

Indefinite Integrals Ex 19.18 Q10

Indefinite Integrals Ex 19.18 Q11

$$\int \frac{\sin 2x}{\sqrt{\cos^{4} x - \sin^{2} x + 2}} dx =$$

$$let \ t = \cos^{2} x \to -dt = 2\cos x \sin x dx$$

$$\int \frac{\sin 2x}{\sqrt{\cos^{4} x - \sin^{2} x + 2}} dx = \int \frac{-1}{\sqrt{t^{2} - (1 - t) + 2}} dt$$

$$= \int \frac{-1}{\sqrt{t^{2} + t + 1}} dt = \int \frac{-1}{\sqrt{t^{2} + t + \frac{1}{4} + \frac{3}{4}}} dt$$

$$= \int \frac{-1}{\sqrt{\left(t + \frac{1}{2}\right)^{2} + \frac{3}{4}}} dt = -\log\left|\left(t + \frac{1}{2}\right) + \sqrt{t^{2} + t + 1}\right|$$

$$= -\log\left|\left(\cos^{2} x + \frac{1}{2}\right) + \sqrt{\cos^{4} x + \cos^{2} x + 1}\right| + C$$

Indefinite Integrals Ex 19.18 Q12

$$I = \sin^{-1}\left(\frac{\sin x}{2}\right) + c$$

Indefinite Integrals Ex 19.18 Q13

Let 
$$I = \int \frac{1}{x^{\frac{2}{3}} \sqrt{x^{\frac{2}{3}} - 4}} dx$$
  
Let  $x^{\frac{1}{3}} = t$   

$$\Rightarrow \qquad \frac{1}{3} x^{\frac{1}{3} - 1} dx = dt$$

$$\Rightarrow \qquad \frac{1}{3} x^{-\frac{2}{3}} dx = dt$$

$$\Rightarrow \qquad \frac{dx}{x^{\frac{2}{3}}} = 3dt$$

$$I = 3\int \frac{dt}{\sqrt{t^2 - (2)^2}}$$

$$= 3\log\left|t + \sqrt{t^2 - 4}\right| + c\left[\text{Since } \int \frac{1}{\sqrt{x^2 - a^2}} dx = \log\left|x + \sqrt{x^2 - a^2}\right| + c\right]$$

$$I == 3\log \left| x^{\frac{1}{3}} + \sqrt{x^{\frac{2}{3}} - 4} \right| + c$$

\*\*\*\*\*\*\*\*\* END \*\*\*\*\*\*\*