



Indefinite Integrals Ex 19.9 Q35

$$\text{Let } I = \int \frac{x \sin^{-1} x^2}{\sqrt{1-x^4}} dx \text{ --- (i)}$$

$$\text{Let } \sin^{-1} x^2 = t \quad \text{then,} \\ d(\sin^{-1} x^2) = dt$$

$$\Rightarrow 2x \times \frac{1}{\sqrt{1-x^4}} dx = dt$$

$$\Rightarrow \frac{x}{\sqrt{1-x^4}} dx = \frac{dt}{2}$$

Putting  $\sin^{-1} x^2 = t$  and  $\frac{x}{\sqrt{1-x^4}} dx = \frac{dt}{2}$  in equation (i),  
we get

$$\begin{aligned} I &= \int t \frac{dt}{2} \\ &= \frac{1}{2} \times \frac{t^2}{2} + c \\ &= \frac{1}{4} (\sin^{-1} x^2)^2 + c \end{aligned}$$

$$\therefore I = \frac{1}{4} (\sin^{-1} x^2)^2 + c$$

Indefinite Integrals Ex 19.9 Q36

$$\text{Let } I = \int x^3 \sin(x^4 + 1) dx \text{ ----- (i)}$$

$$\text{Let } x^4 + 1 = t \quad \text{then,}$$

$$d(x^4 + 1) = dt$$

$$\Rightarrow x^4 dx = dt$$

$$\Rightarrow x^3 dx = \frac{dt}{4}$$

Putting  $x^4 + 1 = t$  and  $x^3 dx = \frac{dt}{4}$  in equation (i), we get

$$I = \int \sin t \frac{dt}{4}$$

$$= -\frac{1}{4} \cos t + c$$

$$= -\frac{1}{4} \cos(x^4 + 1) + c$$

$$\therefore I = -\frac{1}{4} \cos(x^4 + 1) + c$$

Indefinite Integrals Ex 19.9 Q37

$$\text{Let } I = \int \frac{(x+1)e^x}{\cos^2(xe^x)} dx \text{ ----- (i)}$$

$$\text{Let } xe^x = t \quad \text{then,}$$

$$d(xe^x) = dt$$

$$\Rightarrow (e^x + xe^x) dx = dt$$

$$\Rightarrow (x+1)e^x dx = dt$$

Putting  $xe^x = t$  and  $(x+1)e^x dx = dt$  in equation (i), we get

$$I = \int \frac{dt}{\cos^2 t}$$

$$= \int \sec^2 t dt$$

$$= \tan t + c$$

$$= \tan(xe^x) + c$$

$$\therefore I = \tan(xe^x) + c$$

Indefinite Integrals Ex 19.9 Q38

Let  $I = \int x^2 e^{x^3} \cos(e^{x^3}) dx \dots \dots (i)$

Let  $e^{x^3} = t$  then,  
 $d(e^{x^3}) = dt$

$$\Rightarrow 3x^2 e^{x^3} dx = dt$$

$$\Rightarrow x^2 e^{x^3} dx = \frac{dt}{3}$$

Putting  $e^{x^3} = t$  and  $x^2 e^{x^3} dx = \frac{dt}{3}$  in equation (i), we get

$$\begin{aligned} I &= \int \cos t \frac{dt}{3} \\ &= \frac{\sin t}{3} + C \\ &= \frac{\sin(e^{x^3})}{3} + C \end{aligned}$$

$$\therefore I = \frac{1}{3} \sin(e^{x^3}) + C$$

Indefinite Integrals Ex 19.9 Q39

Let  $I = \int 2x \sec^3(x^2 + 3) \tan(x^2 + 3) dx \dots \dots (i)$

Let  $\sec(x^2 + 3) = t$  then,  
 $d[\sec(x^2 + 3)] = dt$

$$\Rightarrow 2x \sec(x^2 + 3) \tan(x^2 + 3) dx = dt$$

Putting  $\sec(x^2 + 3) = t$  and  $2x \sec(x^2 + 3) \tan(x^2 + 3) dx = dt$  in equation (i), we get

$$\begin{aligned} I &= \int t^2 dt \\ &= \frac{t^3}{3} + C \\ &= \frac{1}{3} [\sec(x^2 + 3)]^3 + C \end{aligned}$$

$$\therefore I = \frac{1}{3} [\sec(x^2 + 3)]^3 + C$$

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