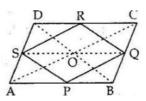


## Exercise 10A

## Question 21:

Given: ABCD is a parallelogram and P,Q,R and S are the midpoints of AB,BC,CD and DA respectively.



To Prove: PQRS is a parallelogram and  $ar(\parallel gmPQRS)$ 

$$= \frac{1}{2} \operatorname{ar} (\| \operatorname{gm} \operatorname{ABCD})$$

Construction: Join AC, BD and SQ.

Proof: As S and R are the midpoints of AD and CD.So, in  $\triangle$  ADC,

Also, as P and Q are the midpoints of AB and BC.So, in  $\triangle$ ABC,

Similarly , we can prove SP  $\parallel$  RQ.

Thus PQRS is a parallelogram as its opposite sides are parallel since diagonals of a parallelogram bisect each other. So in  $\Delta ABD$ ,

O is the midpoint of AC and S is the midpoint of AD.

Similarly in  $\Delta ABC$ , we can prove that,

$$\mathsf{OQ}\, \|\mathsf{AB}$$

Thus, ABQS is a parallelogram.

Now, 
$$ar(\Delta SPQ) = \frac{1}{2}ar(\|gmABQS)$$
 ....(i)

 $\because \Delta \text{SPQ}$  and  $\parallel \text{gm}$  ABQS have the same base and lie between same parallel lines

Similarly, we can prove that;

$$ar(\Delta SRQ) = \frac{1}{2}ar(\parallel gm SQCD)$$
 ....(ii

Adding (i) and (ii) we get

$$\operatorname{ar}(\Delta \mathsf{SPQ}) + \operatorname{ar}(\Delta \mathsf{SRQ}) = \frac{1}{2} \big[ \operatorname{ar}(\|\mathsf{gmABQS}) + \operatorname{ar}(\|\mathsf{gmSQCD}) \big]$$

$$ar(\|gmPQRS) = \frac{1}{2}ar(\|gmABCD)$$

\*\*\*\*\*\*\*\*\* END \*\*\*\*\*\*\*