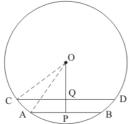


Circles Ex 16.2 Q4

Answer:

Let AB and CD be two parallel chord of the circle with centre O such that AB = 5 cm and CD = 11 cm. let the radius of the circle be r cm.



Draw $\mathit{OP} \perp \mathit{AB}$ and $\mathit{OQ} \perp \mathit{CD}$ as well as point O , Q and P are collinear.

Clearly, PQ = 3 cm

Let OQ = x then OP = x + 3

In $\triangle OAP$ and $\triangle OCQ$ we have $OA^2 = OP^2 + AP^2$

$$\Rightarrow r^2 = (x+3)^2 + \left(\frac{5}{2}\right)^2 \dots (1)$$

And

$$OC^{2} = OQ^{2} + CQ^{2}$$

$$\Rightarrow r^{2} = x^{2} + \left(\frac{11}{2}\right)^{2} \dots (2)$$

From (1) and (2) we get

$$(x+3)^{2} + \left(\frac{5}{2}\right)^{2} = x^{2} + \left(\frac{11}{2}\right)^{2}$$

$$\Rightarrow x^{2} + 6x + 9 + \frac{25}{4} = x^{2} + \frac{121}{4}$$

$$\Rightarrow 6x + \frac{61}{4} = \frac{121}{4}$$

$$\Rightarrow 6x = \frac{121 - 61}{4}$$

$$\Rightarrow 6x = \frac{60}{4}$$

$$\Rightarrow x = \frac{5}{2}$$

Putting the value of x in (2) we get,

$$r^{2} = \left(\frac{5}{2}\right)^{2} + \left(\frac{11}{2}\right)^{2}$$

$$= \frac{25}{4} + \frac{121}{4}$$

$$= \frac{146}{4}$$

$$\Rightarrow r = \sqrt{\frac{146}{4}}$$

$$r = \boxed{\frac{\sqrt{146}}{2} \text{ cm}}$$

******* END ********