

Assignment 1 Report

Entry Number: 2016CS10363

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1 A

2 Locally Weighted Linear Regression:

(a) Linear Regression (unweighted):

$$\theta = \begin{bmatrix} \theta_0 \\ \theta_1 \end{bmatrix} = \begin{bmatrix} 0.327680 \\ 0.175316 \end{bmatrix}$$

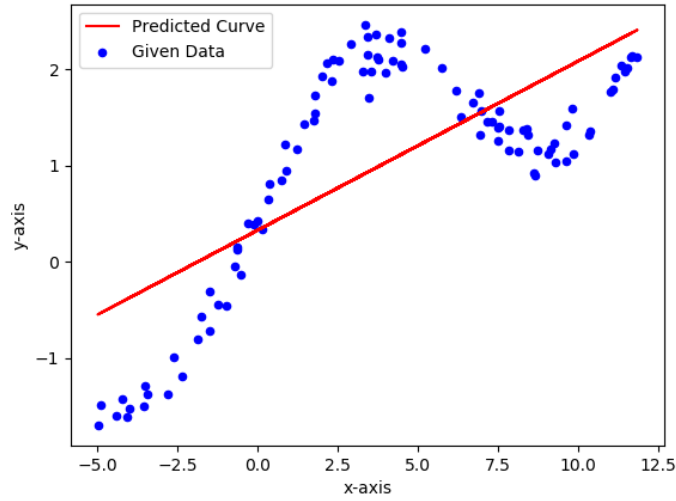


Figure 1: Linear Regression Plot (Underfitting)

Linear Regression(unweighted) is not a good fit for the data as shown in the Figure 1(underfitting).

(b) Locally Weighted Linear Regression:

Weights : $w^{(i)} = \exp\left(-\frac{(x - x^{(i)})^2}{2\tau^2}\right)$ (where τ = Bandwidth Parameter)

Error Function: $J(\theta) = \frac{1}{2m}(X\theta - Y)^T W (X\theta - Y)$ (where $W = \text{diag}(w^{(i)})$)

Minima: $\nabla_{\theta} J(\theta) = 0 \Rightarrow \theta = (X^T W X)^{-1} X^T W Y$

Plots:

Linear Regression (unweighted):

3 Logistic Regression:

Log Likelihood:
$$LL(\theta) = \sum_{i=1}^m y^{(i)} \log(h_{\theta}(x^{(i)})) + (1 - y^{(i)}) \log(1 - h_{\theta}(x^{(i)}))$$

$$\nabla_{\theta} LL(\theta) = X^T (Y - g(X\theta)) \quad (\text{where } g(x) = \frac{1}{1 + \exp(-x)})$$

Hessian Matrix:
$$H = \nabla_{\theta}^2 LL(\theta) = -X^T D X$$

 (where $D = \text{diag}(g(x^{(i)T}\theta)(1 - g(x^{(i)T}\theta)))$)

Newton's Method:

$$\theta^{(t+1)} = \theta^{(t)} - H^{-1} \nabla_{\theta} LL(\theta) \big|_{\theta_t}$$

Convergence Condition:

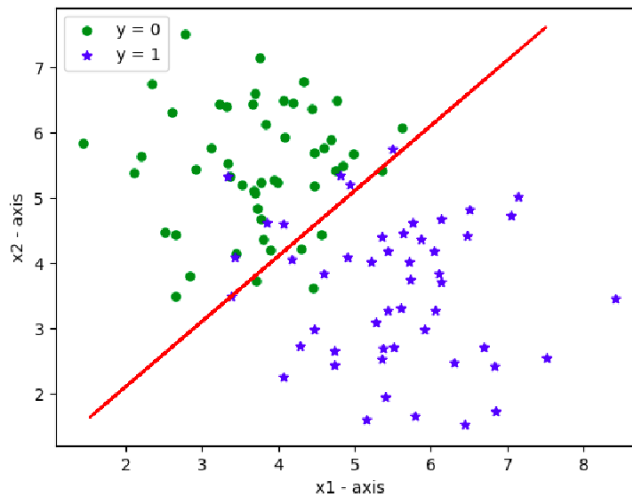
$$|\theta_j^{(t+1)} - \theta_j^{(t)}| < \epsilon \quad (\text{for a sufficiently small } \epsilon)$$

Resulting Parameters:

$$\theta = \begin{bmatrix} \theta_0 \\ \theta_1 \\ \theta_2 \end{bmatrix} = \begin{bmatrix} 0.223295 \\ 1.962616 \\ -1.964861 \end{bmatrix}$$

Decision Boundary is the straight line boundary separating the region where $h_{\theta}(x) \geq 0.5$ (class $y = 1$) from where $h_{\theta}(x) \leq 0.5$ (class $y = 0$).

Plot:



4 Gaussian Discriminant Analysis:

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