

Exercise 20G

We know that a square encloses more area even though its perimeter is the same as that of the rectangle.

:. Area of a square > Area of a rectangle

Q9

Answer:

(b) 13500 m²

Let the length of the rectangular field be 5x.

Breadth = 3x

Perimeter of the field = 2(l + b) = 480 m (given)

$$\Rightarrow$$
 480 = 2(5x + 3x) \Rightarrow 480 = 16x

$$\Rightarrow \chi = \frac{480}{16} = 30$$

:. Length = $5x = (5 \times 30) = 150 \text{ m}$

Breadth = $3x = (3 \times 30) = 90 \text{ m}$

∴ Area of the rectangular park = 150 m × 90 m = 13500 m²

Q10

Answer:

(a) 6 m

Total cost of carpeting = Rs 6000

Rate of carpeting = Rs 50 per m

∴ Length of the carpet =
$$\left(\frac{6000}{50}\right)$$
 m = 120 m

∴ Length of the carpet =
$$\left(\frac{6000}{50}\right)$$
 m = 120 m
∴ Area of the carpet = $\left(120 \times \frac{75}{100}\right)$ m² = 90 m² [since 75 cm = $\frac{75}{100}$ m]
Area of the floor = Area of the carpet = 90 m²

$$\therefore$$
 Width of the room = $\left(\frac{\text{Area}}{\text{Length}}\right) = \left(\frac{90}{15}\right)$ m = 6 m

Q11

Answer:

(a) 84 cm²

Let
$$a = 13$$
 cm, $b = 14$ cm and $c = 15$ cm

Then, $s = \frac{a+b+c}{2} = \left(\frac{13+14+15}{2}\right)$ cm = 21 cm

 \therefore Area of the triangle = $\sqrt{s(s-a)(s-b)(s-c)}$ sq. units

= $\sqrt{21(21-13)(21-14)(21-15)}$ cm²

= $\sqrt{21\times8\times7\times6}$ cm²

= $\sqrt{3\times7\times2\times2\times2\times7\times2\times3}$ cm²

= $(2\times2\times3\times7)$ cm²

= 84 cm²

Q12

Answer:

(b) 48 m²

V

Base = 12 m

Height = 8 m

Area of the triangle =
$$\left(\frac{1}{2} \times \mathbf{Base} \times \mathbf{Height}\right)$$
 sq. units = $\left(\frac{1}{2} \times 12 \times 8\right)$ m² = 48 m²

Q13

Answer:

(b) 4 cm

Area of the equilateral triangle = $4\sqrt{3}$ cm²

We know:

Area of an equilateral triangle = $\frac{\sqrt{3}}{4}$ (side)² sq. units

$$\therefore \text{ Side of the equilateral triangle} = \left[\sqrt{\left(\frac{4\times \text{Area}}{\sqrt{3}}\right)}\right] \text{ cm}$$

$$= \left[\sqrt{\left(\frac{4\times 4\sqrt{3}}{\sqrt{3}}\right)}\right] \text{ cm} = \left(\sqrt{4\times 4}\right) \text{ cm} = \left(\sqrt{16}\right) \text{cm} = 4 \text{ cm}$$

Q14

Answer:

(c) $16\sqrt{3}$ cm²

It is given that one side of an equilateral triangle is 8 cm.

 \therefore Area of the equilateral triangle = $\frac{\sqrt{3}}{4} \left(\text{Side} \right)^2$ sq. units $= \frac{\sqrt{3}}{4} (8)^2 \text{ cm}^2$ $= \left(\frac{\sqrt{3}}{4} \times 64\right) \text{ cm}^2 = 16\sqrt{3} \text{ cm}^2$

Q15

Answer:

(b) $2\sqrt{3} \text{ cm}^2$

Let $\triangle ABC$ be an equilateral triangle with one side of the length a cm.

Diagonal of an equilateral triangle =
$$\frac{\sqrt{3}}{2} a$$
 cm

$$\Rightarrow \frac{\sqrt{3}}{2} a = \sqrt{6}$$

$$\Rightarrow a = \frac{\sqrt{6} \times 2}{\sqrt{3}} = \frac{\sqrt{3} \times \sqrt{2} \times 2}{\sqrt{3}} = 2\sqrt{2} \text{ cm}$$
Area of the equilateral triangle = $\frac{\sqrt{3}}{4} a^2$

$$= \frac{\sqrt{3}}{4} \left(2\sqrt{2}\right)^2 \text{ cm}^2 = \left(\frac{\sqrt{3}}{4} \times 8\right) \text{cm}^2 = 2\sqrt{3} \text{ cm}^2$$

Q16

Answer:

(b) 72 cm²

Base of the parallelogram = 16 cm

Height of the parallelogram = 4.5 cm

:. Area of the parallelogram = Base x Height

$$= (16 \times 4.5) \text{ cm}^2 = 72 \text{ cm}^2$$

Q17

Answer:

(b) 216 cm²

Length of one diagonal = 24 cm

Length of the other diagonal = 18 cm

∴ Area of the rhombus =
$$\frac{1}{2}$$
 × (Product of the diagonals) = $\left(\frac{1}{2} \times 24 \times 18\right)$ cm² = 216 cm²

Q18

Answer:

(c) 154 cm²

Let the radius of the circle be r cm.

Circumference = $2\pi r$

******* END ********