



Real Numbers Ex 1.4 Q3

Answer :

TO FIND: Greatest number of 6 digits exactly divisible by 24, 15 and 36

The greatest 6 digit number be 999999

24, 15 and 36

$$24 = 2^3 \times 3$$

$$15 = 3 \times 5$$

$$36 = 2^2 \times 3^2$$

$$\text{L.C.M of 24, 15 and 36} = \boxed{360}$$

$$\text{Since } \frac{999999}{360} = 2777 \times 360 + 279$$

Therefore, the remainder is 279.

Hence the desired number is equal to

$$= 999999 - 279$$

$$= \boxed{999720}$$

Hence $\boxed{999720}$ is the greatest number of 6 digits exactly divisible by 24, 15 and 36.

Real Numbers Ex 1.4 Q4

Answer :

GIVEN: A rectangular yard is 18 m 72 cm long and 13 m 20 cm broad .It is to be paved with square tiles of the same size.

TO FIND: Least possible number of such tiles.

$$\text{Length of the yard} = 18 \text{ m } 72 \text{ cm} = 1800 \text{ cm} + 72 \text{ cm} = 1872 \text{ cm} \quad (\because 1 \text{ m} = 100 \text{ cm})$$

$$\text{Breadth of the yard} = 13 \text{ m } 20 \text{ cm} = 1300 \text{ cm} + 20 \text{ cm} = 1320 \text{ cm}$$

The size of the square tile of same size needed to the pave the rectangular yard is equal the HCF of the length and breadth of the rectangular yard.

$$\text{Prime factorisation of } 1872 = 2^4 \times 3^2 \times 13$$

$$\text{Prime factorisation of } 1320 = 2^3 \times 3 \times 5 \times 11$$

$$\text{HCF of } 1872 \text{ and } 1320 = 2^3 \times 3 = 24$$

$$\therefore \text{Length of side of the square tile} = 24 \text{ cm}$$

$$\text{Number of tiles required} = \frac{\text{Area of the courtyard}}{\text{Area of each tile}} = \frac{\text{Length} \times \text{Breadth}}{(\text{Side})^2} = \frac{1872 \text{ cm} \times 1320 \text{ cm}}{(24 \text{ cm})^2} = 4290$$

Thus, the least possible number of tiles required is 4290.

Real Numbers Ex 1.4 Q5

Answer :

TO FIND: Least number that is divisible by all the numbers between 1 and 10 (both inclusive)

Let us first find the L.C.M of all the numbers between 1 and 10 (both inclusive)

$$1 = 1$$

$$2 = 2$$

$$3 = 3$$

$$4 = 2^2$$

$$5 = 5$$

$$6 = 2 \times 3$$

$$7 = 7$$

$$8 = 2^3$$

$$9 = 3^2$$

$$10 = 2 \times 5$$

$$\text{L.C.M} = \boxed{2520}$$

Hence $\boxed{2520}$ is the least number that is divisible by all the numbers between 1 and 10 (both inclusive)

Real Numbers Ex 1.4 Q6

Answer :

TO FIND: Smallest number that, when divided by 35, 56 and 91 leaves remainder of 7 in each case
L.C.M OF 35, 56 and 91

$$35 = 5 \times 7$$

$$56 = 2^3 \times 7$$

$$91 = 13 \times 7$$

$$\text{L.C.M of } 35, 56 \text{ and } 91 = 2^3 \times 5 \times 7 \times 13$$

$$= 3640$$

Hence 84 is the least number which exactly divides 28, 42 and 84 i.e. we will get a remainder of 0 in this case. But we need the smallest number that, when divided by 35, 56 and 91 leaves remainder of 7 in each case

Therefore

$$= 3640 + 7$$

$$= 3647$$

Hence $= 3647$ is smallest number that, when divided by 35, 56 and 91 leaves remainder of 7 in each case.

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