



Exercise 2K

Question 15:

$$\begin{aligned} & (x + y - z)(x^2 + y^2 + z^2 - xy + yz + zx) \\ &= [x + y + (-z)] [(x)^2 + (y)^2 + (-z)^2 - (x)(y) - (y)(-z) - (-z)(x)] \\ &= x^3 + y^3 - z^3 + 3xyz. \end{aligned}$$

Question 16:

$$\begin{aligned} & (x - 2y + 3)(x^2 + 4y^2 + 2xy - 3x + 6y + 9) \\ &= [x + (-2y) + 3] [(x)^2 + (-2y)^2 + (3)^2 - (x)(-2y) - (-2y)(3) - (3)(x)] \\ &= (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca) \\ &= a^3 + b^3 + c^3 - 3abc \\ &\text{Where, } x = a, (-2y) = b \text{ and } 3 = c \\ & (x - 2y + 3)(x^2 + 4y^2 + 2xy - 3x + 6y + 9) \\ &= (x)^3 + (-2y)^3 + (3)^3 - 3(x)(-2y)(3) \\ &= x^3 - 8y^3 + 27 + 18xy. \end{aligned}$$

Question 17:

$$\begin{aligned} & (x - 2y - z)(x^2 + 4y^2 + z^2 + 2xy + zx - 2yz) \\ &= [x + (-2y) + (-z)] [(x)^2 + (-2y)^2 + (-z)^2 - (x)(-2y) - (-2y)(-z) - (-z)(x)] \\ &= (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca) \\ &= a^3 + b^3 + c^3 - 3abc \\ &\text{Where } x = a, (-2y) = b \text{ and } (-z) = c \\ & (x - 2y - z)(x^2 + 4y^2 + z^2 + 2xy + zx - 2yz) \\ &= (x)^3 + (-2y)^3 + (-z)^3 - 3(x)(-2y)(-z) \\ &= x^3 - 8y^3 - z^3 - 6xyz. \end{aligned}$$

***** END *****