

Algebra of Matrices Ex 5.5 Q1 Given,

$$A = \begin{bmatrix} 2 & 3 \\ 4 & 5 \end{bmatrix}$$

$$\begin{pmatrix} A - A^T \end{pmatrix} = \begin{pmatrix} 2 & 3 \\ 4 & 5 \end{pmatrix} - \begin{pmatrix} 2 & 3 \\ 4 & 5 \end{pmatrix}^T \\
= \begin{pmatrix} 2 & 3 \\ 4 & 5 \end{pmatrix} - \begin{pmatrix} 2 & 4 \\ 3 & 5 \end{pmatrix} \end{pmatrix} \\
= \begin{pmatrix} 2 - 2 & 3 - 4 \\ 4 - 3 & 5 - 5 \end{pmatrix} \\
\begin{pmatrix} A - A^T \end{pmatrix} = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} \qquad ---(i)$$

$$-\left(A - A^{T}\right)^{T} = -\begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}^{T}$$

$$= -\begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix}$$

$$-\left(A - A^{T}\right)^{T} = \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}$$
---(ii)

From (i) and (ii), 
$$(A - A^T) = -(A - A^T)^T$$

We know that, x is a skew symmetric matrix if  $x = -x^T$ So,  $\left(A - A^T\right)$  is skew symmetric.

Algebra of Matrices Ex 5.5 Q2

Given,

$$A = \begin{bmatrix} 3 & -4 \\ 1 & -1 \end{bmatrix}$$

$$A - A^{T} = \begin{bmatrix} 3 & -4 \\ 1 & -1 \end{bmatrix} - \begin{bmatrix} 3 & -4 \\ 1 & -1 \end{bmatrix}^{T}$$

$$= \begin{bmatrix} 3 & -4 \\ 1 & -1 \end{bmatrix} - \begin{bmatrix} 3 & 1 \\ -4 & -1 \end{bmatrix}$$

$$= \begin{bmatrix} 3 - 3 & -4 - 1 \\ 1 + 4 & -1 + 1 \end{bmatrix}$$

$$A - A^{T} = \begin{bmatrix} 0 & -5 \\ 5 & 0 \end{bmatrix}$$
---(i)

$$-\left(A - A^{T}\right)^{T} = -\begin{bmatrix} 0 & -5 \\ 5 & 0 \end{bmatrix}^{T}$$

$$= -\begin{bmatrix} 0 & 5 \\ -5 & 0 \end{bmatrix}$$

$$-\left(A - A^{T}\right)^{T} = \begin{bmatrix} 0 & -5 \\ 5 & 0 \end{bmatrix}$$
---(ii)

From equation (i) and (ii),

$$\left(A - A^{T}\right) = -\left(A - A^{T}\right)^{T}$$

We know that, x is skewsymmetric matrx if  $x = -x^T$ So,  $\left(A - A^T\right)$  is skewsymmetric matrix.

Algebra of Matrices Ex 5.5 Q3 Given,

$$A = \begin{bmatrix} 5 & 2 & x \\ y & z & -3 \\ 4 & t & -7 \end{bmatrix}$$
 is a symmetric matrix.

We know that  $A = \begin{bmatrix} aij \end{bmatrix}_{n \times n}$  is a symmetric matrix if aij = aji

So, 
$$x = a_{13} = a_{31} = 4$$
  
 $y = a_{21} = a_{12} = 2$   
 $z = a_{22} = a_{22} = z$   
 $t = a_{32} = a_{32} = -3$ 

Hence,

$$x = 4, y = 2, t = -3$$
 and  $z$  can have any value.

\*\*\*\*\*\*\*\*\*\* FND \*\*\*\*\*\*\*