



Exercise 12.1

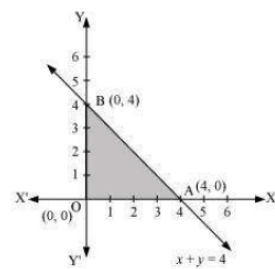
Question 1:

Maximise $Z = 3x + 4y$

Subject to the constraints: $x + y \leq 4, x \geq 0, y \geq 0$.

Answer

The feasible region determined by the constraints, $x + y \leq 4, x \geq 0, y \geq 0$, is as follows.



The corner points of the feasible region are O (0, 0), A (4, 0), and B (0, 4). The values of Z at these points are as follows.

Corner point	$Z = 3x + 4y$	
O(0, 0)	0	
A(4, 0)	12	
B(0, 4)	16	→ Maximum

Therefore, the maximum value of Z is 16 at the point B (0, 4).

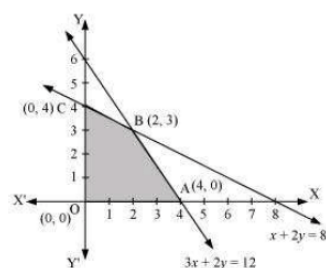
Question 2:

Minimise $Z = -3x + 4y$

subject to $x + 2y \leq 8, 3x + 2y \leq 12, x \geq 0, y \geq 0$.

Answer

The feasible region determined by the system of constraints, $x + 2y \leq 8, 3x + 2y \leq 12, x \geq 0$, and $y \geq 0$, is as follows.



The corner points of the feasible region are O (0, 0), A (4, 0), B (2, 3), and C (0, 4).

The values of Z at these corner points are as follows.

Corner point	$Z = -3x + 4y$	
O(0, 0)	0	
A(4, 0)	-12	→ Minimum
B(2, 3)	6	
C(0, 4)	16	

Therefore, the minimum value of Z is -12 at the point (4, 0).

Question 3:

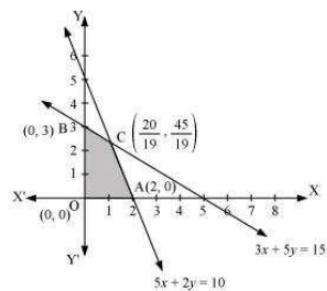
Maximise $Z = 5x + 3y$

subject to $3x + 5y \leq 15, 5x + 2y \leq 10, x \geq 0, y \geq 0$.

Answer

The feasible region determined by the system of constraints, $3x + 5y \leq 15$,

$5x + 2y \leq 10$, $x \geq 0$, and $y \geq 0$, are as follows.



The corner points of the feasible region are O (0, 0), A (2, 0), B (0, 3), and $C\left(\frac{20}{19}, \frac{45}{19}\right)$.
The values of Z at these corner points are as follows.

Corner point	$Z = 5x + 3y$	
O(0, 0)	0	
A(2, 0)	10	
B(0, 3)	9	
$C\left(\frac{20}{19}, \frac{45}{19}\right)$	$\frac{235}{19}$	→ Maximum

Therefore, the maximum value of Z is $\frac{235}{19}$ at the point $\left(\frac{20}{19}, \frac{45}{19}\right)$.

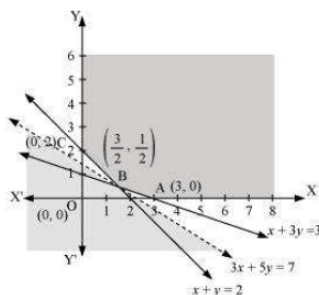
Question 4:

Minimise $Z = 3x + 5y$

such that $x + 3y \geq 3$, $x + y \geq 2$, $x, y \geq 0$.

Answer

The feasible region determined by the system of constraints, $x + 3y \geq 3$, $x + y \geq 2$, and $x, y \geq 0$, is as follows.



It can be seen that the feasible region is unbounded.

The corner points of the feasible region are A (3, 0), $B\left(\frac{3}{2}, \frac{1}{2}\right)$, and C (0, 2).
The values of Z at these corner points are as follows.

Corner point	$Z = 3x + 5y$	
A(3, 0)	9	
$B\left(\frac{3}{2}, \frac{1}{2}\right)$	7	→ Smallest
C(0, 2)	10	

As the feasible region is unbounded, therefore, 7 may or may not be the minimum value of Z.

For this, we draw the graph of the inequality, $3x + 5y < 7$, and check whether the resulting half plane has points in common with the feasible region or not.

It can be seen that the feasible region has no common point with $3x + 5y < 7$. Therefore,

the minimum value of Z is 7 at $\left(\frac{3}{2}, \frac{1}{2}\right)$.

Question 5:

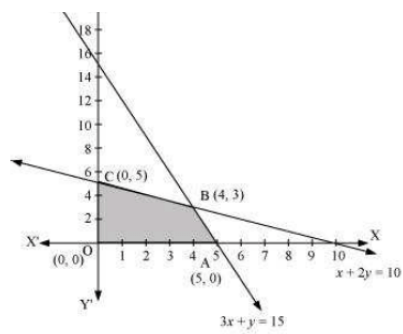
Maximise $Z = 3x + 2y$

subject to $x + 2y \leq 10$, $3x + y \leq 15$, $x, y \geq 0$.

Answer

The feasible region determined by the constraints, $x + 2y \leq 10$, $3x + y \leq 15$, $x \geq 0$, and $y \geq 0$, is as follows.





The corner points of the feasible region are A (5, 0), B (4, 3), and C (0, 5).

The values of Z at these corner points are as follows.

Corner point	$Z = 3x + 2y$	
A(5, 0)	15	
B(4, 3)	18	→ Maximum
C(0, 5)	10	

Therefore, the maximum value of Z is 18 at the point (4, 3).

Question 6:

Minimise $Z = x + 2y$

subject to $2x + y \geq 3$, $x + 2y \geq 6$, $x, y \geq 0$.

Answer

*****END*****