

## Functions Ex 2.3 Q11(ii)

We have,  $f(x) = \sqrt{x-2}$ 

Clearly, Domain $(f) = [2, \infty)$  and Range $(f) = [0, \infty)$ .

We observe that range(f) is not a subset of domain of f.

: Domain of (fof) = 
$$\{x:x \in Domain (f) \text{ and } f(x) \in Domain (f)\}$$

= 
$$\{x: x \in [2, \infty) \text{ and } \sqrt{x-2} \in [2, \infty)\}$$

= 
$$\{x: x \in [2, \infty) \text{ and } \sqrt{x-2} \ge 2\}$$

= 
$$\{x: x \in [2, \infty) \text{ and } x - 2 \ge 4\}$$

= 
$$\{x: x \in [2, \infty) \text{ and } x \ge 6\}$$

$$= \lceil 6, \infty \rangle$$

Clearly, range of  $f = [0, \infty) \not\subset Domain of (fof)$ .

: Domain of 
$$((fof)of) = \{x: x \in Domain (f) \text{ and } f(x) \in Domain (fof)\}$$

= 
$$\{x: x \in [2, \infty) \text{ and } \sqrt{x-2} \in [6, \infty)\}$$

= 
$$\{x: x \in [2, \infty) \text{ and } \sqrt{x-2} \ge 6\}$$

= 
$$\{x: x \in [2, \infty) \text{ and } x - 2 \ge 36\}$$

$$= \{x: x \in [2, \infty) \text{ and } x \ge 38\}$$

$$= [38, \infty)$$

Now,

$$(fof)(x) = f(f(x)) = f(\sqrt{x-2}) = \sqrt{\sqrt{x-2}-2}$$

$$(fofof)(x) = (fof)(f(x)) = (fof)(\sqrt{x-2}) = \sqrt{\sqrt{\sqrt{x-2}-2}-2}$$

∴ fofof :  $[38, ∞) \rightarrow R$  defined as

$$(fofof)(x) = \sqrt{\sqrt{\sqrt{x-2}-2}-2}$$

Functions Ex 2.3 Q11(iii)

We have, 
$$f(x) = \sqrt{x-2}$$
 Clearly, Domain  $(f) = [2, \infty)$  and Range  $(f) = [0, \infty)$ . We observe that range  $(f)$  is not a subset of domain of  $f$ .   
 $\therefore$  Domain of  $(fof) = \{x: x \in Domain (f) \text{ and } f(x) \in Domain (f)\}$ 

$$= \{x: x \in [2, \infty) \text{ and } \sqrt{x-2} \in [2, \infty)\}$$

$$= \{x: x \in [2, \infty) \text{ and } \sqrt{x-2} \ge 2\}$$

$$= \{x: x \in [2, \infty) \text{ and } x - 2 \ge 4\}$$

$$= \{x: x \in [2, \infty) \text{ and } x \ge 6\}$$

$$= [6, \infty)$$
Clearly, range of  $f = [0, \infty) \not\subset Domain of (fof)$ .
$$\therefore Domain of ((fof) of) = \{x: x \in Domain (f) \text{ and } f(x) \in Domain (fof)\}$$

$$= \{x: x \in [2, \infty) \text{ and } \sqrt{x-2} \ge 6\}$$

$$= \{x: x \in [2, \infty) \text{ and } x - 2 \ge 36\}$$

 $= \{x: x \in [2, \infty) \text{ and } x \ge 38\}$ 

Now,

$$(fof)(x) = f(f(x)) = f(\sqrt{x-2}) = \sqrt{\sqrt{x-2}-2}$$

 $= [38, \infty)$ 

$$(fofof)(x) = (fof)(f(x)) = (fof)(\sqrt{x-2}) = \sqrt{\sqrt{x-2}-2} = 2$$
  
 $\therefore fofof: [38, \infty) \rightarrow \mathbb{R}$  defined as  
 $(fofof)(x) = \sqrt{\sqrt{x-2}-2} = 2$ 

(fofof)(38) = 
$$\sqrt{\sqrt{38-2}-2}$$
 =  $\sqrt{\sqrt{36-2}-2}$  =  $\sqrt{\sqrt{6-2}-2}$  =  $\sqrt{4-2}$  =  $\sqrt{2-2}$  = 0 Functions Ex 2.3 Q11(iv)

We have, 
$$f(x) = \sqrt{x-2}$$

Clearly, Domain $(f) = [2, \infty)$  and Range $(f) = [0, \infty)$ .

We observe that range(f) is not a subset of domain of f.

$$\text{:. Domain of (fof)} = \left\{ x : x \in \text{Domain (f) and } f(x) \in \text{Domain (f)} \right\}$$

$$= \left\{ x : x \in [2, \infty) \text{ and } \sqrt{x - 2} \in [2, \infty) \right\}$$

$$= \left\{ x : x \in [2, \infty) \text{ and } \sqrt{x - 2} \ge 2 \right\}$$

$$= \left\{ x : x \in [2, \infty) \text{ and } x - 2 \ge 4 \right\}$$

$$= \left\{ x : x \in [2, \infty) \text{ and } x \ge 6 \right\}$$

$$= \left[ 6, \infty \right)$$

Now,

$$(fof)(x) = f(f(x)) = f(\sqrt{x-2}) = \sqrt{\sqrt{x-2}-2}$$

∴ fof: 
$$[6, \infty) \rightarrow \mathbb{R}$$
 defined as  
(fof)(x) =  $\sqrt{\sqrt{x-2}-2}$ 

$$f^2 \big( \times \big) = \left[ f \big( \times \big) \right]^2 = \left[ \sqrt{\times - 2} \right]^2 = \times - 2$$

∴ 
$$f^2:[2,\infty) \to R$$
 defined as  $f^2(x) = x - 2$ 

$$\therefore$$
 fof  $\neq$  f<sup>2</sup>

Functions Ex 2.3 Q12

$$f(x) \begin{cases} 1+x & 0 \le x \le 2 \\ 3-x & 2 \le x \le 3 \end{cases}$$

 $\therefore \ \, \mathsf{Range} \,\, \mathsf{of} \,\, f = \big[ \, \mathsf{0} \,, \mathsf{3} \, \big] \subseteq \, \mathsf{Dom} \, \mathsf{ain} \,\, \mathsf{of} \, f.$ 

$$f \circ f(x) = f(f(x)) = f \begin{cases} 1+x & 0 \le x \le 2 \\ 3-x & 2 < x \le 3 \end{cases}$$

$$f \circ f \left( x \right) = \begin{cases} 2 + x & 0 \le x \le 1 \\ 2 - x & 1 < x \le 2 \\ 4 - x & 2 < x \le 3 \end{cases}$$

\*\*\*\*\*\*\*\*\* FND \*\*\*\*\*\*\*