



Trigonometric Ratios Ex 5.2 Q24

Answer :

We have,

$$\sqrt{3} \tan 2x = \cos 60^\circ + \sin 45^\circ \cos 45^\circ \dots\dots (1)$$

Now we know that

$$\sin 45^\circ = \cos 45^\circ = \frac{1}{\sqrt{2}} \text{ and } \cos 60^\circ = \frac{1}{2}$$

Now by substituting above values in equation (1), we get,

$$\sqrt{3} \tan 2x = \cos 60^\circ + \sin 45^\circ \cos 45^\circ$$

$$\begin{aligned}\sqrt{3} \tan 2x &= \frac{1}{2} + \frac{1}{\sqrt{2}} \times \frac{1}{\sqrt{2}} \\ &= \frac{1}{2} + \frac{1}{\sqrt{2} \times \sqrt{2}} \\ &= \frac{1}{2} + \frac{1}{2} \\ &= \frac{1+1}{2} \\ &= \frac{2}{2} \\ &= 1\end{aligned}$$

Therefore,

$$\sqrt{3} \tan 2x = 1$$
$$\Rightarrow \tan 2x = \frac{1}{\sqrt{3}} \dots\dots (2)$$

Since,

$$\tan 30^\circ = \frac{1}{\sqrt{3}} \dots\dots (3)$$

Therefore by comparing equation (2) and (3)

We get,

$$2x = 30^\circ$$

$$\Rightarrow x = \frac{30^\circ}{2}$$

$$\Rightarrow x = 15^\circ$$

Therefore,

$$x = 15^\circ$$

Trigonometric Ratios Ex 5.2 Q25

Answer :

We have,

$$\cos 2x = \cos 60^\circ \cos 30^\circ + \sin 60^\circ \sin 30^\circ \dots\dots (1)$$

Now we know that

$$\sin 60^\circ = \cos 30^\circ = \frac{\sqrt{3}}{2} \text{ and } \sin 30^\circ = \cos 60^\circ = \frac{1}{2}$$

Now by substituting above values in equation (1), we get,

$$\cos 2x = \cos 60^\circ \cos 30^\circ + \sin 60^\circ \sin 30^\circ$$

$$\begin{aligned} \cos 2x &= \frac{1}{2} \times \frac{\sqrt{3}}{2} + \frac{\sqrt{3}}{2} \times \frac{1}{2} \\ &= \frac{\sqrt{3}}{4} + \frac{\sqrt{3}}{4} \\ &= \frac{2\sqrt{3}}{4} \end{aligned}$$

Therefore,

$$\cos 2x = \frac{2\sqrt{3}}{4}$$

$$\text{Now } \frac{2\sqrt{3}}{4} \text{ gets reduced to } \frac{\sqrt{3}}{2}$$

Therefore,

$$\cos 2x = \frac{2\sqrt{3}}{4}$$

Now $\frac{2\sqrt{3}}{4}$ gets reduced to $\frac{\sqrt{3}}{2}$

Therefore,

$$\cos 2x = \frac{\sqrt{3}}{2} \dots\dots (2)$$

Since,

$$\cos 30^\circ = \frac{\sqrt{3}}{2} \dots\dots (3)$$

Therefore by comparing equation (2) and (3)

We get,

$$2x = 30^\circ$$

$$\Rightarrow x = \frac{30^\circ}{2}$$

$$\Rightarrow x = 15^\circ$$

Therefore,

$$x = 15^\circ$$

***** END *****