

POKHARA UNIVERSITY

Level: Bachelor
 Programme: BE
 Course: Probability and Statistics

Semester: Spring

Year : 2017
 Full Marks: 100
 Pass Marks: 45
 Time : 3hrs.

Candidates are required to give their answers in their own words as far as practicable.

The figures in the margin indicate full marks.

Attempt all the questions.

1. a) Over a period of 40 days the percentage relative humidity in a vegetable storage building was measured. Mean daily values were recorded as shown below: 7

60	63	64	71	67	73	79	80	83	81
86	90	96	98	98	99	89	80	77	78
71	79	74	84	85	82	90	78	79	79
78	80	82	83	86	81	80	76	66	74

- i. Prepare a stem-and leaf display for these data. Show the leaves sorted in order of increasing magnitude on each stem.
 - ii. Draw a box plot for these data and interpret the data in practical manner.
- b) The temperature in a chemical reactor was measured every half hour under the same conditions. The results were 78.1°C, 79.2°C, 78.9°C, 80.2°C, 78.3°C, 78.8°C, 79.4°C. Calculate the mean, median, lower quartile, upper quartile standard deviation and coefficient of variation. 8
2. a) A problem of statistics is given to three students A, B and C where chance of solving it is $\frac{1}{2}$, $\frac{3}{4}$ and $\frac{2}{3}$ respectively. If they independently solve it, what is the probability that 7
- i. All can solve the problem
 - ii. None can solve the problem
 - iii. Problem can be solved
 - iv. Exactly one can solve the problem
- b) State and Prove Baye's theorem for conditional probability. 8
3. a) A random variable X has the following probability function. 7
- | | | | | | | |
|-------|-----|---|-----|----|-----|---|
| X: | 2 | 3 | 4 | 5 | 6 | 7 |
| F(X): | 0.1 | K | 0.2 | 2k | 0.3 | K |
- Find the value of K and calculate mean and variance.
- b) Customers arrive at complaint department of a store at the rate of 3 per hour. If arrivals follow a Poisson distribution, calculate the 8

probability that

- i. No customer will arrive in a hour
- ii. Two or three customers will arrive in an hour
- iii. At least three customers will arrive in an hour

4. a) In an examination 15% of the candidates got first class (60% marks or above), while 40% failed (securing below 40% marks). Assuming the marks to be normally distributed, estimate the mean and standard deviation. 8

- b) If two random variables have the joint probability density function. 7
 $F(x,y) = \frac{2}{3}(x+2y); 0 < x < 1, 0 < y < 1$

- i. Find marginal density function of X & Y
- ii. Find the conditional density of X given that Y=y
- iii. Are X and Y independent

5. a) A random sample of 8 envelopes is taken from letter box of a post office and their weights in gms are found to be 12.1, 11.9, 12.3, 11.9, 12.1, 12.4, 12.1 and 11.5. Find 99% fiducial limits for the mean weight of envelopes received at that post office. 7

- b) What is P-value? In a factory 2% fans were found to be defective in a lot of 3000 fans, and in another factory 3% fans were found to be defective in a lot of 2500 fans. Do you find that the fans in secondary factory are significantly inferior compared to the fans in the first factory? (Use $\alpha = 0.05$) 8

6. a) An I.Q. test was administered to 5 persons before and after they were trained. The results are given below 8

Candidates	1	2	3	4	5
IQ Before Training	110	120	123	132	125
IQ After Training	120	118	125	136	121

Is training effective at 5% level of significance?

- b) The following table gives the age X and blood pressure Y of 10 women. 7

X	56	42	36	47	49	42	60	72	63	55
Y	147	125	118	128	145	140	155	160	149	150

- i. Find correlation coefficient between age and pressure
- ii. Fit a regression equation of X on Y

7. Write short notes on: (Any two) 2×5

- a) Characteristics of good estimator
- b) Error in hypothesis testing
- c) Confidence Interval