

Exercise 20B

Q11.

Answer:

Curved surface area $=2\pi rh=4400~cm^2$ Circumference $=2\pi r=110~cm$ Now, height= $h=\frac{curved~surface~area}{circumference}=\frac{4400}{110}=40~cm$

Also, radius,
$$r = \frac{4400}{2\pi h} = \frac{4400 \times 7}{2 \times 22 \times 40} = \frac{35}{2}$$

$$\text{.. Volume} = \pi r^2 h = \frac{22}{7} \times \frac{35}{2} \times \frac{35}{2} \times 40 = 22 \times 5 \times 35 \times 10 = 38500 \text{ cm}^3$$

Q12.

Answer:

For the cubic pack: Length of the side, a = 5 cm Height = 14 cm Volume= $a^2h = 5 \times 5 \times 14 = 350$ cm³

For the cylindrical pack: Base radius = r = 3.5 cm Height = 12 cm Volume= $\pi r^2 h = \frac{22}{7} \times 3.5 \times 3.5 \times 12 = 462 \ cm^3$

We can see that the pack with a circular base has a greater capacity than the pack with a square base. Also, difference in volume= $462 - 350 = 112 \text{ cm}^3$

Q13.

Answer:

Diameter = 48 cm Radius = 24 cm = 0.24 m Height = 7 m

Now, we have:

Lateral surface area of one pillar= $\pi dh = \frac{22}{7} \times 0.48 \times 7 = 10.56 \text{ m}^2$ Surface area to be painted = total surface area of 15 pillars = $10.56 \times 15 = 158.4 \text{ m}^2$ \therefore Total cost= Rs (158.4 \times 2.5) = Rs 396

Q14.

Answer:

Volume of the rectangular vessel = $22 \times 16 \times 14 = 4928~cm^3$ Radius of the cylindrical vessel = 8 cm Volume= $\pi r^2 h$

As the water is poured from the rectangular vessel to the cylindrical vessel, we have: Volume of the rectangular vessel = volume of the cylindrical vessel

$$\therefore$$
 Height of the water in the cylindrical vessel= $\frac{volume}{\pi t^2} = \frac{4928 \times 7}{22 \times 8 \times 8} = \frac{28 \times 7}{8} = \frac{49}{2} = 24.5 \ cm$

Q15.

Answer:

Diameter of the given wire = 1 cm

Radius = 0.5 cm

Length = 11 cm

Now, volume=
$$\pi \mathbf{r}^2 \mathbf{h} = \frac{22}{7} \times 0.5 \times 0.5 \times 11 = 8.643~\text{cm}^3$$

The volumes of the two cylinders would be the same.

Now, diameter of the new wire = 1 mm = 0.1 cm

Radius = 0.05 cm

$$\therefore$$
 New length $=\frac{\mathrm{volume}}{\mathrm{rr}^2}=\frac{8.643\times7}{22\times0.05\times0.05}=1100.02~cm$ \cong 11 m $^{\circ}$

Q16.

Answer:

Length of the edge, a = 2.2 cmVolume of the cube $= a^3 = (2.2)^3 = 10.648 \text{ cm}^3$ Volume of the wire= $\pi r^2 h$ Radius = 1 mm = 0.1 cm As volume of cube = volume of wire, we have:

$$h = \frac{\text{volume}}{m^2} = \frac{10.648 \times 7}{22 \times 0.1 \times 0.1} = 338.8 \text{ cm}$$

Answer:

Diameter = 7 m

Radius = 3.5 m

Depth = 20 m

Volume of the earth dug out $= \pi r^2 h = \frac{22}{7} \times 3.5 \times 3.5 \times 20 = 770 \text{ m}^3$ Volume of the earth piled upon the given plot= $28 \times 11 \times h = 770 \text{ m}^3$

$$h = \frac{770}{28 \times 11} = \frac{70}{28} = 2.5 m$$

Q18.

Answer:

Inner diameter = 14 m

i.e., radius = 7 m

Depth = 12 m

Volume of the earth dug out= $\pi r^2 h = \frac{22}{7} \times 7 \times 7 \times 12 = 1848~m^3$

Width of embankment = 7 m

Now, total radius = 7 + 7 = 14 m

Volume of the embankment = total volume - inner volume

$$=\pi r_0^2 h - \pi r_i^2 h = \pi h (r_0^2 - r_i^2)$$

$$=\frac{22}{7} \mathbf{h} \Big(14^2 - 7^2 \Big) = \frac{22}{7} \mathbf{h} (196 - 49)$$

$$=\frac{22}{7}\,\mathbf{h} \times 147 = 21 \times 22\mathbf{h}$$

$$=462 \times h m^3$$

Since volume of embankment = volume of earth dug out, we have:

$$1848 = 462 h$$

$$\Rightarrow h = \frac{1848}{462} = 4 \; m$$

: Height of the embankment = 4 m

Q19.

Answer:

Diameter = 84 cm

i.e., radius = 42 cm

Length = 1 m = 100 cm

Now, lateral surface area $=2\pi rh=2 imes \frac{22}{7} imes 42 imes 100=26400~cm^2$

:. Area of the road

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= lateral surface area \times no. of rotations = 26400 \times 750 = 19800000~\text{cm}^2 = 1980~\text{m}^2
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Q20.

Answer:

Thickness of the cylinder = 1.5 cm External diameter = 12 cm i.e., radius = 6 cm also, internal radius = 4.5 cm Height = 84 cm

Now, we have the following: $\begin{array}{l} \text{Total volume} = \pi r^2 h = \frac{22}{7} \times 6 \times 6 \times 84 = 9504 \ \text{cm}^3 \\ \text{Inner volume} = \pi r^2 h = \frac{22}{7} \times 4.5 \times 4.5 \times 84 = 5346 \ \text{cm}^3 \\ \text{Now, volume of the metal = total volume - inner volume} = 9504 - 5346 = 4158 \ \text{cm}^3 \\ \therefore \text{ Weight of iron} = 4158 \times 7.5 = 31185 \ \text{g} = 31.185 \ \text{kg} \ \text{ [Given: 1 } \text{cm}^3 = 7.5\text{g}] \\ \end{array}$

Q21.

Answer:

Length = 1 m = 100 cm
Inner diameter = 12 cm
Radius = 6 cm
Now, inner volume= $\pi \mathbf{r}^2 \mathbf{h} = \frac{22}{7} \times 6 \times 6 \times 100 = 11314.286 \ \mathbf{cm}^3$
Thickness = 1 cm
Total radius = 7 cm

Now, we have the following:

Total volume = $\pi r^2 h = \frac{22}{7} \times 7 \times 7 \times 100 = 15400 \text{ cm}^3$ Volume of the tube = total volume - inner volume = $15400 - 11314.286 = 4085.714 \text{ cm}^3$

Density of the tube = 7.7 g/cm³ \therefore Weight of the tube = $\mathbf{volume} \times \mathbf{density} = 4085.714 \times 7.7 = 31459.9978 \ \mathbf{g} = 31.459 \ \mathbf{kg}$

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