

## Polynomials Ex 2.3 Q1

## Answer:

$$f(x) = x^3 - 6x^2 + 11x - 6$$

$$g(x) = x^2 + x + 1$$

Here, degree [f(x)]=3 and

Degree 
$$(g(x))=2$$

Therefore, quotient q(x) is of degree 3-2=1 and the remainder r(x) is of degree less than 2

Let 
$$q(x) = ax + b$$
 and

$$r(x) = cx + d$$

Using division algorithm, we have

$$f(x) = g(x) \times q(x) + r(x)$$

$$x^3 - 6x^2 + 11x - 6 = (x^2 + x + 1)(ax + b) + cx + d$$

$$x^3 - 6x^2 + 11x - 6 = ax^3 + ax^2 + ax + bx^2 + bx + b + cx + d$$

$$x^3 - 6x^2 + 11x - 6 = ax^3 + ax^2 + bx^2 + ax + bx + cx + b + d$$

$$x^3 - 6x^2 + 11x - 6 = ax^3 + (a+b)x^2 + (a+b+c)x + b + d$$

Equating the co-efficients of various powers of x on both sides, we get

On equating the co-efficient of  $\chi^3$ 

$$x^3 = ax^3$$

$$\chi^{\delta} = a \chi^{\delta}$$

$$1 = a$$

On equating the co-efficient of  $\chi^2$ 

$$-6x^2 = (a+b)x^2$$

$$-6 \cancel{x} = (a+b) \cancel{x}$$

$$-6 = a + b$$

Substituting a = 1

$$-6 = 1 + b$$

$$-6 - 1 = b$$

$$-7 = b$$

On equating the co-efficient of x

$$11x = (a+b+c)x$$

$$11 \cancel{x} = (a+b+c)\cancel{x}$$

$$11 = a + b + c$$

Substituting a = 1; and b = -7 we get,

$$11 = 1 + (-7) + c$$

$$11 = -6 + c$$

$$11 + 6 = c$$

$$17 = c$$

On equating the constant terms

$$-6 = b + d$$

Substituting b = -7 we get,

$$-6 = -7 + d$$

$$-6+7=d$$

$$1=d$$
Therefore,
Quotient  $q(x)=ax+b$ 

$$=(1x-7)$$
And remainder  $r(x)=cx+d$ 

$$=(17x+1)$$
Hence, the quotient and remainder is given by,
$$q(x)=(x-7)$$

$$r(x)=17x+1$$

$$(ii) \text{ We have}$$

$$f(x)=10x^4+17x^3-62x^2+30x-3$$

$$g(x)=2x^2+7x+1$$
Here, Degree  $(f(x))=4$  and
Degree  $(g(x))=2$ 
Therefore, quotient  $q(x)$  is of degree  $4-2=2$  and remainder  $r(x)$  is of degree less than  $2$ 

$$(=\deg ree(g(x)))$$
Let  $g(x)=ax^2+bx+c$  and
$$r(x)=px+q$$
Using division algorithm, we have

b = -9

Sing division algorithm, we have 
$$f(x) = g(x) \times q(x) + r(x)$$

$$10x^4 + 17x^3 - 62x^2 + 30x - 3 = (2x^2 + 7x + 1)(ax^2 + bx + c) + px + q$$

$$10x^4 + 17x^3 - 62x^2 + 30x - 3 = 2ax^4 + 7ax^3 + ax^2 + 2bx^3 + 7bx^2 + bx + 2cx^2 + 7xc + c + px + q$$

$$10x^4 + 17x^3 - 62x^2 + 30x - 3 = 2ax^4 + 7ax^3 + 2bx^3 + ax^2 + 7bx^2 + 2cx^2 + bx + 7xc + px + c + q$$

$$10x^4 + 17x^3 - 62x^2 + 30x - 3 = 2ax^4 + x^3(7a + 2b) + x^2(a + 7b + 2c) + x(b + 7c + p) + c + q$$
Equating the co-efficients of various powers  $x$  on both sides, we get

On equating the co-efficient of  $x^4$ 

$$2a = 10$$

$$a = \frac{10}{2}$$

$$a = 5$$
On equating the co-efficient of  $x^3$ 

$$7a + 2b = 17$$
Substituting  $a = 5$  we get
$$7 \times 5 + 2b = 17$$

$$2b = 17 - 35$$

$$2b = -18$$

$$b = \frac{-18}{2}$$

\*\*\*\*\*\*\* END \*\*\*\*\*\*