



Tangents and Normals Ex 16.3 Q6

$$xy = 4$$

$$\Rightarrow x = \frac{4}{y} \dots\dots (i)$$

$$x^2 + y^2 = 8 \dots\dots (ii)$$

Substituting eq (i) in (ii) we get,

$$x^2 + y^2 = 8$$

$$\Rightarrow \left(\frac{4}{y}\right)^2 + y^2 = 8$$

$$\Rightarrow 16 + y^4 = 8y^2$$

$$\Rightarrow y^4 - 8y^2 + 16 = 0$$

$$\Rightarrow (y^2 - 4)^2 = 0$$

$$\Rightarrow y^2 = 4$$

$$\Rightarrow y = \pm 2$$

From (i) when $y = 2$, we get $x = 2$ and when $y = -2$, we get $x = -2$

Thus the two curves intersect at $(2, 2)$ and $(-2, 2)$.

Differentiating (i) wrt x , we get

$$y + x \frac{dy}{dx} = 0$$

$$\Rightarrow \frac{dy}{dx} = -\frac{y}{x}$$

Differentiating (i) wrt x , we get

$$y + x \frac{dy}{dx} = 0$$

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Differentiating (ii) wrt x , we get

$$2x + 2y \frac{dy}{dx} = 0$$

$$\Rightarrow \frac{dy}{dx} = -\frac{x}{y}$$

At $(2, 2)$

$$\left(\frac{dy}{dx}\right)_{C_1} = -1$$

$$\left(\frac{dy}{dx}\right)_{C_2} = -1$$

Clearly $\left(\frac{dy}{dx}\right)_{C_1} = \left(\frac{dy}{dx}\right)_{C_2}$ at $(2, 2)$

So given two curves touch each other at $(2, 2)$.

Similarly, it can be seen that two curves touch each other at $(-2, -2)$.

Tangents and Normals Ex 16.3 Q7

$$y^2 = 4x \dots (i)$$

$$x^2 + y^2 - 6x + 1 = 0 \dots (ii)$$

Differentiating (i) wrt x , we get

$$2y \frac{dy}{dx} = 4$$

$$\Rightarrow \frac{dy}{dx} = \frac{2}{y}$$

Differentiating (ii) wrt x , we get

$$2x + 2y \frac{dy}{dx} - 6 + 0 = 0$$

$$\Rightarrow \frac{dy}{dx} = \frac{3-x}{y}$$

At $(1, 2)$

$$\left(\frac{dy}{dx} \right)_{C_1} = \frac{2}{2} = 1$$

$$\left(\frac{dy}{dx} \right)_{C_2} = \frac{3-1}{2} = \frac{2}{2} = 1$$

Clearly $\left(\frac{dy}{dx} \right)_{C_1} = \left(\frac{dy}{dx} \right)_{C_2}$ at $(1, 2)$

So given two curves touch each other at $(1, 2)$.

***** END *****