



EXERCISE 3.1

Question 1:

Find the radian measures corresponding to the following degree measures:

(i) 25° (ii) $-47^\circ 30'$ (iii) 240° (iv) 520°

Ans:

(i) 25°

We know that $180^\circ = \pi$ radian

$$\therefore 25^\circ = \frac{\pi}{180} \times 25 \text{ radian} = \frac{5\pi}{36} \text{ radian}$$

(ii) $-47^\circ 30'$

$$-47^\circ 30' = -47\frac{1}{2} \text{ degree } [1^\circ = 60']$$

$$= \frac{-95}{2} \text{ degree}$$

Since $180^\circ = \pi$ radian

$$\frac{-95}{2} \text{ degree} = \frac{\pi}{180} \times \left(\frac{-95}{2}\right) \text{ radian} = \left(\frac{-19}{36 \times 2}\right) \pi \text{ radian} = \frac{-19}{72} \pi \text{ radian}$$

$$\therefore -47^\circ 30' = \frac{-19}{72} \pi \text{ radian}$$

(iii) 240°

We know that $180^\circ = \pi$ radian

$$\therefore 240^\circ = \frac{\pi}{180} \times 240 \text{ radian} = \frac{4}{3} \pi \text{ radian}$$

(iv) 520°

We know that $180^\circ = \pi$ radian

$$\therefore 520^\circ = \frac{\pi}{180} \times 520 \text{ radian} = \frac{26\pi}{9} \text{ radian}$$

(iii) 240°

We know that $180^\circ = \pi$ radian

$$\therefore 240^\circ = \frac{\pi}{180} \times 240 \text{ radian} = \frac{4}{3} \pi \text{ radian}$$

(iv) 520°

We know that $180^\circ = \pi$ radian

$$\therefore 520^\circ = \frac{\pi}{180} \times 520 \text{ radian} = \frac{26\pi}{9} \text{ radian}$$

Question 2:

Find the degree measures corresponding to the following radian measures

$\left(\text{Use } \pi = \frac{22}{7} \right)$

(i) $\frac{11}{16}$ (ii) -4 (iii) $\frac{5\pi}{3}$ (iv) $\frac{7\pi}{6}$

Ans:

(i) $\frac{11}{16}$

We know that π radian = 180°

$$\begin{aligned}\therefore \frac{11}{16} \text{ radian} &= \frac{180}{\pi} \times \frac{11}{16} \text{ deg ree} = \frac{45 \times 11}{\pi \times 4} \text{ deg ree} \\ &= \frac{45 \times 11 \times 7}{22 \times 4} \text{ deg ree} = \frac{315}{8} \text{ deg ree} \\ &= 39\frac{3}{8} \text{ deg ree} \\ &= 39^\circ + \frac{3 \times 60}{8} \text{ min utes} \quad [1^\circ = 60'] \\ &= 39^\circ + 22' + \frac{1}{2} \text{ min utes} \\ &= 39^\circ 22' 30'' \quad [1' = 60'']\end{aligned}$$

(ii) -4

We know that π radian = 180°

$$\begin{aligned}-4 \text{ radian} &= \frac{180}{\pi} \times (-4) \text{ deg ree} = \frac{180 \times 7(-4)}{22} \text{ deg ree} \\ &= \frac{-2520}{11} \text{ deg ree} = -229\frac{1}{11} \text{ deg ree} \\ &= -229^\circ + \frac{1 \times 60}{11} \text{ min utes} \quad [1^\circ = 60'] \\ &= -229^\circ + 5' + \frac{5}{11} \text{ min utes} \\ &= -229^\circ 5' 27'' \quad [1' = 60'']\end{aligned}$$

(iii) $\frac{5\pi}{3}$

We know that π radian = 180°

$$\therefore \frac{5\pi}{3} \text{ radian} = \frac{180}{\pi} \times \frac{5\pi}{3} \text{ degree} = 300^\circ$$

(iv) $\frac{7\pi}{6}$

We know that π radian = 180°

$$\therefore \frac{7\pi}{6} \text{ radian} = \frac{180}{\pi} \times \frac{7\pi}{6} = 210^\circ$$

Question 3:

A wheel makes 360 revolutions in one minute. Through how many radians does it turn in one second?

Ans:

Number of revolutions made by the wheel in 1 minute = 360

$$\therefore \text{Number of revolutions made by the wheel in 1 second} = \frac{360}{60} = 6$$

In one complete revolution, the wheel turns an angle of 2π radian.

Hence, in 6 complete revolutions, it will turn an angle of $6 \times 2\pi$ radian, i.e.,

12π radian

Thus, in one second, the wheel turns an angle of 12π radian.

Question 4:

Find the degree measure of the angle subtended at the centre of a circle of radius 100 cm by an arc of length 22 cm (Use $\pi = \frac{22}{7}$).

Ans:

We know that in a circle of radius r unit, if an arc of length l unit subtends an angle θ radian at the centre, then

$$\theta = \frac{l}{r}$$

Therefore, for $r = 100$ cm, $l = 22$ cm, we have

$$\begin{aligned} \theta &= \frac{22}{100} \text{ radian} = \frac{180}{\pi} \times \frac{22}{100} \text{ degree} = \frac{180 \times 7 \times 22}{22 \times 100} \text{ degree} \\ &= \frac{126}{10} \text{ degree} = 12\frac{3}{5} \text{ degree} = 12^\circ 36' \quad [1^\circ = 60'] \end{aligned}$$

Thus, the required angle is $12^\circ 36'$.

Question 5:

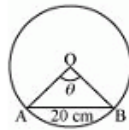
In a circle of diameter 40 cm, the length of a chord is 20 cm. Find the length of minor arc of the chord.

Ans:

Diameter of the circle = 40 cm

$$\therefore \text{Radius } (r) \text{ of the circle} = \frac{40}{2} \text{ cm} = 20 \text{ cm}$$

Let AB be a chord (length = 20 cm) of the circle.



In $\triangle OAB$, $OA = OB = \text{Radius of circle} = 20 \text{ cm}$

Also, $AB = 20 \text{ cm}$

Thus, $\triangle OAB$ is an equilateral triangle.

$$\therefore \theta = 60^\circ = \frac{\pi}{3} \text{ radian}$$

We know that in a circle of radius r unit, if an arc of length l unit subtends an angle θ radian at the centre, then $\theta = \frac{l}{r}$.

$$\frac{\pi}{3} = \frac{\widehat{AB}}{20} \Rightarrow \widehat{AB} = \frac{20\pi}{3} \text{ cm}$$

Thus, the length of the minor arc of the chord is $\frac{20\pi}{3} \text{ cm}$.

We know that in a circle of radius r unit, if an arc of length l unit subtends an angle θ radian at the centre, then $\theta = \frac{l}{r}$.

$$\frac{\pi}{3} = \frac{\widehat{AB}}{20} \Rightarrow \widehat{AB} = \frac{20\pi}{3} \text{ cm}$$

Thus, the length of the minor arc of the chord is $\frac{20\pi}{3} \text{ cm}$.

Question 6:

If in two circles, arcs of the same length subtend angles 60° and 75° at the centre, find the ratio of their radii.

Ans:

Let the radii of the two circles be r_1 and r_2 . Let an arc of length l subtend an angle of 60° at the centre of the circle of radius r_1 , while let an arc of length l subtend an angle of 75° at the centre of the circle of radius r_2 .

$$\text{Now, } 60^\circ = \frac{\pi}{3} \text{ radian and } 75^\circ = \frac{5\pi}{12} \text{ radian}$$

We know that in a circle of radius r unit, if an arc of length l unit subtends an angle θ radian at the centre, then $\theta = \frac{l}{r}$ or $l = r\theta$.

$$\therefore l = \frac{r_1\pi}{3} \text{ and } l = \frac{r_2 5\pi}{12}$$

$$\Rightarrow \frac{r_1\pi}{3} = \frac{r_2 5\pi}{12}$$

$$\Rightarrow r_1 = \frac{r_2 5}{4}$$

$$\Rightarrow \frac{r_1}{r_2} = \frac{5}{4}$$

Thus, the ratio of the radii is 5:4.

Question 7:

Find the angle in radian through which a pendulum swings if its length is 75 cm and the tip describes an arc of length

(i) 10 cm (ii) 15 cm (iii) 21 cm

Ans:

We know that in a circle of radius r unit, if an arc of length l unit subtends an angle θ radian at the centre, then $\theta = \frac{l}{r}$.

It is given that $r = 75$ cm

(i) Here, $l = 10$ cm

$$\theta = \frac{10}{75} \text{ radian} = \frac{2}{15} \text{ radian}$$

(ii) Here, $l = 15$ cm

$$\theta = \frac{15}{75} \text{ radian} = \frac{1}{5} \text{ radian}$$

(iii) Here, $l = 21$ cm

$$\theta = \frac{21}{75} \text{ radian} = \frac{7}{25} \text{ radian}$$

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