

Definite Integrals Ex 20.1 Q59

We have,

$$\int_{0}^{k} \frac{dx}{2 + 8x^2} = \frac{\pi}{16}$$

$$\Rightarrow \frac{1}{8} \int_{0}^{k} \frac{dx}{\left(\frac{1}{2}\right)^{2} + x^{2}} = \frac{\pi}{16}$$

$$\Rightarrow \frac{1}{8} \left[ 2 \tan^{-1} 2x \right]_0^k = \frac{\pi}{16} \qquad \left[ \because \int \frac{dx}{a^2 - x^2} = 2 \tan^{-1} \frac{x}{a} \right]$$

$$\Rightarrow \frac{1}{4} \left[ \tan^{-1} 2k - \tan^{-1} 0 \right] = \frac{\pi}{16}$$

$$\Rightarrow \tan^{-1} 2k - 0 = \frac{\pi}{4}$$

$$\Rightarrow \tan^{-1} 2k = \frac{\pi}{4}$$

$$\Rightarrow 2k = 1$$

$$k = \frac{1}{2}$$

Definite Integrals Ex 20.1 Q60

We have,

$$\int_{0}^{3} 3x^{2} dx = 8$$

$$\Rightarrow \left[\chi^3\right]_0^{\flat} = 8$$

$$\Rightarrow a^3 = 8$$

$$\Rightarrow a = 2$$

Definite Integrals Ex 20.1 Q61

$$\int_{\Pi}^{\frac{3\pi}{2}} \sqrt{1 - (1 - 2\sin^2 x)} dx$$

$$\int_{\Pi}^{\frac{3\pi}{2}} \sqrt{2\sin^2 x} dx$$

$$\sqrt{2} \int_{\Pi}^{\frac{3\pi}{2}} \sin x dx$$

$$\sqrt{2} (-\cos x)_{\Pi}^{\frac{3\pi}{2}}$$

$$= \sqrt{2}$$

Definite Integrals Ex 20.1 Q62

$$I = \int_{0}^{2\pi} \sqrt{1 + \sin \frac{x}{2}} dx$$

$$\Rightarrow I = \int_{0}^{2\pi} \sqrt{\sin^{2} \frac{x}{4} + \cos^{2} \frac{x}{4} + 2\sin \frac{x}{4} \cos \frac{x}{4}} dx$$

$$\Rightarrow I = \int_{0}^{2\pi} \sqrt{\left(\sin \frac{x}{4} + \cos \frac{x}{4}\right)^{2}} dx$$

$$\Rightarrow I = \int_{0}^{2\pi} \left(\sin \frac{x}{4} + \cos \frac{x}{4}\right) dx$$

$$\Rightarrow I = \left[\frac{-\cos \frac{x}{4}}{\frac{1}{4}} + \frac{\sin \frac{x}{4}}{\frac{1}{4}}\right]_{0}^{2\pi}$$

$$\Rightarrow I = 4(0 + 1 + 1 - 0)$$

$$\Rightarrow I = 8$$

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