



Trigonometric Identities Ex 6.1 Q21

Answer :

We have to prove $(1 + \tan^2 \theta)(1 - \sin \theta)(1 + \sin \theta) = 1$

We know that,

$$\sin^2 \theta + \cos^2 \theta = 1,$$

$$\sec^2 \theta - \tan^2 \theta = 1$$

So,

$$\begin{aligned}(1 + \tan^2 \theta)(1 - \sin \theta)(1 + \sin \theta) &= (1 + \tan^2 \theta) \{(1 - \sin \theta)(1 + \sin \theta)\} \\ &= (1 + \tan^2 \theta)(1 - \sin^2 \theta) \\ &= \sec^2 \theta \cos^2 \theta \\ &= \frac{1}{\cos^2 \theta} \cos^2 \theta \\ &= 1\end{aligned}$$

Trigonometric Identities Ex 6.1 Q22

Answer :

We have to prove $\sin^2 A \cot^2 A + \cos^2 A \tan^2 A = 1$

We know that, $\sin^2 A + \cos^2 A = 1$

So,

$$\begin{aligned}\sin^2 A \cot^2 A + \cos^2 A \tan^2 A &= \sin^2 A \frac{\cos^2 A}{\sin^2 A} + \cos^2 A \frac{\sin^2 A}{\cos^2 A} \\ &= \cos^2 A + \sin^2 A \\ &= 1\end{aligned}$$

Trigonometric Identities Ex 6.1 Q23

Answer :

(i) We have to prove $\cot \theta - \tan \theta = \frac{2 \cos^2 \theta - 1}{\sin \theta \cos \theta}$

We know that, $\sin^2 \theta + \cos^2 \theta = 1$

So,

$$\begin{aligned}\cot \theta - \tan \theta &= \frac{\cos \theta}{\sin \theta} - \frac{\sin \theta}{\cos \theta} \\&= \frac{\cos^2 \theta - \sin^2 \theta}{\sin \theta \cos \theta} \\&= \frac{\cos^2 \theta - (1 - \cos^2 \theta)}{\sin \theta \cos \theta} \\&= \frac{\cos^2 \theta - 1 + \cos^2 \theta}{\sin \theta \cos \theta} \\&= \frac{2 \cos^2 \theta - 1}{\sin \theta \cos \theta}\end{aligned}$$

(ii) We have to prove $\tan \theta - \cot \theta = \frac{2 \sin^2 \theta - 1}{\sin \theta \cos \theta}$

We know that, $\sin^2 \theta + \cos^2 \theta = 1$

So,

$$\begin{aligned}\tan \theta - \cot \theta &= \frac{\sin \theta}{\cos \theta} - \frac{\cos \theta}{\sin \theta} \\&= \frac{\sin^2 \theta - \cos^2 \theta}{\sin \theta \cos \theta} \\&= \frac{\sin^2 \theta - (1 - \sin^2 \theta)}{\sin \theta \cos \theta} \\&= \frac{\sin^2 \theta - 1 + \sin^2 \theta}{\sin \theta \cos \theta} \\&= \frac{2 \sin^2 \theta - 1}{\sin \theta \cos \theta}\end{aligned}$$

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