



Exercise 16A

Q5

Answer :

Given :

$$AB = AC, BD = DC$$

To prove : $\triangle ADB \cong \triangle ADC$

Proof :

(i) In $\triangle ADB$ and $\triangle ADC$:

$$AB = AC \quad (\text{given})$$

$$BD = DC \quad (\text{given})$$

$$DA = DA \quad (\text{common})$$

By SSS congruence property :

$$\triangle ADB \cong \triangle ADC$$

$$\angle ADB = \angle ADC \quad (\text{corresponding parts of the congruent triangles}) \quad \dots(1)$$

$\angle ADB$ and $\angle ADC$ are on the straight line.

$$\therefore \angle ADB + \angle ADC = 180^\circ$$

$$\angle ADB + \angle ADB = 180^\circ$$

$$\Rightarrow 2\angle ADB = 180^\circ$$

$$\Rightarrow \angle ADB = 90^\circ$$

From (1) :

$$\angle ADB = \angle ADC = 90^\circ$$

(ii) $\angle BAD = \angle CAD$ (corresponding parts of the congruent triangles)

Q6

Answer :

Given :

AD is a bisector of $\angle A$.

$$\Rightarrow \angle DAB = \angle DAC \quad \dots(1)$$

$$AD \perp BC$$

$$\Rightarrow \angle BDA = \angle CDA \quad (90^\circ \text{ each})$$

To prove :

$\triangle ABC$ is isosceles.

Proof :

In $\triangle DAB$ and $\triangle DAC$:

$$\angle BDA = \angle CDA \quad (90^\circ \text{ each})$$

$$DA = DA \quad (\text{common})$$

$$\angle DAB = \angle DAC \quad (\text{from 1})$$

By ASA congruence property :

$$\triangle DAB \cong \triangle DAC$$

$$\Rightarrow AB = AC \quad (\text{corresponding parts of the congruent triangles})$$

Therefore, $\triangle ABC$ is isosceles.

Q7

Answer :

Given :

$$AB = AD$$

$$CB = CD$$

To prove :

$$\triangle ABC \cong \triangle ADC$$

Proof:

In $\triangle ABC$ and $\triangle ADC$:

$$AB = AD \quad (\text{given})$$

$$BC = DC \quad (\text{given})$$

$$AC = AC \quad (\text{common})$$

$$\therefore \triangle ABC \cong \triangle ADC \quad (\text{by SSS congruence property})$$

Q8

Answer :

Given :

$$PA \perp AB$$

$$QB \perp AB$$

$$PA = QB$$

To prove : $\triangle OAP \cong \triangle OBQ$

Find whether $OA = OB$.

Proof:

In $\triangle OAP$ and $\triangle OBQ$:

$$\angle POA = \angle QOB \quad (\text{vertically opposite angles})$$

$$\angle OAP = \angle OBQ \quad (90^\circ \text{ each})$$

$$PA = QB \quad (\text{given})$$

By AAS congruence property :

$$\triangle OAP \cong \triangle OBQ$$

$$\Rightarrow OA = OB \quad (\text{corresponding parts of the congruent triangles})$$

Q9

Answer :

Given :

Triangles ABC and DCB are right angled at A and D , respectively.

$$AC = DB$$

To prove : $\triangle ABC \cong \triangle DCB$

In $\triangle ABC$ and $\triangle DCB$:

$$\angle CAB = \angle BDC \quad (90^\circ \text{ each})$$

$$BC = BC \quad (\text{common})$$

$$AC = DB \quad (\text{given})$$

By R.H.S. congruence property :

$$\triangle ABC \cong \triangle DCB$$

Q10

Answer :

Given :

$\triangle ABC$ is an isosceles triangle in which $AB = AC$.

E and F are midpoints of AC and AB , respectively.

To prove :

$$BE = CF$$

Proof:

E and F are midpoints of AC and AB , respectively.

$$\Rightarrow AF = FB, AE = EC$$

$$AB = AC$$

$$\Rightarrow \frac{1}{2} AB = \frac{1}{2} AC$$

$$\Rightarrow FB = EC$$

$$\angle ABC = \angle ACB \quad \left(\text{angle opposite to equal sides are equal} \right)$$

$$\Rightarrow \angle FBC = \angle ECB$$

Consider $\triangle BCF$ and $\triangle CBE$:

$$BC = BC \quad \left(\text{common} \right)$$

$$\Rightarrow \angle FBC = \angle ECB$$

Consider $\triangle BCF$ and $\triangle CBE$:

$$BC = BC \quad \left(\text{common} \right)$$

$$\angle FBC = \angle ECB \quad \left(\text{proved above} \right)$$

$$FB = EC \quad \left(\text{proved above} \right)$$

By SAS congruence property:

$$\triangle BCF \cong \triangle CBE$$

$$BE = CF \quad \left(\text{corresponding parts of the congruent triangles} \right)$$

Q11

Answer:

Given:

$$AB = AC$$

$\triangle ABC$ is an isosceles triangle.

***** END *****