

$$A = \begin{bmatrix} 2 & -1 & 4 \\ 4 & 0 & 2 \\ 3 & -2 & 7 \end{bmatrix}$$

Now,
$$A = IA$$

$$\begin{bmatrix}
2 & -1 & 4 \\
4 & 0 & 2 \\
3 & -2 & 7
\end{bmatrix} = \begin{bmatrix}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 1
\end{bmatrix}.A$$

Applying
$$R_1 \rightarrow \frac{1}{2}R_1$$

$$\begin{bmatrix} 1 & \frac{-1}{2} & 2 \\ 4 & 0 & 2 \\ 3 & -2 & 7 \end{bmatrix} = \begin{bmatrix} \frac{1}{2} & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} . A$$

Applying
$$R_2 \rightarrow R_2 - 4R_1$$
, $R_3 \rightarrow R_3 - 3R_1$

$$\begin{bmatrix} 1 & \frac{-1}{2} & 2 \\ 0 & 2 & -6 \\ 0 & \frac{-1}{2} & 1 \end{bmatrix} = \begin{bmatrix} \frac{1}{2} & 0 & 0 \\ -2 & 1 & 0 \\ \frac{-3}{2} & 0 & 1 \end{bmatrix} A$$

Applying
$$R_2 \rightarrow \frac{1}{2} R_2$$

$$\begin{bmatrix} 1 & \frac{-1}{2} & 2 \\ 0 & 1 & -3 \\ 0 & \frac{-1}{2} & 1 \end{bmatrix} = \begin{bmatrix} \frac{1}{2} & 0 & 0 \\ -1 & \frac{1}{2} & 0 & A \\ \frac{-3}{2} & 0 & 1 \end{bmatrix}$$

Applying
$$R_1 \to R_1 + \frac{1}{2}R_2$$
, $R_3 \to R_3 + \frac{1}{2}R_2$

$$\begin{bmatrix} 1 & 0 & \frac{1}{2} \\ 0 & 1 & -3 \\ 0 & 0 & \frac{-1}{2} \end{bmatrix} = \begin{bmatrix} 0 & \frac{1}{4} & 0 \\ -1 & \frac{1}{2} & 0 \\ -2 & \frac{1}{4} & 1 \end{bmatrix}.A$$

Applying $R_3 \rightarrow (-2) R_3$

$$\begin{bmatrix} 1 & 0 & \frac{1}{2} \\ 0 & 1 & -3 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 0 & \frac{1}{4} & 0 \\ -1 & \frac{1}{2} & 0 \\ 4 & \frac{-1}{2} & -2 \end{bmatrix} . A$$

Applying $R_1 \rightarrow R_1 - \frac{1}{2}R_3$, $R_2 \rightarrow R_2 + 3R_3$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} -2 & \frac{1}{2} & 1 \\ 11 & -1 & -6 \\ 4 & \frac{-1}{2} & -2 \end{bmatrix} . A$$

$$I = B.A$$

Hence, B is the inv. of A.

$$A = \begin{bmatrix} 3 & 0 & -1 \\ 2 & 3 & 0 \\ 0 & 4 & 1 \end{bmatrix}$$

Now,
$$A = IA$$

$$\begin{bmatrix} 3 & 0 & -1 \\ 2 & 3 & 0 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix} A$$

$$\begin{bmatrix} 0 & 4 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 1 \end{bmatrix}$$

Applying
$$R_1 \rightarrow \frac{1}{3}R_1$$

$$\begin{bmatrix} 1 & 0 & \frac{-1}{3} \\ 2 & 3 & 0 \\ 0 & 4 & 1 \end{bmatrix} = \begin{bmatrix} \frac{1}{3} & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}.A$$

Applying
$$R_2 \rightarrow R_2 - 2R_1$$

$$\begin{bmatrix} 1 & 0 & \frac{-1}{3} \\ 0 & 3 & \frac{2}{3} \\ 0 & 4 & 1 \end{bmatrix} = \begin{bmatrix} \frac{1}{3} & 0 & 0 \\ \frac{-2}{3} & 1 & 0 & A \\ 0 & 0 & 1 \end{bmatrix}$$

Applying
$$R_2 \rightarrow \frac{1}{3}R_2$$

$$\begin{bmatrix} 1 & 0 & \frac{-1}{3} \\ 0 & 1 & \frac{2}{9} \\ 0 & 4 & 1 \end{bmatrix} = \begin{bmatrix} \frac{1}{3} & 0 & 0 \\ \frac{-2}{9} & \frac{1}{3} & 0 \\ 0 & 0 & 1 \end{bmatrix} A$$

Applying
$$R_3 \rightarrow R_3 - 4R_2$$

$$\begin{bmatrix} 1 & 0 & \frac{-1}{3} \\ 0 & 1 & \frac{2}{9} \\ 0 & 0 & \frac{1}{9} \end{bmatrix} = \begin{bmatrix} \frac{1}{3} & 0 & 0 \\ \frac{-2}{9} & \frac{1}{3} & 0 \\ \frac{8}{9} & \frac{-4}{3} & 1 \end{bmatrix} A$$

Applying
$$R_3 \rightarrow 9.R_3$$

$$\begin{bmatrix} 1 & 0 & \frac{-1}{3} \\ 0 & 1 & \frac{2}{9} \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} \frac{1}{3} & 0 & 0 \\ \frac{-2}{9} & \frac{1}{3} & 0 \\ 8 & -12 & 9 \end{bmatrix} A$$

Applying
$$R_1 \rightarrow R_1 + \frac{1}{3}R_3$$
, $R_2 \rightarrow R_2 - \frac{2}{9}R_3$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 3 & -4 & 3 \\ -2 & 3 & -2 \\ 8 & -12 & 9 \end{bmatrix} .A$$

or
$$I = B.A$$

Hence, B is the inv. of A.

Consider the given matrix:

$$Let A = \begin{bmatrix} 1 & 3 & -2 \\ -3 & 0 & 1 \\ 2 & 1 & 0 \end{bmatrix}$$

We know that A = IA

Thus, we have,

$$\begin{bmatrix} 1 & 3 & -2 \\ -3 & 0 & 1 \\ 2 & 1 & 0 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} A$$

Applying $R_2 \rightarrow 3R_1 + R_2$ and $R_3 \rightarrow R_3 - 2R_1$, we have,

$$\begin{bmatrix} 1 & 3 & -2 \\ 0 & 9 & -5 \\ 0 & -5 & 4 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 3 & 1 & 0 \\ -2 & 0 & 1 \end{bmatrix} A$$

Applying $R_1 \rightarrow R_1 - 3R_2$ and $R_3 \rightarrow R_3 + 5R_2$, we have,

$$\begin{bmatrix} 1 & 0 & \frac{-1}{3} \\ 0 & 1 & \frac{-5}{9} \\ 0 & 0 & \frac{11}{9} \end{bmatrix} = \begin{bmatrix} 0 & \frac{-1}{3} & 0 \\ \frac{1}{3} & \frac{1}{9} & 0 \\ \frac{-1}{3} & \frac{5}{9} & 1 \end{bmatrix} A$$

Applying $R_1 \rightarrow \frac{R_1}{\frac{11}{9}}$ we have,

$$\begin{bmatrix} 1 & 0 & \frac{-1}{3} \\ 0 & 1 & \frac{-5}{9} \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 0 & \frac{-1}{3} & 0 \\ \frac{1}{3} & \frac{1}{9} & 0 \\ \frac{-3}{11} & \frac{5}{11} & \frac{9}{11} \end{bmatrix} A$$

Applying $R_2 \rightarrow R_2 + \frac{5}{9}R_3$ and $R_1 \rightarrow R_1 + \frac{1}{3}R_3$, we have,

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} \frac{-1}{11} & \frac{-2}{11} & \frac{3}{11} \\ \frac{2}{11} & \frac{4}{11} & \frac{5}{11} \\ \frac{-3}{11} & \frac{5}{11} & \frac{9}{11} \end{bmatrix} A$$

⇒ Inverse of the given matrix is $\begin{vmatrix} -1 & -2 & 3 \\ 11 & 11 & 11 \\ 2 & 4 & 5 \\ 11 & 11 & 11 \\ -3 & 5 & 9 \\ 11 & 11 & 11 \end{vmatrix}$

Consider the given matrix
$$\begin{bmatrix} -1 & 1 & 2 \\ 1 & 2 & 3 \end{bmatrix}$$

$$Let \ A = \begin{bmatrix} -1 & 1 & 2 \\ 1 & 2 & 3 \\ 3 & 1 & 1 \end{bmatrix}$$

We know that A = IA

$$\Rightarrow \begin{bmatrix} -1 & 1 & 2 \\ 1 & 2 & 3 \\ 3 & 1 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} A$$

Applying $R_1 \rightarrow (-1)R_1$, we have

$$\begin{bmatrix} 1 & -1 & -2 \\ 1 & 2 & 3 \\ 3 & 1 & 1 \end{bmatrix} = \begin{bmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} A$$

Applying $R_2 \rightarrow R_2 - R_1$, $R_3 \rightarrow R_3 - 3R_1$, we have

$$\begin{bmatrix} 1 & -1 & -2 \\ 0 & 3 & 5 \\ 0 & 4 & 7 \end{bmatrix} = \begin{bmatrix} -1 & 0 & 0 \\ 1 & 1 & 0 \\ 3 & 0 & 1 \end{bmatrix} A$$

Applying $R_2 \rightarrow \frac{R_2}{3}$, we have,

$$\begin{bmatrix} 1 & -1 & -2 \\ 0 & 1 & \frac{5}{3} \\ 0 & 4 & 7 \end{bmatrix} = \begin{bmatrix} -1 & 0 & 0 \\ \frac{1}{3} & \frac{1}{3} & 0 \\ 3 & 0 & 1 \end{bmatrix} A$$

Applying $R_1 \rightarrow R_1 + R_2$ and $R_3 \rightarrow R_3 - 4R_2$, we have

$$\begin{bmatrix} 1 & 0 & -\frac{1}{3} \\ 0 & 1 & \frac{5}{3} \\ 0 & 0 & \frac{1}{3} \end{bmatrix} = \begin{bmatrix} -\frac{2}{3} & \frac{1}{3} & 0 \\ \frac{1}{3} & \frac{1}{3} & 0 \\ \frac{5}{3} & \frac{-4}{3} & 1 \end{bmatrix} A$$

Applying $R_3 \rightarrow \frac{R_3}{3}$, we have

$$\begin{bmatrix} 1 & 0 & -\frac{1}{3} \\ 0 & 1 & \frac{5}{3} \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} -\frac{2}{3} & \frac{1}{3} & 0 \\ \frac{1}{3} & \frac{1}{3} & 0 \\ 5 & -4 & 3 \end{bmatrix}^{A}$$

Applying $R_1 \to R_1 + \frac{1}{3} R_3$, $R_2 \to R_2 - \frac{5}{3} R_3$, we have,

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & -1 & 1 \\ -8 & 7 & -5 \\ 5 & -4 & 3 \end{bmatrix} A$$

Thus, the inverse of the given matrix is $\begin{bmatrix} 1 & -1 & 1 \\ -8 & 7 & -5 \\ 5 & -4 & 3 \end{bmatrix}$.