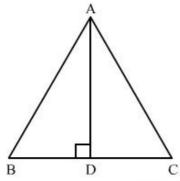


## Triangles Ex 4.7 Q24

## Answer:



We have to prove that  $AD^2 = 3BD^2$ .

In right angled \$\textit{\alpha}BD\$, using Pythagoras theorem we get,

$$AB^2 = AD^2 + BD^2 - \dots (1)$$

We know that in an equilateral triangle every altitude is also median.

Therefore, AD bisects BC.

Therefore, we have BD = DC

Since  $\triangle ABC$  is an equilateral triangle, AB = BC = AC

Therefore, we can write equation (1) as

$$BC^2 = AD^2 + BD^2 - \dots (2)$$

But BC = 2BD

Therefore, equation (2) becomes,

$$(2BD)^2 = AD^2 + BD^2$$

Simplifying the equation we get,

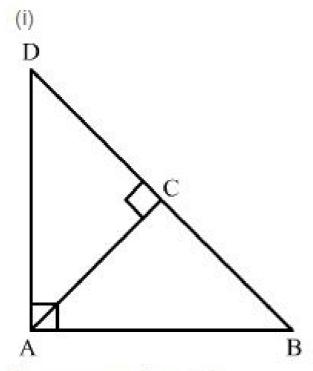
$$4BD^2 - BD^2 = AD^2$$

$$3BD^2 = AD^2$$

Therefore, 
$$AD^2 = 3BD^2$$

Triangles Ex 4.7 Q25

## Answer:



In  $\triangle ABD$  and  $\triangle ABC$ .

$$\angle ACB = \angle A = 90^{\circ}$$

$$\angle B = \angle B$$
 (Common angle)

So, by AA criterion  $\triangle ABD \sim \triangle CBA$ 

$$\therefore \frac{AB}{BC} = \frac{BD}{AB} = \frac{AD}{AC}$$

$$\therefore \frac{AB}{BC} = \frac{BD}{AB}$$

$$\therefore AB^2 = BD.BC \qquad \dots (1)$$

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(ii) In \triangle ABD and \triangle ACD.
\angle C = \angle A = 90^{\circ}
 \angle D = \angle D (Common angle)
So, by AA criterion \Delta ABD \sim \Delta CAD
\therefore \frac{AB}{AC} = \frac{BD}{AD} = \frac{AD}{CD}\therefore \frac{BD}{AD} = \frac{AD}{CD}
                                      ....(2)
\therefore AD^2 = BD.CD
(iii) We have shown that \triangle ABD is similar to \triangle CBA and \triangle ABD is similar to \triangle CAD therefore, by the
property of transitivity \Delta CBA is similar to \Delta CAD.
\frac{BC}{AC} = \frac{AB}{AD} = \frac{AC}{CD}
\frac{BC}{AC} = \frac{AC}{CD}
\therefore AC^2 = BC.CD \qquad \dots (3)
(iv) Now to obtained AB^2/AC^2 = BD/DC, we will divide equation (1) by equation (2) as shown below,
\therefore \frac{AB^2}{AC^2} = \frac{BD.BC}{BC.CD}
Canceling BC we get,
\frac{AB^2}{AC^2} = \frac{BD}{CD}
Therefore, \frac{AB^2}{AC^2} = \frac{BD}{CD}
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\*\*\*\*\*\*\*\*\* END \*\*\*\*\*\*\*