



Congruent Triangles Ex 10.6 Q4

Answer :

As we know that a triangle can only be formed if
The sum of two sides is greater than the third side.
Here we have 2 cm, 3 cm and 7 cm as sides.

If we add $2 + 3 = 5$

$5 < 7$ (Since 5 is less than 7)

Hence the sum of two sides is less than the third sides

So, the triangle will not exist.

Congruent Triangles Ex 10.6 Q5

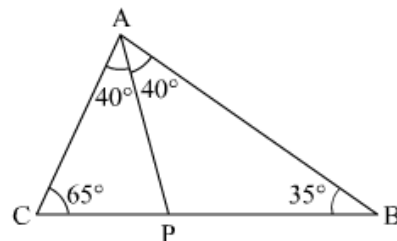
Answer :

It is given that

$$\angle B = 35^\circ$$

$$\angle C = 65^\circ$$

AP is the bisector of $\angle CAB$



We have to arrange AP , BP and CP in descending order.

In $\triangle ACP$ we have

$$\angle ACP = 65^\circ$$

$$\angle CAP = 40^\circ \text{ (As } AP \text{ is the bisector of } \angle CAB \text{)}$$

So $AP > CP$ (Sides in front of greater angle will be greater)(1)

In $\triangle ABP$ we have

$$\angle BAP = 40^\circ \text{ (As } AP \text{ is the bisector of } \angle CAB \text{)}$$

Since,

$$\angle BAP > \angle ABP$$

So $BP > AP$ (2)

Hence

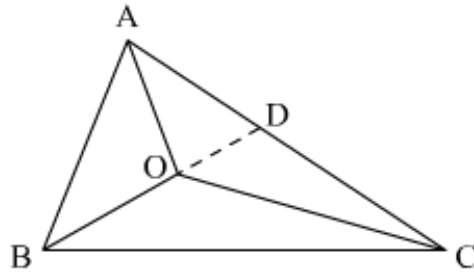
From (1) & (2) we have

$$\boxed{BP > AP > CP}$$

Congruent Triangles Ex 10.6 Q6

Answer :

It is given that, O is any point in the interior of $\triangle ABC$



We have to prove that

(1) $AB + AC > OB + OC$ Produced BO to meet AC at D .

In $\triangle ABD$ we have

$$AB + AD > BD$$

$$\Rightarrow AB + AD > OB + OD \quad \text{.....(1)}$$

And in $\triangle ODC$ we have

$$OD + CD > OC \quad \text{.....(2)}$$

Adding (1) & (2) we get

$$AB + AD + OD + DC > OB + OD + OC$$

Hence $\boxed{AB + AC > OB + OC}$ Proved.

(2) We have to prove that $AB + BC + CA > OA + OB + OC$

From the first result we have

$$BC + BA > OA + OC \quad \text{.....(3)}$$

And

$$CA + CB > OA + OB \quad \text{.....(4)}$$

Adding above (4) equation

$$2(AB + BC + CA) > 2(OA + OB + OC)$$

Hence $\boxed{AB + BC + CA > OA + OB + OC}$ Proved.

(3) We have to prove that $OA + OB + OC > \frac{1}{2}(AB + BC + CA)$

In triangles OAB , OBC and OCA we have

$$OA + OB > AB$$

$$OB + OC > BC$$

$$OC + OA > AC$$

Adding these three results

$$2(OA + OB + OC) > AB + BC + AC$$

Hence $\boxed{OA + OB + OC > \frac{1}{2}(AB + BC + CA)}$ Proved.

***** END *****