

Binomial Theorem Ex 18.2 Q15(vi)

$$\left(3-\frac{x^3}{6}\right)^7$$

Here n = 7, which is odd

∴ middle term is
$$\left(\frac{7+1}{2}\right)$$
 and $\left(\frac{7+1}{2}+1\right) = 4^{sk}, 5^{sk}$ terms
$$T_{\kappa} = T_{r+1} = (-1)^{r} {}^{\kappa}C_{r}x^{\kappa-r}y^{r}$$

$$T_{4} = T_{3+1} = (-1)^{3} {}^{3}C_{3}(3)^{7-3}\left(\frac{x^{3}}{6}\right)^{3}$$

$$= -\frac{7!}{3!4!} \times 3^{4} \times \frac{x^{9}}{6^{3}}$$

$$= -\frac{7 \times 6 \times 5}{3 \times 2 \times 1} \times 81 \times \frac{x^{9}}{216}$$

$$= -\frac{105}{9}x^{9}$$

And

$$\begin{split} T_{\kappa} &= T_{r+1} = (-1)^{r} {}^{\kappa} C_{r} x^{\kappa - r} y^{r} \\ T_{5} &= T_{4+1} = (-1)^{4} {}^{7} C_{4} (3)^{7-4} \left(\frac{x^{3}}{6}\right)^{4} \\ &= \frac{7!}{4!3!} \times 3^{3} \times \frac{x^{12}}{6^{4}} \\ &= \frac{7 \times 6 \times 5}{3 \times 2 \times 1} \times 27 \times \frac{x^{12}}{1296} \\ &= \frac{35}{48} x^{12} \end{split}$$

Binomial Theorem Ex 18.2 Q15(vii)

$$\left(\frac{x}{3} + 9y\right)^{10}$$

Here n=10, which is even, therefore it has 11 terms

.. middle term is
$$\left(\frac{n}{2}+1\right) = 6^{\frac{1}{6}}$$
 term
$$T_{x} = T_{y+1} = (-1)^{y} C_{y} x^{x-y} y^{y}$$

$$T_{6} = T_{5+1} = (-1)^{5} C_{5} \left(\frac{x}{3}\right)^{10-5} (9y)^{5}$$

$$= -\frac{10!}{5!5!} \times \frac{x^{5}}{3^{5}} \times 9^{5} \times y^{5}$$

$$= 61236 x^{5} y^{5}$$

Binomial Theorem Ex 18.2 Q15(viii)

For the given binomial expansion n = 12.

So middle term is $\left(\frac{12}{2} + 1\right) = 7^{\text{th}}$ term.

$$T_7 = {}^{12}C_6 (2ax)^{12-6} \left(-\frac{b}{x^2}\right)^6$$

$$T_7 = {}^{12}C_6 (2ax)^6 \left(\frac{b}{x^2}\right)^6$$

$$T_7 = {}^{12}C_6 (2^6a^6x^6) \left(\frac{b^6}{x^{12}}\right)$$

$$T_7 = {}^{12}C_6 \left(\frac{2^6a^6b^6}{x^6}\right)$$

Middle term is
$${}^{12}C_6 \left(\frac{2^6 a^6 b^6}{x^6}\right)$$
.

Binomial Theorem Ex 18.2 Q15(ix)

For the given binomial expansion n = 9.

So middle terms are $\left(\frac{9+1}{2}\right) = 5^{\text{th}}$ term and $\left(\frac{9+3}{2}\right) = 6^{\text{th}}$ term.

$$T_{5} = {}^{9}C_{4} \left(\frac{p}{x}\right)^{9-4} \left(\frac{x}{p}\right)^{4}$$

$$T_{5} = {}^{9}C_{4} \left(\frac{p}{x}\right)^{5} \left(\frac{x}{p}\right)^{4}$$

$$T_{5} = {}^{9}C_{4} \left(\frac{p}{x}\right)$$

$$T_{6} = {}^{9}C_{5} \left(\frac{p}{x}\right)^{9-5} \left(\frac{x}{p}\right)^{5}$$

$$T_{6} = {}^{9}C_{5} \left(\frac{p}{x}\right)^{4} \left(\frac{x}{p}\right)^{5}$$

$$T_{6} = {}^{9}C_{5} \left(\frac{x}{p}\right)$$

The middle terms are ${}^9C_4\!\left(\!\frac{p}{\times}\!\right)$ and ${}^9C_5\!\left(\!\frac{\times}{p}\!\right)$

Binomial Theorem Ex 18.2 Q15(x)

For the given binomial expansion n = 10.

So middle term is $\left(\frac{10}{2} + 1\right) = 6^{\text{th}}$ term.

$$T_{6} = {}^{10}C_{5} \left(\frac{x}{a}\right)^{10-5} \left(-\frac{a}{x}\right)^{5}$$

$$T_{6} = -{}^{10}C_{5} \left(\frac{x}{a}\right)^{5} \left(\frac{a}{x}\right)^{5}$$

$$T_{6} = -{}^{10}C_{5} = -252$$

Middle term is -252.