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$$f(x) = |x - 3|$$

$$= \begin{cases} -(x - 3), & \text{if } x < 3 \\ x - 3, & \text{if } x \ge 3 \end{cases}$$

$$f(3) = 3 - 3 = 0$$
LHL
$$= \lim_{x \to 3^{-}} f(x)$$

$$= \lim_{h \to 0} f(3 - h)$$

$$= \lim_{h \to 0} 3 - (3 - h)$$

$$= \lim_{h \to 0} 0$$
RHL
$$= \lim_{h \to 0} f(x)$$

$$= \lim_{h \to 0} f(x)$$

$$= \lim_{h \to 0} f(3 + h)$$

$$= \lim_{h \to 0} 3 + h - 3$$

$$= 0$$

$$LHL = f(3) = RHL$$

$$f(x) is continuous at x = 3$$

(LHD at 
$$x = 3$$
) =  $\lim_{x \to 3^{-}} \frac{f(x) - f(3)}{x - 3}$   
=  $\lim_{h \to 0} \frac{f(3 - h) - f(3)}{3 - h - 3}$   
=  $\lim_{h \to 0} \frac{3 - (3 - h) - 0}{-h}$   
=  $\lim_{h \to 0} \frac{h}{-h}$ 

(RHD at 
$$x = 3$$
) =  $\lim_{x \to 3^+} \frac{f(x) - f(3)}{x - 3}$   
=  $\lim_{h \to 0} \frac{f(3 + h) - f(3)}{3 + h - 3}$   
=  $\lim_{h \to 0} \frac{3 + h - 3 - 0}{h}$   
=  $\lim_{h \to 0} \frac{h}{h}$   
= 1

(LHD at 
$$x = 3$$
)  $\neq$  (RHD at  $x = 3$ )

 $f(x) ext{ is continuous but not differentiable at } x = 3.$ 

$$f(x) = x^{\frac{1}{3}}$$
(LHD at  $x = 0$ ) =  $\lim_{x \to 0^+} \frac{f(x) - f(0)}{x - 0}$ 
=  $\lim_{h \to 0} \frac{f(0 - h) - f(0)}{0 - h - 0}$ 
=  $\lim_{h \to 0} \frac{(-h)^{\frac{1}{3}} - 0}{-h}$ 
=  $\lim_{h \to 0} \frac{(-h)^{\frac{1}{3}} - 0}{-h}$ 
=  $\lim_{h \to 0} \frac{(-1)^{\frac{1}{3}} h^{\frac{1}{3}}}{(-1) h}$ 
=  $\lim_{h \to 0} (-1)^{\frac{-2}{3}} h^{\frac{1}{3}}$ 
= Not defined

(RHD at  $x = 0$ ) =  $\lim_{h \to 0} \frac{f(x) - f(0)}{x - 0}$ 
=  $\lim_{h \to 0} \frac{f(0 + h) - f(0)}{0 + h - 0}$ 
=  $\lim_{h \to 0} \frac{h^{\frac{1}{3}} - 0}{h}$ 
=  $\lim_{h \to 0} h^{\frac{-2}{3}}$ 
= Not defined

Since,

LHD and RHD does not exists at x = 0

f(x) is not differentiable at x = 0

Chapter 10 Differentiability Ex 10.1 Q3

$$f(x) = \begin{cases} 12x - 13, & \text{if } x \le 3 \\ 2x^2 + 5, & \text{if } x > 3 \end{cases}$$

$$(LHD \text{ at } x = 3) = \lim_{x \to 3} \frac{f(x) - f(3)}{x - 3}$$

$$= \lim_{h \to 0} \frac{f(3 - h) - f(3)}{3 - h - 3}$$

$$= \lim_{h \to 0} \frac{36 - 12h - 13 - 36 + 13}{-h}$$

$$= \lim_{h \to 0} \frac{-12h}{-h}$$

$$= 12$$

$$(RHD \text{ at } x = 3) = \lim_{x \to 3^+} \frac{f(x) - f(3)}{x - 3}$$

$$= \lim_{h \to 0} \frac{f(3 + h) - f(3)}{x - 3}$$

$$= \lim_{h \to 0} \frac{2(3 + h^2) + 5 - [12(3) - 13]}{3 + h - 3}$$

$$= \lim_{h \to 0} \frac{18 + 12h + 2h^2 + 5 - 36 + 13}{h}$$

$$= \lim_{h \to 0} \frac{2h^2 + 12h}{h}$$

$$= \lim_{h \to 0} \frac{h(2h + 12)}{h}$$

$$= 12$$

Now,

$$(LHD at x = 3) = (RHD at x = 3)$$

f(x) is differentiable at x = 3f'(x) = 12

Chapter 10 Differentiability Ex 10.1 Q4

$$f(x) = \begin{cases} 3x - 2, & 0 < x \le 1 \\ 2x^2 - x, & 1 < x \le 2 \end{cases}$$

$$f(2) = 2(2)^2 - 2$$

$$= 8 - 2 = 6$$

$$LHL = \lim_{h \to 0} f(x)$$

$$= \lim_{h \to 0} [2(2 - h)^2 - (2 - h)]$$

$$= 8 - 2$$

$$= 6$$

RHL = 
$$\lim_{x \to 2^{+}} f(x)$$
  
=  $\lim_{h \to 0} f(2+h)$   
=  $\lim_{h \to 0} 5(2+h) - 4$   
= 6  
LHL =  $f(2)$  = RHL  
 $f(x)$  is continuous at  $x = 2$   
(LHD at  $x = 2$ ) =  $\lim_{x \to 2^{-}} \frac{f(x) - f(2)}{x - 2}$   
=  $\lim_{h \to 0} \frac{f(2-h) - f(2)}{2 - h - 2}$   
=  $\lim_{h \to 0} \frac{2(2-h)^{2} - (2-h) - [8-2]}{-h}$   
=  $\lim_{h \to 0} \frac{2h^{2} - 6h}{-h}$   
=  $\lim_{h \to 0} \frac{2h^{2} - 6h}{-h}$   
=  $\lim_{h \to 0} \frac{h(2h - 6)}{-h}$   
=  $\lim_{h \to 0} \frac{h(2h - 6)}{-h}$   
=  $\lim_{h \to 0} \frac{f(x) - f(2)}{x - 2}$   
=  $\lim_{h \to 0} \frac{f(2+h) - f(2)}{2 + h - 2}$   
=  $\lim_{h \to 0} \frac{[5(2+h) - 4] - [8-2]}{h}$   
=  $\lim_{h \to 0} \frac{10 + 5h - 4 - 6}{h}$ 

\*\*\*\*\*\*\*\*\* END \*\*\*\*\*\*\*