

NCERT Solutions For Class 10 Chapter 5 Maths Arithmetic Progressions Exercise 5.2

1. Find the missing variable from a, d, n and a_n , where a is the first term, d is the common difference and a_n is the nth term of AP.

(i)
$$a = 7$$
, $d = 3$, $n = 8$

(ii)
$$a = -18$$
, $n = 10$, $a_n = 0$

(iii)
$$d = -3$$
, $n = 18$, $a_n = -5$

(iv)
$$a = -18.9$$
, $d = 2.5$, $a_n = 3.6$

$$(v)$$
 a = 3.5, d = 0, n = 105

Ans. (i)
$$a = 7$$
, $d = 3$, $n = 8$

We need to find a_n here.

Using formula $a_n = a + (n-1)d$

Putting values of a, d and n,

$$a_n = 7 + (8 - 1)3$$

$$= 7 + (7) 3 = 7 + 21 = 28$$

(ii)
$$a = -18$$
, $n = 10$, $a_n = 0$

We need to find d here.

Using formula $a_n = a + (n-1)d$

Putting values of a, a_n and n,

$$0 = -18 + (10 - 1) d$$

$$\Rightarrow 0 = -18 + 9d$$

$$\Rightarrow$$
 18 = 9 $d \Rightarrow d = 2$

(iii)
$$d = -3$$
, $n = 18$, $a_n = -5$

We need to find a here.

Using formula $a_n = a + (n-1)d$

Putting values of d, a_n and n,

$$-5 = a + (18 - 1)(-3)$$

$$\Rightarrow -5 = a + (17)(-3)$$

$$\Rightarrow -5 = a - 51 \Rightarrow a = 46$$

(iv)
$$a = -18.9$$
, $d = 2.5$, $a_n = 3.6$

We need to find n here.

Using formula $a_n = a + (n-1)d$

Putting values of d, a_n and n,

$$3.6 = -18.9 + (n - 1)(2.5)$$

$$\Rightarrow 3.6 = -18.9 + 2.5n - 2.5$$

$$\Rightarrow 2.5n = 25 \Rightarrow n = 10$$

We need to find a_n here.

Using formula $a_n = a + (n-1)d$

Putting values of d, n and a,

$$a_n = 3.5 + (105 - 1)(0)$$

$$\Rightarrow a_n = 3.5 + 104 \times 0$$

$$\Rightarrow a_n = 3.5 + 0 \Rightarrow a_n = 3.5$$

- 2. Choose the correct choice in the following and justify:
- (i) 30th term of the AP: 10, 7, 4... is
- (A) 97
- (B) 77
- (C) -77
- (D) 87
- (ii) 11^{th} term of the AP: -3, -12, 2... is
- (A) 28
- (B) 22
- (C) 38
- **(D)** $-48\frac{1}{2}$

Ans.(i) 10, 7, 4...

First term = a = 10, Common difference = d = 7- 10 = 4 - 7 = -3

And n = 30{Because, we need to find 30^{th} term}

$$a_n = a + (n-1)d$$

$$\Rightarrow a_{30} = 10 + (30 - 1)(-3) = 10 - 87 = -77$$

Therefore, the answer is (C).

First term = a = -3, Common difference = d = -

$$\frac{1}{2}$$
 - (-3) = 2 - ($-\frac{1}{2}$) = $\frac{5}{2}$

And n = 11 (Because, we need to find 11^{th} term)

$$a_n = -3 + (11 - 1) \frac{5}{2} = -3 + 25 = 22$$

Therefore 11th term is 22 which means answer is (B).

3. In the following AP's find the missing terms:

(iii) 5, ___, __,
$$9\frac{1}{2}$$

We know that difference between consecutive terms is equal in any A.P.

Let the missing term be x.

$$x - 2 = 26 - x$$

$$\Rightarrow 2x = 28 \Rightarrow x = 14$$

Therefore, missing term is 14.

Let missing terms be x and y.

The sequence becomes x, 13, y, 3

We know that difference between consecutive terms is constant in any A.P.

$$y - 13 = 3 - y$$

$$\Rightarrow 2y = 16 \Rightarrow y = 8$$

And
$$13 - x = y - 13$$

$$\Rightarrow x + y = 26$$

But, we have y = 8,

$$\Rightarrow x + 8 = 26 \Rightarrow x = 18$$

Therefore, missing terms are 18 and 8.

Here, first term = a = 5 And, 4^{th} term = $a_4 = 9\frac{1}{2}$

Using formula $a_n = a + (n-1)d$, to find nth term of arithmetic progression,

$$a_4 = 5 + (4 - 1)d$$

$$\Rightarrow \frac{19}{2} = 5 + 3d$$

$$\Rightarrow$$
 19 = 2 (5 + 3d)

$$\Rightarrow$$
 19 = 10 + 6d

$$\Rightarrow 6d = 9 \Rightarrow d = \frac{3}{2}$$

Therefore, we get common difference = $d = \frac{3}{2}$

Second term =
$$a + d = 5 + \frac{3}{2} = \frac{13}{2}$$

Third term = second term + d = $\frac{13}{2} + \frac{3}{2} = \frac{16}{2} = 8$

Therefore, missing terms are $\frac{13}{2}$ and 8

Here, First term = a = -4 and 6^{th} term = $a_6 = 6$

Using formula $a_n = a + (n-1)d$, to find n^{th} term of arithmetic progression,

$$a_6 = -4 + (6 - 1) d$$

$$\Rightarrow 6 = -4 + 5d$$

$$\Rightarrow 5d = 10 \Rightarrow d = 2$$

Therefore, common difference = d = 2

Second term = first term + d = a + d = -4 + 2 = -2

Third term = second term + d = -2 + 2 = 0

Fourth term = third term + d = 0 + 2 = 2

Fifth term = fourth term + d = 2 + 2 = 4

Therefore, missing terms are -2, 0, 2 and 4.

We are given 2nd and 6th term.

Using formula $a_n = a + (n-1)d$, to find nth term of arithmetic progression,

$$a_2 = a + (2 - 1) d$$
 And $a_6 = a + (6 - 1) d$

$$\Rightarrow 38 = a + d \text{ And } -22 = a + 5d$$

These are equations in two variables, we can solve them using any method.

Using equation (38 = a + d), we can say that a = 38 - d.

Putting value of a in equation (-22 = a + 5d),

$$-22 = 38 - d + 5d$$

$$\Rightarrow 4d = -60$$

$$\Rightarrow d = -15$$

Using this value of d and putting this in equation 38 = a + d,

$$38 = a - 15 \Rightarrow a = 53$$

Therefore, we get a = 53 and d = -15

First term = a = 53

Third term = second term + d = 38 - 15 = 23

Fourth term = third term + d = 23 - 15 = 8

Fifth term = fourth term + d = 8 - 15 = -7

Therefore, missing terms are 53, 23, 8 and -7.

******* END *******