



Tangents and Normals Ex 16.2 Q17

The given equations are,

$$x^2 + 3y - 3 = 0 \quad \text{--- (i)}$$

$$y = 4x - 5 \quad \text{--- (ii)}$$

Slope  $m_1$  of (i)

$$m_1 = \frac{dy}{dx} = -\frac{2x}{3}$$

Slope  $m_2$  of (ii)

$$m_2 = 4$$

According to the question

$$m_1 = m_2$$

$$\Rightarrow -\frac{2x}{3} = 4$$

$$\Rightarrow x = -6$$

From (i)

$$36 + 3y - 3 = 0$$

$$\Rightarrow 3y = -33$$

$$\therefore y = -11$$

$$\text{So, } P = (-6, -11)$$

Thus, the equation of tangent is

$$(y + 11) = 4(x + 6)$$

$$\Rightarrow 4x - y + 13 = 0$$

Tangents and Normals Ex 16.2 Q18

The equations are

$$\left(\frac{x}{a}\right)^n + \left(\frac{y}{b}\right)^n = 2 \quad \text{---(i)}$$

$$\frac{x}{a} + \frac{y}{b} = 2 \quad \text{---(ii)}$$

$$P = (a, b)$$

We need to prove (ii) is the tangent to (i)

Differentiating (i) with respect to  $x$ , we get

$$n\left(\frac{x}{a}\right)^{n-1} \times \frac{1}{a} + n\left(\frac{y}{b}\right)^{n-1} \times \frac{1}{b} \times \frac{dy}{dx} = 0$$

$$\Rightarrow \frac{x^{n-1}}{a^n} + \frac{y^{n-1}}{b^n} \times \frac{dy}{dx} = 0$$

$$\Rightarrow \frac{dy}{dx} = -\left(\frac{x}{y}\right)^{n-1} \times \left(\frac{b}{a}\right)^n$$

$$\begin{aligned} \therefore \text{Slope } m &= \left(\frac{dy}{dx}\right)_P = -\left(\frac{a}{b}\right)^{n-1} \times \left(\frac{b}{a}\right)^n \\ &= -\frac{b}{a} \end{aligned}$$

Thus, the equation of tangent is

$$(y - b) = -\frac{b}{a}(x - a)$$

$$\Rightarrow bx + ay = ab + ab$$

$$\Rightarrow bx + ay = 2ab$$

$$\Rightarrow \frac{x}{a} + \frac{y}{b} = 2$$

Tangents and Normals Ex 16.2 Q19

We have,

$$x = \sin 3t, \quad y = \cos 2t, \quad t = \frac{\pi}{4}$$

$$\therefore P = \left( x = \frac{1}{\sqrt{2}}, y = 0 \right)$$

Now,

$$\frac{dx}{dt} = 3 \cos 3t, \quad \frac{dy}{dt} = -2 \sin 2t$$

$$\begin{aligned} \therefore \text{Slope } m &= \frac{dy}{dx} = \frac{\frac{dy}{dt}}{\frac{dx}{dt}} = \frac{-2 \sin 2t}{3 \cos 3t} \\ &= \frac{-2}{-3 \times \frac{1}{\sqrt{2}}} \\ &= \frac{+2\sqrt{2}}{3} \end{aligned}$$

Thus, equation of tangent is

$$(y - 0) = \frac{+2\sqrt{2}}{3} \left( x - \frac{1}{\sqrt{2}} \right)$$

$$2\sqrt{2}x - 3y = 2$$

\*\*\*\*\* END \*\*\*\*\*