



Exercise 4D

Question 24:

In the given $\triangle ABC$, we have,

$$\angle A : \angle B : \angle C = 3 : 2 : 1$$

Let $\angle A = 3x$, $\angle B = 2x$, $\angle C = x$. Then,

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\Rightarrow 3x + 2x + x = 180^\circ$$

$$\Rightarrow 6x = 180^\circ$$

$$\Rightarrow x = 30^\circ$$

$$\angle A = 3x = 3 \times 30^\circ = 90^\circ$$

$$\angle B = 2x = 2 \times 30^\circ = 60^\circ$$

$$\text{and, } \angle C = x = 30^\circ$$

Now, in $\triangle ABC$, we have,

$$\text{Ext } \angle ACE = \angle A + \angle B = 90^\circ + 60^\circ = 150^\circ$$

$$\angle ACD + \angle ECD = 150^\circ$$

$$\Rightarrow \angle ECD = 150^\circ - \angle ACD$$

$$\Rightarrow \angle ECD = 150^\circ - 90^\circ \quad [\text{since, } AD \perp CD, \angle ACD = 90^\circ]$$

$$\Rightarrow \angle ECD = 60^\circ$$

Question 25:

In $\triangle ABC$, AN is the bisector of $\angle A$ and $AM \perp BC$.

Now in $\triangle ABC$ we have;

$$\angle A = 180^\circ - \angle B - \angle C$$

$$\Rightarrow \angle A = 180^\circ - 65^\circ - 30^\circ$$

$$= 180^\circ - 95^\circ$$

$$= 85^\circ$$

Now, in $\triangle ANC$ we have;

$$\text{Ext. } \angle MNA = \angle NAC + 30^\circ$$

$$\begin{aligned} &= \frac{1}{2} \angle A + 30^\circ \\ &= \frac{85^\circ}{2} + 30^\circ \\ &= \frac{85^\circ + 60^\circ}{2} \\ &= \frac{145^\circ}{2} \end{aligned}$$

$$\text{Therefore, } \angle MNA = \frac{145^\circ}{2}$$

In $\triangle MAN$, we have;

$$\angle MAN = 180^\circ - \angle AMN - \angle MNA$$

$$= 180^\circ - 90^\circ - \angle MNA \quad [\text{since } AM \perp BC, \angle AMN = 90^\circ]$$

$$\begin{aligned} &= 90^\circ - \frac{145^\circ}{2} \quad [\text{since } \angle MNA = \frac{145^\circ}{2}] \\ &= \frac{180^\circ - 145^\circ}{2} \\ &= \frac{35^\circ}{2} \\ &= 17.5^\circ \end{aligned}$$

Thus, $\angle MAN =$

Question 26:

(i) False (ii) True (iii) False (iv) False (v) True (vi) True.

***** END *****