

Exercise 8B

Q1

Answer:

Let the numbers be 8x and 3x.

$$8x + 3x = 143$$

$$\Rightarrow 11x = 143$$

$$\Rightarrow x = \frac{143}{11}$$

$$\Rightarrow x = 13$$

 \therefore One number $= 8x = 8 \times 13 = 104$ Other number $= 3x = 3 \times 13 = 39$

Q2.

Answer:

Let the original number be x.

 $\frac{2}{3}$ of the number is 20 less than the original number.

$$\therefore \frac{2}{3}x = x - 20$$

$$\Rightarrow \frac{2x}{3} = x - 20$$

$$\Rightarrow 2x = 3\left(x - 20\right) \qquad \text{(by cross multiplication)}$$

$$\Rightarrow 2x = 3x - 60$$

$$\Rightarrow 2x - 3x = -60$$

$$\Rightarrow -x = -60$$

$$\Rightarrow x = 60$$

Therefore, the original number is 60.

Answer:

Let the number be x.

Four fifths of the number is 10 more than two thirds of the number.

$$\therefore \frac{4}{5}x = 10 + \frac{2}{3}x$$

$$\Rightarrow \frac{4x}{5} = 10 + \frac{2x}{3}$$

$$\Rightarrow \frac{4x}{5} = \frac{30 + 2x}{3} \qquad (L.C.M. \text{ of } 1 \text{ and } 3 \text{ is } 3)$$

$$\Rightarrow 3(4x) = 5(30 + 2x) \qquad \text{(by cross multiplication)}$$

$$\Rightarrow 12x = 150 + 10x$$

$$\Rightarrow 12x - 10x = 150$$

$$\Rightarrow 2x = 150$$

$$\Rightarrow x = \frac{150}{2} = 75$$

Therefore, the number is 75.

Q4.

Answer:

Let one part be x.

7 times the first part = 7x

Let the other part be (24-x).

5 times the second part = 5(24-x)

 $\Rightarrow x = \frac{26}{2} = 13$

Therefore, one part is 13.

Other part =
$$(24 - x) = (24 - 13) = 11$$

Q5.

Answer:

Let the number be x. Fifth part increased by $5 = \frac{x}{5} + 5$ Fourt part diminished by $5 = \frac{x}{4} - 5$

$$\therefore \frac{x}{5} + 5 = \frac{x}{4} - 5$$

$$\Rightarrow 5 + 5 = \frac{x}{4} - \frac{x}{5}$$

$$\Rightarrow 10 = \frac{5x - 4x}{20}$$

$$\Rightarrow 10 = \frac{x}{20}$$

$$\Rightarrow 200 = x$$

$$\Rightarrow x = 200$$

Therefore, the number is 200.

Q6.

Answer:

Let the common multiple for the given three numbers be x. Then, the three numbers would be 4x, 5x and 6x.

$$\therefore 4x + 6x = 5x + 55$$

$$\Rightarrow 10x = 5x + 55$$

$$\Rightarrow 10x - 5x = 55$$

$$\Rightarrow 5x = 55$$

$$\Rightarrow x = \frac{55}{5} = 11$$

$$\therefore$$
 Smallest number = $4x = 4(11) = 44$

Largest number is = 6x = 6(11) = 66

Third number = 5x = 5(11) = 55Therefore, the three numbers are 44, 55 and 66.

Q7.

Answer:

Let the number be x. $\therefore 10 + 4x = 5x - 5$ $\Rightarrow 10 + 5 = 5x - 4x$ $\Rightarrow 15 = x$ $\Rightarrow x = 15 \text{ (by transposition)}$ Therefore, the number is 15.

Q8.

Answer:

Let us consider x as the common multiple of both the number. Then, first number = 3xSecond number = 5x

$$\therefore \frac{3x+10}{5x+10} = \frac{5}{7}$$

$$\Rightarrow 7(3x+10) = 5(5x+10)$$
 (by cross multiplication)
$$\Rightarrow 21x + 70 = 25x + 50$$

$$\Rightarrow 21x - 25x = 50 - 70$$

$$\Rightarrow -4x = -20$$

$$\Rightarrow x = \frac{-20}{-4} = 5$$

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Therefore, the common multiple of both the numbers is 5.
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First number =
$$3x = 3 \times 5 = 15$$

Second number = $5x = 5 \times 5 = 25$

Q9.

Answer:

Let the first odd number be x.

Let the second odd number be (x+2).

Let the third odd number be (x+4).

$$\therefore x + (x+2) + (x+4) = 147$$

$$\Rightarrow x + x + 2 + x + 4 = 147$$

$$\Rightarrow 3x + 6 = 147$$

$$\Rightarrow 3x = 147 - 6$$

$$\Rightarrow 3x = 141$$

$$\Rightarrow x = \frac{141}{3} = 47$$

Therefore, the first odd number is 47.

Second odd number =
$$(x+2)$$
 = $(47+2)$ = 49

Third odd number =
$$(x+4) = (47+4) = 51$$

Q10.

Answer:

Let the first even number be x.

Let the second even number be x+2.

Let the third even number be x+4.

$$\therefore x + x + 2 + x + 4 = 234$$

$$\Rightarrow x + x + 2 + x + 4 = 234$$

$$\Rightarrow$$
 3x + 6 = 234

$$\Rightarrow 3x = 234 - 6$$

$$\Rightarrow 3x = 228$$

$$\Rightarrow x = \frac{228}{3} = 76$$

 \therefore First even number = x = 76

Second even number = x+2 = 76+2 = 78

Third even number = x + 4 = 80

Q11.

Answer:

Let the digit in the units place be x.

Digit in the tens place =
$$(12-x)$$

$$\therefore$$
 Original number = $10(12 - x) + x = 120 - 9x$

On reversing the digits, we have x at the tens place and (12-x) at the units

place.

:. New number =
$$10x + 12 - x = 9x + 12$$

New number - Original number = 54

$$\Rightarrow 9x + 12 - (120 - 9x) = 54$$

$$\Rightarrow 9x + 12 - 120 + 9x = 54$$

$$\Rightarrow 18x - 108 = 54$$

$$\Rightarrow 18x = 54 + 108$$

$$\Rightarrow 18x = 162$$

$$\Rightarrow x = \frac{162}{18} = 9$$

Therefore, the digit in the units place is 9.

Digit in tens place =
$$(12-x)$$
 = $(12-9)$ = 3

Therefore, the original number is 39.

Check:

The original number is 39.

Sum of the digits in the original number
$$= (3+9) = 12$$

New number obtained on reversing the digit s = 93

New number – Original number =
$$(93 - 39) = 54$$

Thus, both the given conditions are satisfied by 39. Hence, the original number is 39.

Q12.

Answer:

Let the digit in the units place be x.

Digit in the tens place = 3x

Original number =
$$10(3x) + x = 30x + x$$

On reversing the digits, we have x at the tens place and (3x) at the units place.

$$\therefore New number = 10(x) + 3x = 10x + 3x$$

New number = Original number - 36

$$\Rightarrow 10x + 3x = 30x + x - 36$$

$$\Rightarrow 13x = 31x - 36$$

$$\Rightarrow$$
 36 = 31 x - 13 x

$$\Rightarrow 36 = 18x$$

$$\Rightarrow 18x = 36$$

$$\Rightarrow x = \frac{36}{18} = 2$$

Therefore, the digit in the units place is 2.

Digit in the tens place =
$$(3x)$$
 = $3 \times 2 = 6$

Therefore, the original number is 62.

Check:

New number +36 = Original Number

$$26 + 36 = 62$$

Hence, both the conditions are satisfied.

Therefore, the original number is 62.

Q13.

Answer:

Let the numerator be x.

The denominator is greater than the numerator by 7.

$$\therefore \left(x+7\right)$$

$$\therefore \frac{x+17}{(x+7)-6} = 2$$

$$\Rightarrow \frac{x+17}{(x+7)} = 2$$

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