

## Co-Ordinate Geometry Ex 14.3 Q22

We have two points P (3, 3) and Q (6,-6). There are two points A and B which trisect the line segment joining P and Q.

Let the co-ordinate of A be  $\mathbf{A}ig(x_1,y_1ig)$ 

Now according to the section formula if any point P divides a line segment joining  $A(x_1,y_1)$  and

 $\mathbf{B}(x_2,y_2)$  in the ratio m: n internally than,

$$P(x,y) = \left(\frac{nx_1 + mx_2}{m+n}, \frac{ny_1 + my_2}{m+n}\right)$$

The point A is the point of trisection of the line segment PQ. So, A divides PQ in the ratio 1: 2

Now we will use section formula to find the co-ordinates of unknown point A as,

$$A(x,y) = \left(\frac{2(3)+1(6)}{1+2}, \frac{2(3)+1(-6)}{1+2}\right)$$
$$= (4,0)$$

Therefore, co-ordinates of point A is(4, 0)

It is given that point A lies on the line whose equation is

$$2x + y + k = 0$$

So point A will satisfy this equation.

$$2(4)+0+k=0$$

So,

k = -8

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## Answer:

Let ABCD be a parallelogram in which the co-ordinates of the vertices are A (-2,-1); B (1,0); C (x,3) and D (1,y).

Since ABCD is a parallelogram, the diagonals bisect each other. Therefore the mid-point of the diagonals of the parallelogram will coincide.

In general to find the mid-point P(x,y) of two points  $A(x_1,y_1)$  and  $B(x_2,y_2)$  we use section formula as

$$P(x,y) = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$

The mid-point of the diagonals of the parallelogram will coincide.

So

Co-ordinate of mid-point of AC = Co-ordinate of mid-point of BD

Therefore

$$\left(\frac{x-2}{2}, \frac{3-1}{2}\right) = \left(\frac{1+1}{2}, \frac{y+0}{2}\right)$$

Now equate the individual terms to get the unknown value. So,

$$\frac{x-2}{2} = 1$$

$$x = 4$$

Similarly,

$$\frac{y+0}{2} = 1$$

$$y = 2$$

Therefore.

$$x = 4$$
$$y = 2$$

## Answer:

Let A (2, 0); B (9, 1); C (11, 6) and D (4, 4) be the vertices of a quadrilateral. We have to check if the quadrilateral ABCD is a rhombus or not.

So we should find the lengths of sides of quadrilateral ABCD.

$$AB = \sqrt{(9-2)^2 + (1-0)^2}$$

$$= \sqrt{49+1}$$

$$= \sqrt{50}$$

$$BC = \sqrt{(11-9)^2 + (6-1)^2}$$

$$= \sqrt{4+25}$$

$$= \sqrt{29}$$

$$CD = \sqrt{(11-4)^2 + (6-4)^2}$$

$$= \sqrt{49+4}$$

$$= \sqrt{53}$$

$$AD = \sqrt{(4-2)^2 + (4-0)^2}$$

$$= \sqrt{4+16}$$

$$= \sqrt{20}$$

All the sides of quadrilateral are unequal. Hence ABCD is not a rhombus.

