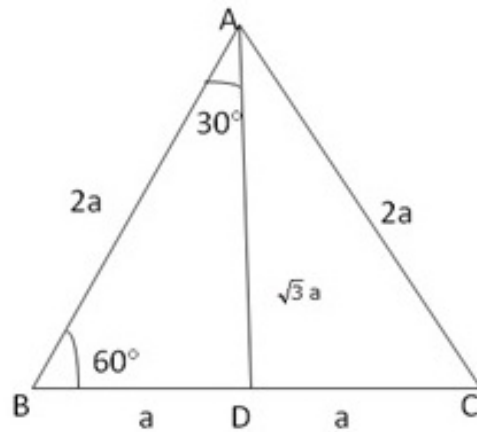




Question 26:



$$\therefore \angle A = \angle B = \angle C = 60^\circ$$

Draw $AD \perp BC$

In $\triangle ABD$ and $\triangle ACD$,

$$AD = AD \quad (\text{common})$$

$$\angle ADB = \angle ADC \quad (90^\circ)$$

$$AB = AC \quad (\triangle ABC \text{ is an equilateral triangle})$$

$$\therefore \triangle ABD \cong \triangle ACD \quad (\text{RHS congruence criterion})$$

$$BD = DC \quad (\text{pct})$$

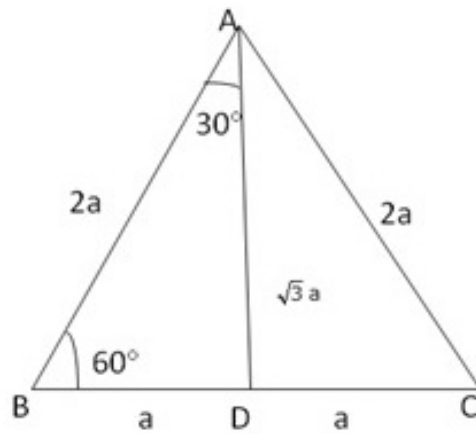
$$\angle BAD = \angle CAD \quad (\text{pct})$$

$$\therefore BD = \frac{2a}{2} = a \text{ and } \angle BAD = \frac{60^\circ}{2} = 30^\circ$$

In $\triangle ABD$,

$$\sin 30^\circ = \frac{BD}{AB} = \frac{a}{2a} = \frac{1}{2}$$

Question 27:



$$\therefore \angle A = \angle B = \angle C = 60^\circ$$

Draw $AD \perp BC$

In $\triangle ABD$ and $\triangle ACD$,

$$AD = AD \quad (\text{common})$$

$$\angle ADB = \angle ADC \quad (90^\circ)$$

$$AB = AC \quad (\triangle ABC \text{ is an equilateral triangle})$$

$$\therefore \triangle ABD \cong \triangle ACD \quad (\text{RHS congruence criterion})$$

$$BD = DC \quad (\text{pct})$$

$$\angle BAD = \angle CAD \quad (\text{pct})$$

$$\therefore BD = \frac{2a}{2} = a \text{ and } \angle BAD = \frac{60^\circ}{2} = 30^\circ$$

In $\triangle ABD$, $\angle D = 90^\circ$

By Pythagoras theorem,

$$AB^2 = BD^2 + DA^2$$

$$\therefore DA^2 = AB^2 - BD^2$$

$$\begin{aligned} DA^2 &= (2a)^2 - a^2 \\ &= 4a^2 - a^2 = 3a^2 \end{aligned}$$

$$\therefore DA = AD = \sqrt{3} a$$

In $\triangle ABD$,

$$\sin 60^\circ = \frac{AD}{DB} = \frac{\sqrt{3} a}{2a} = \frac{\sqrt{3}}{2}$$

***** END *****