

Differentiation Ex 11.2 Q57

Consider

$$y = \log \sqrt{\frac{x-1}{x+1}}$$

 $y=\log\sqrt{\frac{x-1}{x+1}}$ Differentiating it with respect to x and applying the chain and product rule, we get

$$y = \log\left(\frac{x-1}{x+1}\right)^{\frac{1}{2}}$$

$$y = \frac{1}{2}\log\left(\frac{x-1}{x+1}\right)$$

$$y = \frac{1}{2}\left[\log\left(x-1\right) - \log\left(x+1\right)\right]$$

$$\frac{dy}{dx} = \frac{1}{2}\left[\frac{d}{dx}\log\left(x-1\right) - \frac{d}{dx}\log\left(x+1\right)\right]$$

$$= \frac{1}{2}\left(\frac{1}{x-1} - \frac{1}{x+1}\right)$$

$$= \frac{1}{2}\left(\frac{2}{x^2-1}\right)$$

$$\frac{dy}{dx} = \frac{1}{x^2-1}$$
Therefore,
$$\frac{dy}{dx} = \frac{1}{x^2-1}$$

Differentiation Ex 11.2 Q58

Here
$$y = \log \left\{ \sqrt{x-1} - \sqrt{x+1} \right\}$$

Differentiating it with respect to x and applying the chain and product rule, we get

Differentiating it with respect to x and applying the charge
$$\frac{dy}{dx} = \frac{d}{dx} \log \left\{ \sqrt{x-1} - \sqrt{x+1} \right\}$$

$$\frac{dy}{dx} = \frac{1}{\left\{ \sqrt{x-1} - \sqrt{x+1} \right\}} \frac{d}{dx} \left(\sqrt{x-1} - \sqrt{x+1} \right)$$

$$= \frac{1}{\left\{ \sqrt{x-1} - \sqrt{x+1} \right\}} \left[\frac{d}{dx} \sqrt{x-1} - \frac{d}{dx} \sqrt{x+1} \right]$$

$$= \frac{1}{\left\{ \sqrt{x-1} - \sqrt{x+1} \right\}} \left[\frac{1}{2} (x-1)^{-\frac{1}{2}} - \frac{1}{2} (x+1)^{-\frac{1}{2}} \right]$$

$$= \frac{1}{2} \frac{1}{\left\{ \sqrt{x-1} - \sqrt{x+1} \right\}} \left(\frac{1}{\sqrt{x-1}} - \frac{1}{\sqrt{x+1}} \right)$$

$$= \frac{1}{2} \frac{1}{\left\{ \sqrt{x-1} - \sqrt{x+1} \right\}} \left(\frac{-\left\{ \sqrt{x-1} - \sqrt{x+1} \right\}}{\left(\sqrt{x-1} \right) \left(\sqrt{x+1} \right)} \right)$$

$$= \frac{-1}{2} \left(\frac{1}{\left(\sqrt{x-1} \right) \left(\sqrt{x+1} \right)} \right)$$
Therefore,
$$\frac{dy}{dx} = \frac{-1}{2\sqrt{x^2-1}}$$

Differentiation Ex 11.2 Q59

Here
$$y = \sqrt{x+1} + \sqrt{x-1}$$

Differentiating it with respect to x and applying the chain and product rule, we get $\frac{dy}{dx} = \frac{d}{dx}\sqrt{x+1} + \frac{d}{dx}\sqrt{x-1}$

$$\frac{dy}{dx} = \frac{d}{dx}\sqrt{x+1} + \frac{d}{dx}\sqrt{x-1}$$

$$= \frac{1}{2}(x+1)^{-\frac{1}{2}} + \frac{1}{2}(x-1)^{-\frac{1}{2}}$$

$$= \frac{1}{2}\left(\frac{1}{\sqrt{x+1}} + \frac{1}{\sqrt{x-1}}\right)$$

$$= \frac{1}{2}\left(\frac{\sqrt{x-1} + \sqrt{x+1}}{(\sqrt{x+1})(\sqrt{x-1})}\right)$$

$$\frac{dy}{dx} = \frac{1}{2}\left(\frac{y}{(\sqrt{x^2-1})}\right)$$

$$\sqrt{x^2-1}\frac{dy}{dx} = \frac{1}{2}y$$

Differentiation Ex 11.2 Q60

Here
$$y = \frac{x}{x+2}$$

Differentiating it with respect to x and applying the chain and product rule, we get

$$\frac{dy}{dx} = \frac{d}{dx} \left(\frac{x}{x+2} \right)$$

$$= \frac{(x+2)\frac{dx}{dx} - x\frac{d}{dx}(x+2)}{(x+2)^2}$$

$$= \frac{x+2-x}{(x+2)^2}$$

$$= \frac{x+2}{(x+2)^2} - \frac{x}{(x+2)^2}$$

$$= \frac{1}{x+2} - \frac{xy^2}{x^2}$$

$$= \frac{y}{x} - \frac{y^2}{x}$$

$$\frac{dy}{dx} = \frac{1}{x}y(1-y)$$

$$x\frac{dy}{dx} = (1-y)y$$

Differentiation Ex 11.2 Q61

Here
$$y = \log\left(\sqrt{x} + \frac{1}{\sqrt{x}}\right)$$

Differentiating it with respect to x and applying the chain and product rule, we get

$$\frac{dy}{dx} = \frac{d}{dx} \log \left(x^{\frac{1}{2}} + x^{-\frac{1}{2}} \right)$$

$$= \frac{1}{x^{\frac{1}{2}} + x^{-\frac{1}{2}}} \frac{d}{dx} \left(x^{\frac{1}{2}} + x^{-\frac{1}{2}} \right)$$

$$= \frac{1}{\sqrt{x} + \frac{1}{\sqrt{x}}} \left(\frac{1}{2} x^{-\frac{1}{2}} - \frac{1}{2} x^{-\frac{1}{2}} x^{-1} \right)$$

$$= \frac{1}{2} \frac{\sqrt{x}}{x + 1} \left(\frac{1}{\sqrt{x}} - \frac{1}{x \sqrt{x}} \right)$$

$$= \frac{1}{2} \frac{\sqrt{x}}{x + 1} \left(\frac{x - 1}{x \sqrt{x}} \right)$$

$$\frac{dy}{dx} = \frac{x - 1}{2x(x + 1)}$$

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