

Differentiation Ex 11.1 Q5

Let
$$f(x) = e^{\sqrt{2x}}$$

$$\Rightarrow f(x+h) = e^{\sqrt{2(x+h)}}$$

$$\frac{d}{dx}(f(x)) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

$$= \lim_{h \to 0} e^{\sqrt{2x}} \frac{e^{\sqrt{2(x+h)} - \sqrt{2x}} - 1}{h}$$

$$= e^{\sqrt{2x}} \lim_{h \to 0} \frac{\sqrt{2(x+h) - \sqrt{2x}} - 1}{\sqrt{2(x+h) - \sqrt{2x}}} \left[\frac{\sqrt{2(x+h) - \sqrt{2x}}}{h} \right]$$

$$= e^{\sqrt{2x}} \lim_{h \to 0} \frac{\sqrt{2(x+h) - \sqrt{2x}}}{h} \left[\text{Since, } \lim_{h \to 0} \frac{e^{h} - 1}{h} = 1 \right]$$

$$= e^{\sqrt{2x}} \lim_{h \to 0} \frac{\sqrt{2(x+h) - \sqrt{2x}}}{h} \times \frac{\sqrt{2(x+h) + \sqrt{2x}}}{\sqrt{2(x+h) + \sqrt{2x}}}$$

$$= e^{\sqrt{2x}} \lim_{h \to 0} \frac{2(x+h) - 2x}{h(\sqrt{2(x+h) + \sqrt{2x}})}$$

$$= e^{\sqrt{2x}} \lim_{h \to 0} \frac{2x + 2h - 2x}{h(\sqrt{2(x+h) + \sqrt{2x}})}$$

$$= e^{\sqrt{2x}} \lim_{h \to 0} \frac{2h}{h(\sqrt{2(x+h) + \sqrt{2x}})}$$

Differentiation Ex 11.1 Q6

Let
$$f(x) = \log \cos x$$

$$\Rightarrow f(x+h) = \log \cos (x+h)$$

$$\therefore \frac{d}{dx} (f(x)) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

$$\frac{d}{dx}(f(x)) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

$$= \lim_{h \to 0} \frac{\log \cos(x+h) - \log \cos x}{h}$$

$$= \lim_{h \to 0} \frac{\log \frac{\cos(x+h)}{\cos x}}{h} \qquad \left[\text{Since, } \log A - \log B = \log \frac{A}{B} \right]$$

$$= \lim_{h \to 0} \frac{\log \left\{ 1 + \frac{\cos(x+h)}{\cos x} - 1 \right\}}{h}$$

$$= \lim_{h \to 0} \frac{\log \left\{ 1 + \frac{\cos(x+h)}{\cos x} - 1 \right\}}{h}$$

$$= \lim_{h \to 0} \frac{\log \left\{ 1 + \frac{\cos(x+h)}{\cos x} - 1 \right\}}{\left(\frac{\cos(x+h)}{\cos x} \right) h \times \left(\frac{\cos x}{\cos(x+h) - \cos x} \right)}$$

$$= \lim_{h \to 0} \frac{\cos(x+h) - \cos x}{\cos x \times h} \qquad \left[\text{Since, } \lim_{x \to 0} \frac{\log(1+x)}{x} = 1 \right]$$

$$= \lim_{h \to 0} \frac{-2\sin\left(\frac{x+h+x}{2}\right)\sin\left(\frac{x+h-x}{2}\right)}{\cos x \times h}$$

$$= -2\lim_{h \to 0} \frac{\sin\left(\frac{2x+h}{2}\right) \times \left(\sin\frac{h}{2}\right)}{2\cos x}$$

$$= -\tan x$$

$$\left[\text{Since, } \lim_{x \to 0} \frac{\sin x}{x} = 1 \right]$$

So, $\frac{d}{dx} (\log \cos x) = -\tan x$

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