

Co-Ordinate Geometry Ex 14.4 Q6 Answer:

Let $A(x_1,y_1)$; $B(x_2,y_2)$; $C(x_3,y_3)$ be the coordinates of the vertices of \triangle ABC.

Let us assume that centroid of the \triangle ABC is at the origin G.

So, the coordinates of G are G(0,0).

So, the coordinates of G are
$$G(0,0)$$
. Now, $\frac{x_1+x_2+x_3}{3}=0$; $\frac{y_1+y_2+y_3}{3}=0$ so, $x_1+x_2+x_3=0$ (1) $y_1+y_2+y_3=0$ (2) Squaring (1) and (2), we get $x_1^2+x_2^2+x_3^2+2x_1x_2+2x_2x_3+2x_3x_1=0$ (3) $y_1^2+y_2^2+y_3^2+2y_1y_2+2y_2y_3+2y_3y_1=0$ (4) LHS = AB² + BC² + CA² = $\left[\sqrt{(x_2-x_1)^2+(y_2-y_1)^2}\right]^2+\left[\sqrt{(x_3-x_2)^2+(y_3-y_2)^2}\right]^2$ + $\left[\sqrt{(x_3-x_1)^2+(y_2-y_1)^2}\right]^2+\left[\sqrt{(x_3-x_2)^2+(y_3-y_2)^2}\right]^2$ = $(x_2-x_1)^2+(y_2-y_1)^2+(x_3-x_2)^2+(y_3-y_2)^2+(x_3-x_1)^2+(y_3-y_1)^2$ = $x_1^2+x_2^2-2x_1x_2+y_1^2+y_2^2-2y_1y_2+x_2^2+x_3^2-2x_2x_3+y_2^2+y_3^2-2y_2y_3+x_1^2+x_3^2-2x_1x_3+y_1^2+y_3^2-2y_1y_3$ = $2(x_1^2+x_2^2+x_3^2)+2(y_1^2+y_2^2+y_3^2)-(2x_1x_2+2x_2x_3+2x_3x_1)-(2y_1y_2+2y_2y_3+2y_3y_1)$ = $2(x_1^2+x_2^2+x_3^2)+2(y_1^2+y_2^2+y_3^2)+(x_1^2+x_2^2+x_3^2)+(y_1^2+y_2^2+y_3^2)$ = $3(x_1^2+x_2^2+x_3^2+y_1^2+y_2^2+y_3^2)$ RHS = $3\left(GA^2+GB^2+GC^2\right)$

Co-Ordinate Geometry Ex 14.4 Q7

Let $\triangle ABC$ be ant triangle such that P (-2, 3); Q (4,-3) and R (4, 5) are the mid-points of the sides AB, BC, CA respectively.

We have to find the co-ordinates of the centroid of the triangle

Let the vertices of the triangle be $A(x_1, y_1)$; $B(x_2, y_2)$; $C(x_3, y_3)$

In general to find the mid-point P(x,y) of two points $A(x_1,y_1)$ and $B(x_2,y_2)$ we use section formula as

$$P(x,y) = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$

So, co-ordinates of P,

$$(-2,3) = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$

Equate the x component on both the sides to get,

$$x_1 + x_2 = -4$$
(1)

Similarly,

$$y_1 + y_2 = 6$$
 (2)

Similarly, co-ordinates of Q,

$$(4,-3) = \left(\frac{x_3 + x_2}{2}, \frac{y_3 + y_2}{2}\right)$$

Equate the x component on both the sides to get,

$$x_3 + x_2 = 8 \dots (3)$$

Similarly,

$$y_3 + y_2 = -6$$
 (4)

Similarly, co-ordinates of R,

$$(4,5) = \left(\frac{x_3 + x_1}{2}, \frac{y_3 + y_1}{2}\right)$$

Equate the x component on both the sides to get,

$$x_3 + x_1 = 8 \dots (5)$$

Similarly,

$$y_3 + y_1 = 10$$
 (6)

Add equation (1) (3) and (5) to get,

$$2(x_1 + x_2 + x_3) = 12$$

$$x_1 + x_2 + x_3 = 6$$

Similarly, add equation (2) (4) and (6) to get,

$$2(y_1 + y_2 + y_3) = 10$$

$$y_1 + y_2 + y_3 = 5$$

We know that the co-ordinates of the centroid G of a triangle whose vertices are

$$(x_1, y_1), (x_2, y_2), (x_3, y_3)$$
 is-

$$G\left(\frac{x_1+x_2+x_3}{3}, \frac{y_1+y_2+y_3}{3}\right)$$

So, centroid G of a triangle $\Delta ABC\,$ is,

$$G\left(2,\frac{5}{3}\right)$$

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