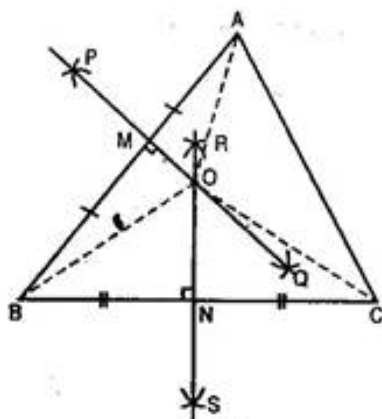




NCERT solutions for class 9 Maths Triangles Ex 7.5

Q1. ABC is a triangle. Locate a point in the interior of $\triangle ABC$ which is equidistant from all the vertices of $\triangle ABC$.

Ans. Let ABC be a triangle.



Draw perpendicular bisectors PQ and RS of sides AB and BC respectively of triangle ABC. Let PQ bisect AB at M and RS bisect BC at point N.

Let PQ and RS intersect at point O.

Join OA, OB and OC.

Now in $\triangle AOM$ and $\triangle BOM$,

$AM = MB$ [By construction]

$\angle AMO = \angle BMO = 90^\circ$ [By construction]

$OM = OM$ [Common]

$\therefore \triangle AOM \cong \triangle BOM$ [By SAS congruency]

$\Rightarrow OA = OB$ [By C.P.C.T.](i)

Similarly, $\triangle BON \cong \triangle CON$

$\Rightarrow OB = OC$ [By C.P.C.T.](ii)

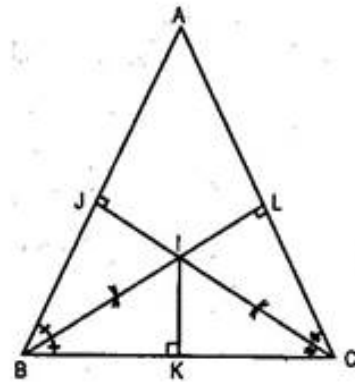
From eq. (i) and (ii),

$OA = OB = OC$

Hence O, the point of intersection of perpendicular bisectors of any two sides of $\triangle ABC$ equidistant from its vertices.

Q2. In a triangle locate a point in its interior which is equidistant from all the sides of the triangle.

Ans. Let ABC be a triangle.



Draw bisectors of $\angle B$ and $\angle C$.

Let these angle bisectors intersect each other at point I.

Draw $IK \perp BC$

Also draw $IJ \perp AB$ and $IL \perp AC$.

Join AI.

In $\triangle BIK$ and $\triangle BIJ$,

$$\angle IKB = \angle IJB = 90^\circ \text{ [By construction]}$$

$$\angle IBK = \angle IBJ$$

[\because BI is the bisector of $\angle B$ (By construction)]

$$BI = BI \text{ [Common]}$$

$$\therefore \triangle BIK \cong \triangle BIJ \text{ [ASA criteria of congruency]}$$

$$\therefore IK = IJ \text{ [By C.P.C.T.](i)}$$

Similarly, $\triangle CIK \cong \triangle CIL$

$$\therefore IK = IL \text{ [By C.P.C.T.](ii)}$$

From eq (i) and (ii),

$$IK = IJ = IL$$

Hence, I is the point of intersection of angle bisectors of any two angles of $\triangle ABC$ equidistant from its sides.

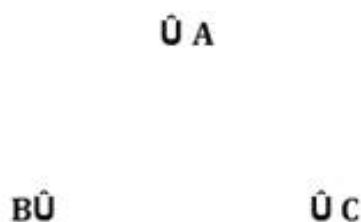
Q3. In a huge park, people are concentrated at three points (See figure).

A: where there are different slides and swings for children.

B: near which a man-made lake is situated.

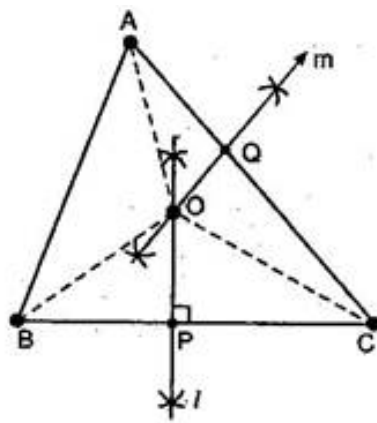
C: which is near to a large parking and exit.

Where should an ice cream parlour be set up so that maximum number of persons can approach it?



Ans. The parlour should be equidistant from A, B and C.

For this let we draw perpendicular bisector say l of line joining points B and C also draw perpendicular bisector say m of line joining points A and C.



Let l and m intersect each other at point O.

Now point O is equidistant from points A, B and C.

Join OA, OB and OC.

Proof: In $\triangle BOP$ and $\triangle COP$,

$OP = OP$ [Common]

$\angle OPB = \angle OPC = 90^\circ$

$BP = PC$ [P is the mid-point of BC]

$\therefore \triangle BOP \cong \triangle COP$ [By SAS congruency]

$\Rightarrow OB = OC$ [By C.P.C.T.](i)

Similarly, $\triangle AOQ \cong \triangle COQ$

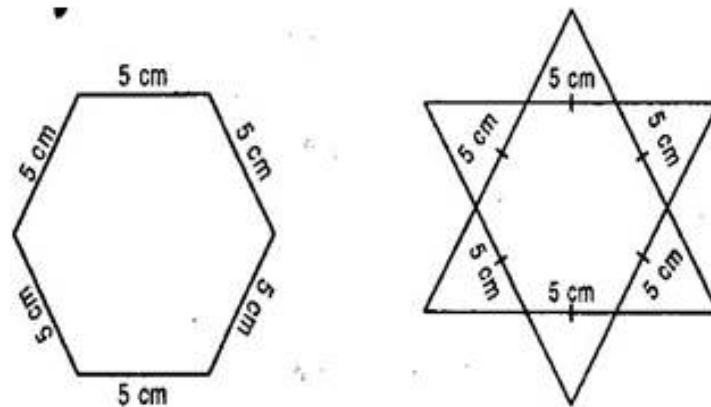
$\Rightarrow OA = OC$ [By C.P.C.T.](ii)

From eq. (i) and (ii),

$OA = OB = OC$

Therefore, ice cream parlour should be set up at point O, the point of intersection of perpendicular bisectors of any two sides out of three formed by joining these points.

Q4. Complete the hexagonal rangoli and the star rangolis (See figure) but filling them with as many equilateral triangles of side 1 cm as you can. Count the number of triangles in each case. Which has more triangles?



Ans. In hexagonal rangoli, Number of equilateral triangles each of side 5 cm are 6.

$$\begin{aligned}\text{Area of equilateral triangle} &= \frac{\sqrt{3}}{4} (\text{side})^2 = \frac{\sqrt{3}}{4} (5)^2 \\ &= \frac{\sqrt{3}}{4} \times 25 \text{ sq. cm}\end{aligned}$$

Area of hexagonal rangoli = 6 x Area of an equilateral triangle

$$= 6 \times \frac{\sqrt{3}}{4} \times 25 = 150 \times \frac{\sqrt{3}}{4} \text{ sq. cm(i)}$$

Now area of equilateral triangle of side 1 cm =

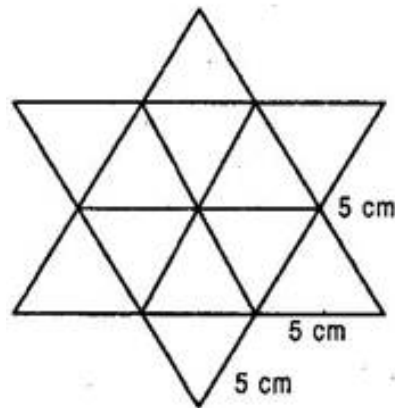
$$\frac{\sqrt{3}}{4} (\text{side})^2 = \frac{\sqrt{3}}{4} (1)^2 = \frac{\sqrt{3}}{4} \text{ sq. cm(ii)}$$

Number of equilateral triangles each of side 1 cm in hexagonal rangoli

$$= 150 \times \frac{\sqrt{3}}{4} \div \frac{\sqrt{3}}{4} = 150 \times \frac{\sqrt{3}}{4} \times \frac{4}{\sqrt{3}} = 150 \dots\dots(\text{iii})$$

Now in Star rangoli,

Number of equilateral triangles each of side 5 cm
= 12



Therefore, total area of star rangoli = 12 \times Area of an equilateral triangle of side 5 cm

$$= 12 \times \left(\frac{\sqrt{3}}{4} (5)^2 \right)$$

$$= 12 \times \frac{\sqrt{3}}{4} \times 25$$

$$= 300 \frac{\sqrt{3}}{4} \text{ sq. cm } \dots\dots\dots(\text{iv})$$

Number of equilateral triangles each of side 1 cm in star rangoli

$$= 300 \frac{\sqrt{3}}{4} \div \frac{\sqrt{3}}{4}$$

$$= 300 \frac{\sqrt{3}}{4} \times \frac{4}{\sqrt{3}}$$

$$= 300 \dots\dots\dots(\text{v})$$

From eq. (iii) and (v), we observe that star rangoli has more equilateral triangles each of side 1 cm.

***** END *****