

Co-Ordinate Geometry Ex 14.2 Q3

Answer:

The distance d between two points (x_1, y_1) and (x_2, y_2) is given by the formula

$$d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

Here it is said that the points (2, 1) and (1, -2) are equidistant from (x, y).

Let d_1 be the distance between (2, 1) and (x, y).

Let d_2 be the distance between (1, -2) and (x, y).

So, using the distance formula for both these pairs of points we have

$$d_1 = \sqrt{(2-x)^2 + (1-y)^2}$$

$$d_2 = \sqrt{(1-x)^2 + (-2-y)^2}$$

Now since both these distances are given to be the same, let us equate both d_1 and d_2

$$d_1 = d_2$$

$$\sqrt{(2-x)^2 + (1-y)^2} = \sqrt{(1-x)^2 + (-2-y)^2}$$

Squaring on both sides we have,

$$(2-x)^{2} + (1-y)^{2} = (1-x)^{2} + (-2-y)^{2}$$

$$4+x^{2}-4x+1+y^{2}-2y=1+x^{2}-2x+4+y^{2}+4y$$

$$-4x-2y=-2x+4y$$

$$-2x-6y=0$$

$$x+3y=0$$

Hence we have proved that when the points (2, 1) and (1, -2) are equidistant from (x, y) we have x + 3y = 0.

Co-Ordinate Geometry Ex 14.2 Q4

Answer

The distance d between two points (x_1, y_1) and (x_2, y_2) is given by the formula

$$d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

It is said that (x, y) is equidistant from both (-3,0) and (3,0).

Let d_1 be the distance between (x, y) and (-3,0).

Let d_2 be the distance between (x, y) and (3,0).

So, using the distance formula for both these pairs of points we have

$$d_1 = \sqrt{(x+3)^2 + (y-0)^2}$$

$$d_2 = \sqrt{(x-3)^2 + (y-0)^2}$$

Now since both these distances are given to be the same, let us equate both d_1 and d_2 .

$$d_1 = d_2$$

$$\sqrt{(x+3)^2 + (y-0)^2} = \sqrt{(x-3)^2 + (y-0)^2}$$

Squaring on both sides we have,

$$(x+3)^2 + (y-0)^2 = (x-3)^2 + (y-0)^2$$
$$x^2 + 9 + 6x + y^2 = x^2 + 9 - 6x + y^2$$

$$12x = 0$$

$$x = 0$$

It is also said that the value of both d_1 and d_2 is 4 units.

Substituting the value of 'x' in the equation for either d_1 or d_2 we can get the value of 'y'.

$$d_1 = \sqrt{(x+3)^2 + (y-0)^2}$$

$$4 = \sqrt{(0+3)^2 + (y-0)^2}$$
$$4 = \sqrt{9+y^2}$$

Squaring on both sides of the equation we have,

$$16 = 9 + y^{2}$$
$$y^{2} = 7$$
$$y = \pm \sqrt{7}$$

Hence the values of 'x' and 'y' are
$$x = 0$$

 $y = \pm \sqrt{7}$

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