

## Mathematical Induction Ex 12.2 Q24

Let P(n): n(n+1)(n+5) is a multiple of 3 for all  $n \in N$ 

For 
$$n = 1$$
  
1. $(1+1)(1+5)$   
=  $(2)(6)$ 

= 12

it is a multiple of 3

Let P(n) is true for n = kk(k+1)(k+5) is a multiple of 3

We have to show that,

$$(k+1)[(k+1)+1][(k+1)+5]$$
 is a multiple of 3  $(k+1)[(k+1)+1][(k+1)+5] = 3\mu$ 

Now,

$$(k+1)(k+2)[(k+1)+5]$$

$$= [k(k+1)+2(k+1)][(k+5)+1]$$

$$= k(k+1)(k+5)+k(k+1)+2(k+1)(k+5)+2(k+1)$$

$$= 3\lambda + k^2 + k + 2(k^2 + 6k + 5) + 2k + 2$$

$$= 3\lambda + k^2 + k + 2k^2 + 12k + 10 + 2k + 2$$

$$= 3\lambda + 3k^2 + 15k + 12$$

$$= 3(\lambda + k^2 + 5k + 4)$$
[Using equation (1)]

 $= 3\mu$ 

$$\Rightarrow$$
  $P(n)$  is true for  $n = k + 1$ 

 $\Rightarrow$  P(n) is true for all  $n \in N$  by PMI

Mathematical Induction Ex 12.2 Q25

Let 
$$P(n): 7^{2n} + 2^{3n-3} \cdot 3^{n-1}$$
 is divisible by 25

For  $n = 1$ 
 $7^2 + 2^0 \cdot 3^0$ 
 $= 49 + 1$ 
 $= 50$ 

it is divisible of 25
 $\Rightarrow P(n)$  is true for  $n = 1$ 
Let  $P(n)$  is true for  $n = k$ ,

 $7^{2k} + 2^{3k-3} \cdot 3^{k-1}$  is divisible by 25
 $\Rightarrow 7^{2k} + 2^{3k-3} \cdot 3^{k-1} = 25\lambda$  ---- (1)

We have to show that,

 $7^{2(k+1)} + 2^{3k} \cdot 3^k$  is divisible by 25
 $7^{2(k+1)} + 2^{3k} \cdot 3^k$  is divisible by 25
 $7^{2(k+1)} + 2^{3k} \cdot 3^k = 25\mu$ 

Now,

 $7^{2(k+1)} + 2^{3k} \cdot 3^k = 25\mu$ 

Now,

 $7^{2(k+1)} + 2^{3k} \cdot 3^k = 25\mu$ 

[Using equation (1)]
 $= 25\lambda \cdot 49 - 2^{3k} \cdot 3^k \cdot 49 + 2^{3k} \cdot 3^k = 24 \cdot 25 \cdot 49\lambda - 2^{3k} \cdot 3^k \cdot 49 + 24 \cdot 2^{3k} \cdot 3^k = 24 \cdot 25 \cdot 49\lambda - 2^{3k} \cdot 3^k \cdot 49 + 24 \cdot 2^{3k} \cdot 3^k = 25 \cdot 2^{4k} \cdot 49\lambda - 2^{3k} \cdot 3^k \cdot 3^k = 25 \cdot 2^{4k} \cdot 49\lambda - 2^{4k} \cdot 4$ 

= 25*µ* 

 $\Rightarrow$  P(n) is true for n = k + 1

 $\Rightarrow$  P (n) is true for all  $n \in N$  by PMI Mathematical Induction Ex 12.2 Q26

Let  $P(n): 2.7^n + 3.5^n - 5$  is divisible by 24 For n = 12.7 + 3.5 - 5= 24 it is divisible of 24  $\Rightarrow$  P(n) is true for n = 1Let P(n) is true for n = k, so  $2.7^k + 3.5^k - 5$  is divisible by 24  $2.7^k + 3.5^k - 5 = 24\lambda$ ---(1) We have to show that,

$$2.7^{(k+1)} + 3.5^{(k+1)} - 5$$

$$= 2.7^{k}.7 + 3.5^{k}.5 - 5$$

$$= (24\lambda - 3.5^{k} + 5)7 + 15.5^{k} - 5$$

$$= 24.7\lambda - 21.5^{k} + 35 + 15.5^{k} - 5$$

$$= 24.7\lambda - 6.5^{k} + 30$$

$$= 24.7\lambda - 6 (5^{k} - 5)$$

$$= 24.7\lambda - 6.(20\nu)$$

$$= 24(7\lambda - 5\nu)$$

$$= 24\mu$$
[Since  $5^{k} - 5$  is multiple of  $20$ ]

$$\Rightarrow$$
  $P(n)$  is true for  $n = k + 1$ 

 $\Rightarrow$  P(n) is true for all  $n \in N$  by PMI

\*\*\*\*\*\*\*\*\* END \*\*\*\*\*\*\*