

Trigonometric Identities Ex 6.1 Q33

Answer:

We need to prove
$$\frac{\left(1+\tan^2\theta\right)\cot\theta}{\csc^2\theta} = \tan\theta$$
Solving the L.H.S, we get
$$\frac{\left(1+\tan^2\theta\right)\cot\theta}{\cos\csc^2\theta} = \frac{\sec^2\theta(\cot\theta)}{\csc^2\theta}$$
Using $\sec\theta = \frac{1}{\cos\theta}$, $\cot\theta = \frac{\cos\theta}{\sin\theta}$ and $\csc\theta = \frac{1}{\sin\theta}$, we get
$$\frac{\sec^2\theta(\cot\theta)}{\csc^2\theta} = \frac{\frac{1}{\cos^2\theta}\left(\frac{\cos\theta}{\sin\theta}\right)}{\frac{1}{\sin^2\theta}}$$

$$= \frac{1}{\frac{\cos\theta\sin\theta}{\cos\theta\sin\theta}}$$

$$= \frac{\sin^2\theta}{\cos\theta\sin\theta}$$

$$= \frac{\sin\theta}{\cos\theta}$$

$$= \tan\theta$$

Hence proved.

Trigonometric Identities Ex 6.1 Q34

Answer:

We need to prove
$$\frac{1+\cos A}{\sin^2 A} = \frac{1}{1-\cos A}$$
Using the property
$$\cos^2 \theta + \sin^2 \theta = 1$$
. we get
$$LHS = \frac{1+\cos A}{\sin^2 A} = \frac{1+\cos A}{1-\cos^2 A}$$
Further using the identity,
$$a^2 - b^2 = (a+b)(a-b)$$
. we get
$$\frac{1+\cos A}{1-\cos^2 A} = \frac{1+\cos A}{(1-\cos A)(1+\cos A)}$$

$$= \frac{1}{1-\cos A}$$

$$= RHS$$

Hence proved.

Trigonometric Identities Ex 6.1 Q35

Answer:

We need to prove
$$\frac{\sec A - \tan A}{\sec A + \tan A} = \frac{\cos^2 A}{(1 + \sin A)^2}$$

Here, we will first solve the LHS.

Now, using
$$\sec \theta = \frac{1}{\cos \theta}$$
 and $\tan \theta = \frac{\sin \theta}{\cos \theta}$, we get
$$\frac{\sec A - \tan A}{\sec A + \tan A} = \frac{\frac{1}{\cos A} - \frac{\sin A}{\cos A}}{\frac{1}{\cos A} + \frac{\sin A}{\cos A}}$$
$$= \frac{1 - \sin A}{\frac{\cos A}{\cos A}}$$
$$= \frac{1 - \sin A}{\frac{\cos A}{\cos A}}$$
$$= \frac{1 - \sin A}{\frac{\cos A}{\cos A}}$$

Further, multiplying both numerator and denominator by $1 + \sin A$, we get

$$\frac{1-\sin A}{1+\sin A} = \left(\frac{1-\sin A}{1+\sin A}\right) \left(\frac{1+\sin A}{1+\sin A}\right)$$
$$= \frac{(1-\sin A)(1+\sin A)}{(1+\sin A)^2}$$
$$= \frac{1-\sin^2 A}{(1+\sin A)^2}$$

Now, using the property $\cos^2 \theta + \sin^2 \theta = 1$, we get So.

$$\frac{1-\sin^2 A}{(1+\sin A)^2} = \frac{\cos^2 A}{(1+\sin A)^2} = RHS$$

Hence proved.

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