



Chapter 6 Determinants Ex 6.2 Q45

$$\text{Let } \Delta = \begin{vmatrix} a^3 & 2 & a \\ b^3 & 2 & b \\ c^3 & 2 & c \end{vmatrix}$$

$$\Delta = 2 \begin{vmatrix} a^3 & 1 & a \\ b^3 & 1 & b \\ c^3 & 1 & c \end{vmatrix}$$

$$\Delta = 2 \{ a^3(c-b) - 1(b^3c - bc^3) + a(b^3 - c^3) \}$$

$$\Delta = 2 \{ a^3(c-b) - bc(b-c)(b+c) + a(b-c)(b^2 + bc + c^2) \}$$

$$\Delta = 2(b-c) \{ -a^3 - bc(b+c) + a(b^2 + bc + c^2) \}$$

$$\Delta = 2(a-b)(b-c)(c-a)(a+b+c)$$

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$$\begin{aligned} \begin{vmatrix} a & b & c \\ x & y & z \\ p & q & r \end{vmatrix} &= - \begin{vmatrix} x & y & z \\ a & b & c \\ p & q & r \end{vmatrix} = (-1)^2 \begin{vmatrix} x & y & z \\ p & q & r \\ a & b & c \end{vmatrix} = \begin{vmatrix} x & y & z \\ p & q & r \\ a & b & c \end{vmatrix} \\ &= (-1) \begin{vmatrix} y & x & z \\ q & p & r \\ b & a & c \end{vmatrix} \\ &= (-1)^2 \begin{vmatrix} y & x & z \\ b & a & c \\ q & p & r \end{vmatrix} \end{aligned}$$

Taking transpose, we get

$$= \begin{vmatrix} y & b & p \\ x & a & q \\ z & c & r \end{vmatrix}$$

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Consider the determinant $\begin{vmatrix} x+1 & x+2 & x+a \\ x+2 & x+3 & x+b \\ x+3 & x+4 & x+c \end{vmatrix}$, where a, b, c are in A.P.

$$\text{Let } \Delta = \begin{vmatrix} x+1 & x+2 & x+a \\ x+2 & x+3 & x+b \\ x+3 & x+4 & x+c \end{vmatrix}$$

Applying $C_1 \rightarrow C_1 + C_2 + C_3$, we have,

$$\Delta = \begin{vmatrix} 3x+1+2+a & x+2 & x+a \\ 3x+2+3+b & x+3 & x+b \\ 3x+3+4+c & x+4 & x+c \end{vmatrix}$$

$$\Rightarrow \Delta = \begin{vmatrix} 3x+3+a & x+2 & x+a \\ 3x+5+b & x+3 & x+b \\ 3x+7+c & x+4 & x+c \end{vmatrix}$$

Applying $R_2 \rightarrow R_2 - R_1$ and $R_3 \rightarrow R_3 - R_2$, we have,

$$\Rightarrow \Delta = \begin{vmatrix} 3x+3+a & x+2 & x+a \\ 2+b-a & 1 & b-a \\ 2+c-b & 1 & c-b \end{vmatrix}$$

Since a, b and c are in arithmetic progression, we have

$$b-a = c-b = k(\text{say}).$$

Thus,

$$\Delta = \begin{vmatrix} 3x+3+a & x+2 & x+a \\ 2+k & 1 & k \\ 2+k & 1 & k \end{vmatrix}$$

Since the second row and the third row are identical, we have

$$\Delta = 0$$

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Since, α, β, γ are in A.P, $2\beta = \alpha + \gamma$

$$\text{LHS} = \begin{vmatrix} x-3 & x-4 & x-\alpha \\ x-2 & x-3 & x-\beta \\ x-1 & x-2 & x-\gamma \end{vmatrix}$$

$$R_2 \rightarrow R_2 - \frac{R_1}{2} - \frac{R_3}{2}$$

$$= \begin{vmatrix} x-3 & x-4 & x-\alpha \\ (x-2) - \frac{x-3}{2} - \frac{x-1}{2} & (x-3) - \frac{x-4}{2} - \frac{x-2}{2} & (x-\beta) - \frac{x-\alpha}{2} - \frac{x-\gamma}{2} \\ x-1 & x-2 & x-\gamma \end{vmatrix}$$

$$= \begin{vmatrix} x-3 & x-4 & x-\alpha \\ 0 & 0 & 0 \\ x-1 & x-2 & x-\gamma \end{vmatrix} \quad [\because 2\beta = \alpha + \gamma]$$

$$= 0$$

***** END *****