

Algebra of Matrices Ex 5.3 Q18 Given,

A =
$$\begin{bmatrix} 1 & 0 & -2 \\ 3 & -1 & 0 \\ -2 & 1 & 1 \end{bmatrix}$$
, B = $\begin{bmatrix} 0 & 5 & -4 \\ -2 & 1 & 3 \\ -1 & 0 & 2 \end{bmatrix}$
C = $\begin{bmatrix} 1 & 5 & 2 \\ -1 & 1 & 0 \\ 0 & -1 & 1 \end{bmatrix}$
A(B-C) = $\begin{bmatrix} 1 & 0 & -2 \\ 3 & -1 & 0 \\ -2 & 1 & 1 \end{bmatrix}$, D = $\begin{bmatrix} 0 & 5 & -4 \\ -2 & 1 & 3 \\ -1 & 0 & 2 \end{bmatrix}$, D = $\begin{bmatrix} 1 & 0 & -2 \\ -2 & 1 & 1 \end{bmatrix}$, D = $\begin{bmatrix} 1 & 0 & -2 \\ -2 & 1 & 1 \end{bmatrix}$, D = $\begin{bmatrix} 1 & 0 & -2 \\ 3 & -1 & 0 \\ -2 & 1 & 1 \end{bmatrix}$, D = $\begin{bmatrix} 1 & 0 & -2 \\ -2 + 1 & 1 - 1 & 3 - 0 \\ -2 & 1 & 1 \end{bmatrix}$, D = $\begin{bmatrix} 1 & 0 & -2 \\ -2 + 1 & 1 - 1 & 3 - 0 \\ -2 & 1 & 1 \end{bmatrix}$, D = $\begin{bmatrix} 1 & 0 & -2 \\ -2 + 1 & 1 & 1 \end{bmatrix}$, D = $\begin{bmatrix} 1 & 0 & -2 \\ -2 & 1 & 1 \end{bmatrix}$, D = $\begin{bmatrix} 1 & 0 & -2 \\ -3 & -1 & 0 \\ -2 & 1 & 1 \end{bmatrix}$, D = $\begin{bmatrix} 1 & 0 & -2 \\ -3 & -1 & 0 \\ -2 & 1 & 1 \end{bmatrix}$, D = $\begin{bmatrix} -1 & 0 & -6 \\ -1 & 0 & 3 \\ -2 & 1 & 1 \end{bmatrix}$, D = $\begin{bmatrix} -1 & 0 & -6 \\ -1 & 0 & 3 \\ -2 & 1 & 1 \end{bmatrix}$, D = $\begin{bmatrix} -1 & 0 & -6 \\ -1 & 0 & 3 \\ -2 & 1 & 1 \end{bmatrix}$, D = $\begin{bmatrix} -1 & 0 & -6 \\ -1 & 0 & 3 \\ -2 & 1 & 1 \end{bmatrix}$, D = $\begin{bmatrix} -1 & 0 & -6 \\ -1 & 0 & 3 \\ -2 & 1 & 1 \end{bmatrix}$, D = $\begin{bmatrix} -1 & 0 & -2 \\ -3 & -1 & 0 \\ -2 & 1 & 3 \end{bmatrix}$, D = $\begin{bmatrix} 1 & 5 & 2 \\ 3 & -1 & 0 \\ -2 & 1 & 1 \end{bmatrix}$, D = $\begin{bmatrix} 1 & 0 & -2 \\ -2 & 1 & 1 \end{bmatrix}$,

Algebra of Matrices Ex 5.3 Q19

A(B-C) = AB - AC

Given,

$$A = \begin{bmatrix} 0 & 1 & 0 \\ 2 & 0 & 2 \\ 0 & 3 & 2 \\ 4 & 0 & 4 \end{bmatrix} \begin{bmatrix} 2 & -1 \\ -3 & 2 \\ 4 & 3 \end{bmatrix} \begin{bmatrix} 0 & 1 & -1 & 2 & -2 \\ 3 & -3 & 4 & -4 & 0 \end{bmatrix}$$

$$A = \begin{bmatrix} 0 - 3 + 0 & 0 + 2 + 0 \\ 4 + 0 + 8 & -2 + 0 + 6 \\ 0 - 9 + 8 & 0 + 6 + 6 \\ 8 + 0 + 16 & -4 + 0 + 12 \end{bmatrix} \begin{bmatrix} 0 & 1 & -1 & 2 & -2 \\ 3 & -3 & 4 & -4 & 0 \end{bmatrix}$$

$$A = \begin{bmatrix} -3 & 2 \\ 12 & 4 \\ -1 & 12 \\ 24 & 8 \end{bmatrix} \begin{bmatrix} 0 & 1 & -1 & 2 & -2 \\ 3 & -3 & 4 & -4 & 0 \end{bmatrix}$$

$$A = \begin{bmatrix} 0 + 6 & -3 - 6 & 3 + 8 & -6 - 8 & 6 + 0 \\ 0 + 12 & 12 - 12 & -12 + 16 & 24 - 16 & -24 + 0 \\ 0 + 36 & -1 - 36 & 1 + 48 & -2 - 48 & 2 + 0 \\ 0 + 24 & 24 - 24 & -24 + 34 & 48 - 32 & -48 + 0 \end{bmatrix}$$

$$A = \begin{bmatrix} 6 & -9 & 11 & -14 & 6 \\ 12 & 0 & 4 & 8 & -24 \\ 36 & -37 & 49 & -50 & 2 \\ 24 & 0 & 8 & 16 & -48 \end{bmatrix}$$

Here,
$$a_{43} = 8, a_{22} = 0$$

Algebra of Matrices Ex 5.3 Q20 Given.

$$A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ p & q & r \end{bmatrix}$$

$$A^{2} = A \times A$$

$$= \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ p & q & r \end{bmatrix} \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ p & q & r \end{bmatrix}$$

$$= \begin{bmatrix} 0+0+0 & 0+0+0 & 0+1+0 \\ 0+0+p & 0+0+q & 0+0+r \\ 0+0+pr & p+0+qr & 0+q+r^{2} \end{bmatrix}$$

$$A^{3} = A^{2} \times A$$

$$= \begin{bmatrix} 0 & 0 & 1 \\ p & q & r \\ pr & p+qr & q+r^{2} \end{bmatrix} \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ p & q & r \end{bmatrix}$$

$$= \begin{bmatrix} 0+0+p & 0+0+q & 0+0+r \\ 0+0+pr & p+0+qr & 0+q+r^{2} \\ 0+0+pq+pr^{2} & pr+0+q^{2}+qr^{2} & 0+p+qr+qr+r^{2} \end{bmatrix}$$

$$A^{3} = \begin{bmatrix} p & q & r \\ pr & p+qr & q+r^{2} \end{bmatrix}$$

$$---(i)$$

$$pI + qA + rA^{2}$$

$$= p \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} + q \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ p & q & r \end{bmatrix} + r \begin{bmatrix} 0 & 0 & 1 \\ p & q & r \\ pr & p + qr & q + r^{2} \end{bmatrix}$$

$$= \begin{bmatrix} p + 0 + 0 & 0 + q + 0 & 0 + 0 + r \\ 0 + 0 + pr & p + 0 + qr & 0 + q + r^{2} \\ 0 + pq + pr^{2} & 0 + q^{2} + pr + qr^{2} & p + qr + qr + r^{2} \end{bmatrix}$$

 $pq+pr^2$ $pr+q^2+qr^2$ $p+2qr+r^2$

$$pI + qA + rA^{2}$$

$$= \begin{bmatrix} p & q & r \\ pr & p+qr & q+r^{2} \\ pq+pr^{2} & pr+q^{2}+qr^{2} & p+2qr+r^{2} \end{bmatrix}$$

********* END *******