

## Trigonometric Identities Ex 6.1 Q48 Answer:

In the given question, we need to prove  $\frac{1}{\sec A + \tan A} - \frac{1}{\cos A} = \frac{1}{\cos A} - \frac{1}{\sec A - \tan A}$ 

Here, we will first solve the L.H.S.

Now, using 
$$\sec \theta = \frac{1}{\cos \theta}$$
 and  $\tan \theta = \frac{\sin \theta}{\cos \theta}$ , we get
$$\frac{1}{\sec A + \tan A} - \frac{1}{\cos A} = \frac{1}{\left(\frac{1}{\cos A} + \frac{\sin A}{\cos A}\right)} - \left(\frac{1}{\cos A}\right)$$

$$= \frac{1}{\left(\frac{1 + \sin A}{\cos A}\right)} - \left(\frac{1}{\cos A}\right)$$

$$= \left(\frac{\cos A}{1 + \sin A}\right) - \left(\frac{1}{\cos A}\right)$$

$$= \frac{\cos^2 A - (1 + \sin A)}{(1 + \sin A)(\cos A)}$$

On further solving, we get

$$\frac{\cos^2 A - (1+\sin A)}{(1+\sin A)(\cos A)} = \frac{\cos^2 A - 1 - \sin A}{(1+\sin A)(\cos A)}$$

$$= \frac{-\sin^2 A - \sin A}{(1+\sin A)(\cos A)} \qquad (Using \sin^2 \theta = 1 - \cos^2 \theta)$$

$$= \frac{-\sin A (\sin A + 1)}{(1+\sin A)(\cos A)}$$

$$= \frac{-\sin A}{\cos A}$$

$$= -\tan A$$

Similarly we solve the R.H.S.

Now, using 
$$\sec\theta = \frac{1}{\cos\theta}$$
 and  $\tan\theta = \frac{\sin\theta}{\cos\theta}$ , we get 
$$\frac{1}{\cos A} - \frac{1}{\sec A - \tan A} = \left(\frac{1}{\cos A}\right) - \frac{1}{\left(\frac{1}{\cos A} - \frac{\sin A}{\cos A}\right)}$$
$$= \left(\frac{1}{\cos A}\right) - \frac{1}{\left(\frac{1 - \sin A}{\cos A}\right)}$$
$$= \left(\frac{1}{\cos A}\right) - \left(\frac{\cos A}{1 - \sin A}\right)$$
$$= \frac{(1 - \sin A) - \cos^2 A}{(\cos A)(1 - \sin A)}$$

On further solving, we get

Contributes solving, we get
$$\frac{(1-\sin A)-\cos^2 A}{(\cos A)(1-\sin A)} = \frac{1-\sin A-\cos^2 A}{(\cos A)(1-\sin A)}$$

$$= \frac{\sin^2 A-\sin A}{(\cos A)(1-\sin A)}$$

$$= \frac{-\sin A(1-\sin A)}{(\cos A)(1-\sin A)}$$

$$= \frac{-\sin A}{\cos A}$$

$$= -\tan A$$
(Using  $\sin^2 \theta = 1-\cos^2 \theta$ )

So, L.H.S = R.H.S Hence proved.

\*\*\*\*\*\* END \*\*\*\*\*\*