



Since, it is an absolute function. So, it is continuous function. The graph of the function is as below:-

Chapter 10 Differentiability Ex 10.2 Q10

$$f(x) = e^{|x|}$$

$$f(x) = \begin{cases} e^{-x} & , x < 0 \\ e^{x} & , x \ge 0 \end{cases}$$

For continuity at x = 0

RHL = 
$$\lim_{x \to 0^{+}} f(x)$$
  
=  $\lim_{h \to 0} f(0+h)$   
=  $\lim_{h \to 0} e^{(0+h)}$   
=  $\lim_{h \to 0} e^{h}$   
=  $e^{0}$   
RHL = 1  
LHL =  $\lim_{x \to 0^{-}} f(x)$   
=  $\lim_{h \to 0} f(0-h)$   
=  $\lim_{h \to 0} e^{-(0-h)}$   
=  $\lim_{h \to 0} e^{h}$   
LHL = 1  
 $f(0) = e^{0}$   
= 1

Now,

$$LHL = f(0) = RHL$$

So, f(x) is continuous at x = 0

For differentiablility at x = 0

LHD 
$$= \lim_{x \to 0^{-}} \frac{f(x) - f(0)}{x - 0}$$

$$= \lim_{h \to 0} \frac{f(0 - h) - e^{0}}{(0 - h) - 0}$$

$$= \lim_{h \to 0} \frac{e^{-(0 - h)} - 1}{-h}$$

$$= \lim_{h \to 0} \frac{e^{h} - 1}{-h}$$

$$= 1$$

Since 
$$\lim_{x \to 0} \frac{e^x - 1}{x} = 1$$

RHD 
$$= \lim_{h \to 0^+} \frac{f(x) - f(0)}{x - 0}$$
$$= \lim_{h \to 0} \frac{f(0 + h) - f(0)}{(0 + h) - 0}$$
$$= \lim_{h \to 0} \frac{e^x - e^0}{h}$$
$$= \lim_{h \to 0} \frac{e^h - 1}{h}$$
$$= 1$$

Since 
$$\lim_{x\to 0} \frac{e^x - 1}{x} = 1$$

Clearly,

So,

$$f(x)$$
 is not differentiable at  $x = 0$ .

Differentiability Ex 10.2 Q11

$$f\left(x\right) = \begin{cases} \left(x-c\right)\cos\frac{1}{\left(x-c\right)} & , x \neq c \\ 0 & , x = c \end{cases}$$

(LHL at 
$$x = c$$
) =  $\lim_{x \to c} f(x)$ 

$$\begin{aligned} & \underset{h \to 0}{\text{lim } f(-h)} \\ & = \underset{h \to 0}{\text{lim } (c - h - c) \cos \left(\frac{1}{c - h - c}\right)} \\ & = \underset{h \to 0}{\text{lim } - h \cos \left(-\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } - h \cos \left(\frac{1}{h}\right)} \\ & = 0 \\ \text{(RHL at } x = c) = \underset{h \to 0}{\text{lim } f(x)} \\ & = \underset{h \to 0}{\text{lim } f(c + h)} \\ & = \underset{h \to 0}{\text{lim } f(c + h)} \\ & = \underset{h \to 0}{\text{lim } f(c + h)} \\ & = \underset{h \to 0}{\text{lim } h \cos \left(\frac{1}{h}\right)} \\ & = 0 \\ \text{Since, LHL} = f(x) = \text{RHL at } x = c \\ \Rightarrow f(x) \text{ is continuous at } x = c \\ \text{(LHD at } x = c) = \underset{h \to 0}{\text{lim } \frac{f(c - h) - f(c)}{-h}} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h \to 0}{\text{lim } \cos \left(\frac{1}{h}\right)} \\ & = \underset{h$$

f(x) is differentiable and continuous at x = c. Differentiability Ex 10.2 Q12

$$f(x) = |\sin x| = \begin{cases} -\sin x , & x < n\pi \\ \sin x , & x \ge n\pi \end{cases}$$
For  $x = m\pi$  ( $n$  even)

$$(LHD at  $x = n\pi$ ) =  $\lim_{x \to m^{-1}} \frac{f(x) - f(m\pi)}{x - n\pi}$ 

$$= \lim_{h \to 0} \frac{-\sin(n\pi - h) - \sin n\pi}{n\pi - h - n\pi}$$

$$= \lim_{h \to 0} \frac{\sinh - 0}{-h}$$

$$= -1$$

$$(RHD at  $x = n\pi$ ) =  $\lim_{h \to 0} \frac{\sin(n\pi + h) - \sin n\pi}{h}$ 

$$= \lim_{h \to 0} \frac{\sinh - h}{h}$$

$$= 1$$

$$(LHD at  $x = n\pi$ )  $\neq$  ( $n$  is odd)
$$(LHD at  $x = n\pi$ ) =  $\lim_{h \to 0} \frac{-\sin(n\pi - h) - \sin n\pi}{-h}$ 

$$= \lim_{h \to 0} \frac{-\sinh - h}{-h}$$

$$= 1$$

$$(RHD at  $x = n\pi$ ) =  $\lim_{h \to 0} \frac{\sin(n\pi + h) - \sin n\pi}{-h}$ 

$$= \lim_{h \to 0} \frac{-\sinh - 0}{h}$$

$$= \lim_{h \to 0} \frac{-\sinh - 0}{h}$$

$$= -1$$

$$(LHD at  $x = n\pi$ )  $\neq$  ( $n$  is not differentiable at  $n$  and  $n$  and  $n$  and  $n$  and  $n$  and  $n$  and  $n$  are  $n$  and  $n$  and  $n$  and  $n$  are  $n$  and  $n$  and  $n$  are  $n$  and  $n$  and  $n$  are  $n$  are  $n$  are  $n$  are  $n$  and  $n$  are  $n$$$$$$$$$$$$$

$$f(x) = |\sin x|$$
 is not differentiable at  $x = n\pi$ 

Since, cos(-x) = cos x

$$\Rightarrow$$
  $f(x) = \cos x$ 

$$\Rightarrow$$
  $f(x) = \cos |x|$  is differnetiable everywhere.

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