



Relations Ex 1.2 Q9

(i) We have, L is the set of lines.

$R = \{(L_1, L_2) : L_1 \text{ is parallel to } L_2\}$ be a relation on L

Now,

Reflexivity: Let $L_1 \in L$

Since a line is always parallel to itself.

$$\therefore (L_1, L_1) \in R$$

$\Rightarrow R$ is reflexive

Symmetric: Let $L_1, L_2 \in L$ and $(L_1, L_2) \in R$

$\Rightarrow L_1$ is parallel to L_2

$\Rightarrow L_2$ is parallel to L_1

$\Rightarrow (L_2, L_1) \in R$

$\Rightarrow R$ is symmetric

Transitive: Let L_1, L_2 and $L_3 \in L$ such that $(L_1, L_2) \in R$ and $(L_2, L_3) \in R$

$\Rightarrow L_1$ is parallel to L_2 and L_2 is parallel to L_3

$\Rightarrow L_1$ is parallel to L_3

$\Rightarrow (L_1, L_3) \in R$

$\Rightarrow R$ is transitive

Since, R is reflexive, symmetric and transitive, so R is an equivalence relation.

(ii) The set of lines parallel to the line $y = 2x + 4$ is

$y = 2x + c$ For all $c \in R$

Where R is the set of real numbers.

Relations Ex 1.2 Q10

$R = \{(P_1, P_2) : P_1 \text{ and } P_2 \text{ have same the number of sides}\}$
 R is reflexive since $(P_1, P_1) \in R$ as the same polygon has the same number of sides with itself.
 Let $(P_1, P_2) \in R$.
 $\Rightarrow P_1$ and P_2 have the same number of sides.
 $\Rightarrow P_2$ and P_1 have the same number of sides.
 $\Rightarrow (P_2, P_1) \in R$
 $\therefore R$ is symmetric.
 Now,
 Let $(P_1, P_2), (P_2, P_3) \in R$.
 $\Rightarrow P_1$ and P_2 have the same number of sides. Also, P_2 and P_3 have the same number of sides.
 $\Rightarrow P_1$ and P_3 have the same number of sides.
 $\Rightarrow (P_1, P_3) \in R$
 $\therefore R$ is transitive.
 Hence, R is an equivalence relation.
 The elements in A related to the right-angled triangle (T) with sides 3, 4, and 5 are those polygons which have 3 sides (since T is a polygon with 3 sides).
 Hence, the set of all elements in A related to triangle T is the set of all triangles.

Relations Ex 1.2 Q11

Let A be set of points on plane.

Let $R = \{(P, Q) : OP = OQ\}$ be a relation on A where O is the origin.

To prove R is an equivalence relation, we need to show that R is reflexive, symmetric and transitive on A .

Now,

Reflexivity: Let $p \in A$

Since $OP = OP \Rightarrow (P, P) \in R$

$\Rightarrow R$ is reflexive

Symmetric: Let $(P, Q) \in R$ for $P, Q \in A$

Then $OP = OQ$

$\Rightarrow OQ = OP$

$\Rightarrow (Q, P) \in R$

$\Rightarrow R$ is symmetric

Transitive: Let $(P, Q) \in R$ and $(Q, S) \in R$

$\Rightarrow OP = OQ$ and $OQ = OS$

$\Rightarrow OP = OS$

$\Rightarrow (P, S) \in R$

$\Rightarrow R$ is transitive

Thus, R is an equivalence relation on A

Relations Ex 1.2 Q12

Given $A = \{1, 2, 3, 4, 5, 6, 7\}$ and $R = \{(a, b) : \text{both } a \text{ and } b \text{ are either odd or even number}\}$

Therefore,

$$R = \{(1, 1), (1, 3), (1, 5), (1, 6), (3, 3), (3, 5), (3, 7), (5, 5), (5, 7), (7, 7), (7, 5), (7, 3), (5, 3), (6, 1), (5, 1), (3, 1), (2, 2), (2, 4), (2, 6), (4, 4), (4, 6), (6, 6), (6, 4), (6, 2), (4, 2)\}$$

Form the relation R it is seen that R is symmetric, reflexive and transitive also. Therefore R is an equivalent relation.

From the relation R it is seen that $\{1, 3, 5, 7\}$ are related with each other only and $\{2, 4, 6\}$ are related with each other

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