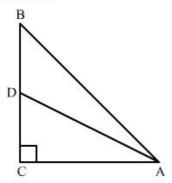


## Triangles Ex 4.7 Q18 Answer:

 $\triangle$ ABC is a right-angled triangle with  $\angle$ C = 90°. D is the mid-point of BC.

We need to prove that  $AB^2 = 4AD^2 - 3AC^2$ . Join AD.



Since D is the midpoint of the side BC, we get

BD = DC

$$\therefore BC = 2DC$$

Using Pythagoras theorem in triangles right angled triangle ABC

$$AB^2 = AC^2 + BC^2$$

$$AB^2 = AC^2 + (2DC)^2$$

$$AB^2 = AC^2 + 4DC^2 \qquad \dots (1)$$

Again using Pythagoras theorem in the right angled triangle ADC

$$AD^2 = AC^2 + DC^2$$

$$DC^2 = AD^2 - AC^2$$
 .....(2)

From (1) and (2), we get

$$AB^2 = AC^2 + 4(AD^2 - AC^2)$$

$$AB^2 = AC^2 + 4AD^2 - 4AC^2$$

$$AB^2 = 4AD^2 - 3AC^2$$

Hence, 
$$AB^2 = 4AD^2 - 3AC^2$$

Triangles Ex 4.7 Q19

## Answer:

(i) It is given that D is the midpoint of BC and BC = a.

Therefore, 
$$BD = DC = \frac{a}{2}$$
....(1)

Using Pythagoras theorem in the right angled triangle AED,

$$AD^2 = AE^2 + ED^2 \cdot \dots (2)$$

Let us substitute AD = p, AE = h and ED = x in equation (2), we get

$$p^2 = h^2 + x^2$$

Let us take another right angled triangle that is triangle AEC.

Using Pythagoras theorem,

$$AC^2 = AE^2 + EC^2$$
 .....(3)

Let us substitute AE = h and  $EC = x + \frac{a}{2}$  in equation (3) we get,

Here we know that  $DC = \frac{a}{2}$  and ED = x.

$$EC = ED + DC$$

Substituting AC = b,  $DC = \frac{a}{2}$  and ED = x we get  $EC = \left(x + \frac{a}{2}\right)$ 

$$b^2 = h^2 + \left(x + \frac{a}{2}\right)^2$$

$$b^2 = h^2 + x^2 + xa + \frac{a^2}{4}$$
 .....(4)

From equation (1) we can substitute  $h^2 + x^2 = p^2$  in equation (4),

$$b^2 = h^2 + x^2 + xa + \frac{a^2}{4}$$
 .....(5)

(ii) Using Pythagoras theorem in right angled triangle AEB,

$$AB^2 = AE^2 + BE^2 - (6)$$

We know that AB = c and AE = h now we will find BE.

$$BD = BE + ED$$

Therefore, BE = BD - ED

We know that  $BD = \frac{a}{2}$  and ED = x substituting these values in BE = BD - ED we get,

$$BE = \frac{a}{2} - x$$

Now we will substitute AB = c, AE = h and  $BE = \frac{a}{2} - x$  in equation (6) we get,

$$c^2 = h^2 + \left(\frac{a}{2} - x\right)^2$$

$$c^2 = h^2 + \frac{a^2}{4} - ax + x^2$$
 .....(7)

Let us rewrite the equation (7) as below,

$$c^2 = h^2 + x^2 + \frac{a^2}{4} - ax$$
 .....(8)

From equation (1) we can substitute  $h^2 + x^2 = p^2$  in equation (8),

$$c^2 = p^2 + \frac{a^2}{4} - ax$$

$$c^2 = p^2 - ax + \frac{a^2}{4} - \dots (9)$$

(iii) Now we will add equations (5) and (9) as shown below,

$$b^2 + c^2 = p^2 + xa + \frac{a^2}{4} + p^2 - ax + \frac{a^2}{4}$$

$$b^2 + c^2 = p^2 + \frac{a^2}{4} + p^2 + \frac{a^2}{4}$$

$$b^2 + c^2 = 2p^2 + \frac{a^2}{2}$$

Therefore, 
$$b^2 + c^2 = 2p^2 + \frac{a^2}{2}$$
.

\*\*\*\*\*\*\* END \*\*\*\*\*\*\*\*