

## Trigonometric Identities Ex 6.1 Q45 Answer:

In the given question, we need to prove  $\frac{\tan^2 A}{1+\tan^2 A} + \frac{\cot^2 A}{1+\cot^2 A} = 1$ 

Here, we will first solve the LHS.

Now, using 
$$\tan\theta = \frac{\sin\theta}{\cos\theta}$$
 and  $\cot\theta = \frac{\cos\theta}{\sin\theta}$  , we get

$$\frac{\tan^{2} A}{1 + \tan^{2} A} + \frac{\cot^{2} A}{1 + \cot^{2} A} = \frac{\left(\frac{\sin^{2} A}{\cos^{2} A}\right)}{\left(1 + \frac{\sin^{2} A}{\cos^{2} A}\right)} + \frac{\left(\frac{\cos^{2} A}{\sin^{2} A}\right)}{\left(1 + \frac{\cos^{2} A}{\sin^{2} A}\right)}$$

$$= \frac{\left(\frac{\sin^{2} A}{\cos^{2} A}\right)}{\left(\frac{\cos^{2} A + \sin^{2} A}{\cos^{2} A}\right)} + \frac{\left(\frac{\cos^{2} A}{\sin^{2} A}\right)}{\left(\frac{\sin^{2} A + \cos^{2} A}{\sin^{2} A}\right)}$$

$$= \frac{\left(\frac{\sin^{2} A}{\cos^{2} A}\right)}{\left(\frac{\cos^{2} A}{\sin^{2} A}\right)} + \frac{\left(\frac{\cos^{2} A}{\sin^{2} A}\right)}{\left(\frac{\sin^{2} A}{\sin^{2} A}\right)}$$

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$$= \frac{\cos^{2} A}{\cos^{2} A} + \frac{\cos^{2} A}{\sin^{2} A}$$

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On further solving by taking the reciprocal of the denominator, we get,

$$\frac{\left(\frac{\sin^2 A}{\cos^2 A}\right)}{\left(\frac{1}{\cos^2 A}\right)} + \frac{\left(\frac{\cos^2 A}{\sin^2 A}\right)}{\left(\frac{1}{\sin^2 A}\right)} = \left(\frac{\sin^2 A}{\cos^2 A}\right) \left(\frac{\cos^2 A}{1}\right) + \left(\frac{\cos^2 A}{\sin^2 A}\right) \left(\frac{\sin^2 A}{1}\right)$$

$$= \sin^2 A + \cos^2 A \qquad \qquad \left(\text{Using } \sin^2 \theta + \cos^2 \theta = 1\right)$$

$$= 1$$

Hence proved.

Trigonometric Identities Ex 6.1 Q46

## Answer:

In the given question, we need to prove  $\frac{\cot A - \cos A}{\cot A + \cos A} = \frac{\cos \cot A - 1}{\cos \cot A + 1}$ 

Here, we will first solve the LHS.

Now, using 
$$\cot \theta = \frac{\cos \theta}{\sin \theta}$$
, we get 
$$\frac{\cot A - \cos A}{\cot A + \cos A} = \frac{\left(\frac{\cos A}{\sin A} - \cos A\right)}{\left(\frac{\cos A}{\sin A} + \cos A\right)}$$
$$= \frac{\left(\frac{\cos A - \cos A \sin A}{\sin A}\right)}{\left(\frac{\cos A + \cos A \sin A}{\sin A}\right)}$$

On further solving by taking the reciprocal of the denominator, we get,

$$\frac{\left(\frac{\cos A - \cos A \sin A}{\sin A}\right)}{\left(\frac{\cos A + \cos A \sin A}{\sin A}\right)} = \left(\frac{\cos A - \cos A \sin A}{\sin A}\right) \left(\frac{\sin A}{\cos A + \cos A \sin A}\right)$$
$$= \left(\frac{\cos A - \cos A \sin A}{\cos A + \cos A \sin A}\right)$$

Now, taking  $\cos A \sin A$  common from both the numerator and the denominator, we get

$$\left(\frac{\cos A - \cos A \sin A}{\cos A + \cos A \sin A}\right) = \frac{\cos A \sin A \left(\frac{1}{\sin A} - 1\right)}{\cos A \sin A \left(\frac{1}{\sin A} + 1\right)}$$

$$= \frac{\left(\frac{1}{\sin A} - 1\right)}{\left(\frac{1}{\sin A} + 1\right)}$$

$$= \frac{\cos \cot A - 1}{\cos \cot A + 1}$$

$$\left(\text{Using } \frac{1}{\sin \theta} = \csc \theta\right)$$

Hence proved.

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