

Complex Numbers Ex 13.2 Q11

$$\begin{aligned}
\det z &= \frac{\left(1+i\right)^n}{\left(1-i\right)^{n-2}} \\
&= \frac{\left(1+i\right)^n}{\left(1-i\right)^n} \left(1-i\right)^2 \\
&= \left(\frac{1+i}{1-i}\right)^n \times \left(1-i\right)^2 \\
&= i^n \left(1+i^2-2\times 1\times i\right) \qquad \left(\because \frac{1+i}{1-i} = i, \text{usingproblem } 10\right) \\
&= i^n \left(1-1-2i\right) \\
&= -2i \times i^n \\
&= -2i^{n+1}
\end{aligned}$$

$$\therefore For n = 1$$

$$z = -2i^{1+1}$$

$$= -2i^{2}$$

= 2, which is a real number

 \therefore The smallest positive integer value of nis1.

Complex Numbers Ex 13.2 Q12

$$\left(\frac{1+i}{1-i}\right)^3 - \left(\frac{1-i}{1+i}\right)^3 = x + iy$$

$$\Rightarrow \left(\frac{(1+i)(1+i)}{(1-i)(1+i)}\right)^3 - \left(\frac{(1-i)(1-i)}{(1+i)(1-i)}\right)^3 = x + iy [\text{Rationalizing the denomiantor}]$$

$$\Rightarrow \left(\frac{1+2i-1}{1+1}\right)^3 - \left(\frac{1-2i-1}{1+1}\right)^3 = x + iy$$

$$\Rightarrow \left(\frac{2i}{2}\right)^3 - \left(\frac{-2i}{2}\right)^3 = x + iy$$

$$\Rightarrow i^3 - (-i)^3 = x + iy$$

$$\Rightarrow -i - i = x + iy$$

$$\Rightarrow -2i = x + iy$$
Comparing the real and imaginary parts,

$$(x,y) = (0,2)$$

Complex Numbers Ex 13.2 Q13

$$\frac{(1+i)^2}{2-i} = x+iy$$

$$\Rightarrow \frac{(1+2i-1)}{2-i} = x+iy$$

$$\Rightarrow \frac{2i}{2-i} = x+iy$$

$$\Rightarrow \frac{2i(2+i)}{(2-i)(2+i)} = x+iy [Rationalizing the denominator]$$

$$\Rightarrow \frac{2(2i-1)}{4+1} = x+iy$$

$$\Rightarrow \frac{4i-2}{5} = x+iy$$

$$\Rightarrow -\frac{2}{5} + i\frac{4}{5} = x+iy$$

Comparing the real and imaginary parts, we get

$$x = -\frac{2}{5}, y = \frac{4}{5}$$
$$x + y = \frac{2}{5}$$

Complex Numbers Ex 13.2 Q14

Comparing, we get (a,b)=(1,0)

$$\left(\frac{1-i}{1+i}\right)^{100} = a+ib$$

$$\Rightarrow \left(\frac{(1-i)(1-i)}{(1+i)(1-i)}\right)^{100} = a+ib \text{ [Rationalizing the denominator]}$$

$$\Rightarrow \left(\frac{(1-2i-1)}{(1+1)}\right)^{100} = a+ib$$

$$\Rightarrow \left(\frac{-2i}{2}\right)^{100} = a+ib$$

$$\Rightarrow (-i)^{100} = a+ib$$

$$\Rightarrow 1=a+ib$$

****** END ******