

## Continuity Ex 9.1 Q36 The given function will be continuous at x = 0 if LHL = RHL = f(0)....(1)

$$\begin{split} f\left(0\right) &= 8 \ldots \ldots \left(A\right) \\ \text{LHL} &= \lim_{x \to 0^{-}} f\left(x\right) = \lim_{h \to 0} f\left(0 - h\right) = \lim_{h \to 0} \frac{1 - \cos 2k \left(-h\right)}{\left(-h\right)^{2}} = \lim_{h \to 0} \frac{1 - \cos 2kh}{h^{2}} = \lim_{h \to 0} \frac{2 \sin^{2} kh}{h^{2}} \\ &= \lim_{h \to 0} 2 \left(\frac{\sin kh}{kh}\right)^{2}.k^{2} \\ &= 2k^{2} \end{split}$$

Thus, using (1) we get,  

$$2k^2 = 8 \implies k^2 = 4 \implies k = \pm 2$$

Hence,  $k = \pm 2$ 

Let x-1=v

Since the function is continuous, L.H.Limit = R.H.Limit Thus,  $k = -\frac{2}{\pi}$ 

Since the function is continuous at every point, therefore

$$LHL = RHL = f(0)$$

Now

$$f(0) = \cos 0$$
$$= 1$$

Again

$$LHL = \lim_{x \to 0} k \left( x^2 - 2x \right)$$
$$= \lim_{h \to 0^+} k \left( h^2 - 2h \right)$$
$$= 0$$

Therefore there is no value of k

Since the function is continuous at every point, therefore

$$LHL = RHL = f(\pi)$$

Now

$$f(\pi) = k\pi + 1$$

Again

$$RHL = \lim_{x \to \pi^{+}} \cos x$$

$$= \lim_{h \to 0^{+}} \cos (\pi - h)$$

$$= -\lim_{h \to 0^{+}} \cosh$$

$$= -1$$

Therefore we can write

$$k\pi + 1 = -1$$
$$k = -\frac{2}{\pi}$$

We are given that function is continuous at x = 5.

: LHL = RHL = 
$$f(5)$$
 .... (1)

$$f(5) = 5k + 1$$

LHL = 
$$\lim_{x \to 5^{+}} f(x) = \lim_{h \to 0} f(5+h) = \lim_{h \to 0} 3(5+h) - 5 = 10$$

Thus, using (1), we get,

$$5k + 1 = 10$$

$$5k = 9$$

$$k = \frac{9}{5}$$

We know that the function will be continuous at x = 5. if LHL = RHL = f(5)....(1)

$$f(5) = k$$

$$LHL = \lim_{x \to 5} f\left(x\right) = \lim_{h \to 0} \left(5 - h\right) = \lim_{h \to 0} \frac{\left(5 - h\right)^2 - 25}{\left(5 - h\right) - 5} = \lim_{h \to 0} \frac{h^2 - 10h}{-h} = \lim_{h \to 0} h + 10 = 10$$

Thus, using (1), we get,

k = 10

We know that a function will be continuous at x = 1. if

$$LHL = RHL = f(1) \qquad \dots (1)$$

$$f(1) = k \cdot 1^2 = k$$

LHL = 
$$\lim_{x \to 1^{-}} f(x) = \lim_{h \to 0} f(1-h) = \lim_{h \to 0} 4 = 4$$

Thus, using (1), we get,

$$k = 4$$

We know that a function will be continuous at x = 0. if LHL = RHL = f(0)....(1)

$$f(0) = k(0+2) = 2k$$

$$\mathsf{LHL} = \lim_{x \to 0^+} f\left(x\right) = \lim_{h \to 0} f\left(0 + h\right) = \lim_{h \to 0} 3\left(h\right) + 1 = 1$$

Thus, using (1), we get,

$$2k = 1$$

$$k = \frac{1}{2}$$

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