



Continuity Ex 9.1 Q15

We want to discuss the continuity of the function at $x = 0$.

$$\text{LHL} = \lim_{x \rightarrow 0^-} f(x) = \lim_{h \rightarrow 0} f(0 - h) = \lim_{h \rightarrow 0} (-h) = 0$$

$$\text{RHL} = \lim_{x \rightarrow 0^+} f(x) = \lim_{h \rightarrow 0} f(0 + h) = \lim_{h \rightarrow 0} h = 0$$

$$f(0) = 1$$

Thus, $\text{LHL} = \text{RHL} \neq f(0)$

Hence, the function is discontinuous at $x = 0$. And this is removable discontinuity.

Continuity Ex 9.1 Q16

We want to discuss the continuity of the function at $x = \frac{1}{2}$.

$$\text{LHL} = \lim_{x \rightarrow \frac{1}{2}^-} f(x) = \lim_{h \rightarrow 0} f\left(\frac{1}{2} - h\right) = \lim_{h \rightarrow 0} \frac{1}{2} - h = \frac{1}{2}$$

$$\text{RHL} = \lim_{x \rightarrow \left(\frac{1}{2}\right)^+} f(x) = \lim_{h \rightarrow 0} f\left(\frac{1}{2} + h\right) = \lim_{h \rightarrow 0} 1 - \left(\frac{1}{2} + h\right) = \frac{1}{2}$$

$$f\left(\frac{1}{2}\right) = \frac{1}{2}$$

$$\text{Thus, } \text{LHL} = \text{RHL} = f\left(\frac{1}{2}\right) = \frac{1}{2}$$

Hence, the function is continuous at $x = \frac{1}{2}$.

Continuity Ex 9.1 Q17

We want to check the continuity of the function at $x = 0$.

$$\text{LHL} = \lim_{x \rightarrow 0^-} f(x) = \lim_{h \rightarrow 0} f(0 - h) = \lim_{h \rightarrow 0} 2(-h) - 1 = -1$$

$$\text{RHL} = \lim_{x \rightarrow 0^+} f(x) = \lim_{h \rightarrow 0} f(0 + h) = \lim_{h \rightarrow 0} 2h + 1 = 1$$

Thus, $\text{LHL} \neq \text{RHL}$

Hence, the function is discontinuous at $x = 0$. This is discontinuity of 1st kind.

Continuity Ex 9.1 Q18

We have given that the function is continuous at $x = 1$

$$\text{LHL} = \text{RHL} = f(1) \dots (1)$$

$$\text{Now, } \text{LHL} = \lim_{x \rightarrow 1^-} f(x) = \lim_{h \rightarrow 0} f(1 - h) = \lim_{h \rightarrow 0} \frac{(1 - h)^2 - 1}{(1 - h) - 1} = \lim_{h \rightarrow 0} \frac{h^2 - 2h}{-h} = 2$$

$$f(1) = k$$

$$\text{From } (1), \text{LHL} = f(1)$$

$$\therefore 2 = k$$

***** END *****

