

Exercise 3D

Question 23:

$$(a - 1)x + 3y - 2 = 0$$
  
 $6x + (1 - 2b)y - 6 = 0$ 

These equations are of the form

$$a_1x + b_1y + c_1 = 0$$
,  $a_2x + b_2y + c_2 = 0$   
where,  $a_1 = (a - 1)$ ,  $b_1 = 3$ ,  $c_1 = -2$   
 $a_2 = 6$ ,  $b_2 = (1 - 2b)$ ,  $c_2 = -6$ 

For infinite many solutions, we must have

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$$

$$\frac{(a-1)}{6} = \frac{3}{(1-2b)} = \frac{-2}{-6}$$

$$\Rightarrow \frac{a-1}{6} = \frac{3}{(1-2b)} = \frac{1}{3}$$

$$\Rightarrow \frac{a-1}{6} = \frac{3}{(1-2b)} = \frac{1}{3}$$

$$\Rightarrow \frac{a-1}{6} = \frac{1}{3} \text{ and } \frac{3}{(1-2b)} = \frac{1}{3}$$

$$\Rightarrow 3a-3=6 \text{ and } 9=1-2b$$

$$\Rightarrow 3a=6+3 \text{ and } 2b=1-9$$

$$3a=9 \Rightarrow a=\frac{9}{3}=3 \text{ and } 2b=-8$$

$$b=\frac{-8}{2}=-4$$

Question 24:

$$(2a - 1)x + 3y - 5 = 0$$
  
 $3x + (b - 1)y - 2 = 0$ 

These equations are of the form

$$a_1 \times + b_1 y + c_1 = 0$$
,  $a_2 \times + b_2 y + c_2 = 0$   
where,  $a_1 = (2a - 1)$ ,  $b_1 = 3$ ,  $c_1 = -5$   
 $a_2 = 3$ ,  $b_2 = (b - 1)$ ,  $c_2 = -2$ 

These holds only when

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$$

$$\frac{(2a-1)}{3} = \frac{3}{(b-1)} = \frac{-5}{-2}$$

$$\frac{(2a-1)}{3} = \frac{3}{(b-1)} = \frac{5}{2}$$

$$\frac{(2a-1)}{3} = \frac{5}{2} \text{ and } \frac{3}{(b-1)} = \frac{5}{2}$$

$$4a-2 = 15 \text{ and } 5(b-1) = 6$$

$$4a = 17 \text{ and } 5b-5 = 6$$

$$a = \frac{17}{4} \text{ and } 5b = 11$$

$$b = \frac{11}{5}$$

$$a = \frac{17}{4} \text{ and } b = \frac{11}{5}$$

\*\*\*\*\*\*\*\*\* END \*\*\*\*\*\*\*\*