

Tangents and Normals Ex 16.1 Q4 We have,

$$y = x^3 - 3x$$
 ---(i)

$$\frac{dy}{dx} = 3x^2 - 3 \qquad ---(ii)$$

Also,

The slope of the chord obtained by joining the points (1,-2) and (2,2) is

$$\frac{2-(-2)}{2-1}$$

$$\left[\mathsf{Slope}\,\frac{\mathsf{y}_2-\mathsf{y}_1}{\mathsf{x}_2-\mathsf{x}_1}\right]$$

According to the question slope of tangent to (i) and the chord are parallel

$$3x^2 - 3 = 4$$

$$\Rightarrow$$
 $3x^2 = 7$

$$\Rightarrow \qquad \times = \pm \sqrt{\frac{7}{3}}$$

From (i)

$$y = \pm \sqrt{\frac{7}{3}} \mp 3\sqrt{\frac{7}{3}}$$
$$= \mp \frac{2}{3}\sqrt{\frac{7}{3}}$$

Thus, the required point is

$$\pm\sqrt{\frac{7}{3}}, \quad \mp\,\frac{2}{3}\,\sqrt{\frac{7}{3}}$$

Tangents and Normals Ex 16.1 Q5

The given equations are

$$y = x^3 - 2x^2 - 2x$$
 ---(i)
 $y = 2x - 3$ ---(ii)

Slope to the tangents of (i) and (ii) are

$$\frac{dy}{dx} = 3x^2 - 4x - 2 \qquad ---(iii)$$
and
$$\frac{dy}{dx} = 2 \qquad ---(iv)$$

According to the question slope to (i) and (ii) are parallel, so

$$3x^{2} - 4x - 2 = 2$$

$$\Rightarrow 3x^{2} - 4x - 4 = 0$$

$$\Rightarrow 3x^{2} - 6x + 2x - 4 = 0$$

$$\Rightarrow 3x(x - 2) + 2(x - 2) = 0$$

$$\Rightarrow (3x + 2)(x - 2) = 0$$

$$\Rightarrow x = \frac{-2}{3} \text{ or } 2$$

From (i)
$$y = \frac{4}{27} \text{ or } -4$$

Thus, the points are

$$\left(\frac{-2}{3}, \frac{4}{27}\right)$$
 and $\left(2, -4\right)$

Tangents and Normals Ex 16.1 Q6

$$y^2 = 2x^3$$
 ---(i)

Differentiating (i) with respect to x, we get

$$2y \frac{dy}{dx} = 6x^{2}$$

$$\Rightarrow \frac{dy}{dx} = \frac{3x^{2}}{y} \qquad ---(ii)$$

According to the question

$$\frac{3x^2}{y} = 3$$

$$\Rightarrow x^2 = y \qquad ---(iii)$$

$$(x^2)^2 = 2x^3$$

$$\Rightarrow x^4 - 2x^3 = 0$$

$$\Rightarrow$$
 $x^4 - 2x^3 = 0$

$$\Rightarrow \qquad x^3 \left(x - 2 \right) = 0$$

$$\Rightarrow$$
 $x = 0 \text{ or } 2$

If
$$x = 0$$
, then

$$\frac{dy}{dx} = \frac{3x^2}{y} \Rightarrow \frac{dy}{dx} = 0$$

Which is not possible.

$$\therefore x = 2.$$

Putting x = 2 in the equation of the curve $y^2 = 2x^3$, we get y = 4.

Hence the required point is (2,4)

Tangents and Normals Ex 16.1 Q7

We know that the slope to any curve is $\frac{dy}{dx} = \tan\theta$ where θ is the angle with possitive direction of x-axis.

Now,

The given curve is
$$xy + 4 = 0$$
 ---(i)

Differentiating with respect to \boldsymbol{x} , we get

$$y + x \frac{dy}{dx} = 0$$

$$\Rightarrow \frac{dy}{dx} = \frac{-y}{x}$$
 ---(ii)

Also,

$$\frac{dy}{dx} = \tan 45^\circ = 1 \qquad ---(iii)$$

: From (ii) and (iii)

$$\frac{-y}{x} = 1$$
$$x = -y$$

$$\Rightarrow$$
 $x = -y$ ---(iv)

From (i) and (iv), we get

$$-y^2+4=0$$

$$\Rightarrow$$
 $y = \pm 2$

$$\therefore \quad x = \mp 2$$

Thus, the points are

$$(2,-2)$$
 and $(-2,2)$

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