

Tangents and Normals Ex 16.1 Q1(v)

We know that the slope of the tangent to the curve y = f(x) is

$$\frac{dy}{dx} = f'(x) \qquad ---(A)$$

And the slope of the normal is

$$\frac{-1}{\frac{dy}{dx}} = \frac{-1}{f'(x)} \qquad ---(B)$$

$$x=a\left(\theta-\sin\theta\right),\ y=a\left(1+\cos\theta\right)$$

Now,

$$\frac{dy}{dx} = \frac{\frac{dy}{d\theta}}{\frac{dx}{d\theta}} = \frac{-a\sin\theta}{a\left(1-\cos\theta\right)}$$

 $\therefore \qquad \text{Slope of tangent of } \theta = -\frac{\pi}{2}$ 

$$\begin{split} \left(\frac{dy}{dx}\right)_{\theta = -\frac{\pi}{2}} &= \frac{-a\sin\left(-\frac{\pi}{2}\right)}{a\left(1 - \cos\left(-\frac{\pi}{2}\right)\right)} \\ &= \frac{a}{a(1 - 0)} = 1 \end{split}$$

Also, the slope of normal is

$$\frac{-1}{\frac{dy}{dx}} = \frac{-1}{f'(x)} = -1$$

Tangents and Normals Ex 16.1 Q1(vi)

We know that the slope of the tangent to the curve y = f(x) is

$$\frac{dy}{dx} = f'(x) \qquad ---(A)$$

And the slope of the normal is

$$\frac{-1}{\frac{dy}{dx}} = \frac{-1}{f'(x)} \qquad ---(B)$$

$$x = a\cos^3\theta$$
,  $y = a\sin^3\theta$ 

$$\therefore \frac{dx}{d\theta} = 3a\cos^2\theta \times (-\sin\theta) = -3a\sin\theta \times \cos^2\theta$$

and 
$$\frac{dy}{dx} = 3a \sin^2 \theta \times \cos \theta$$

Now,

$$\frac{dy}{dx} = \frac{\frac{dy}{d\theta}}{\frac{dx}{d\theta}} = \frac{3a\sin^2\theta \times \cos\theta}{-3a\sin\theta \times \cos^2\theta}$$
$$= -\tan\theta$$

 $\therefore \qquad \text{Slope of tangent at } \theta = \frac{\pi}{4} \text{ is}$ 

$$\left(\frac{dy}{dx}\right)_{\theta = \frac{x}{4}} = 1$$

Also, the slope of normal is

$$\frac{-1}{\frac{dy}{dx}} = \frac{-1}{f'(x)} = -1$$

Tangents and Normals Ex 16.1 Q1(vii)

We know that the slope of the tangent to the curve y = f(x) is

$$\frac{dy}{dx} = f'(x) \qquad ---(A)$$

And the slope of the normal is

$$\frac{-1}{\frac{dy}{dx}} = \frac{-1}{f'(x)} \qquad ---(B)$$

$$x = a(\theta - \sin \theta), y = a(1 - \cos \theta)$$

$$\therefore \frac{dx}{d\theta} = a(1 - \cos\theta), \frac{dy}{d\theta} = a(0 + \sin\theta) = a\sin\theta$$

Now,

$$\frac{dy}{dx} = \frac{\frac{dy}{d\theta}}{\frac{dx}{d\theta}} = \frac{a\sin\theta}{a(1-\cos\theta)}$$

Now, the slope of tangent at  $\theta = \frac{\pi}{2}$  is

$$\left(\frac{dy}{dx}\right)_{\theta = \frac{\pi}{2}} = \frac{a\sin\frac{\pi}{2}}{a\left(1 - \cos\frac{\pi}{2}\right)} = \frac{a}{a} = 1$$

And, the slope of normal is

$$\frac{-1}{\frac{dy}{dx}} = -1$$

Tangents and Normals Ex 16.1 Q1(viii)

We know that the slope of the tangent to the curve y = f(x) is

$$\frac{dy}{dx} = f'(x) \qquad ---(A)$$

And the slope of the normal is

$$\frac{-1}{\frac{dy}{dx}} = \frac{-1}{f'(x)}$$
 --- (B)

$$y = (\sin 2x + \cot x + 2)^2$$

$$\frac{dy}{dx} = 2\left(\sin 2x + \cot x + 2\right)\left(2\cos 2x - \cos ec^2x\right)$$

$$\therefore \qquad \text{Slope of tangent of } x = \frac{\pi}{2} \text{ is}$$

$$\left(\frac{dy}{dx}\right)_{x=\frac{\pi}{2}} = 2\left(\sin \pi + \cos \frac{\pi}{2} + 2\right)\left(2\cos \pi - \csc^2 \frac{\pi}{2}\right)$$
$$= 2\left(0 + 0 + 2\right)\left(-2 - 1\right)$$
$$= -12$$

: Slope of normal is

$$\frac{-1}{\frac{dy}{dx}} = \frac{1}{12}$$