

Polynomials Ex 2.3 Q5

Answer:

We know that if $x = \alpha$ is a zero of a polynomial, then $(x - \alpha)$ is a factor of f(x). Since $-\sqrt{3}$ and $\sqrt{3}$ are zeros of f(x)

Therefore

$$(x+\sqrt{3})(x-\sqrt{3}) = x^2 + \sqrt{3}x - \sqrt{3}x - 3$$

$$= x^2 + \sqrt{3}x - \sqrt{3}x - 3$$

 x^2-3 is a factor of f(x). Now, we divide $f(x)=x^4-3x^3-x^2+9x-6$ by $g(x)=x^2-3$ to find the other zeros of f(x).

$$\begin{array}{r}
x^{2} - 3x + 2 \\
x^{2} - 3) + \cancel{x} - 3x^{3} - x^{2} + 9x - 6 \\
+ \cancel{x} - 0x^{3} - 3x^{2} \\
\hline
- 3\cancel{x} + 2x^{2} + 9\cancel{x} \\
- 3\cancel{x} + 0 + 9\cancel{x} \\
2\cancel{x} - \cancel{x} \\
- \cancel{x} \\
0
\end{array}$$

By using division algorithm we have, $f(x) = g(x) \times q(x) + r(x)$.

$$x^4 - 3x^3 - x^2 + 9x - 6 = (x^2 - 3)(x^2 - 3x + 2) + 0$$

$$x^4 - 3x^3 - x^2 + 9x - 6 = (x^2 - 3)(x^2 - 2x - 1x + 2)$$

$$x^4 - 3x^3 - x^2 + 9x - 6 = (x^2 - 3)[x(x-2) - 1(x-2)]$$

$$x^4 - 3x^3 - x^2 + 9x - 6 = (x^2 - 3)[(x - 1)(x - 2)]$$

$$x^4 - 3x^3 - x^2 + 9x - 6 = (x - \sqrt{3})(x + \sqrt{3})(x - 1)(x - 2)$$

Hence, the zeros of the given polynomials are $-\sqrt{3}, +\sqrt{3}, +1, +2$

Polynomials Ex 2.3 Q6

Answer:

Since
$$-\sqrt{\frac{3}{2}}$$
 and $\sqrt{\frac{3}{2}}$ are two zeros of $f(x)$. Therefore,
$$= \left(x - \sqrt{\frac{3}{2}}\right) \left(x + \sqrt{\frac{3}{2}}\right)$$
$$= \left(x^2 - \frac{3}{2}\right)$$
$$= \frac{1}{2}(2x^2 - 3) \text{ is a factor of } f(x).$$
 Also $2x^2 - 3$ is a factor of $f(x)$.

Let us now divide f(x) by $2x^2-3$. We have,

$$\begin{array}{r}
1x^{2}-1x-2 \\
2x^{2}-3 + 2x^{4}-2x^{3}-7x^{2}+3x+6 \\
+ 2x^{4}+0 -3x^{2} \\
- 2x^{5}-4x^{2}+3x \\
- 2x^{5}-0 + 3x \\
- 4x^{5}+6 \\
- 4x^{5}+6 \\
- 4x^{5}+6 \\
0
\end{array}$$

By using division algorithm we have, $f(x) = g(x) \times q(x) + r(x)$

$$2x^4 - 2x^3 - 7x^2 + 3x + 6 = \left(2x^2 - 3\right)\left(x^2 - x - 2\right) + 0$$

$$2x^4 - 2x^3 - 7x^2 + 3x + 6 = \left(\sqrt{2}x + \sqrt{3}\right)\left(\sqrt{2}x - \sqrt{3}\right)\left(x^2 + 1x - 2x - 2\right)$$

$$2x^4 - 2x^3 - 7x^2 + 3x + 6 = \left(\sqrt{2}x + \sqrt{3}\right)\left(\sqrt{2}x - \sqrt{3}\right)\left[x(x+1) - 2(x+1)\right]$$

$$2x^4 - 2x^3 - 7x^2 + 3x + 6 = \left(\sqrt{2}x + \sqrt{3}\right)\left(\sqrt{2}x - \sqrt{3}\right)\left(x - 2\right)(x+1)$$
Hence, The zeros of $f(x)$ are
$$-\sqrt{\frac{3}{2}}, \sqrt{\frac{3}{2}}, 2, -1$$
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