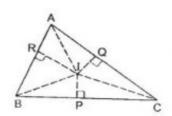


Exercise 5A

Question 30:

Given: A triangle ABC in which bisectors of $\angle B$ and $\angle C$ meet at I.



Also, we have IP \perp BC, IQ \perp CA and IR \perp AB

To Prove:(i) IP=IQ=IR

(ii) ∠IAR=∠IAQ

Proof:(i) In ΔBIP and ΔBIR we have,

 $\angle PBI = \angle RBI$ [Given]

 $\angle IRB = \angle IPB = 90^{\circ}$ [Given]

[By AAS]

and, IB = IB [Common]

Thus by Angle-Angle-Side criterion of congruence, we have

ΔBIP ≅ ΔBIR

The corresponding parts of the congruent triangles are equal.

So, IP = IR

Similarly IP = IQ

: IP = IQ = IR

(ii) Now in ΔAIR and ΔAIQ we have

IR = IQ [Proved above]

IA = IA [Common]

and, $\angle IRA = \angle IQA = 90^{\circ}$

Thus by Side-Angle-Side criterion of congruence, we have

∴ ΔAIR ≅ ΔAIQ [By SAS]

The corresponding parts of the congruent triangles are equal.

So, $\angle IAR = \angle IAQ$ [by c.p.c.t]

⇒ IA bisects ∠A