



Trigonometric Ratios Ex 5.1 Q11

**Answer :**

Given:

$$3 \cot \theta = 2$$

Therefore,

$$\cot \theta = \frac{2}{3} \dots\dots (1)$$

Now, we know that  $\cot \theta = \frac{\cos \theta}{\sin \theta}$

Therefore equation (1) becomes

$$\frac{\cos \theta}{\sin \theta} = \frac{2}{3} \dots\dots (2)$$

Now, by applying Invertendo to equation (2)

We get,

$$\frac{\sin \theta}{\cos \theta} = \frac{3}{2} \dots\dots (3)$$

Now, multiplying by  $\frac{4}{3}$  on both sides

We get,

$$\frac{4}{3} \times \frac{\sin \theta}{\cos \theta} = \frac{4}{3} \times \frac{3}{2}$$

Therefore, 3 cancels out on R.H.S and

We get,

$$\frac{4 \sin \theta}{3 \cos \theta} = \frac{2}{1}$$

Now by applying dividendo in above equation

We get,

$$\frac{4 \sin \theta - 3 \cos \theta}{3 \sin \theta} = \frac{2-1}{1}$$

$$\frac{4 \sin \theta - 3 \cos \theta}{3 \sin \theta} = \frac{1}{1} \dots\dots (4)$$

Now, multiplying by  $\frac{2}{6}$  on both sides of equation (3)

We get,

$$\frac{2}{6} \times \frac{\sin \theta}{\cos \theta} = \frac{2}{6} \times \frac{3}{2}$$

Therefore, 2 cancels out on R.H.S and

We get,

$$\frac{2 \sin \theta}{6 \cos \theta} = \frac{3}{6}$$

$$\frac{2 \sin \theta}{6 \cos \theta} = \frac{1}{2}$$

Now by applying componendo in above equation

We get,

$$\frac{2 \cos \theta + 6 \sin \theta}{6 \sin \theta} = \frac{1+2}{2}$$

$$\frac{2 \cos \theta + 6 \sin \theta}{6 \sin \theta} = \frac{3}{2} \dots\dots (5)$$

Now, by dividing equation (4) by equation (5)

We get,

$$\frac{\frac{4 \sin \theta - 3 \cos \theta}{3 \sin \theta}}{\frac{2 \cos \theta + 6 \sin \theta}{6 \sin \theta}} = \frac{\frac{1}{1}}{\frac{3}{2}}$$

Therefore,

$$\frac{4 \sin \theta - 3 \cos \theta}{3 \sin \theta} \times \frac{6 \sin \theta}{2 \cos \theta + 6 \sin \theta} = \frac{1}{1} \times \frac{2}{3}$$

$$\frac{4 \sin \theta - 3 \cos \theta}{3 \sin \theta} \times \frac{2 \times (3 \sin \theta)}{2 \cos \theta + 6 \sin \theta} = \frac{1}{1} \times \frac{2}{3}$$

Therefore, on L.H.S  $(3 \sin \theta)$  cancels out and we get,

$$\frac{2 \times (4 \sin \theta - 3 \cos \theta)}{2 \cos \theta + 6 \sin \theta} = \frac{2}{3}$$

Now, by taking 2 in the numerator of L.H.S on the R.H.S

We get,

$$\frac{4 \sin \theta - 3 \cos \theta}{2 \cos \theta + 6 \sin \theta} = \frac{2}{3 \times 2}$$

Therefore, 2 cancels out on R.H.S. and

We get,

$$\frac{4 \sin \theta - 3 \cos \theta}{2 \cos \theta + 6 \sin \theta} = \frac{1}{3}$$

Hence,

$$\frac{4 \sin \theta - 3 \cos \theta}{2 \cos \theta + 6 \sin \theta} = \frac{1}{3}$$

**Answer :**

Given:

$$\tan \theta = \frac{a}{b} \dots\dots (1)$$

$$\text{Now, we know that } \tan \theta = \frac{\sin \theta}{\cos \theta}$$

Therefore equation (1) becomes

$$\frac{\sin \theta}{\cos \theta} = \frac{a}{b} \dots\dots (2)$$

Now, multiplying by  $\frac{a}{b}$  on both sides of equation (2)

We get,

$$\frac{a}{b} \times \frac{\sin \theta}{\cos \theta} = \frac{a}{b} \times \frac{a}{b}$$

Therefore,

$$\frac{a \sin \theta}{b \cos \theta} = \frac{a^2}{b^2} \dots\dots (3)$$

Now by applying dividendo in above equation (3)

We get,

$$\frac{a \sin \theta - b \cos \theta}{b \cos \theta} = \frac{a^2 - b^2}{b^2} \dots\dots (4)$$

Now by applying componendo in equation (3)

We get,

$$\frac{a \sin \theta - b \cos \theta}{b \cos \theta} = \frac{a^2 - b^2}{b^2} \dots\dots (4)$$

Now by applying componendo in equation (3)

We get,

$$\frac{a \sin \theta + b \cos \theta}{b \cos \theta} = \frac{a^2 + b^2}{b^2} \dots\dots (5)$$

Now, by dividing equation (4) by equation (5)

We get,

$$\frac{\frac{a \sin \theta - b \cos \theta}{b \cos \theta}}{\frac{a \sin \theta + b \cos \theta}{b \cos \theta}} = \frac{\frac{a^2 - b^2}{b^2}}{\frac{a^2 + b^2}{b^2}}$$

Therefore,

$$\frac{a \sin \theta - b \cos \theta}{b \cos \theta} \times \frac{b \cos \theta}{a \sin \theta + b \cos \theta} = \frac{a^2 - b^2}{b^2} \times \frac{b^2}{a^2 + b^2}$$

Therefore,  $b \cos \theta$  and  $b^2$  cancels on L.H.S and R.H.S respectively and we get,

$$\frac{a \sin \theta - b \cos \theta}{a \sin \theta + b \cos \theta} = \frac{a^2 - b^2}{a^2 + b^2}$$

Hence, it is proved that

$$\frac{a \sin \theta - b \cos \theta}{a \sin \theta + b \cos \theta} = \frac{a^2 - b^2}{a^2 + b^2}$$

\*\*\*\*\* END \*\*\*\*\*