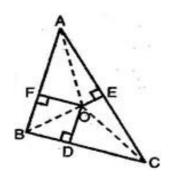


Exercise 6.5



Adding all these, we get

$$OA^{2} + OB^{2} + OC^{2}$$
 =
 $AF^{2} + BD^{2} + CE^{2} + OF^{2} + OD^{2} + OE^{2}$
 $\Rightarrow OA^{2} + OB^{2} + OC^{2} - OD^{2} - OE^{2} - OF^{2}$ =
 $AF^{2} + BD^{2} + CE^{2}$

(ii) In right \triangle s ODB and ODC, we have

$$OB^2 = BD^2 + OD^2$$
 and $OC^2 = OD^2 + CD^2$

$$\Rightarrow OB^2 - OC^2 = BD^2 - CD^2 \dots (1)$$

Similarly, we have $OB^2 - OC^2 = BD^2 - CD^2$ (2)

and
$$OB^2 - OC^2 = BD^2 - CD^2$$
(3)

Adding equations (1), (2) and (3), we get

$$=(OB^2 - OC^2) + (OC^2 - OA^2) + (OA^2 - OB^2)$$

$$= (BD^2 - CD^2) + (CE^2 - AE^2) + (AF^2 - BF^2)$$

$$\Rightarrow (BD^2 + CE^2 + AF^2) - (AE^2 + CD^2 + BF^2) =$$

O

$$\Rightarrow$$
 $AF^2 + BD^2 + CE^2 = AE^2 + BF^2 + CD^2$

9. A ladder 10 m long reaches a window 8 m above the ground. Find the distance of the foot of the ladder from base of the wall.

Ans. Let AB be the ladder, B be the window and CB be the wall. Then, ABC is a

right triangle, right angled at C.

$$A = AB^{2} = AC^{2} + BC^{2}$$

$$\Rightarrow AB^{2} = AC^{2} + BC^{2}$$

$$\Rightarrow 10^{2} = AC^{2} + 8^{2}$$

$$\Rightarrow AC^{2} = 100 - 64$$

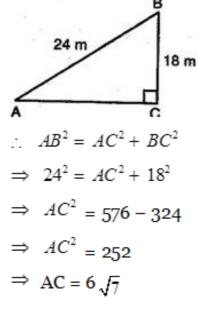
$$\Rightarrow AC^{2} = 36$$

$$\Rightarrow AC = 6$$

Hence, the foot of the ladder is at a distance 6 m from the base of the wall.

10. A guy wire attached to a vertical pole of height 18 m is 24 m long and has a stake attached to the other hand. How far from the base of the pole should the stake be driven so that the wire will be taut?

Ans. Let AB (= 24m) be a guy wire attached to a vertical pole. BC of height 18 m. To keep the wire taut, let it be fixed to a stake at A. Then, ABC is a right triangle, right angled at C.

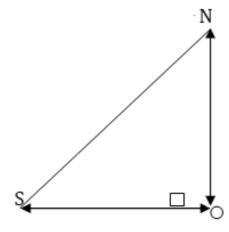


Hence, the stake may be placed at distance of 6 $\sqrt{7}$ m from the base of the pole.

11. An aeroplane leaves an airport and flies due north at a speed of 1000 km pwe hour. At the same time, another aeroplane leaves the same airport and flies due west at a speed of 1200 km per hour. How far apart will be the two planes after $1\frac{1}{2}$ hours?

Ans. Let the first aeroplane starts from O and goes up to A towards north where

$$\mathbf{OA} = \left(1000 \times \frac{3}{2}\right) \mathbf{km} = \mathbf{1500} \mathbf{km}$$



Let the second aeroplane starts from O at the same time and goes up to 1500 km

B towards west where

$$OB = \left(1200 \times \frac{3}{2}\right) \text{ km} = 1800 \text{ km}$$

According to the question the required distance = BA

In right angled triangle ABC, by Pythagoras theorem, we have,

$$AB^{2} = OA^{2} + OB^{2}$$

$$= (1500)^{2} + (1800)^{2}$$

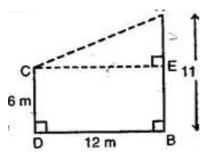
$$= 2250000 + 3240000$$

$$= 5490000 = 9 \times 61 \times 100 \times 100$$

$$\Rightarrow AB = 300\sqrt{61} \text{ km}$$

12. Two poles of heights 6 m and 11 m stand on a plane ground. If the distance between the feet of the poles is 12 m, find the distance between their tops.

Ans. Let AB = 11 m and CD = 6 m be the two poles such that BD = 12 m A



Draw CE^{\perp} AB and join AC.

$$\therefore$$
 CE = DB = 12 m

$$AE = AB - BE = AB - CD = (11 - 6)m = 5 m$$

In right angled triangle ACE, by Pythagoras theorem, we have

$$AC^2 = CE^2 + AE^2 = 12^2 + 5^2$$

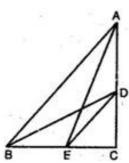
$$= 144 + 25 = 169$$

$$\Rightarrow$$
 AC = 13 m

Hence, the distance between the tops of the two poles is 13 m.

13. D and E are points on the sides CA and CB respectively of a triangle ABC right angled at C. Prove that $AE^2 + BD^2 = AB^2 + DE^2$.

Ans. In right angled Δ s ACE and DCB, we have



$$AE^2 = AC^2 + CE^2$$
 and $BD^2 = DC^2 + BC^2$

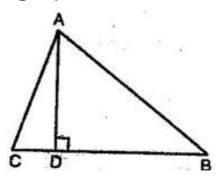
$$\Rightarrow AE^2 + BD^2 = (AC^2 + CE^2) + (DC^2 + BC^2)$$

$$\Rightarrow AE^2 + BD^2 = (AC^2 + BC^2) + (DC^2 + CE^2)$$

$$\Rightarrow AE^2 + BD^2 = AB^2 + DE^2$$

[By Pythagoras theorem, $AC^2 + BC^2 = AB^2$ and $DC^2 + CE^2 = DE^2$

14. The perpendicular from A on side BC of a \triangle ABC intersects BC at D such that DB = 3CD (see figure). Prove that $2AB^2 = 2AC^2 + BC^2$.



Ans. We have, DB = 3CD

Now,
$$BC = DB + CD$$

$$\Rightarrow$$
 BC = 3CD + CD

$$\Rightarrow$$
 BC = 4CD

$$\therefore CD = \frac{1}{4} BC \text{ and } DB = 3CD = \frac{3}{4} BC \dots (1)$$

Since, Δ ABD is a right triangle, right angled at D. Therefore by Pythagoras theorem, we have,

$$AB^2 = AD^2 + DB^2 \dots (2)$$

Similarly, from \triangle ACD, we have, $AC^2 = AD^2 + CD^2$ (3)

From eq. (2) and (3) $AB^2 - AC^2 = DB^2 - CD^2$

$$\Rightarrow AB^2 - AC^2 = \left(\frac{3}{4}BC\right)^2 - \left(\frac{1}{4}BC\right)^2 \text{ [Using eq. (1)]}$$

$$\Rightarrow AB^2 - AC^2 = \left(\frac{9}{16} - \frac{1}{16}\right)BC^2$$

$$\Rightarrow AB^2 - AC^2 = \frac{1}{2}BC^2$$

$$\Rightarrow 2AB^2 - 2AC^2 = BC^2$$

$$\Rightarrow 2AB^2 = 2AC^2 + BC^2$$

******** FND *******