

NCERT Solutions for Class 10 Maths Chapter 11 Constructions Exercise 11.1

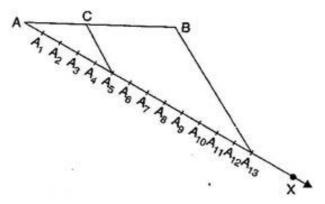
In each of the following, give the justification of the construction also:

Q1. Draw a line segment of length 7.6 cm and divide it in the ratio 5: 8. Measure the two parts.

Ans: Given: A line segment of length 7.6 cm.

To construct: To divide it in the ration 5: 8 and to measure the two parts.

Steps of construction:



- (a) From any ray AX, making an acute angle with AB.
- (b) Locate 13 (=5 + 8) points

 A_1 , A_2 , A_3 , A_4 , A_5 , A_6 , A_7 , A_8 , A_9 , A_{10} , A_{11} , A_{12} and A_{13} on AX such that

$$AA_1 = A_1A_2 = A_2A_3 = A_3A_4 = A_4A_5 = A_5A_6 = A_5A_7 = A_7A_8 = A_8A_9 = A_9A_{10} = A_{10}A_{11} = A_{11}A_{12} = A_{12}A_{13} = A_{13}A_{13} = A_{$$

- (c) Join BA_{13} .
- (d) Through the point A_5 , draw a line parallel to

 $A_{13}B$ intersecting AB at the point C.

Then,
$$AC:CB=5:8$$

On measurement, AC = 3.1 cm, CB = 4.5 cm

Justification:

 $A_5C \parallel A_{13}B$ [By construction]

$$\frac{AA_5}{A_5A_{13}} = \frac{AC}{CB}$$

[By Basic Proportionality Theorem]

But
$$\frac{AA_5}{A_5A_{13}} = \frac{5}{8}$$
 [By construction]

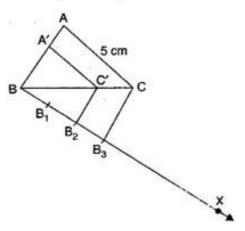
Therefore,
$$\frac{AC}{CB} = \frac{5}{8}$$

$$\Rightarrow$$
 AC: CB = 5:8

Q2. Construct a triangle of sides 4 cm, 5 cm and 6 cm

and then a triangle similar to it whose sides are $\frac{2}{3}$ of the corresponding sides of the first triangle.

Ans: To construct: To construct a triangle of sides 4 cm, 5 cm and 6 cm and then a triangle similar to it whose sides are $\frac{2}{3}$ of the corresponding sides of the first triangle.



Steps of construction:

- (a) Draw a triangle ABC of sides 4 cm, 5 cm and 6 cm.
- (b) From any ray BX, making an acute angle with BC on the side opposite to the vertex A.
- (c) Locate 3 points B_1 , B_2 and B_3 on BX such that
- (d) Join B_3C and draw a line through the point B_2 , draw a line parallel to B_3C intersecting BC at the point C'.
- (e) Draw a line through C' parallel to the line CA to intersect BA at A'.

Then, A'BC' is the required triangle.

Justification:

 $B_3C \parallel B_2C'$ [By construction]

$$\frac{BB_2}{B_2B_3} = \frac{BC'}{C'C}$$

[By Basic Proportionality Theorem]

But
$$\frac{BB_2}{B_2B_3} = \frac{2}{1}$$
 [By construction]

Therefore,
$$\frac{BC'}{C'C} = \frac{2}{1}$$

$$\Rightarrow \frac{C'C}{BC'} = \frac{1}{2}$$

$$\Rightarrow \frac{C'C}{BC'} + 1 = \frac{1}{2} + 1$$

$$\Rightarrow \frac{C'C + BC'}{BC'} = \frac{1+2}{2}$$

$$\Rightarrow \frac{BC}{BC'} = \frac{3}{2}$$

$$\Rightarrow \frac{BC'}{BC} = \frac{2}{3}$$
(i)

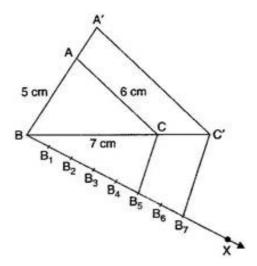
∵ CA || C'A' [By construction]

$$\triangle$$
 BC'A' $\sim \Delta$ BCA [AA similarity]

$$\frac{AB'}{AB} = \frac{A'C'}{AC} = \frac{BC'}{BC} = \frac{2}{3} \text{ [From eq. (i)]}$$

Q3. Construct a triangle with sides 6 cm, 6 cm and 7 cm and then another triangle whose sides are $\frac{7}{5}$ of the corresponding sides of the first triangle.

Ans: To construct: To construct a triangle of sides 5 cm, 6 cm and 7 cm and then a triangle similar to it whose sides are $\frac{7}{5}$ of the corresponding sides of the first triangle. Steps of construction:



- (a) Draw a triangle ABC of sides 5 cm, 6 cm and 7 cm.
- (b) From any ray BX, making an acute angle with BC on the side opposite to the vertex A.
- (c) Locate 7 points B_1 , B_2 , B_3 , B_4 , B_5 , B_6 and B_7 on BX such that

$$BB_1 = B_1B_2 = B_2B_3 = B_3B_4 = B_4B_5 = B_5B_6 = B_6B_7$$

- (d) Join B_5C and draw a line through the point B_7 , draw a line parallel to B_5C intersecting BC at the point C'.
- (e) Draw a line through C' parallel to the line CA to intersect BA at A'.

Then, A'BC' is the required triangle.

Justification:

∵ C'A' || CA [By construction]

$$\therefore \frac{A'B}{AB} = \frac{A'C'}{AC} = \frac{BC'}{BC}$$

[By Basic Proportionality Theorem]

$$\therefore B_7C^* \parallel B_5C$$
 [By construction]

$$\triangle BB_7C^\circ \sim \Delta BB_5C$$
 [AA similarity]

But
$$\frac{BB_5}{BB_7} = \frac{5}{7}$$
 [By construction]

Therefore,
$$\frac{BC}{BC'} = \frac{5}{7}$$

$$\Rightarrow \frac{BC'}{BC} = \frac{7}{5}$$

$$\therefore \frac{A'B}{AB} = \frac{A'C'}{AC} = \frac{BC'}{BC} = \frac{7}{5}$$

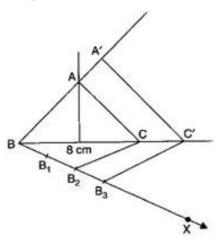
Q4. Construct an isosceles triangle whose base is 8 cm and altitude 4 cm and then another

triangle whose sides are $1\frac{1}{2}$ times the corresponding sides of the isosceles triangle.

triangle whose base is 8 cm and altitude 4 cm and then a triangle similar to it whose sides are $1\frac{1}{2}\left(\text{or }\frac{3}{2}\right)$ of the corresponding sides of the first triangle.

Ans: To construct: To construct an isosceles

Steps of construction:



- (a) Draw BC = 8 cm
- (b) Draw perpendicular bisector of BC. Let it meets BC at D.
- (c) Mark a point A on the perpendicular bisector such that AD = 4 cm.
- (d) Join AB and AC. Thus \triangle ABC is the required isosceles triangle.
- (e) From any ray BX, making an acute angle with BC on the side opposite to the vertex A.

- (f) Locate 3 points B_1 , B_2 and B_3 on BX such that $BB_1 = B_1B_2 = B_2B_3$.
- (g) Join B_2C and draw a line through the point B_3 , draw a line parallel to B_2C intersecting BC at the point C.
- (h) Draw a line through C' parallel to the line CA to intersect BA at A'.

Then, A'BC' is the required triangle.

Justification:

- ∵ C'A' || CA [By construction]
- ∴ △ ABC~ △ A'BC' [AA similarity]

$$\frac{A'B}{AB} = \frac{A'C'}{AC} = \frac{BC'}{BC}$$

[By Basic Proportionality Theorem]

- $B_3C' \parallel B_2C' \parallel B_2C' \parallel By construction$
- $\triangle BB_3C^* \sim \Delta BB_2C$ [AA similarity]

But
$$\frac{BB_3}{BB_2} = \frac{3}{2}$$
 [By construction]

Therefore,

$$\Rightarrow \frac{BC'}{BC} = \frac{3}{2}$$

$$\therefore \frac{A'B}{AB} = \frac{A'C'}{AC} = \frac{BC'}{BC} = \frac{3}{2}$$

Q5. Draw a triangle ABC with side BC = 6 cm, AB = 5 cm and \angle ABC = 60°. Then construct a triangle whose sides are $\frac{3}{4}$ of the corresponding sides of triangle ABC.

Ans: To construct: To construct a triangle ABC with side BC = 6 cm, AB = 5 cm and \angle ABC = 60° and then a triangle similar to it whose sides are $\frac{3}{4}$ of the corresponding sides of the first triangle ABC.

Steps of construction:

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