

Trigonometric Ratios Ex 5.1 Q13

## Answer:

Given:

$$\sec \theta = \frac{13}{5}$$

To show that 
$$\frac{2\sin\theta - 3\cos\theta}{4\sin\theta - 9\cos\theta} = 3$$

Now, we know that 
$$\cos \theta = \frac{1}{\sec \theta}$$

Therefore,

$$\cos\theta = \frac{1}{\frac{13}{5}}$$

Therefore,

$$\cos\theta = \frac{5}{13} \dots (1)$$

Now, we know that

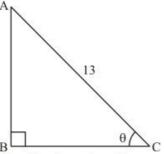
$$\cos \theta = \frac{\text{Base side adjacent to} \angle \theta}{\text{Hypotenuse}}$$
 ..... (2)

Now, by comparing equation (1) and (2) We get,

Base side adjacent to  $\angle \theta = 5$ 

And

Hypotenuse = 13



Therefore from above figure

Base side BC = 5

Hypotenuse AC = 13

Side AB is unknown, It can be determined by using Pythagoras theorem

Therefore by applying Pythagoras theorem

We get,

$$AC^2 = AB^2 + BC^2$$

Therefore by substituting the values of known sides

We get,

$$13^2 = AB^2 + 5^2$$

Therefore,

$$AB^2 = 13^2 - 5^2$$

$$AB^2 = 169 - 25$$

$$AB^2 = 144$$

$$AB = \sqrt{144}$$

Therefore,

$$AB = 12 \dots (3)$$

Now, we know that

$$\sin \theta = \frac{\text{Perpendicular side opposite to } \angle \theta}{\text{Hypotenuse}}$$

Now from figure (a)

We get,

$$\sin\theta = \frac{AB}{AC}$$

Therefore,

$$\sin\theta = \frac{12}{13} \dots (4)$$

Now L.H.S. of the equation to be proved is as follows

$$L.H.S. = \frac{2\sin\theta - 3\cos\theta}{4\sin\theta - 9\cos\theta}$$

Substituting the value of  $\cos\theta$  and  $\sin\theta$  from equation (1) and (4) respectively We get,

$$L.H.S. = \frac{2\left(\frac{12}{13}\right) - 3\left(\frac{5}{13}\right)}{4\left(\frac{12}{13}\right) - 9\left(\frac{5}{13}\right)}$$

Therefore,

$$L.H.S. = \frac{2 \times 12 - 3 \times 5}{4 \times 12 - 9 \times 5}$$

$$L.H.S. = \frac{24 - 15}{48 - 45}$$

$$L.H.S. = \frac{9}{3}$$

$$L.H.S. = \frac{24-15}{48-45}$$

$$L.H.S. = \frac{9}{3}$$

$$L.H.S. = 3$$

Hence proved that,

$$\frac{2\sin\theta - 3\cos\theta}{4\sin\theta - 9\cos\theta} = 3$$

\*\*\*\*\*\*\*\*\*\* END \*\*\*\*\*\*\*\*