

Exercise 7.2: Solutions of Questions on Page Number: 304

Q1: $\frac{2x}{1+x^2}$

Answer:

Let $1 + x^2 = t$

 $\therefore 2x dx = dt$

$$\Rightarrow \int \frac{2x}{1+x^2} dx = \int \frac{1}{t} dt$$

 $=\log|t|+C$

 $= \log \left| 1 + x^2 \right| + C$

 $= \log(1+x^2) + C$

Answer needs Correction? Click Here

Q2: $\frac{(\log x)^2}{x}$

Answer:

Let $\log |x| = t$

$$\therefore \frac{1}{x} dx = dt$$

$$x \Rightarrow \int \frac{(\log|x|)^2}{x} dx = \int t^2 dt$$
$$= \frac{t^3}{3} + C$$
$$= \frac{(\log|x|)^3}{3} + C$$

Answer needs Correction? Click Here

Q3: $\frac{1}{x + x \log x}$

Answer:

$$\frac{1}{x + x \log x} = \frac{1}{x \left(1 + \log x\right)}$$

Let $1 + \log x = t$

$$\therefore \frac{1}{x} dx = dt$$

$$\Rightarrow \int \frac{1}{x(1+\log x)} dx = \int \frac{1}{t} dt$$

$$=\log |t| + C$$

$$= \log |1 + \log x| + C$$

Answer needs Correction? Click Here

Q4: sin xâ‹â€¦ sin (cos x)

Answer:

sin x â‹â€¦ sin (cos x)

Let $\cos x = t$

$$\therefore$$
 - $\sin x \, dx = dt$

$$\Rightarrow \int \sin x \cdot \sin(\cos x) dx = -\int \sin t dt$$
$$= -[-\cos t] + C$$

 $=\cos t + C$

 $=\cos(\cos x)+C$

Answer needs Correction? Click Here

Q5: $\sin(ax+b)\cos(ax+b)$

Answer:

$$\sin(ax+b)\cos(ax+b) = \frac{2\sin(ax+b)\cos(ax+b)}{2} = \frac{\sin 2(ax+b)}{2}$$

Let 2(ax+b)=t

∴ 2*adx = dt*

$$\Rightarrow \int \frac{\sin 2(ax+b)}{2} dx = \frac{1}{2} \int \frac{\sin t}{2a} dt$$

$$= \frac{1}{4a} [-\cos t] + C$$

$$= \frac{-1}{4a} \cos 2(ax+b) + C$$

Answer needs Correction? Click Here

Q6: $\sqrt{ax+b}$

Answer:

Let ax + b = t

$$\Rightarrow adx = dt$$

$$\therefore dx = \frac{1}{a}dt$$

$$\Rightarrow \int (ax+b)^{\frac{1}{2}} dx = \frac{1}{a} \int t^{\frac{1}{2}} dt$$

$$=\frac{1}{a}\left(\frac{t^{\frac{3}{2}}}{\frac{3}{2}}\right)+C$$

$$=\frac{2}{3a}(ax+b)^{\frac{3}{2}}+C$$

Answer needs Correction? Click Here

Q7: $x\sqrt{x+2}$

Answer:

Let (x+2)=t

$$\therefore dx = dt$$

$$\Rightarrow \int x\sqrt{x+2}dx = \int (t-2)\sqrt{t}dt$$

$$= \int (t^{\frac{3}{2}}-2t^{\frac{1}{2}})dt$$

$$= \int t^{\frac{3}{2}}dt - 2\int t^{\frac{1}{2}}dt$$

$$= \frac{t^{\frac{5}{2}}}{\frac{5}{2}} - 2\left(\frac{t^{\frac{3}{2}}}{\frac{3}{2}}\right) + C$$

$$= \frac{2}{5}t^{\frac{5}{2}} - \frac{4}{3}t^{\frac{3}{2}} + C$$

$$= \frac{2}{5}(x+2)^{\frac{5}{2}} - \frac{4}{3}(x+2)^{\frac{3}{2}} + C$$

Answer needs Correction? Click Here

Q8: $x\sqrt{1+2x^2}$

Answer:

Let
$$1 + 2x^2 = t$$

$$\therefore 4xdx = dt$$

$$\Rightarrow \int x\sqrt{1+2x^2} dx = \int \frac{\sqrt{t}dt}{4}$$

$$= \frac{1}{4} \int t^{\frac{1}{2}} dt$$

$$= \frac{1}{4} \left(\frac{t^{\frac{3}{2}}}{\frac{3}{2}}\right) + C$$

$$= \frac{1}{6} \left(1+2x^2\right)^{\frac{3}{2}} + C$$

Answer needs Correction? Click Here

Q9: $(4x+2)\sqrt{x^2+x+1}$

Answer:

Let $x^2 + x + 1 = t$

 $\therefore (2x+1)dx = dt$

$$\int (4x+2)\sqrt{x^2+x+1} \ dx$$
=\int 2\sqrt{t} \ dt
=2\int \frac{t^\frac{3}{2}}{\frac{3}{2}} + C
=\frac{4}{3}(x^2+x+1)^\frac{3}{2} + C

Answer needs Correction? Click Here

Q10:
$$\frac{1}{x - \sqrt{x}}$$

Answer:

$$\frac{1}{x - \sqrt{x}} = \frac{1}{\sqrt{x} \left(\sqrt{x} - 1\right)}$$

Let
$$(\sqrt{x}-1)=t$$

$$\therefore \frac{1}{2\sqrt{x}} dx = dt$$

$$\Rightarrow \int \frac{1}{\sqrt{x} \left(\sqrt{x} - 1 \right)} dx = \int \frac{2}{t} dt$$

$$=2\log|t|+C$$

$$=2\log\left|\sqrt{x}-1\right|+C$$

Answer needs Correction? Click Here

Q11:
$$\frac{x}{\sqrt{x+4}}, x > 0$$

Answer:

Let
$$x+4=t$$

$$\therefore dx = dt$$

********* END *******