

Derivatives as a Rate Measurer Ex 13.2 Q16(i) Here,

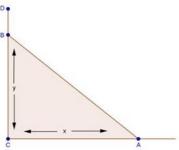
$$2\frac{d(\sin\theta)}{dt} = \frac{d\theta}{dt}$$
$$2 \times \cos\theta \frac{d\theta}{dt} = \frac{d\theta}{dt}$$
$$2\cos\theta = 1$$
$$\cos\theta = \frac{1}{2}$$

$$\theta = \frac{\pi}{3}.$$

Derivatives as a Rate Measurer Ex 13.2 Q16(ii)

$$\frac{d\theta}{dt} = -2\frac{d}{dt}(\cos\theta)$$
$$\frac{d\theta}{dt} = -2(-\sin\theta)\frac{d\theta}{dt}$$
$$1 = 2\sin\theta$$
$$\sin\theta = \frac{1}{2}$$
$$\theta = \frac{\pi}{6}$$

Derivatives as a Rate Measurer Ex 13.2 Q17



Let CD be the wall and AB is the ladder

Here, AB = 6 meter and $\left(\frac{dx}{dt}\right)_{x=4} = 0.5$ m/sec.

From figure,

$$AB^{2} = x^{2} + y^{2}$$

$$(6)^{2} = x^{2} + y^{2}$$

$$36 = x^{2} + y^{2}$$

$$(6)^2 = x^2 + y$$

$$36 = x^2 + v^2$$

$$0 = 2x \frac{ax}{dt} + 2y \frac{ay}{dt}$$

$$\frac{dy}{dt} = -\frac{x}{y}\frac{dx}{dt}$$

Differentiating it with respect to
$$t$$
,
$$0 = 2x \frac{dx}{dt} + 2y \frac{dy}{dt}$$
$$\frac{dy}{dt} = -\frac{x}{y} \frac{dx}{dt}$$
$$\left(\frac{dy}{dt}\right)_{x=4} = \frac{4(0.5)}{\sqrt{36 - x^2}}$$
$$= -\frac{2}{\sqrt{36 - 16}}$$
$$= -\frac{2}{2\sqrt{5}}$$
$$= -\frac{1}{\sqrt{5}} \text{ m/sec.}$$

So, ladder top is sliding at the rate of $\frac{1}{\sqrt{5}}$ m/sec.

Now, to find x when $\frac{dx}{dt} = -\frac{dy}{dt}$

From equation (i),

$$\frac{dy}{dt} = -\frac{x}{v} \frac{dx}{dt}$$

$$\frac{dy}{dt} = -\frac{x}{y}\frac{dx}{dt}$$
$$-\frac{dx}{dt} = -\frac{x}{y}\frac{dx}{dt}$$
$$x = y$$

$$x = y$$

Now,

$$36 = x^2 + y^2$$

$$36 = x^2 + x^2$$

$$2x^2 = 36$$

$$x^2 = 18$$

$$x = 3.5 \text{ r}$$

When foot and top are moving at the same rate, foot of wall is $3\sqrt{2}$ meters away from the wall

********* END *******