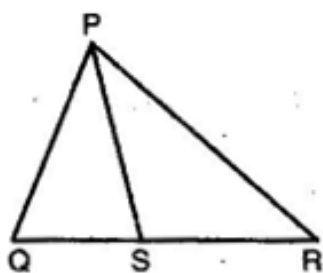


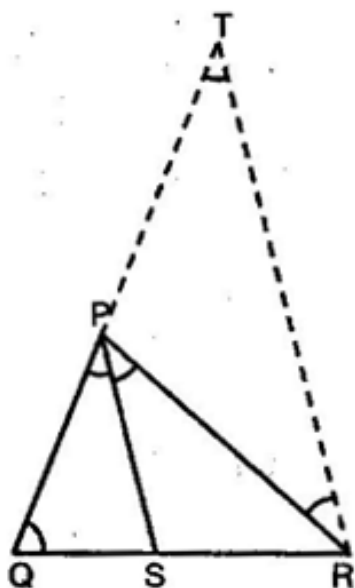


NCERT Solutions For Class 10 Chapter 6 Triangles Exercise 6.6

1. In figure, PS is the bisector of $\angle QPR$ of ΔPQR . Prove that $\frac{QS}{SR} = \frac{PQ}{PR}$.



Ans. Given: PQR is a triangle and PS is the internal bisector of $\angle QPR$ meeting QR at S.



$$\therefore \angle QPS = \angle SPR$$

To prove: $\frac{QS}{SR} = \frac{PQ}{PR}$

Construction: Draw $RT \parallel SP$ to cut QP produced at T.

Proof: Since $PS \parallel TR$ and PR cuts them, hence,

$$\angle SPR = \angle PRT \dots\dots\dots(i) \text{ [Alternate } \angle \text{ s]}$$

$$\text{And } \angle QPS = \angle PTR \dots\dots\dots(ii) \text{ [Corresponding } \angle \text{ s]}$$

$\angle s]$

But $\angle QPS = \angle SPR$ [Given]

$\therefore \angle PRT = \angle PTR$ [From eq. (i) & (ii)]

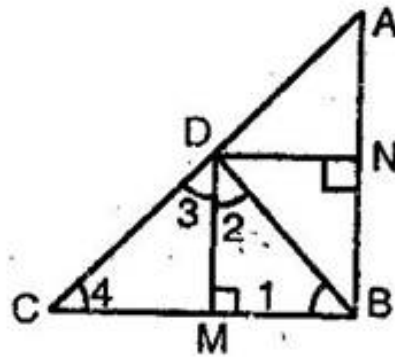
$\Rightarrow PT = PR$(iii)

[Sides opposite to equal angles are equal]

Now, in $\triangle QRT$,

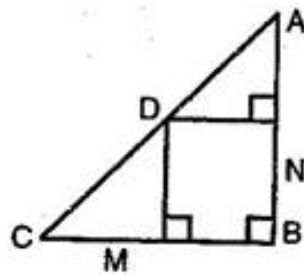
$RT \parallel SP$ [By construction]

$$\therefore \frac{QS}{SR} = \frac{PQ}{PT} \text{ [Thales theorem]}$$



$$\Rightarrow \frac{QS}{SR} = \frac{PQ}{PR} \text{ [From eq. (iii)]}$$

2. In figure, D is a point on hypotenuse AC of $\triangle ABC$, $BD \perp AC$, $DM \perp BC$ and $DN \perp AB$. Prove that:



(i) $DM^2 = DN \cdot MC$

(ii) $DN^2 = DM \cdot AN$

Ans. Since, $AB \perp BC$ and $DM \perp BC$

$$\Rightarrow AB \parallel DM$$

Similarly, $BC \perp AB$ and $DN \perp AB$

$$\Rightarrow CB \parallel DN$$

\therefore quadrilateral BMDN is a rectangle.

$$\therefore BM = ND$$

(i) In $\triangle BMD$, $\angle 1 + \angle BMD + \angle 2 = 180^\circ$

$$\Rightarrow \angle 1 + 90^\circ + \angle 2 = 180^\circ$$

$$\Rightarrow \angle 1 + \angle 2 = 90^\circ$$

Similarly, in $\triangle DMC$, $\angle 3 + \angle 4 = 90^\circ$

Since $BD \perp AC$,

$$\therefore \angle 2 + \angle 3 = 90^\circ$$

Now, $\angle 1 + \angle 2 = 90^\circ$ and $\angle 2 + \angle 3 = 90^\circ$

$$\Rightarrow \angle 1 + \angle 2 = \angle 2 + \angle 3$$

$$\Rightarrow \angle 1 = \angle 3$$

Also, $\angle 3 + \angle 4 = 90^\circ$ and $\angle 2 + \angle 3 = 90^\circ$

$$\Rightarrow \angle 3 + \angle 4 = \angle 2 + \angle 3$$

$$\Rightarrow \angle 4 = \angle 2$$

Thus, in $\triangle BMD$ and $\triangle DMC$,

$$\angle 1 = \angle 3 \text{ and } \angle 4 = \angle 2$$

$$\therefore \triangle BMD \sim \triangle DMC$$

$$\Rightarrow \frac{BM}{DM} = \frac{MD}{MC}$$

$$\Rightarrow \frac{DN}{DM} = \frac{DM}{MC} [BM = ND]$$

$$\Rightarrow DM^2 = DN.MC$$

(ii) Processing as in (i), we can prove that

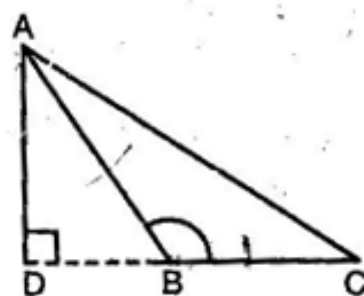
$$\triangle BND \sim \triangle DNA$$

$$\Rightarrow \frac{BN}{DN} = \frac{ND}{NA}$$

$$\Rightarrow \frac{DM}{DN} = \frac{DN}{AN} [BN = DM]$$

$$\Rightarrow DN^2 = DM.AN$$

3. In figure, ABC is a triangle in which $\angle ABC > 90^\circ$ and $AD \perp CB$ produced. Prove that:



$$AC^2 = AB^2 + BC^2 + 2BC.BD$$

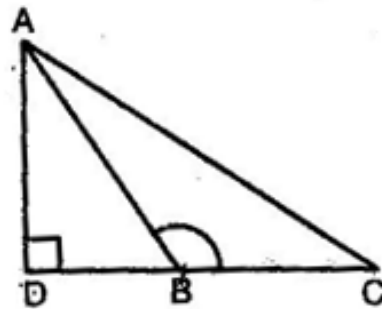
Ans. Given: ABC is a triangle in which $\angle ABC > 90^\circ$ and $AD \perp CB$ produced.

To prove: $AC^2 = AB^2 + BC^2 + 2BC \cdot BD$

Proof: Since $\triangle ADB$ is a right triangle, right angled at D, therefore, by Pythagoras theorem,

$$AB^2 = AD^2 + DB^2 \dots\dots\dots(i)$$

Again, $\triangle ADC$ is a right triangle, right angled at D, therefore, by Pythagoras theorem,



$$AC^2 = AD^2 + DC^2$$

$$\Rightarrow AC^2 = AD^2 + (DB + BC)^2$$

$$\Rightarrow AC^2 = AD^2 + DB^2 + BC^2 + 2DB \cdot BC$$

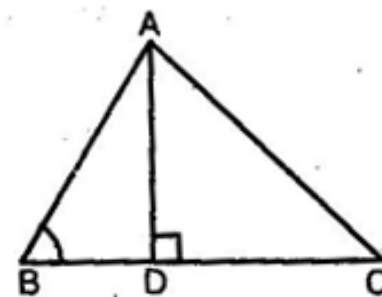
$$\Rightarrow AC^2 = (AD^2 + DB^2) + BC^2 + 2DB \cdot BC$$

$$\Rightarrow AC^2 = AB^2 + BC^2 + 2DB \cdot BC$$

[Using eq. (i)]

4. In figure, ABC is a triangle in which $\angle ABC < 90^\circ$ and $AD \perp BC$ produced. Prove that:

$$AC^2 = AB^2 + BC^2 - 2BC \cdot BD$$



Ans. Given: ABC is a triangle in which $\angle ABC < 90^\circ$ and $AD \perp BC$ produced.

To prove: $AC^2 = AB^2 + BC^2 - 2BC \cdot BD$

Proof: Since $\triangle ADB$ is a right triangle, right angled at D, therefore, by Pythagoras theorem,

$$AB^2 = AD^2 + BD^2 \dots\dots\dots(i)$$

Again, $\triangle ADB$ is a right triangle, right angled at D, therefore, by Pythagoras theorem,

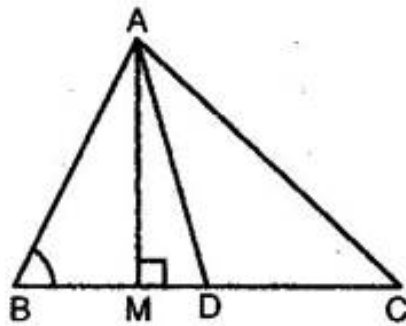
$$AC^2 = AD^2 + DC^2$$

$$\Rightarrow AC^2 = AD^2 + (BC - BD)^2$$

$$\Rightarrow AC^2 = AD^2 + BC^2 + BD^2 - 2BC \cdot BD$$

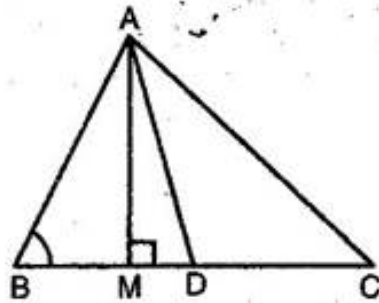
$$\Rightarrow AC^2 = (AD^2 + DB^2) + BC^2 - 2DB \cdot BC$$

$$\Rightarrow AC^2 = AB^2 + BC^2 - 2DB \cdot BC$$



[Using eq. (i)]

5. In figure, AD is a median of a triangle ABC and $AM \perp BC$. Prove that:



$$(i) AC^2 = AD^2 + BC \cdot DM + \left(\frac{BC}{2}\right)^2$$

$$(ii) AB^2 = AD^2 - BC \cdot DM + \left(\frac{BC}{2}\right)^2$$

$$(iii) AC^2 + AB^2 = 2AD^2 + \frac{1}{2} BC$$

Ans. Since $\angle AMD = 90^\circ$, therefore $\angle ADM < 90^\circ$ and $\angle ADC > 90^\circ$

Thus, $\angle ADC$ is acute angle and $\angle ADC$ is obtuse angle.

***** END *****

