

Properties of Triangles Ex 15.2 Q19

Answer:

- (i) No, because if there are two right angles in a triangle, then the third angle of the triangle must be zero, which is not possible.
- (ii) No, because as we know that the sum of all three angles of a triangle is always 180° . If there are two obtuse angles, then their sum will be more than 180° , which is not possible in case of a triangle.
- (iii) Yes, in right triangles and acute triangles, it is possible to have two acute angles.
- (iv) No, because if each angle is less than 60°, then the sum of all three angles will be less than 180°, which is not possible in case of a triangle.

Proof

Let the three angles of the triangle be $\angle A$, $\angle B$ and $\angle C$.

As per the given information,

∠A < 60° ...(i)

∠B < 60° ...(ii)

∠C < 60° ...(iii)

On adding (i), (ii) and (iii), we get:

$$\angle A + \angle B + \angle C < 60^{\circ} + 60^{\circ} + 60^{\circ}$$

$$\angle A + \angle B + \angle C < 180^{\circ}$$

We can see that the sum of all three angles is less than $180\degree$, which is not possible for a triangle.

Hence, we can say that it is not possible for each angle of a triangle to be less than 60° .

(v) No, because if each angle is greater than 60° , then the sum of all three angles will be greater than 180° , which is not possible.

Proof

Let the three angles of the given triangle be $\angle A$, $\angle B$ and $\angle C$.

As per the given information,

∠A > 60° ...(i)

 $\angle B > 60^{\circ}$...(ii)

 $\angle C > 60^{\circ} \dots (iii)$

On adding (i), (ii) and (iii), we get:

$$\angle A + \angle B + \angle C > 60^{\circ} + 60^{\circ} + 60^{\circ}$$

$$\angle A + \angle B + \angle C > 180^{\circ}$$

We can see that the sum of all three angles of the given triangle are greater than 180°, which is not possible for a triangle.

Hence, we can say that it is not possible for each angle of a triangle to be greater than 60° .

(vi) Yes, if each angle of the triangle is equal to 60°, then the sum of all three angles will be 180°, which is possible in case of a triangle.

Proof

Let the three angles of the given triangle be $\angle A$, $\angle B$ and $\angle C$.

As per the given information,

$$\angle A = 60^{\circ} \dots (i)$$

$$\angle C = 60^{\circ} \dots (iii)$$

On adding (i), (ii) and (iii), we get:

$$\angle A + \angle B + \angle C = 60^{\circ} + 60^{\circ} + 60^{\circ}$$

$$\angle A + \angle B + \angle C = 180^{\circ}$$

We can see that the sum of all three angles of the given triangle is equal to 180° , which is possible in case of a triangle.

Hence, we can say that it is possible for each angle of a triangle to be equal to 60° .