

Factorisation of Polynomials Ex 6.2 Q5

Answer:

The given polynomial is

$$f(x) = 2x^3 - 3x^2 + ax + b$$

If x = 0 is zeros of the polynomial f(x), then f(0) = 0

$$2 \times (0)^{3} - 3 \times (0)^{2} + a \times 0 + b = 0$$
$$0 - 0 + 0 + b = 0$$
$$b = 0 \qquad(1)$$

Similarly, if x = -1 is the zeros of the polynomial of f(x),

Then,
$$f(-1) = 0$$

$$2 \times (-1)^3 - 3 \times (-1)^2 + a \times (-1) + b = 0$$
$$-2 - 3 - a + b = 0$$
$$-5 - a + b = 0$$

Putting the value of b from equation (1)

$$-5 - a + 0 = 0$$

$$a = -5$$

Thus,

$$a = -5,$$

$$b = 0$$

Factorisation of Polynomials Ex 6.2 Q6 Answer:

The given polynomial is

$$f(x) = x^3 + 6x^2 + 11x + 6$$

Here, f(x) is a polynomial with integer coefficient and the coefficient of highest degree term is 1. So, the integer roots of f(x) are factors of 6. Which are ± 1 , ± 2 , ± 3 , ± 6 by observing.

$$f(-1) = (-1)^3 + 6 \times (-1)^2 + 11(-1) + 6$$

$$= -1 + 6 - 11 + 6$$

$$= -12 + 12$$

$$= 0$$

Also,

$$f(-2) = (-2)^3 + 6(-2)^2 + 11(-2) + 6$$

$$= -8 + 6 \times 4 - 22 + 6$$

$$= -8 + 24 - 22 + 6$$

$$= 30 - 30$$

$$= 0$$

And similarly,

$$f(-3) = 0$$

Therefore, the integer roots of the polynomial f(x) are -1, -2, -3

Factorisation of Polynomials Ex 6.2 Q7

Answer:

The given polynomial is

$$f(x) = 2x^3 + x^2 - 7x - 6$$

f(x) is a cubic polynomial with integer coefficients. If bc is rational root in lowest terms, then the values of b are limited

to the factors of 6 which are $\pm 1, \pm 2, \pm 3, \pm 6$ and the values of c are limited to the factor of 2 as $\pm 1, \pm 2$.

Hence, the possible

rational roots are $\pm 1, \pm 2, \pm 3, \pm 6, \pm 12, \pm 32$.

Since,
$$f(2) = 2 \cdot 2^3 + 2^2 - 7.2 - 6 = 0$$

So, 2 is a root of the polynomial $f(x) = 2x^3 + x^2 - 7x - 6$

Now, the polynomial can be written as,

$$f(x) = (x-2)(2x^2+5x+3)$$

A1so

$$f(-1) = (-1-2)(2-5+3) = 0$$

Therefore,

$$f(x) = (x-2)(x+1)(2x+3)$$

Hence, the rational roots of the polynomial $f(x) = 2x^3 + x^2 - 7x - 6$ are 2, -3/2 and -1.

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