

## Transformation Formulae Ex 8.2 Q9(i)

We have,

LHS 
$$= \sin \alpha + \sin \beta + \sin \gamma - \sin (\alpha + \beta + \gamma)$$

$$= (\sin \alpha + \sin \beta) + (\sin \gamma - \sin (\alpha + \beta + \gamma))$$

$$= 2 \sin \left(\frac{\alpha + \beta}{2}\right) \cos \left(\frac{\alpha - \beta}{2}\right) + 2 \sin \left(\frac{\gamma - (\alpha + \beta + \gamma)}{2}\right) \cos \left(\frac{\gamma + \alpha + \beta + \gamma}{2}\right)$$

$$= 2 \sin \left(\frac{\alpha + \beta}{2}\right) \cos \left(\frac{\alpha - \beta}{2}\right) + 2 \sin \left(\frac{-\alpha - \beta}{2}\right) \cos \left(\frac{\alpha + \beta + 2\gamma}{2}\right)$$

$$= 2 \sin \left(\frac{\alpha + \beta}{2}\right) \cos \left(\frac{\alpha - \beta}{2}\right) - 2 \sin \left(\frac{\alpha + \beta}{2}\right) \cos \left(\frac{\alpha + \beta + 2\gamma}{2}\right)$$

$$= 2 \sin \left(\frac{\alpha + \beta}{2}\right) \left[\cos \left(\frac{\alpha - \beta}{2}\right) - \cos \left(\frac{\alpha + \beta + 2\gamma}{2}\right)\right]$$

$$= 2 \sin \left(\frac{\alpha + \beta}{2}\right) \left[-2 \sin \left(\frac{\alpha - \beta}{2}\right) - \cos \left(\frac{\alpha + \beta + 2\gamma}{2}\right)\right]$$

$$= 2 \sin \left(\frac{\alpha + \beta}{2}\right) \left[-2 \sin \left(\frac{\alpha - \beta}{2}\right) + \frac{\alpha + \beta + 2\gamma}{2}\right]$$

$$= -4 \sin \left(\frac{\alpha + \beta}{2}\right) \left[\sin \left(\frac{\alpha + \gamma}{2}\right) \sin \left(\frac{-2\beta - 2\gamma}{2}\right)\right]$$

$$= 4 \sin \left(\frac{\alpha + \beta}{2}\right) \sin \left(\frac{\alpha + \gamma}{2}\right) \sin \left(\frac{\beta + \gamma}{2}\right)$$

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$$= 2 \sin \left(\frac{\alpha + \beta}{2}\right) \sin \left(\frac{\beta + \gamma}{2}\right) \sin \left(\frac{\alpha + \gamma}{2}\right)$$

$$: \quad \sin\alpha + \sin\beta + \sin\gamma - \sin\left(\alpha + \beta + \gamma\right) = 4\sin\left(\frac{\alpha + \beta}{2}\right)\sin\left(\frac{\beta + \gamma}{2}\right)\sin\left(\frac{\alpha + \gamma}{2}\right) \quad \text{Hence proved.}$$

## Transformation Formulae Ex 8.2 Q9(ii)

Ve have,

LHS = 
$$\cos (A + B + C) + \cos (A - B + C) + \cos (A + B - C) + \cos (-A + B + C)$$
  
=  $\left[\cos (A + B + C) + \cos (A - B + C)\right] + \left[\cos (A + B - C) + \cos (-A + B + C)\right]$   
=  $2\cos \left\{\frac{A + B + C + A - B + C}{2}\right\}\cos \left\{\frac{A + B + C - A + B - C}{2}\right\} + 2\left\{\frac{\cos \left\{\frac{A + B - C - A + B + C}{2}\right\}}{\cos \left\{\frac{A + B - C + A - B - C}{2}\right\}}\right\}$   
=  $2\cos \left\{\frac{2A + 2C}{2}\right\}\cos \left\{\frac{2B}{2}\right\} + 2\cos \left\{\frac{2B}{2}\right\}\cos \left\{\frac{2A - 2C}{2}\right\}$   
=  $2\cos (A + C)\cos (B) + 2\cos (B)\cos (A - C)$   
=  $2\cos (B)\left[\cos (A + C) + \cos (A - C)\right]$   
=  $2\cos (B)\left[\cos (A + C) + \cos (A - C)\right]$   
=  $2\cos (B)\left[2\cos A\cos C\right]$   
=  $4\cos A\cos B\cos C$ .

Transformation Formulae Ex 8.2 Q10

We have,

$$\cos A + \cos B = \frac{1}{2}$$
and,  $\sin A + \sin B = \frac{1}{4}$ 
Now,
$$\frac{\sin A + \sin B}{\cos A + \cos B} = \frac{\frac{1}{4}}{\frac{1}{2}}$$

$$\Rightarrow \frac{2 \sin \left(\frac{A + B}{2}\right) \cos \left(\frac{A - B}{2}\right)}{2 \cos \left(\frac{A + B}{2}\right) \cos \left(\frac{A - B}{2}\right)} = \frac{1}{2}$$

$$\Rightarrow \frac{\sin \left(\frac{A + B}{2}\right)}{\cos \left(\frac{A + B}{2}\right)} = \frac{1}{2}$$

Hence proved.

## Transformation Formulae Ex 8.2 Q 11.

 $\Rightarrow \qquad \tan A \tan B = \cot \left( \frac{A+B}{2} \right) \qquad \text{Hence proved.}$ 

We have,

$$cos ecA + sec A = cos ecB + sec B$$

$$cos ecA - sec B = cos ecB - cos ecA$$

$$\frac{1}{\cos A} - \frac{1}{\cos B} = \frac{1}{\sin B} - \frac{1}{\sin A}$$

$$\frac{cos B - cos A}{\cos A \cos B} = \frac{\sin A - \sin B}{\sin A \sin B}$$

$$\frac{\sin A \sin B}{\cos A \cos B} = \frac{\sin A - \sin B}{\cos B - \cos A}$$

$$\frac{\sin A \sin B}{\cos B} = \frac{2 \sin (A - B)}{2} \cos (\frac{A + B}{2})$$

$$\frac{1}{\cos A \cos B} = \frac{2 \sin (\frac{A - B}{2}) \cos (\frac{A + B}{2})}{-2 \sin (\frac{B - A}{2}) \sin (\frac{B + A}{2})}$$

$$\frac{1}{\sin A \cos B} = \frac{-\sin (\frac{A - B}{2}) \cos (\frac{A + B}{2})}{-\sin (\frac{A - B}{2}) \sin (\frac{A + B}{2})}$$

$$\frac{1}{\sin A \cos B} = \frac{-\sin (\frac{A - B}{2}) \cos (\frac{A + B}{2})}{-\sin (\frac{A - B}{2}) \sin (\frac{A + B}{2})}$$

$$\frac{1}{\sin A \cos B} = \frac{-\sin (\frac{A - B}{2}) \cos (\frac{A + B}{2})}{-\sin (\frac{A - B}{2}) \sin (\frac{A + B}{2})}$$

$$\frac{1}{\sin A \cos B} = \frac{-\sin (\frac{A - B}{2}) \cos (\frac{A + B}{2})}{-\sin (\frac{A - B}{2}) \sin (\frac{A + B}{2})}$$

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