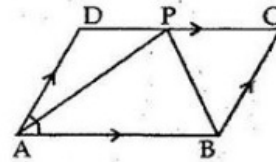




### Exercise 9B

Question 3:

ABCD is a parallelogram in which  $\angle A = 60^\circ$  and bisectors of A and B meet DC at P.



(i) In a parallelogram, opposite angles are equal.

$$\text{So, } \angle C = \angle A = 60^\circ$$

In a parallelogram the sum of all the four angles is  $360^\circ$ .

$$\Rightarrow \angle A + \angle B + \angle C + \angle D = 360^\circ$$

$$\begin{aligned} \text{Now, } \angle B + \angle D &= 360^\circ - (\angle A + \angle C) \\ &= 360^\circ - (60^\circ + 60^\circ) = 240^\circ \end{aligned}$$

$$\therefore 2\angle B = 240^\circ \quad [\because \angle B = \angle D]$$

$$\text{So, } \angle B = \angle D = \frac{240^\circ}{2} = 120^\circ$$

Since  $AB \parallel DC$  and AP is a transversal

$$\begin{aligned} \text{So, } \angle APD &= \angle PAB = \frac{60^\circ}{2} = 30^\circ \quad \dots(1) \\ &[\because \text{alternate angles}] \end{aligned}$$

Also,  $AB \parallel DC$  and BP is a transversal.

$$\text{So, } \angle ABP = \angle CPB$$

$$\text{But, } \angle ABP = \frac{\angle B}{2} = \frac{120^\circ}{2} = 60^\circ$$

$$\therefore \angle CPB = 60^\circ \quad \dots(2)$$

$$\text{Now, } \angle APD + \angle APB + \angle CPB = 180^\circ$$

[As DPC is a straightline]

$$\begin{aligned} \Rightarrow 30^\circ + \angle APB + 60^\circ &= 180^\circ \\ \angle APB &= 180^\circ - 30^\circ - 60^\circ = 90^\circ \end{aligned}$$

$$(ii) \quad \text{Since } \angle APD = 30^\circ \quad [\text{from (1)}]$$

$$\text{and } \angle DAP = \frac{60^\circ}{2} = 30^\circ$$

$$\text{So, } \angle APD = \angle DAP$$

Now in  $\triangle APD$ ,

$$\angle APD = \angle DAP \dots(3)$$

$$\therefore DP = AD \quad [\text{isosceles triangle, sides are equal}]$$

$$\text{As } \angle CPB = 60^\circ \quad [\text{from (2)}]$$

$$\text{and } \angle C = 60^\circ$$

$$\text{So, } \angle PBC = 180^\circ - 60^\circ - 60^\circ = 60^\circ$$

Since all angles in the  $\triangle PCB$  are equal, it is an equilateral triangle.

$$\therefore PB = PC = BC \dots(4)$$

$$(iii) \quad \angle DPA = \angle PAD, \quad [\text{from (3)}]$$

$$\therefore DP = AD \quad [\text{isosceles triangle, sides are equal}]$$

$$= BC \quad [\text{opposite sides are equal}]$$

$$= PC \quad [\text{from (4)}]$$

$$= \frac{1}{2} DC \quad [\because DP = PC \Rightarrow P \text{ is the midpoint of } DC]$$

$$\therefore DC = 2AD.$$

\*\*\*\*\* END \*\*\*\*\*

