



Definite Integrals Ex 20.4B Q44

$$I = \int_a^b x f(x) dx$$

$$\Rightarrow I = \int_a^b (a+b-x) f(a+b-x) dx$$

$$\Rightarrow I = \int_a^b (a+b-x) f(x) dx, \dots \dots \dots [\text{Given that } f(a+b-x) = f(x)]$$

$$\Rightarrow I = \int_a^b (a+b) f(x) dx - \int_a^b x f(x) dx$$

$$\Rightarrow I = \int_a^b (a+b) f(x) dx - I$$

$$\Rightarrow 2I = \int_a^b (a+b) f(x) dx$$

$$\Rightarrow I = \frac{a+b}{2} \int_a^b f(x) dx$$

Definite Integrals Ex 20.4B Q45

We have,

$$I = \int_{-a}^a f(x) dx = \int_{-a}^0 f(x) dx + \int_0^a f(x) dx$$

Let $x = -t$ then $dx = -dt$

$$x = -a \Rightarrow t = a$$

$$x = 0 \Rightarrow t = 0$$

$$\therefore \int_{-a}^0 f(x) dx = \int_a^0 f(-t) (-dt) = - \int_a^0 f(-t) dt$$

$$\Rightarrow \int_{-a}^0 f(x) dx = \int_0^a f(-t) dt$$

$$\Rightarrow \int_{-a}^0 f(x) dx = \int_0^a f(-x) dx$$

$$\therefore \int_{-a}^a f(x) dx = \int_0^a f(-x) dx + \int_0^a f(x) dx$$

Hence,

$$\int_{-a}^a f(x) dx = \int_0^a \{f(-x) + f(x)\} dx$$

Proved

Definite Integrals Ex 20.4B Q46

$$I = \int_0^{\pi} x f(\sin x) dx$$

$$I = \int_0^{\pi} (\pi - x) f(\sin(\pi - x)) dx$$

$$I = \int_0^{\pi} (\pi - x) f(\sin x) dx$$

$$2I = \int_0^{\pi} \pi f(\sin x) dx$$

$$I = \frac{\pi}{2} \int_0^{\pi} f(\sin x) dx$$

***** END *****