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Exercise

1. An athlete completes one round of a circular track of diameter 200 m in 40 s. What will be the distance covered and the displacement at the end of 2 minutes 20 s?

Answer:

Diameter of circular track (D) = 200 m

Radius of circular track (r) = $200 / 2 = 100$ m

Time taken by the athlete for one round (t) = 40 s

Distance covered by athlete in one round (s) = $2\pi r$

$$= 2 \times (22 / 7) \times 100$$

Speed of the athlete (v) = Distance / Time

$$= (2 \times 2200) / (7 \times 40)$$

$$= 4400 / 7 \times 40$$

Therefore, Distance covered in 140 s = Speed (s) × Time(t)

$$= 4400 / (7 \times 40) \times (2 \times 60 + 20)$$

$$= 4400 / (7 \times 40) \times 140$$

$$= 4400 \times 140 / 7 \times 40$$

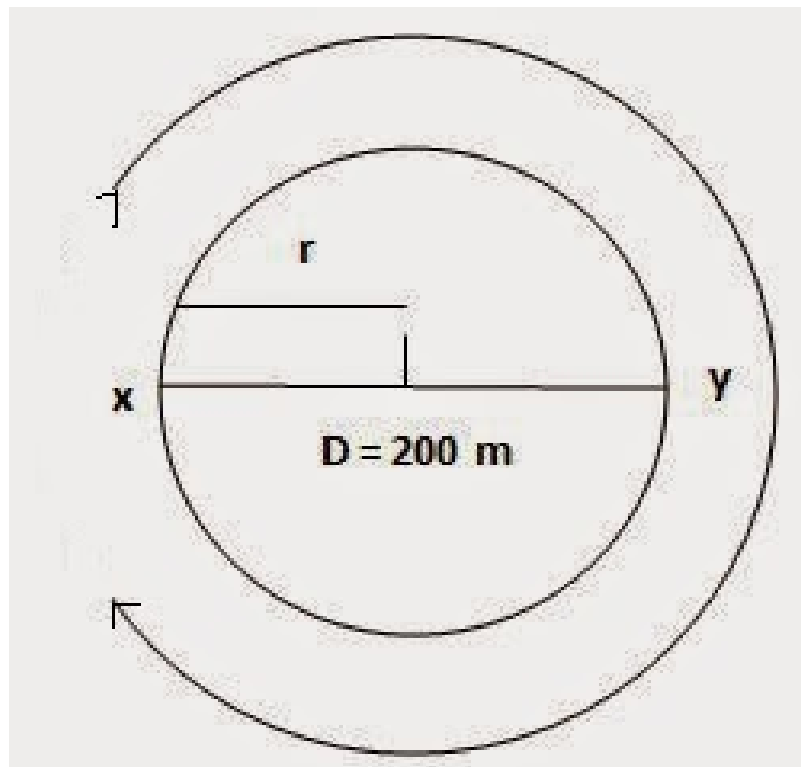
$$= 2200 \text{ m}$$

Number of round in 40 s = 1 round

Number of round in 140 s = $140 / 40$

$$= 3 \frac{1}{2}$$

After taking start from position X, the athlete will be at position Y after $3 \frac{1}{2}$ rounds as shown in figure



Hence, Displacement of the athlete with respect to initial position at

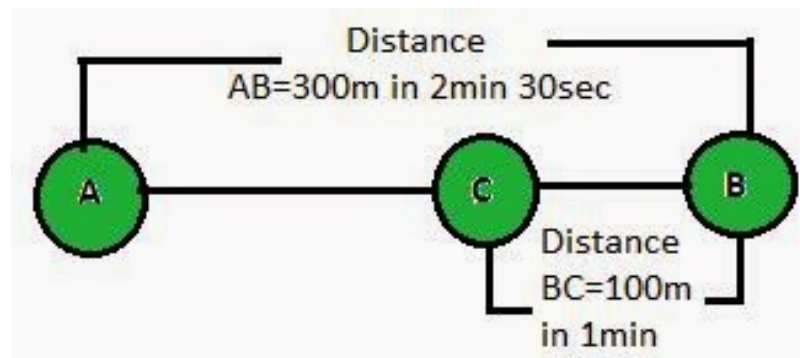
X = XY

= Diameter of circular track

= 200 m

2. Joseph jogs from one end A to the other end B of a straight 300 m road in 2 minutes 30 seconds and then turns around and jogs 100 m back to point C in another 1 minute. What are Joseph's average speeds and velocities in jogging (a) from A to B and (b) from A to C?

Answer: Total Distance covered from AB = 300 m
 Total time taken = $2 \times 60 + 30$ s
 = 150 s



Therefore, Average Speed from AB = Total Distance / Total Time
 = $300 / 150 \text{ m s}^{-1}$
 = 2 m s^{-1}
 Therefore, Velocity from AB = Displacement AB / Time = $300 / 150 \text{ m s}^{-1}$
 = 2 m s^{-1}
 Total Distance covered from AC = AB + BC
 = $300 + 100 \text{ m}$
 Total time taken from A to C = Time taken for AB + Time taken for BC
 = $(2 \times 60 + 30) + 60 \text{ s}$
 = 210 s
 Therefore, Average Speed from AC = Total Distance / Total Time
 = $400 / 210 \text{ m s}^{-1}$
 = 1.904 m s^{-1}
 Displacement (S) from A to C = AB - BC
 = $300 - 100 \text{ m}$
 = 200 m
 Time (t) taken for displacement from AC = 210 s
 Therefore, Velocity from AC = Displacement (s) / Time(t)
 = $200 / 210 \text{ m s}^{-1}$
 = 0.952 m s^{-1}

3. Abdul, while driving to school, computes the average speed for his trip to be 20 km h^{-1} . On his return trip along the same route, there is less traffic and the average speed is 40 km h^{-1} . What is the average speed for Abdul's trip?

Answer:

The distance Abdul commutes while driving from Home to School = S

Let us assume time taken by Abdul to commutes this distance = t_1

Distance Abdul commutes while driving from School to Home = S

Let us assume time taken by Abdul to commutes this distance = t_2

Average speed from home to school $v_{1av} = 20 \text{ km h}^{-1}$

Average speed from home to school $v_{2av} = 40 \text{ km h}^{-1}$

Also we know Time taken form Home to School $t_1 = S / v_{1av}$

Similarly Time taken form School to Home $t_2 = S / v_{2av}$

Total distance from home to school and backward = 2 S

Total time taken from home to school and backward (T) = $S/20 + S/40$

Therefore, Average speed (V_{av}) for covering total distance (2S) = Total Distance/Total Time

$$\begin{aligned}
&= 2S / (S/20 + S/30) \\
&= 2S / [(30S+20S)/600] \\
&= 1200S / 50S \\
&= 24 \text{ kmh}^{-1}
\end{aligned}$$

4. A motorboat starting from rest on a lake accelerates in a straight line at a constant rate of 3.0 m s^{-2} for 8.0 s . How far does the boat travel during this time?

Answer: Given Initial velocity of motorboat, $u = 0$

Acceleration of motorboat, $a = 3.0 \text{ m s}^{-2}$

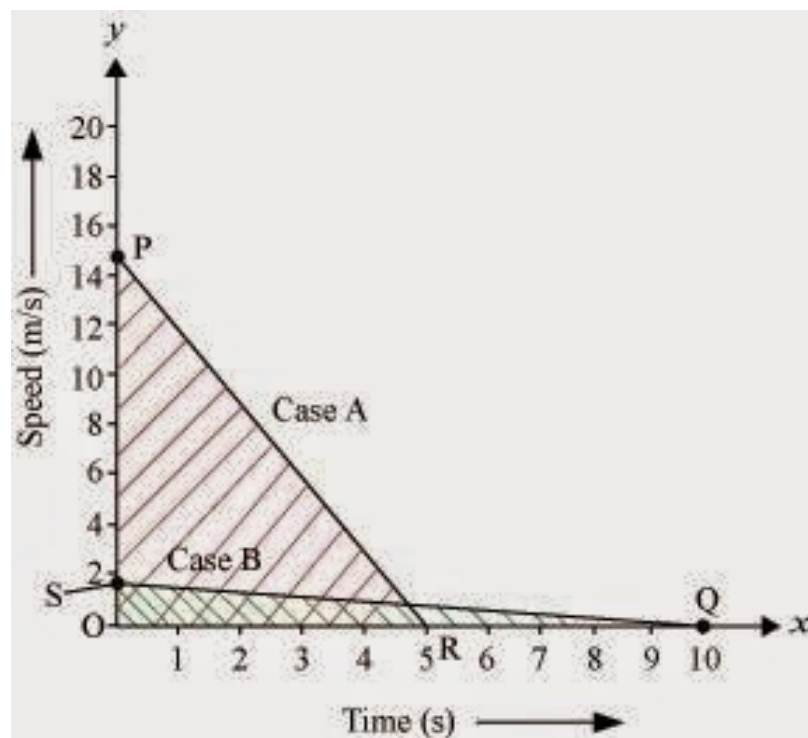
Time under consideration, $t = 8.0 \text{ s}$

We know that Distance, $s = ut + (1/2)at^2$

$$\begin{aligned}
\text{Therefore, The distance travel by motorboat} &= 0 \times 8 + (1/2)3.0 \times 8^2 \\
&= (1/2) \times 3 \times 8 \times 8 \text{ m} \\
&= 96 \text{ m}
\end{aligned}$$

5. A driver of a car travelling at 52 km h^{-1} applies the brakes and accelerates uniformly in the opposite direction. The car stops in 5 s . Another driver going at 3 km h^{-1} in another car applies his brakes slowly and stops in 10 s . On the same graph paper, plot the speed versus time graphs for the two cars. Which of the two cars travelled farther after the brakes were applied?

Answer: As given in the figure below PR and SQ are the Speed-time graph for given two cars with initial speeds 52 kmh^{-1} and 3 kmh^{-1} respectively.



Distance Travelled by first car before coming to rest = Area of triangle OPR

$$\begin{aligned}
&= (1/2) \times OR \times OP \\
&= (1/2) \times 5 \text{ s} \times 52 \text{ kmh}^{-1} \\
&= (1/2) \times 5 \times (52 \times 1000) / 3600 \text{ m} \\
&= (1/2) \times 5 \times (130 / 9) \text{ m} \\
&= 325 / 9 \text{ m} \\
&= 36.11 \text{ m}
\end{aligned}$$

Distance Travelled by second car before coming to rest = Area of triangle OSQ

$$\begin{aligned}
&= (1/2) \times OQ \times OS \\
&= (1/2) \times 10 \text{ s} \times 3 \text{ kmh}^{-1} \\
&= (1/2) \times 10 \times (3 \times 1000) / 3600 \text{ m} \\
&= (1/2) \times 10 \times (5/6) \text{ m} \\
&= 5 \times (5/6) \text{ m}
\end{aligned}$$

= 25/6 m
= 4.16 m

***** END *****