

Question 26:

$$\frac{3 \tan 25^{\circ} \tan 40^{\circ} \tan 50^{\circ} \tan 65^{\circ} - \frac{1}{2} \tan^{2} 60^{\circ}}{4 \left(\cos^{2} 29^{\circ} + \cos^{2} 61^{\circ}\right)}$$

$$= \frac{3 \tan 25^{\circ} \tan 40^{\circ} \tan (90^{\circ} - 40^{\circ}) \tan (90^{\circ} - 25^{\circ}) - \frac{1}{2} \times \left(\sqrt{3}\right)^{2}}{4 \left[\cos^{2} 29^{\circ} + \cos^{2} (90^{\circ} - 29^{\circ})\right]}$$

$$= \frac{3 \tan 25^{\circ} \tan 40^{\circ} \cot 40^{\circ} \cot 25^{\circ} - \frac{3}{2}}{4 \left(\cos^{2} 29^{\circ} + \sin^{2} 29^{\circ}\right)}$$

$$\left[\because \cos^{2} \theta + \sin^{2} \theta = 1\right]$$

$$= \frac{3 \times \tan 25^{\circ} \times \tan 40^{\circ} \times \frac{1}{\tan 40^{\circ}} \times \frac{1}{\tan 25^{\circ}} - \frac{3}{2}}{4 \times 1}$$

$$= \frac{3 - \frac{3}{2}}{4} = \frac{3}{2} \times \frac{1}{4} = \frac{3}{8}$$

Question 27:

$$\frac{2}{3}\csc^2 58^\circ - \frac{2}{3}\cot 58^\circ \tan 32^\circ$$

$$-\frac{5}{3}\tan 13^\circ \tan 37^\circ \tan 45^\circ \tan 53^\circ \tan 77^\circ$$

$$=\frac{2}{3}\csc^2 58^\circ - \frac{2}{3}\cot 58^\circ \tan (90^\circ - 58^\circ)$$

$$-\frac{5}{3}\tan 13^\circ \tan 37^\circ \times 1 \times \tan (90^\circ - 37^\circ)\tan (90^\circ - 13)$$

$$=\frac{2}{3}(\cos \sec^2 58^\circ - \cot^2 58^\circ) - \frac{5}{3}(\tan 13^\circ \cot 13^\circ) \times (\tan 37^\circ \cot 37^\circ)$$

$$\left[\text{But } \csc^2 \theta - \cot^2 \theta = 1, \tan \theta \cot \theta = 1\right]$$

$$=\frac{2}{3}\times 1 - \frac{5}{3}\times 1\times 1 = \frac{2}{3} - \frac{5}{3} = -1$$

\*\*\*\*\*\*\* END \*\*\*\*\*\*