

Transformation Formulae Ex 8.2 Q 8(i) We have,

LHS
$$= \frac{\sin A + \sin 3A + \sin 5A}{\cos A + \cos 3A + \cos 5A}$$

$$= \frac{(\sin 5A + \sin A) + \sin 3A}{(\cos 5A + \cos A) + \cos 3A}$$

$$= \frac{2 \sin \left(\frac{5A + A}{2}\right) \cos \left(\frac{5A - A}{2}\right) + \sin 3A}{2 \cos \left(\frac{5A + A}{2}\right) \cos \left(\frac{5A - A}{2}\right) + \cos 3A}$$

$$= \frac{2 \sin 3A \cos 2A + \sin 3A}{2 \cos 3A \cos 2A + \cos 3A}$$

$$= \frac{\sin 3A (2 \cos 2A + 1)}{\cos 3A (2 \cos 2A + 1)}$$

$$= \frac{\sin 3A}{\cos 3A}$$

$$= \tan 3A$$

$$= \text{RHS}$$

$$\frac{\sin A + \sin 3A + \sin 5A}{\cos A + \cos 3A + \cos 5A} = \tan 3A$$

Hence proved.

Transformation Formulae Ex 8.2 Q 8(ii)

We have,

LHS
$$= \frac{\cos 3A + 2\cos 5A + \cos 7A}{\cos A + 2\cos 3A + \cos 5A}$$

$$= \frac{(\cos 7A + \cos 3A) + 2\cos 5A}{(\cos 5A + \cos A) + 2\cos 3A}$$

$$= \frac{2\cos\left(\frac{7A + 3A}{2}\right)\cos\left(\frac{7A - 3A}{2}\right) + 2\cos 5A}{2\cos\left(\frac{5A + A}{2}\right)\cos\left(\frac{5A - A}{2}\right) + \cos 3A}$$

$$= \frac{2\cos 5A\cos 2A + 2\cos 5A}{2\cos 3A\cos 2A + 2\cos 3A}$$

$$= \frac{2\cos 5A(\cos 2A + 1)}{2\cos 3A(\cos 2A + 1)}$$

$$= \frac{\cos 5A}{\cos 3A}$$

$$= RHS$$

$$\frac{\cos 3A + 2\cos 5A + \cos 7A}{\cos A + 2\cos 3A + \cos 5A} = \frac{\cos 5A}{\cos 3A}$$

Hence proved.

Transformation Formulae Ex 8.2 Q 8(iii)

LHS
$$= \frac{\cos 4A + \cos 3A + \cos 2A}{\sin 4A + \sin 3A + \sin 2A}$$

$$= \frac{(\cos 4A + \cos 2A) + \cos 3A}{(\sin 4A + \sin 2A) + \sin 3A}$$

$$= \frac{2\cos\left(\frac{4A + 2A}{2}\right)\cos\left(\frac{4A - 2A}{2}\right) + \cos 3A}{2\sin\left(\frac{4A + 2A}{2}\right)\cos\left(\frac{4A - 2A}{2}\right) + \sin 3A}$$

$$= \frac{2\cos 3A\cos A + \cos 3A}{2\sin 3A\cos A + \sin 3A}$$

$$= \frac{\cos 3A(2\cos A + 1)}{\sin 3A(2\cos A + 1)}$$

$$= \frac{\cos 3A}{\sin A}$$

$$= \cot 3A$$

$$= RHS$$

$$\frac{\cos 4A + \cos 3A + \cos 2A}{\sin 4A + \sin 3A + \sin 2A} = \cot 3A \text{ Hence proved.}$$

Transformation Formulae Ex 8.2 Q 8(iv)

We have,

LHS =
$$\frac{\sin 3A + \sin 5A + \sin 7A + \sin 9A}{\cos 3A + \cos 5A + \cos 7A + \cos 9A}$$

= $\frac{(\sin 9A + \sin 3A) + (\sin 7A + \sin 5A)}{(\cos 9A + \cos 3A) + (\cos 7A + \cos 5A)}$
= $\frac{2 \sin \left(\frac{9A + 3A}{2}\right) \cos \left(\frac{9A - 3A}{2}\right) + 2 \sin \left(\frac{7A + 5A}{2}\right) \cos \left(\frac{7A - 5A}{2}\right)}{2 \cos \left(\frac{9A + 3A}{2}\right) \cos \left(\frac{9A - 3A}{2}\right) + 2 \cos \left(\frac{7A + 5A}{2}\right) \cos \left(\frac{7A - 5A}{2}\right)}$
= $\frac{2 \sin 6A \cos 3A + 2 \sin 6A \cos A}{2 \cos 6A \cos 3A + 2 \cos 6A \cos A}$
= $\frac{2 \sin 6A (\cos 3A + \cos A)}{2 \cos 6A (\cos 3A + \cos A)}$
= $\frac{\sin 6A}{\cos 6A}$
= $\tan 6A$
= RHS

$$\frac{\sin 3A + \sin 5A + \sin 7A + \sin 9A}{\cos 3A + \cos 5A + \cos 7A + \cos 9A} = \tan 6A$$

Hence proved.

Transformation Formulae Ex 8.2 Q 8(v)

LHS
$$= \frac{\sin 5A - \sin 7A + \sin 8A - \sin 4A}{\cos 4A + \cos 7A - \cos 5A - \cos 8A}$$

$$= \frac{-(\sin 7A - \sin 5A) + (\sin 8A - \sin 4A)}{-(\cos 7A - \cos 5A) - (\cos 8A - \cos 4A)}$$

$$= \frac{-\left[2\sin\left(\frac{7A - 5A}{2}\right)\cos\left(\frac{7A + 5A}{2}\right)\right] + \left[2\sin\left(\frac{8A - 4A}{2}\right)\cos\left(\frac{8A + 4A}{2}\right)\right]}{-2\sin\left(\frac{7A + 5A}{2}\right)\sin\left(\frac{7A - 5A}{2}\right) - \left[-2\sin\left(\frac{8A + 4A}{2}\right)\sin\left(\frac{8A - 4A}{2}\right)\right]}$$

$$= \frac{-2\sin A\cos 6A + 2\sin 2A\cos 6A}{-2\sin 6A\sin A + 2\sin 6A\sin 2A}$$

$$= \frac{2\cos 6A[-\sin A + \sin 2A]}{2\sin 6A[-\sin A + \sin 2A]}$$

$$= \frac{\cos 6A}{\sin 6A}$$

$$= \cot 6A$$

$$= \text{RHS}$$

 $\frac{\sin 5A - \sin 7A + \sin 8A - \sin 4A}{\cos 4A + \cos 7A - \cos 5A - \cos 8A} = \cot 6A$ Hence proved.

Transformation Formulae Ex 8.2 Q 8(vi) We have,

LHS
$$= \frac{\sin 5A \cos 2A - \sin 6A \cos A}{\sin A \sin 2A - \cos 2A \cos 3A}$$

$$= \frac{2(\sin 5A \cos 2A - \sin 6A \cos A)}{2(\sin A \sin 2A - \cos 2A \cos 3A)}$$

$$= \frac{2 \sin 5A \cos 2A - 2 \sin 6A \cos A}{2 \sin A \sin 2A - 2 \cos 2A \cos 3A}$$

$$= \frac{\sin (5A + 2A) + \sin (5A - 2A) - [\sin (6A + A) + \sin (6A - A)]}{\cos (2A - A) - \cos (2A + A) - [\cos (3A + 2A) + \cos (3A - 2A)]}$$

$$= \frac{\sin 7A + \sin 3A - \sin 7A - \sin 5A}{\cos A - \cos 3A - \cos 5A}$$

$$= \frac{\sin 3a - \sin 5A}{-\cos 3A - \cos 5A}$$

$$= \frac{-(\sin 5A - \sin 3A)}{-(\cos 5A + \cos 3A)}$$

$$= \frac{\sin 5A - \sin 3A}{\cos 5A + \cos 3A}$$

$$= \frac{2 \sin (\frac{5A - 3A}{2}) \cos (\frac{5A + 3A}{2})}{2\cos (\frac{5A + 3A}{2}) \cos (\frac{5A - 3A}{2})}$$

$$= \frac{\sin A \cos 4A}{\cos 4A \cos A}$$

$$= \frac{\sin A}{\cos A}$$

$$= \tan A$$

$$= \text{RHS}$$

 $\frac{\sin 5A \cos 2A - \sin 6A \cos A}{\sin A \sin 2A - \cos 2A \cos 3A} = \tan A$ Hence proved.

Transformation Formulae Ex 8.2 Q 8(vii)

We have, $= \frac{\sin 11A \sin A + \sin 7 A \sin 3A}{\sin 3A}$ LHS cos 11A sin A + cos 7A sin 3A 2 (sin 1 1 A sin A + sin 7 A sin 3 A) $= \frac{2\left(\cos 11A \sin A + \cos 7A \sin 3A\right)}{2\left(\cos 11A \sin A + \cos 7A \sin 3A\right)}$ 2 sin 1 1A sin A + 2 sin 7 A sin 3 A $= \frac{2\sin 12\cos 3}{2\cos 11A\sin A + 2\cos 7A\sin 3A}$ $=\frac{\cos \left(11 A-A\right)-\cos \left(11 A+A\right)+\cos \left(7 A-3 A\right)-\cos \left(7 A+3 A\right)}{\sin \left(11 A+A\right)-\sin \left(11 A-A\right)+\sin \left(7 A+3 A\right)-\sin \left(7 A-3 A\right)}$ = cos 10 A - cos 12 A + cos 4A - cos 10 A sin 12 A - sin 10 A + sin 10 A - sin 4A $= \frac{-(\cos 12A - \cos 4A)}{-(\cos 12A - \cos 4A)}$ sin 12A – sin 4A $-\left[-2\sin\left(\frac{12A+4A}{2}\right)\sin\left(\frac{12A-4A}{2}\right)\right]$ 2 sin 8 A sin 4A $= \frac{}{2 \sin 4A \cos 8A}$ *<u>_ sin</u>8A* cos 8A = tan 8A = RHS sin 11 A sin A + sin 7 A sin 3 A

$$\frac{\sin 11A \sin A + \sin 7A \sin 3A}{\cos 11A \sin A + \cos 7A \sin 3A} = \tan 8A$$
 Hence proved.

Transformation Formulae Ex 8.2 Q 8(viii)

$$LHS = \frac{\sin 3A \cos 4A - \sin A\cos 2A}{\sin 4A \sin A + \cos 6A \cos A}$$

$$= \frac{2(\sin 3A \cos 4A - \sin A\cos 2A)}{2(\sin 4A \sin A + \cos 6A \cos A)}$$

$$= \frac{2\sin 3A \cos 4A - \sin A\cos 2A}{2\sin 4A \sin A + 2\cos 6A \cos A}$$

$$= \frac{\sin (4A + 3A) - \sin (4A - 3A) - [\sin (2A + A) - \sin (2A - A)]}{\cos (4A - A) - \cos (4A + A) + \cos (6A + A) + \cos (6A - A)}$$

$$= \frac{\sin (7A) - \sin (A) - \sin (A) + \sin (A)}{\cos (A) - \cos (A) + \cos (A) + \cos (A)}$$

$$= \frac{\sin (7A) - \sin (A)}{\cos (A) + \cos (A)}$$

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Transformation Formulae Ex 8.2 Q 8(ix)

= tan2A= RHS

LHS =
$$\frac{\sin A \sin 2A + \sin 3A \sin 6A}{\sin A \cos 2A + \sin 3A \cos 6A}$$

= $\frac{2[\sin A \sin 2A + \sin 3A \cos 6A]}{2[\sin A \cos 2A + \sin 3A \cos 6A]}$
= $\frac{2 \sin 2A \sin A + 2 \sin 6A \sin 3A}{2 \cos 2A \sin A + 2 \cos 6A \sin 3A}$
= $\frac{\cos (2A - A) - \cos (2A + A) + \cos (6A - 3A) - \cos (6A + 3A)}{\sin (2A + A) - \sin (2A - A) + \sin (6A + 3A) - \sin (6A - 3A)}$
= $\frac{\cos A - \cos 3A + \cos 3A - \cos 9A}{\sin 3A - \sin A + \sin 9A - \sin 3A}$
= $\frac{\cos A - \cos 9A}{\sin 9A - \sin A}$
= $\frac{\cos A - \cos 9A}{\sin 9A - \sin A}$
= $\frac{-[\cos 9A - \cos A]}{\sin 9A - \sin A}$
= $\frac{-[\cos 9A - \cos A]}{\sin 9A - \sin A}$
= $\frac{\sin 5A \sin 4A}{\sin 4A \cos 5A}$
= $\tan 5A$
= RHS

$$\therefore \frac{\sin A \sin 2A + \sin 3A \sin 6A}{\sin A \cos 2A + \sin 3A \cos 6A} = \tan 5A \qquad \text{Hence proved.}$$

Transformation Formulae Ex 8.2 Q 8(x)

We have,

LHS
$$= \frac{\sin A + 2 \sin 3A + \sin 5A}{\sin 3A + 2 \sin 5A + \sin 7A}$$

$$= \frac{\sin 5A + \sin A + 2 \sin 3A}{\sin 7A + \sin 3A + 2 \sin 5A}$$

$$= \frac{2 \sin \left(\frac{5A + A}{2}\right) \cos \left(\frac{5A - A}{2}\right) + 2 \sin 3A}{2 \sin \left(\frac{7A + 3A}{2}\right) \cos \left(\frac{7A - 3A}{2}\right) + 2 \sin 5A}$$

$$= \frac{2 \sin 3A \cos 2A + 2 \sin 3A}{2 \sin 5A \cos 2A + 2 \sin 5A}$$

$$= \frac{2 \sin 3A (\cos 2A + 1)}{2 \sin 5A (\cos 2A + 1)}$$

$$= \frac{\sin 3A}{\sin 5A}$$
= RHS

$$\therefore \frac{\sin A + 2\sin 3A + \sin 5A}{\sin 3A + 2\sin 5A + \sin 7A} = \frac{\sin 3A}{\sin 5A}$$
 Hence proved.

Transformation Formulae Ex 8.2 Q 8(xi)

$$\begin{aligned} \mathsf{LHS} &= \frac{\sin \left(\theta + \phi\right) - 2 \sin \theta + \sin \left(\theta - \phi\right)}{\cos \left(\theta + \phi\right) - 2 \cos \theta + \cos \left(\theta - \phi\right)} \\ &= \frac{\sin \left(\theta + \phi\right) + \sin \left(\theta - \phi\right) - 2 \sin \theta}{\cos \left(\theta + \phi\right) + \cos \left(\theta - \phi\right) - 2 \cos \theta} \\ &= \frac{2 \sin \left[\frac{\left(\theta + \phi\right) + \left(\theta - \phi\right)}{2}\right] \cos \left[\frac{\left(\theta + \phi\right) - \left(\theta - \phi\right)}{2}\right] - 2 \sin \theta}{2 \cos \left[\frac{\left(\theta + \phi\right) + \left(\theta - \phi\right)}{2}\right] \cos \left[\frac{\left(\theta + \phi\right) - \left(\theta - \phi\right)}{2}\right] - 2 \cos \theta} \\ &= \frac{2 \sin \left(\theta\right) \cos \left(\phi\right) - 2 \sin \theta}{2 \cos \left(\theta\right) \cos \left(\phi\right) - 2 \cos \theta} \\ &= \frac{2 \sin \theta \left(\cos \phi\right) - 1}{2 \cos \theta \left(\cos \phi\right) - 1} \\ &= \frac{\sin \theta}{\cos \theta} = \tan \theta \\ &= \mathsf{RHS} \end{aligned}$$

$$\therefore \quad \frac{\sin\left(\theta+\phi\right)-2\sin\theta+\sin\left(\theta-\phi\right)}{\cos\left(\theta+\phi\right)-2\cos\theta+\cos\left(\theta-\phi\right)} = \tan\theta \qquad \qquad \text{Hence proved.}$$

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