



Exercise 8

Question 1:

(i)

$$\frac{\sin 16^\circ}{\cos 74^\circ} = \frac{\sin(90^\circ - 74^\circ)}{\cos 74^\circ} = \frac{\cos 74^\circ}{\cos 74^\circ} = 1$$

$$[\because \sin(90^\circ - \theta) = \cos \theta]$$

(ii)

$$\frac{\sec 11^\circ}{\operatorname{cosec} 79^\circ} = \frac{\sec(90^\circ - 79^\circ)}{\operatorname{cosec} 79^\circ} = \frac{\operatorname{cosec} 79^\circ}{\operatorname{cosec} 79^\circ} = 1$$

(iii)

$$\frac{\tan 27^\circ}{\cot 63^\circ} = \frac{\tan(90^\circ - 63^\circ)}{\cot 63^\circ} = \frac{\cot 63^\circ}{\cot 63^\circ} = 1$$

$$[\because \tan(90^\circ - \theta) = \cot \theta]$$

(iv)

$$\frac{\cos 35^\circ}{\sin 55^\circ} = \frac{\cos 35^\circ}{\sin(90^\circ - 35^\circ)} = \frac{\cos 35^\circ}{\cos 35^\circ} = 1$$

(v)

$$\frac{\operatorname{cosec} 42^\circ}{\sec 48^\circ} = \frac{\operatorname{cosec} 42^\circ}{\sec(90^\circ - 42^\circ)} = \frac{\operatorname{cosec} 42^\circ}{\operatorname{cosec} 42^\circ} = 1$$

(vi)

$$\frac{\cot 38^\circ}{\tan 52^\circ} = \frac{\cot 38^\circ}{\tan(90^\circ - 38^\circ)} = \frac{\cot 38^\circ}{\cot 38^\circ} = 1$$

Question 2:

(i)

$$\sin \theta \cos(90^\circ - \theta) + \sin(90^\circ - \theta) \cos \theta \quad \left[\because \cos(90^\circ - \theta) = \sin \theta \text{ and } \sin(90^\circ - \theta) = \cos \theta \right]$$

$$\sin^2 \theta + \cos^2 \theta = 1$$

\therefore LHS = RHS

(ii)

$$\text{LHS} = \frac{\sin \theta}{\cos(90^\circ - \theta)} + \frac{\cos \theta}{\sin(90^\circ - \theta)}$$

$$[\because \sin(90^\circ - \theta) = \cos \theta \text{ and } \cos(90^\circ - \theta) = \sin \theta]$$

$$\Rightarrow \frac{\sin \theta}{\sin \theta} + \frac{\cos \theta}{\cos \theta} = 1 + 1 = 2 = \text{RHS}$$

\therefore LHS = RHS

(iii)

$$\text{LHS} = \frac{\sin \theta \cos (90^\circ - \theta) \cos \theta}{\sin (90^\circ - \theta)} + \frac{\cos \theta \sin (90^\circ - \theta) \sin \theta}{\cos (90^\circ - \theta)}$$

$$[\because \cos (90^\circ - \theta) = \sin \theta \text{ and } \sin (90^\circ - \theta) = \cos \theta]$$

$$= \frac{\sin^2 \theta \cos \theta}{\cos \theta} + \frac{\cos^2 \theta \sin \theta}{\sin \theta}$$

$$= \sin^2 \theta + \cos^2 \theta = 1 = \text{RHS}$$

$$\therefore \text{LHS} = \text{RHS}$$

(iv)

$$\begin{aligned} \text{LHS} &= \frac{\cos (90^\circ - \theta) \sec (90^\circ - \theta) \tan \theta}{\operatorname{cosec} (90^\circ - \theta) \sin (90^\circ - \theta) \cot (90^\circ - \theta)} + \frac{\tan (90^\circ - \theta)}{\cot \theta} \\ &= \frac{\sin \theta \cos \theta \tan \theta}{\sec \theta \cos \theta \tan \theta} + \frac{\cot \theta}{\cot \theta} \\ &= \frac{\sin \theta \times \frac{1}{\sin \theta}}{\frac{1}{\cos \theta} \times \cos \theta} + 1 = \frac{1}{1} + 1 = 2 = \text{RHS} \end{aligned}$$

$$\therefore \text{LHS} = \text{RHS}$$

(v)

$$\text{LHS} = \frac{\cos (90^\circ - \theta)}{1 + \sin (90^\circ - \theta)} + \frac{1 + \sin (90^\circ - \theta)}{\cos (90^\circ - \theta)}$$

$$[\because \sin (90^\circ - \theta) = \cos \theta \text{ and } \cos (90^\circ - \theta) = \sin \theta]$$

$$= \frac{\sin \theta}{1 + \cos \theta} + \frac{1 + \cos \theta}{\sin \theta} = \frac{\sin^2 \theta + (1 + \cos \theta)^2}{(1 + \cos \theta) \sin \theta}$$

$$= \frac{\sin^2 \theta + 1 + \cos^2 \theta + 2 \cos \theta}{(1 + \cos \theta) \sin \theta} = \frac{1 + 1 + 2 \cos \theta}{(1 + \cos \theta) \sin \theta}$$

$$= \frac{2(1 + \cos \theta)}{(1 + \cos \theta) \sin \theta} = \frac{2}{\sin \theta} = 2 \operatorname{cosec} \theta$$

$$\therefore \text{LHS} = \text{RHS}$$

***** END *****