



Solution of Simultaneous Linear Equations Ex 8.2 Q5

$$x + y + z = 0$$

$$x - y - 5z = 0$$

$$x + 2y + 4z = 0$$

$$\begin{aligned}|A| &= \begin{vmatrix} 1 & 1 & 1 \\ 1 & -1 & -5 \\ 1 & 2 & 4 \end{vmatrix} \\ &= 1(6) - 1(9) + 1(3) = 9 - 9 = 0\end{aligned}$$

Hence, the system has infinite solutions.

Let $z = k$

$$x + y = -k$$

$$x - y = 5k$$

$$\begin{aligned}\begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} &= \begin{bmatrix} -k \\ 5k \end{bmatrix} \\ \text{or } A X &= B\end{aligned}$$

$|A| = -2 \neq 0$, hence A^{-1} exists.

$$\text{adj } A = \begin{bmatrix} -1 & -1 \\ -1 & 1 \end{bmatrix}$$

$$\text{so, } X = A^{-1} B = \frac{1}{|A|} (\text{adj } A) B = \frac{1}{-2} \begin{bmatrix} -1 & -1 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} -k \\ 5k \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \end{bmatrix} = \left(\frac{1}{-2} \right) \begin{bmatrix} k - 5k \\ k + 5k \end{bmatrix} = \begin{bmatrix} 2k \\ -3k \end{bmatrix}$$

$$x = 2k, y = -3k, z = k$$

Solution of Simultaneous Linear Equations Ex 8.2 Q6

$$\begin{aligned}x + y - z &= 0 \\x - 2y + z &= 0 \\3x + 6y - 5z &= 0\end{aligned}$$

$$\begin{aligned}\text{Hence, } |A| &= \begin{vmatrix} 1 & 1 & -1 \\ 1 & -2 & 1 \\ 3 & 6 & -5 \end{vmatrix} \\&= 1(4) - 1(-8) - 1(12) \\&= 4 + 8 - 12 = 0\end{aligned}$$

Hence, the system will have infinite solutions.

$$\begin{aligned}\text{Let } z &= k \\x + y &= -k \\x - 2y &= -k\end{aligned}$$

$$\begin{aligned}\text{or } \begin{bmatrix} 1 & 1 \\ 1 & -2 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} &= \begin{bmatrix} k \\ -k \end{bmatrix} \\ \text{or } A X &= B\end{aligned}$$

$|A| = -3 \neq 0$, hence A^{-1} exists.

$$\text{Now, } \text{adj } A = \begin{bmatrix} -2 & -1 \\ -1 & 1 \end{bmatrix} = \begin{bmatrix} -2 & -1 \\ -1 & 1 \end{bmatrix}$$

$$\begin{aligned}\text{Next } X &= A^{-1}B \\&= \frac{1}{|A|} (\text{adj } A)(B) = \frac{1}{-3} \begin{bmatrix} -2 & -1 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} k \\ -k \end{bmatrix} \\&= \frac{-1}{3} \begin{bmatrix} -2k + k \\ -2k \end{bmatrix} \\&= \frac{-1}{3} \begin{bmatrix} -k \\ -2k \end{bmatrix} = \begin{bmatrix} \frac{k}{3} \\ \frac{2k}{3} \end{bmatrix}\end{aligned}$$

$$\begin{aligned}\text{Hence, } x &= \frac{k}{3}, y = \frac{2k}{3}, z = k \\ \text{or } x &= k, y = 2k, z = 3k\end{aligned}$$

$$3x + y - 2z = 0$$

$$x + y + z = 0$$

$$x - 2y + z = 0$$

$$\text{Hence, } |A| = \begin{vmatrix} 3 & 1 & -2 \\ 1 & 1 & 1 \\ 1 & -2 & 1 \end{vmatrix}$$

$$\begin{aligned} |A| &= 3(1+2) - 1(1-1) - 2(-3) \\ &= 9 - 0 + 6 \\ &= 15 \neq 0 \end{aligned}$$

Hence, the given system has only trivial solutions given by $x = y = z = 0$

Solution of Simultaneous Linear Equations Ex 8.2 Q8

$$2x + 3y - z = 0$$

$$x - y - 2z = 0$$

$$3x + y + 3z = 0$$

$$\text{Hence, } A = \begin{bmatrix} 2 & 3 & -1 \\ 1 & -1 & -2 \\ 3 & 1 & 3 \end{bmatrix}$$

$$|A| = \begin{vmatrix} 2 & 3 & -1 \\ 1 & -1 & -2 \\ 3 & 1 & 3 \end{vmatrix}$$

$$\begin{aligned} &= 2(-3+2) - 3(3+6) - 1(4) \\ &= -2 - 27 - 4 \\ &\neq 0 \end{aligned}$$

Hence, the system has only trivial solutions given by $x = y = z = 0$

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