



### Polynomials Ex 2.2 Q2

**Answer :**

If  $\alpha, \beta$  and  $\gamma$  are the zeros of a cubic polynomial  $f(x)$ , then

$$f(x) = k \{x^3 - (\alpha + \beta + \gamma)x^2 + (\alpha\beta + \beta\gamma + \gamma\alpha)x - \alpha\beta\gamma\} \text{ where } k \text{ is any non-zero real number.}$$

Here,

$$\alpha + \beta + \gamma = 3,$$

$$\alpha\beta + \beta\gamma + \gamma\alpha = -1$$

$$\alpha\beta\gamma = -3$$

Therefore

$$f(x) = k \{x^3 - (3)x^2 + (-1)x - (-3)\}$$

$$f(x) = k \{x^3 - 3x^2 - 1x + 3\}$$

Hence, cubic polynomial is  $f(x) = k \{x^3 - 3x^2 - 1x + 3\}$ , where  $k$  is any non-zero real number.

### Polynomials Ex 2.2 Q3

**Answer :**

Let  $\alpha = a - d, \beta = a$  and  $\gamma = a + d$  be the zeros of the polynomial

$$f(x) = 2x^3 - 15x^2 + 37x - 30$$

Therefore

$$\alpha + \beta + \gamma = \frac{\text{Coefficient of } x^2}{\text{Coefficient of } x^3}$$

$$= -\left(\frac{-15}{2}\right)$$

$$= \frac{15}{2}$$

$$\alpha\beta\gamma = \frac{-\text{Constant term}}{\text{Coefficient of } x^3}$$

$$= -\left(\frac{-30}{2}\right)$$

$$= 15$$

$$\text{Sum of the zeros} = \frac{\text{Coefficient of } x^2}{\text{Coefficient of } x^3}$$

$$(a - d) + a + (a + d) = \frac{15}{2}$$

$$a + a + a - \cancel{d} + \cancel{d} = \frac{15}{2}$$

$$3a = \frac{15}{2}$$

$$a = \frac{15}{2} \times \frac{1}{3}$$

$$a = \frac{5}{2}$$

$$\text{Product of the zeros} = \frac{-\text{Constant term}}{\text{Coefficient of } x^2}$$

$$\alpha\beta\gamma = 15$$

$$(a-d) + a + (a+d) = 15$$

$$a(a^2 - d^2) = 15$$

$$\text{Substituting } a = \frac{5}{2} \text{ we get}$$

$$\frac{5}{2} \left( \left( \frac{5}{2} \right)^2 - d^2 \right) = 15$$

$$\frac{5}{2} \left( \frac{25}{4} - d^2 \right) = 15$$

$$\frac{25}{4} - d^2 = 15 \times \frac{2}{5}$$

$$\frac{25}{4} - d^2 = 3 \times 2$$

$$\frac{25}{4} - d^2 = 6$$

$$-d^2 = 6 - \frac{25}{4}$$

$$-d^2 = \frac{24-25}{4}$$

$$\cancel{d^2} = \cancel{\frac{1}{4}}$$

$$d \times d = \frac{1}{2} \times \frac{1}{2}$$

$$d = \frac{1}{2}$$

Therefore, substituting  $a = \frac{5}{2}$  and  $d = \frac{1}{2}$  in  $\alpha = a - d$ ,  $\beta = a$  and  $\gamma = a + d$

$$\alpha = a - d$$

$$\alpha = \frac{5}{2} - \frac{1}{2}$$

$$\alpha = \frac{5-1}{2}$$

$$\alpha = \frac{4}{2}$$

$$\alpha = 2$$

$$\beta = a$$

$$\beta = \frac{5}{2}$$

$$\gamma = a + d$$

$$\gamma = \frac{5}{2} + \frac{1}{2}$$

$$\gamma = \frac{5+1}{2}$$

$$\gamma = \frac{6}{2}$$

$$\gamma = 3$$

Hence, the zeros of the polynomial are  $\boxed{2, \frac{5}{2}, 3}$ .

\*\*\*\*\* END \*\*\*\*\*