

Exercise 11D

Question 11:

The given AP is 25, 20, 15, ...

 \therefore first term a = 25, common difference = 20 - 25 = -5

Let for lowest value of n, nth term is negative

$$a + (n - 1) d < 0$$

or
$$25 + (n-1)(-5) < 0$$

$$\Rightarrow$$
 5 (n-1) > 25

$$\Rightarrow 5n > 25 + 5 = 30$$

So, the first negative term is the 7th term

Question 12:

The given AP is 5, 7, 9, ... 201

last term I = 201, common difference d = 7 - 5 = 2

 6^{th} term from the end = I - (n - 1)d

Question 13:

Sum of n natural numbers = 1 + 2 + 3 + ... + n

Here a = 1, d = 2 - 1 = 1

$$S_n = \frac{n}{2} \left[2a + (n-1)d \right]$$

:. Sum of natural numbers =
$$\frac{n}{2}[2 \times 1 + (n-1)d]$$

= $\frac{n}{2}[2 + (n-1)] = \frac{n(n+1)}{2}$

Question 14:

Sum of even natural numbers = 2 + 4 + 6 + ... to n terms a = 2, d = 4 - 2 = 2

$$S_n = \frac{n}{2} \left[2a + (n-1)d \right]$$

.: Sum of even numbers

$$= \frac{n}{2} \left[2 \times 2 + (n-1) \times 2 \right]$$

$$=\frac{n}{2}[4+2n-2]$$

$$=\frac{n}{2}(2n+2)$$

$$=\frac{2n\left(n+1\right) }{2}$$

$$= n(n+1)$$

Question 15:

Sum of n odd natural numbers = 1 + 3 + 5 + ... to n terms a = 1, d = 3 - 1 = 2

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

:: Sum of n odd numbers

$$= \frac{n}{2} [2 \times 1 + (n-1) \times 2] = [2 + 2n - 2]$$
$$= \frac{n}{2} \times 2n = n^2$$

********** END *******