

Mr. C loves Round Trips

ESC101: Fundamentals of Computing

Purushottam Kar

Announcements - Quiz

- Major quiz **tomorrow** – (syllabus till **Friday Aug 24**)
 - Wednesday, August 29, 2018, 12PM-12:50PM, L20 (i.e. lecture hour)
 - During lecture hours – don't be absent
 - **Bring your institute ID card** with you – will lose time if you forget
 - No minor quizzes during lab this week (August 27-August 30)
- Bring a **pencil, eraser and sharpener** with you
 - Answers to be written on question paper itself and returned back
 - If you make a mistake with pen – no extra question papers
 - If unsure, **first write answer with pencil** and **finally write it in pen**
 - We WONT HAVE EXTRA QUESTION PAPERS in case you spoil yours
 - We WONT HAVE PENCILS, ERASERS in case you forget



Announcements - Holiday

- Institute holiday next Monday (03 September, 2018)
- No lecture, no lab on that day
- Extra lecture on Saturday 08 September, 2018
 - 12 noon, L20 (same as usual)
 - Scheduled by DoAA, not by me – I like to sleep on Sat too ☹
- Extra lab for B1, B2, B3 on Saturday 08 September
 - 2PM – 5PM, New Core Labs CC-02 (same as usual)



The for loop

4



The for loop

General form of a for loop

4



The for loop

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General form of a for loop

```
for(init_expr; stopping_expr; update_expr){  
    statement1;  
    statement2;  
    ...  
}  
statement3;  
statement4;  
...
```



The for loop

4

General form of a for loop

```
for(init_expr; stopping_expr; update_expr){
```

```
    statement1;
```

How we usually speak to a human

```
    statement2;
```

```
    ...
```

```
}
```

```
statement3;
```

```
statement4;
```

```
...
```



The for loop

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General form of a for loop

```
for(init_expr; stopping_expr; update_expr){
```

```
    statement1;
```

```
    statement2;
```

```
    ...
```

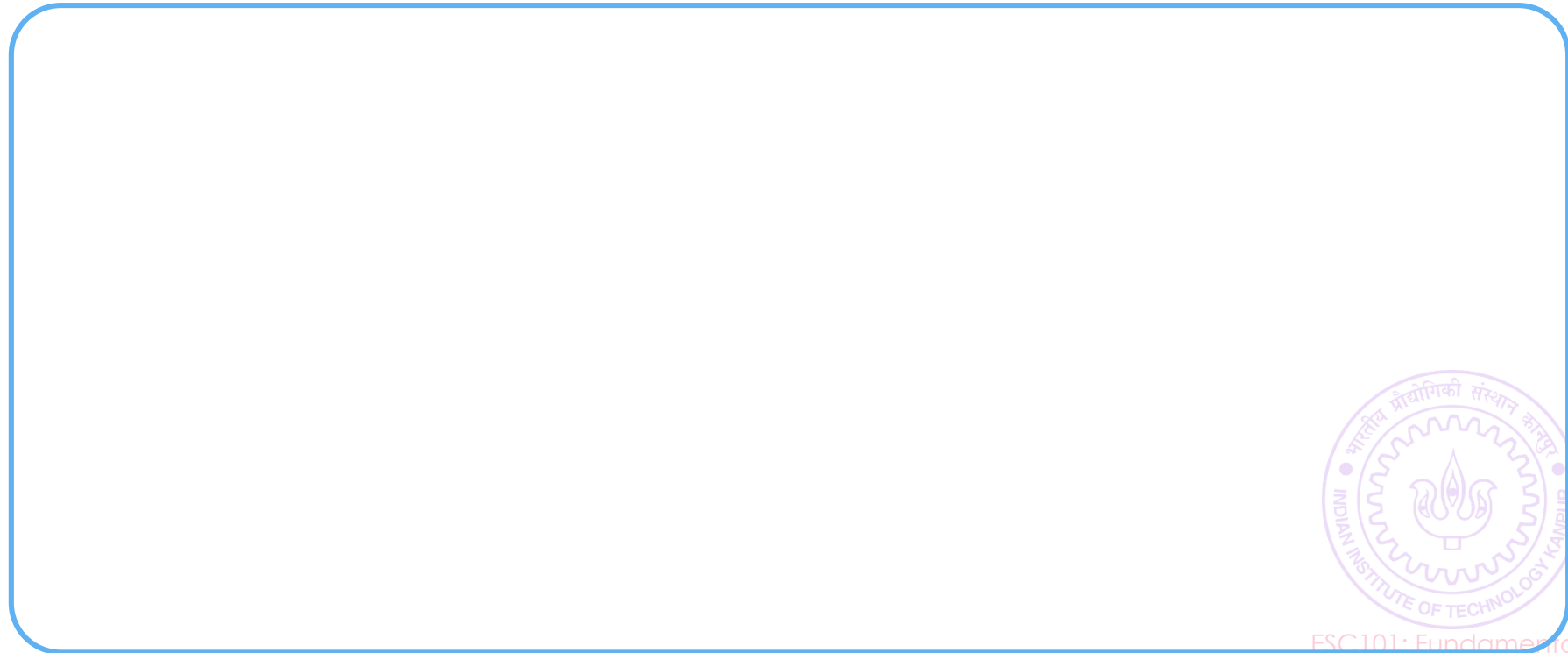
```
}
```

```
statement3;
```

```
statement4;
```

```
...
```

How we usually speak to a human



The for loop

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General form of a for loop

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    statement1;
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    ...
```

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statement3;
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statement4;
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```
...
```

How we usually speak to a human

1. First do what is told in initialization expression



The for loop

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General form of a for loop

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for(init_expr; stopping_expr; update_expr){
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```
    statement1;
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    statement2;
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```
    ...
```

```
}
```

```
statement3;
```

```
statement4;
```

```
...
```

How we usually speak to a human

1. First do what is told in **initialization expression**



The for loop

4

General form of a for loop

```
for(init_expr; stopping_expr; update_expr){  
    statement1;  
    statement2;  
    ...  
}  
statement3;  
statement4;  
...
```

How we usually speak to a human

1. First do what is told in **initialization expression**
2. Then check the stopping expression



The for loop

4

General form of a for loop

```
for(init_expr; stopping_expr; update_expr){  
    statement1;  
    statement2;  
    ...  
}  
statement3;  
statement4;  
...
```

How we usually speak to a human

1. First do what is told in initialization expression
2. Then check the stopping expression



The for loop

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General form of a for loop

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for(init_expr; stopping_expr; update_expr){  
    statement1;  
    statement2;  
    ...  
}  
statement3;  
statement4;  
...
```

How we usually speak to a human

1. First do what is told in initialization expression
2. Then check the stopping expression
3. If stopping expression is true



The for loop

4

General form of a for loop

```
for(init_expr; stopping_expr; update_expr){
```

```
    statement1;
```

```
    statement2;
```

```
    ...
```

```
}
```

```
statement3;
```

```
statement4;
```

```
...
```

How we usually speak to a human

1. First do what is told in **initialization expression**
2. Then check the **stopping expression**
3. If stopping expression is true
Execute all statements inside braces



The for loop

4

General form of a for loop

```
for(init_expr; stopping_expr; update_expr){
```

```
    statement1;  
    statement2;
```

```
    ...
```

```
}
```

```
statement3;
```

```
statement4;
```

```
...
```

How we usually speak to a human

1. First do what is told in initialization expression
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The for loop

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    statement1;  
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```
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statement3;  
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```

```
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How we usually speak to a human

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The for loop

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    statement1;  
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statement3;  
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```
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How we usually speak to a human

1. First do what is told in initialization expression
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The for loop

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General form of a for loop

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    statement1;  
    statement2;
```

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    ...
```

```
}
```

```
statement3;  
statement4;
```

```
...
```

How we usually speak to a human

1. First do what is told in initialization expression
2. Then check the stopping expression
3. If stopping expression is true
 - Execute all statements inside braces
 - Execute update expression
 - Go back to step 2



The for loop

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General form of a for loop

```
for(init_expr; stopping_expr; update_expr){
```

```
    statement1;  
    statement2;
```

```
    ...
```

```
}
```

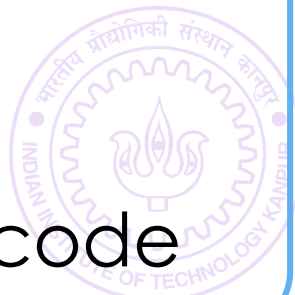
```
statement3;
```

```
statement4;
```

```
...
```

How we usually speak to a human

1. First do what is told in initialization expression
 2. Then check the stopping expression
 3. If stopping expression is true
 - Execute all statements inside braces
 - Execute update expression
 - Go back to step 2
- Else stop looping and execute rest of code



The for loop

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General form of a for loop

```
for(init_expr; stopping_expr; update_expr){
```

```
    statement1;  
    statement2;
```

```
    ...
```

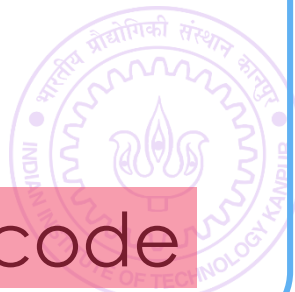
```
}
```

```
    statement3;  
    statement4;
```

```
    ...
```

How we usually speak to a human

1. First do what is told in initialization expression
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The for loop

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General form of a for loop

```
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```

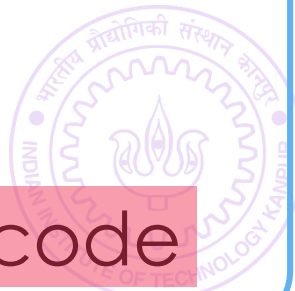
```
statement1;  
statement2;  
...
```

```
}
```

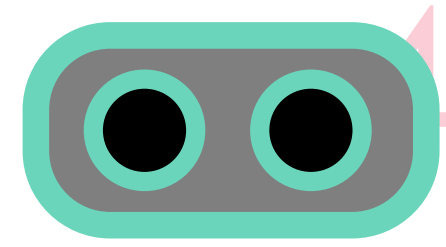
```
statement3;  
statement4;  
...
```

How we usually speak to a human

1. First do what is told in initialization expression
2. Then check the stopping expression
3. If stopping expression is true
 - Execute all statements inside braces
 - Execute update expression
 - Go back to step 2
- Else stop looping and execute rest of code



The for loop



General form of a for loop

```
for(init_expr; stopping_expr; update_expr) {
```

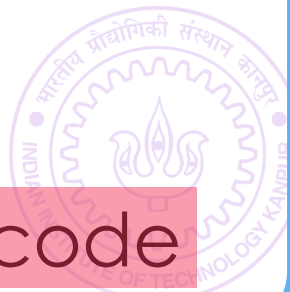
```
statement1;  
statement2;  
...
```

```
}
```

```
statement3;  
statement4;  
...
```

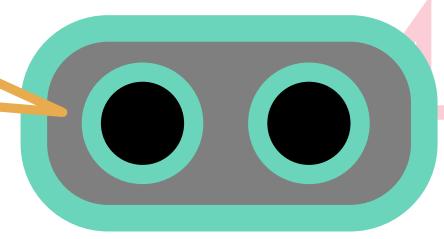
How we usually speak to a human

1. First do what is told in **initialization expression**
2. Then check the **stopping expression**
3. If stopping expression is true
 - Execute **all statements inside braces**
 - Execute **update expression**
 - Go back to step 2
- Else stop looping and execute **rest of code**



The for loop

Brackets essential if you want me to do many things while looping



General form of a for loop

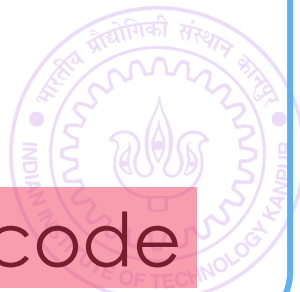
```
for(init_expr; stopping_expr; update_expr){
```

```
statement1;  
statement2;  
...
```

How we usually speak to a human

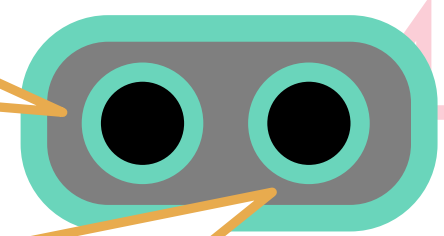
1. First do what is told in initialization expression
 2. Then check the stopping expression
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```
}  
statement3;  
statement4;  
...
```



The for loop

Brackets essential if you want me to do many things while looping



General form of a for loop

```
for(init_expr; stopping_expr; update_
```

Each time I execute the statements inside the braces – called one *iteration* of the loop

```
statement1;  
statement2;
```

How we usually speak to a human

```
...
```

```
}
```

```
statement3;  
statement4;
```

```
...
```

1. First do what is told in **initialization expression**

2. Then check the **stopping expression**

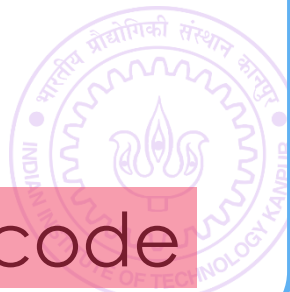
3. If stopping expression is true

Execute **all statements inside braces**

Execute **update expression**

Go back to step 2

Else stop looping and execute **rest of code**



Some useful Tips for using Loops

5



Some useful Tips for using Loops

5

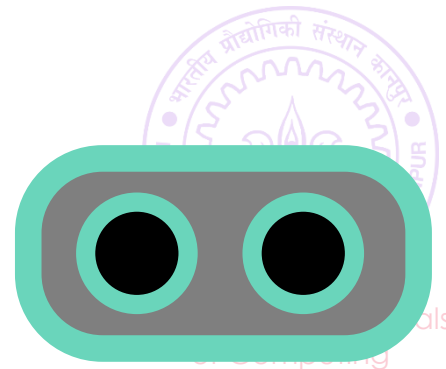
Read the problem carefully and identify some tasks that have to be repeated again and again



Some useful Tips for using Loops

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Read the problem carefully and identify some tasks that have to be repeated again and again

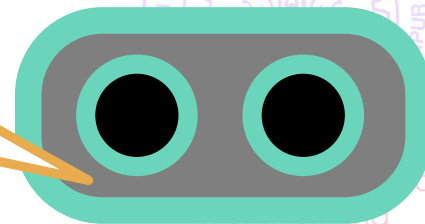


Some useful Tips for using Loops

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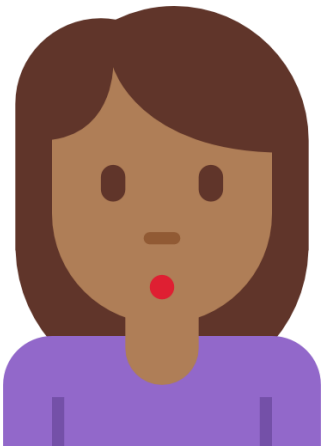
The tasks may be slightly different from each other



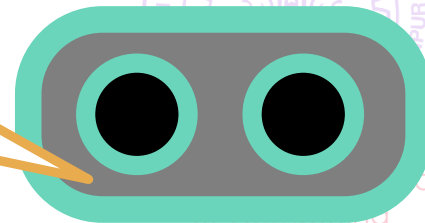
Some useful Tips for using Loops

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Some useful Tips for using Loops

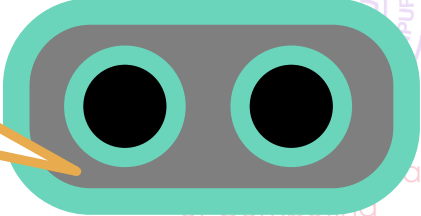
5

Read the problem carefully and identify some tasks that have to be repeated again and again



Yes, in the multiplication table example, the tasks were slightly different. First print $2 \times 1 = 2$, then print $2 \times 2 = 4$ etc etc.

The tasks may be slightly different from each other



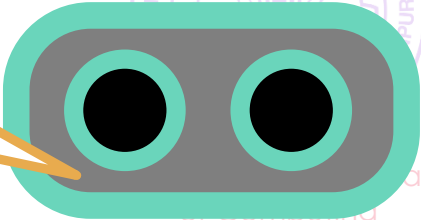
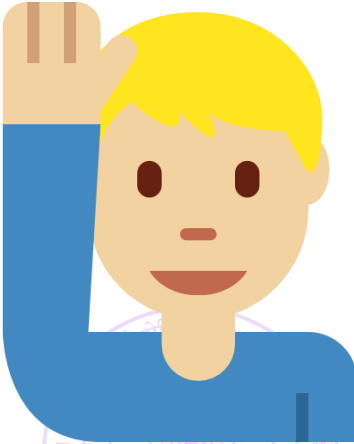
Some useful Tips for using Loops

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Some useful Tips for using Loops

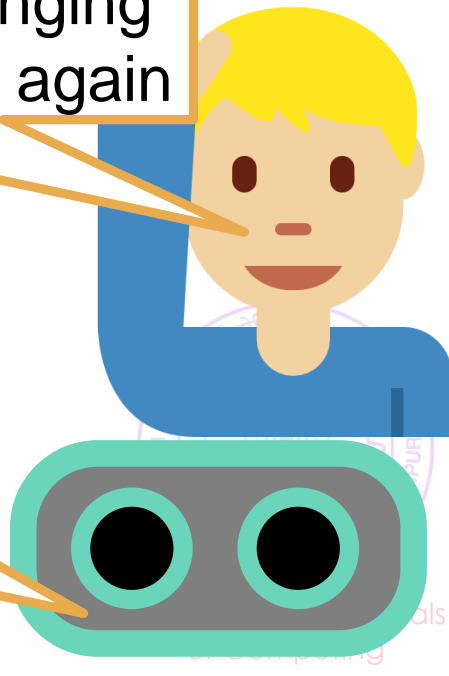
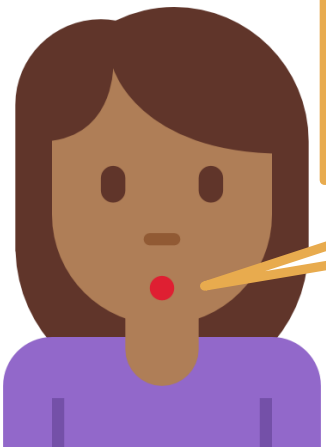
5

Read the problem carefully and identify some tasks that have to be repeated again and again

Yes, but we could write the same code
`printf("%d x %d = %d\n", a, b, a*b);`
to do all the tasks by simply changing
the value of variable b again and again

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Some useful Tips for using Loops

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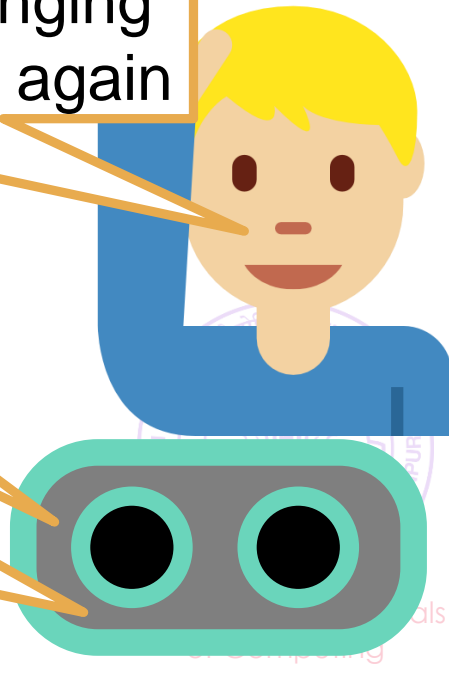
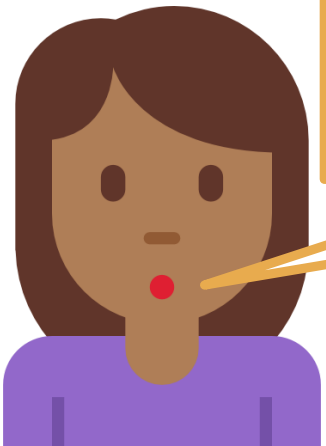
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Very Good!

The tasks may be slightly
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Some useful Tips for using Loops

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Read the problem carefully and identify some tasks that have to be repeated again and again

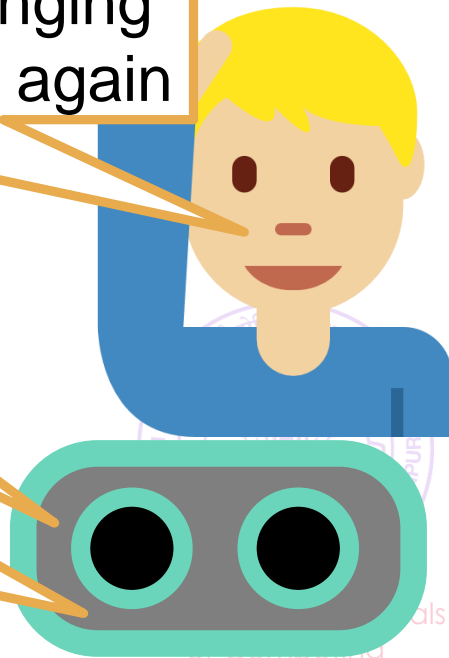
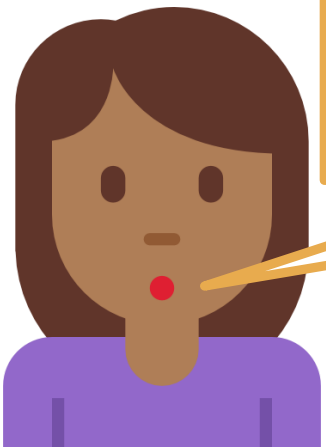
Use this variable that is changing as the variable of loop

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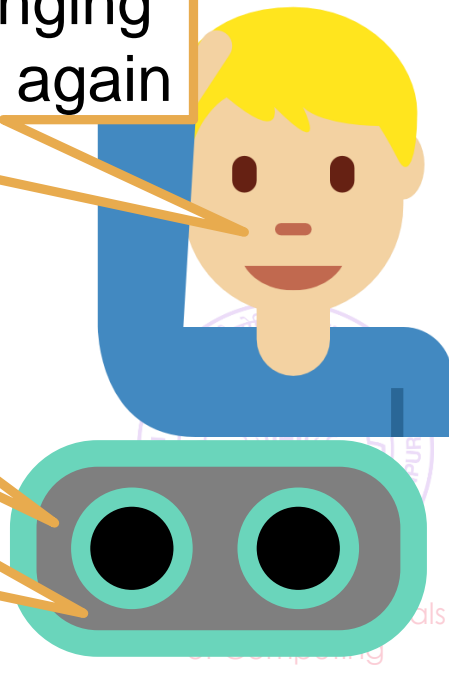
```
int a = 2, b;  
for(b = 1; b <= 10; b++){  
    printf("%d x %d = %d\n", a, b, a*b);  
}
```

Yes, but we could write the same code
`printf("%d x %d = %d\n", a, b, a*b);`
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Yes, in the multiplication table example,
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The tasks may be slightly
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When loops are not very useful

6



When loops are not very useful

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Read a number then print a number, then read another number and then print it – repeat 100 times



When loops are not very useful

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Read a number then print a number, then read another number and then print it – repeat 100 times

Loops are very very useful for problems like the above



When loops are not very useful

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Read a number then print a number, then read another number and then print it – repeat 100 times

Loops are very very useful for problems like the above

Read a number then print it, then calculate the 4th power of 20, then print the string “Hello World”, then read another number, then add it to the first number, then print the string “Bye” and then calculate $\log(\text{first number})$, then calculate $\sin(\text{second number})$



When loops are not very useful

6

Read a number then print a number, then read another number and then print it – repeat 100 times

Loops are very very useful for problems like the above

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Long list of tasks but no structure, no repeated pattern



When loops are not very useful

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Read a number then print a number, then read another number and then print it – repeat 100 times

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Read a number then print it, then calculate the 4th power of 20, then print the string “Hello World”, then read another number, then add it to the first number, then print the string “Bye” and then calculate $\log(\text{first number})$, then calculate $\sin(\text{second number})$

Long list of tasks but no structure, no repeated pattern

Loops are not very useful for the above problem



Print sum of reciprocals of $1, 2 \dots n$

7



Print sum of reciprocals of 1, 2 ... n 7

Take $n \geq 1$ from the user and give as output



Print sum of reciprocals of 1, 2 ... n 7

Take $n \geq 1$ from the user and give as output

$$\frac{1}{1} + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{n}$$



Print sum of reciprocals of 1, 2 ... n 7

Take $n \geq 1$ from the user and give as output

$$\frac{1}{1} + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{n}$$

The repeating task can be



Print sum of reciprocals of 1, 2 ... n 7

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The repeating task can be

Given the sum of first $i-1$ reciprocals and add $\frac{1}{i}$ to it



Print sum of reciprocals of 1, 2 ... n 7

Take $n \geq 1$ from the user and give as output

$$\frac{1}{1} + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{n}$$

The repeating task can be

Given the sum of first $i-1$ reciprocals and add $\frac{1}{i}$ to it

Define a variable (lets call it **sum**) to store partial sums



Print sum of reciprocals of 1, 2 ... n 7

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Lovingly called *partial sums* or *running sums*

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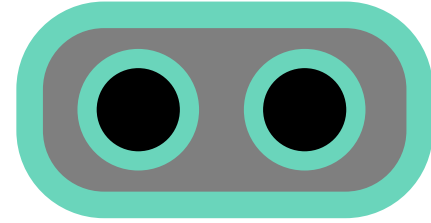
```
sum = sum + 1/i;
```

Lovingly called *partial sums* or *running sums*

Print sum of reciprocals of 1, 2 ... n 7

Take $n \geq 1$ from the user and give as output

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Oops! Integer division!

The repeating task can be

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Define a variable (lets call it **sum**) to store partial sums

The above task is accomplished by the code

```
sum = sum + 1.0/i;
```

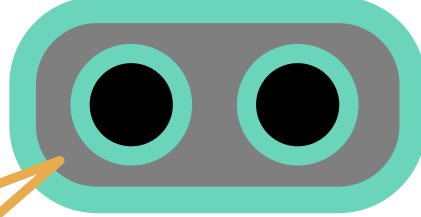
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The repeating task can be

Given the sum of first $i-1$ reciprocals and add $\frac{1}{i}$ to it

Define a variable (lets call it **sum**) to store partial sums

The above task is accomplished by the code

```
sum = sum + 1.0/i;
```

```
sum = sum + (double)1/i;
```

Lovingly called *partial sums* or *running sums*



Loop Invariants

8



Loop Invariants

8

Notice that in previous example



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At the beginning of i -th iteration, sum stored the value



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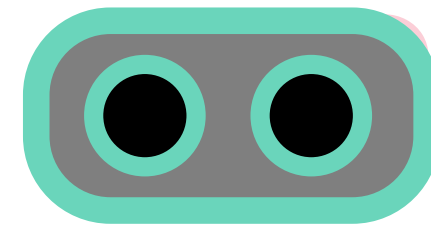
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These are known as *loop invariants* – few nice properties that hold for all iterations of a loop



Loop Invariants



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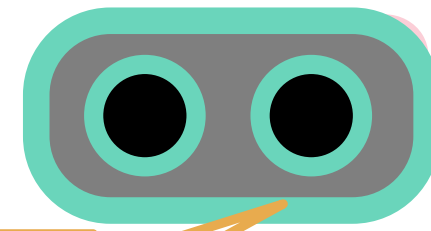
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Loop Invariants



Notice that in previous examples, we used loop invariants. Loop invariants are powerful ways to ensure that your loop code is correct!

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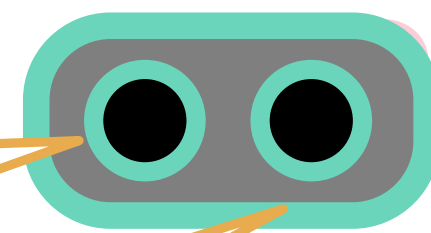
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Loop Invariants

Very important once loops get more complicated



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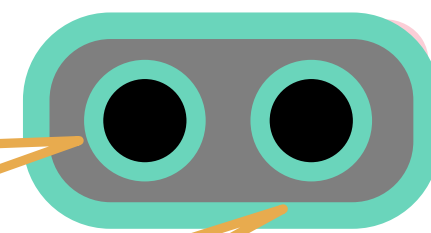
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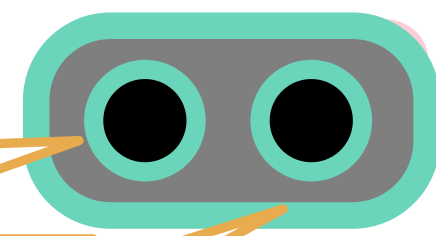
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Quiz: what is loop invariant in multiplication table code?



Loop Invariants

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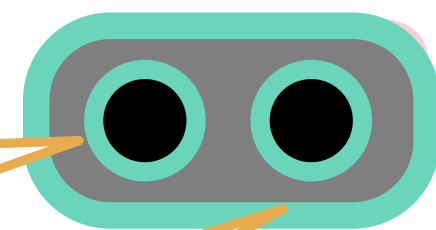
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In i -th iteration the string
 $2 \times i = 2i$ will get printed



the iteration with $i = 1$, sum stored 0

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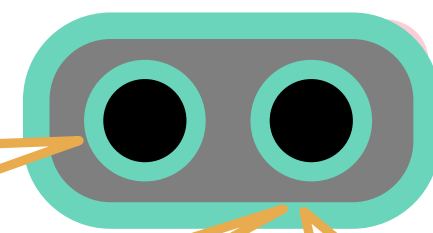
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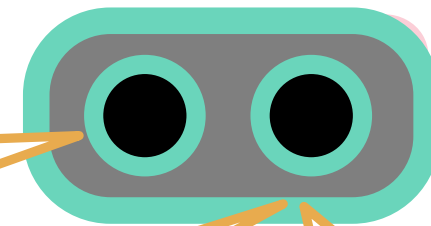
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Exercise 1: sum of reciprocals of the first n even numbers

Exercise 2*: sum of reciprocals of the first n prime numbers

Quiz: what is loop invariant for the following code?

From running sums to running counts



From running sums to running counts

Read n from input, then scan n numbers, and print how many numbers were divisible by 3 or divisible by 5



From running sums to running counts

Read n from input, then scan n numbers, and print how many numbers were divisible by 3 or divisible by 5

Repeating task seems to be



From running sums to running counts

Read n from input, then scan n numbers, and print how many numbers were divisible by 3 or divisible by 5

Repeating task seems to be

*Given the count of numbers div by 3 or 5 till now,
read another number and add 1 to count if div by 3 or 5*



From running sums to running counts

Read n from input, then scan n numbers, and print how many numbers were divisible by 3 or divisible by 5

Repeating task seems to be

Given the count of numbers div by 3 or 5 till now, read another number and add 1 to count if div by 3 or 5

Here, we can use a variable (lets call it **count**) to store the *running count* of numbers div by 3 or 5 seen till now



From running sums to running counts?

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From running sums to running counts

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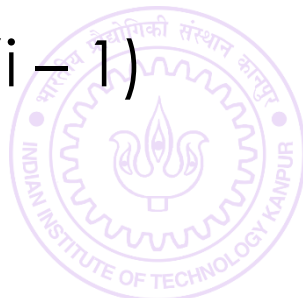
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Here, we can use a variable (lets call it **count**) to store the *running count* of numbers div by 3 or 5 seen till now

Loop invariants

At the beginning of i -th iteration, count stores how many of the first $(i - 1)$ numbers were divisible by 3 or divisible by 5



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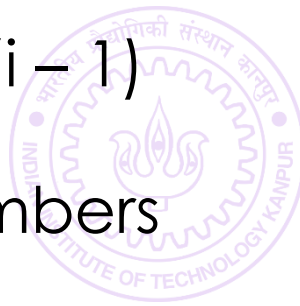
Given the count of numbers div by 3 or 5 till now, read another number and add 1 to count if div by 3 or 5

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Loop invariants

At the beginning of i -th iteration, count stores how many of the first $(i - 1)$ numbers were divisible by 3 or divisible by 5

After the i -th iteration is over, count stores how many of the first i numbers were divisible by 3 or divisible by 5



The while loop

10



The while loop

10

Remember that we could write fancy for loops where `init_expr` and `update_expr` were empty?



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If we do the above, we had to write the `init_expr` before starting the for loop and write `update_expr` inside loop



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There is a much neater way to write the above



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If we do the above, we had to write the `init_expr` before starting the for loop and write `update_expr` inside loop

There is a much neater way to write the above

```
while(stopping_expr){  
    statement1;  
    statement2;  
}
```



The while loop

11



The while loop

General form of a while loop

11



The while loop

11

General form of a while loop

```
while(stopping_expr){  
    statement1;  
    statement2;  
    ...  
}  
statement3;  
statement4;  
...
```



The while loop

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General form of a while loop

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    statement1;
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```
    ...
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How we usually speak to a human



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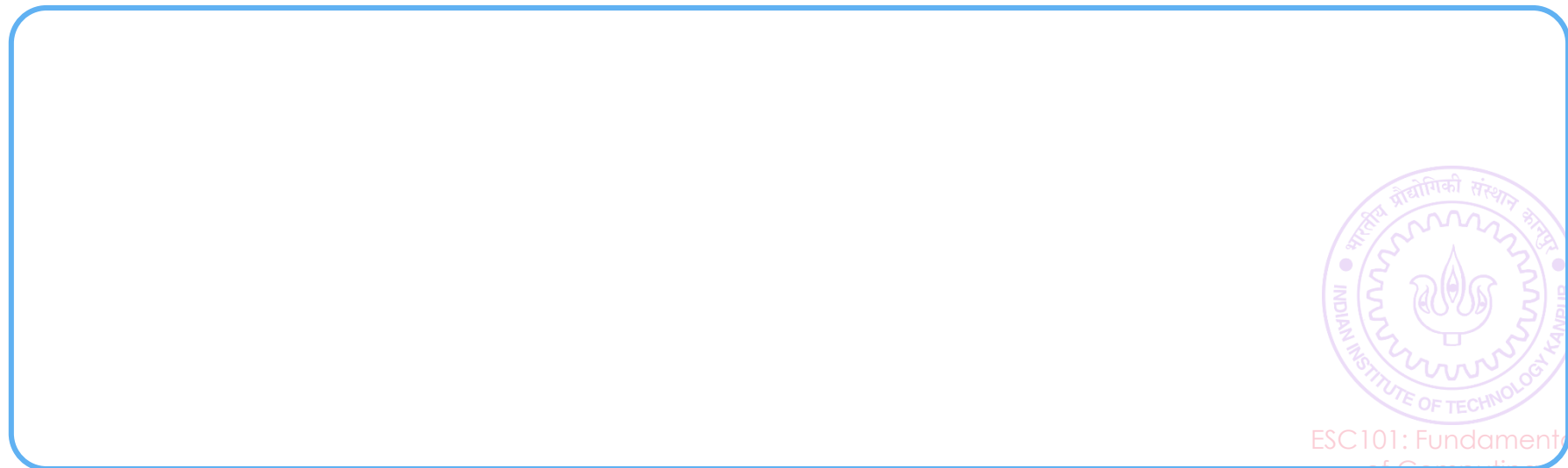
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How we usually speak to a human

1. First check the stopping expression



The while loop

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How we usually speak to a human

1. First check the stopping expression
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Execute all statements inside braces



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How we usually speak to a human

1. First check the stopping expression
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Execute all statements inside braces
Go back to step 2



The while loop

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How we usually speak to a human

1. First check the stopping expression
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 - Else stop looping and execute rest of code

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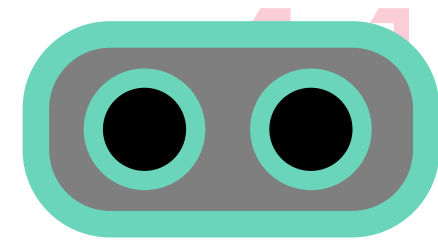
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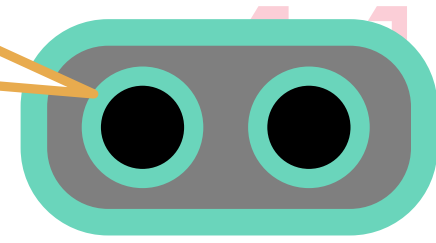
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The while loop

Brackets essential if you want me to do many things while looping



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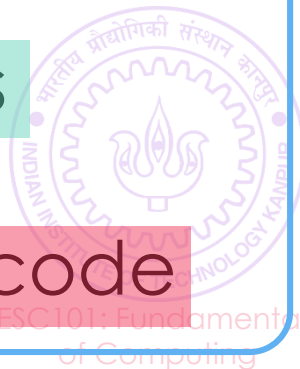
1. First check the stopping expression

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Execute all statements inside braces

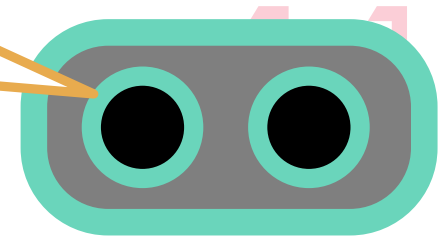
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The while loop

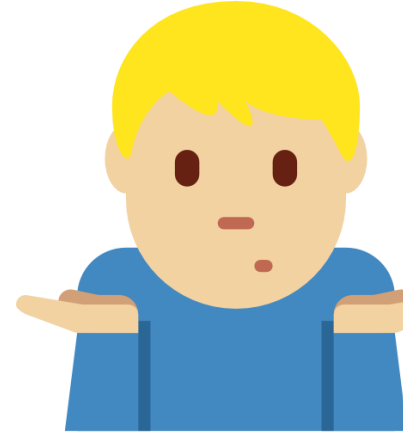
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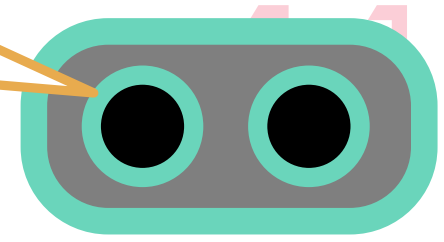
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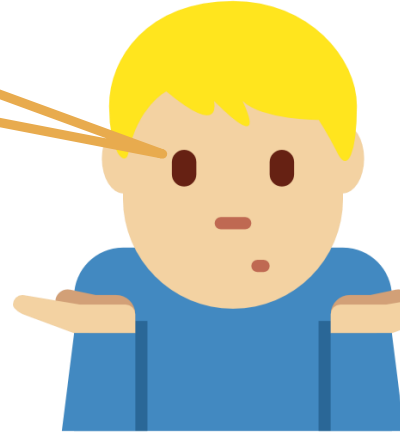
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So what is the difference between for and while?



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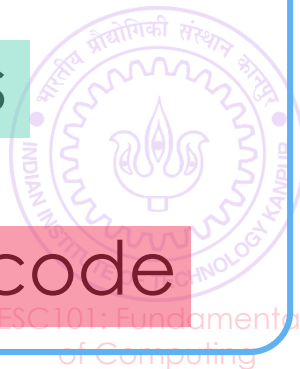
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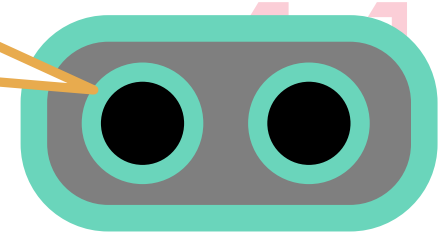
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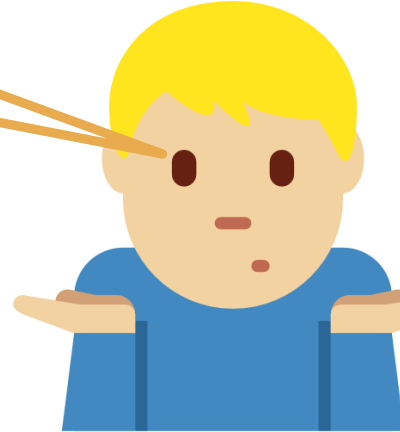
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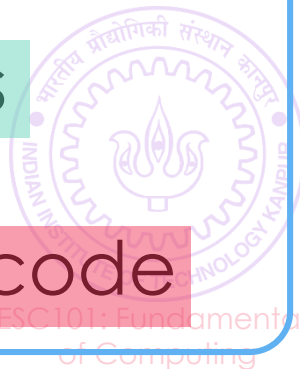
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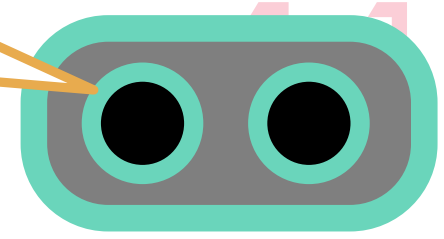
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The while loop

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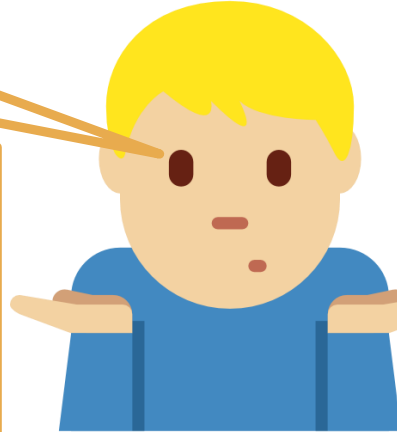
General form of a while loop

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statement1;  
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...
```

So what is the difference between for and while?

In general not much – it is a matter of style. Use while when you don't know how many iterations will loop run



How we usually speak to a human

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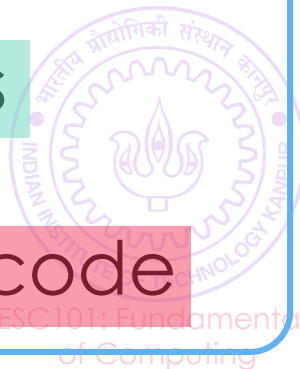
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Scanning a list of numbers

12



Scanning a list of numbers

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Read integers from the input till you read the number -1
and print the sum of all numbers except the -1



Scanning a list of numbers

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Here, number of iterations is not given to us as it was in the divisible-by-3-or-5 or reciprocal sum examples



Scanning a list of numbers

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Use a variable (lets call it **sum**) to store partial sums



Scanning a list of numbers

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Use a variable (lets call it **sum**) to store partial sums

Even while loops have invariants



Scanning a list of numbers

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Read integers from the input till you read the number -1 and print the sum of all numbers except the -1

Here, number of iterations is not given to us as it was in the divisible-by-3-or-5 or reciprocal sum examples

Use a variable (lets call it **sum**) to store partial sums

Even while loops have invariants

At the beginning of i -th iteration, sum will store sum of first $(i - 1)$ numbers



Scanning a list of numbers

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Usually if you can find a nice clear variable of loop, try using for loops



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Exercise 1: read integers till -1, print sum of all primes in the list

Exercise 2*: read integers till -1, print sum of all numbers greater than the number encountered just before that number