



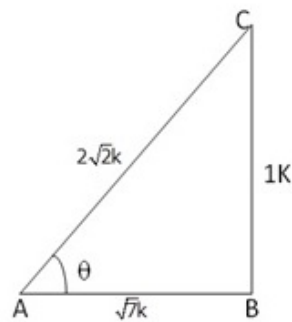
Question 8

Given: $\tan \theta = \frac{BC}{AB} = \frac{1}{\sqrt{7}}$

Let $BC = 1k$ and $AB = \sqrt{7}k$,

Where k is positive

Let us draw a ΔABC in which $\angle B = 90^\circ$ and $\angle BAC = \theta$



By pythagoras theorem, we have

$$AC^2 = (AB^2 + BC^2)$$

$$\Rightarrow AC^2 = \left[(\sqrt{7}k)^2 + (1k)^2 \right]$$

$$= 7k^2 + 1k^2 = 8k^2$$

$$\Rightarrow AC = 2\sqrt{2}k$$

$$\operatorname{cosec} \theta = \frac{AC}{BC} = \frac{2\sqrt{2}k}{1k} = 2\sqrt{2}$$

$$\sec \theta = \frac{AC}{AB} = \frac{2\sqrt{2}k}{\sqrt{7}k} = \frac{2\sqrt{2}}{\sqrt{7}}$$

$$\Rightarrow \frac{(\operatorname{cosec}^2 \theta - \sec^2 \theta)}{(\operatorname{cosec}^2 \theta + \sec^2 \theta)} = \frac{\left[(2\sqrt{2})^2 - \left(\frac{2\sqrt{2}}{\sqrt{7}} \right)^2 \right]}{\left[(2\sqrt{2})^2 + \left(\frac{2\sqrt{2}}{\sqrt{7}} \right)^2 \right]}$$

$$= \frac{\left(8 - \frac{8}{7} \right)}{\left(8 + \frac{8}{7} \right)} = \frac{\left(\frac{48}{7} \right)}{\left(\frac{64}{7} \right)} = \frac{48}{64} = \frac{3}{4}$$

Hence, $\frac{(\operatorname{cosec}^2 \theta - \sec^2 \theta)}{(\operatorname{cosec}^2 \theta + \sec^2 \theta)} = \frac{3}{4}$

***** END *****