

Binary Operations Ex 3.2 Q4(viii) Commutativity: Let  $a,b \in R$ , then

$$a*b = a+b-7$$
  
=  $b+a-7$   
=  $b*a$ 

$$\Rightarrow a*b=b*a$$

⇒ \* is commutative on R

Associativity: Let 
$$a,b,c \in Q$$
, then  $(a*b)*c = (a+b-7)*c$   
  $= a+b-7+c-7$   
  $= a+b+c-17$   $---(i)$   
and,  $a*(b*c) = a*(b+c-7)$   
  $= a+b+c-7-7$   
  $= a+b+c-17$   $---(ii)$ 

From (i) & (ii) 
$$(a*b)*c = a*(b*c)$$

 $\Rightarrow$  \* is associative on R Binary Operations Ex 3.2 Q4(ix) Commutativity:

Let  $a, b \in R - \{-1\}$ , then

$$a*b = \frac{a}{b+1} \neq \frac{b}{a+1} = b*a$$

 $\Rightarrow$  \* is not commutative on R -  $\{-1\}$ 

Associativity:

Let  $a, b, c \in R - \{-1\}$ , then

$$(a*b)*c = \left(\frac{a}{b+1}\right)*c$$

$$= \frac{\frac{a}{b+1}}{c+1} = \frac{a}{(b+1)(c+1)}$$
---(i)

$$a*(b*c) = a*\left(\frac{b}{c+1}\right)$$

$$= \frac{a}{\frac{b}{c+1}+1} = \frac{a(c+1)}{b+c+1} \qquad ---(ii)$$

From (i) and (ii) 
$$(a*b)*c \neq a*(b*c)$$

$$\Rightarrow$$
 \* is not associative on R -  $\{-1\}$ 

Binary Operations Ex 3.2 Q4(x)

Commutativity:

Let  $a,b \in Q$ , then

$$a * b = ab + 1 = ba + 1 = b * a$$

Associativity:

Let  $a,b,c \in \mathbb{Q}$ , then

$$(a*b)*c = (ab+1)*c$$
  
=  $abc+c+1$  ---(i)

From (i) and (ii)
$$(a*b)*c \neq a*(b*c)$$

Binary Operations Ex 3.2 Q4(xi)

Commutativity:

Let  $a, b \in N$ , then

$$a * b = a^b \neq b^a = b * a$$

⇒ '\*' is not commutative on N

Associativity:

Let  $a, b, c \in N$ , then

$$(a*b)*c = a^b*c = (a^b)^c = a^{bc}$$
 --- (i)

$$a * (b * c) = a * b^c = (a)^{b^c}$$
 --- (ii)

From (i) and (ii)

$$a^{bc} \neq (a)^{b^c}$$

$$\Rightarrow (a*b)*c \neq a*(b*c)$$

⇒ '\*' is not associative on N.

Binary Operations Ex 3.2 Q4(xii)

Commutativity:

Let  $a, b \in N$ , then

$$a*b=a^b\neq b^a=b*a$$

⇒ '\*' is not commutative on N

Associativity:

Let  $a,b,c \in N$ , then

$$(a*b)*c = a^b*c = (a^b)^c = a^{bc}$$
 ---(i)

$$a * (b * c) = a * b^c = (a)^{b^c}$$
 --- (ii)

From (i) and (ii)

$$a^{bc} \neq (a)^{b^c}$$

$$\Rightarrow (a*b)*c \neq a*(b*c)$$

 $\Rightarrow$  '\*' is not associative on N.

Binary Operations Ex 3.2 Q4(xiii)

Commutativity:

Let  $a, b \in \mathbb{Z}$  then,

$$a*b = a - b \neq b - a = b*a$$

 $\Rightarrow$  \* is not commutative on Z

Associativity:

Let  $a, b, c \in \mathbb{Z}$ , then

$$(a*b)*c = (a-b)*c = (a-b-c)$$
 ---(i)

& 
$$a*(b*c) = a*(b-c) = (a-b+c)$$
 ---(ii)

From (i) & (ii) 
$$(a*b)*c \neq a*(b*c)$$

 $\Rightarrow$  '\*' is not associative on Z.

Binary Operations Ex 3.2 Q4(xiv)

Commutativity:

Let  $a, b \in Q$  then,

$$a*b = \frac{ab}{4} = \frac{ba}{4} = b*a$$

.: \* is commutative on Q

Associativity:

Let  $a, b, c \in Q$  then,

$$(a*b)*c = \frac{ab}{4}*c = \frac{abc}{16} \qquad \qquad ---(i)$$

and, 
$$a * (b * c) = a * \frac{bc}{4} = \frac{abc}{16}$$
 --- (ii)

From (i) and (ii)
$$(a*b)*c=a*(b*c)$$

 $\dot{\,}$  '\*' is associative on Q.

Binary Operations Ex 3.2 Q4(xv)

Commutativity:

Let  $a,b \in Q$  then,

$$a * b = (a - b)^2 = (b - a)^2 = b * a$$

$$\Rightarrow a*b=b*a$$

∴ '\*' is commutative on Q.

Associativity:

Let  $a, b, c \in Q$  then,

$$(a*b)*c = (a-b)^2*c = [(a-b)^2-c]^2$$
 ---(i)

and, 
$$a*(b*c) = a*(b-c)^2 = [a-(b-c)^2]^2$$
 ---(ii)

From (i) and (ii) 
$$(a*b)*c \neq a*(b*c)$$

:. \* is not associative on Q.

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