

Algebraic Identities Ex 4.3 Q18

Answer:

From given problem we have to find the value of $64x^3 - 125z^3$

Given
$$(4x-5z) = 16, xz = 12$$

On cubing both sides of (4x-5z) = 16 we get

$$(4x-5z)^3 = (16)^3$$

We shall use identity $(a-b)^3 = a^3 - b^3 - 3ab(a-b)$

$$4x^3 - 125z^3 - 3(4x)(5z)(4x - 5z) = 16 \times 16 \times 16$$

$$64x^3 - 125z^3 - 60(xz)(16) = 4096$$

$$64x^3 - 125z^3 - 60(12)(16) = 4096$$

$$64x^3 - 125z^3 - 11520 = 4096$$

$$64x^3 - 125z^3 = 4096 + 11520$$

$$64x^3 - 125z^3 = 15616$$

Hence the value of $64x^3 - 125z^3$ is 15616.

Algebraic Identities Ex 4.3 Q19

Answer:

In the given problem, we have to find the value of $x^3 - \frac{1}{x^3}$

Given
$$x - \frac{1}{x} = 3 + 2\sqrt{2}$$

Cubing on both sides of $x - \frac{1}{x} = 3 + 2\sqrt{2}$ we get $\left(x - \frac{1}{x}\right)^3 = \left(3 + 2\sqrt{2}\right)^3$

$$\left(x - \frac{1}{x}\right)^3 = \left(3 + 2\sqrt{2}\right)$$

We shall use identity $(a+b)^3 = a^3 + b^3 + 3ab(a+b)$

$$(3+2\sqrt{2})^3 = x^3 - \frac{1}{x^3} - 3 \times x \times \frac{1}{x} \left(x - \frac{1}{x} \right)$$

$$3^3 + \left(2\sqrt{2} \right)^3 + 3 \times 3 \times 2\sqrt{2} \left(3 + 2\sqrt{2} \right) = x^3 - \frac{1}{x^3} - 3 \times x \times \frac{1}{x} \times \left(3 + 2\sqrt{2} \right)$$

$$27 + 16\sqrt{2} + 18\sqrt{2} \left(3 + 2\sqrt{2} \right) = x^3 - \frac{1}{x^3} - 3\left(3 + 2\sqrt{2} \right)$$

$$27 + 16\sqrt{2} + 18\sqrt{2} \times 3 + 18\sqrt{2} \times 2\sqrt{2} = x^3 - \frac{1}{x^3} - 9 - 6\sqrt{2}$$

$$27 + 16\sqrt{2} + 54\sqrt{2} + 72 = x^3 - \frac{1}{x^3} - 9 - 6\sqrt{2}$$

$$27 + 16\sqrt{2} + 54\sqrt{2} + 72 + 9 + 6\sqrt{2} = x^3 - \frac{1}{x^3}$$

$$[27 + +72 + 9] + \left[16\sqrt{2} + 54\sqrt{2} + 6\sqrt{2}\right] = x^3 - \frac{1}{x^3}$$

$$108 + 76\sqrt{2} = x^3 - \frac{1}{x^3}$$

Hence the value of
$$x^3 - \frac{1}{x^3}$$
 is $108 + 76\sqrt{2}$

******* END *******