



(xix) The given quadric equation is $k^2x^2 - 2(2k-1)x + 4 = 0$, and roots are real and equal

Then find the value of k .

Here,

$$a = k^2, b = -2(2k-1) \text{ and } c = 4$$

As we know that $D = b^2 - 4ac$

Putting the value of $a = k^2, b = -2(2k-1)$ and $c = 4$

$$= \{-2(2k-1)\}^2 - 4 \times k^2 \times 4$$

$$= \{4(4k^2 - 4k + 1)\} - 16k^2$$

$$= 16k^2 - 16k + 4 - 16k^2$$

$$= -16k + 4$$

The given equation will have real and equal roots, if $D = 0$

$$-16k + 4 = 0$$

$$16k = 4$$

$$k = \frac{4}{16}$$

$$= \frac{1}{4}$$

Therefore, the value of $k = \boxed{\frac{1}{4}}$

(xx) The given quadric equation is $(k+1)x^2 - 2(k-1)x + 1 = 0$, and roots are real and equal

Then find the value of k .

Here,

$$a = k+1, b = -2(k-1) \text{ and } c = 1$$

As we know that $D = b^2 - 4ac$

Putting the value of $a = k+1, b = -2(k-1)$ and $c = 1$

$$= \{-2(k-1)\}^2 - 4 \times (k+1) \times 1$$

$$= \{4(k^2 - 2k + 1)\} - 4k - 4$$

$$= 4k^2 - 8k + 4 - 4k - 4$$

$$= 4k^2 - 12k + 0$$

The given equation will have real and equal roots, if $D = 0$

$$4k^2 - 12k + 0 = 0$$

$$4k^2 - 12k = 0$$

Now factorizing of the above equation

$$4k(k-3) = 0$$

$$k(k-3) = 0$$

So, either

$$k = 0 \text{ or } (k-3) = 0$$

$$k = 3$$

Therefore, the value of $k = \boxed{0, 3}$

(xxi) The given quadric equation is $2x^2 + kx + 3 = 0$, and roots are real and equal
Then find the value of k .

Here,

$$a = 2, b = k \text{ and } c = 3$$

$$\text{As we know that } D = b^2 - 4ac$$

$$\text{Putting the value of } a = 2, b = k \text{ and } c = 3$$

$$= k^2 - 4 \times 2 \times 3$$

$$= k^2 - 24$$

The given equation will have real and equal roots, if $D = 0$

$$k^2 - 24 = 0$$

$$k^2 = 24$$

$$k = \sqrt{24}$$

$$= \sqrt{4 \times 6}$$

$$= \pm 2\sqrt{6}$$

Therefore, the value of $k = \boxed{\pm 2\sqrt{6}}$

(xxii) The given quadric equation is $kx(x - 2) + 6 = 0$, and roots are real and equal
Then find the value of k .

Here,

$$kx(x - 2) + 6 = 0$$

$$kx^2 - 2kx + 6 = 0$$

So,

$$a = k, b = -2k \text{ and } c = 6$$

$$\text{As we know that } D = b^2 - 4ac$$

$$\text{Putting the value of } a = k, b = -2k \text{ and } c = 6$$

$$= (-2k)^2 - 4 \times k \times 6$$

$$= 4k^2 - 24k$$

The given equation will have real and equal roots, if $D = 0$

$$4k^2 - 24k = 0$$

Now factorizing of the above equation

$$4k(k - 6) = 0$$

$$k(k - 6) = 0$$

So, either

$$k = 0 \text{ or } (k - 6) = 0$$

$$k = 6$$

Therefore, the value of $k = \boxed{0, 6}$

(xxiii) The given quadratic equation is $x^2 - 4kx + k = 0$, and roots are real and equal.
Then find the value of k .

Here,

$$x^2 - 4kx + k = 0$$

So,

$$a = 1, b = -4k \text{ and } c = k.$$

$$\text{As we know that } D = b^2 - 4ac$$

$$\text{Putting the value of } a = 1, b = -4k \text{ and } c = k.$$

$$D = (-4k)^2 - 4(1)(k)$$

$$= 16k^2 - 4k$$

The given equation will have real and equal roots, if $D = 0$.

$$\text{So, } 16k^2 - 4k = 0$$

Now factorizing the above equation,

$$16k^2 - 4k = 0$$

$$\Rightarrow 4k(4k - 1) = 0$$

$$\Rightarrow 4k = 0 \text{ or } 4k - 1 = 0$$

$$\Rightarrow k = 0 \text{ or } k = \frac{1}{4}$$

Therefore, the value of $k = 0, \frac{1}{4}$.

(xxv) The given quadratic equation is $px(x - 3) + 9 = 0$, and roots are real and equal. Then find the value of p .

Here,

$$px(x - 3) + 9 = 0$$

$$\Rightarrow px^2 - 3px + 9 = 0$$

So,

$$a = p, b = -3p \text{ and } c = 9.$$

$$\text{As we know that } D = b^2 - 4ac$$

Putting the value of $a = p$, $b = -3p$ and $c = 9$.

$$D = (-3p)^2 - 4(p)(9)$$

$$= 9p^2 - 36p$$

The given equation will have real and equal roots, if $D = 0$.

$$\text{So, } 9p^2 - 36p = 0$$

Now factorizing the above equation,

$$9p^2 - 36p = 0$$

$$\Rightarrow 9p(p - 4) = 0$$

$$\Rightarrow 9p = 0 \text{ or } p - 4 = 0$$

$$\Rightarrow p = 0 \text{ or } p = 4$$

Therefore, the value of $p = 0, 4$.

(xxiv) The given quadratic equation is $kx(x - 2\sqrt{5}) + 10 = 0$, and roots are real and equal. Then find the value of k .

Here,

$$kx(x - 2\sqrt{5}) + 10 = 0$$

$$\Rightarrow kx^2 - 2\sqrt{5}kx + 10 = 0$$

So,

$$a = k, b = -2\sqrt{5}k \text{ and } c = 10.$$

$$\text{As we know that } D = b^2 - 4ac$$

Putting the value of $a = k$, $b = -2\sqrt{5}k$ and $c = 10$.

$$D = (-2\sqrt{5}k)^2 - 4(k)(10)$$

$$= 20k^2 - 40k$$

The given equation will have real and equal roots, if $D = 0$.

$$\text{So, } 20k^2 - 40k = 0$$

Now factorizing the above equation,

$$20k^2 - 40k = 0$$

$$\Rightarrow 20k(k - 2) = 0$$

$$\Rightarrow 20k = 0 \text{ or } k - 2 = 0$$

$$\Rightarrow k = 0 \text{ or } k = 2$$

Therefore, the value of $k = 0, 2$.

(xxvi) The given quadratic equation is $4x^2 + px + 3 = 0$, and roots are real and equal. Then find the value of p .

Here,

$$4x^2 + px + 3 = 0$$

So,

$$a = 4, b = p \text{ and } c = 3.$$

$$\text{As we know that } D = b^2 - 4ac$$

Putting the value of $a = 4$, $b = p$ and $c = 3$.

$$D = (p)^2 - 4(4)(3)$$

$$= p^2 - 48$$

The given equation will have real and equal roots, if $D = 0$.

$$\text{So, } p^2 - 48 = 0$$

Now factorizing the above equation,

$$p^2 - 48 = 0$$

$$\Rightarrow p^2 - (4\sqrt{3})^2 = 0$$

$$\Rightarrow (p - 4\sqrt{3})(p + 4\sqrt{3}) = 0$$

$$\Rightarrow p - 4\sqrt{3} = 0 \text{ or } p + 4\sqrt{3} = 0$$

$$\Rightarrow p = 4\sqrt{3} \text{ or } p = -4\sqrt{3}$$

Therefore, the value of $p = \pm 4\sqrt{3}$.

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