

## Differentiation Ex 11.5 Q58

Consider the given function,  $(x-y)e^{\frac{x}{x-y}}=a$ .

We need to prove that  $y \frac{dy}{dx} + x = 2y$ .

Differentiating the given equation w.r.t. 'x' we get

$$(x-y) \left[ e^{\frac{R}{R-y}} \left( \frac{(x-y)-x\left(1-\frac{dy}{dx}\right)}{(x-y)^2} \right) \right] + e^{\frac{R}{R-y}} \left( 1-\frac{dy}{dx} \right) = 0$$

$$\Rightarrow \frac{(x-y)-x\left(1-\frac{dy}{dx}\right)}{(x-y)} + \left( 1-\frac{dy}{dx} \right) = 0$$

$$\Rightarrow \left( 1-\frac{dy}{dx} \right) \left( 1-\frac{x}{x-y} \right) + 1 = 0$$

$$\Rightarrow \left( 1-\frac{dy}{dx} \right) \left( \frac{-y}{x-y} \right) + 1 = 0$$

$$\Rightarrow -y+y\frac{dy}{dx} + x-y = 0$$

$$\Rightarrow y\frac{dy}{dx} + x = 2y$$

Differentiation Ex 11.5 Q59

$$x = e^{x/y}$$

$$\log x = \frac{x}{y}.....(i)$$

$$y = \frac{x}{\log x}$$

$$\frac{dy}{dx} = \frac{\log x \frac{d}{dx}(x) - x \frac{d}{dx}(\log x)}{(\log x)^2}$$

$$\frac{dy}{dx} = \frac{\log x - x \times \frac{1}{x}}{\left(\log x\right)^2}$$

$$\frac{dy}{dx} = \frac{\log x - 1}{\left(\log x\right)^2}$$

$$\frac{dy}{dx} = \frac{\frac{x}{y} - 1}{(\log x)^2} \cdot \dots \cdot [from (i)]$$

$$\frac{dy}{dx} = \frac{x - y}{v(loqx)^2}$$

$$\frac{dy}{dx} = \frac{x - y}{x(log x)} \dots \left[from (i)\right]$$

Differentiation Ex 11.5 Q60

$$\begin{aligned} & y = x^{tan \times} + \sqrt{\frac{x^2 + 1}{2}} \\ & y = e^{tan \times log \times} + e^{\frac{1}{2}log\left(\frac{x^2 + 1}{2}\right)} \\ & \frac{dy}{dx} = e^{tan \times log \times} \frac{d}{dx} \left(tan \times log \times\right) + e^{\frac{1}{2}log\left(\frac{x^2 + 1}{2}\right)} \frac{d}{dx} \left(\frac{1}{2}log\left(\frac{x^2 + 1}{2}\right)\right) \\ & \frac{dy}{dx} = x^{tan \times} \left[\frac{tan \times}{x} + sec^2 \times log \times\right] + \sqrt{\frac{x^2 + 1}{2}} \left(\frac{1}{2} \times \frac{2}{x^2 + 1} \times (x)\right) \\ & \frac{dy}{dx} = x^{tan \times} \left[\frac{tan \times}{x} + sec^2 \times log \times\right] + \sqrt{\frac{x^2 + 1}{2}} \left(\frac{x}{x^2 + 1}\right) \\ & \frac{dy}{dx} = x^{tan \times} \left[\frac{tan \times}{x} + sec^2 \times log \times\right] + \frac{x}{\sqrt{2(x^2 + 1)}} \end{aligned}$$

Differentiation Ex 11.5 Q61

$$y = 1 + \frac{\alpha}{\left(\frac{1}{x} - \alpha\right)} + \frac{\beta/x}{\left(\frac{1}{x} - \alpha\right)\left(\frac{1}{x} - \beta\right)} + \frac{\gamma/x^2}{\left(\frac{1}{x} - \alpha\right)\left(\frac{1}{x} - \beta\right)\left(\frac{1}{x} - \gamma\right)}$$

$$\begin{cases} \text{Using the theorem,} \\ \text{If } y = 1 + \frac{ax^2}{\left(x - a\right)\left(x - b\right)\left(x - c\right)} + \frac{bx}{\left(x - b\right)\left(x - c\right)} + \frac{c}{\left(x - c\right)} \text{ then,} \end{cases}$$

$$\frac{dy}{dx} = \frac{y}{x} \left\{ \frac{a}{a - x} + \frac{b}{b - x} + \frac{c}{c - x} \right\}$$

Here we have  $\frac{1}{x}$  instead of x.

So using above theorem we get,

$$\frac{dy}{dx} = \frac{\alpha}{\left(\frac{1}{x} - \alpha\right)} + \frac{\beta}{\left(\frac{1}{x} - \beta\right)} + \frac{\gamma}{\left(\frac{1}{x} - \gamma\right)}$$

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