



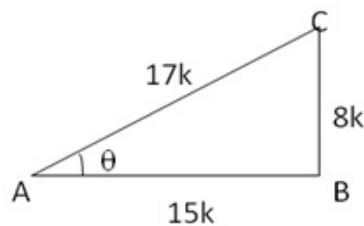
Question 6

Given: $\cot\theta = \frac{AB}{BC} = \frac{15}{8}$

Let $AB = 15k$ and $BC = 8k$,

Where k is positive

Let us draw a $\triangle ABC$ in which $\angle B = 90^\circ$ and $\angle BAC = \theta$



By Pythagoras theorem, we have

$$AC^2 = AB^2 + BC^2$$

$$= (15k)^2 + (8k)^2$$

$$= 225k^2 + 64k^2$$

$$= 289k^2$$

$$AC = 17k$$

$$\sin\theta = \frac{BC}{AC} = \frac{8k}{17k} = \frac{8}{17}, \quad \cos\theta = \frac{AB}{AC} = \frac{15k}{17k} = \frac{15}{17}$$

$$\begin{aligned} \therefore \frac{(2 + 2\sin\theta)(1 - \sin\theta)}{(1 + \cos\theta)(2 - 2\cos\theta)} &= \frac{\left(2 + 2 \times \frac{8}{17}\right)\left(1 - \frac{8}{17}\right)}{\left(1 + \frac{15}{17}\right)\left(2 - 2 \times \frac{15}{17}\right)} \\ &= \frac{\frac{50}{17} \times \frac{9}{17}}{\frac{32}{17} \times \frac{4}{17}} = \frac{50 \times 9}{32 \times 4} = \frac{25 \times 9}{32 \times 2} = \frac{225}{64} \end{aligned}$$

***** END *****