



Adjoint and Inverse of Matrix Ex 7.1 Q7 (i)

$$A = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix}$$

Now, $|A| = 1 \neq 0$

Hence A^{-1} exists.

Cofactors of A are:

$$\begin{aligned} C_{11} &= \cos \theta & C_{21} &= -\sin \theta \\ C_{12} &= \sin \theta & C_{22} &= \cos \theta \end{aligned}$$

$$\begin{aligned} \therefore \text{adj} A &= \begin{bmatrix} C_{11} & C_{12} \\ C_{21} & C_{22} \end{bmatrix}^T \\ &= \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix} \end{aligned}$$

$$\therefore \text{adj} A = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}$$

$$\text{Now, } A^{-1} = \frac{1}{|A|} \text{adj} A$$

$$A^{-1} = \frac{1}{1} \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}$$

$$A^{-1} = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}$$

Adjoint and Inverse of Matrix Ex 7.1 Q7 (ii)

$$A = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$$

Now, $|A| = -1 \neq 0$

Hence A^{-1} exists.

Cofactors of A are:

$$\begin{array}{ll} C_{11} = 0 & C_{12} = -1 \\ C_{21} = -1 & C_{22} = 0 \end{array}$$

$$\begin{aligned} \therefore \text{adj } A &= \begin{bmatrix} C_{11} & C_{12} \\ C_{21} & C_{22} \end{bmatrix}^T \\ &= \begin{bmatrix} 0 & -1 \\ -1 & 0 \end{bmatrix} \end{aligned}$$

Also, $A^{-1} = \frac{1}{|A|} (\text{adj } A)$

$$A^{-1} = \frac{1}{(-1)} \begin{bmatrix} 0 & -1 \\ -1 & 0 \end{bmatrix}$$

$$A^{-1} = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$$

$$A = \begin{bmatrix} a & b \\ c & \frac{1+bc}{a} \end{bmatrix}$$

$$\text{Now, } |A| = \frac{a+abc}{a} - bc = \frac{a+abc-abc}{a} = 1 \neq 0$$

Hence A^{-1} exists.

Now, cofactors of A are:

$$C_{11} = \frac{1+bc}{a} \quad C_{12} = -c$$

$$C_{21} = -b \quad C_{22} = a$$

$$\begin{aligned} \therefore \text{adj} A &= \begin{bmatrix} C_{11} & C_{12} \\ C_{21} & C_{22} \end{bmatrix}^T \\ &= \begin{bmatrix} \frac{1+bc}{a} & -c \\ -b & a \end{bmatrix}^T \end{aligned}$$

$$\therefore \text{adj} A = \begin{bmatrix} \frac{1+bc}{a} & -b \\ -c & a \end{bmatrix}$$

$$\text{Also, } A^{-1} = \frac{1}{|A|} \cdot \text{adj} A$$

$$A^{-1} = \frac{1}{1} \begin{bmatrix} \frac{1+bc}{a} & -b \\ -c & a \end{bmatrix}$$

$$\text{or } A^{-1} = \begin{bmatrix} \frac{1+bc}{a} & -b \\ -c & a \end{bmatrix}$$

Adjoint and Inverse of Matrix Ex 7.1 Q7 (iv)

$$A = \begin{bmatrix} 2 & 5 \\ -3 & 1 \end{bmatrix}$$

$$\text{Now, } |A| = 2 + 15 = 17 \neq 0$$

Hence A^{-1} exists.

Now, cofactors of A are:

$$C_{11} = 1 \qquad C_{12} = 3$$

$$C_{21} = -5 \qquad C_{22} = 2$$

$$\begin{aligned} \therefore \quad \text{adj } A &= \begin{bmatrix} C_{11} & C_{12} \\ C_{21} & C_{22} \end{bmatrix}^T \\ &= \begin{bmatrix} 1 & 3 \\ -5 & 2 \end{bmatrix} \end{aligned}$$

$$\therefore \quad \text{adj } A = \begin{bmatrix} 1 & -5 \\ 3 & 2 \end{bmatrix}$$

$$A^{-1} = \frac{1}{|A|} \cdot (\text{adj } A)$$

$$A^{-1} = \frac{1}{17} \begin{bmatrix} 1 & -5 \\ 3 & 2 \end{bmatrix}$$

$$\text{Hence, } A^{-1} = \frac{1}{17} \begin{bmatrix} 1 & -5 \\ 3 & 2 \end{bmatrix}$$

***** END *****

