



### Polynomials Ex 2.3 Q10

**Answer :**

We know that if  $x = \alpha$  is a zero of a polynomial, and then  $x - \alpha$  is a factor of  $f(x)$ .

Since  $\sqrt{2}$  and  $-\sqrt{2}$  are zeros of  $f(x)$ .

Therefore

$$\begin{aligned}(x + \sqrt{2})(x - \sqrt{2}) &= x^2 - (\sqrt{2})^2 \\ &= x^2 - 2\end{aligned}$$

$x^2 - 2$  is a factor of  $f(x)$ . Now, we divide  $2x^4 + 7x^3 - 19x^2 - 14x + 30$  by  $g(x) = x^2 - 2$  to find the zero of  $f(x)$ .

$$\begin{array}{r} 2x^2 + 7x - 15 \\ x^2 - 2 \overline{) 2x^4 + 7x^3 - 19x^2 - 14x + 30} \\ \underline{+ 2x^4 + 0 - 4x^2} \phantom{- 14x + 30} \\ \phantom{2x^4 + } 7x^3 - 15x^2 - 14x \phantom{+ 30} \\ \underline{+ 7x^3 + 0 - 14x} \phantom{+ 30} \\ \phantom{2x^4 + 7x^3 - } -15x^2 + 30 \phantom{- 14x +} \\ \underline{+ 15x^2 - 30} \\ 0 \end{array}$$

By using division algorithm we have  $f(x) = g(x) \times q(x) - r(x)$

$$2x^4 + 7x^3 - 19x^2 - 14x + 30 = (x^2 - 2)(2x^2 + 7x - 15) + 0$$

$$2x^4 + 7x^3 - 19x^2 - 14x + 30 = (x + \sqrt{2})(x - \sqrt{2})(2x^2 + 10x - 3x - 15)$$

$$2x^4 + 7x^3 - 19x^2 - 14x + 30 = (x + \sqrt{2})(x - \sqrt{2})[2x(x + 5) - 3(x + 5)]$$

$$2x^4 + 7x^3 - 19x^2 - 14x + 30 = (x + \sqrt{2})(x - \sqrt{2})(2x - 3)(x + 5)$$

Hence, the zeros of the given polynomial are  $\boxed{-\sqrt{2}, +\sqrt{2}, \frac{+3}{2}, -5}$ .

### Polynomials Ex 2.3 Q11

**Answer :**

We know that if  $x = \alpha$  is a zero of a polynomial, and then  $x - \alpha$  is a factor of  $f(x)$ .

Since  $\sqrt{3}$  and  $-\sqrt{3}$  are zeros of  $f(x)$ .

Therefore

$$\begin{aligned}(x + \sqrt{3})(x - \sqrt{3}) &= x^2 - 3 \\ &= x^2 - 3\end{aligned}$$

$x^2 - 3$  is a factor of  $f(x)$ . Now, we divide  $2x^3 + x^2 - 6x - 3$  by  $g(x) = x^2 - 3$  to find the other zeros of  $f(x)$ .

$$\begin{array}{r} 2x + 1 \\ x^2 - 3 \overline{) 2x^3 + x^2 - 6x - 3} \\ \underline{+ 2x^3 + 0 - 6x} \phantom{- 3} \\ \phantom{2x^3 + } x^2 - 6x - 3 \phantom{+ 3} \\ \underline{+ x^2 + 0 - 3} \phantom{+ 3} \\ \phantom{2x^3 + x^2 - } -6x - 6 \phantom{+ 3} \\ \underline{+ 6x + 6} \\ 0 \end{array}$$

By using division algorithm we have  $f(x) = g(x) \times q(x) - r(x)$

$$2x^3 + x^2 - 6x - 3 = (x^2 - 3)(2x + 1) + 0$$

$$2x^3 + x^2 - 6x - 3 = (x^2 + \sqrt{3})(x - \sqrt{3})(2x + 1)$$

Hence, the zeros of the given polynomial are  $\boxed{-\sqrt{3}, +\sqrt{3}, \frac{-1}{2}}$ .

### Polynomials Ex 2.3 Q12

**Answer :**

We know that if  $x = \alpha$  is a zero of a polynomial, and then  $x - \alpha$  is a factor of  $f(x)$ .

Since  $\sqrt{2}$  and  $-\sqrt{2}$  are zeros of  $f(x)$ .

Therefore

$$(x + \sqrt{2})(x - \sqrt{2}) = x^2 - (\sqrt{2})^2 \\ = x^2 - 2$$

$x^2 - 2$  is a factor of  $f(x)$ . Now, we divide  $x^3 + 3x^2 - 2x - 6$  by  $g(x) = x^2 - 2$  to find the other zeros of  $f(x)$ .

$$\begin{array}{r} x+3 \\ x^2-2 \overline{) \cancel{x^3} + 3x^2 - 2x - 6} \\ \underline{+ \cancel{x^2} - 0 \quad - 2x} \phantom{- 6} \\ \phantom{x^2-2 \overline{) \cancel{x^3} + 3x^2 - 2x - 6}} + 3x - 6 \\ \underline{+ 3x - 6} \\ \phantom{x^2-2 \overline{) \cancel{x^3} + 3x^2 - 2x - 6}} 0 \end{array}$$

By using division algorithm we have  $f(x) = g(x) \times q(x) - r(x)$

$$x^3 + 3x^2 - 2x - 6 = (x^2 - 2)(x + 3) - 0 \\ = (x + \sqrt{2})(x - \sqrt{2})(x + 3)$$

Hence, the zeros of the given polynomials are  $\boxed{-\sqrt{2}, +\sqrt{2}, \text{ and } -3}$ .

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