



Binary Operations Ex 3.1 Q2

(i) On \mathbf{Z}^+ , $*$ is defined by $a * b = a - b$.

It is not a binary operation as the image of $(1, 2)$ under $*$ is $1 * 2 = 1 - 2 = -1 \notin \mathbf{Z}^+$.

(ii) On \mathbf{Z}^+ , $*$ is defined by $a * b = ab$.

It is seen that for each $a, b \in \mathbf{Z}^+$, there is a unique element ab in \mathbf{Z}^+ .

This means that $*$ carries each pair (a, b) to a unique element $a * b = ab$ in \mathbf{Z}^+ . Therefore, $*$ is a binary operation.

(iii) On \mathbf{R} , $*$ is defined by $a * b = ab^2$.

It is seen that for each $a, b \in \mathbf{R}$, there is a unique element ab^2 in \mathbf{R} .

This means that $*$ carries each pair (a, b) to a unique element $a * b = ab^2$ in \mathbf{R} . Therefore, $*$ is a binary operation.

(iv) On \mathbf{Z}^+ , $*$ is defined by $a * b = |a - b|$.

It is seen that for each $a, b \in \mathbf{Z}^+$, there is a unique element $|a - b|$ in \mathbf{Z}^+ .

This means that $*$ carries each pair (a, b) to a unique element $a * b = |a - b|$ in \mathbf{Z}^+ .

Therefore, $*$ is a binary operation.

(v) On \mathbf{Z}^+ , $*$ is defined by $a * b = a$.

$*$ carries each pair (a, b) to a unique element $a * b = a$ in \mathbf{Z}^+ .

Therefore, $*$ is a binary operation.

(vi) on \mathbf{R} , $*$ is defined by $a * b = a + 4b^2$

it is seen that for each element $a, b \in \mathbf{R}$, there is unique element $a + 4b^2$ in \mathbf{R}

This means that $*$ carries each pair (a, b) to a unique element $a * b =$

$a + 4b^2$ in \mathbf{R} .

Therefore, $*$ is a binary operation.

Binary Operations Ex 3.1 Q3

It is given that, $a * b = 2a + b - 3$

Now

$$\begin{aligned} 3 * 4 &= 2 \times 3 + 4 - 3 \\ &= 10 - 3 \\ &= 7 \end{aligned}$$

Binary Operations Ex 3.1 Q4

The operation $*$ on the set $A = \{1, 2, 3, 4, 5\}$ is defined as

$a * b = \text{L.C.M. of } a \text{ and } b$.

$2 * 3 = \text{L.C.M of } 2 \text{ and } 3 = 6$. But 6 does not belong to the given set.

Hence, the given operation $*$ is not a binary operation.

Binary Operations Ex 3.1 Q5

We have,

$$S = \{a, b, c\}$$

We know that the total number of binary operation on a set S with n element is n^{n^2}

$$\Rightarrow \text{Total number of binary operation on } S = \{a, b, c\} = 3^{3^2} = 3^9$$

Binary Operations Ex 3.1 Q6

We have,

$$S = \{a, b\}$$

The total number of binary operation on $S = \{a, b\}$ in $2^{2^2} = 2^4 = 16$

***** END *****

