



Co-Ordinate Geometry Ex 14.2 Q26

Answer :

The distance d between two points (x_1, y_1) and (x_2, y_2) is given by the formula

$$d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

In a rhombus all the sides are equal in length. And the area 'A' of a rhombus is given as

$$A = \frac{1}{2} (\text{Product of both diagonals})$$

Here the four points are $A(-3, 2)$, $B(-5, -5)$, $C(2, -3)$ and $D(4, 4)$

First let us check if all the four sides are equal.

$$AB = \sqrt{(-3+5)^2 + (2+5)^2}$$

$$= \sqrt{(2)^2 + (7)^2}$$

$$= \sqrt{4+49}$$

$$AB = \sqrt{53}$$

$$BC = \sqrt{(-5-2)^2 + (-5+3)^2}$$

$$= \sqrt{(-7)^2 + (-2)^2}$$

$$= \sqrt{49+4}$$

$$BC = \sqrt{53}$$

$$CD = \sqrt{(2-4)^2 + (-3-4)^2}$$

$$= \sqrt{(-2)^2 + (-7)^2}$$

$$= \sqrt{4+49}$$

$$CD = \sqrt{53}$$

$$AD = \sqrt{(-3-4)^2 + (2-4)^2}$$

$$= \sqrt{(-7)^2 + (-2)^2}$$

$$= \sqrt{49+4}$$

$$AD = \sqrt{53}$$

Here, we see that all the sides are equal, so it has to be a rhombus.

Hence we have proved that the quadrilateral formed by the given four vertices is a **rhombus**.

Now let us find out the lengths of the diagonals of the rhombus.

$$AC = \sqrt{(-3-2)^2 + (2+3)^2}$$

$$= \sqrt{(-5)^2 + (5)^2}$$

$$= \sqrt{25+25}$$

$$= \sqrt{50}$$

$$AC = 5\sqrt{2}$$

$$BD = \sqrt{(-5-4)^2 + (-5-4)^2}$$

$$= \sqrt{(-9)^2 + (-9)^2}$$

$$= \sqrt{81+81}$$

$$= \sqrt{162}$$

$$BD = 9\sqrt{2}$$

Now using these values in the formula for the area of a rhombus we have,

$$A = \frac{(5\sqrt{2})(9\sqrt{2})}{2}$$

$$= \frac{(5)(9)(2)}{2}$$

$$A = 45$$

Thus the area of the given rhombus is **45 square units**.

Co-Ordinate Geometry Ex 14.2 Q27

Answer :

The distance d between two points (x_1, y_1) and (x_2, y_2) is given by the formula

$$d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

The circumcentre of a triangle is the point which is equidistant from each of the three vertices of the triangle.

Here the three vertices of the triangle are given to be $A(3,0)$, $B(-1,-6)$ and $C(4,-1)$

Let the circumcentre of the triangle be represented by the point $R(x, y)$.

So we have $AR = BR = CR$

$$AR = \sqrt{(3-x)^2 + (-y)^2}$$

$$BR = \sqrt{(-1-x)^2 + (-6-y)^2}$$

$$CR = \sqrt{(4-x)^2 + (-1-y)^2}$$

Equating the first pair of these equations we have,

$$AR = BR$$

$$\sqrt{(3-x)^2 + (-y)^2} = \sqrt{(-1-x)^2 + (-6-y)^2}$$

Squaring on both sides of the equation we have,

$$(3-x)^2 + (-y)^2 = (-1-x)^2 + (-6-y)^2$$

$$9 + x^2 - 6x + y^2 = 1 + x^2 + 2x + 36 + y^2 + 12y$$

$$8x + 12y = -28$$

$$2x + 3y = -7$$

Equating another pair of the equations we have,

$$AR = CR$$

$$\sqrt{(3-x)^2 + (-y)^2} = \sqrt{(4-x)^2 + (-1-y)^2}$$

Squaring on both sides of the equation we have,

$$(3-x)^2 + (-y)^2 = (4-x)^2 + (-1-y)^2$$

$$9 + x^2 - 6x + y^2 = 16 + x^2 - 8x + 1 + y^2 + 2y$$

$$2x - 2y = 8$$

$$x - y = 4$$

Now we have two equations for 'x' and 'y', which are

$$2x + 3y = -7$$

$$x - y = 4$$

From the second equation we have $y = x - 4$. Substituting this value of 'y' in the first equation we have,

$$2x + 3(x - 4) = -7$$

$$2x + 3x - 12 = -7$$

$$5x = 5$$

$$x = 1$$

Therefore the value of 'y' is,

$$y = x - 4$$

$$= 1 - 4$$

$$y = -3$$

Hence the co-ordinates of the circumcentre of the triangle with the given vertices are $(1, -3)$.

The length of the circumradius can be found out substituting the values of 'x' and 'y' in 'AR'

$$AR = \sqrt{(3-x)^2 + (-y)^2}$$

$$= \sqrt{(3-1)^2 + (3)^2}$$

$$= \sqrt{(2)^2 + (3)^2}$$

$$= \sqrt{4+9}$$

$$AR = \sqrt{13}$$

Thus the circumradius of the given triangle is $\sqrt{13}$ units.

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