

Trigonometric Ratios Ex 5.3 Q1

Answer:

(i) Given that
$$\frac{\sin 20}{\cos 70}$$

Since $\sin (90 - \theta) = \cos \theta$

$$\Rightarrow \frac{\sin 20}{\cos 70} = \frac{\sin (90 - 70)}{\cos 70}$$

$$\Rightarrow \frac{\sin 20}{\cos 70} = \frac{\cos 70}{\cos 70}$$

$$\Rightarrow \frac{\sin 20}{\cos 70} = 1$$
Therefore $\frac{\sin 20}{\cos 70} = 1$
(ii) Given that $\frac{\cos 19}{\sin 71}$

$$\Rightarrow \frac{\cos 19}{\sin 71} = \frac{\cos (90 - 71)}{\sin 71}$$

$$\Rightarrow \frac{\cos 19}{\sin 71} = \frac{\sin 71}{\sin 71}$$

$$\Rightarrow \frac{\cos 19}{\sin 71} = 1$$

Since $\cos(90-\theta) = \sin\theta$

Therefore
$$\frac{\cos 19}{\sin 71} = \boxed{1}$$

(iii) Given that
$$\frac{\sin 21}{\cos 69}$$

Since $\sin(90-\theta) = \cos\theta$

$$\Rightarrow \frac{\sin 21}{\cos 69} = \frac{\sin (90 - 69)}{\cos 69}$$

$$\Rightarrow \frac{\sin 21}{\cos 69} = \frac{\cos 69}{\cos 69}$$

$$\Rightarrow \frac{\sin 21}{\cos 69} = \boxed{1}$$

(iv) We are given that
$$\frac{\tan 10}{\cot 80}$$

Since $\tan(90-\theta) = \cot\theta$

$$\Rightarrow \frac{\tan 10}{\cot 80} = \frac{\tan (90 - 80)}{\cot 80}$$

$$\Rightarrow \frac{\tan 10}{\cot 80} = \frac{\cot 80}{\cot 80}$$

$$\Rightarrow \frac{\tan 10}{\cot 80} = 1$$

Therefore
$$\frac{\tan 10}{\cot 80} = \boxed{1}$$

(v) Given that
$$\frac{\sec 11}{\cos ec79}$$

Since $\sec (90 - \theta) = \csc \theta$

$$\Rightarrow \frac{\sec 11}{\csc 79} = \frac{\sec (90 - 79)}{\csc 79}$$

$$\Rightarrow \frac{\sec 11}{\csc 79} = \frac{\csc 79}{\csc 79}$$

$$\Rightarrow \frac{\sec 11}{\csc 79} = 1$$

Therefore
$$\frac{\sec 11}{\csc 79} = \boxed{1}$$

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