

Exercise 16C

Question 3:

(i) Let A(0, 1), B(1, 2) and C(-2, -1) be the given points. Then, $(x_1 = 0, y_1 = 1)(x_2 = 1, y_2 = 2), (x_3 = -2, y_3 = -1)$

:. Area of
$$\triangle ABC = \frac{1}{2} \left[x_1 (y_2 - y_3) + x_2 (y_3 - y_1) + x_3 (y_1 - y_2) \right]$$

$$= \frac{1}{2} \left[0 \times (2+1) + 1(-1-1) + (-2) \times (1-2) \right]$$

$$= \frac{1}{2} (0-2+2) = 0$$

Hence the given points are collinear

(ii) Let A(-5, 1), B(5,5) and C(10, 7) be the given points.

:. Then,
$$(x_1 = -5, y_1 = 1)(x_2 = 5, y_2 = 5)(x_3 = 10, y_3 = 7)$$

:. Area of
$$\triangle ABC = \frac{1}{2} \left[x_1 (y_2 - y_1) + x_2 (y_3 - y_1) + x_3 (y_1 - y_2) \right]$$

$$= \frac{1}{2} \left[(-5) (5 - 7) + 5 (7 - 1) + 10 (1 - 5) \right]$$

$$= \frac{1}{2} \left[10 + 30 - 40 \right] = 0$$

Hence the given points are collinear

(iii) Let P(a, b + c), Q(b, c + a) and R(c, a + B) be the given points.

Then,
$$(x_1 = 1, y_1 = b + c)$$
, $(x_2 = b, y_2 = c + a)$, $(x_3 = c, y_3 = a + b)$

:. Area of
$$\triangle PQR = \frac{1}{2} \left[x_1 (y_2 - y_3) + x_2 (y_3 - y_1) + x_3 (y_1 - y_3) \right]$$

$$= \frac{1}{2} a(c+a-a-b) + b(a+b-b-c) + c(b+c-c-a)$$

$$= \frac{1}{2} [a(c-b) + b(a-c) + c(b-a)] = 0$$

Hence the given points are collinear

Question 4:

(i) The given points are A(-1, 3), B(2, p) and C(5, -1)

$$(x_1 = -1, y_1 = 3)(x_2 = 2, y_2 = p)(x_3 = 5, y_3 = -1)$$

The given point A,B,C are collinear if

$$x_1(y_2 - y_1) + x_2(y_3 - y_1) + x_3(y_1 - y_2) = 0$$

$$\Rightarrow (-1)(p+1)+2(-1-3)+5(3-p)=0$$

$$\Rightarrow -p - 1 - 8 + 15 - 5p = 0$$

$$\Rightarrow$$
 -6p + 6 = 0 \Rightarrow -6p = -6

$$p = \frac{6}{6} = 1$$

Hence, p = 1

(ii) The given points are A(3, 2), B(4, p) and C(5, 3)

$$(\mathbf{x}_1 = 3, y_1 = 2), (\mathbf{x}_2 = 4, y_2 = p) \text{ and } (\mathbf{x}_3 = 5, y_3 = 3)$$
 The given point s A, B, C are collinear if
$$\mathbf{x}_1(y_2 - y_3) + \mathbf{x}_2(y_3 - y_1) + \mathbf{x}_3(y_1 - y_2) = 0$$

$$\Rightarrow 3(p-3) + 4(3-2) + 5(2-p) = 0$$

$$3p-9+4+10-5p=0$$

$$-2p=-5 \Rightarrow p=\frac{5}{2}$$
 Hence,
$$p=\frac{5}{2}$$
 (iii) The three points are A(-3, 9), B(2, p), C(4, -5) Let
$$\mathbf{x}_1 = -3, \ y_1 = 9; \ \mathbf{x}_2 = 2, y_2 = p; \ \mathbf{x}_3 = 4, y_3 = -5$$
 Three points $(\mathbf{x}_1y_1), (\mathbf{x}_2y_2)$ and (\mathbf{x}_3y_3) are collinear if
$$\mathbf{x}_1(y_2-y_3) + \mathbf{x}_2(y_3-y_2) + (y_1-y_2) = 0$$

$$\Rightarrow -3(p+5) + 2(-5-9) + 4(9-p) = 0$$

$$\Rightarrow -3p-15-28+36-4p=0 \text{ or } -7p-7=0$$

$$\therefore 7p=-7$$

$$p=\frac{-7}{7}=-1$$

********* END *******