



Triangles Ex 4.6 Q13

Answer :

GIVEN: In $\triangle ABC$, P divides the side AB such that $AP : PB = 1 : 2$, Q is a point on AC such that $PQ \parallel BC$.

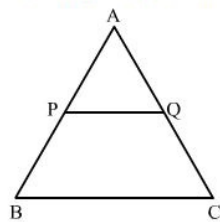
TO FIND: The ratio of the areas of $\triangle APQ$ and the trapezium BPQC.

In $\triangle APQ$ and $\triangle ABC$

$$\angle APQ = \angle B \quad (\text{Corresponding angles})$$

$$\angle PAQ = \angle BAC \quad (\text{Common})$$

So, $\triangle APQ \sim \triangle ABC$ (AA Similarity)



We know that the ratio of areas of two similar triangles is equal to the ratio of squares of their corresponding sides.

$$\begin{aligned} \frac{Ar(\triangle APQ)}{Ar(\triangle ABC)} &= \frac{AP^2}{AB^2} \\ \frac{Ar(\triangle APQ)}{Ar(\triangle ABC)} &= \frac{1x^2}{(1x + 2x)^2} \\ \frac{Ar(\triangle APQ)}{Ar(\triangle ABC)} &= \frac{1}{9} \end{aligned}$$

Let Area of $\triangle APQ = 1$ sq. units and Area of $\triangle ABC = 9x$ sq. units

$$\begin{aligned} Ar[\text{trap}BCED] &= Ar(\triangle ABC) - Ar(\triangle APQ) \\ &= 9x - 1x \\ &= 8x \text{ sq units} \end{aligned}$$

Now,

$$\frac{Ar(\triangle APQ)}{Ar(\text{trap}BCED)} = \frac{x \text{ sq units}}{8x \text{ sq units}} = \frac{1}{8}$$

Triangles Ex 4.6 Q14

Answer :

Given: The area of two similar triangles is 100cm^2 and 49cm^2 respectively. If the altitude of bigger triangle is 5 cm

To find: their corresponding altitude of other triangle

We know that the ratio of areas of two similar triangles is equal to the ratio of squares of their corresponding altitudes.

$$\begin{aligned} \frac{Ar(\text{bigger triangle1})}{Ar(\text{triangle2})} &= \left(\frac{\text{altitude of bigger triangle1}}{\text{altitude2}} \right)^2 \\ \frac{100}{49} &= \left(\frac{5}{\text{altitude2}} \right)^2 \end{aligned}$$

Taking square root on both side

$$\begin{aligned} \frac{10}{7} &= \frac{5}{\text{altitude2}} \\ \boxed{\text{altitude2} = 3.5 \text{ cm}} \end{aligned}$$

Triangles Ex 4.6 Q15

Answer :

Given: The area of two similar triangles is 121cm^2 and 64cm^2 respectively. IF the median of the first triangle is 12.1cm

To find: corresponding medians of the other triangle

We know that the ratio of areas of two similar triangles is equal to the ratio of squares of their medians.

$$\frac{ar(\text{triangle1})}{ar(\text{triangle2})} = \left(\frac{\text{median1}}{\text{median2}} \right)^2$$

$$\frac{121}{64} = \left(\frac{12.1}{\text{median2}} \right)^2$$

taking squareroot on bothside

$$\frac{11}{8} = \frac{12.1}{\text{median2}}$$

$$\boxed{\text{median 2} = 8.8\text{cm}}$$

***** END *****