

Exercise 9.1

$$\Rightarrow h = 20\sqrt{3} - 20$$

$$\Rightarrow h = 20(\sqrt{3} - 1)$$
 m

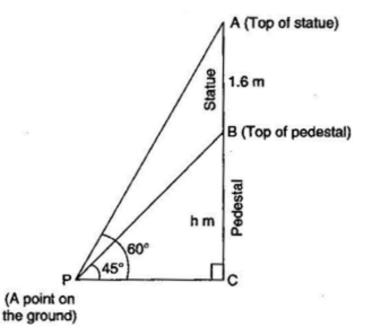
... The height of the tower is  $20(\sqrt{3}-1)$  m.

**Q8.** A statue, 1.6 m tall, stands on the top of a postal. From a point on the ground, the angle of elevation of the top of the statue is  $60^{\circ}$  and from the same point the angle of elevation of the top of the pedestal is  $45^{\circ}$ . Find the height of the pedestal.

Ans: Let the height of the pedestal be h m.

$$\therefore$$
 BC =  $h$  m

In right triangle ACP,



$$\tan 60^{\circ} = \frac{AC}{PC}$$

$$\Rightarrow \sqrt{3} = \frac{AB + BC}{PC}$$

$$\Rightarrow \sqrt{3} = \frac{1.6 + h}{PC} \dots (i)$$

In right triangle BCP,

$$\tan 45^{\circ} = \frac{BC}{PC}$$

$$\Rightarrow 1 = \frac{h}{PC} \Rightarrow PC = h$$

$$\sqrt{3} = \frac{1.6 + h}{h}$$
 [From eq. (i)]

$$\Rightarrow \sqrt{3}h = 1.6 + h$$

$$\Rightarrow h(\sqrt{3}-1)=1.6$$

$$\Rightarrow h = \frac{1.6}{\sqrt{3} - 1}$$

$$\Rightarrow h = \frac{1.6(\sqrt{3} + 1)}{(\sqrt{3} - 1)(\sqrt{3} + 1)}$$

$$\Rightarrow h = \frac{1.6\sqrt{3} + 1}{3 - 1}$$

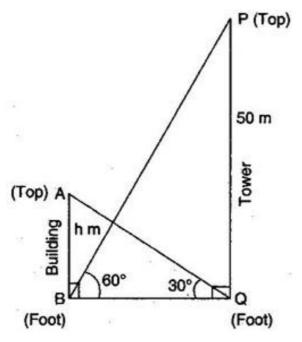
$$\Rightarrow h = \frac{1.6(\sqrt{3} + 1)}{2}$$

$$\Rightarrow h = 0.8(\sqrt{3} + 1) \text{ m}$$

Hence, the height of the pedestal is  $0.8(\sqrt{3} + 1)$  m.

**Q9.** The angle of elevation of the top of a building from the foot of the tower is  $30^{\circ}$  and the angle of elevation of the top of the tower from the foot of the building is  $60^{\circ}$ . If the tower is 50 m high, find the height of the building.

Ans: Let the height of the building be h m.



$$\tan 60^{\circ} = \frac{PQ}{BQ} \Rightarrow \sqrt{3} = \frac{50}{BQ}$$

$$\Rightarrow$$
 BQ =  $\frac{50}{\sqrt{3}}$  m....(i)

In right triangle ABQ,

$$\tan 30^{\circ} = \frac{AB}{BQ} \Rightarrow \frac{1}{\sqrt{3}} = \frac{h}{BQ}$$

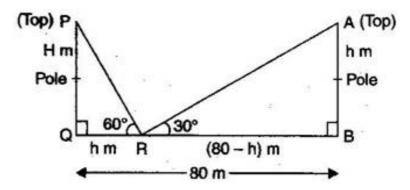
$$\Rightarrow$$
 BQ =  $h\sqrt{3}$  m....(ii)

From eq. (i) and (ii),

$$h\sqrt{3} = \frac{50}{\sqrt{3}} \implies h = \frac{50}{3} = 16\frac{2}{3}$$
 m

**Q10.** Two poles of equal heights are standing opposite each other on either side of the road, which is 80 m wide. From a point between them on the road, the angles of elevation of the top of the poles are <sup>60°</sup> and <sup>30°</sup> respectively. Find the height of the poles and the distances of the point from the poles.

Ans: In right triangle PRQ,



$$\tan 60^{\circ} = \frac{PQ}{QR} \Rightarrow \sqrt{3} = \frac{H}{h}$$

$$\Rightarrow$$
 H =  $h\sqrt{3}$  m....(i)

In right triangle ABR,

$$\tan 30^\circ = \frac{AB}{BR}$$

$$\Rightarrow \frac{1}{\sqrt{3}} = \frac{H}{80 - h}$$

$$\Rightarrow \frac{1}{\sqrt{3}} = \frac{h\sqrt{3}}{80 - h}$$
 [From eq. (i)]

$$\Rightarrow$$
 80 - h = 3h

$$\Rightarrow 4h = 80$$

$$\Rightarrow h = 20 \text{ m}$$

$$\therefore \mathbf{H} = h\sqrt{3} = 20\sqrt{3} \mathbf{m}$$

Also, 
$$BR = 80 - h = 80 - 20 = 60 \text{ m}$$

Hence the heights of the poles are  $20\sqrt{3}$  m each and the distances of the point from poles are 20 m and 60 m respectively.

\*\*\*\*\*\*\* END \*\*\*\*\*\*\*