



Indefinite Integrals Ex 19.2 Q36

$$\begin{aligned}\int \cos^{-1}(\sin x) dx &= \int \cos^{-1}\left[\cos\left(\frac{\pi}{2} - x\right)\right] dx \\&= \int \left(\frac{\pi}{2} - x\right) dx \\&= \frac{\pi}{2} \int dx - \int x dx \\&= \frac{\pi}{2} \times x - \frac{x^2}{2} + c \\ \therefore \int \cos^{-1}(\sin x) dx &= \frac{\pi}{2} \times x - \frac{x^2}{2} + c.\end{aligned}$$

Indefinite Integrals Ex 19.2 Q37

$$\begin{aligned}\int \cos^{-1}(\sin x) dx &= \int \cot^{-1}\left[\frac{\sin 2x}{1 - \cos 2x}\right] dx \\&= \int \cot^{-1}\left(\frac{\cos x}{\sin x}\right) dx \\&= \int \cot^{-1}(\cot x) dx \\&= \int x dx \\&= \frac{x^2}{2} + c \\ \therefore \int \cot^{-1}\left[\frac{\sin 2x}{1 - \cos 2x}\right] dx &= \frac{x^2}{2} + c.\end{aligned}$$

Indefinite Integrals Ex 19.2 Q38

$$\begin{aligned}\int \sin^{-1}\left(\frac{2 \tan x}{1 + \tan^2 x}\right) dx &= \int \sin^{-1}(\sin 2x) dx && \left[ \because \sin 2x = \frac{2 \tan x}{1 + \tan^2 x} \right] \\&= \int 2x dx \\&= 2 \int x dx \\&= \frac{2x^2}{2} + c \\&= x^2 + c \\ \therefore \int \sin^{-1}\left(\frac{2 \tan x}{1 + \tan^2 x}\right) &= x^2 + c.\end{aligned}$$

Indefinite Integrals Ex 19.2 Q39

$$\begin{aligned}
& \int \frac{(x^3 + 8)(x - 1)}{x^2 - 2x + 4} dx \\
&= \int \frac{(x + 2)(x^2 - 2x + 4)(x - 1)}{x^2 - 2x + 4} dx \\
&= \int (x + 2)(x - 1) dx \\
&= \int (x^2 - x + 2x - 2) dx \\
&= \int (x^2 + x - 2) dx \\
&= \frac{x^3}{3} + \frac{x^2}{2} - 2x + c \\
\therefore \int \frac{(x^3 + 8)(x - 1)}{x^2 - 2x + 4} dx &= \frac{x^3}{3} + \frac{x^2}{2} - 2x + c.
\end{aligned}$$

Indefinite Integrals Ex 19.2 Q40

$$\begin{aligned}
& \int (a \tan x + b \cot x)^2 dx \\
&= \int (a^2 \tan^2 x + b^2 \cot^2 x + 2ab \tan x \cot x) dx \\
&= \int [a^2 (\sec^2 x - 1) + b^2 (\operatorname{cosec}^2 x - 1) + 2ab] dx \\
&= \int [a^2 \sec^2 x - a^2 + b^2 \operatorname{cosec}^2 x - b^2 + 2ab] dx \\
&= a^2 \tan x - a^2 x - b^2 \cot x - b^2 x + 2abx + c \\
&= a^2 \tan x - b^2 \cot x - (a^2 + b^2 - 2ab)x + c \\
\therefore \int (a \tan x + b \cot x)^2 dx &= a^2 \tan x - b^2 \cot x - (a^2 + b^2 - 2ab)x + c.
\end{aligned}$$

Indefinite Integrals Ex 19.2 Q41

$$\begin{aligned}
& \int \frac{x^3 - 3x^2 + 5x - 7 + x^2 a^x}{2x^2} dx \\
&= \frac{1}{2} \int \frac{x^3}{x^2} dx - \frac{3}{2} \int \frac{x^2}{x^2} dx + \frac{5}{2} \int x \frac{x}{x^2} dx - \frac{7}{2} \int x^{-2} dx + \frac{1}{2} \int \frac{x^2 a^x}{x^2} dx \\
&= \frac{1}{2} \times \frac{x^2}{2} - \frac{3}{2} x + \frac{5}{2} \log x - \frac{7}{2} x^{-1} + \frac{1}{2} \frac{a^x}{\log a} + c \\
&= \frac{1}{2} \left[ \frac{x^2}{2} - 3x + 5 \log x + \frac{7}{x} + \frac{a^x}{\log a} \right] + c \\
\therefore \int \frac{x^3 - 3x^2 + 5x - 7 + x^2 a^x}{2x^2} dx &= \frac{1}{2} \left[ \frac{x^2}{2} - 3x + 5 \log x + \frac{7}{x} + \frac{a^x}{\log a} \right] + c
\end{aligned}$$

Indefinite Integrals Ex 19.2 Q42

$$\begin{aligned}
\frac{\cos x}{1+\cos x} &= \frac{\cos^2 \frac{x}{2} - \sin^2 \frac{x}{2}}{2 \cos^2 \frac{x}{2}} & \left[ \cos x = \cos^2 \frac{x}{2} - \sin^2 \frac{x}{2} \text{ and } \cos x = 2 \cos^2 \frac{x}{2} - 1 \right] \\
&= \frac{1}{2} \left[ 1 - \tan^2 \frac{x}{2} \right] \\
\therefore \int \frac{\cos x}{1+\cos x} dx &= \frac{1}{2} \int \left( 1 - \tan^2 \frac{x}{2} \right) dx \\
&= \frac{1}{2} \int \left( 1 - \sec^2 \frac{x}{2} + 1 \right) dx \\
&= \frac{1}{2} \int \left( 2 - \sec^2 \frac{x}{2} \right) dx \\
&= \frac{1}{2} \left[ 2x - \frac{\tan \frac{x}{2}}{\frac{1}{2}} \right] + C \\
&= x - \tan \frac{x}{2} + C
\end{aligned}$$

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