



Tangents and Normals Ex 16.1 Q16

The given equations of curve and the line are

$$y = x^2 - 4x + 5 \quad \text{---(i)}$$

$$2y + x = 7 \quad \text{---(ii)}$$

Slope of the tangent to (i) is

$$m_1 = \frac{dy}{dx} = 2x - 4 \quad \text{---(iii)}$$

Slope of the line (ii) is

$$m_2 = \frac{dy}{dx} = \frac{-1}{2} \quad \text{---(iv)}$$

We have given that slope of (i) and (ii) are perpendicular to each other.

$$\therefore m_1 \times m_2 = -1$$

$$\Rightarrow (2x - 4) \left(\frac{-1}{2} \right) = -1$$

$$\Rightarrow -2x + 4 = -2$$

$$\Rightarrow x = 3$$

From (i)

$$y = 2$$

Thus, the required point is $(3, 2)$.

Tangents and Normals Ex 16.1 Q17

Differentiating $\frac{x^2}{4} + \frac{y^2}{25} = 1$ with respect to x , we get

$$\frac{x}{2} + \frac{2y}{25} \cdot \frac{dy}{dx} = 0$$

$$\text{or } \frac{dy}{dx} = \frac{-25}{4} \cdot \frac{x}{y}$$

(i) Now, the tangent is parallel to the x - axis if the slope of the tangent is zero.

$$\therefore \frac{-25}{4} \cdot \frac{x}{y} = 0$$

This is possible if $x = 0$.

$$\text{Then } \frac{x^2}{4} + \frac{y^2}{25} = 1 \text{ for } x = 0 \text{ gives } y^2 = 25$$

$$\therefore y = \pm 5$$

Thus, the points at which the tangents are parallel to the x - axis are $(0, 5)$ and $(0, -5)$.

(ii) Now, the tangent is parallel to the y - axis if the slope of the normal is zero.

$$\therefore \frac{4y}{25x} = 0$$

This is possible if $y = 0$.

$$\text{Then } \frac{x^2}{4} + \frac{y^2}{25} = 1 \text{ for } y = 0 \text{ gives } x^2 = 4$$

$$\therefore x = \pm 2$$

Thus, the points at which the tangents are parallel to the y - axis are $(2, 0)$ and $(-2, 0)$.

Tangents and Normals Ex 16.1 Q18

The equation of the given curve is $x^2 + y^2 - 2x - 3 = 0$.

On differentiating with respect to x , we have:

$$2x + 2y \frac{dy}{dx} - 2 = 0$$

$$\Rightarrow y \frac{dy}{dx} = 1 - x$$

$$\Rightarrow \frac{dy}{dx} = \frac{1-x}{y}$$

Now, the tangents are parallel to the x -axis if the slope of the tangent is 0.

$$\therefore \frac{1-x}{y} = 0 \Rightarrow 1-x=0 \Rightarrow x=1$$

But, $x^2 + y^2 - 2x - 3 = 0$ for $x=1$.

$$\Rightarrow y^2 = 4 \Rightarrow y = \pm 2$$

Hence, the points at which the tangents are parallel to the x -axis are $(1, 2)$ and $(1, -2)$

(b)

Now, the tangents are parallel to the x -axis if the slope of the tangents is 0

$$\frac{y}{1-x} = 0$$

$$y = 0$$

But,

$$x^2 + y^2 - 2x - 3 = 0 \text{ for } y = 0$$

$$x^2 - 2x - 3 = 0$$

$$x = -1, 3$$

Hence, the points at which the tangents are parallel to the y -axis are,

$(-1, 0), (3, 0)$

***** END *****