



### Solutions Of Geometric Progressions Ex 20.1 Q 11

5, 10, 20, ...  $n$  term

1280, 640, 320, ...,  $n$  terms.

Let  $t_n$  be the general term of first G.P and  $t_n'$  be general term of second G.P whose  $n$ th terms are equal.

$a$  for first G.P = 5

$a$  for second G.P = 1280

$r$  for first G.P =  $\frac{10}{5} = 2$

$r$  for second G.P =  $\frac{640}{1280} = \frac{1}{2}$

$t_n = ar^{n-1}$

Applying and equating for both G.P's

$$(5)(2)^{n-1} = 1280 \left(\frac{1}{2}\right)^{n-1}$$

$$(2)^{n-1} = \frac{1280}{5} \left(\frac{1}{2}\right)^{n-1}$$

$$= 256 \left(\frac{1}{2}\right)^{n-1}$$

$$= 2^8 \left(\frac{1}{2}\right)^{n-1}$$

$$\frac{(2)^{n-1}}{28} = \left(\frac{1}{2}\right)^{n-1} = 2^{n-1} = 2^{-n+1}$$

$$\Rightarrow \begin{aligned} 2n &= 10 \\ n &= 5 \end{aligned}$$

### Solutions Of Geometric Progressions Ex 20.1 Q 12

We have

$$(a^2 + b^2 + c^2)p^2 - 2(ab + bc + cd)p + (b^2 + c^2 + d^2) \leq 0$$

$$(a^2p^2 - 2abp + b^2) + (b^2p^2 - 2bcp + c^2) + (c^2p^2 - 2cdp + d^2) \leq 0$$

$$(ap - b)^2 + (bp - c)^2 + (cp - d)^2 \leq 0$$

This is only possible when

$$ap - b = 0 \Rightarrow p = \frac{b}{a}$$

$$bp - c = 0 \Rightarrow p = \frac{c}{b}$$

$$cp - d = 0 \Rightarrow p = \frac{d}{c}$$

Thus

$$\frac{b}{a} = \frac{c}{b} = \frac{d}{c}$$

Hence  $a, b, c$  and  $d$  are in G.P

### Solutions Of Geometric Progressions Ex 20.1 Q 13

$$\frac{a+bx}{a-bx} = \frac{b+cx}{b-cx} = \frac{c+dx}{c-dx}, \text{ to show that } a, b, c, d \text{ are in G.P}$$

$$\Rightarrow \text{ to show } \frac{b}{a} = \frac{c}{b} = \frac{d}{c} \quad \text{---(i)}$$

Now,

$$\frac{a+bx}{a-bx} = \frac{b+cx}{b-cx} \text{ and } \frac{b+cx}{b-cx} = \frac{c+dx}{c-dx}$$

Cross multiplying

$$(a+bx)(b-cx) = (b+cx)(a-bx)$$

$$ab - acx + b^2x - bcx^2 = ab - b^2x + acx - bcx^2$$

Cancelling  $ab$  and  $-bcx^2$  on both sides

$$-acx + b^2x = -b^2x + acx$$

$$x(b^2 - ac) = -x(b^2 - ac)$$

$$2b^2x = 2acx$$

$$2b^2 = 2ac = b^2 = ac$$

$$\text{From (i)} \quad b^2 = ac$$

Also,

$$\frac{cx+b}{b-cx} = \frac{c+dx}{c-dx}, \text{ cross multiplying}$$

$$c^2x - cdx^2 + bc - bdx = bc + bdx - c^2x - cdx^2$$

$$2c^2x = 2bdx$$

$$\text{From (i)} \quad c^2 = bd$$

Hence,  $a, b, c, d$  are in G.P.

Solutions Of Geometric Progressions Ex 20.1 Q 14

We have

$$a_5 = p$$

$$a_8 = q$$

$$a_{11} = s$$

We have to show that

$$q^2 = ps$$

$$\Rightarrow \frac{q}{p} = \frac{s}{q}$$

$$\text{Now, } q = ar^7$$

$$p = ar^4$$

$$s = ar^{10}$$

$$\therefore \frac{q}{p} = \frac{s}{q}$$

$$\Rightarrow \frac{ar^7}{ar^4} = \frac{ar^{10}}{ar^7}$$

$$\Rightarrow r^3 = r^3$$

Hence proved.

\*\*\*\*\* END \*\*\*\*\*