

Quadratic Equations Ex 8.7 Q22

Answer:

Let the tens digit be x, then, the unit digits = $\frac{8}{x}$

Therefore, number
$$=$$
 $\left(10x + \frac{8}{x}\right)$

And number obtained by interchanging the digits = $\left(10 \times \frac{8}{x} + x\right)$

Then according to question

$$\left(10x + \frac{8}{x}\right) - \left(10 \times \frac{8}{x} + x\right) = 18$$

$$\left(10x + \frac{8}{x}\right) - \left(10 \times \frac{8}{x} + x\right) = 18$$

$$\frac{\left(10x^2 + 8\right) - \left(80 + x^2\right)}{x} = 18$$

$$\frac{10x^2 + 8 - 80 - x^2}{x} = 18$$

$$\frac{9x^2 - 72}{x} = 18$$

$$9x^2 - 72 = 18x$$

$$9x^2 - 18x - 72 = 0$$

$$9(x^2 - 2x - 8) = 0$$

$$x^{2}-2x-8=0$$

$$x^{2}-4x+2x-8=0$$

$$x(x-4)+2(x-4)=0$$

$$(x-4)(x+2)=0$$

$$(x-4)=0$$

$$x=4$$
Or
$$(x+2)=0$$

$$x=-2$$

So the digit can never be negative. Therefore,

When x = 4 then the unit digits is

$$=\frac{8}{x}$$
$$=\frac{8}{4}$$
$$=2$$

And therefore the number is

$$= \left(10x + \frac{8}{x}\right)$$
$$= \left(10 \times 4 + 2\right)$$
$$= 42$$

Thus, the required number be 42

$$x^{2}-2x-8=0$$

$$x^{2}-4x+2x-8=0$$

$$x(x-4)+2(x-4)=0$$

$$(x-4)(x+2)=0$$

$$(x-4)=0$$

$$x=4$$
Or
$$(x+2)=0$$

$$x=-2$$

So the digit can never be negative. Therefore,

When x = 4 then the unit digits is

$$=\frac{8}{x}$$
$$=\frac{8}{4}$$
$$=2$$

And therefore the number is

$$= \left(10x + \frac{8}{x}\right)$$
$$= \left(10 \times 4 + 2\right)$$
$$= 42$$

Thus, the required number be 4

Answer:

Let the tens digit be x then, the unit digits = $\frac{12}{x}$

Therefore, number = $\left(10x + \frac{12}{x}\right)$

And number obtained by interchanging the digits = $\left(10 \times \frac{12}{x} + x\right)$

Then according to question

$$\left(10x + \frac{12}{x}\right) + 36 = \left(10 \times \frac{12}{x} + x\right)$$

$$\left(10x + \frac{12}{x}\right) + 36 = \left(\frac{120}{x} + x\right)$$

$$\left(10x + \frac{12}{x}\right) - \left(\frac{120}{x} + x\right) + 36 = 0$$

$$\frac{\left(10x^2 + 12\right) - \left(120 + x^2\right) + 36x}{x} = 0$$

$$10x^2 + 12 - 120 - x^2 + 36x = 0$$

$$9\left(x^2 + 4x - 12\right) = 0$$

$$x^{2} + 4x - 12 = 0$$

$$x^{2} - 2x + 6x - 12 = 0$$

$$x(x-2) + 6(x-2) = 0$$

$$(x-2)(x+6) = 0$$

$$(x-2) = 0$$

$$x = 2$$
Or
$$(x+6) = 0$$

$$x = -6$$

So, the digit can never be negative.

Therefore,

When x = 2 then the unit digits

$$= \frac{12}{x}$$
$$= \frac{12}{2}$$
$$= 6$$

And number

$$= \left(10x + \frac{12}{x}\right)$$
$$= \left(10 \times 2 + 6\right)$$
$$= 26$$

Thus, the required number be 26

******* END ******