

Chapter 6 Determinants Ex 6.2 Q8

$$\begin{vmatrix} 0 & xy^2 & xz^2 \\ x^2y & 0 & yz^2 \\ x^2z & zy^2 & 0 \end{vmatrix}$$

$$= 0(0 - y^3z^3) - xy^2(0 - x^2yz^3) + xz^2(x^2y^3z - 0)$$

$$= 0 + x^3y^3z^3 + x^3y^3z^3$$

$$= 2x^3y^3z^3$$

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Let 
$$\Delta = \begin{vmatrix} a+x & y & z \\ x & a+y & z \\ x & y & a+z \end{vmatrix}$$

Applying 
$$R_1 \rightarrow R_1 - R_2$$
 and  $R_3 \rightarrow R_3 - R_2$ 

$$\Delta = \begin{vmatrix} a & -a & 0 \\ x & a+y & z \\ 0 & -a & a \end{vmatrix}$$

Applying 
$$C_2 \rightarrow C_2 + C_1$$

$$\Delta = \begin{vmatrix} a & 0 & 0 \\ x & a+x+y & z \\ 0 & -a & a \end{vmatrix}$$

$$\Delta = a[a(a+x+y)+az]+0+0$$

$$\Delta = a^2 (a + x + y + z)$$

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$$\Delta + \Delta_{1} = \begin{vmatrix} 1 & \times & \times^{2} \\ 1 & y & y^{2} \\ 1 & z & z^{2} \end{vmatrix} + \begin{vmatrix} 1 & 1 & 1 \\ yz & zx & xy \\ x & y & z \end{vmatrix}$$

$$= \begin{vmatrix} 1 & \times & \times^{2} \\ 1 & y & y^{2} \\ 1 & z & z^{2} \end{vmatrix} + \begin{vmatrix} 1 & yz & x \\ 1 & zx & y \\ 1 & xy & z \end{vmatrix} \dots \dots \left[ \because |A| = |A^{T}| \right]$$

$$= \begin{vmatrix} 1 & \times & \times^{2} \\ 1 & y & y^{2} \\ 1 & z & z^{2} \end{vmatrix} - \begin{vmatrix} 1 & \times & yz \\ 1 & y & zx \\ 1 & z & xy \end{vmatrix}$$

$$= \begin{vmatrix} 1 & \times & x^{2} \\ 1 & y & z^{2} \\ 1 & z & z^{2} \end{vmatrix} - \begin{vmatrix} 1 & x & yz \\ 1 & y & zx \\ 1 & z & xy \end{vmatrix}$$

 $\cdots \begin{bmatrix} \text{If any two rows (columns) of the determinant are interchanged} \\ \text{then value of the determinant changes in sign.} \end{bmatrix}$ 

$$= \begin{vmatrix} 0 & 0 & x^2 - yz \\ 0 & 0 & y^2 - zx \\ 0 & 0 & z^2 - xy \end{vmatrix}$$

= 0..... [ $\cdot \cdot C_1$  and  $C_2$  are identical]

Chapter 6 Determinants Ex 6.2 Q11

$$\begin{vmatrix} a & b & c \\ a-b & b-c & c-a \\ b+c & c+a & a+b \end{vmatrix} = a^3+b^3+c^3-3abc$$

$$\begin{vmatrix} a & b & c \\ a-b & b-c & c-a \\ b+c & c+a & a+b \end{vmatrix}$$

$$\begin{array}{lll} \text{Apply: } C_1 \to C_1 + C_2 + C_3, \\ & = \left| \begin{array}{cccc} a + b + c & b & c \\ & 0 & b - c & c - a \\ 2 \left( a + b + c \right) & c + a & a + b \end{array} \right| \end{array}$$

Take (a+b+c) common from  $C_1$ 

Apply: 
$$R_3 \rightarrow R_3 - 2R_1$$

$$= (a+b+c) \begin{vmatrix} 1 & b & c \\ 0 & b-c & c-a \\ 0 & c+a-2b & a+b-2c \end{vmatrix}$$
$$= (a+b+c)[(b-c)(a+b-2c)-(c-a)(c+a-2b)]$$

$$= a^3 + b^3 + c^3 - 3abc$$

\*\*\*\*\*\*\* END \*\*\*\*\*\*\*