



## Increasing and Decreasing Functions Ex 17.2 Q2

We have,

$$f(x) = x^2 - 6x + 9$$

$$\therefore f'(x) = 2x - 6$$

Critical points

$$f'(x) = 0$$

$$\Rightarrow 2(x - 3) = 0$$

$$\Rightarrow x = 3$$

Clearly,  $f'(x) > 0$  if  $x > 3$

$$f'(x) < 0 \text{ if } x < 3$$

Thus,  $f(x)$  increases in  $(3, \infty)$ , decreases in  $(-\infty, 3)$

IIInd part

The given equation of curves

$$y = x^2 - 6x + 9 \quad \text{---(i)}$$

$$y = x + 5 \quad \text{---(ii)}$$

Slope of (i)

$$m_1 = \frac{dy}{dx} = 2x - 6$$

Slope of (ii)

$$m_2 = 1$$

Given that slope of normal to (i) is parallel to (ii)

$$\therefore \frac{-1}{2x - 6} = 1$$

$$\Rightarrow 2x - 6 = -1$$

$$\Rightarrow x = \frac{5}{2}$$

From (i)

$$y = \frac{25}{4} - 15 + 9$$

$$= \frac{25}{4} - 6$$

$$= \frac{1}{4}$$

Thus, the required point is  $\left(\frac{5}{2}, \frac{1}{4}\right)$ .

We have,

$$f(x) = \sin x - \cos x, \quad 0 < x < 2\pi$$

$$\therefore f'(x) = \cos x + \sin x$$

Critical points

$$f'(x) = 0$$

$$\Rightarrow \cos x + \sin x = 0$$

$$\Rightarrow \tan x = -1$$

$$\Rightarrow x = \frac{3\pi}{4}, \frac{7\pi}{4}$$

Clearly,  $f'(x) > 0$  if  $0 < x < \frac{3\pi}{4}$  and  $\frac{7\pi}{4} < x < 2\pi$

$$f'(x) < 0 \text{ if } \frac{3\pi}{4} < x < \frac{7\pi}{4}$$

Thus,  $f(x)$  increases in  $\left(0, \frac{3\pi}{4}\right) \cup \left(\frac{7\pi}{4}, 2\pi\right)$ , decreases in  $\left(\frac{3\pi}{4}, \frac{7\pi}{4}\right)$ .

Increasing and Decreasing Functions Ex 17.2 Q4

We have,

$$f(x) = e^{2x}$$

$$\therefore f'(x) = 2e^{2x}$$

We know that

$$f(x) \text{ is increasing if } f'(x) > 0$$

$$\Rightarrow 2e^{2x} > 0$$

$$\Rightarrow e^{2x} > 0$$

Since, the value of  $e$  lies between 2 and 3

So, any power of  $e$  will be greater than zero.

Thus,  $f(x)$  is increasing on  $R$ .

Increasing and Decreasing Functions Ex 17.2 Q5

We have,

$$f(x) = e^{\frac{1}{x}}, \quad x \neq 0$$

$$f'(x) = e^{\frac{1}{x}} \times \left( \frac{-1}{x^2} \right)$$

$$\therefore f'(x) = -\frac{e^{\frac{1}{x}}}{x^2}$$

Now,

$$x \in \mathbb{R}, x \neq 0$$

$$\Rightarrow \frac{1}{x^2} > 0 \text{ and } e^{\frac{1}{x}} > 0$$

$$\Rightarrow \frac{e^{\frac{1}{x}}}{x^2} > 0$$

$$\Rightarrow -\frac{e^{\frac{1}{x}}}{x^2} < 0$$

$$\Rightarrow f'(x) < 0$$

Hence,  $f(x)$  is a decreasing function for all  $x \neq 0$ .

\*\*\*\*\* END \*\*\*\*\*