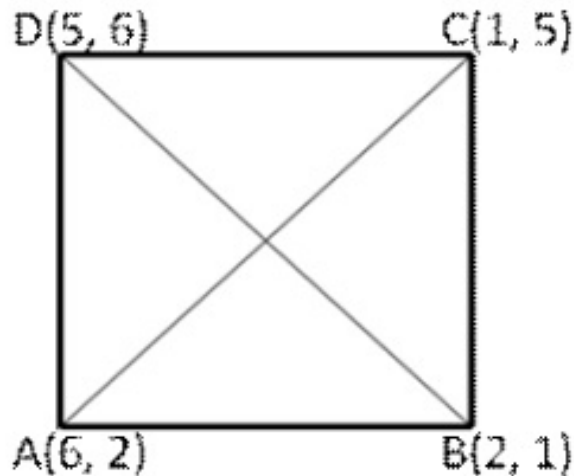




Exercise 16A

Question 21:

(i) Let A(6,2), B(2,1), C(1,5) and D(5,6) be the angular points of quad. ABCD. Join AC and BD



Now,

$$AB = \sqrt{(2-6)^2 + (1-2)^2} = \sqrt{(-4)^2 + (-1)^2} = \sqrt{16+1} = \sqrt{17} \text{ units}$$

$$BC = \sqrt{(1-2)^2 + (5-1)^2} = \sqrt{(-1)^2 + (4)^2} = \sqrt{1+16} = \sqrt{17} \text{ units}$$

$$CD = \sqrt{(5-1)^2 + (6-5)^2} = \sqrt{(4)^2 + (1)^2} = \sqrt{16+1} = \sqrt{17} \text{ unit}$$

$$DA = \sqrt{(6-5)^2 + (2-6)^2} = \sqrt{(1)^2 + (-4)^2} = \sqrt{1+16} = \sqrt{17} \text{ unit}$$

thus, $AB = BC = CD = DA$

$$\text{Diag } AC = \sqrt{(1-6)^2 + (5-2)^2} = \sqrt{(-5)^2 + (3)^2} = \sqrt{25+9} = \sqrt{34} \text{ units}$$

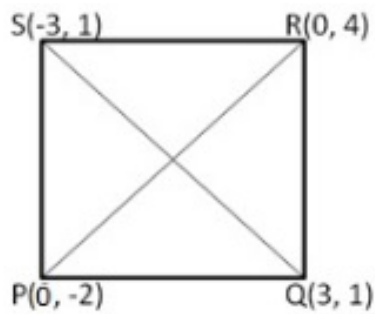
$$\text{Diag } BD = \sqrt{(5-2)^2 + (6-1)^2} = \sqrt{(3)^2 + (5)^2} = \sqrt{9+25} = \sqrt{34} \text{ units}$$

$\therefore \text{Diag } AC = \text{Diag } BD$

Thus, ABCD is a quadrilateral in which all sides are equal and the diagonals are equal.

Hence, quad ABCD is a square.

(ii) Let P(0, -2), Q(3,1), R(0,4) and S(-3,1) be the angular points of quad. ABCD



Join PR and QS

Now,

$$PQ = \sqrt{(3-0)^2 + (1+2)^2} = \sqrt{(3)^2 + (3)^2} = \sqrt{9+9} = \sqrt{18} = 3\sqrt{2} \text{ units}$$

$$QR = \sqrt{(0-3)^2 + (4-1)^2} = \sqrt{(-3)^2 + (3)^2} = \sqrt{9+9} = \sqrt{18} = 3\sqrt{2} \text{ unit}$$

$$RS = \sqrt{(-3-0)^2 + (1-4)^2} = \sqrt{(-3)^2 + (-3)^2} = \sqrt{9+9} = \sqrt{18} = 3\sqrt{2} \text{ unit}$$

$$SP = \sqrt{(0+3)^2 + (-2-1)^2} = \sqrt{(3)^2 + (-3)^2} = \sqrt{9+9} = \sqrt{18} = 3\sqrt{2} \text{ unit}$$

Thus, $PQ = QR = RS = SP$

$$\text{Diag. PR} = \sqrt{(0-0)^2 + (4+2)^2} = \sqrt{(6)^2} = 6 \text{ units}$$

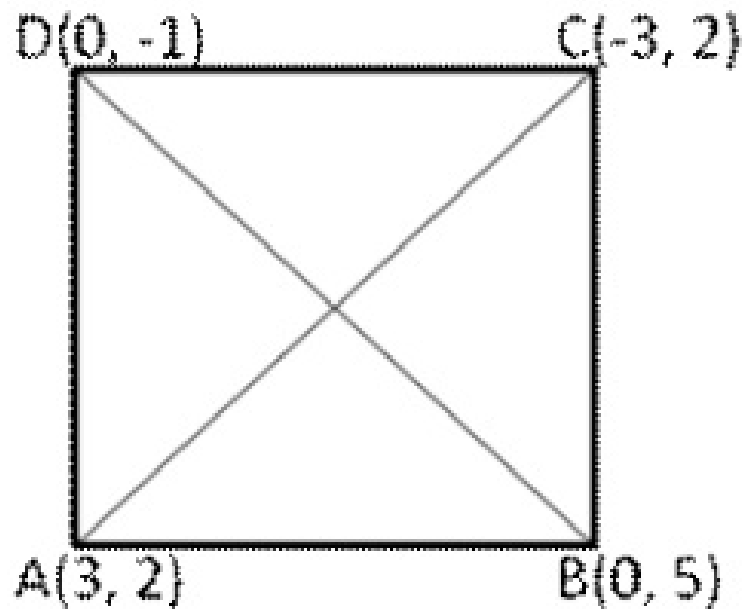
$$\text{Diag. QS} = \sqrt{(-3-3)^2 + (1-1)^2} = \sqrt{(-6)^2} = 6 \text{ units}$$

$\therefore \text{Diag. PR} = \text{Diag. QS}$

Thus, PQRS is a quadrilateral in which all sides are equal and the diagonals are equal.

Hence, quad. PQRS is a square.

(iii) The angular points of quadrilateral ABCD are A(3,2), B(0,5), C(-3,2) and D(0,-1)



$$AB = \sqrt{(0-3)^2 + (5-2)^2} = \sqrt{9+9} = \sqrt{18} = 3\sqrt{2}$$

$$BC = \sqrt{(-3-0)^2 + (2-5)^2} = \sqrt{9+9} = \sqrt{18} = 3\sqrt{2}$$

$$CD = \sqrt{(0+3)^2 + (-1-2)^2} = \sqrt{9+9} = \sqrt{18} = 3\sqrt{2}$$

$$DA = \sqrt{(3-0)^2 + (2+1)^2} = \sqrt{9+9} = \sqrt{18} = 3\sqrt{2}$$

$$\therefore AB = BC = CD = DA = 3\sqrt{2}$$

$$\text{Diag. AC} = \sqrt{(-3-3)^2 + (2-2)^2} = 6$$

$$\text{Diag. BD} = \sqrt{(0-0)^2 + (-1-5)^2} = 6$$

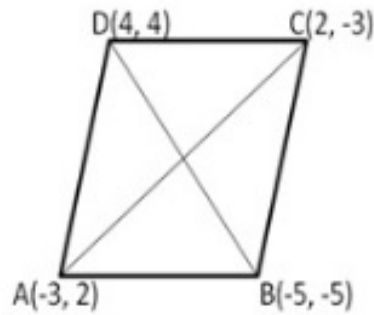
$$\therefore \text{Diag. AC} = \text{Diag. BD}$$

Thus, all sides of quad. ABCD are equal and diagonals are also equal.

Quad. ABCD is a square.

Question 22:

Let A(-3,2), B(-5, -5), C(2, -3) and D(4,4) be the angular point of quad ABCD. Join AC and BD.



$$\begin{aligned}\text{Now, } AB &= \sqrt{(-5+3)^2 + (-5-2)^2} \\ &= \sqrt{(-2)^2 + (-7)^2} = \sqrt{4+49} = \sqrt{53} \text{ units}\end{aligned}$$

$$\begin{aligned}BC &= \sqrt{(2+5)^2 + (-3+5)^2} \\ &= \sqrt{(7)^2 + (2)^2} = \sqrt{49+4} = \sqrt{53} \text{ units}\end{aligned}$$

$$\begin{aligned}CD &= \sqrt{(4-2)^2 + (4+3)^2} \\ &= \sqrt{(2)^2 + (7)^2} = \sqrt{4+49} = \sqrt{53} \text{ units}\end{aligned}$$

$$\begin{aligned}DA &= \sqrt{(-3-4)^2 + (2-4)^2} \\ &= \sqrt{(-7)^2 + (2)^2} = \sqrt{4+49} = \sqrt{53} \text{ units}\end{aligned}$$

$$\therefore AB = BC = CD = DA = \sqrt{53} \text{ units}$$

$$\begin{aligned}\text{Diag. AC} &= \sqrt{(2+3)^2 + (-3-2)^2} = \sqrt{(5)^2 + (-5)^2} \\ &= \sqrt{25+25} = \sqrt{50} = 5\sqrt{2} \text{ unit}\end{aligned}$$

$$\begin{aligned}\text{Diag. BD} &= \sqrt{(4+5)^2 + (4+5)^2} = \sqrt{(9)^2 + (9)^2} \\ &= \sqrt{81+81} = \sqrt{162} = 9\sqrt{2} \text{ unit}\end{aligned}$$

$$\therefore \text{Diag. AC} \neq \text{Diag. BD}$$

Thus, ABCD is a quadrilateral having all sides equal but diagonals are unequal.

Hence, ABCD is a rhombus.

$$\text{Area of rhombus ABCD} = \frac{1}{2} \times \text{Product of diagonals}$$

$$\begin{aligned}&= \left(\frac{1}{2} \times AC \times BD \right) = \left(\frac{1}{2} \times 5\sqrt{2} \times 9\sqrt{2} \right) \\ &= 45 \text{ sq unit}\end{aligned}$$

***** END *****