

Exercise 10D

Question 28:

Let the speed of the Deccan Queen = x kmph The, speed of other train = (x - 20)kmph Then, time taken by Deccan Queen = 192/x hours Time taken by other train = 192/(x-20) hours Difference of time taken by two trains is 48/60 = 4/5 h

$$\frac{192}{x-20} - \frac{192}{x} = \frac{4}{5} \Rightarrow \frac{1}{x-20} - \frac{1}{x} = \frac{1}{240}$$

$$\Rightarrow \frac{x-x+20}{x^2-20x} = \frac{1}{240}$$

$$\Rightarrow x^2-20x-4800 = 0$$

$$\Rightarrow x^2-80x+60x-4800 = 0$$

$$\Rightarrow x(x-80)+60(x-80) = 0$$

$$\Rightarrow (x-80)(x+60) = 0$$

$$\Rightarrow x = 80 \text{ or } x = -60$$

$$\therefore x = 80 \left[\because \text{Speed cannot be negative} \right]$$

Hence, speed of Deccan Queen = 80km/h.

Question 29:

Let the speed of the stream be = x km/hSpeed of boat in still waters = 9 km/hSpeed of boat down stream = 9 + xtime taken by boat to go 15 km downstream = 15/(9+x) hours Speed of boat upstream = 9 - xtime taken by boat to go 15 km of stream = 15/(9-x) hours

Total time =
$$\frac{15}{9+x} + \frac{15}{9-x} = 3\frac{45}{60} = 3\frac{3}{4} = \frac{15}{4}$$

Dividing by 15

$$\frac{1}{9+x} + \frac{1}{9-x} = \frac{1}{4}$$
 or $\frac{9+x+9-x}{(9+x)(9-x)} = \frac{1}{4}$

$$\Rightarrow \frac{18}{81 - x^2} = \frac{1}{4}$$
 or $81 - x^2 = 72$

$$x^2 = 81 - 72 = 9$$
 $x = \pm 3$

But
$$x \neq -3$$

:: Speed of stream = 3km / h

Question 30:

Let the speed of stream be x km/h

Speed of boat in still stream = 18 km/h

Speed of boat up the stream = $18 - x \, \text{km/h}$

Time taken by boat to go up the stream 24 km = 24/(18+x) hours Time taken by boat to go down the stream = 24/(18-x) hours Time taken by the boat to go up the stream is 1 hour more that the

time taken down the stream

$$\frac{24}{18-x} - \frac{24}{18+x} = 1 \Rightarrow \frac{1}{18-x} - \frac{1}{18+x} = \frac{1}{24}$$
or
$$\frac{18+x-(18-x)}{(18+x)(18-x)} = \frac{1}{24} \text{ or } \frac{2x}{324-x^2} = \frac{1}{24}$$

$$\Rightarrow 324-x^2 = 48x \text{ or } x^2 + 48x - 324 = 0$$

$$\Rightarrow x^2 + 54x - 6x - 324 = 0$$

$$\Rightarrow x(x+54) - 6(x+54) = 0 \text{ or } (x+54)(x-6) = 0$$

$$\therefore x+54 = 0 \text{ or } x-6 = 0$$

$$\Rightarrow x = -54 \text{ which is not true}$$

$$\therefore x-6 = 0 \qquad \therefore x = 6$$

Speed of the stream = 6 km/h.

Question 31:

Let the speed of the stream be x kmph
Then the speed of boat down stream = (8 + x) kmph
And the speed of boat upstream = (8 - x)kmph
Time taken to cover 15 km upstream = 15/(8-x) hours
Time taken to cover 22 km downstream = 22/(8+x) hours
Total time taken = 5 hours

Hence, the speed of stream is 3 kmph.

Question 32:

Let the speed of the boat in still water be x kmph, then Speed of boat downstream = (x + 2)km/h And the speed of boat upstream = (x - 2)kmph Time taken to cover 8 km downstream = 8/(x+2) hours Time taken to cover 8 km upstream = 8/(x-2) hours Total time taken = 5/3 hours

$$\frac{8}{(x+2)} + \frac{8}{(x-2)} = \frac{5}{3} \Rightarrow \frac{1}{x+2} + \frac{1}{x-2} = \frac{5}{24}$$

$$\Rightarrow \frac{x-2+x+2}{(x+2)(x-2)} = \frac{5}{24} \Rightarrow \frac{2x}{x^2-4} = \frac{5}{24}$$

$$\Rightarrow 5x^2 - 20 - 48x = 0$$

$$\Rightarrow 5x^2 - 48x - 20 = 0$$

$$\Rightarrow 5x^2 - 50x + 2x - 20 = 0$$

$$\Rightarrow 5x(x-10) + 2(x-10) = 0$$

$$\Rightarrow (x-10)(5x+2) = 0$$

$$\Rightarrow x = 10 \text{ or } x = \frac{-2}{5}$$

$$\Rightarrow x = 10 \text{ (speed cannot be negative)}$$

Then speed of the boat in still water is 10 kmph.

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