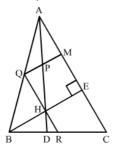


## Quadrilaterals Ex 14.4 Q10

 $\Delta ABC$  is given with  $BE \perp AC$ AD is any line from A to BC intersecting BE in H.



P,Q and R respectively are the mid-points of AH,AB and BC.

We need to prove that  $\angle PQR = 90^{\circ}$ 

Let us extend QP to meet AC at M.

In  $\triangle ABC$ , R and Q are the mid-points of BC and AB respectively.

Theorem states, the line segment joining the mid-points of any two sides of a triangle is parallel to the third side and equal to half of it.

Therefore, we get:

 $QR \parallel AC$ 

*OH* || *ME* ..... (i)

Similarly, in  $\triangle ABH$ ,

 $QP \parallel BH$ 

QM || HE ..... (ii)

From (i) and (ii), we get:

 $QM \parallel HE$  and  $QH \parallel ME$ 

We get, QHME is a parallelogram.

Also,  $BE \perp AC$ 

Therefore, QHME is a rectangle.

Thus,  $\angle MQH = 90^{\circ}$ 

Or,

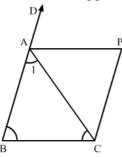
$$\angle PQR = 90^{\circ}$$

Hence proved.

Quadrilaterals Ex 14.4 Q11

## Answer:

We have the following given figure:



We have AB = AC and  $CP \parallel BA$  and AP is the bisector of exterior angle  $\angle CAD$  of  $\triangle ABC$ .

(i) We need to prove that  $\angle PAC = \angle BCA$ 

In  $\triangle ABC$ ,

We have AB = AC (Given)

Thus,  $\angle ABC = \angle BCA$  (Angles opposite to equal sides are equal)

By angle sum property of a triangle, we get:

$$\angle 1 + \angle BCA + \angle ABC = 180^{\circ}$$

$$\angle 1 + \angle BCA + \angle BCA = 180^{\circ}$$

$$\angle 1 + 2 \angle BCA = 180^{\circ}$$
 ..... (i)

Now,

 $\angle PAC = \angle PAD$  (AP is the bisector of exterior angle  $\angle CAD$ )

$$\angle 1 + \angle PAC + \angle PAD = 180^{\circ}$$
 (Linear Pair)

$$\angle 1 + \angle PAC + \angle PAC = 180^{\circ}$$

$$\angle 1 + 2 \angle PAC = 180^{\circ}$$
 ..... (ii)

From equation (i) and (ii), we get:

$$\angle 1 + 2 \angle | RCA = \angle 1 + 2 \angle PAC$$

$$\angle BCA = \angle PAC$$

(ii) We need to prove that ABCP is a parallelogram.

We have proved that  $\angle PAC = \angle BCA$ 

This means,  $AP \parallel BC$ 

Also it is given that  $CP \parallel BA$ 

We know that a quadrilateral with opposite sides parallel is a parallelogram.

Therefore, ABCP is a parallelogram.

