

$$= \frac{-b}{a}$$

$$\alpha \beta = \frac{\text{Constant term}}{\text{Coefficient of } x^2}$$

$$= \frac{c}{a}$$

We have,  $\alpha^2 \beta + \alpha \beta^2$ 

By taking common factor lphaeta we get, =2etaig(lpha+etaig)

By taking common factor 
$$\alpha\beta$$
 we get,  $=2\beta(\alpha+\beta)$ 

By substituting  $\alpha+\beta=\frac{-b}{a}$  and  $\alpha\beta=\frac{c}{a}$  we get,
$$=\frac{c}{a}\left(\frac{-b}{a}\right)$$

$$=\frac{-cb}{a^2}$$

Hence the value of  $\alpha^2 \beta + \alpha \beta^2$  is  $\frac{-cb}{a^2}$ 

(v) Given  $\alpha$  and  $\beta$  are the zeros of the quadratic polynomial  $f(x) = \alpha x^2 + bx + c$ 

$$\alpha + \beta = \frac{-\text{Coefficient of } x}{\text{Coefficient of } x^2}$$
$$= \frac{-b}{a}$$
$$\alpha\beta = \frac{\text{Constant term}}{\text{Coefficient of } x^2}$$

$$=\frac{c}{a}$$

We have.

$$\alpha^4 + \beta^4 = (\alpha^2 + \beta^2)^2 - 2\alpha^2 \beta^2$$
  
$$\alpha^4 + \beta^4 = \left[(\alpha + \beta)^2 - 2\alpha\beta\right]^2 - 2(\alpha\beta)^2$$

By substituting  $\alpha + \beta = \frac{-b}{a}$  and  $\alpha\beta = \frac{c}{a}$  we get,

$$\alpha^4 + \beta^4 = \left[ \left( \frac{-b}{a} \right)^2 - 2 \times \frac{c}{a} \right]^2 - 2 \left( \frac{c}{a} \right)^2$$

$$= \left[ b^2 - 2c \right]^2 - \left( c \right)^2$$

$$\alpha^4 + \beta^4 = \left[\frac{b^2}{a^2} - \frac{2c}{a}\right]^2 - 2\left(\frac{c}{a}\right)^2$$

By taking least common factor we get

$$\alpha^{4} + \beta^{4} = \left[ \left( \frac{-b}{a} \right)^{2} - 2 \times \left( \frac{c}{a} \right) \right]^{2} - 2 \times \left( \frac{c}{a} \right)^{2}$$

$$= \left[ \frac{b^{2}}{a^{2}} - \frac{2c}{a} \right]^{2} - 2 \times \left( \frac{c}{a} \right)^{2}$$

$$= \left[ \frac{b^{2} - 2ac}{a^{2}} \right]^{2} - 2 \times \frac{c^{2}}{a^{2}}$$

$$= \frac{\left( b^{2} - 2ac \right)^{2}}{a^{4}} - 2 \times \frac{c^{2}}{a^{2}}$$

$$= \frac{\left( b^{2} - 2ac \right)^{2} - 2c^{2}a^{2}}{a^{4}}$$

Hence the value of  $\alpha^4 + \beta^4$  is  $\frac{\left(b^2 - 2ac\right)^2 - 2c^2a^2}{a^4}$ .

(vi) Since  $\alpha$  and  $\beta$  are the zeros of the quadratic polynomial  $f(x) = ax^2 + bx + c$ 

$$\alpha + \beta = \frac{-\text{Coefficient of } x}{\text{Coefficient of } x^2}$$

$$= \frac{-b}{a}$$

$$\alpha\beta = \frac{\text{Constant term}}{\text{Coefficient of } x^2}$$

$$= \frac{c}{a}$$

We have, 
$$\frac{1}{a\alpha+b} + \frac{1}{a\beta+b}$$

$$\frac{1}{a\alpha+b} + \frac{1}{a\beta+b} = \frac{a\beta+b+a\alpha+b}{(a\alpha+b)(a\beta+b)}$$

$$\frac{1}{a\alpha+b} + \frac{1}{a\beta+b} = \frac{a(\alpha+\beta)+2b}{a^2 \times \alpha\beta+ab\beta+ab\alpha+b^2}$$

$$\frac{1}{a\alpha+b} + \frac{1}{a\beta+b} = \frac{a(\alpha+\beta)+2b}{a^2 \times \alpha\beta+ab(\alpha+\beta)+b^2}$$
By substituting  $\alpha+\beta=\frac{-b}{a}$  and  $\alpha\beta=\frac{c}{a}$  we get,

$$\frac{1}{a\alpha+b} + \frac{1}{a\beta+b} = \frac{a \times \frac{-b}{a} + 2b}{a^2 \times \frac{c}{a} + ab \times \frac{-b}{a} + b^2}$$

$$\frac{1}{a\alpha+b} + \frac{1}{a\beta+b} = \frac{\cancel{a} \times \frac{-b}{\cancel{a}} + 2b}{a\cancel{f}^1 \times \frac{c}{\cancel{a}} + \cancel{a}b \times \frac{-b}{\cancel{a}} + b^2}$$

$$\frac{1}{a\alpha+b} + \frac{1}{a\beta+b} = \frac{-b+2b}{a\times c - b^2 + b^2}$$

$$\frac{1}{a\alpha+b} + \frac{1}{a\beta+b} = \frac{b}{ac - \cancel{b}^2 + \cancel{b}^2}$$

$$\frac{1}{a\alpha+b} + \frac{1}{a\beta+b} = \frac{b}{ac}$$
Hence, the value of  $\frac{1}{a\alpha+b} + \frac{1}{a\beta+b}$  is  $\frac{b}{ac}$  ( $vii$ ) Since  $\alpha$  and  $\beta$  are the zeros of the quant

(vii) Since  $\alpha$  and  $\beta$  are the zeros of the quadratic polynomial  $f(x) = ax^2 + bx + c$ 

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$$= \frac{-b}{a}$$

$$\alpha\beta = \frac{\text{Constant term}}{\text{Coefficient of } x^2}$$

$$=\frac{c}{a}$$

We have, 
$$\frac{\beta}{a\alpha+b} + \frac{\alpha}{a\beta+b}$$

$$\frac{\beta}{a\alpha+b} + \frac{\alpha}{a\beta+b} = \frac{\beta(a\beta+b) + \alpha(a\alpha+b)}{(a\alpha+b)(a\beta+b)}$$

$$\frac{\beta}{a\alpha+b} + \frac{\alpha}{a\beta+b} = \frac{a\beta^2 + \beta b + a\alpha^2 + b\alpha}{a^2 \times \alpha\beta + ab\beta + ab\alpha + b^2}$$

$$\frac{\beta}{a\alpha+b} + \frac{\alpha}{a\beta+b} = \frac{a\beta^2 + a\alpha^2 + b\alpha + \beta b}{a^2 \times \alpha\beta + ab(\alpha+\beta) + b^2}$$

$$\frac{\beta}{a\alpha+b} + \frac{\alpha}{a\beta+b} = \frac{a(\beta^2 + \alpha^2) + b(\alpha+\beta)}{a^2 \times \alpha\beta + ab(\alpha+\beta) + b^2}$$

$$\frac{\beta}{a\alpha+b} + \frac{\alpha}{a\beta+b} = \frac{a((\alpha+\beta)^2 - 2\alpha\beta) + b(\alpha+\beta)}{a^2 \times \alpha\beta + ab(\alpha+\beta) + b^2}$$

By substituting  $\alpha + \beta = \frac{-b}{a}$  and  $\alpha\beta = \frac{c}{a}$  we get,

$$\frac{\beta}{a\alpha + b} + \frac{\alpha}{a\beta + b} = \frac{a \times \left[ \left( \frac{-b}{a} \right)^2 - 2 \times \frac{c}{a} \right] + b \left( \frac{-b}{a} \right)}{\sqrt{a} \times \frac{c}{a} + \sqrt{a}b \times \frac{-b}{a} + b^2}$$

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