

Binary Operations Ex 3.1 Q1(i) We have,

$$a*b=a^b$$
 for all $a,b\in N$

Let $a \in N$ and $b \in N$

$$\Rightarrow$$
 $a^b \in N$

$$\Rightarrow a*b \in N$$

The operation * defines a binary operation on N

Binary Operations Ex 3.1 Q1(ii) We have,

$$a \circ b = a^b$$
 for all $a, b \in Z$

Let $a \in Z$ and $b \in Z$

$$\Rightarrow a^b \notin Z \Rightarrow a \circ b \notin Z$$

For example, if a=2, b=-2

$$\Rightarrow \qquad a^b = 2^{-2} = \frac{1}{4} \notin Z$$

.. The operation 'o' does not define a binary operation on Z.

Binary Operations Ex 3.1 Q1(iii)

We have,

$$a*b=a+b-2$$
 for all $a,b\in N$

Let $a \in N$ and $b \in N$

Then, $a+b-2 \notin N$ for all $a,b \in N$

For example a=1, b=1

 \therefore The operation * does not define a binary operation on W Binary Operations Ex 3.1 Q1(iv)

We have,

$$S = \{1, 2, 3, 4, 5\}$$

and, $a \times_6 b = Remainder when ab is divided by 6$

Let $a \in S$ and $b \in S$

$$\Rightarrow a \times_6 b \notin S \text{ for all } a, b \in S$$

For example, a = 2, b = 3

⇒
$$2 \times_6 3$$
 = Remainder when 6 is divided by 6 = $0 \notin S$

 x_6 does not define a binary oparation on S

Binary Operations Ex 3.1 Q1(v) We have,

$$S = \{0,1,2,3,4,5\}$$
 and,
$$a+_{6}b = \begin{cases} a+b; & \text{if } a+b < 6 \\ a+b-6; & \text{if } a+b \geq 6 \end{cases}$$

Let $a \in S$ and $b \in S$ such that a + b < 6

Then
$$a+_6b=a+b\in S$$
 $[\because a+b<6=0,1,2,3,4,5]$

Let $a \in S$ and $b \in S$ such that a + b > 6

Then
$$a+_6b=a+b-6\in S$$
 [vif $a+b\geq 6$ then $a+b-6\geq 0=0,1,2,3,4,5$]

$$\therefore$$
 a+6 b e S for a, b e S

 \therefore +₆ defines a binary oparation on S

Binary Operations Ex 3.1 Q1(vi)

We have,

$$a \circ b = a^b + b^a$$
 for all $a, b \in N$

Let $a \in N$ and $b \in N$

$$\Rightarrow a^b \in N \text{ and } b^a \in N$$

$$\Rightarrow \qquad a^b + b^a \in N$$

Thus, the operation 'o' defines a binary relation on N Binary Operations Ex 3.1 Q1(vii) We have,

$$a*b = \frac{a-1}{b+1}$$
 for all $a,b \in Q$

Let $a \in Q$ and $b \in Q$

Then
$$\frac{a-1}{b+1} \notin Q$$
 for $b=-1$

$$\Rightarrow a*b\notin Q \text{ for all } a,b\in Q$$

Thus, the operation * does not define a binary operation on Q

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