

Chapter 6 Determinants Ex 6.2 Q33

$$\begin{vmatrix} b^2 + c^2 & ab & ac \\ ba & c^2 + a^2 & bc \\ ca & cb & a^2 + b^2 \end{vmatrix} = 4a^2b^2c^2$$

$$LHS = \begin{vmatrix} b^2 + c^2 & ab & ac \\ ba & c^2 + a^2 & bc \\ ca & cb & a^2 + b^2 \end{vmatrix}$$

Multiply R_1 , R_2 and R_3 by a,b and c respectively.

$$= \frac{1}{abc} \begin{vmatrix} ab^2 + ac^2 & a^2b & a^2c \\ b^2a & bc^2 + ba^2 & b^2c \\ c^2a & c^2b & ca^2 + cb^2 \end{vmatrix}$$

Take a,b and c common from C_1,C_2 and C_3 respectively.

$$= \frac{abc}{abc} \begin{vmatrix} b^2 + c^2 & a^2 & a^2 \\ b^2 & c^2 + a^2 & b^2 \\ c^2 & c^2 & a^2 + b^2 \end{vmatrix}$$

Now apply $R_1 \rightarrow R_1 + R_2 + R_3$

$$= \begin{vmatrix} 2(b^{2}+c^{2}) & 2(c^{2}+a^{2}) & 2(a^{2}+b^{2}) \\ b^{2} & c^{2}+a^{2} & b^{2} \\ c^{2} & c^{2} & a^{2}+b^{2} \end{vmatrix}$$

$$= 2\begin{vmatrix} (b^{2}+c^{2}) & (c^{2}+a^{2}) & (a^{2}+b^{2}) \\ b^{2} & c^{2}+a^{2} & b^{2} \\ c^{2} & c^{2} & a^{2}+b^{2} \end{vmatrix}$$

$$= 2\begin{vmatrix} c^{2} & 0 & a^{2} \\ b^{2} & c^{2}+a^{2} & b^{2} \\ c^{2} & c^{2} & a^{2}+b^{2} \end{vmatrix}$$

$$= 2\left[c^{2}\left(\left(c^{2}+a^{2}\right)\left(a^{2}+b^{2}\right)-b^{2}c^{2}\right)+a^{2}\left(b^{2}c^{2}-\left(c^{2}+a^{2}\right)c^{2}\right)\right]$$

$$= 4a^{2}b^{2}c^{2}$$

$$= RHS$$

Chapter 6 Determinants Ex 6.2 Q34

$$\begin{vmatrix} 0 & b^{2}a & c^{2}a \\ a^{2}b & 0 & c^{2}b \\ a^{2}c & b^{2}c & 0 \end{vmatrix} = 2a^{3}b^{3}c^{3}$$

$$A = \begin{vmatrix} 0 & b^{2}a & c^{2}a \\ a^{2}b & 0 & c^{2}b \\ a^{2}c & b^{2}c & 0 \end{vmatrix}$$

$$= a^{2}b^{2}c^{2}\begin{vmatrix} 0 & a & a \\ b & 0 & b \\ c & c & 0 \end{vmatrix}$$

$$= a^{3}b^{3}c^{3}\begin{vmatrix} 1 & 0 & 1 \\ 1 & 1 & 0 \end{vmatrix}$$

$$= a^{3}b^{3}c^{3}\begin{vmatrix} 1 & -1 & 1 \\ 1 & 1 & 0 \end{vmatrix}$$

$$= 2a^{3}b^{3}c^{3}$$

$$= RHS$$

Chapter 6 Determinants Ex 6.2 Q35

$$\begin{vmatrix} \frac{a^2 + b^2}{c} & c & c \\ a & \frac{b^2 + c^2}{a} & a \\ b & b & \frac{c^2 + a^2}{b} \end{vmatrix}$$

$$= \frac{1}{abc} \begin{vmatrix} a^2 + b^2 & c^2 & c^2 \\ a^2 & c^2 + b^2 & a^2 \\ b^2 & b^2 & c^2 + a^2 \end{vmatrix}$$

$$= \frac{1}{abc} \begin{vmatrix} 0 & -2b^2 & -2a^2 \\ a^2 & c^2 + b^2 & a^2 \\ b^2 & b^2 & c^2 + a^2 \end{vmatrix}$$

$$= \frac{-2}{abc} \begin{vmatrix} 0 & b^2 & a^2 \\ a^2 & c^2 + b^2 & a^2 \\ b^2 & b^2 & c^2 + a^2 \end{vmatrix}$$

$$= \frac{-2}{abc} \begin{vmatrix} 0 & b^2 & a^2 \\ a^2 & c^2 + b^2 & a^2 \\ b^2 & 0 & c^2 \end{vmatrix}$$

$$= \frac{-2}{abc} \begin{vmatrix} 0 & b^2 & a^2 \\ a^2 & c^2 + b^2 & a^2 \\ b^2 & 0 & c^2 \end{vmatrix}$$

$$= \frac{-2}{abc} [(-a^2)(b^2c^2) + (b^2)(-a^2c^2)]$$

$$= \frac{-2}{abc} (-2a^2b^2c^2)$$

$$= 4abc$$

$$= RHS$$

Chapter 6 Determinants Ex 6.2 Q36

$$-bc$$
 b^2+bc c^2+bc
 a^2+ac $-ac$ c^2+ac
 a^2+ab b^2+ab $-ab$

Multiply R_1, R_2 and R_3 by a, b and c respectively

$$= \frac{1}{abc}\begin{vmatrix} -abc & ab^2 + abc & ac^2 + abc \\ a^2b + abc & -abc & bc^2 + abc \\ a^2c + abc & b^2c + abc & -abc \end{vmatrix}$$

Take a,b and c common from C_1,C_2 and C_3 respectively.

$$= \qquad \frac{abc}{abc} \begin{vmatrix} -bc & ab+ac & ac+ab \\ ab+bc & -ac & bc+ab \\ ac+bc & bc+ac & -ab \end{vmatrix}$$

$$\mathsf{Apply}(R_1 \to R_1 + R_2 + R_3$$

$$= (ab + bc + ca)^{3} \begin{vmatrix} 0 & 1 & 0 \\ 1 & -ac & 1 \\ 0 & bc + ac & -1 \end{vmatrix}$$

$$= \left(ab + bc + ca\right)^3$$

= RHS

********* END *******