



Exercise 11C

Question 31:

First term 'a' of an AP = 2

The last term l = 29

Sum of n terms = $S_n = \frac{n}{2}(a+l) = 155$

$$\therefore \frac{n}{2}(2+29) = 155$$

$$n = \frac{155 \times 2}{31} = 10$$

Also, $l = a + (n-1)d$

$$\text{or } 29 = 2 + (10-2)d = 2 + 9d$$

$$\Rightarrow 9d = 29 - 2 = 27 \therefore d = \frac{27}{9} = 3$$

\therefore common difference = 3

Question 32:

The given AP is $\left(1 - \frac{1}{n}\right) + \left(1 - \frac{2}{n}\right) + \left(1 - \frac{3}{n}\right) + \dots$

First term $a = 1 - \frac{1}{n}$

Common difference $d = \left(1 - \frac{2}{n}\right) - \left(1 - \frac{1}{n}\right) = -\frac{1}{n}$

Sum of n terms = $S_n = \frac{n}{2}[2a + (n-1)d]$

$$\begin{aligned} \therefore S_n &= \frac{n}{2} \left[2 \left(1 - \frac{1}{n} \right) + (n-1) \left(-\frac{1}{n} \right) \right] \\ &= \frac{n}{2} \left(2 - \frac{2}{n} - \frac{n-1}{n} \right) \\ &= \frac{n}{2} \left(1 - \frac{1}{n} \right) = \frac{n}{2} \times \frac{n-1}{n} = \frac{n-1}{2} \end{aligned}$$

Question 33:

TV production every year forms an AP

Let a be the TV production in first year and d be the common difference

Production in nth year = $a + (n-1)d$

production in 6th year = $a + 5d = 8000$

$$a + 5d = 8000 \text{ ----(1)}$$

Production in 9th year = $a + (9-1)d = 11300$

$$a + 8d = 11300 \text{ ----(2)}$$

Subtracting (1) from (2), we get

$$3d = 11300 - 8000 = 3300$$

$$\therefore d = \frac{3300}{3} = 1100$$

$$\text{From (1), } a + 5 \times 1100 = 8000$$

$$\Rightarrow a = 8000 - 5500 = 2500$$

$$\text{Production in } n^{\text{th}} \text{ year} = a + (n - 1)d$$

$$\begin{aligned} \therefore \text{Production in } 8^{\text{th}} \text{ year} &= 2500 + (8 - 1) \times 1100 \\ &= 2500 + 7700 = 10200 \end{aligned}$$

$$\text{Total Production in } n \text{ years} = \frac{n}{2}(a + l)$$

$$\begin{aligned} \therefore \text{Production in 6 years} &= \frac{6}{2}(2500 + 8000) \\ &= 3 \times 10500 = 31500 \end{aligned}$$

Thus,

(i) TV production in first year = 2500

(ii) Production in 8th year = 10200

(iii) Total production in 6 years = 31500.

Question 34:

Let the value of first prize be Rs. a

Subsequent prizes are Rs ($a - 200$), Rs ($a - 400$) and Rs ($a - 600$)

Total value of these prizes

$$\begin{aligned} &= \text{Rs}[a + (a - 200) + (a - 400) + (a - 600)] \\ &= \text{Rs}[4a - 1200] \end{aligned}$$

Value of these prizes = Rs. 2800 (given)

$$\therefore 4a - 1200 = 2800$$

$$4a = 2800 + 1200 = 4000$$

$$\therefore a = \frac{4000}{4} = 1000$$

Hence the first prize is Rs. 1000 and subsequent prizes are worth Rs. 800, Rs. 600 and Rs. 400.

Question 35:

Number of logs in 1st row (from bottom) = 20

Number of logs in 2nd row = 19

Number of logs in 3rd row = 18

Let there are n number of rows

20 + 19 + 18 + ... to n terms = 200

$$S_n = \frac{n}{2}[2a + (n - 1)d] = 200$$

$$\Rightarrow \frac{n}{2}[2 \times 20 + (n - 1) \times (-1)] = 200$$

$$\Rightarrow \frac{n}{2}[40 - n + 1] = 200$$

$$\Rightarrow \frac{n}{2}(41 - n) = 200 \text{ or } 41n - n^2 = 400$$

$$\Rightarrow n^2 - 41n + 400 = 0$$

$$\Rightarrow n^2 - 16n - 25n + 400 = 0$$

$$\Rightarrow n(n - 16) - 25(n - 16) = 0 \text{ or } (n - 16)(n - 25) = 0$$

$$\therefore n = 16 \text{ or } 25$$

For $n = 16$, number of logs in n th row

$$= a + (n - 1)d$$

$$= 20 + (16 - 1)(-1)$$

$$= 20 - 15$$

$$= 5$$

$n = 25$, since number of logs in 25th row is negative which is not admissible.

Thus, there are 16 rows and number of logs at the top is 5.

***** END *****