



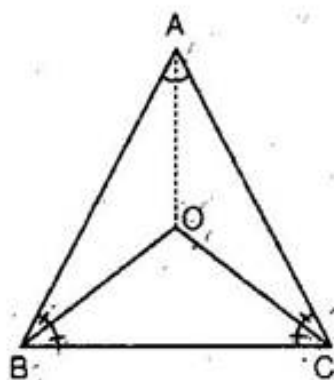
NCERT solutions for class 9 Maths Triangles Ex 7.2

**Q1.** In an isosceles triangle  $ABC$ , with  $AB = AC$ , the bisectors of  $\angle B$  and  $\angle C$  intersect each other at  $O$ . Join  $A$  to  $O$ . Show that:

(i)  $OB = OC$

(ii)  $AO$  bisects  $\angle A$ .

**Ans. (i)**  $ABC$  is an isosceles triangle in which  $AB = AC$ .



$\therefore \angle C = \angle B$  [Angles opposite to equal sides]

$\Rightarrow \angle OCA + \angle OCB = \angle OBA + \angle OBC$

$\because OB$  bisects  $\angle B$  and  $OC$  bisects  $\angle C$

$\therefore \angle OBA = \angle OBC$  and  $\angle OCA = \angle OCB$

$\Rightarrow \angle OCB + \angle OCB = \angle OBC + \angle OBC$

$\Rightarrow 2\angle OCB = 2\angle OBC$

$\Rightarrow \angle OCB = \angle OBC$

Now in  $\triangle OBC$ ,

$\angle OCB = \angle OBC$  [Prove above]

$\therefore OB = OC$  [Sides opposite to equal sides]

**(ii)** In  $\triangle AOB$  and  $\triangle AOC$ ,

$AB = AC$  [Given]

$$\angle OBA = \angle OCA \text{ [Given]}$$

$$\text{And } \angle B = \angle C$$

$$\Rightarrow \frac{1}{2} \angle B = \frac{1}{2} \angle C$$

$$\Rightarrow \angle OBA = \angle OCA$$

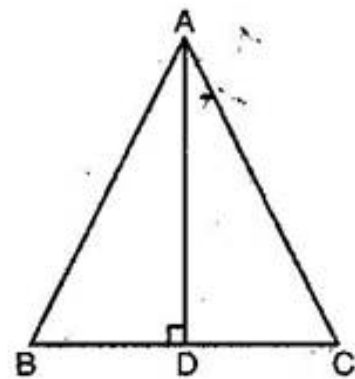
$$\Rightarrow OB = OC \text{ [Prove above]}$$

$$\therefore \triangle AOB \cong \triangle AOC \text{ [By SAS congruency]}$$

$$\Rightarrow \angle OAB = \angle OAC \text{ [By C.P.C.T.]}$$

Hence AO bisects  $\angle A$ .

**Q2.** In  $\triangle ABC$ , AD is the perpendicular bisector of BC (See figure). Show that  $\triangle ABC$  is an isosceles triangle in which  $AB = AC$ .



**Ans.** In  $\triangle AOB$  and  $\triangle AOC$ ,

$$BD = CD \text{ [AD bisects BC]}$$

$$\angle ADB = \angle ADC = 90^\circ \text{ [AD } \perp \text{ BC]}$$

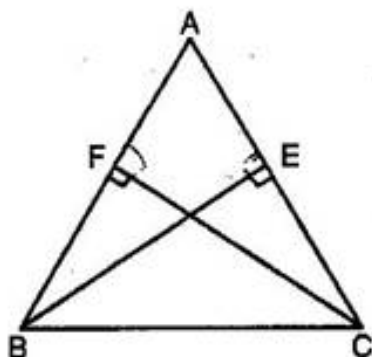
$$AD = AD \text{ [Common]}$$

$$\therefore \triangle ABD \cong \triangle ACD \text{ [By SAS congruency]}$$

$$\Rightarrow AB = AC \text{ [By C.P.C.T.]}$$

Therefore, ABC is an isosceles triangle.

**Q3.** ABC is an isosceles triangle in which altitudes BE and CF are drawn to sides AC and AB respectively (See figure). Show that these altitudes are equal.



**Ans.** In  $\triangle ABE$  and  $\triangle ACF$ ,

$\angle A = \angle A$  [Common]

$\angle AEB = \angle AFC = 90^\circ$  [Given]

$AB = AC$  [Given]

$\therefore \triangle ABE \cong \triangle ACF$  [By ASA congruency]

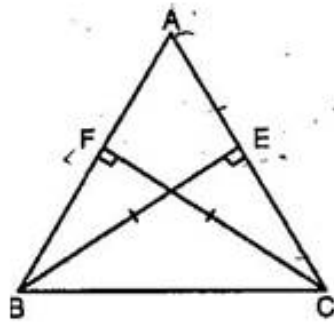
$\Rightarrow BE = CF$  [By C.P.C.T.]

$\Rightarrow$  Altitudes are equal.

**Q4.** ABC is a triangle in which altitudes BE and CF to sides AC and AB are equal (See figure). Show that:

(i)  $\triangle ABE \cong \triangle ACF$

(ii)  $AB = AC$  or  $\triangle ABC$  is an isosceles triangle.



**Ans. (i)** In  $\triangle ABE$  and  $\triangle ACF$ ,

$\angle A = \angle A$  [Common]

$\angle AEB = \angle AFC = 90^\circ$  [Given]

$BE = CF$  [Given]

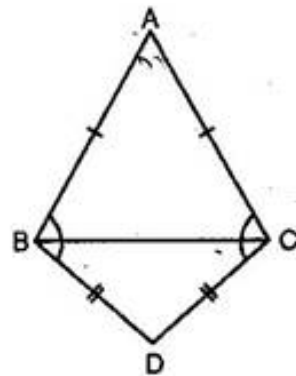
$\therefore \triangle ABE \cong \triangle ACF$  [By ASA congruency]

**(ii)** Since  $\triangle ABE \cong \triangle ACF$

$\Rightarrow BE = CF$  [By C.P.C.T.]

$\Rightarrow ABC$  is an isosceles triangle.

**Q5.**  $ABC$  and  $DBC$  are two isosceles triangles on the same base  $BC$  (See figure). Show that  $\angle ABD = \angle ACD$ .



**Ans.** In isosceles triangle ABC,

$AB = AC$  [Given]

$\angle ACB = \angle ABC$  .....(i) [Angles opposite to equal sides]

Also in Isosceles triangle BCD.

$BD = DC$

$\therefore \angle BCD = \angle CBD$  .....(ii) [Angles opposite to equal sides]

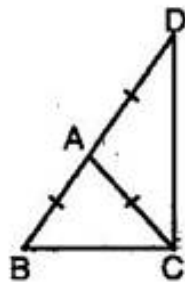
Adding eq. (i) and (ii),

$\angle ACB + \angle BCD = \angle ABC + \angle CBD$

$\Rightarrow \angle ACD = \angle ABD$

Or  $\angle ABD = \angle ACD$

**Q6.**  $\triangle ABC$  is an isosceles triangle in which  $AB = AC$ . Side BA is produced to D such that  $AD = AB$ . Show that  $\angle BCD$  is a right angle (See figure).



**Ans.** In isosceles triangle ABC,

$AB = AC$  [Given]

$\angle ACB = \angle ABC$  .....(i) [Angles opposite to equal sides]

Now  $AD = AB$  [By construction]

But  $AB = AC$  [Given]

$$\therefore AD = AB = AC$$

$$\Rightarrow AD = AC$$

Now in triangle ADC,

$$AD = AC$$

$$\Rightarrow \angle ADC = \angle ACD \dots\dots\dots(ii) \text{ [Angles opposite to equal sides]}$$

$$\text{Since } \angle BAC + \angle CAD = 180^\circ \dots\dots\dots(iii) \text{ [Linear pair]}$$

And Exterior angle of a triangle is equal to the sum of its interior opposite angles.

$\therefore$  In  $\triangle ABC$ ,

$$\angle CAD = \angle ABC + \angle ACB = \angle ACB + \angle ACB$$

[Using (i)]

$$\Rightarrow \angle CAD = 2\angle ACB \dots\dots\dots(iv)$$

Similarly, for  $\triangle ADC$ ,

$$\begin{aligned} \angle BAC &= \angle ACD + \angle ADC \\ &= \angle ACD + \angle ACD = 2\angle ACD \dots\dots\dots(v) \end{aligned}$$

From eq. (iii), (iv) and (v),

$$2\angle ACB + 2\angle ACD = 180^\circ$$

$$\Rightarrow 2(\angle ACB + \angle ACD) = 180^\circ$$

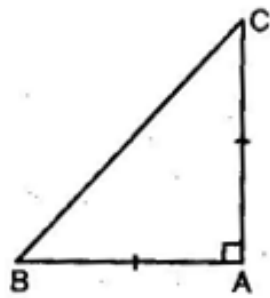
$$\Rightarrow \angle ACB + \angle ACD = 90^\circ$$

$$\Rightarrow \angle BCD = 90^\circ$$

Hence  $\angle BCD$  is a right angle.

**Q7.** ABC is a right angled triangle in which  $\angle A = 90^\circ$  and  $AB = AC$ . Find  $\angle B$  and  $\angle C$ .

**Ans.** ABC is a right triangle in which,



$\angle A = 90^\circ$  And  $AB = AC$

In  $\triangle ABC$ ,

$AB = AC$

$\Rightarrow \angle C = \angle B$  .....(i)

We know that, in  $\triangle ABC$ ,

$\angle A + \angle B + \angle C = 180^\circ$  [Angle sum property]

$\Rightarrow 90^\circ + \angle B + \angle B = 180^\circ$

[ $\angle A = 90^\circ$  (given) and  $\angle B = \angle C$  (from eq. (i))]

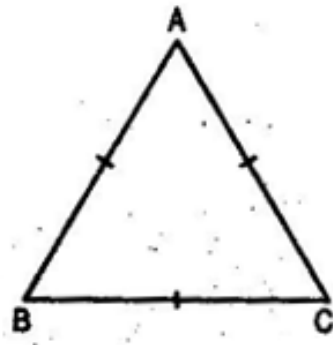
$\Rightarrow 2\angle B = 90^\circ$

$\Rightarrow \angle B = 45^\circ$

Also  $\angle C = 45^\circ$  [ $\angle B = \angle C$ ]

**Q8.** Show that the angles of an equilateral triangle are  $60^\circ$  each.

**Ans.** Let ABC be an equilateral triangle.



$$\therefore AB = BC = AC$$

$$\Rightarrow AB = BC$$

$$\Rightarrow \angle C = \angle A \dots\dots\dots(i)$$

Similarly,  $AB = AC$

$$\Rightarrow \angle C = \angle B \dots\dots\dots(ii)$$

From eq. (i) and (ii),

$$\angle A = \angle B = \angle C \dots\dots\dots(iii)$$

Now in  $\triangle ABC$

$$\angle A + \angle B + \angle C = 180^\circ \dots\dots\dots(iv)$$

$$\Rightarrow \angle A + \angle A + \angle A = 180^\circ$$

$$\Rightarrow 3\angle A = 180^\circ$$

$$\Rightarrow \angle A = 60^\circ$$

Since  $\angle A = \angle B = \angle C$  [From eq. (iii)]

$$\therefore \angle A = \angle B = \angle C = 60^\circ$$

Hence each angle of equilateral triangle is  $60^\circ$ .

\*\*\*\*\* END \*\*\*\*\*