

$$A(adjA) = \begin{bmatrix} 2 & 3 \\ -4 & -6 \end{bmatrix} \begin{bmatrix} -6 & -3 \\ 4 & 2 \end{bmatrix}$$

$$= \begin{bmatrix} -12 + 12 & -6 + 6 \\ 24 - 24 & 12 - 12 \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$$
Also,  $(adjA)A = \begin{bmatrix} -6 & -3 \\ 4 & 2 \end{bmatrix} \begin{bmatrix} 2 & 3 \\ -4 & -6 \end{bmatrix}$ 

$$= \begin{bmatrix} -12 + 12 & -18 + 18 \\ 8 - 8 & 12 - 12 \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$$
Hence,  $A(adjA) = (adjA)A = |A|I$ 

Hence, A(adjA) = (adjA)A = |A|I.

# Question 4:

Verify  $A (adj A) = (adj A) A = \frac{|A|}{I}$ .

$$\begin{bmatrix} 1 & -1 & 2 \\ 3 & 0 & -2 \\ 1 & 0 & 3 \end{bmatrix}$$

Answer

$$A = \begin{bmatrix} 1 & -1 & 2 \\ 3 & 0 & -2 \\ 1 & 0 & 3 \end{bmatrix}$$
$$|A| = 1(0-0) + 1(9+2) + 2(0-0) = 11$$
$$\begin{bmatrix} 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} 11 \end{bmatrix}$$

$$|A|I = 11 \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 11 & 0 & 0 \\ 0 & 11 & 0 \\ 0 & 0 & 11 \end{bmatrix}$$

Now,

$$A_{11} = 0, A_{12} = -(9+2) = -11, A_{13} = 0$$

$$A_{21} = -(-3-0) = 3, A_{22} = 3-2 = 1, A_{23} = -(0+1) = -1$$

$$A_{31} = 2-0 = 2, A_{32} = -(-2-6) = 8, A_{33} = 0+3 = 3$$

$$\therefore adjA = \begin{bmatrix} 0 & 3 & 2 \\ -11 & 1 & 8 \\ 0 & -1 & 3 \end{bmatrix}$$

Now,

$$A(adjA) = \begin{bmatrix} 1 & -1 & 2 \\ 3 & 0 & -2 \\ 1 & 0 & 3 \end{bmatrix} \begin{bmatrix} 0 & 3 & 2 \\ -11 & 1 & 8 \\ 0 & -1 & 3 \end{bmatrix}$$
$$= \begin{bmatrix} 0+11+0 & 3-1-2 & 2-8+6 \\ 0+0+0 & 9+0+2 & 6+0-6 \\ 0+0+0 & 3+0-3 & 2+0+9 \end{bmatrix}$$
$$= \begin{bmatrix} 11 & 0 & 0 \\ 0 & 11 & 0 \\ 0 & 0 & 11 \end{bmatrix}$$

Also,

$$(adjA) \cdot A = \begin{bmatrix} 0 & 3 & 2 \\ -11 & 1 & 8 \\ 0 & -1 & 3 \end{bmatrix} \begin{bmatrix} 1 & -1 & 2 \\ 3 & 0 & -2 \\ 1 & 0 & 3 \end{bmatrix}$$

$$= \begin{bmatrix} 0+9+2 & 0+0+0 & 0-6+6 \\ -11+3+8 & 11+0+0 & -22-2+24 \\ 0-3+3 & 0+0+0 & 0+2+9 \end{bmatrix}$$

$$= \begin{bmatrix} 11 & 0 & 0 \\ 0 & 11 & 0 \\ 0 & 0 & 11 \end{bmatrix}$$

Hence, A(adjA) = (adjA)A = |A|I.

# Question 6:

Find the inverse of each of the matrices (if it exists).

$$\begin{bmatrix} -1 & 5 \\ -3 & 2 \end{bmatrix}$$

Answer

Let 
$$A = \begin{bmatrix} -1 & 5 \\ -3 & 2 \end{bmatrix}$$
.

we have,

$$|A| = -2 + 15 = 13$$

Now,

$$A_{11} = 2, A_{12} = 3, A_{21} = -5, A_{22} = -1$$

$$\therefore adjA = \begin{bmatrix} 2 & -5 \\ 3 & -1 \end{bmatrix}$$

$$\therefore A^{-1} = \frac{1}{|A|} adjA = \frac{1}{13} \begin{bmatrix} 2 & -5 \\ 3 & -1 \end{bmatrix}$$

### Question 7:

Find the inverse of each of the matrices (if it exists).

$$\begin{bmatrix} 1 & 2 & 3 \\ 0 & 2 & 4 \\ 0 & 0 & 5 \end{bmatrix}$$

Answer

$$Let A = \begin{bmatrix} 1 & 2 & 3 \\ 0 & 2 & 4 \\ 0 & 0 & 5 \end{bmatrix}$$

We have,

$$|A| = 1(10-0)-2(0-0)+3(0-0)=10$$

Now.

$$A_{11} = 10 - 0 = 10, A_{12} = -(0 - 0) = 0, A_{13} = 0 - 0 = 0$$

$$A_{21} = -(10 - 0) = -10, A_{22} = 5 - 0 = 5, A_{23} = -(0 - 0) = 0$$

$$A_{31} = 8 - 6 = 2, A_{32} = -(4 - 0) = -4, A_{33} = 2 - 0 = 2$$

$$\therefore adjA = \begin{bmatrix} 10 & -10 & 2 \\ 0 & 5 & -4 \\ 0 & 0 & 2 \end{bmatrix}$$
$$\therefore A^{-1} = \frac{1}{|A|}adjA = \frac{1}{10} \begin{bmatrix} 10 & -10 & 2 \\ 0 & 5 & -4 \\ 0 & 0 & 2 \end{bmatrix}$$

#### Question 8:

Find the inverse of each of the matrices (if it exists).

$$\begin{bmatrix} 1 & 0 & 0 \\ 3 & 3 & 0 \\ 5 & 2 & -1 \end{bmatrix}$$

Answer

$$Let A = \begin{bmatrix} 1 & 0 & 0 \\ 3 & 3 & 0 \\ 5 & 2 & -1 \end{bmatrix}$$

We have,

$$|A| = 1(-3-0)-0+0=-3$$

Now,

$$A_{11} = -3 - 0 = -3, A_{12} = -(-3 - 0) = 3, A_{13} = 6 - 15 = -9$$
  
 $A_{21} = -(0 - 0) = 0, A_{22} = -1 - 0 = -1, A_{23} = -(2 - 0) = -2$   
 $A_{31} = 0 - 0 = 0, A_{32} = -(0 - 0) = 0, A_{33} = 3 - 0 = 3$ 

$$\therefore adjA = \begin{bmatrix} -3 & 0 & 0 \\ 3 & -1 & 0 \\ -9 & -2 & 3 \end{bmatrix}$$
$$\therefore A^{-1} = \frac{1}{|A|}adjA = -\frac{1}{3}\begin{bmatrix} -3 & 0 & 0 \\ 3 & -1 & 0 \\ -9 & -2 & 3 \end{bmatrix}$$

# Question 9:

Find the inverse of each of the matrices (if it exists).

$$\begin{bmatrix} 2 & 1 & 3 \\ 4 & -1 & 0 \\ -7 & 2 & 1 \end{bmatrix}$$

Answer

$$Let A = \begin{bmatrix} 2 & 1 & 3 \\ 4 & -1 & 0 \\ -7 & 2 & 1 \end{bmatrix}.$$

We have,

$$|A| = 2(-1-0)-1(4-0)+3(8-7)$$

$$= 2(-1)-1(4)+3(1)$$

$$= -2-4+3$$

$$= -3$$

Now,

$$A_{11} = -1 - 0 = -1, A_{12} = -(4 - 0) = -4, A_{13} = 8 - 7 = 1$$

$$A_{21} = -(1 - 6) = 5, A_{22} = 2 + 21 = 23, A_{23} = -(4 + 7) = -11$$

$$A_{31} = 0 + 3 = 3, A_{32} = -(0 - 12) = 12, A_{33} = -2 - 4 = -6$$

$$\therefore adjA = \begin{bmatrix} -4 & 23 & 12 \\ 1 & -11 & -6 \end{bmatrix}$$
$$\therefore A^{-1} = \frac{1}{|A|} adjA = -\frac{1}{3} \begin{bmatrix} -1 & 5 & 3 \\ -4 & 23 & 12 \\ 1 & -11 & -6 \end{bmatrix}$$

Question 10:

Find the inverse of each of the matrices (if it exists).

$$\begin{bmatrix} 1 & -1 & 2 \\ 0 & 2 & -3 \\ 3 & -2 & 4 \end{bmatrix}$$

Answer

$$Let A = \begin{bmatrix} 1 & -1 & 2 \\ 0 & 2 & -3 \\ 3 & -2 & 4 \end{bmatrix}.$$

By expanding along C1, we have:

$$|A| = 1(8-6)-0+3(3-4)=2-3=-1$$

Now,

$$A_{11} = 8 - 6 = 2, A_{12} = -(0+9) = -9, A_{13} = 0 - 6 = -6$$

$$A_{21} = -(-4+4) = 0, A_{22} = 4-6 = -2, A_{23} = -(-2+3) = -1$$
  
 $A_{31} = 3-4 = -1, A_{32} = -(-3-0) = 3, A_{33} = 2-0 = 2$ 

\*\*\*\*\*\*\*\*\* END \*\*\*\*\*\*\*\*