



Pair of Linear Equations in Two variables Ex 3.11 Q9

Answer :

We know that the sum of the opposite angles of cyclic quadrilateral is 180° . In the cyclic quadrilateral $ABCD$, angles A and C and angles B and D pairs of opposite angles

Therefore $\angle A + \angle C = 180^\circ$ and $\angle B + \angle D = 180^\circ$

Taking $\angle A + \angle C = 180^\circ$

By substituting $\angle A = (2x + 4)^\circ$ and $\angle C = (2y + 10)^\circ$ we get

$$2x + 4 + 2y + 10 = 180$$

$$2x + 2y + 14 = 180^\circ$$

$$2x + 2y = 180^\circ - 14^\circ$$

$$2x + 2y = 166 \dots (i)$$

Taking $\angle B + \angle D = 180^\circ$

By substituting $\angle B = (y + 3)^\circ$ and $\angle D = (4x - 5)^\circ$ we get

$$y + 3 + 4x - 5 = 180^\circ$$

$$4x + y - 5 + 3 = 180^\circ$$

$$4x + y - 2 = 180^\circ$$

$$4x + y = 180^\circ + 2^\circ$$

$$4x + y = 182^\circ \dots (ii)$$

By multiplying equation (ii) by 2 we get $8x + 2y = 364 \dots (iii)$

By subtracting equation (iii) from (i) we get

$$\begin{aligned}2x + 2y &= 166 \\-8x - 2y &= -364 \\ \hline -6x &= -198 \\ x &= \frac{-198}{-6} \\ x &= 33^\circ\end{aligned}$$

By substituting $x = 33^\circ$ in equation (ii) we get

$$\begin{aligned}4x + y &= 182 \\ 4 \times 33 + y &= 182 \\ 132 + y &= 182 \\ y &= 182 - 132 \\ y &= 50\end{aligned}$$

The angles of a cyclic quadrilateral are

$$\begin{aligned}\angle A &= 2x + 4 \\ &= 2 \times 33 + 4 \\ &= 66 + 4 \\ &= 70^\circ \\ \angle B &= y + 3 \\ &= 50 + 3 \\ &= 53^\circ\end{aligned}$$

$$\begin{aligned}\angle C &= 2y + 10^\circ \\ &= 2 \times 50 + 10 \\ &= 100 + 10 \\ &= 110^\circ\end{aligned}$$

$$\begin{aligned}\angle D &= 4x - 5 \\ &= 4 \times 33 - 5 \\ &= 132 - 5 \\ &= 127^\circ\end{aligned}$$

Hence, the angles of cyclic quadrilateral ABCD are $\angle A = 70^\circ, \angle B = 53^\circ, \angle C = 110^\circ, \angle D = 127^\circ$.

Pair of Linear Equations in Two variables Ex 3.11 Q10

Answer :

Let take first class full of fare is Rs x and reservation charge is Rs y per ticket

Then half of the ticket as on full ticket = $\frac{x}{2}$

According to the given condition we have

$$x + y = 216 \dots (i)$$

$$x + y + \left(\frac{x}{2}\right) + y = 327$$

$$x + \frac{x}{2} + y + y = 327$$

$$\frac{3x}{2} + 2y = 327 \dots (ii)$$

Multiplying equation (i) by 2 we have

$$2x + 2y = 432 \dots (iii)$$

Subtracting (ii) from (iii) we get

$$2x + 2y = 432$$

$$-\frac{3x}{2} - 2y = -327$$

$$2x - \frac{3x}{2} = 105$$

$$\frac{4x - 3x}{2} = 105$$

$$\frac{1x}{2} = 105$$

$$x = 105 \times 2$$

$$x = 210$$

Putting $x = 210$ in equation (i) we get

$$x + y = 216$$

$$210 + y = 216$$

$$y = 216 - 210$$

$$y = 6$$

Hence, the basic first class full fare is **Rs 210**

The reservation charge is **Rs 6**.

***** END *****