

Algebraic Identities Ex 4.3 Q3

Answer:

In the given problem, we have to find the value of $a^3 + b^3$

Given a + b = 10, ab = 21

We shall use the identity $(a+b)^3 = a^3 + b^3 + 3ab(a+b)$

Here putting a + b = 10, ab = 21.

$$(10)^3 = a^3 + b^3 + 3(21)(10)$$

$$1000 = a^3 + b^3 + 630$$

$$1000 - 630 = a^3 + b^3$$

$$370 = a^3 + b^3$$

Hence the value of $a^3 + b^3$ is 370.

Algebraic Identities Ex 4.3 Q4

Answer:

In the given problem, we have to find the value of $a^3 - b^3$

Given a - b = -4, ab = 21

We shall use the identity $(a-b)^3 = a^3 - b^3 - 3ab(a-b)$

Here putting a-b=-4, ab=21.

$$(4)^3 = a^3 - b^3 - 3(21)(4)$$

$$64 = a^3 - b^3 - 252$$

$$64 + 252 = a^3 - b^3$$

$$316 = a^3 - b^3$$

Hence the value of $a^3 - b^3$ is 316.

Algebraic Identities Ex 4.3 Q5

Answer:

In the given problem, we have to find the value of $x^3 + \frac{1}{x^3}$

Given
$$x + \frac{1}{x} = 5$$

We shall use the identity $(a+b)^3 = a^3 + b^3 + 3ab(a+b)$

Here putting $x + \frac{1}{x} = 5$.

$$\left(x + \frac{1}{x}\right)^{3} = x^{3} + \frac{1}{x^{3}} + 3\left(x \times \frac{1}{x}\right)\left(x + \frac{1}{x}\right)$$

$$5^{3} = x^{3} + \frac{1}{x^{3}} + 3\left(x \times \frac{1}{x^{6}}\right)\left(x + \frac{1}{x}\right)$$

$$125 = x^{3} + \frac{1}{x^{3}} + 3\left(x + \frac{1}{x}\right)$$

$$125 = x^{3} + \frac{1}{x^{3}} + 3 \times 5$$

$$125 = x^{3} + \frac{1}{x^{3}} + 15$$

$$125 - 15 = x^{3} + \frac{1}{x^{3}}$$

$$110 = x^{3} + \frac{1}{x^{3}}$$

Hence the value of $x^3 + \frac{1}{x^3}$ is 110

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