



Definite Integrals Ex 20.1 Q1

We know that $\int x^n dx = \frac{x^{n+1}}{n+1} + C$

Now,

$$\begin{aligned} & \int_4^9 \frac{1}{\sqrt{x}} dx \\ &= \left[\frac{x^{-\frac{1}{2}+1}}{-\frac{1}{2}+1} \right]_4^9 \\ &= \left[\frac{\sqrt{x}}{\frac{1}{2}} \right]_4^9 \\ &= 2[\sqrt{9} - \sqrt{4}] \\ &= 2[3 - 2] \\ &= 2 \end{aligned}$$

$$\therefore \int_4^9 \frac{1}{\sqrt{x}} dx = 2$$

Definite Integrals Ex 20.1 Q2

We know that $\int \frac{dx}{x} = \log x + C$

Now,

$$\begin{aligned} & \int_{-2}^3 \frac{1}{x+7} dx \\ &= [\log(x+7)]_{-2}^3 \\ &= [\log 10 - \log 5]_{-2}^3 \\ &= \log \frac{10}{5} \quad \left[\because \log a - \log b = \log \frac{a}{b} \right] \\ &= \log 2 \end{aligned}$$

$$\therefore \int_{-2}^3 \frac{1}{x+7} dx = \log 2$$

Definite Integrals Ex 20.1 Q3

$$\begin{aligned}\text{Let } x &= \sin \theta \\ \Rightarrow dx &= \cos \theta d\theta\end{aligned}$$

Now,

$$x = 0 \Rightarrow \theta = 0$$

$$x = \frac{1}{2} \Rightarrow \theta = \frac{\pi}{6}$$

$$\begin{aligned}\therefore \int_0^{\frac{\pi}{6}} \frac{1}{\sqrt{1 - \sin^2 \theta}} \cos \theta d\theta \\ &= \int_0^{\frac{\pi}{6}} \frac{\cos \theta d\theta}{\cos \theta} \\ &= \int_0^{\frac{\pi}{6}} d\theta \\ &= [\theta]_0^{\frac{\pi}{6}} \\ &= \left[\frac{\pi}{6} - 0 \right] \\ &= \frac{\pi}{6}\end{aligned}$$

$$\therefore \int_0^{\frac{1}{2}} \frac{1}{\sqrt{1 - x^2}} = \frac{\pi}{6}$$

Definite Integrals Ex 20.1 Q4

We have,

$$I = \int_0^1 \frac{1}{1+x^2} dx$$

$$= \left[\tan^{-1} x \right]_0^1$$

$$= \left[\tan^{-1} 1 - \tan^{-1} 0 \right]$$

$$= \left[\frac{\pi}{4} - 0 \right]$$

$$\left[\because \tan^{-1} 1 = \frac{\pi}{4} \right]$$

$$= \frac{\pi}{4}$$

$$\therefore \int_0^1 \frac{1}{1+x^2} dx = \frac{\pi}{4}$$

***** END *****