

Arithmetic Progressions Ex 9.5 Q32

Answer:

(i) Here, we have an A.P. whose n^{th} term (a_n) , first term (a) and common difference (d) are given. We need to find the number of terms (n) and the sum of first n terms (S_n) .

Here,

First term (a) = 5

Last term $(a_n) = 50$

Common difference (d) = 3

So here we will find the value of n using the formula, $a_n = a + (n-1)d$

So, substituting the values in the above mentioned formula

$$50 = 5 + (n-1)3$$

$$50 = 5 + 3n - 3$$

$$50 = 2 + 3n$$

$$3n = 50 - 2$$

Further simplifying for n,

$$3n = 48$$

$$n = \frac{48}{3}$$

$$n = 16$$

Now, here we can find the sum of the n terms of the given A.P., using the formula,

$$S_n = \left(\frac{n}{2}\right) \left(a+l\right)$$

Where, a = the first term

/ = the last term

So, for the given A.P. on substituting the values in the formula for the sum of *n* terms of an A.P., we get

$$S_{16} = \left(\frac{16}{2}\right) [5+50]$$
$$= 8(55)$$

Therefore, for the given A.P n = 16 and $S_{16} = 440$

(ii) Here, we have an A.P. whose n^{th} term (a_n) , sum of first n terms (S_n) and common difference (d) are given. We need to find the number of terms (n) and the first term (a).

Here,

Last term $(a_n) = 4$

Common difference (d) = 2

Sum of *n* terms $(S_n) = -14$

So here we will find the value of n using the formula, $a_n = a + (n-1)d$

So, substituting the values in the above mentioned formula

$$4 = a + (n-1)2$$

$$4 = a + 2n - 2$$

$$4+2=a+2n$$

$$n = \frac{6-a}{2} \qquad \dots (1$$

Now, here the sum of the n terms is given by the formula,

$$S_n = \left(\frac{n}{2}\right) (a+l)$$

Where, a = the first term

/ = the last term

So, for the given A.P. on substituting the values in the formula for the sum of *n* terms of an A.P., we

$$-14 = \left(\frac{n}{2}\right)[a+4]$$

$$-14(2) = n(a+4)$$

$$n = \frac{-28}{a+4} \qquad \dots (2)$$

Equating (1) and (2), we get,

$$\frac{6-a}{2} = \frac{-28}{a+4}$$
$$(6-a)(a+4) = -28(2)$$

$$(6-a)(a+4) = -28(2)$$

$$6a - a^2 + 24 - 4a = -56$$

$$-a^2 + 2a + 24 + 56 = 0$$

So, we get the following quadratic equation,

$$-a^2 + 2a + 80 = 0$$

$$a^2 - 2a - 80 = 0$$

Further, solving it for a by splitting the middle term,

$$a^2 - 2a - 80 = 0$$

$$a^2 - 10a + 8a - 80 = 0$$

$$a(a-10)+8(a-10)=0$$

$$(a-10)(a+8)=0$$

So, we get,

$$a - 10 = 0$$

$$a = 10$$

Or

$$a + 8 = 0$$

$$a = -8$$

Substituting, a = 10 in (1),

$$n = \frac{6-10}{2}$$

$$n = \frac{-4}{2}$$

$$n = -2$$

Here, we get n as negative, which is not possible. So, we take a = -8,

$$n = \frac{6 - \left(-8\right)}{2}$$

$$n = \frac{6+8}{2}$$