



Co-Ordinate Geometry Ex 14.3 Q14

Answer :

The ratio in which the x-axis divides two points (x_1, y_1) and (x_2, y_2) is $-y_1 : y_2$

The ratio in which the y-axis divides two points (x_1, y_1) and (x_2, y_2) is $-x_1 : x_2$

The co-ordinates of the point dividing two points (x_1, y_1) and (x_2, y_2) in the ratio $m : n$ is given as,

$$(x, y) = \left(\left(\frac{\lambda x_2 + x_1}{\lambda + 1} \right), \left(\frac{\lambda y_2 + y_1}{\lambda + 1} \right) \right) \text{ where } \lambda = \frac{m}{n}$$

Here the two given points are $A(-2, -3)$ and $B(5, 6)$.

The ratio in which the x-axis divides these points is

$$\begin{aligned} & -y_1 : y_2 \\ & -(-3) : 6 \\ & 3 : 6 \\ & 1 : 2 \end{aligned}$$

Let point $P(x, y)$ divide the line joining 'AB' in the ratio **1 : 2**

Substituting these values in the earlier mentioned formula we have,

$$(x, y) = \left(\left(\frac{\frac{1}{2}(5) + (-2)}{\frac{1}{2} + 1} \right), \left(\frac{\frac{1}{2}(6) + (-3)}{\frac{1}{2} + 1} \right) \right)$$

$$(x, y) = \left(\left(\frac{5 + 2(-2)}{1 + 2} \right), \left(\frac{6 + 2(-3)}{1 + 2} \right) \right)$$

$$(x, y) = \left(\left(\frac{1}{3} \right), \left(\frac{0}{3} \right) \right)$$

$$(x, y) = \left(\frac{1}{3}, 0 \right)$$

Thus the ratio in which the x-axis divides the two given points and the co-ordinates of the point is

$$\boxed{1 : 2 \text{ and } \left(\frac{1}{3}, 0 \right)}$$

The ratio in which the y-axis divides these points is

$$\begin{aligned} & -x_1 : x_2 \\ & -(-2) : 5 \\ & 2 : 5 \end{aligned}$$

Let point $P(x, y)$ divide the line joining 'AB' in the ratio **2 : 5**

Substituting these values in the earlier mentioned formula we have,

$$(x, y) = \left(\left(\frac{\frac{2}{5}(5) + (-2)}{\frac{2}{5} + 1} \right), \left(\frac{\frac{2}{5}(6) + (-3)}{\frac{2}{5} + 1} \right) \right)$$

$$(x, y) = \left(\left(\frac{10 + 5(-2)}{2 + 5} \right), \left(\frac{12 + 5(-3)}{2 + 5} \right) \right)$$

$$(x, y) = \left(\left(\frac{0}{7} \right), \left(-\frac{3}{7} \right) \right)$$

$$(x, y) = \left(0, -\frac{3}{7} \right)$$

Thus the ratio in which the x-axis divides the two given points and the co-ordinates of the point is

$$\boxed{2 : 5 \text{ and } \left(0, -\frac{3}{7} \right)}$$

Co-Ordinate Geometry Ex 14.3 Q15

Answer :

Let A (4, 5); B (7, 6); C (6, 3) and D (3, 2) be the vertices of a quadrilateral. We have to prove that the quadrilateral ABCD is a parallelogram.

We should proceed with the fact that if the diagonals of a quadrilateral bisect each other then the quadrilateral is a parallelogram.

Now to find the mid-point $P(x, y)$ of two points $A(x_1, y_1)$ and $B(x_2, y_2)$ we use section formula as,

$$P(x, y) = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

So the mid-point of the diagonal AC is,

$$\begin{aligned} Q(x, y) &= \left(\frac{4+6}{2}, \frac{5+3}{2} \right) \\ &= (5, 4) \end{aligned}$$

Similarly mid-point of diagonal BD is,

$$\begin{aligned} R(x, y) &= \left(\frac{7+3}{2}, \frac{6+2}{2} \right) \\ &= (5, 4) \end{aligned}$$

Therefore the mid-points of the diagonals are coinciding and thus diagonal bisects each other.

Hence ABCD is a parallelogram.

Now to check if ABCD is a rectangle, we should check the diagonal length.

$$\begin{aligned} AC &= \sqrt{(6-4)^2 + (3-5)^2} \\ &= \sqrt{4+4} \\ &= 2\sqrt{2} \end{aligned}$$

Similarly,

$$\begin{aligned} BD &= \sqrt{(7-3)^2 + (6-2)^2} \\ &= \sqrt{16+16} \\ &= 4\sqrt{2} \end{aligned}$$

Diagonals are of different lengths.

Hence ABCD is not a rectangle.

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