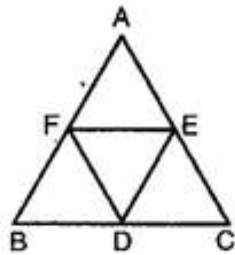




Exercise 6.4

$$\therefore DF \parallel CA \Rightarrow DE \parallel AE \dots\dots(ii)$$



From (i) and (ii), we can say that AFDE is a parallelogram.

Similarly, BDEF is a parallelogram.

Now, in Δ s DEF and ABC, we have

$$\angle FDE = \angle A[\text{opposite angles of } \parallel \text{ gm AFDE}]$$

$$\text{And } \angle DEF = \angle B[\text{opposite angles of } \parallel \text{ gm BDEF}]$$

\therefore By AA-criterion of similarity, we have $\Delta DEF \sim \Delta ABC$

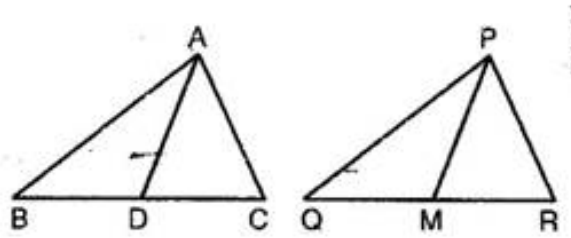
$$\Rightarrow \frac{\text{Area}(\Delta DEF)}{\text{Area}(\Delta ABC)} = \frac{DE^2}{AB^2} = \left(\frac{1}{2}AB\right)^2 \frac{1}{AB^2}$$

$$[\because DE = \frac{1}{2}AB]$$

$$\text{Hence, Area}(\Delta DEF) : \text{Area}(\Delta ABC) = 1 : 4$$

6. Prove that the ratio of the areas of two similar triangles is equal to the square of the ratio of their corresponding medians.

Ans. Given: $\triangle ABC \sim \triangle PQR$, AD and PM are the medians of \triangle s ABC and PQR respectively.



To Prove: $\frac{\text{Area}(\triangle ABC)}{\text{Area}(\triangle PQR)} = \frac{AD^2}{PM^2}$

Proof: Since $\triangle ABC \sim \triangle PQR$

$$\therefore \frac{\text{Area}(\triangle ABC)}{\text{Area}(\triangle PQR)} = \frac{AB^2}{PQ^2} \dots\dots\dots(1)$$

But, $\frac{AB}{PQ} = \frac{AD}{PM}$ (2)

∴ From eq. (1) and (2), we have,

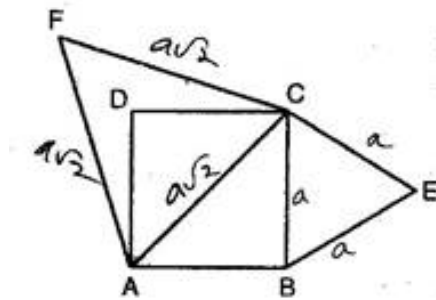
$$\frac{\text{Area}(\triangle ABC)}{\text{Area}(\triangle PQR)} = \frac{AD^2}{PM^2}$$

7. Prove that the area of an equilateral triangle described on one side of a square is equal to half the area of the equilateral triangle described on one of the diagonals.

Tick the correct answer and justify:

Ans. Given: A square ABCD,

Equilateral \triangle s BCE and ACF have been drawn on side BC and the diagonal AC respectively.



To Prove: $\text{Area}(\triangle BCE) = \frac{1}{2} \text{Area}(\triangle ACF)$

Proof: $\triangle BCE \sim \triangle ACF$

[Being equilateral so similar by AAA criterion of similarity]

$$\Rightarrow \frac{\text{Area}(\triangle BCE)}{\text{Area}(\triangle ACF)} = \frac{BC^2}{AC^2}$$

$$\Rightarrow \frac{\text{Area}(\triangle BCE)}{\text{Area}(\triangle ACF)} = \frac{BC^2}{(\sqrt{2}BC)^2}$$

$$[\because \text{Diagonal} = \sqrt{2} \text{ side} \Rightarrow AC = \sqrt{2} BC]$$

$$\Rightarrow \frac{\text{Area}(\triangle BCE)}{\text{Area}(\triangle ACF)} = \frac{1}{2}$$

8. ABC and BDE are two equilateral triangles such that D is the mid-point of BC. Ratio of the areas of triangles ABC and BDE is:

(A) 2: 1

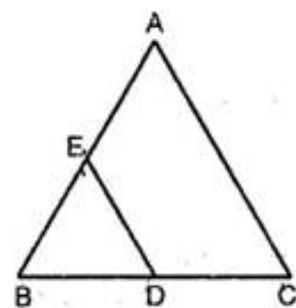
(B) 1: 2

(C) 4: 1

(D) 1: 4

Ans. (C) Since $\triangle ABC$ and $\triangle BDE$ are equilateral, they are equiangular and hence,

$$\triangle ABC \sim \triangle BDE$$



$$\Rightarrow \frac{\text{Area}(\triangle ABC)}{\text{Area}(\triangle BDE)} = \frac{BC^2}{BD^2}$$

$$\Rightarrow \frac{\text{Area}(\triangle ABC)}{\text{Area}(\triangle BDE)} = \frac{(2BD)^2}{BD^2}$$

$[\because D \text{ is the mid-point of } BC]$

$$\Rightarrow \frac{\text{Area}(\triangle ABC)}{\text{Area}(\triangle BDE)} = \frac{4}{1}$$

\therefore (C) is the correct answer.

9. Sides of two similar triangles are in the ratio 4 : 9. Areas of these triangles are in the ratio:

- (A) 2: 3
- (B) 4: 9
- (C) 81: 16
- (D) 16: 81

Ans. (D) Since the ratio of the areas of two similar triangles is equal to the ratio of the squares of any two corresponding sides. Therefore,

$$\text{Ratio of areas} = \frac{(4)^2}{(9)^2} = \frac{16}{81}$$

∴ (D) is the correct answer.

***** END *****