

Exercise 5A

Q1

Answer:

(i)
$$\frac{5}{7} \times \frac{5}{7} \times \frac{5}{7} \times \frac{5}{7} = \left(\frac{5}{7}\right)^4$$

$$\text{(ii)} \left(\frac{-4}{3} \right) \times \left(\frac{-4}{3} \right) \times \left(\frac{-4}{3} \right) \times \left(\frac{-4}{3} \right) \times \left(\frac{-4}{3} \right) = \left(\frac{-4}{3} \right)^5$$

$$\text{(iii) } \left(\frac{-1}{6} \right) \times \left(\frac{-1}{6} \right) \times \left(\frac{-1}{6} \right) = \left(\frac{-1}{6} \right)^3$$

(iv)
$$(-8) \times (-8) \times (-8) \times (-8) \times (-8) = (-8)^5$$

Q2

Answer:

(i)
$$\frac{25}{36} = \frac{5^2}{6^2}$$
 [since 25 = 5² and 36 = 6²]
$$= \left(\frac{5}{6}\right)^2$$

(ii)
$$\frac{-27}{64} = \frac{\left(-3\right)^3}{4^3}$$
 [since $-27 = (-3)^3$ and $64 = 4^3$]
$$= \left(\frac{-3}{4}\right)^3$$

(iii)
$$\frac{-32}{243} = \frac{\left(-2\right)^5}{3^5}$$
 [since $-32 = (-2)^5$ and $243 = 3^5$]
$$= \left(\frac{-2}{3}\right)^5$$

(iv)
$$\frac{-1}{128} = \frac{\left(-1\right)^7}{2^7}$$
 [since $(-1)^7 = -1$ and $128 = 2^7$]
$$= \left(\frac{-1}{2}\right)^7$$

Answer :

(i)
$$\left(\frac{2}{3}\right)^5 = \frac{(2)^5}{(3)^5} = \frac{2 \times 2 \times 2 \times 2 \times 2}{3 \times 3 \times 3 \times 3 \times 3} = \frac{32}{243}$$

(ii)
$$\left(\frac{-8}{5}\right)^3 = \frac{\left(-8\right)^3}{\left(5\right)^3} = \frac{\left(-8\right) \times \left(-8\right) \times \left(-8\right)}{5 \times 5 \times 5} = \frac{-512}{125}$$

(iii)
$$\left(\frac{-13}{11}\right)^2 = \frac{\left(-13\right)^2}{\left(11\right)^2} = \frac{\left(-13\right) \times \left(-13\right)}{11 \times 11} = \frac{169}{121}$$

(iv)
$$\left(\frac{1}{6}\right)^3 = \frac{\left(1\right)^3}{\left(6\right)^3} = \frac{1 \times 1 \times 1}{6 \times 6 \times 6} = \frac{1}{216}$$

$$\text{(V)} \left(\frac{-1}{2} \right)^5 = \frac{\left(-1 \right)^5}{\left(2 \right)^5} = \frac{\left(-1 \right) \times \left(-1 \right) \times \left(-1 \right) \times \left(-1 \right) \times \left(-1 \right)}{2 \times 2 \times 2 \times 2 \times 2} = \frac{-1}{32}$$

$$\text{(vi) } \left(\frac{-3}{2}\right)^4 = \frac{\left(-3\right)^4}{\left(2\right)^4} = \frac{\left(-3\right) \times \left(-3\right) \times \left(-3\right) \times \left(-3\right)}{2 \times 2 \times 2 \times 2} = \frac{81}{16}$$

$$\text{(Vii)} \left(\frac{-4}{7} \right)^3 = \frac{\left(-4 \right)^3}{\left(7 \right)^3} = \frac{\left(-4 \right) \times \left(-4 \right) \times \left(-4 \right)}{7 \times 7 \times 7} = \frac{-64}{343}$$

(VIII)
$$\left(-1\right)^9 = -1$$
 [Since (-1) an odd natural number = -1]

Q4

Answer:

(i)
$$(4)^{-1}=\left(\frac{4}{1}\right)^{-1}=\left(\frac{1}{4}\right)^1=\frac{1}{4}$$
 [since $\left(\frac{a}{b}\right)^{-n}=\left(\frac{b}{a}\right)^n$]

$$(\mathrm{ii}) \left(-6\right)^{-1} = \left(\frac{-6}{1}\right)^{-1} = \left(\frac{1}{-6}\right)^1 = \frac{-1}{6} \qquad \qquad [\mathrm{since} \left(\frac{a}{b}\right)^{-n} = \left(\frac{b}{a}\right)^n]$$

$$(\mathrm{iii}) \left(\frac{1}{3}\right)^{-1} = \left(\frac{3}{1}\right)^1 = \frac{3}{1} \qquad \qquad [\mathrm{since} \left(\frac{a}{b}\right)^{-n} = \left(\frac{b}{a}\right)^n]$$

(iv)
$$\left(\frac{-2}{3}\right)^{-1} = \left(\frac{3}{-2}\right)^1 = \frac{-3}{2}$$
 [since $\left(\frac{a}{b}\right)^{-n} = \left(\frac{b}{a}\right)^n$]

Q5

Answer:

We know that the reciprocal of $\left(\frac{a}{b}\right)^m$ is $\left(\frac{b}{a}\right)^m$.

(i) Reciprocal of
$$\left(\frac{3}{8}\right)^4 = \left(\frac{8}{3}\right)^4$$

(ii) Reciprocal of
$$\left(\frac{-5}{6}\right)^{11}=\left(\frac{-6}{5}\right)^{11}$$

(iii) Reciprocal of
$$6^7$$
 = Reciprocal of $\left(\frac{6}{1}\right)^7$ = $\left(\frac{1}{6}\right)^7$

(iv) Reciprocal of
$$(-4)^3$$
 = Reciprocal of $\left(\frac{-4}{1}\right)^3 = \left(\frac{-1}{4}\right)^3$

Answer:

(i)
$$8^0 = 1$$

(ii)
$$(-3)^0 = 1$$

(iii)
$$4^0 + 5^0 = 1 + 1 = 2$$

(iv)
$$6^0 \times 7^0 = 1 \times 1 = 1$$

Note: a0 = 1

Q7

Answer:

(i)
$$\left(\frac{3}{2}\right)^4 \times \left(\frac{1}{5}\right)^2 = \frac{3^4}{2^4} \times \frac{1^2}{5^2} = \frac{81 \times 1}{16 \times 25} = \frac{81}{400}$$

(ii)
$$\left(\frac{-2}{3}\right)^5 \times \left(\frac{-3}{7}\right)^3 = \frac{\left(-2\right)^5}{\left(3\right)^5} \times \frac{\left(-3\right)^3}{\left(7\right)^3}$$

$$= \frac{\left(-2\right)^5}{\left(7\right)^3} \times \frac{\left(-1\right)\left(3\right)^3}{\left(3\right)^5}$$

$$= \frac{-32 \times -1 \times 3^{3-5}}{343}$$

$$= \frac{-32 \times -1 \times 3^{-2}}{343}$$

$$= \frac{-32 \times -1 \times 1}{343 \times 9}$$

$$= \frac{32}{3087}$$

$$\begin{array}{l} \text{(iii)} \left(\frac{-1}{2}\right)^5 \times 2^3 \times \left(\frac{3}{4}\right)^2 = \frac{\left(-1\right)^5}{2^5} \times 2^3 \times \frac{3^2}{4^2} \\ = \frac{\left(-1\right)^5}{2^5} \times 2^3 \times \frac{3^2}{\left(2^2\right)^2} \\ = \frac{-1 \times 2^3 \times 3^2}{2^5 \times 2^4} \\ = \frac{-1 \times 2^3 \times 3^2}{2^9} = -1 \times 2^{3-9} \times 3^2 = -9 \times 2^{-6} = \frac{-9}{2^6} = \frac{-9}{64} \\ \left[s \operatorname{ince} \left(\frac{a}{b}\right)^{-1} = \left(\frac{b}{a}\right)^1\right] \end{array}$$

$$\begin{array}{l} \text{(iv)} \left(\frac{2}{3}\right)^2 \times \left(\frac{-3}{5}\right)^3 \times \left(\frac{7}{2}\right)^2 = \frac{2^2}{3^2} \times \frac{\left(-3\right)^3}{5^3} \times \frac{7^2}{2^2} \\ \frac{-1 \times 3^{3-2} \times 7^2}{5^3} = \frac{-1 \times 3^1 \times 7^2}{5^3} = \frac{-1 \times 3 \times 49}{125} = \frac{-147}{125} \end{array}$$

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