

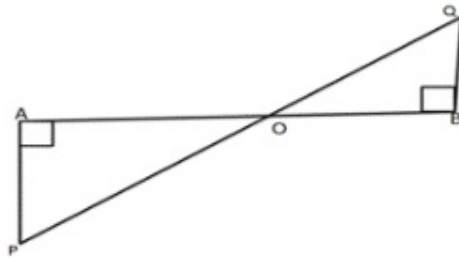


### Exercise 5A

Question 9:

Given:  $PA \perp AB$ ,  $QB \perp AB$ , and  $PA = QB$

To Prove:  $AO = OB$  and  $PO = OQ$



Proof: In  $\triangle APO$  and  $\triangle BPO$ ,

$$\angle PAO = \angle QBO = 90^\circ \text{ [Given]}$$

$$PA = QB \quad \text{[Given]}$$

$$\angle PAO = \angle QBO \quad \text{[Since } PA \perp AB, \text{ and } QB \perp AB, PA \parallel QB, \text{ and thus } PQ \text{ is a transversal, therefore, alternate angles are equal]}$$

So, by Angle-Side-Angle criterion of congruence, we have

$$\triangle APO \cong \triangle BPO$$

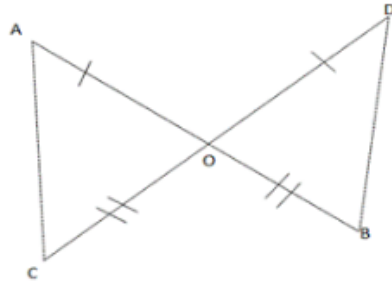
$$\Rightarrow AO = OB \text{ and } PO = OQ \quad \text{[Since corresponding parts of congruent triangles are equal]}$$

Thus, we have

O is the midpoint of AB and PQ.

Question 10:

Given: Line segments AB and CD intersect at O such that  $OA = OD$  and  $OB = OC$ .



To prove:  $AC = BD$

Proof: In  $\triangle AOC$  and  $\triangle BOD$ , we have

$$AO = OD \quad [\text{Given}]$$

$$\angle AOC = \angle BOD \quad [\text{Vertically opposite angles are equal}]$$

$$OC = OB \quad [\text{Given}]$$

So, by Side-Angle-Side criterion of congruence, we have,

$$\Rightarrow \triangle AOC \cong \triangle BOD$$

$$\Rightarrow AC = BD \quad [\text{Since the corresponding parts of the congruent triangles are equal}]$$

$$\Rightarrow \angle CAO = \angle BDO \quad [\text{by c.p.t}]$$

Thus, we have,  $AC = BD$

In case  $\angle ODB = \angle OBD$ , then  $\angle CAO = \angle OBD$  which means alternate angles made by lines AC and BD with transversal AB are equal and then lines AC and BD will be parallel.

\*\*\*\*\* END \*\*\*\*\*