

Arithematic Progressions Ex 19.4 Q27

Let the number of terms is n.

Now the sum of the series is:

$$1+3+5+\cdots+2001$$

Here l = 2001 and d = 2.

Therefore

$$l = a + (n-1)d$$

$$2001 = 1 + (n-1) \cdot 2$$

$$2(n-1) = 2000$$

$$n-1=1000$$

$$n = 1001$$

Therefore the sum of the series is:

$$S = \frac{1001}{2} \left[2 + (1001 - 1)2 \right]$$

$$=1001^{2}$$

$$=1002001$$

Arithematic Progressions Ex 19.4 Q28

Let the number of terms to be added to the series is n.

Now a = -6 and d = 0.5.

Therefore

$$-25 = \frac{n}{2} \left[2(-6) + (n-1)(0.5) \right]$$

$$-50 = n[-12 + 0.5n - 0.5]$$

$$-12.5n + 0.5n^2 + 50 = 0$$

$$n^2 - 25n + 100 = 0$$

$$n = 20,5$$

Therefore the value of n will be either 20 or 5.

Arithematic Progressions Ex 19.4 Q29

Here the first term a = 2. Let the common difference is d. Now

$$\frac{5}{2} \left[2a + (5-1)d \right] = \frac{1}{4} \left[\frac{5}{2} \left[2(a+5d) + (5-1)d \right] \right]$$

$$\frac{5}{2} \left[2 \cdot 2 + 4d \right] = \frac{5}{8} \left[2 \cdot 2 + 14d \right]$$

$$10 + 10d = \frac{5}{2} + \frac{35}{4}d$$

$$\frac{5}{4}d = -7.5$$

$$d = -6$$

The 20th term will be:

$$a+(n-1)d = 2+(20-1)(-6)$$

= -112

Hence it is shown.

Arithematic Progressions Ex 19.4 Q30

$$\begin{split} S_{(2n+1)} &= S_1 = \frac{(2n+1)}{2} \big[2a + (2n+1-1)d \big] \\ S_1 &= \frac{(2n+1)}{2} \big[2a + 2nd \big] \\ &= (2n+1) (a+nd) \end{split} \qquad \qquad --- (i) \end{split}$$

Sum of odd terms = S_2

$$\begin{split} S_2 &= \frac{(n+1)}{2} \Big[2a + (n+1-1)(2d) \Big] \\ &= \frac{(n+1)}{2} \Big[2a + 2nd \Big] \\ S_2 &= (n+1)(a+nd) \end{split} \qquad --- (ii) \end{split}$$

From equation (i) and (ii),

$$S_1: S_2 = (2n+1)(a+nd): (n+1)(a+nd)$$

 $S_1: S_2 = (2n+1); (n+1)$

********** END *******