



Surface Areas and Volumes Ex.16.1 Q4

Answer :

The brass volume that has to be drawn into a cylindrical wire is given is $2.2 \text{ dm}^3 = 2.2 \times 10^{-3} \text{ m}^3$

We have to make a cylindrical wire out of it with diameter = 0.25 cm

So the radius of this wire $0.125 \times 10^{-2} \text{ m}$

We have to find the length of this wire.

Let the length of this wire be h

We know that the volume of a cylinder $= \pi r^2 h$.

We know, the volume of the cylinder should be equal to the volume of the given brass

$$\Rightarrow \pi (0.125 \times 10^{-2})^2 \times h = 2.2 \times 10^{-3}$$

$$\begin{aligned} h &= \frac{2.2 \times 10^{-3} \times 10^4}{\pi \times .125 \times .125} \\ &= \frac{22 \times 7}{22 \times .125 \times .125} \\ &= \frac{4 \times 7}{.25 \times .25} \\ &= 448 \end{aligned}$$

Therefore, $h = 448 \text{ m}$

Hence, the length of the cylindrical wire that can be formed is 448 m

Surface Areas and Volumes Ex.16.1 Q5

Answer :

We are given a solid cylinder of, diameter = 2 cm

We have to recast it into a hollow cylinder of length = 16 cm

External Diameter = 20 cm and thickness = 2.5 mm = 0.25 cm

We have to find the height of the solid cylinder that can be used to get a hollow cylinder of the desired dimensions.

Volume of a solid cylinder $= \pi r^2 h$

So,

The volume of the given solid cylinder $= \pi (1)^2 h$ (a)

Here, height h has to be found.

Volume of a hollow cylinder $= \pi h (R^2 - r^2)$

Where R is the external radius and r is the internal radius

External radius is given. Thickness of the hollow cylinder is also given.

So, we can find the internal radius of the hollow cylinder.

Thickness $= R - r$

$$\Rightarrow 0.25 = 10 - r$$

$$\Rightarrow r = 9.75 \text{ cm}$$

So, the volume of the hollow cylinder $= \pi \times 16 \times (100 - 95.0625)$ (b)

From (a) and (b) we get,

$$\pi (1)^2 h = \pi \times 16 \times (100 - 95.0625)$$

$$\cancel{\pi} h = \cancel{\pi} \times 16 \times (100 - 95.0625)$$

$$h = 16 \times (4.9375)$$

$$h = 79 \text{ cm}$$

Hence, the required height of the solid cylinder is $h = 79 \text{ cm}$

Surface Areas and Volumes Ex.16.1 Q6

Answer :

A cylindrical vessel whose height is equal to its diameter is given.

It is filled with water.

We know that the volume of a cylinder $= \pi r^2 h$

In this particular case,

Height is equal to the diameter, that is $h = 2r$,

The volume of cylindrical vessel becomes $= 2\pi r^3$

The water from this vessel is transferred into two identical cylindrical vessels of

Diameter = 42 cm and, height $h = 21$ cm

Volume of each vessel $= \pi (21)^2 \times 21$

We know that the sum of the volumes of the two identical vessels must be equal to the volume of the given cylindrical vessel.

$$\Rightarrow 2\pi r^3 = 2 \times (\pi (21)^2 \times 21)$$

$$r^3 = (21)^3$$

Therefore, $r = 21$

The diameter of the given cylinder is 42 cm

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