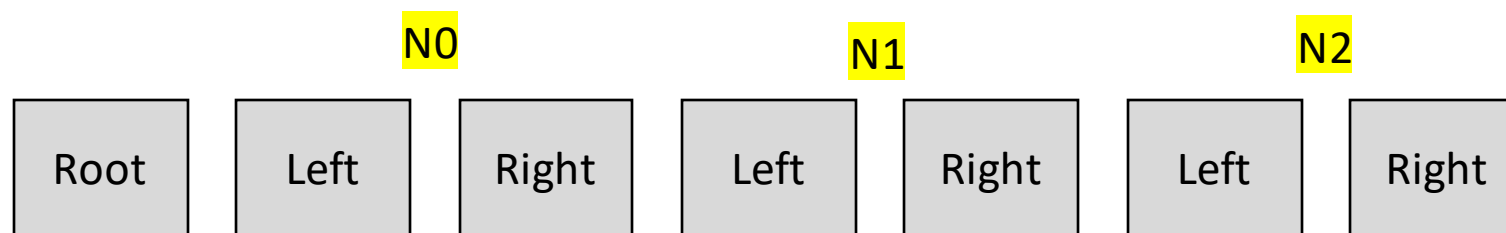


# Scheme for Representing Shapes

- Order all possible values of each field assigning each order a unique ID
- Order all fields into a vector
- Each shape == vector of field values

**Example:** BinaryTree of up to 3 Nodes:

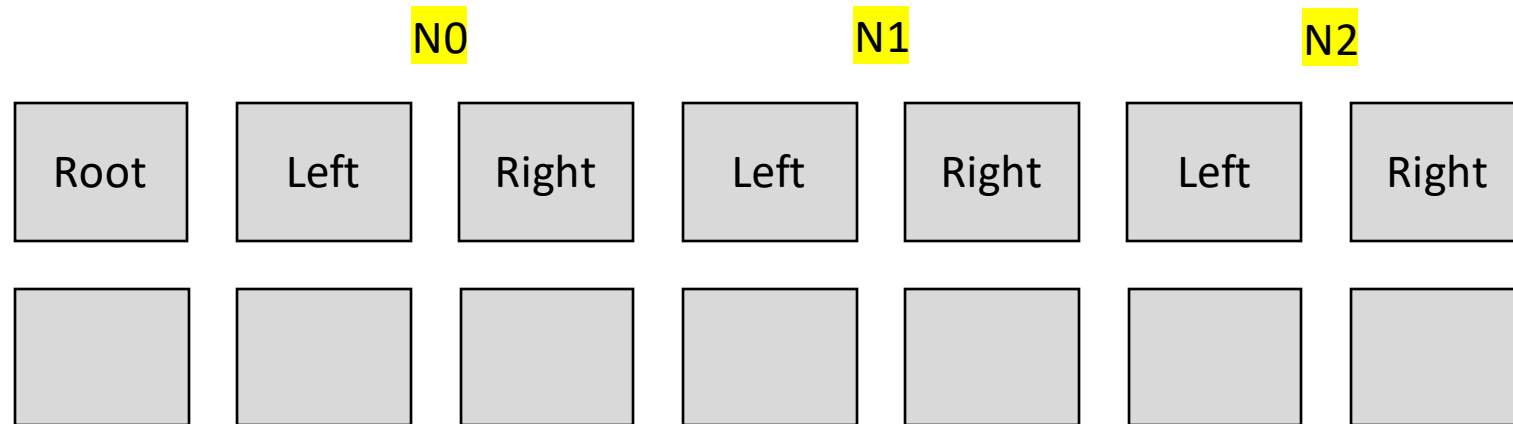
```
class BinaryTree {
    Node root;
    class Node {
        Node left;
        Node right;
    }
}
```



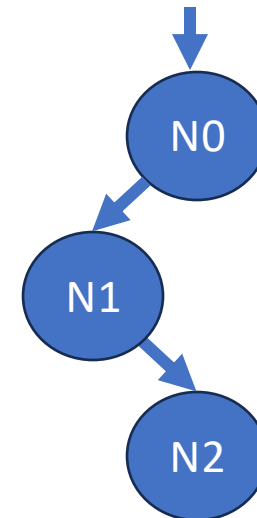
Each box can be assigned null, N0, N1, or N2

# QUIZ: Representing Shapes

- Fill in the values in the box to represent the depicted shape:

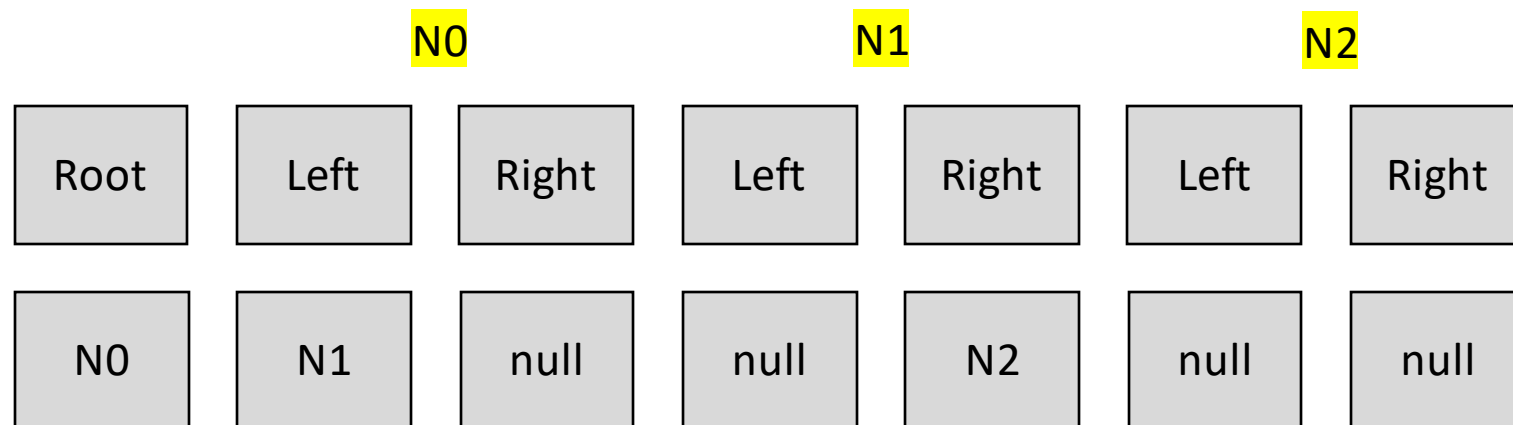


Each box can be assigned null, N0, N1, or N2

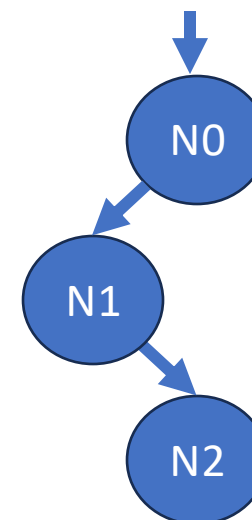


# QUIZ: Representing Shapes

- Fill in the values in the box to represent the depicted shape:



Each box can be assigned null, N0, N1, or N2

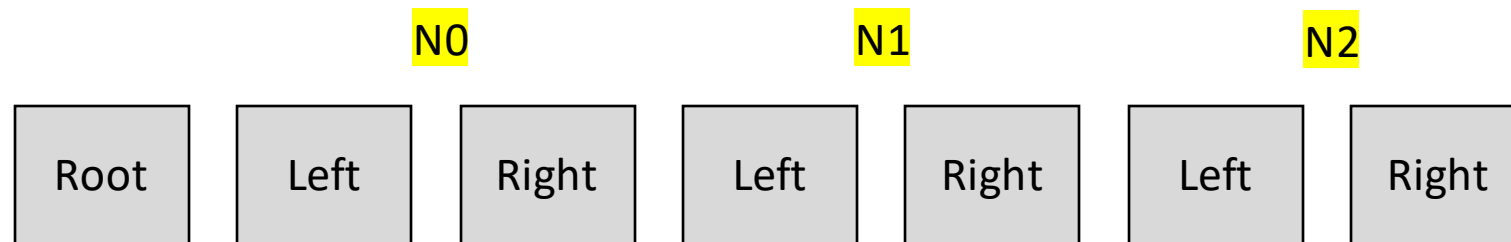


# A Simple Algorithm

- User selects some maximum input size **k**
- Generate all possible inputs up to size **k**
- Discard inputs where **pre-condition** is false
  - E.g., calling `removeRoot()` method on empty `BinaryTree`
- Run program on remaining inputs
- Check results using **post-condition**

# Enumerating Shapes

- Korat represents each input shape as a vector of the following form:

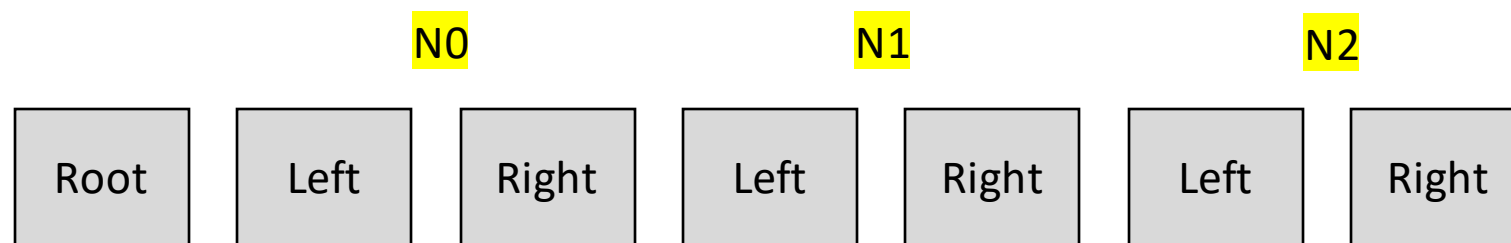


Each box can be assigned null, N0, N1, or N2

- What is the total number of vectors of the above form?

# Enumerating Shapes

- Korat represents each input shape as a vector of the following form:



Each box can be assigned null, N0, N1, or N2

- What is the total number of vectors of the above form?

$$4^7 = 16,384$$

Size of the state space of generating binary trees of up to 3 nodes

# The General Case for Binary Trees

- How many binary trees shapes can be enumerated using  $\leq k$  nodes?
- Calculation:
  - A BinaryTree object bt
  - $k$  Node objects,  $N_0, N_1, \dots$
  - $2k+1$  Node pointers
    - Root (for bt)
    - left, right (for each Node object)
  - $k+1$  possible values ( $N_0, N_1, \dots, N_k$ , or null) per pointer
- $(k+1)^{(2k+1)}$  possible “binary trees”

# A Lot of “Binary Trees”!

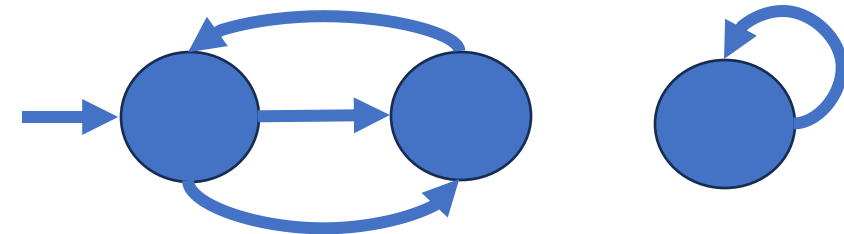
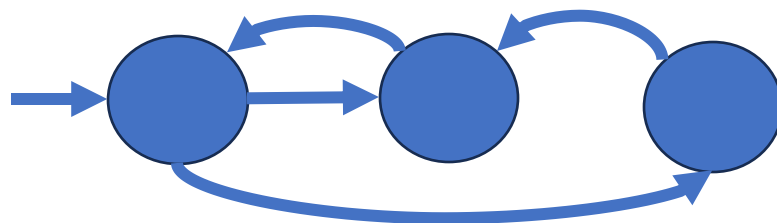
- The number of trees grows exponentially in input size  $((k+1)^{(2k+1)})$ 
  - $k = 3$ : over 16,000 trees
  - $k = 4$ : over 1,900,000 trees
  - $k = 5$ : over 360,000,000 trees
- Limits us to testing only very small input sizes
- Can we do better?



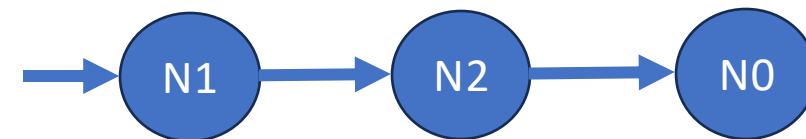
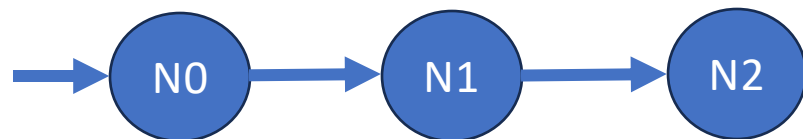
# An Overestimate

- $(k+1)^{(2k+1)}$  is gross overestimate!

- Many of the shapes are not even trees:

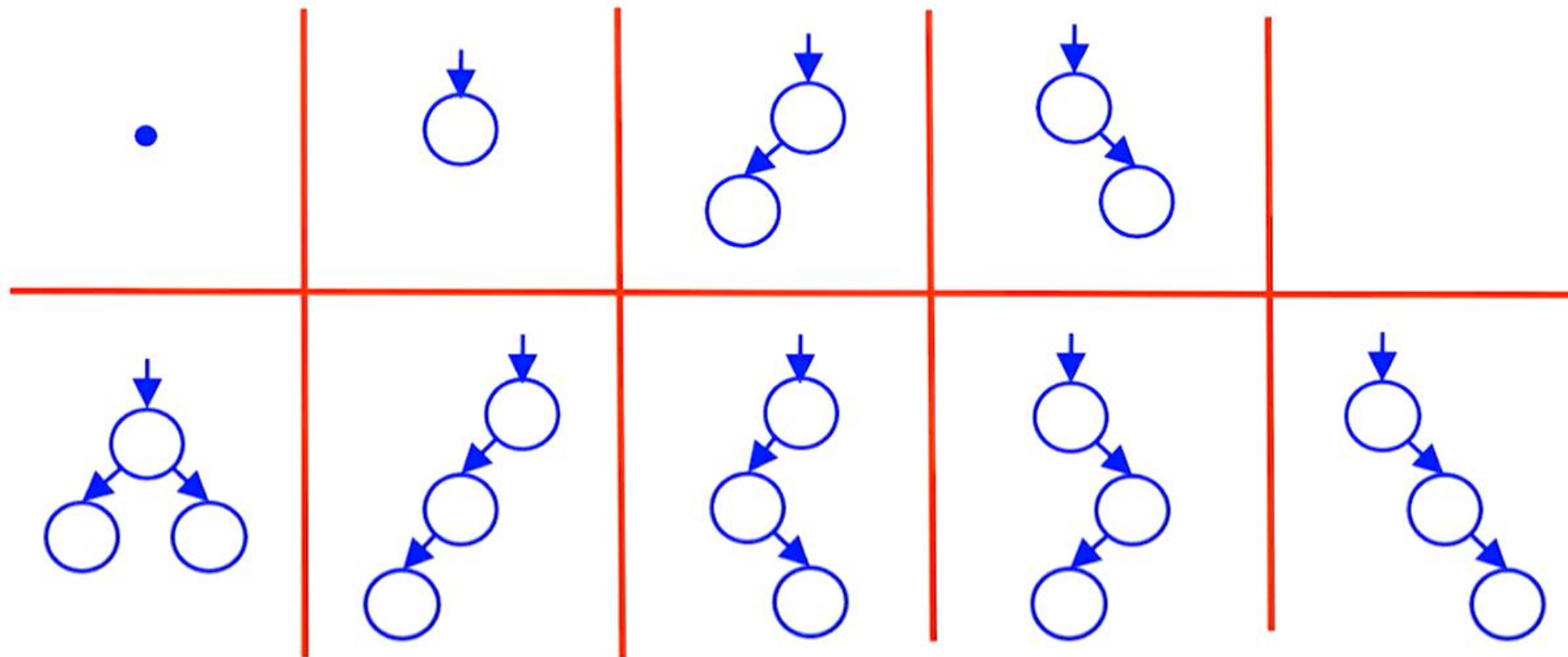


- Many of the trees are isomorphic (indistinguishable for the purpose of testing):



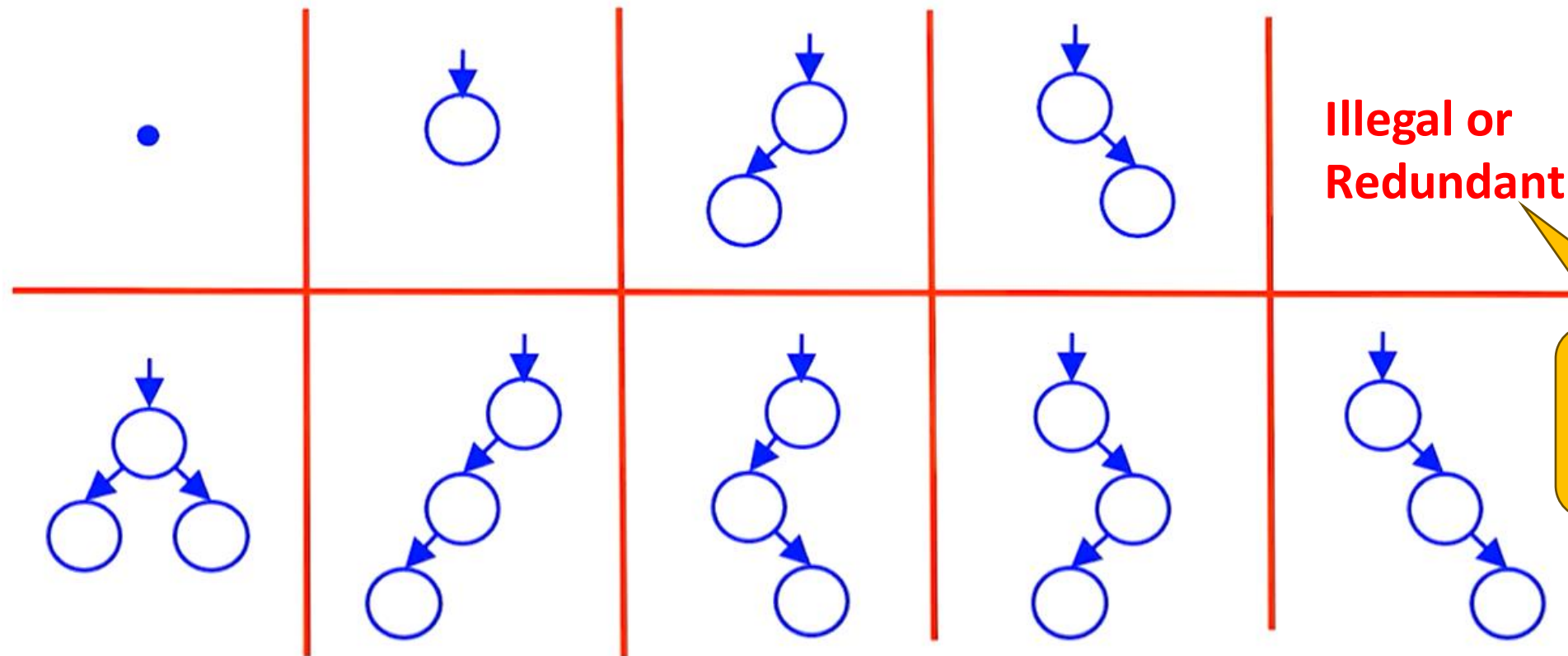
# How Many Trees?

- There are only 9 distinct binary trees with at most 3 nodes:



# How Many Trees?

- There are only 9 distinct binary trees with at most 3 nodes:



Challenges:  
How to  
avoid?

# Another Insight

- Avoid generating inputs that do not satisfy the **invariant**
- Use the **invariant** to guide the generation of tests

# Korat – The Technique

- Instrument the **invariant**
  - Add code to record which fields of the input are accessed by the **invariant**
- **Observation:**
  - If the invariant doesn't access a field, then it doesn't depend on that field

# The Invariant for Binary Trees

- Root may be null
- If Root is not null:
  - No cycles
  - Each node (except Root) must have one parent
  - Root has no parent

```
class BinaryTree {  
    Node root;  
    class Node {  
        Node left;  
        Node right;  
    }  
}
```

# The Invariant for Binary Trees

```
public boolean repOK(BinaryTree bt) {  
    if (bt.root == null) return true;  
    Set visited = new HashSet();  
    List workList = new LinkedList();  
    visited.add(bt.root);  
    workList.add(bt.root);  
    while (!workList.isEmpty()) {  
        Node current = workList.removeFirst();  
        if (current.left != null) {  
            if (!visited.add(current.left)) return false;  
            workList.add(current.left);  
        }  
        ... // similarly for current.right  
    }  
    return true;  
}
```

```
class BinaryTree {  
    Node root;  
    class Node {  
        Node left;  
        Node right;  
    }  
}
```

Returns true when  
binary tree object  
satisfies the invariant

# The Invariant for Binary Trees

```
public boolean repOK(BinaryTree bt) {  
    if (bt.root == null) return true;  
    Set visited = new HashSet();  
    List workList = new LinkedList();  
    visited.add(bt.root);  
    workList.add(bt.root);  
    while (!workList.isEmpty()) {  
        Node current = workList.removeFirst();  
        if (current.left != null) {  
            if (!visited.add(current.left)) return false;  
            workList.add(current.left);  
        }  
        ... // similarly for current.right  
    }  
    return true;  
}
```

```
class BinaryTree {  
    Node root;  
    class Node {  
        Node left;  
        Node right;  
    }  
}
```

How is this method  
traversing the tree?  
BFS or DFS?



# The Invariant for Binary Trees

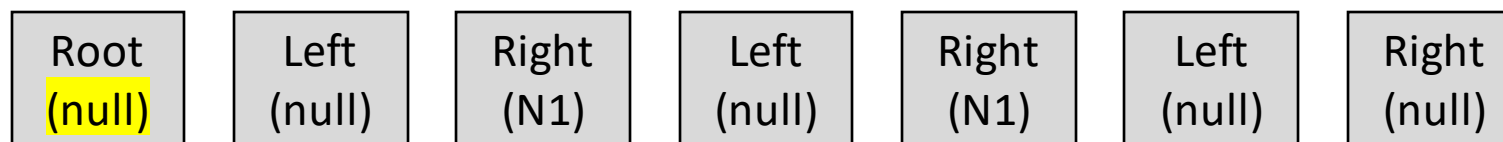
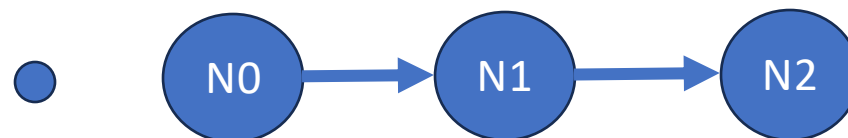
```
public boolean repOK(BinaryTree bt) {  
    if (bt.root == null) return true;  
    Set visited = new HashSet();  
    List workList = new LinkedList();  
    visited.add(bt.root);  
    workList.add(bt.root);  
    while (!workList.isEmpty()) {  
        Node current = workList.removeFirst();  
        if (current.left != null) {  
            if (!visited.add(current.left)) return false;  
            workList.add(current.left);  
        }  
        ... // similarly for current.right  
    }  
    return true;  
}
```

```
class BinaryTree {  
    Node root;  
    class Node {  
        Node left;  
        Node right;  
    }  
}
```

How is this method  
traversing the tree?  
BFS or DFS?

# Example: Using the Invariant

- Consider the following tree:

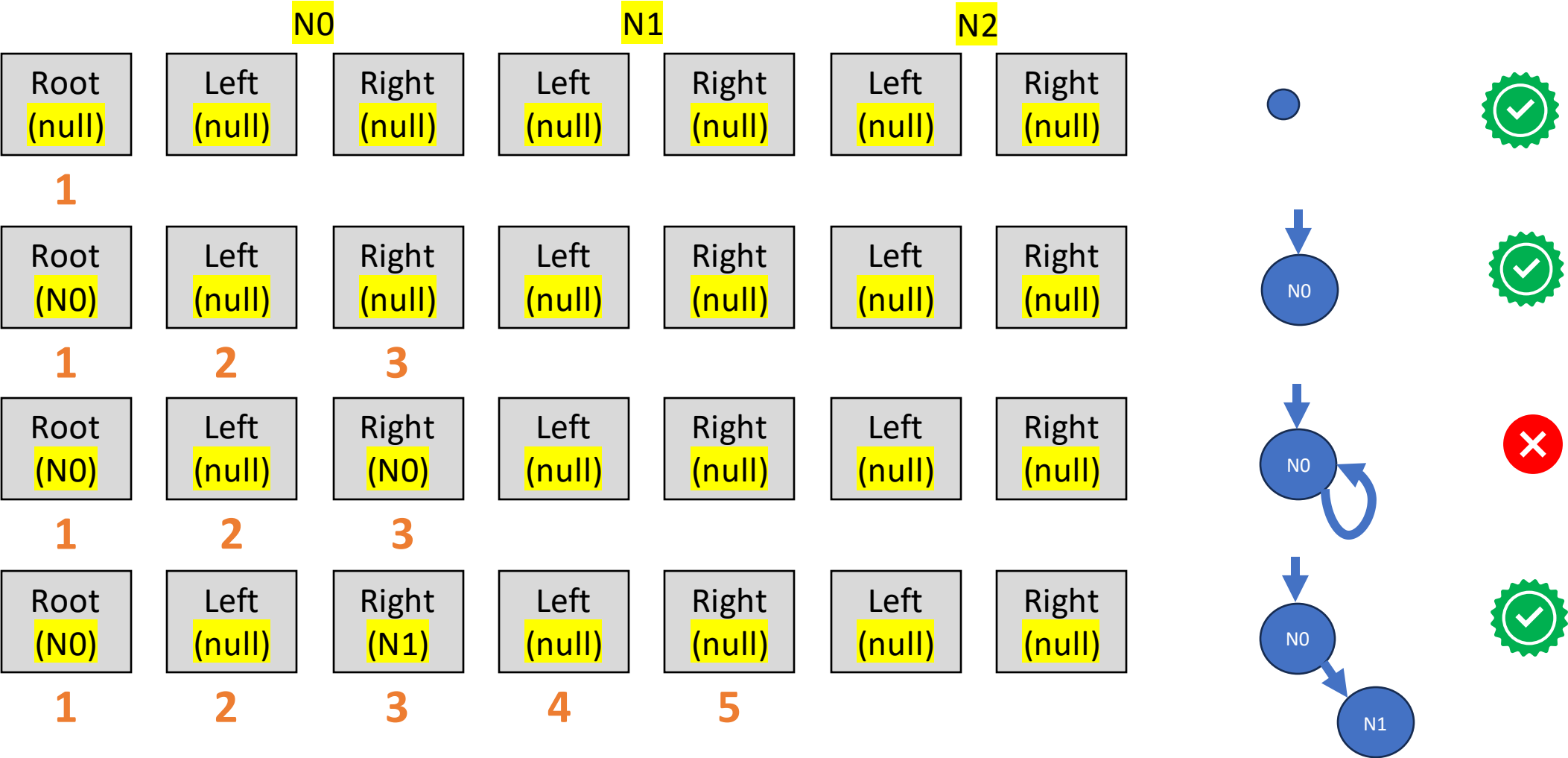


- The **invariant (repOK)** accesses **only the root** as it is **null**
  - Every possible shape for nodes other than root will yield the same result
  - This single input eliminates 25% of the tests!

# Korat Approach

- Shapes are enumerated according to their associated vectors
  - Initial candidate vector: all fields null
  - Next shape generated by:
    - Expanding last field accessed in invariant
    - Backtracking if all possibilities for a field are exhausted
- Key idea: Never expand fields not examined by invariant
- Also: cleverly check and discard shapes isomorphic to previously generated shapes

# Example: Enumerating Binary Trees



# Experimental Results

benchmark	size	time (sec)	structures generated	candidates considered	state space
BinaryTree	8	1.53	1430	54418	$2^{53}$
	9	3.97	4862	210444	$2^{63}$
	10	14.41	16796	815100	$2^{72}$
	11	56.21	58786	3162018	$2^{82}$
	12	233.59	208012	12284830	$2^{92}$
HeapArray	6	1.21	13139	64533	$2^{20}$
	7	5.21	117562	519968	$2^{25}$
	8	42.61	1005075	5231385	$2^{29}$
LinkedList	8	1.32	4140	5455	$2^{91}$
	9	3.58	21147	26635	$2^{105}$
	10	16.73	115975	142646	$2^{120}$
	11	101.75	678570	821255	$2^{135}$
	12	690.00	4213597	5034894	$2^{150}$
TreeMap	7	8.81	35	256763	$2^{92}$
	8	90.93	64	2479398	$2^{111}$
	9	2148.50	122	50209400	$2^{130}$

# Korat: Strengths and Weaknesses

- Strong when we can enumerate all possibilities
  - E.g., Four nodes, two edge per node
  - Good for:
    - **Linked data structures**
    - Small easily specified procedures
    - Unit testing
- Weaker when
  - Enumeration is weak
    - Integers, Floating-point numbers, Strings.
  - Only good as pre- and post-conditions
    - **is\_member(x, list)** vs **!is\_empty(list)** pre-condition for remove() method of List
    - **!contains(x, list')** vs **is\_list(list')** post-condition for remove() method of List

# Announcements

- **Project Plan Presentation and Report assignment** released  
Due **next Wednesday, 02/14/2024**
  - Describe **exactly** what you have decided to do in project
- **Homework-2** released  
Due **in two weeks, 02/19/2024**
- **Class Participation**
  - Involve in project and paper presentations by asking/answering questions on Canvas (see Class Participation assignment)