

Functions Ex 2.3 Q2

We have, 
$$f(x) = x^2 + x + 1$$
 and  $g(x) = \sin x$ 

Now,

$$f \circ g(x) = f(g(x)) = f(\sin x)$$

$$\Rightarrow f \circ g(x) = \sin^2 x + \sin x + 1$$

Again, 
$$g \circ f(x) = g(f(x)) = g(x^2 + x + 1)$$
  

$$\Rightarrow g \circ f(x) = sin(x^2 + x + 1)$$
Clearly

Functions Ex 2.3 Q3

We have 
$$f(x) = |x|$$

We assume the domain of f = RRange of  $f = (0, \infty)$ 

- $\therefore$  Range of  $f \subset domain of f$
- $\therefore f \circ f$  exists.

Now,

$$f \circ f(x) = f(f(x)) = f(x) = |x| = f(x)$$

$$\therefore \ f\circ f=f$$

Functions Ex 2.3 Q4

$$f(x) = 2x + 5$$
 and  $g(x) = x^2 + 1$ 

- $\therefore$  Range of f = R and range of  $g = [1, \infty]$
- $\therefore$  Range of  $f \subseteq Domain of <math>g(R)$  and range of  $g \subseteq domain of <math>f(R)$
- .. both fog and gof exist.

i) 
$$f \circ g(x) = f(g(x)) = f(x^2 + 1)$$
  
=  $2(x^2 + 1) + 5$ 

$$\Rightarrow f \circ g(x) = 2x^2 + 7$$

ii) 
$$g \circ f(x) = g(f(x)) = g(2x + 5)$$
  
=  $(2x + 5)^2 + 1$ 

$$\Rightarrow g \circ f(x) = 4x^2 + 20x + 26$$

ii) 
$$f \circ f(x) = f(f(x)) = f(2x + 5)$$
  
=  $2(2x + 5) + 5$   
 $f \circ f(x) = 4x + 15$ 

iv) 
$$f^2(x) = [f(x)]^2 = (2x + 5)^2$$
  
=  $4x^2 + 20x + 25$ 

∴ from (iii)&(iv)  
$$f \circ f \neq f^2$$

Functions Ex 2.3 Q5

We have,  $f(x) = \sin x$  and g(x) = 2x.

Domain of f and g is R

Range of 
$$f = [-1, 1]$$
  
Range of  $g = R$ 

- ∴ Range of f ⊂ Domain g and Range of g ⊆Domain f
- .. fog and gof both exist.

i) 
$$g \circ f(x) = g(f(x)) = g(\sin x) = g \circ f(x) = 2\sin x$$

ii) 
$$f \circ g(x) = f(g(x)) = f(2x) = \sin 2x$$

Functions Ex 2.3 Q6

f,g, and h are real functions given by  $f(x) = \sin x$ , g(x) = 2x and  $h(x) = \cos x$ . To prove:  $f \circ g = g \circ (fh)$ L.H.S  $f \circ g(x) = f(g(x))$   $= f(2x) = \sin 2x$   $\Rightarrow f \circ g(x) = 2 \sin x \cos x \dots (A)$ R.H.S  $g \circ (fh)(x) = go(f(x).h(x))$   $= g(\sin x \cos x)$   $g \circ (fh)(x) = 2 \sin x \cos x \dots (B)$ from A & B  $f \circ g(x) = g \circ (fh)(x)$ 

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