

NCERT solutions for class 8 maths chapter 14 factorisation Ex-14.2

### 1. Factorize the following expressions:

(i) 
$$a^2 + 8a + 16$$

(ii) 
$$p^2-10p+25$$

(iii) 
$$25m^2 + 30m + 9$$

(iv) 
$$49y^2 + 84yz + 36z^2$$

(v) 
$$4x^2 - 8x + 4$$

(vi) 
$$121b^2 - 88bc + 16c^2$$

(vii) 
$$(l+m)^2 - 4lm$$

# [Hint: Expand $(l+m)^2$ first]

(viii) 
$$a^4 + 2a^2b^2 + b^4$$

**Ans.** (i) 
$$a^2 + 8a + 16 = a^2 + (4+4)a + 4 \times 4$$

# Using identity

$$x^{2} + (a+b)x + ab = (x+a)(x+b)$$

Here 
$$x = a$$
,  $a = 4$  and  $b = 4$ 

$$a^2 + 8a + 16 = (a+4)(a+4) = (a+4)^2$$

(ii) 
$$p^2 - 10p + 25 = p^2 + (-5 - 5)p + (-5)(-5)$$

# Using identity

$$x^{2} + (a+b)x + ab = (x+a)(x+b)$$

Here 
$$x = p, a = -5$$
 and  $b = -5$ 

$$p^2-10p+25=(p-5)(p-5)=(p-5)^2$$

(iii) 
$$25m^2 + 30m + 9 = (5m)^2 + 2 \times 5m \times 3 + (3)^2$$

Using identity  $a^2 + 2ab + b^2 = (a+b)^2$ , here a = 5m, b = 3

$$25m^2 + 30m + 9 = (5m + 3)^2$$

(iv) 
$$49y^2 + 84yz + 36z^2$$
  
=  $(7y)^2 + 2 \times 7y \times 6z + (6z)^2$ 

Using identity  $a^2 + 2ab + b^2 = (a+b)^2$ , here a = 7y, b = 6z

$$49y^2 + 84yz + 36z^2 = (7y + 6z)^2$$

(v) 
$$4x^2 - 8x + 4 = (2x)^2 - 2 \times 2x \times 2 + (2)^2$$

Using identity  $a^2 - 2ab + b^2 = (a - b)^2$ , here a = 2x, b = 2

$$4x^{2}-8x+4=(2x-2)^{2}$$
$$=(2)^{2}(x-1)^{2}=4(x-1)^{2}$$

(vi) 
$$121b^2 - 88bc + 16c^2$$
  
=  $(11b)^2 - 2 \times 11b \times 4c + (4c)^2$ 

Using identity  $a^2 - 2ab + b^2 = (a - b)^2$ , here a = 11b, b = 4c

$$121b^2 - 88bc + 16c^2 = (11b - 4c)^2$$

(vii) 
$$(l+m)^2 - 4lm$$

$$= l^2 + 2 \times l \times m + m^2 - 4lm$$

$$\left[ \because \left( a+b \right)^2 = a^2 + 2ab + b^2 \right]$$

$$= l^2 + 2lm + m^2 - 4lm$$

$$= l^2 - 2lm + m^2$$

$$=(l-m)^{2}$$
  $[: (a-b)^{2} = a^{2}-2ab+b^{2}]$ 

#### (viii)

$$a^4 + 2a^2b^2 + b^4 = (a^2)^2 + 2 \times a^2 \times b^2 + (b^2)^2$$

$$= (a^{2} + b^{2})^{2} \left[ \because (a+b)^{2} = a^{2} + 2ab + b^{2} \right]$$

Q2. Factorize:

(i) 
$$4p^2 - 9q^2$$

(ii) 
$$63a^2 - 112b^2$$

(iii) 
$$49x^2 - 36$$

(iv) 
$$16x^5 - 144x^2$$

(v) 
$$(l+m)^2 - (l-m)^2$$

(vi) 
$$9x^2y^2-16$$

(vii) 
$$(x^2 - 2xy + y^2) - z^2$$

(viii) 
$$25a^2 - 4b^2 + 28bc - 49c^2$$

**Ans.** (i) 
$$4p^2 - 9q^2 = (2p)^2 - (3q)^2$$

$$=(2p-3q)(2p+3q)$$

$$\left[ \because a^2 - b^2 = (a - b)(a + b) \right]$$

(ii) 
$$63a^2 - 112b^2 = 7(9a^2 - 16b^2)$$

$$=7\Big[\big(3a\big)^2-\big(4b\big)^2\Big]$$

$$= 7(3a-4b)(3a+4b)$$

$$\left[ \because a^2 - b^2 = (a - b)(a + b) \right]$$

(iii) 
$$49x^2 - 36 = (7x)^2 - (6)^2$$

(iii) 
$$49x^2 - 36 = (7x)^2 - (6)^2$$
  
=  $(7x-6)(7x+6) \left[\because a^2 - b^2 = (a-b)(a+b)\right]$   
(iv)  $16x^5 - 144x^3 = 16x^3(x^2 - 9)$   
=  $16x^3 \left[(x)^2 - (3)^2\right]$   
=  $16x^3 (x-3)(x+3)$   
 $\left[\because a^2 - b^2 = (a-b)(a+b)\right]$   
(v)  $(l+m)^2 - (l-m)^2$   
=  $\left[(l+m) + (l-m)\right] \left[(l+m) - (l-m)\right]$   
 $\left[\because a^2 - b^2 = (a-b)(a+b)\right]$   
=  $(l+m+l-m)(l+m-l+m)$   
=  $(2m)(2l) = 4lm$   
(vi)  $9x^2y^2 - 16 = (3xy)^2 - (4)^2$   
=  $(3xy-4)(3xy+4)$   
 $\left[\because a^2 - b^2 = (a-b)(a+b)\right]$   
(vii)  $(x^2 - 2xy + y^2) - z^2 = (x-y)^2 - z^2$   
 $\left[\because (a-b)^2 = a^2 - 2ab + b^2\right]$ 

= (x-y-z)(x-y+z)

$$[\because a^2 - b^2 = (a - b)(a + b)]$$

$$(viii) 25a^2 - 4b^2 + 28bc - 49c^2$$

$$= 25a^2 - (4b^2 - 28bc + 49c^2)$$

$$= 25a^2 - [(2b)^2 - 2 \times 2b \times 7c + (7c)^2]$$

$$= 25a^2 - (2b - 7c)^2$$

$$[\because (a - b)^2 = a^2 - 2ab + b^2]$$

$$= (5a)^2 - (2b - 7c)^2$$

$$= [5a - (2b - 7c)][5a + (2b - 7c)]$$

$$[\because a^2 - b^2 = (a - b)(a + b)]$$

$$= (5a - 2b + 7c)(5a + 2b - 7c)$$

# Q3. Factorize the expressions:

(i) 
$$ax^2 + bx$$

(ii) 
$$7p^2 + 21q^2$$

(iii) 
$$2x^3 + 2xy^2 + 2xz^2$$

(iv) 
$$am^2 + bm^2 + bn^2 + an^2$$

(v) 
$$(lm+l)+m+1$$

(vi) 
$$y(y+z)+9(y+z)$$

(vii) 
$$5y^2 - 20y - 8z + 2yz$$

(viii) 
$$10ab + 4a + 5b + 2$$

(ix) 
$$6xy - 4y + 6 - 9x$$

**Ans.** (i) 
$$ax^{2} + bx = x(ax + b)$$

(ii) 
$$7p^2 + 21q^2 = 7(p^2 + 3q^2)$$

(iii) 
$$2x^3 + 2xy^2 + 2xz^2 = 2x(x^2 + y^2 + z^2)$$

(iv) 
$$am^2 + bm^2 + bn^2 + an^2$$

$$_{m^{2}}(a+b)+n^{2}(a+b)$$

$$= (a+b)(m^2+n^2)$$

(v) 
$$(lm+l)+m+1=l(m+1)+l(m+1)$$

$$=(m+1)(l+1)$$

(vi) 
$$y(y+z)+9(y+z)=(y+z)(y+9)$$

(vii) 
$$5y^2 - 20y - 8z + 2yz$$

$$=5y^2-20y+2yz-8z$$

$$= 5y(y-4)+2z(y-4)$$

$$=(y-4)(5y+2z)$$

(viii) 
$$10ab + 4a + 5b + 2$$

$$= 2a(5b+2)+1(5b+2)$$

$$=(5b+2)(2a+1)$$

(ix) 
$$6xy - 4y + 6 - 9x$$

$$= 6xy - 9x - 4y + 6$$

$$= 3x(2y-3)-2(2y-3)$$

$$=(2y-3)(3x-2)$$

### Q4. Factorize:

(i) 
$$a^4 - b^4$$
 (ii)  $p^4 - 81$ 

(iii) 
$$x^4 - (y+z)^4$$
 (iv)  $x^4 - (x-z)^4$ 

(v) 
$$a^4 - 2a^2b^2 + b^4$$

**Ans.** (i) 
$$a^4 - b^4 = (a^2)^2 - (b^2)^2$$

$$=(a^2-b^2)(a^2+b^2)$$

$$\left[ \because a^2 - b^2 - (a - b)(a + b) \right]$$

$$=(a-b)(a+b)(a^2+b^2)$$

$$\left[ \because a^2 - b^2 - (a - b)(a + b) \right]$$

(ii) 
$$p^4 - 81 = (p^2)^2 - (9)^2$$

$$= (p^2 - 9)(p^2 + 9) \left[ \because a^2 - b^2 - (a - b)(a + b) \right]$$

$$=(p^2-3^2)(p^2+9)$$

$$= (p-3)(p+3)(p^{2}+9)$$

$$[\because a^{2}-b^{2}-(a-b)(a+b)]$$

$$(iii) x^{4}-(y+z)^{4} = (x^{2})^{2}-[(y+z)^{2}]^{2}$$

$$= [x^{2}-(y+z)^{2}][x^{2}+(y+z)^{2}]$$

$$[\because a^{2}-b^{2}-(a-b)(a+b)]$$

$$= [x-(y+z)][x+(y+z)][x^{2}+(y+z)^{2}]$$

$$[\because a^{2}-b^{2}-(a-b)(a+b)]$$

$$= (x-y+z)(x+y+z)[x^{2}+(y+z)^{2}]$$

$$(iv) x^{4}-(x-z)^{4} = (x^{2})^{2}-[(x-z)^{2}]^{2}$$

$$= [x^{2}-(x-z)^{2}][x^{2}+(x-z)^{2}]$$

$$[\because a^{2}-b^{2}-(a-b)(a+b)]$$

$$= [x-(x-z)][x+(x+z)][x^{2}+(x-z)^{2}]$$

$$[\because a^{2}-b^{2}-(a-b)(a+b)]$$

$$= (x-x+z)(x+x+z)(x^{2}+x^{2}-2xz+z^{2})$$

$$[\because (a-b)^{2}=a^{2}-2ab+b^{2}]$$

$$= x(2x+z)(2x^{2}-2xz+z^{2})$$

$$(v) a^{4}-2a^{2}b^{2}+b^{4}=(a^{2})^{2}-2a^{2}b^{2}+(b^{2})^{2}$$

$$= (a^{2}-b^{2})^{2}[\because (a-b)^{2}=a^{2}-2ab+b^{2}]$$

$$= [(a-b)(a+b)]^{2}[\because a^{2}-b^{2}-(a-b)(a+b)]$$

$$= (a-b)^{2}(a+b)^{2}[\because (xy)^{m}=x^{m}.y^{m}]$$

Q5. Factorize the following expressions:

(i) 
$$p^2 + 6p + 8$$
 (ii)  $q^2 - 10q + 21$ 

(iii) 
$$p^2 + 6p - 16$$

**Ans.** (i) 
$$p^2 + 6p + 8 = p^2 + (4+2)p + 4 \times 2$$

$$= p^2 + 4p + 2p + 4 \times 2$$

$$= p(p+4)+2(p+4)$$

$$=(p+4)(p+2)$$

(ii) 
$$q^2 - 10q + 21 = q^2 - (7+3)q + 7 \times 3$$

$$= q^2 - 7q - 3q + 7 \times 3$$

$$= q(q-7)-3(q-7)$$

$$=(q-7)(q-3)$$

(iii) 
$$p^2 + 6p - 16 = p^2 + (8-2)p - 8 \times 2$$

$$= p^2 + 8p - 2p - 8 \times 2$$

$$= p(p+8)-2(p+8)$$

$$= (p+8)(p-2)$$

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