

Arithematic Progressions Ex 19.4 Q15

Sum first n terms of the given AP is

$$S_n = 3n^2 + 2n$$

$$S_{n-1} = 3(n-1)^2 + 2(n-1)$$

$$a_n = S_n - S_{n-1}$$

$$a_n = 3n^2 + 2n - 3(n-1)^2 - 2(n-1)$$

$$a_n = 6n - 1$$

rth term is 6r - 1.

Arithematic Progressions Ex 19.4 Q16 Given,

$$a_1 = -14 = a + 0d$$

$$a_5 = 2 = a + 4d$$

Solving (i) and (ii)

$$a_1 = a = -14$$
 and $d = 4$

Let ther be n terms then sum of there n terms = 40

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$\Rightarrow 40 = \frac{n}{2} \left[-28 + (n-1) 4 \right]$$

$$\Rightarrow$$
 $4n^2 - 32n - 80 = 0$

or
$$n = 10 \text{ or } -2$$

But n can't be negative

$$n = 10$$

The given A.P has 10 terms.

Arithematic Progressions Ex 19.4 Q17

Given,

$$a_7 = 10$$

$$S_{14} - S_7 = 17 \qquad ---(i)$$

$$S_{14} = 17 + S_7 = 17 + 10 = 27 \qquad ---(ii)$$

From (i) and (ii)

and

$$S_{14} = \frac{14}{2} [2a + 13d]$$

 $\Rightarrow 27 = 28a + 182d ---(iv)$

Solving (iii) and (iv)

$$a = 1 \text{ and } d = \frac{1}{7}$$

:. The required A.P is

$$1, 1 + \frac{1}{7}, 1 + \frac{2}{7}, 1 + \frac{3}{7}, \dots, +\infty$$

or
$$1, \frac{8}{7}, \frac{9}{7}, \frac{10}{7}, \frac{11}{7}, \dots, \infty$$

Arithematic Progressions Ex 19.4 Q18 Given,

$$a_3 = 7 = a + 2d$$
 ---(i)
 $a_7 = 3a_3 + 2$
 $a_7 = 3(7) + 2$ [: $a_3 = 7$]
 $a_7 = 3 = a_7 + 6d$ ---(ii)

solving (i) and (ii) a = -1, d = 4

Then, sum of 20 terms of this A.P

$$S_{20} = \frac{20}{2} [2 + (20 - 1)4] \qquad \left[\text{Using } S_n = \frac{n}{2} [2a + (n - 1)d] \right]$$

$$= 10 \times 74$$

$$= 740$$

First term is -1 common defference = 4, sum of 20 terms = 740.

******* END *******