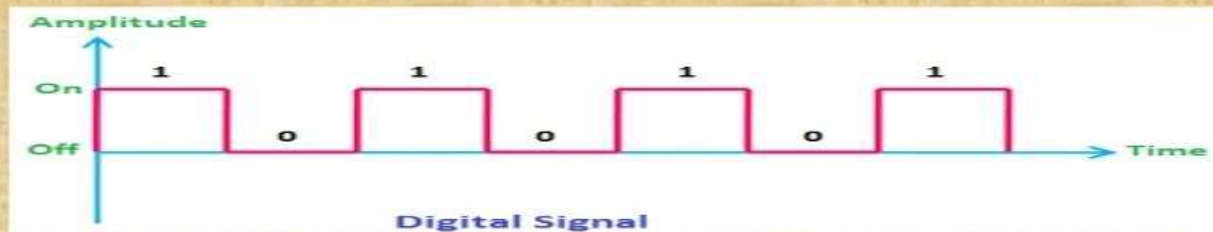


# **Register Transfer Language & Microoperations**

# Register Transfer Language (RTL)

- **Digital System:** An interconnection of hardware modules that do a certain task on the information.



- **Digital Module** = Registers + Operations performed on the data and stored
- Modules are interconnected with common data and control paths to form a digital computer system



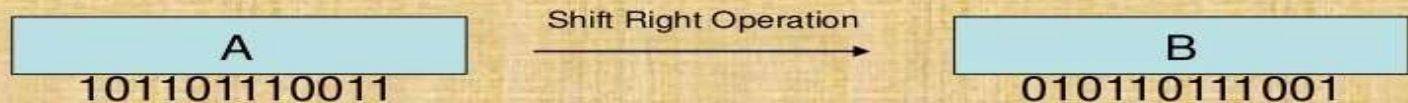
# Register

- Basically Register is collection of individual flip flops.
- Register is a temporary storage area built into a CPU.
- A special, high-speed storage area within the **CPU**. All data must be represented in a **register** before it can be processed.



# Register Transfer Language

- Micro operations: operations executed on data stored in one or more registers.
- For any function of the computer, a sequence of microoperations is used to describe it
- The result of the operation may be:
  - replace the previous binary information of a register or
  - transferred to another register



# RTL

example

- $A = B + C$
- $A - B$
- $A = A - C$
- $A == 1$
- $A++$
- $A--$



# Register Transfer Language

- The internal hardware organization of a digital computer is defined by specifying:
  - The set of registers it contains and their function
  - The sequence of micro operations performed on the binary information stored in the registers
- Registers + Microoperations Hardware + Control Functions = Digital Computer



# Register Transfer Language

- Register Transfer Language (RTL) :
- A symbolic notation to describe the microoperation transfers among registers

Next steps:

- Define symbols for various types of micro operations
- Describe the hardware that implements these microoperations



# Register Transfer

- The individual flip-flops in an n-bit register are numbered in sequence from 0 to n-1 (from the right position toward the left position)



Register R1



Showing individual bits

**A block diagram of a register**



# Register Transfer

- Information transfer from one register to another is described by a *replacement operator*:  $R2 \leftarrow R1$
- This statement denotes a transfer of the content of register R1 into register R2
- The content of the R1 (source) does not change
- The content of the R2 (destination) will be lost and replaced by the new data transferred from R1



# Register Transfer with Control Function

- Conditional transfer occurs only under a control condition
- Representation of a (conditional) transfer  
P:  $R2 \leftarrow R1$
- A binary condition (P equals to 0 or 1) determines when the transfer occurs
- The content of R1 is transferred into R2 only if P is 1

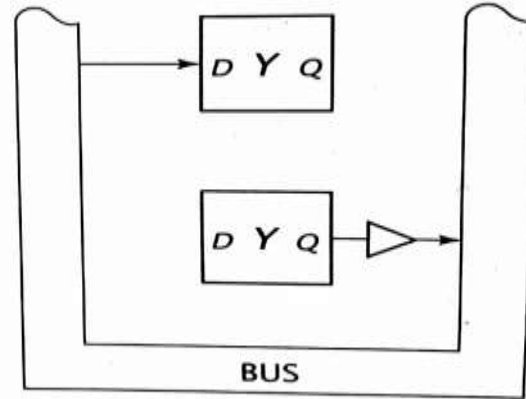


Consider a digital system with two 1-bit registers, X and Y. The  $\mu$ op that copies the contents of register Y to register X can be expressed as  $X \leftarrow Y$ .

Implementations of the micro-operation  $X \leftarrow Y$  using (a) a direct connection and (b) a bus connection



(a)



(b)

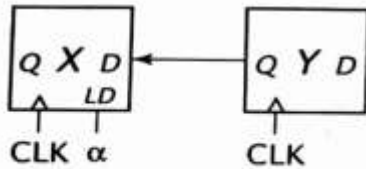
## Contd...

- Both designs provide a path for data to flow from register Y to register X, but neither specifies when X should load this data.
- Assume that the transfer should occur when control input  $\alpha$  is high.  
 $\alpha: X \leftarrow Y$
- When all conditions to the left of the colon are asserted, the data transfers specified by the  $\mu$ ops are performed.
- $\alpha$  is used to load register X and, in the bus-based implementation, to enable the tri-state buffer so that the contents of register Y are placed on the bus.

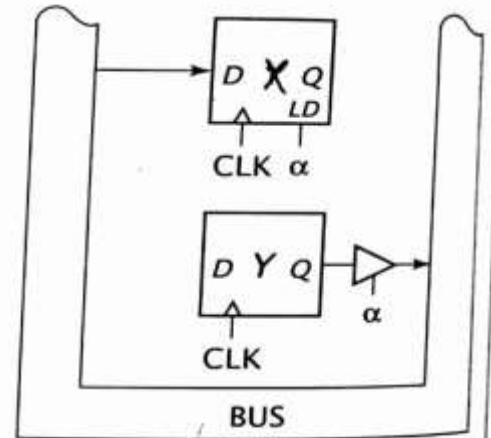


## Contd...

Implementations of the data transfer  $\alpha: X \leftarrow Y$  with control signals: (a) with direct path, and (b) using a bus



(a)

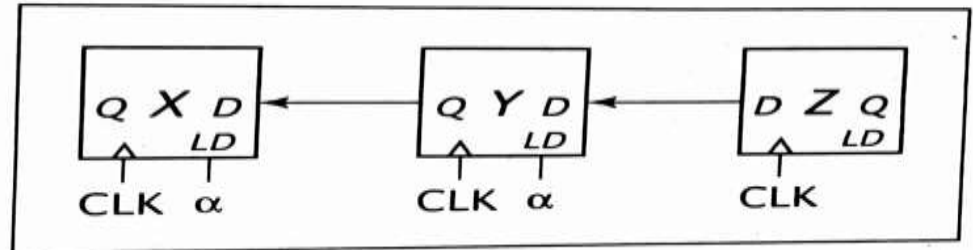


(b)

## Contd...

- One way to improve system performance is to perform two or more  $\mu$ ops simultaneously.
- The  $\mu$ ops are separated by commas; the order in which they are written is unimportant because they are performed concurrently.
- Consider:  $\alpha: X \leftarrow Y, Y \leftarrow Z$  or  $\alpha: Y \leftarrow Z, X \leftarrow Y$   
If  $X=0, Y=1$  and  $Z=0$  just before  $\alpha$  becomes 1, these  $\mu$ ops set  $X=1$  (the original value of  $Y$ ) and  $Y=0$ .
- Note that a single bus cannot be used here because a bus can hold only one value at a time.
- When  $\alpha=1$ , both  $Y$  and  $Z$  must travel on the data paths simultaneously.

**Implementation of the data transfer  $\alpha: X \leftarrow Y, Y \leftarrow Z$**



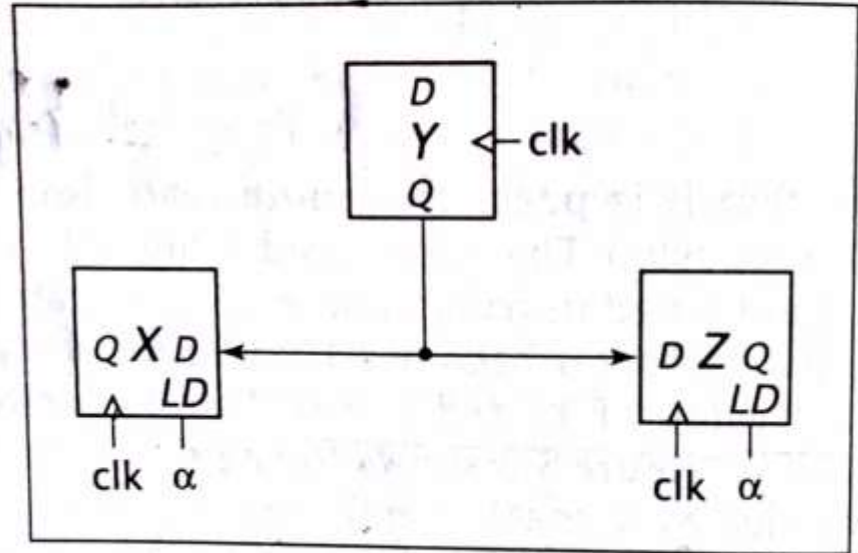


Consider the transfers that occur when  $\alpha = 1$ .

$\alpha: X \leftarrow Y, Z \leftarrow Y$

Register Y can be read by many other registers simultaneously; both micro operations can be performed concurrently.

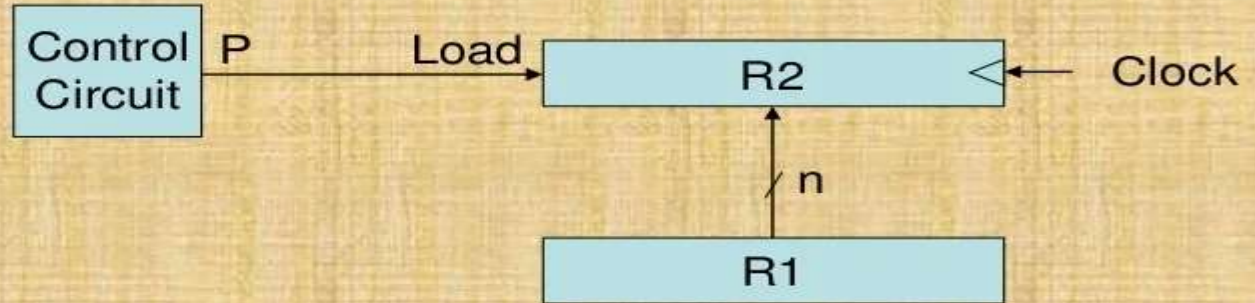
Implementation of the data transfer  $\alpha: X \leftarrow Y, Z \leftarrow Y$



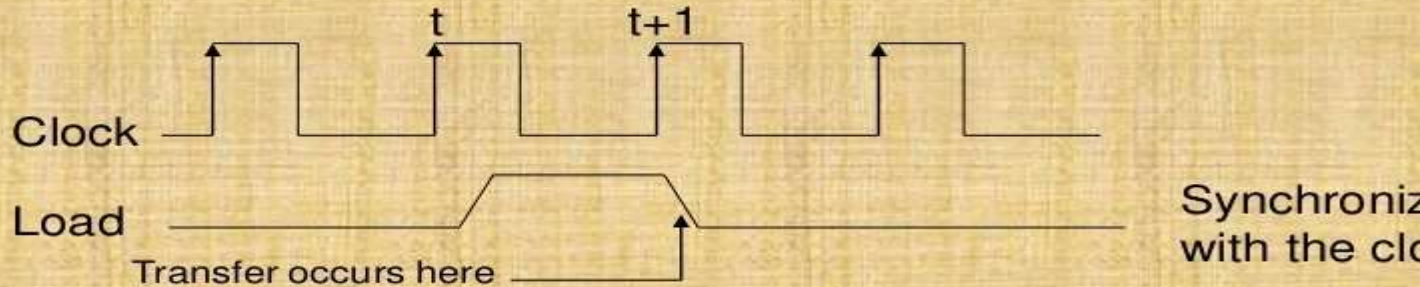
# Register Transfer

Hardware implementation of a controlled transfer:  $P: R2 \leftarrow R1$

**Block diagram:**



**Timing diagram**





# Register Transfer

## Basic Symbols for Register Transfers

Symbol	Description	Examples
Letters & numerals	Denotes a register	MAR, R2
Parenthesis ( )	Denotes a part of a register	R2(0-7), R2(L)
Arrow $\leftarrow$	Denotes transfer of information	$R2 \leftarrow R1$
Comma ,	Separates two microoperations	$R2 \leftarrow R1, R1 \leftarrow R$



# **Bus and Memory Transfers**

- Paths must be provided to transfer information from one register to another
- A bus: set of common lines, one for each bit of a register, through which binary information transferred one at a time..



# Memory Operations

- **READ operation**
- Helps to retrieve data from memory.
- **WRITE operation**
- Storing data into a memory.
  
- Memory read : Transfer from memory
- Memory write : Transfer to memory



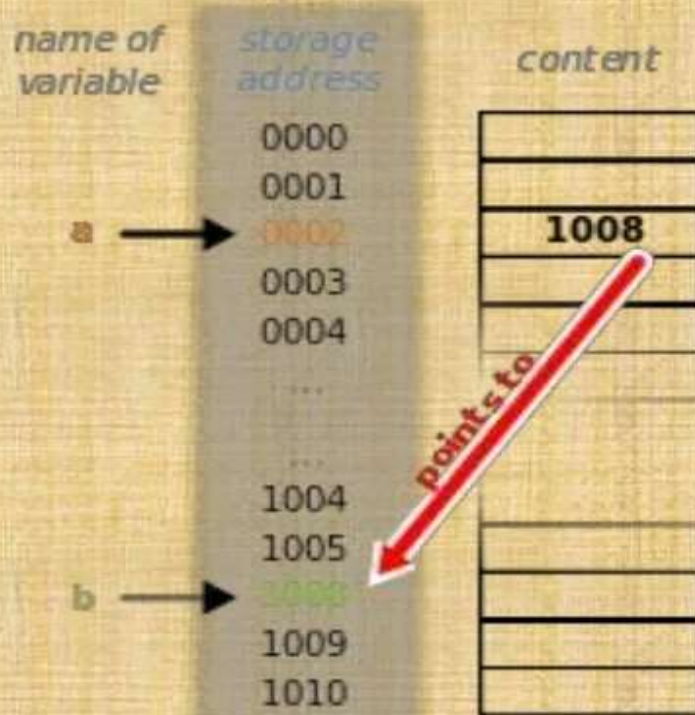
# Bus and Memory Transfers:

## Memory Transfer

- Data being read or write is called a memory word (called M)
- It is necessary to specify the address of M when writing /reading memory
- This is done by enclosing the address in square brackets following the letter M
- Example: M[0016] : the memory contents at address 0x0016

Note: 0x written in front of a number is an alternative way to say “this is hexadecimal.





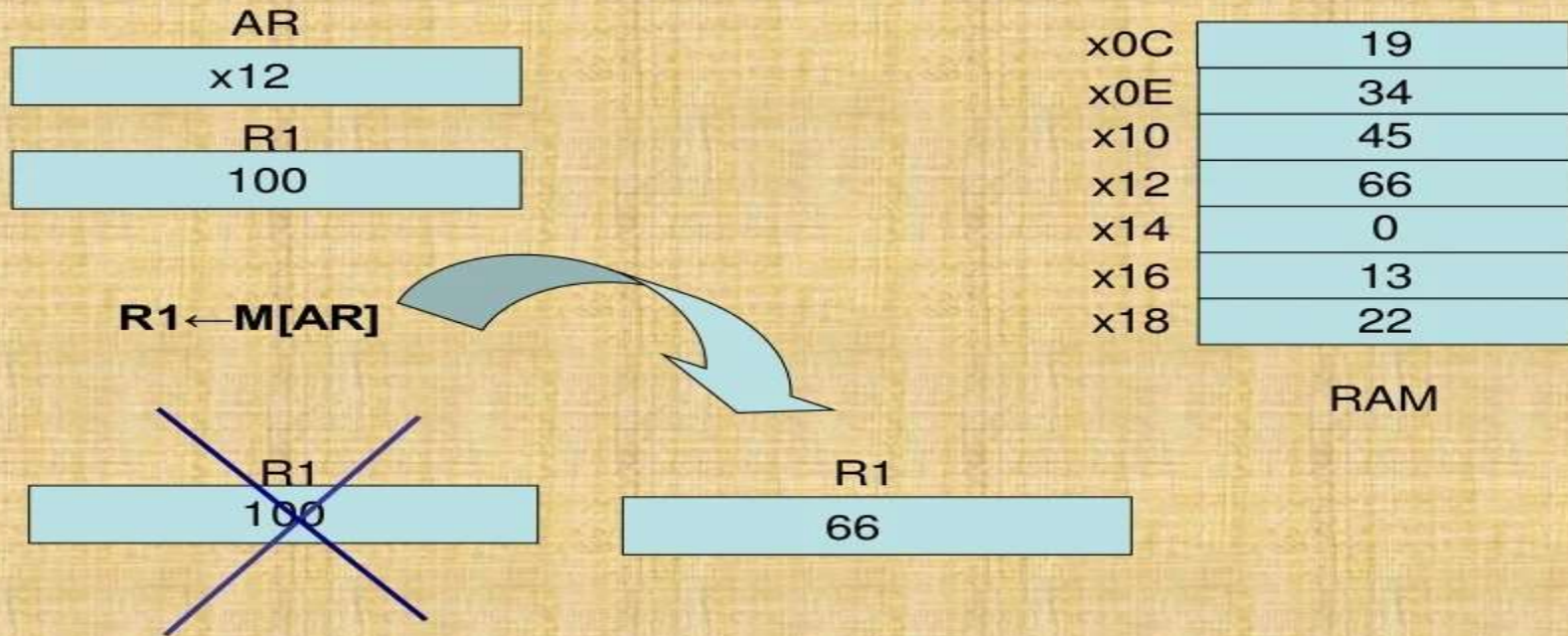
Address	Value
0x00	01001010
0x01	10111010
0x02	01011111
0x03	00100100
0x04	01000100
0x05	10100000
0x06	01110100
0x07	01101111
0x08	10111011
...	...
0xFE	11011110
0xFF	10111011

# Memory related registers

1. Memory Address Register (MAR)
  2. Memory Data Register (MDR)
- **MAR** is the CPU register that either stores the memory address from which data will be fetched to the CPU or the address to which data will be sent and stored.
  - **MDR** is the register in a computer's processor that stores the data being transferred to and from the immediate access storage.



# Bus and Memory Transfers: Memory Transfer



# Arithmetic Microoperations

- The micro operations in digital computers are classified into four categories:
  - Register transfer microoperations
  - Arithmetic microoperations
  - Logic microoperations
  - Shift microoperations



# Arithmetic Microoperations

- The basic arithmetic microoperations are: addition, subtraction, increment, decrement, and shift
- Addition Microoperation:

$$R3 \leftarrow R1 + R2$$

- Subtraction Microoperation:

$$R3 \leftarrow R1 - R2 \text{ or :}$$

$$R3 \leftarrow R1 + \overline{R2} + 1$$

1's complement



# Arithmetic Microoperations

## cont.

- One's Complement Microoperation:

$$R2 \leftarrow \overline{R2}$$

- Two's Complement Microoperation:

$$R2 \leftarrow R2 + 1$$

- Increment Microoperation:

$$R2 \leftarrow R2 + 1$$

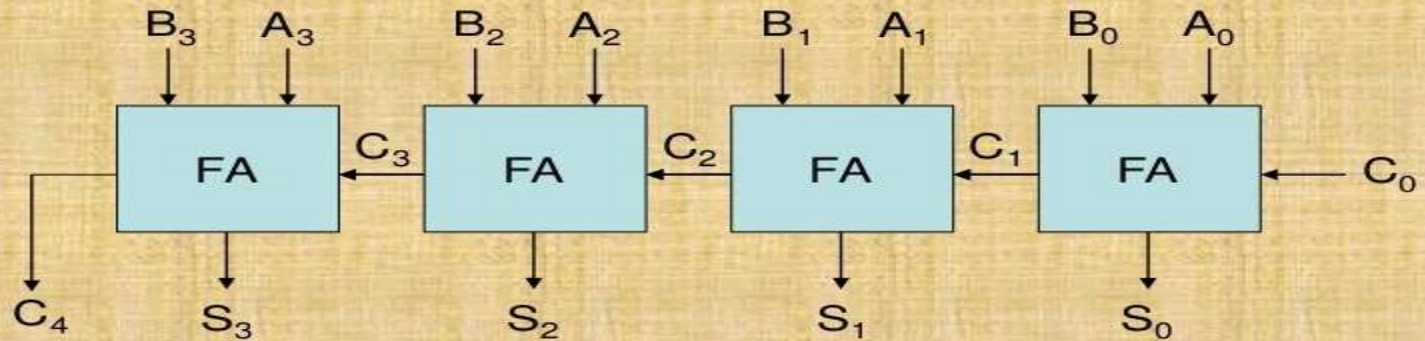
- Decrement Microoperation:

$$R2 \leftarrow R2 - 1$$



# Arithmetic Microoperations

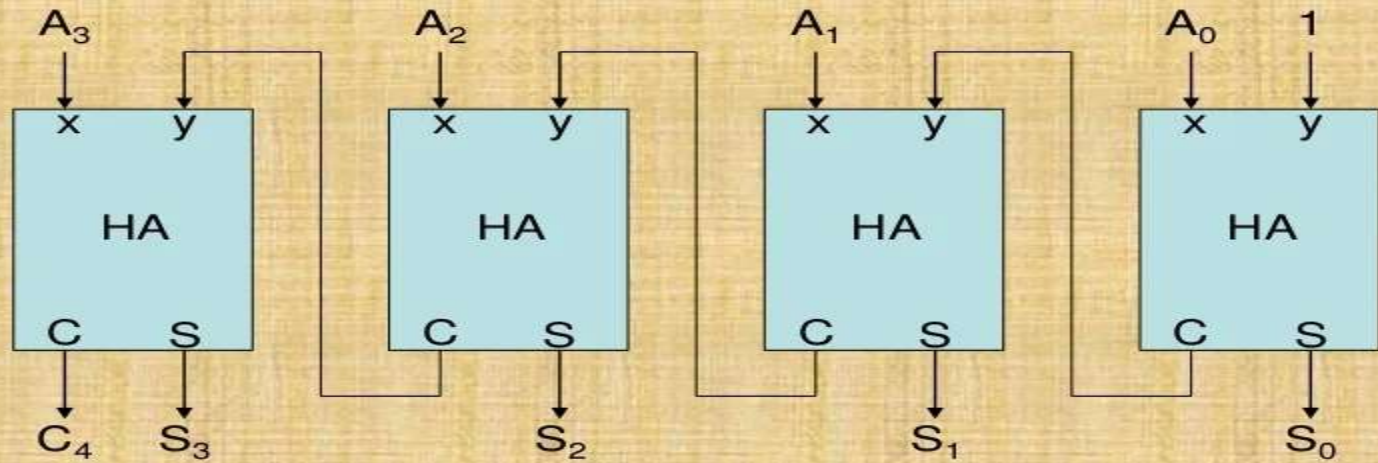
## Binary Adder



**4-bit binary adder  
(connection of FAs)**

# Arithmetic Microoperations

## Binary Incrementer



**4-bit Binary Incrementer**



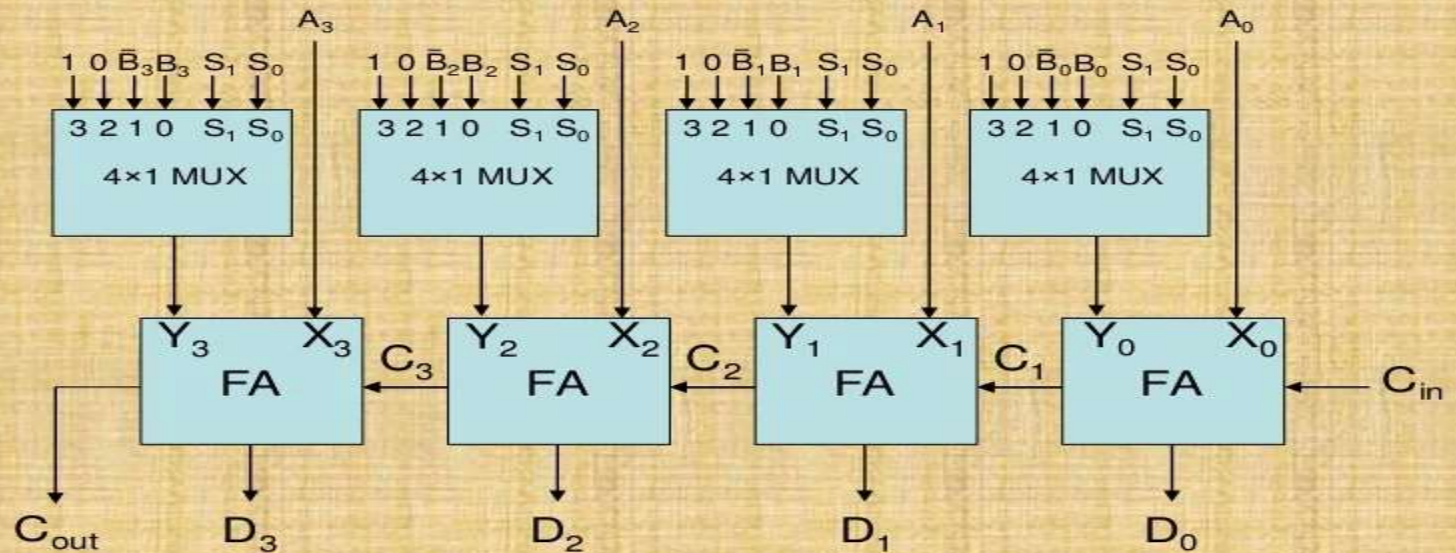
# Arithmetic Microoperations

## Binary Incrementer

- Binary Incrementer can also be implemented using a counter
- A binary decrementer can be implemented by subtracting 1111 to the register each time!

# Arithmetic Microoperations

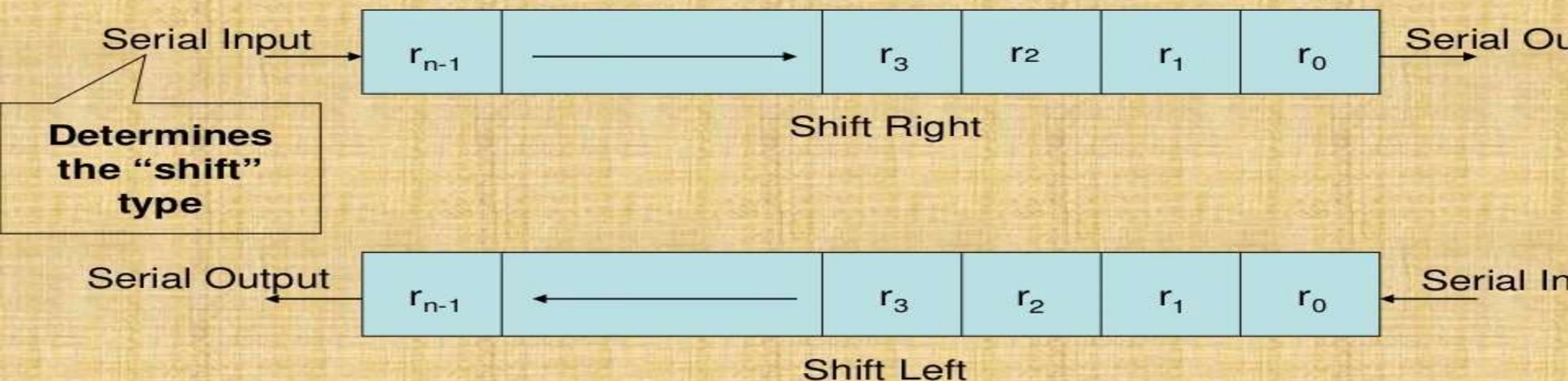
## Arithmetic Circuit



**4-bit Arithmetic Circuit**



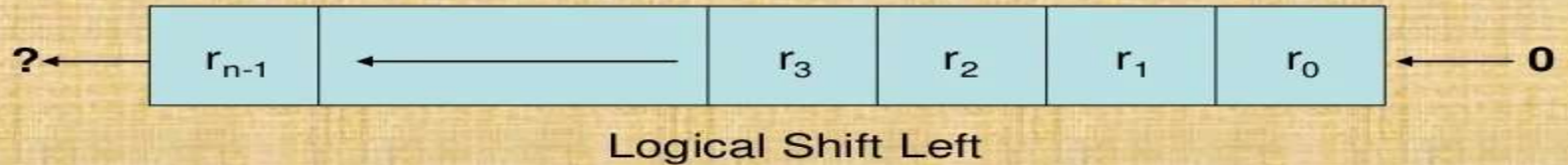
# Shift Microoperations cont.



**\*\***Note that the bit  $r_i$  is the bit at position (i) of the register

# Shift Microoperations: Logical Shifts

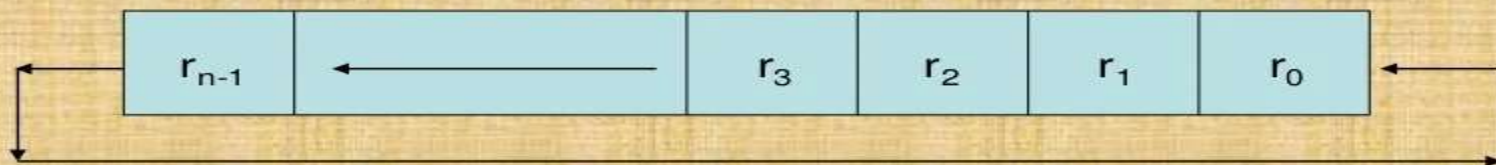
- Transfers 0 through the serial input
- Logical Shift Right:  $R1 \leftarrow \text{shr } R1$   
The same
- Logical Shift Left:  $R2 \leftarrow \text{shl } R2$   
The same





## Shift Microoperations: Circular Shifts (Rotate Operation)

- Circulates the bits of the register around the two ends without loss of information
- Circular Shift Right:  $R1 \leftarrow \text{cir } R1$   
The same
- Circular Shift Left:  $R2 \leftarrow \text{cil } R2$   
The same



Circular Shift Left



# Shift Microoperations

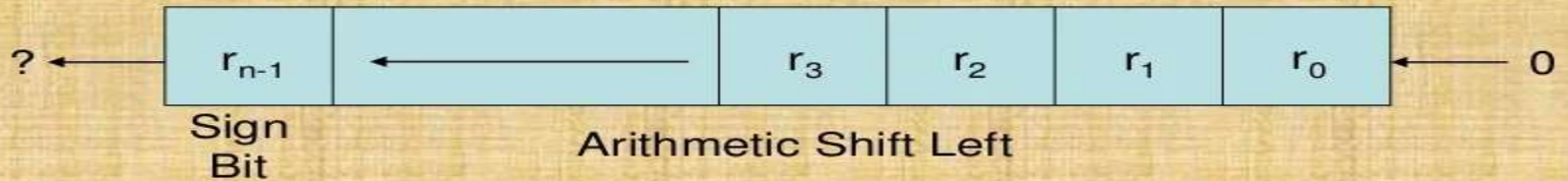
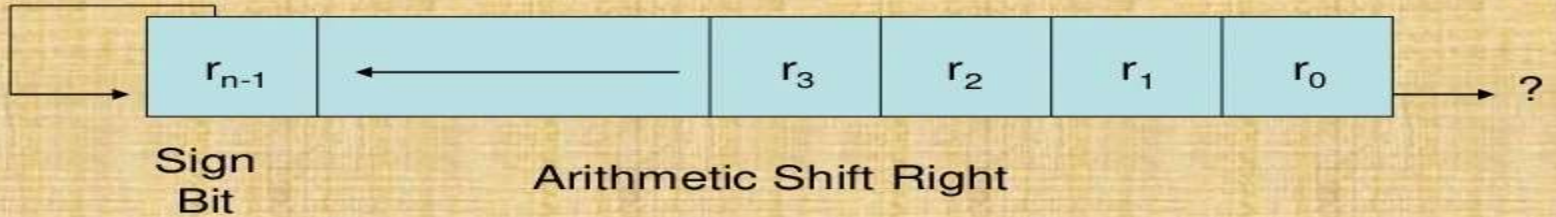
## Arithmetic Shifts

- Shifts a signed binary number to the left or right
- An arithmetic shift-left multiplies a signed binary number by 2:    `ashl (00100): 01000`
- An arithmetic shift-right divides the number by 2  
      `ashr (00100) : 00010`
- An overflow may occur in arithmetic shift-left, and occurs when the sign bit is changed (sign reversal)



# Shift Microoperations

## Arithmetic Shifts cont.

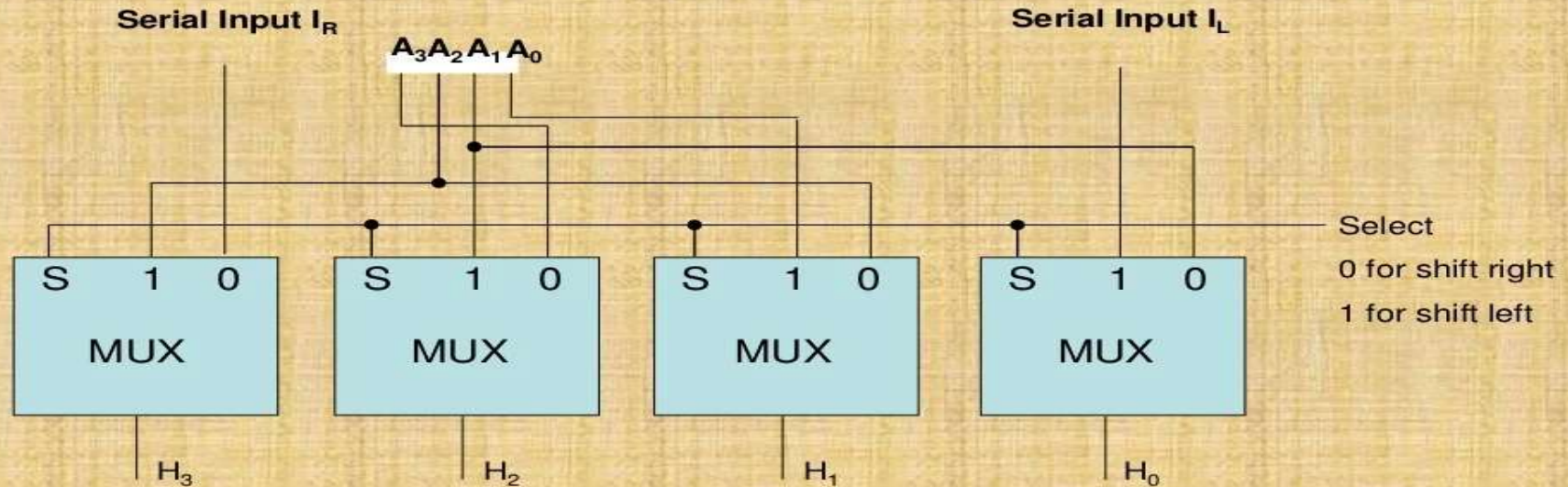


# Shift Microoperations cont.

- Example: Assume  $R1 = 11001110$ , then:
  - Arithmetic shift right once :  $R1 = 11100111$
  - Arithmetic shift right twice :  $R1 = 11110011$
  - Arithmetic shift left once :  $R1 = 10011100$
  - Arithmetic shift left twice :  $R1 = 00111000$
  - Logical shift right once :  $R1 = 01100111$
  - Logical shift left once :  $R1 = 10011100$
  - Circular shift right once :  $R1 = 01100111$
  - Circular shift left once :  $R1 = 10011101$



# Shift Microoperations Hardware Implementation



**4-bit Combinational Circuit Shifter**

# Logical micro-operations

- Specify binary operations on the strings of bits in registers
  - Logic micro-operations are bit-wise operations, i.e., they work on the individual bits of data
- There are, in principle, 16 different logic functions that can be defined over two binary input variables

A	B	$F_0$	$F_1$	$F_2$	...	$F_{13}$	$F_{14}$	$F_{15}$
0	0	0	0	0	...	1	1	1
0	1	0	0	0	...	1	1	1
1	0	0	0	1	...	0	1	1
1	1	0	1	0	...	1	0	1

- However, most systems only implement four of these
  - AND ( $\wedge$ ), OR ( $\vee$ ), XOR ( $\oplus$ ), Complement/NOT
- The others can be created from combination of these

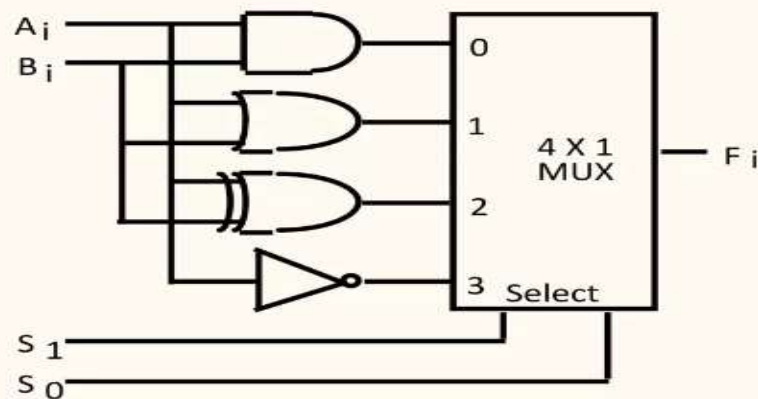


# Logical Micro-operation

- List of Logic Micro-operations
  - 16 different logic operations with 2 binary vars.
  - n binary vars  $\rightarrow 2^{2^n}$  functions
- Truth tables for 16 functions of 2 variables and the corresponding 16 logic micro-operations

x	0 0 1 1	Boolean Function	Micro-Operations	Name
y	0 1 0 1			
	0 0 0 0	$F_0 = 0$	$F \leftarrow 0$	Clear
	0 0 0 1	$F_1 = xy$	$F \leftarrow A \wedge B$	AND
	0 0 1 0	$F_2 = xy'$	$F \leftarrow A \wedge B'$	
	0 0 1 1	$F_3 = x$	$F \leftarrow A$	Transfer A
	0 1 0 0	$F_4 = x'y$	$F \leftarrow A' \wedge B$	
	0 1 0 1	$F_5 = y$	$F \leftarrow B$	Transfer B
	0 1 1 0	$F_6 = x \oplus y$	$F \leftarrow A \oplus B$	Exclusive-OR
	0 1 1 1	$F_7 = x + y$	$F \leftarrow A \vee B$	OR
	1 0 0 0	$F_8 = (x + y)'$	$F \leftarrow (A \vee B)'$	NOR
	1 0 0 1	$F_9 = (x \oplus y)'$	$F \leftarrow (A \oplus B)'$	Exclusive-NOR
	1 0 1 0	$F_{10} = y'$	$F \leftarrow B'$	Complement B
	1 0 1 1	$F_{11} = x + y'$	$F \leftarrow A \vee B$	
	1 1 0 0	$F_{12} = x'$	$F \leftarrow A'$	Complement A
	1 1 0 1	$F_{13} = x' + y$	$F \leftarrow A' \vee B$	
	1 1 1 0	$F_{14} = (xy)'$	$F \leftarrow (A \wedge B)'$	NAND
	1 1 1 1	$F_{15} = 1$	$F \leftarrow \text{all 1's}$	Set to all 1's

# Hardware implementation of logic Micro-operation



Function table

$S_1$	$S_0$	Output	$\mu$ -operation
0	0	$F = A \wedge B$	AND
0	1	$F = A \vee B$	OR
1	0	$F = A \oplus B$	XOR
1	1	$F = A'$	Complement