

Binomial Theorem Ex 18.2 Q16(ix)

We have,

$$\left(\sqrt[3]{x} + \frac{1}{2\sqrt[3]{x}}\right)^{18}, x > 0$$

Let  $(r+1)^{th}$  term be independent of x.

$$\begin{split} &: \qquad T_{r+1} = \, ^{18}C_r \left( \sqrt[3]{x} \right)^{18-r} \, \times \left( \frac{1}{2\sqrt[3]{x}} \right)^r \\ &= \, ^{18}C_r \left( (x)^{\frac{1}{3}} \right)^{18-r} \, \times \left( \frac{1}{2} \right)^r \, \times \left( \frac{1}{\frac{1}{x^{\frac{1}{3}}}} \right)^r \\ &= \, ^{18}C_r \left( x \right)^{\frac{8-r}{3}} \, \times \left( \frac{1}{\frac{r}{x^{\frac{1}{3}}}} \right) \times \left( \frac{1}{2} \right)^r \\ &= \, ^{18}C_r \left( x \right)^{\frac{18-r}{3}} \, \times \left( \frac{1}{2} \right)^r \\ &= \, ^{18}C_r \left( x \right)^{\frac{18-r}{3}} \, \times \left( \frac{1}{2} \right)^r \end{split}$$

If it is independent of x, we must have

$$\frac{18-2r}{3}=0$$

$$\Rightarrow$$
 18 = 2r

 $\therefore$  Term independet of  $x = T_{9+1} = T_{10}$ 

Now,

$$\begin{split} & 7_{10} = {}^{18}C_{9} \left( \sqrt[3]{x} \right)^{18-9} \left( \frac{1}{2\sqrt[3]{x}} \right)^{9} \\ & = {}^{18}C_{9} \left( \sqrt[3]{x} \right)^{9} \times \frac{1}{2^{9}} \times \left( \frac{1}{\sqrt[3]{x}} \right)^{9} \\ & = \frac{{}^{18}C_{9}}{2^{9}} \end{split}$$

Hence, required term =  $\frac{^{18}C_9}{2^9}$ .

Binomial Theorem Ex 18.2 Q16(x)

$$\left(\frac{3x^2}{2} - \frac{1}{3x}\right)^6$$

In expansion

$$\begin{split} T_{r+1} &= {}^{6}C_{r} \left(\frac{3x^{2}}{2}\right)^{6-r} \left(-\frac{1}{3x}\right)^{r} \\ &= {}^{6}C_{r} \left(\frac{3}{2}\right)^{6-r} \left(x^{12-3r}\right) \left(-\frac{1}{3}\right)^{r} \end{split}$$

Let  $T_{r+1}$  be independent of x,

$$12 - 3r = 0$$
 or  $r = 4$ 

.. Required term

$$\Rightarrow T_{r+1} = T_{4+1} = T_5 = {}^6C_4 \left(\frac{3}{2}\right)^{6-4} \left(\frac{-1}{3}\right)^4 x^{12-3(4)}$$
$$= 15 \left(\frac{9}{4}\right) \left(\frac{1}{81}\right) x^0 = \frac{5}{12}$$

## Binomial Theorem Ex 18.2 Q17

We know that the coefficient of rth term in the expansion of  $(1+x)^n$  is  ${}^nC_{r-1}$ 

: Coefficient of (2r+4) th term of the expansion  $(1+x)^{18} = {}^{18}C_{2r+4-1} = {}^{18}C_{2r+3}$  and, coefficient of (r-2) th term of the expansion  $(1+x)^{18} = {}^{18}C_{r-2-1} = {}^{18}C_{r-3}$  It is given that these coefficients are equal.

$$\Rightarrow$$
 2r+3=r-3 or, 2r+3+r-3=18

$$"C_r = "C_s$$

$$\Rightarrow r = s \text{ or, } r + s = n$$

$$\Rightarrow$$
  $r = -6$  or,  $3r = 18$ 

$$\Rightarrow$$
  $r = -6$  or,  $r = 6$ 

$$\Rightarrow$$
  $r = 6$ 

$$[\because r = -6 \text{ is not possible}]$$

## Binomial Theorem Ex 18.2 Q18

$$(1+x)^{43}$$

$$\begin{pmatrix} 43 \\ 2r \end{pmatrix} = \begin{pmatrix} 43 \\ r+1 \end{pmatrix}$$

$$2r + r + 1 = 43$$

$$3r = 42$$

$$r = 14$$

\*\*\*\*\*\*\*\*\* END \*\*\*\*\*\*\*