

## Trigonometric Ratios of Compound Angles Ex 7.2 Q3

We have,

sin100° - sin10°

$$=\sqrt{2}\left(\frac{1}{\sqrt{2}}\times\sin 100^{\circ}-\frac{1}{\sqrt{2}}\times\cos 100^{\circ}\right) \hspace{1cm} \begin{bmatrix} \text{Multiplying and dividing} \\ \text{by } \sqrt{1^{2}+1^{2}} \text{ ie., by } \sqrt{2} \end{bmatrix}$$

- = √2 (cos 45° × sin 100° − sin 45° × cos 100°)
- $= \sqrt{2} (\sin 100^{\circ} \times \cos 45^{\circ} \cos 100^{\circ} \times \sin 45^{\circ})$
- $=\sqrt{2}\left(\sin(100^{\circ}-45^{\circ})\right)$
- =  $\sqrt{2}$  sin 55°, which is positive real number.

[∵ sinθ is positive in first quadrant]

Trigonometric Ratios of Compound Angles Ex 7.2 Q4

 $(2\sqrt{3}+3)\sin\theta+2\sqrt{3}\cos\theta$ 

as sume  $a=2\sqrt{3}+3$ ,  $b=2\sqrt{3}$ 

$$\sqrt{a^2+b^2} = \sqrt{12+9+12\sqrt{3}+12} = \sqrt{33+12\sqrt{3}}$$

Dividing and multiplying the above equation with above value

we get, 
$$\sqrt{33+12\sqrt{3}} \left( \frac{2\sqrt{3}+3}{\sqrt{33+12\sqrt{3}}} \sin \theta + \frac{2\sqrt{3}}{\sqrt{33+12\sqrt{3}}} \cos \theta \right)$$

Assume 
$$\tan \phi = \frac{a}{b}$$
, we have  $\sin \phi = \frac{a}{\sqrt{a^2 + b^2}}$ ,  $\cos \phi = \frac{b}{\sqrt{a^2 + b^2}}$ 

so above expressions changes to  $\sqrt{33+12\sqrt{3}}$  ( $\sin \phi \sin \theta + \cos \phi \cos \theta$ )

which is equal to 
$$\sqrt{33+12\sqrt{3}}\cos(\theta-\phi)$$

We know that maximum and minimum value of any cosine term is +1 and -1

$$\sqrt{33+12\sqrt{3}} = \sqrt{15+12+6+12\sqrt{3}}$$

we know that  $12\sqrt{3} + 6 < 12\sqrt{5}$  becasue value of  $\sqrt{5} - \sqrt{3}$  is more than 0.5

so if we replace  $12\sqrt{3} + 6$  with  $12\sqrt{5}$  the above inequality still holds

So range of above expression can be 
$$\sqrt{15+12+12\sqrt{5}} = 2\sqrt{3} + \sqrt{15}$$

$$-(2\sqrt{3}+\sqrt{15})<\sqrt{33+12\sqrt{3}}\cos{(\theta-\phi)}<2\sqrt{3}+\sqrt{15}$$

\*\*\*\*\*\*\*\*\* FND \*\*\*\*\*\*\*