

Exercise 16D

Question 1:

$$\left(\frac{-8}{5},2\right)$$
 and $\left(\frac{2}{5},2\right)$

Distance between the points

$$= \sqrt{\left(-\frac{8}{5} - \frac{2}{5}\right)^2 + (2 - 2)^2}$$

$$= \sqrt{\left(-\frac{10}{5}\right)^2 + 0}$$

$$= \sqrt{(-2)^2 + 0}$$

$$= 2 \text{ units}$$

Question 2:

The points (3, a) lies on the line 2x - 3y = 5. Substituting the values of x and y in the given equation:

$$2 \times 3 - 3 \times a = 5$$
 or $6 - 3a = 5$

$$\Rightarrow$$
 3a = 1

$$\Rightarrow$$
 a = $1/3$

Question 3:

The points A(4,3) and B(x,5) lie on the circle with center O(2,3) OA and OB are radius of the circle.

$$\Rightarrow OA = OB \text{ or } OA^{2} = OB^{2}$$

$$\therefore (2-4)^{2} + (3-3)^{2} = (2-x)^{2} + (3-5)^{2}$$
or $4+0=4+x^{2}-4x+4$

$$\Rightarrow x^{2}-4x+4=0$$
or $(x-2)^{2}=0$: $x=2$

Question 4:

The point P(x, y) is equidistant from the point A(7, 1) and B(3, 5)

$$\Rightarrow PA = PB \text{ or } PA^2 = PB^2$$

$$\therefore (x-7)^2 + (y-1)^2 = (x-3)^2 + (y-5)^2$$
or $x^2 + y^2 - 14x - 2y + 49 + 1 = x^2 + y^2 - 6x - 10y + 9 + 25$

$$\Rightarrow -14x - 2y + 50 = -6x - 10y + 34$$

$$(-14+6)x + (-2+10)y + 50 - 34 = 0$$

$$-8x + 8y + 16 = 0$$
Hence, $x - y = 2$

******* END ******