

Some Applications of Trigonometry Ex 12.1 Q10

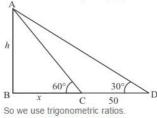
Answer:

Let AB be the tower of height h. And person makes an angle of elevation of top of tower is 30°, he walks $50\,\text{m}$ towards the foot of tower then makes an angle of elevation 60°

Let
$$BC = x$$
, $CD = 50$, and $\angle ACB = 60^{\circ}$, $\angle ADB = 30^{\circ}$

Now we have to find height of tower.

We have the corresponding figure as follows



In a triangle ABC,

$$\Rightarrow \tan C = \frac{AB}{BC}$$

$$\Rightarrow \tan 60^\circ = \frac{h}{x}$$

$$\Rightarrow \sqrt{3} = \frac{h}{x}$$

$$\Rightarrow$$
 $x = \frac{h}{\sqrt{3}}$

Again in a triangle ADB,

$$\Rightarrow \tan D = \frac{AB}{BC + CD}$$

$$\Rightarrow$$
 $\tan 30^\circ = \frac{h}{x+50}$

$$\Rightarrow \frac{1}{\sqrt{3}} = \frac{h}{x + 50}$$

$$\Rightarrow \sqrt{3}h = x + 50$$

$$\Rightarrow \sqrt{3}h = \frac{h}{\sqrt{3}} + 50$$

$$\Rightarrow 3h = h + 50\sqrt{3}$$

$$\Rightarrow 2h = 50\sqrt{3}$$

$$\Rightarrow h = 25\sqrt{3}$$

$$\Rightarrow h = 25 \times 1.73$$

$$\Rightarrow h = 43.25$$

Hence the height of tower is 43.25 m

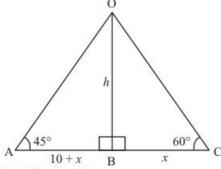
Some Applications of Trigonometry Ex 12.1 Q11

Answer:

Let h be height of tower AB and angle of elevation are 45° and 60° are given. In a triangle OAC, given that AB = 10+x and BC = x

Now we have to find height of tower.

So we use trigonometrical ratios.



In a triangle OAB,

$$\Rightarrow$$
 $\tan A = \frac{OB}{AB}$

$$\Rightarrow \tan 45^{\circ} = \frac{OB}{AB}$$

$$\Rightarrow 1 = \frac{h}{10 + x}$$

$$\Rightarrow h = 10 + x$$

Therefore x = h - 10Again in a triangle OCB,

Again in a triangle
$$OCB$$
,
$$\Rightarrow \tan C = \frac{OB}{BC}$$

$$\Rightarrow \tan 60^{\circ} = \frac{OB}{BC}$$

$$\Rightarrow \int 3 = \frac{h}{x}$$

$$\Rightarrow h = \sqrt{3}x$$
Put $x = h - 10$

$$\Rightarrow h = \sqrt{3}(h - 10)$$

$$\Rightarrow h = \sqrt{3}h - 10\sqrt{3}$$

$$\Rightarrow 10\sqrt{3} = h(\sqrt{3} - 1)$$

$$\Rightarrow h = \frac{10\sqrt{3}}{(\sqrt{3} - 1)}$$

$$\Rightarrow h = \frac{10 \times 1.732}{(1.732 - 1)}$$

$$\Rightarrow h = \frac{17.32}{0.372}$$

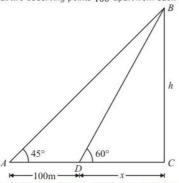
Hence height of tower is 23.66 m.

h = 23.66

Some Applications of Trigonometry Ex 12.1 Q12

Answer:

Let BC be the height h of the parachutist and makes an angle of elevations 45° and 60° respectively at two observing points 100 apart from each other.



Let AD=100 , CD = x , BC = h and \angle CAB = 45° , \angle CDB = 60°

So we use trigonometric ratios.

In triangle BCD

$$\tan 60^\circ = \frac{h}{x}$$

Now in triangle ABC ,

Now in triangle
$$ABC$$
.
 $\tan 45^\circ = \frac{h}{x+100}$

$$\Rightarrow 1 = \frac{h}{x+100}$$

$$\Rightarrow x+100 = h$$

$$\Rightarrow h+100\sqrt{3} = \sqrt{3}h$$

$$\Rightarrow h = \frac{100\sqrt{3}}{\sqrt{3}-1}$$

$$\Rightarrow h = 50(3+\sqrt{3})$$

$$\Rightarrow x = \frac{h}{\sqrt{3}}$$

$$x = \frac{50(3+\sqrt{3})}{\sqrt{3}}$$

 $=50\left(1+\sqrt{3}\right)$

Hence the maximum height is $50(3+\sqrt{3})$ m = 236.6 m. and distance is $50(1+\sqrt{3})$ m = 136.6 m.

********* END *******