Finally … Functions!

ESC101: Fundamentals of Computing

Purushottam Kar

Announcements

- Mid-sem lab exam marks available on Prutor
  - Maximum: 150, Average: 80, Standard deviation: 47
  - See rubric on website carefully before applying for regrading
  - Frivolous regrading requests will simply get penalty negative marks
- Last date for dropping Advanced Track October 12
  - Application must be an email to instructor, mentors, teammates
- Last date for dropping ESC101 course October 12
  - Application must be on standard DoAA course drop form – no email!
- Joint tutorial for B1 and B14 on October 12
  - 12 – 1 PM (same time), L19 - just an arrangement for this week ☺

The Golden Rules of Pointers

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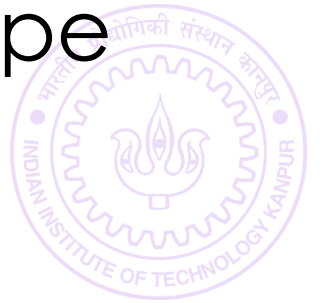

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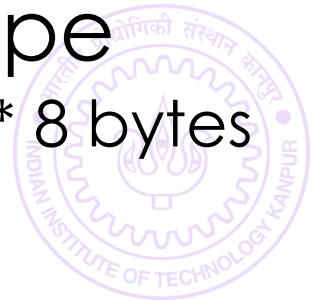

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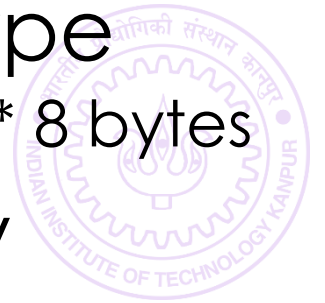

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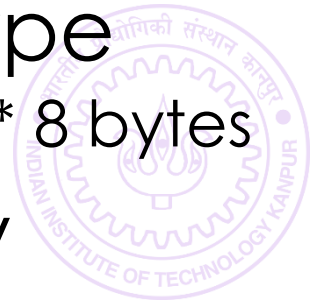

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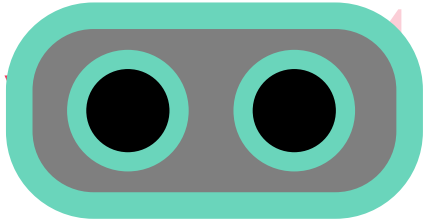

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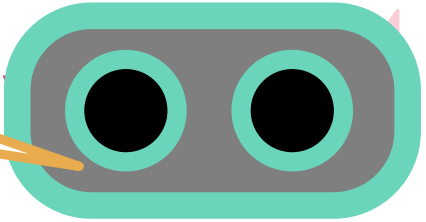
a, b, c all point to their respective first elements ☺



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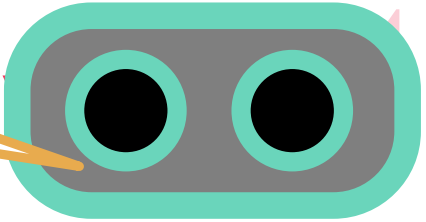

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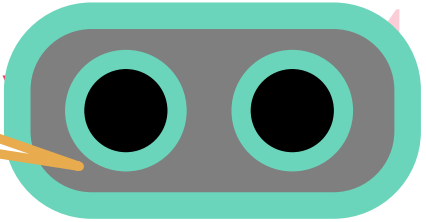

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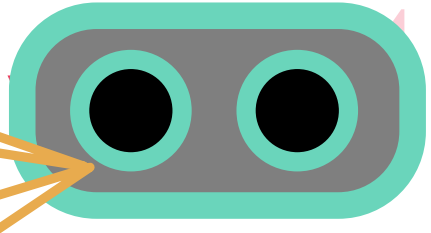

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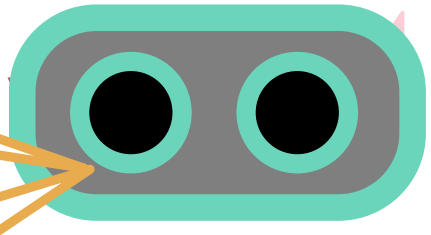

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You can modify the pointer c by saying c++ but I will not allow you to say things like a++, b++. I also dont allow you to free/realloc a and b ☺

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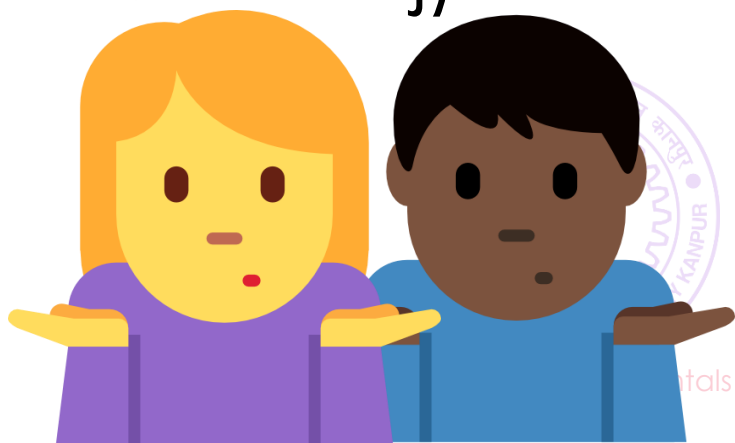

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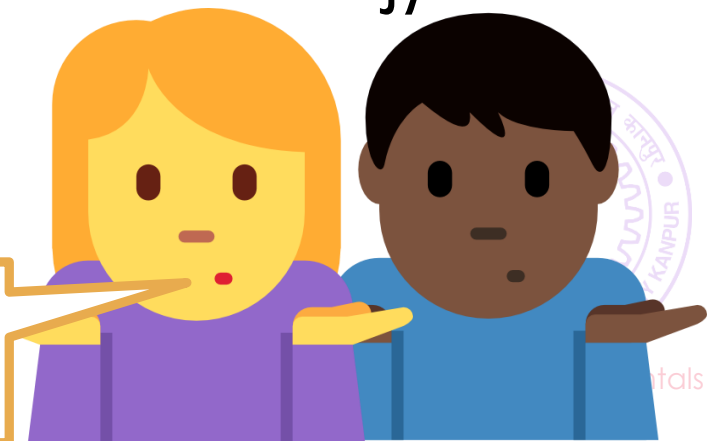

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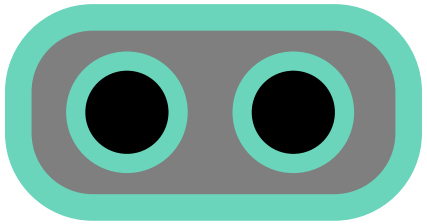

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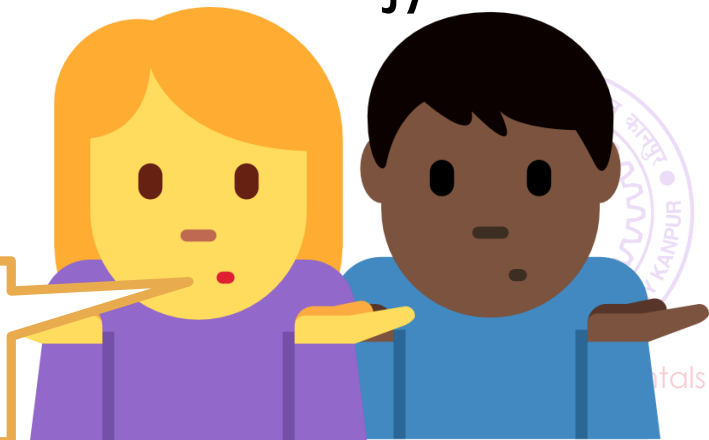

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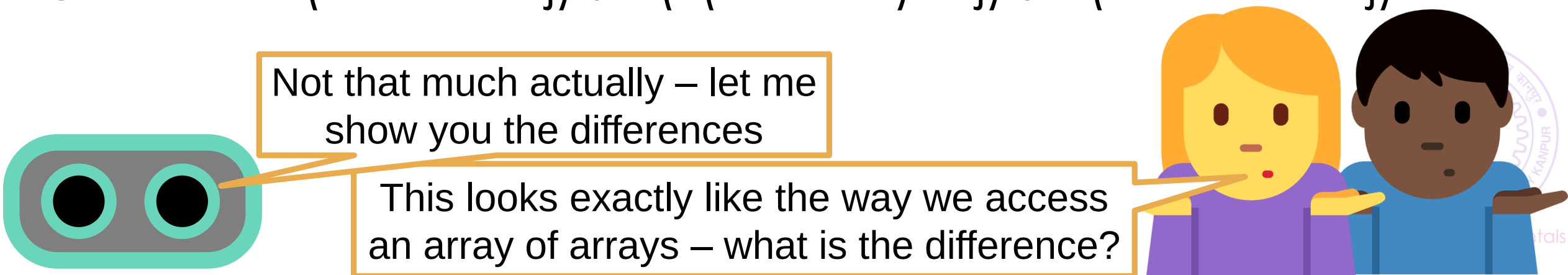

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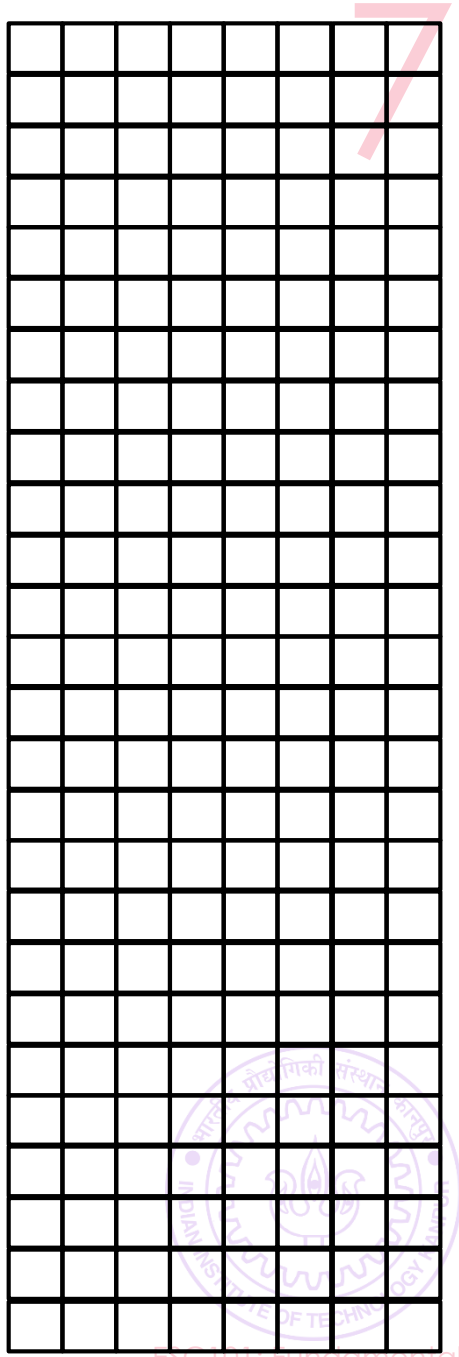

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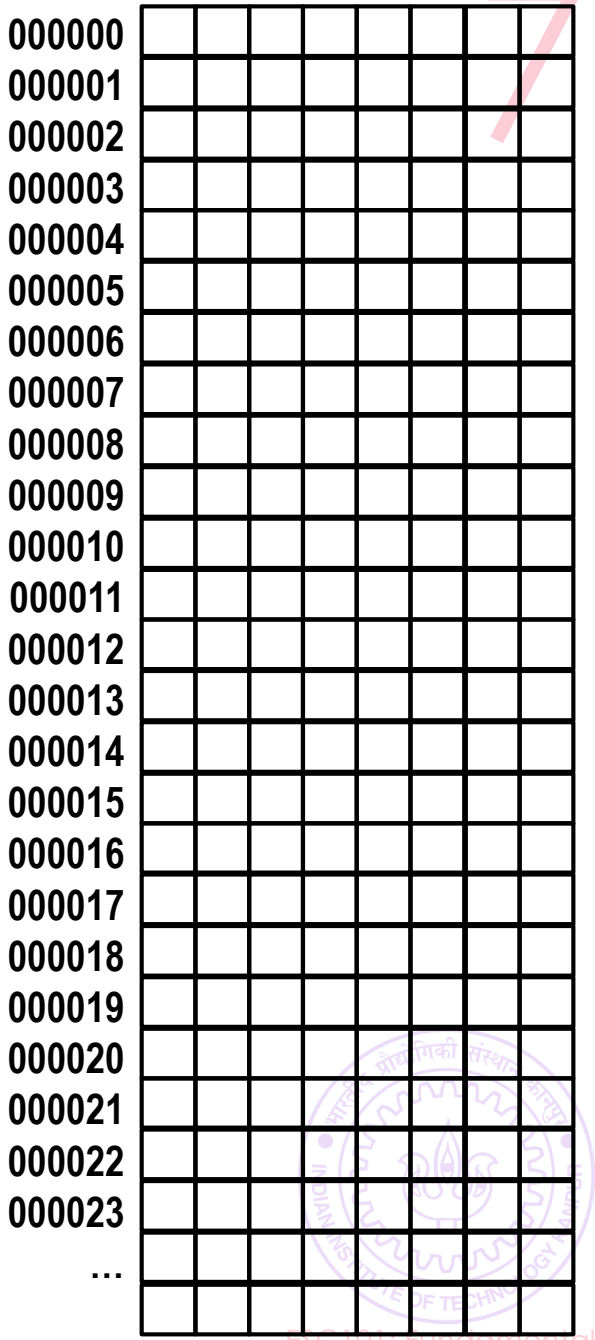

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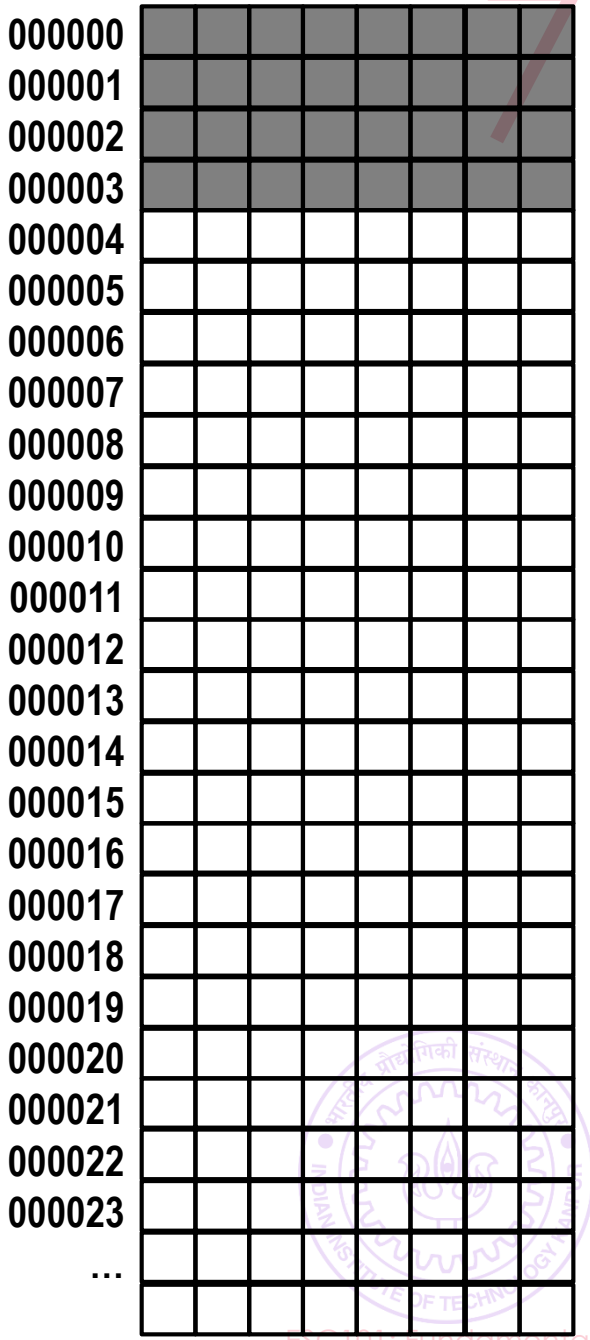

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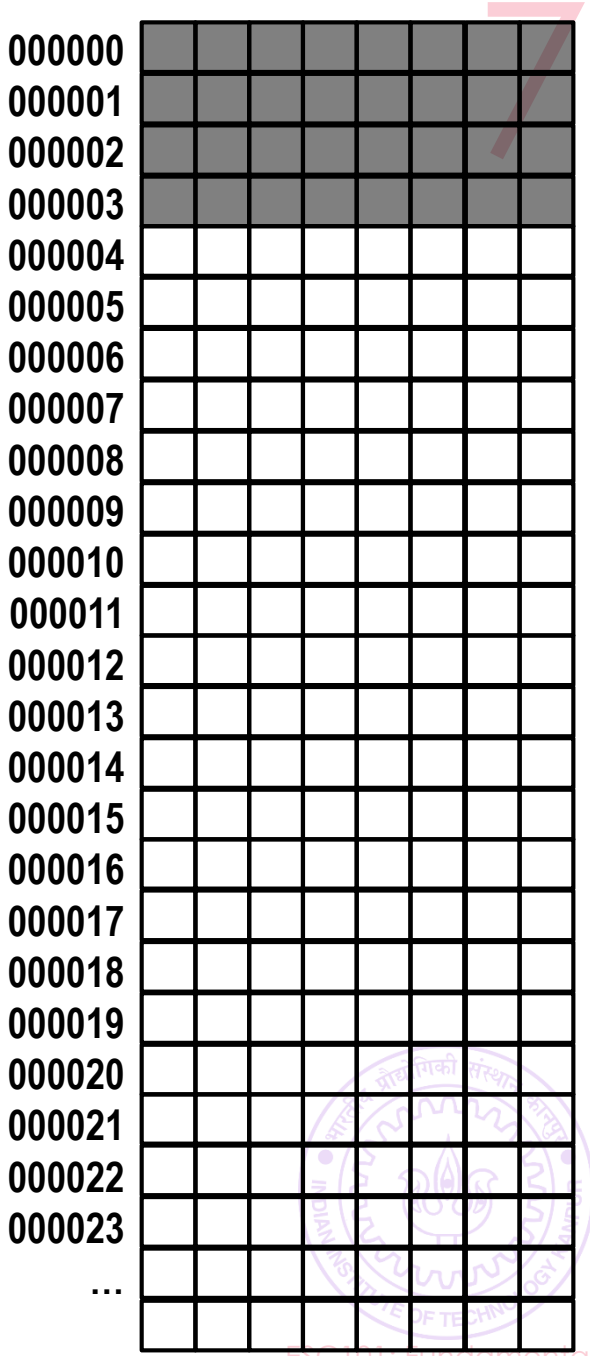

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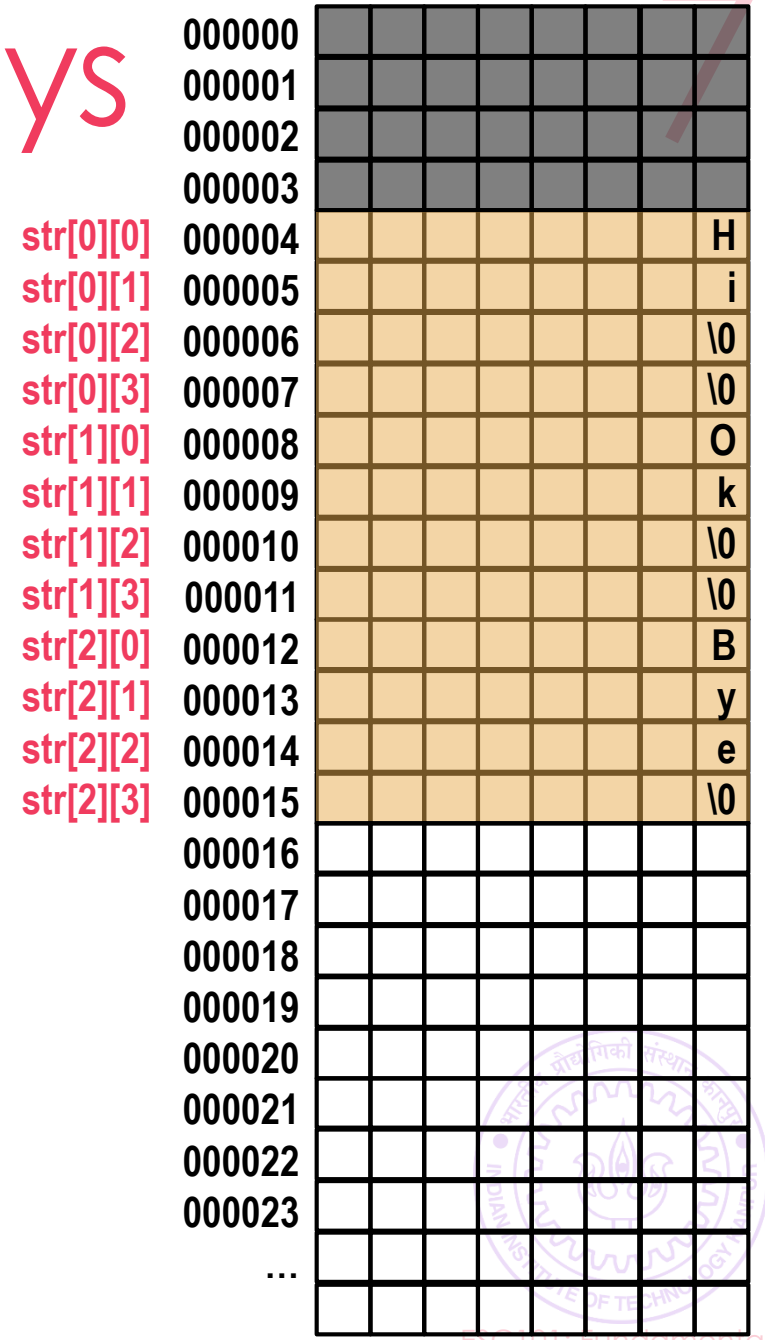

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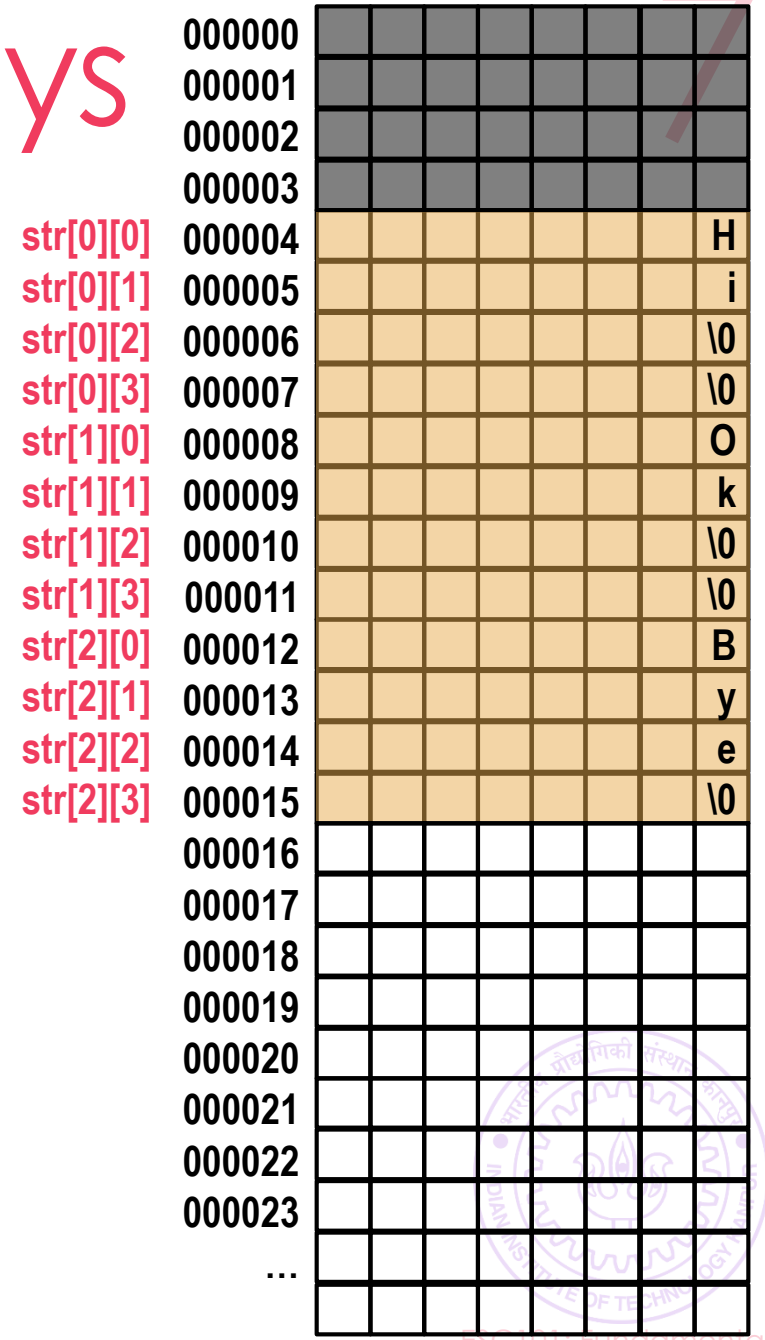

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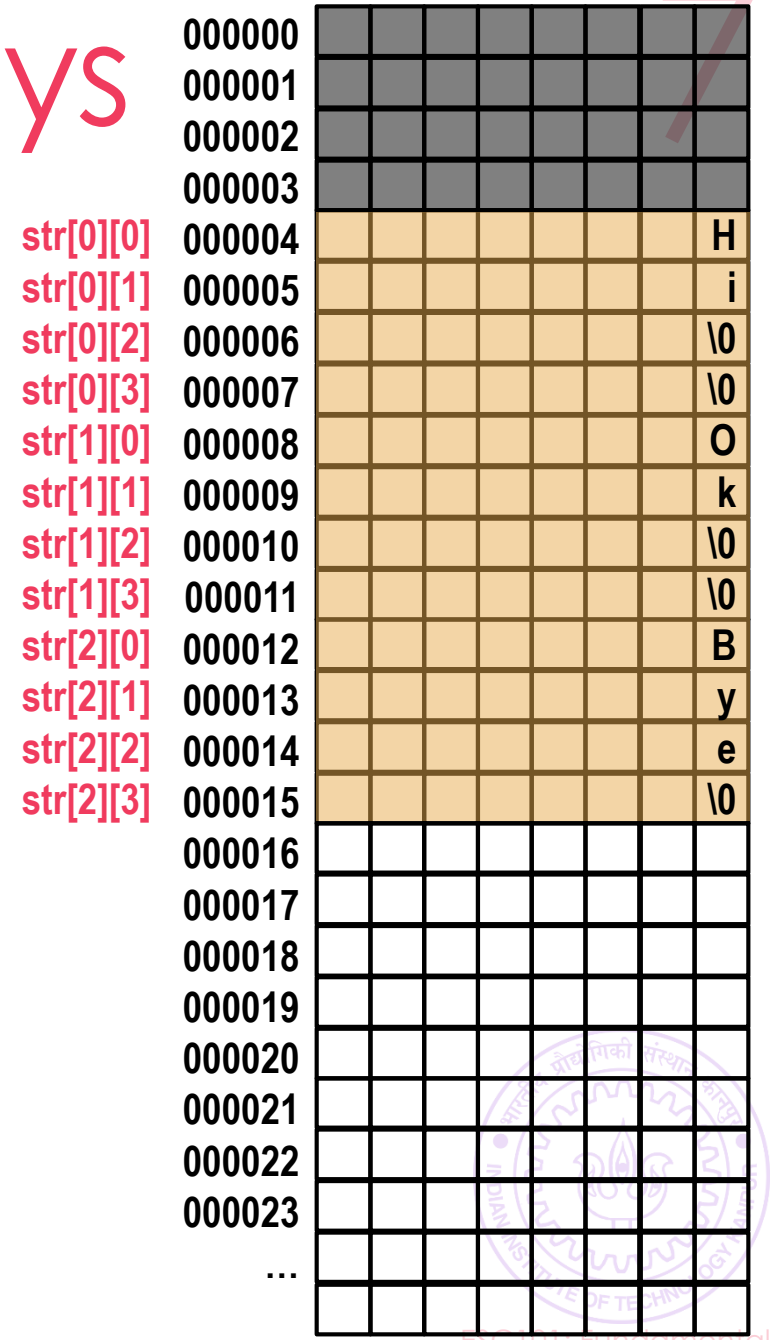

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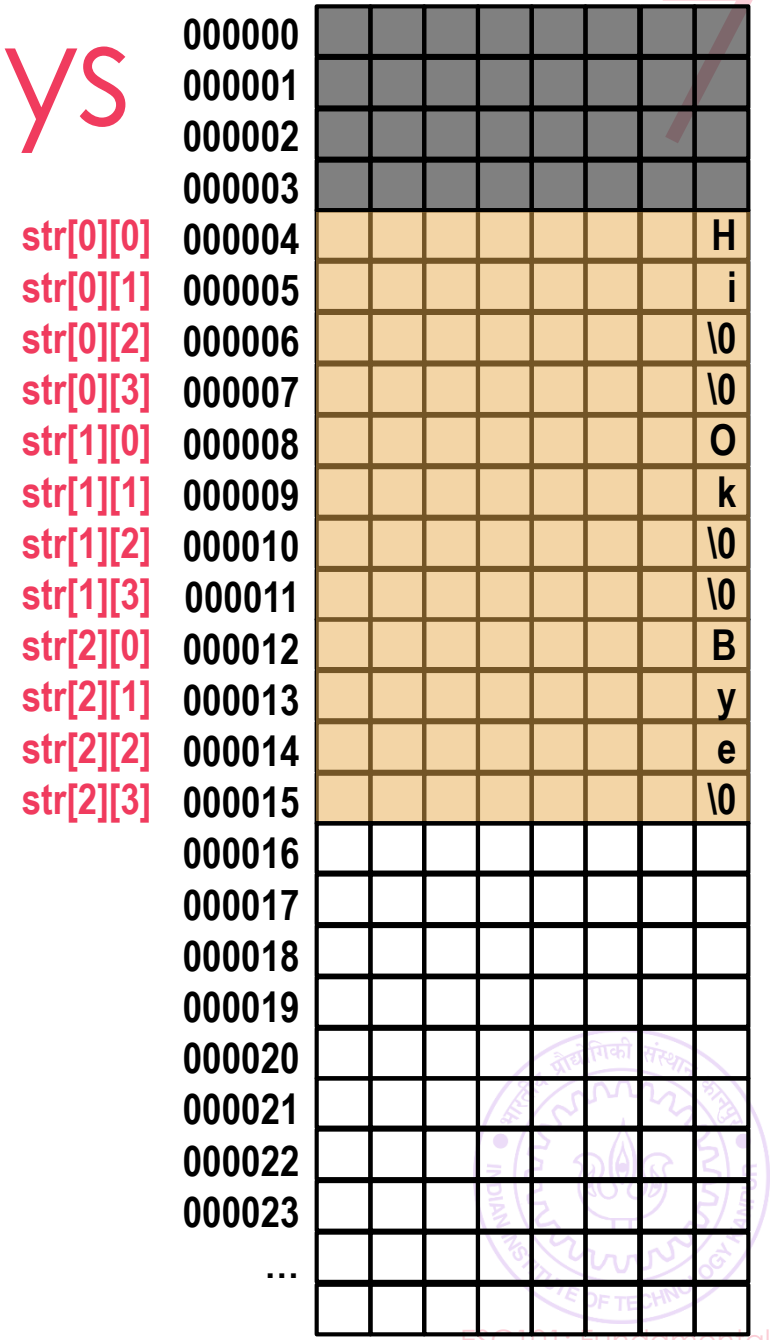
- Location of the str pointer not shown
- First all elements of row 0 stored in continuous sequence
- Then without breaking sequence, all elements of row 1 stored and so on



Memory layout of 2D arrays

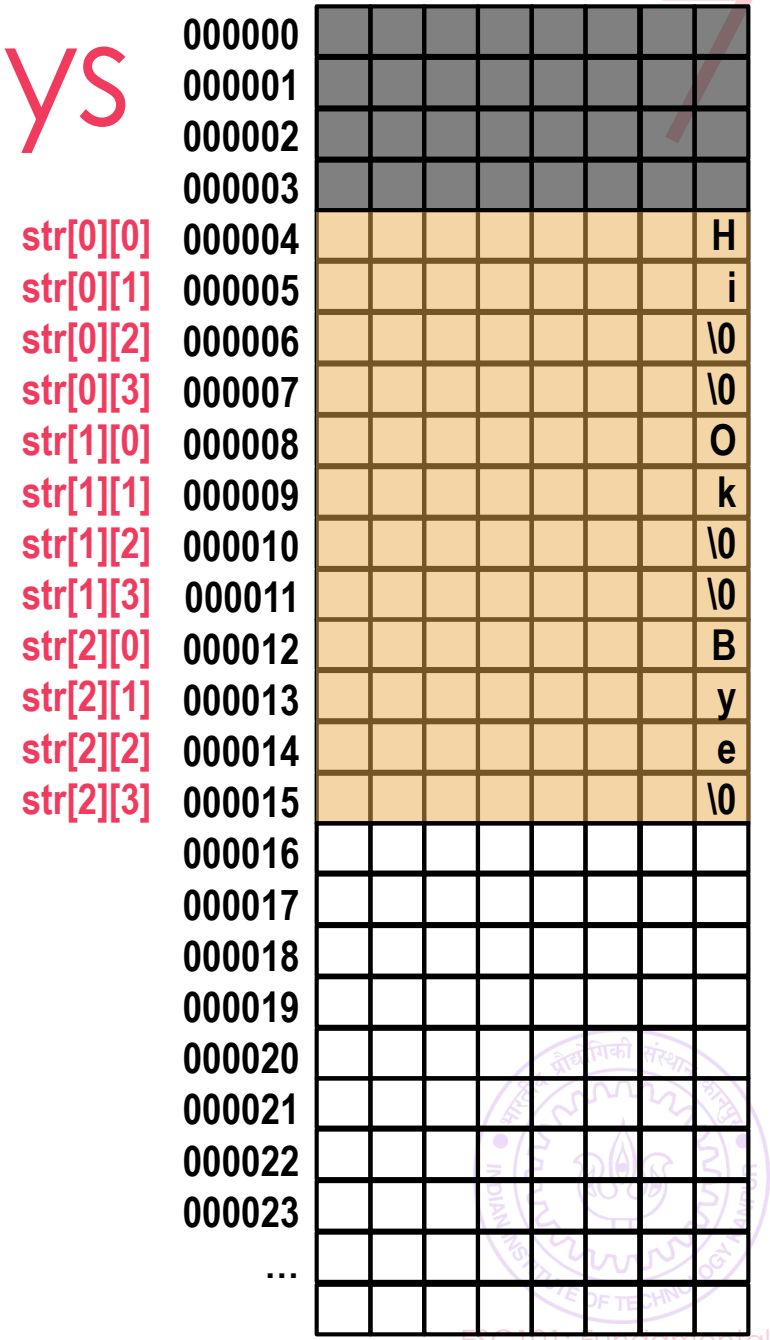
```
char str[3][4] = {"Hi","Ok","Bye"};
```

Location of the str pointer not shown

First all elements of row 0 stored in continuous sequence

Then without breaking sequence, all elements of row 1 stored and so on

```
char* ptr = *str; // ptr points to str[0][0]
ptr += 4; // ptr now points to str[1][0]
ptr += 4; // ptr now points to str[2][0]
ptr += 1; // ptr now points to str[2][1]
```



Layout of arrays of arrays

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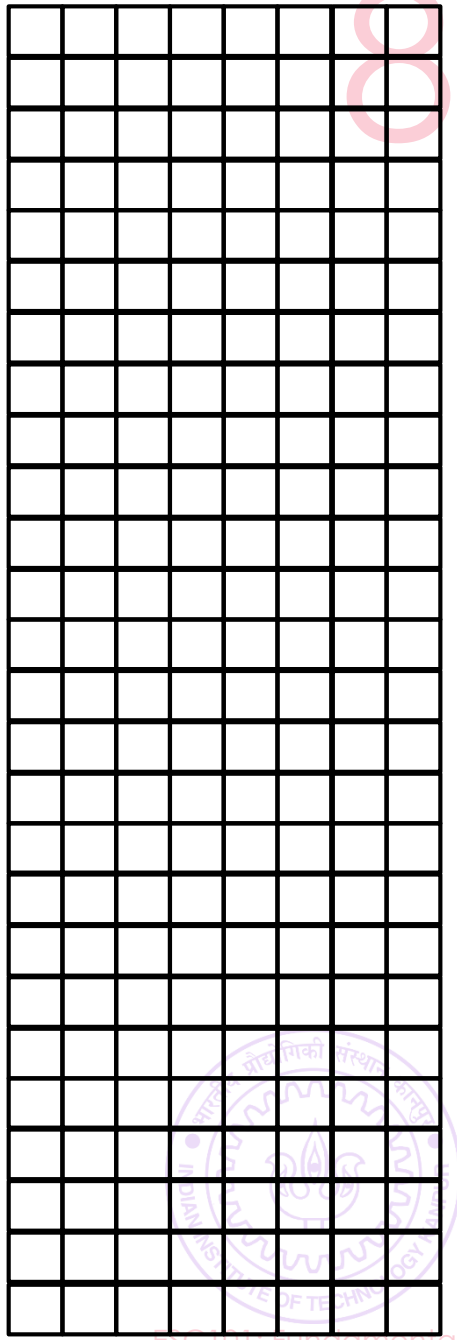

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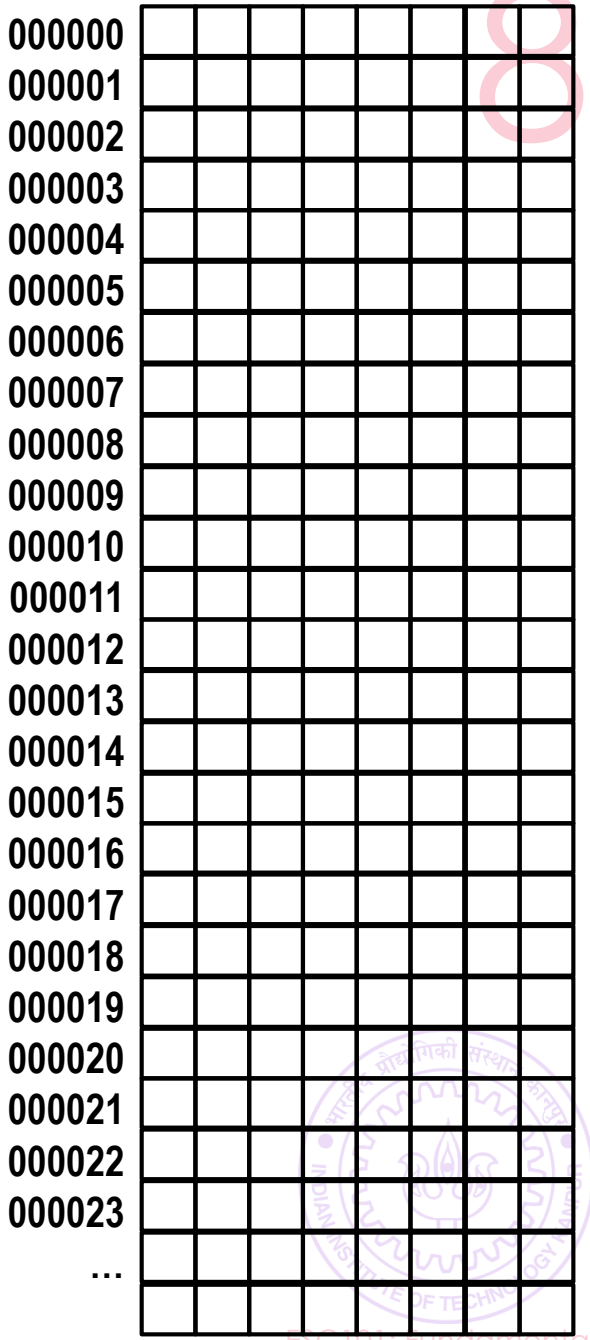

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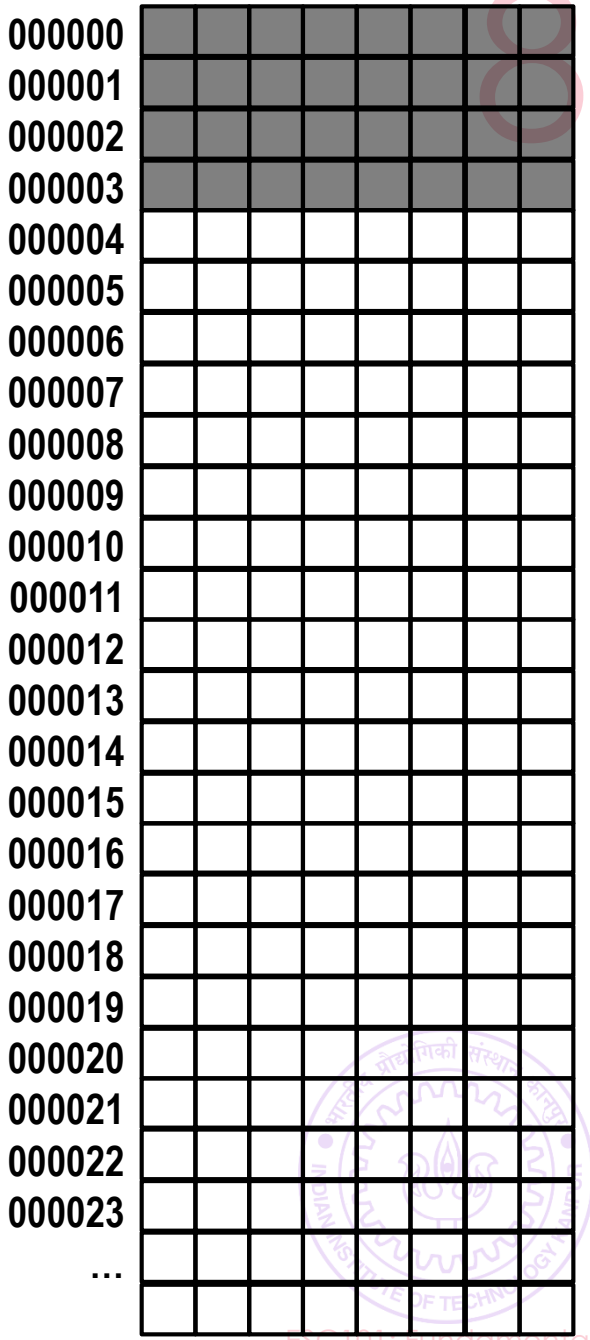

Layout of arrays of arrays

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char **str = (char**)malloc(3*sizeof(char*));
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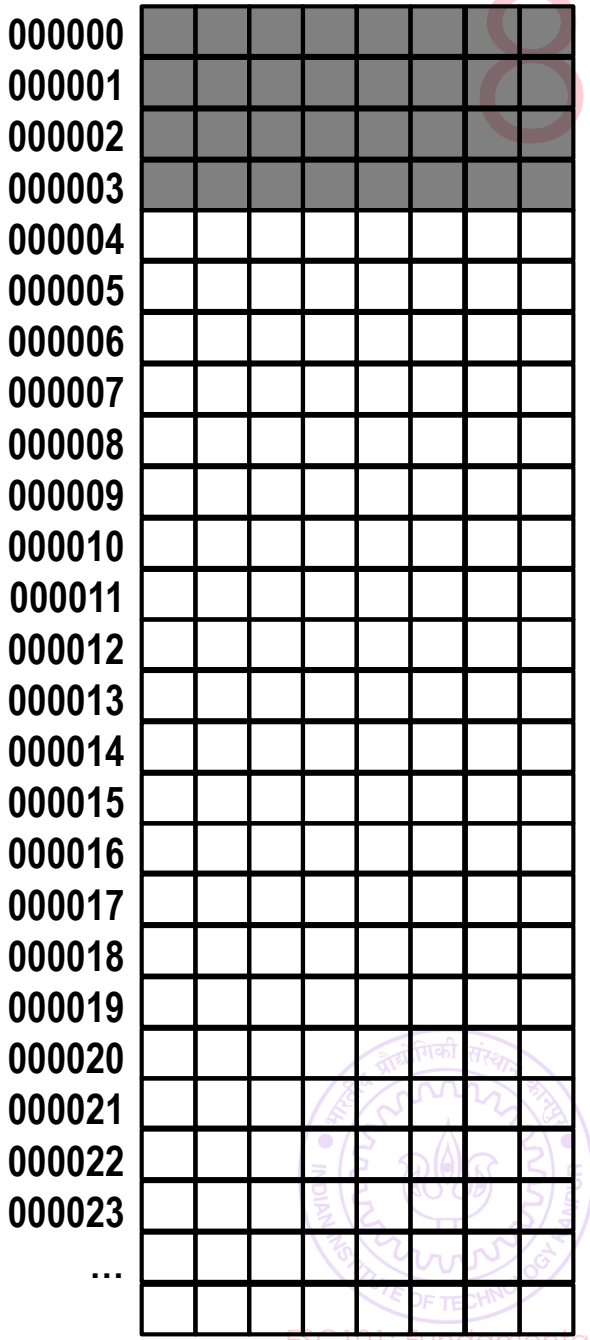

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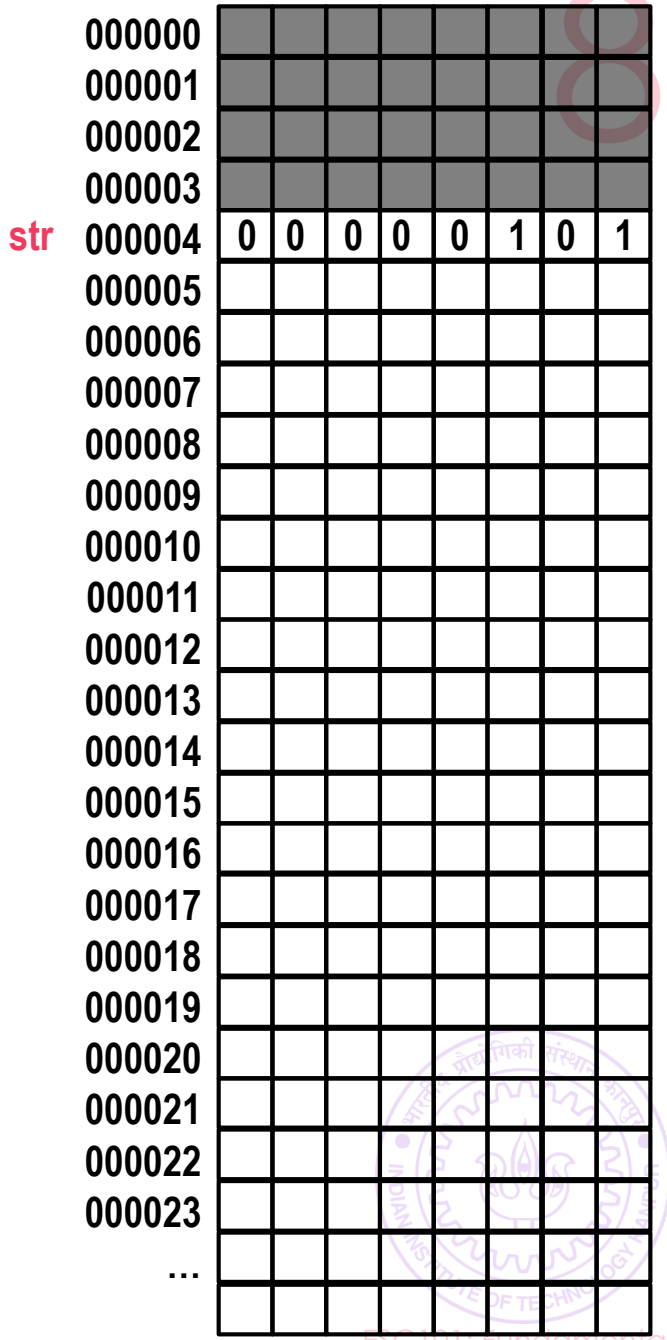

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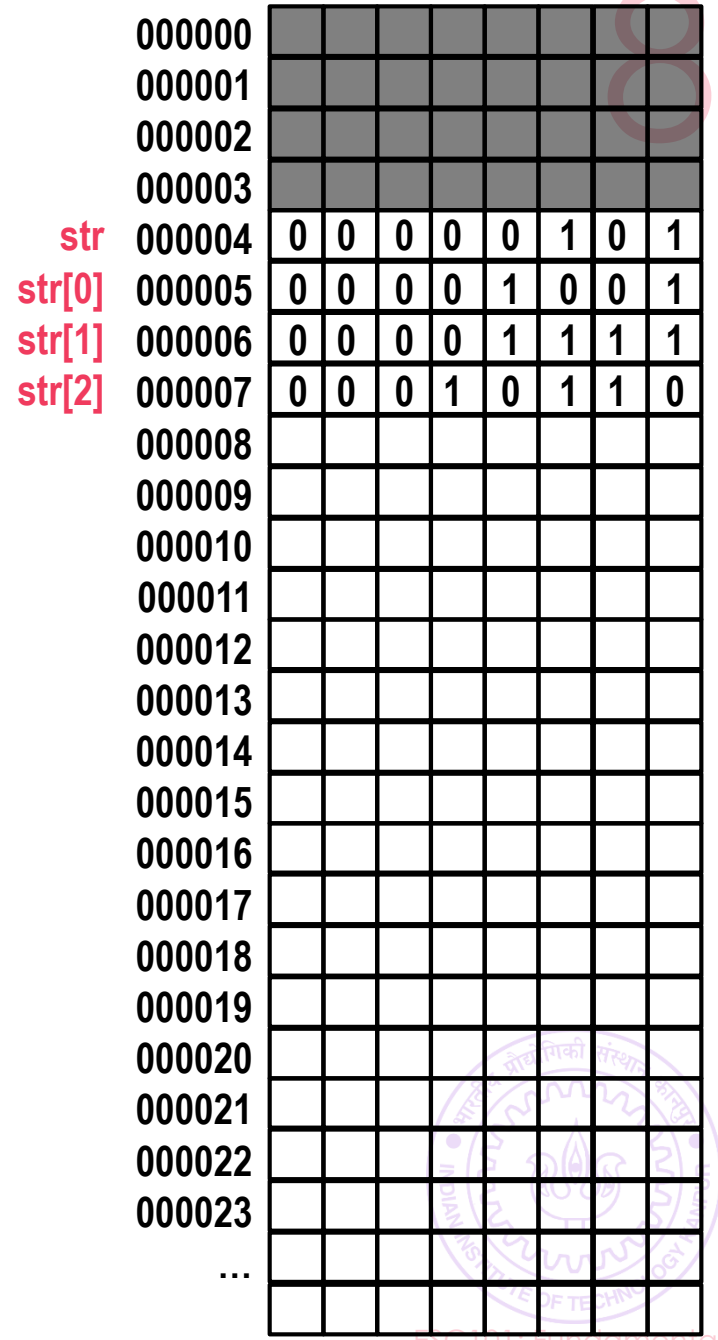

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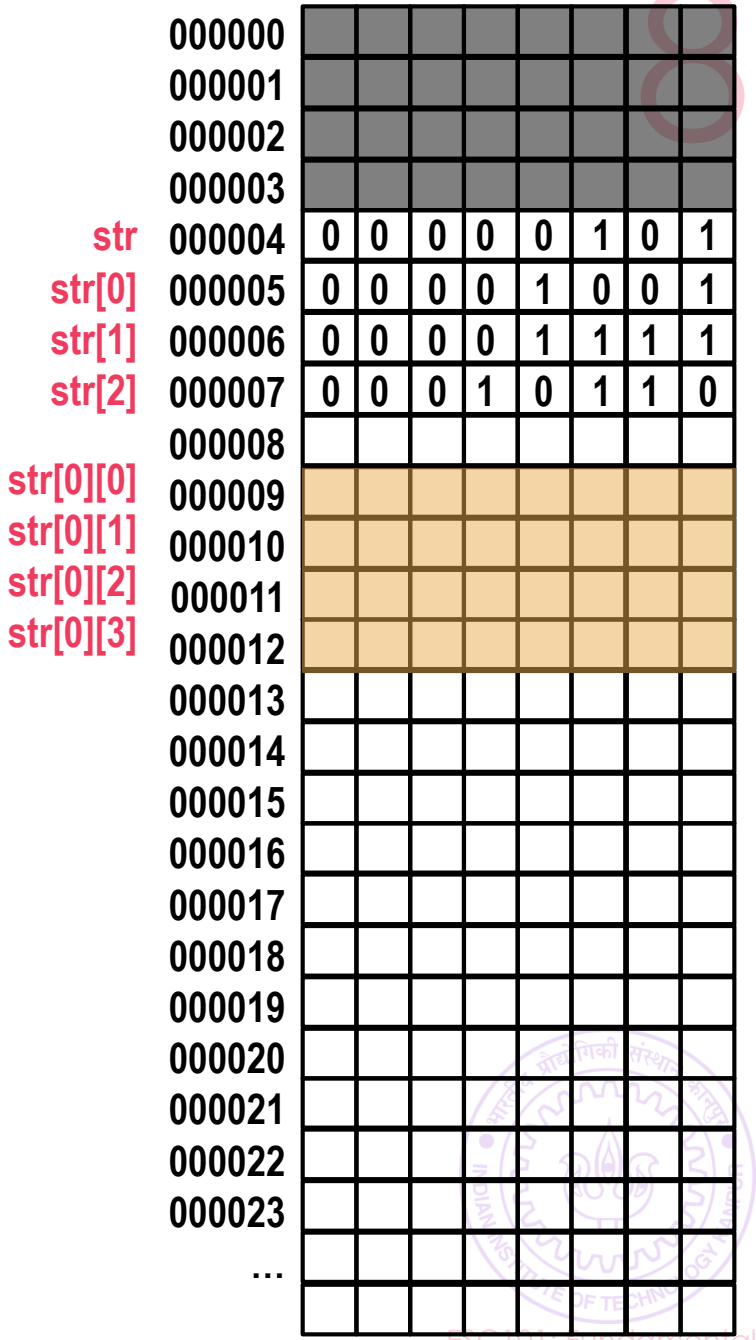

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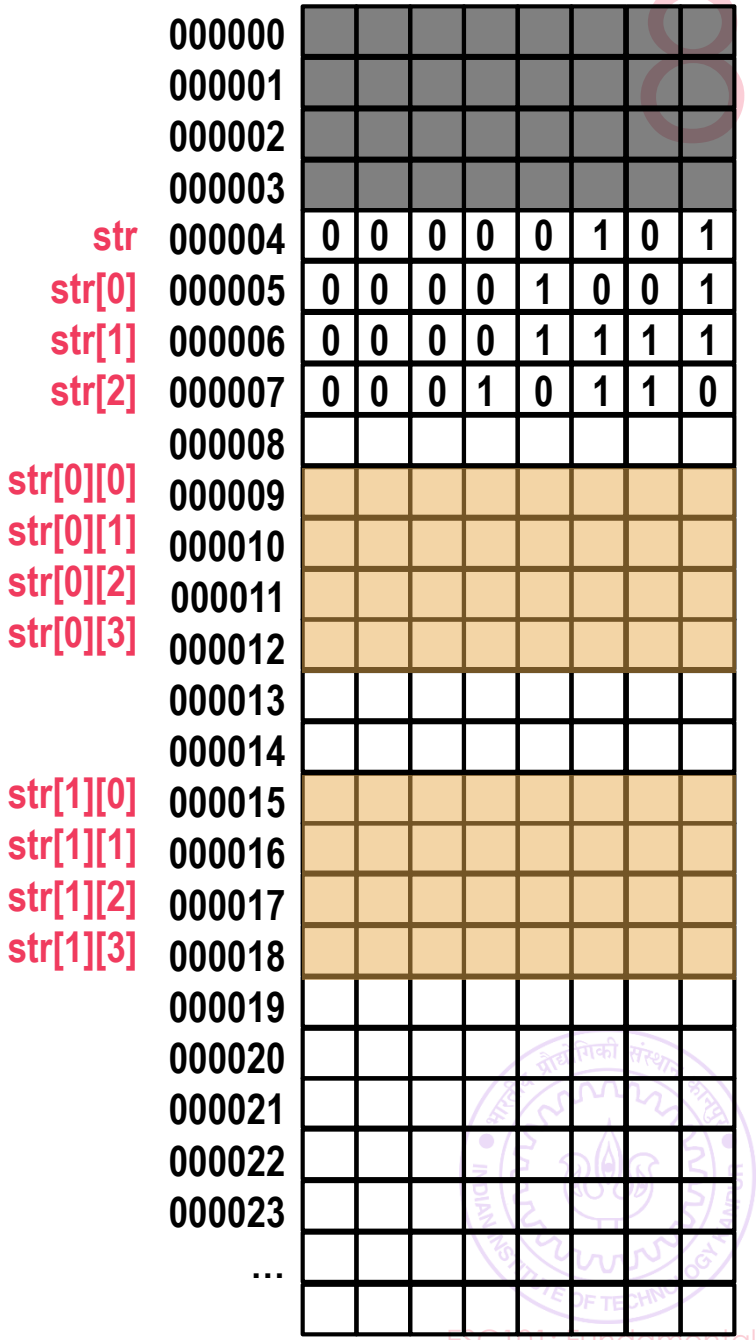

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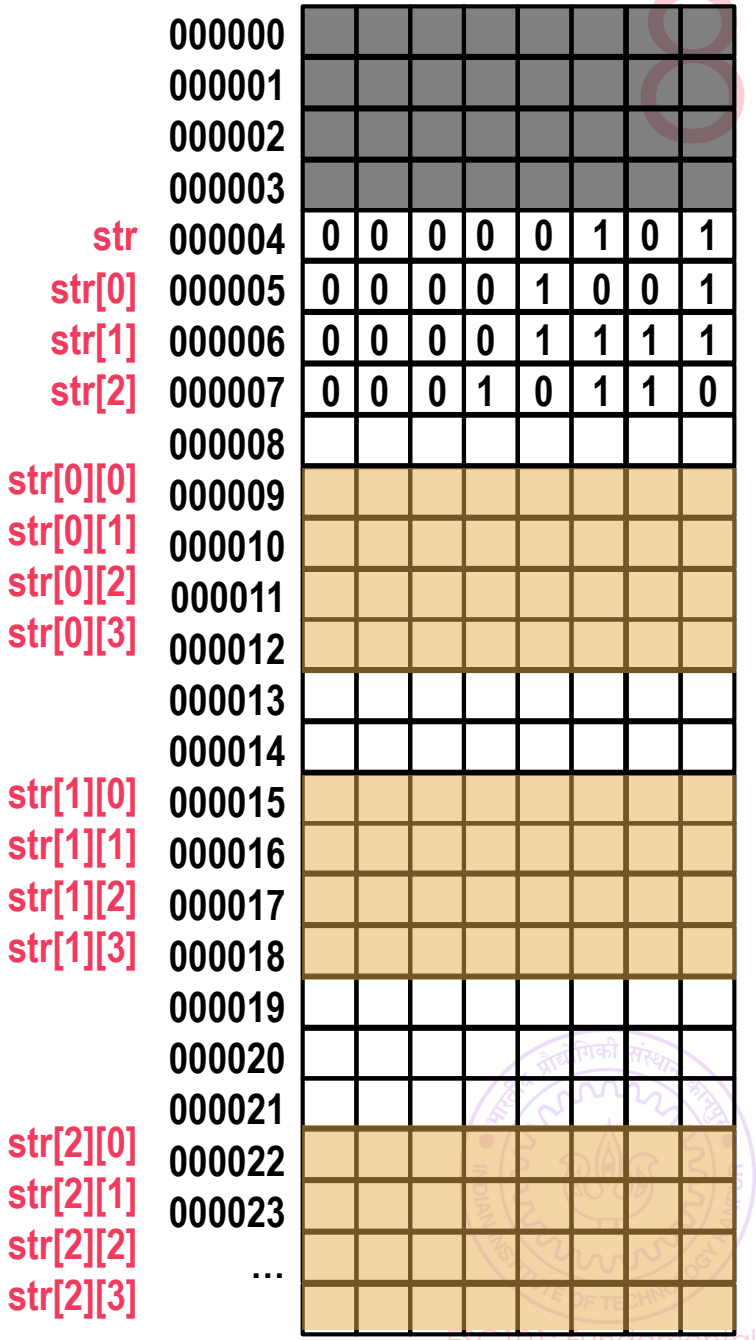

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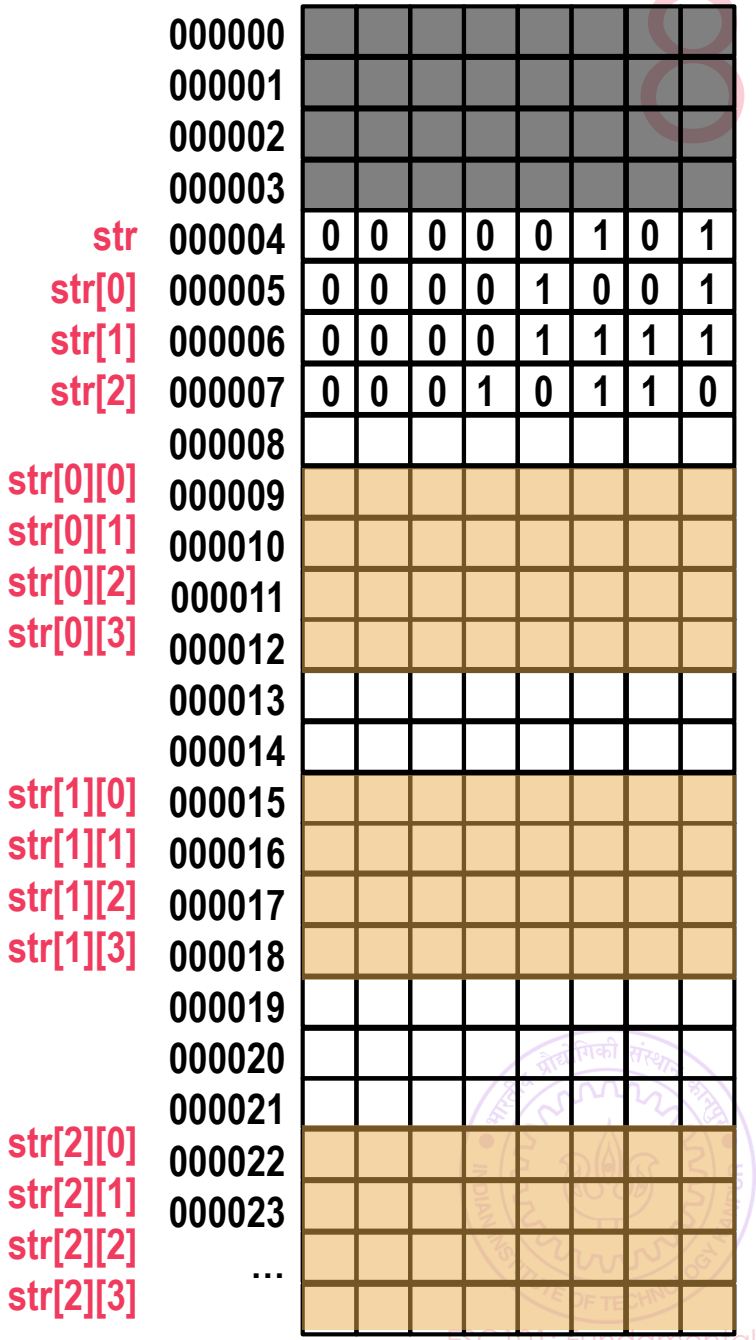
Element within a single array always stored in sequence



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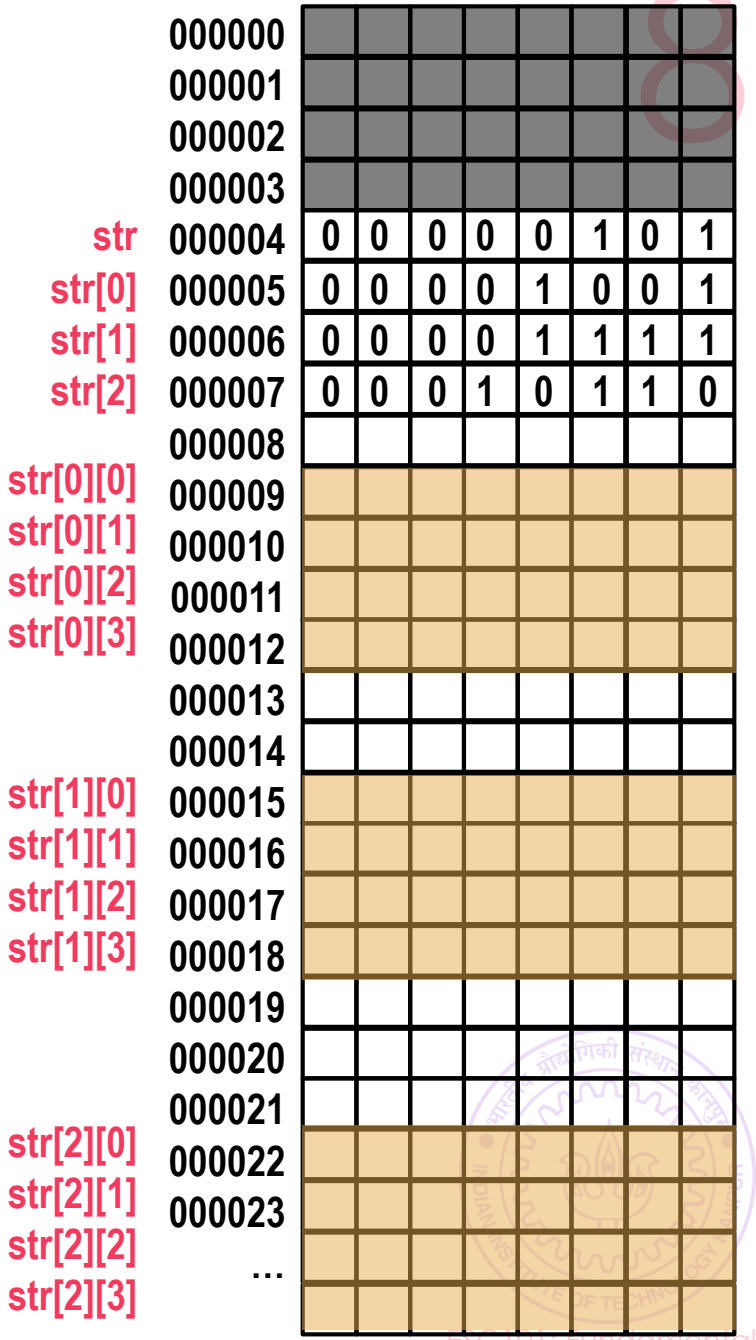
Element within a single array always stored in sequence

Different arrays may be stored far away from each other



Mr C takes a Math Lesson

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Mathematics is full of functions - we define more powerful functions using simple functions

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Although we can write tan(x) in terms of addition, subtraction, multiplication and division, we almost never do that. We always write tan(x) = sin(x)/cos(x)

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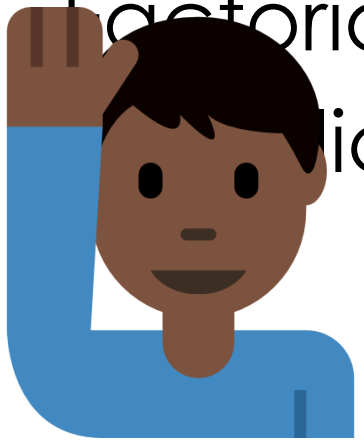

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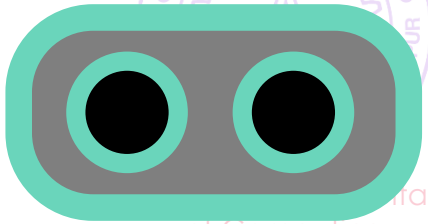

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I too allow you to write your own functions for your comfort and to make your code easier to read and easier to debug!