

## Maxima and Minima 18.5 Q33

Let P(x,y) be a point on the curve  $y^2 = 2x$  which is minimum distance from the point A(1,4).

S =square of the length of AP

$$S = (x-1)^2 + (y-4)^2$$

Using this equation, we have

$$S = x^2 + 1 - 2x + y^2 + 16 - 8y$$

$$S = x^2 - 2x + 2x + 17 - 8y$$

$$S = \frac{y^4}{4} - 8y + 1$$

$$S = \frac{y^4}{4} - 8y + 17$$
 
$$\left[ \text{Since } x = \frac{y^2}{2} \right]$$

$$\frac{dS}{dy} = y^3 - 8$$

For maxima and minima, we have

$$\frac{dS}{dv} = 0$$

$$y^3 - 8 = 0$$
$$y^3 = 2^3$$
$$y = 2$$

$$y^3 = 2$$

$$y = 2$$

Now,

$$\frac{d^2S}{dv^2} = 3y^2$$

$$\frac{d^2S}{dy^2} = 12 > 0$$

$$\therefore y = 2 \text{ is minimum point}$$
We have

$$x = \frac{y^2}{2}$$

We have  $x = \frac{y^2}{2}$   $= \frac{4}{2}$  = 2Hence, (2,2) is at a minimum distance from the point (1,4).

Maxima and Minima 18.5 Q34

The given equation of curve is

$$y = x^3 + 3x^2 + 2x - 27$$
 --- (i)

Slope of (i)

$$m = \frac{dy}{dx} = -3x^2 + 6x + 2$$
 --- (ii)

Now,

$$\frac{dm}{dx} = -6x + 6$$

and 
$$\frac{d^2m}{dx^2} = -6 < 0$$

For maxima and minima,

$$\frac{dm}{dx} = 0$$

$$\Rightarrow$$
  $-6x + 6 = 0$ 

$$\Rightarrow x = 1$$

$$\frac{d^2m}{dx^2} = -6 < 0$$

x = 1 is point of local maxima

Hence, maximum slope = -3+6+2=5

Maxima and Minima 18.5 Q35

We have,

Cost of producing x radio sets is Rs.  $\frac{x^2}{4} + 35x + 25$ Selling price of x radio is Rs.  $x \left( 50 - \frac{x}{2} \right)$ 

So,

Profit on x radio sets is

$$P = Rs \left( 50x - \frac{x^2}{2} - \frac{x^2}{4} - 35x - 25 \right)$$

$$\frac{dP}{dx} = 50 - x - \frac{x}{2} - 35$$
$$= 15 - \frac{3}{2}x$$

For maxima and minima,

$$\frac{dP}{dx} = 0$$

$$\Rightarrow 15 - \frac{3}{2}x = 0$$

$$\Rightarrow x = 10$$

Also,

$$\frac{d^2P}{dx^2} = \frac{-3}{2} < 0$$

x = 10 is the point of local maxima

Hence, the daily output should be 10 radio sets.

Maxima and Minima 18.5 Q35 We have,

Cost of producing 
$$x$$
 radio sets is Rs.  $\frac{x^2}{4} + 35x + 25$   
Selling price of  $x$  radio is Rs.  $x \left( 50 - \frac{x}{2} \right)$ 

So,

Profit on x radio sets is

$$P = Rs \left( 50x - \frac{x^2}{2} - \frac{x^2}{4} - 35x - 25 \right)$$

$$\frac{dP}{dx} = 50 - x - \frac{x}{2} - 35$$

$$\therefore \frac{dP}{dx} = 50 - x - \frac{x}{2} - 35$$
$$= 15 - \frac{3}{2}x$$

For maxima and minima,

$$\frac{dP}{dx} = 0$$

$$\Rightarrow 15 - \frac{3}{2}x = 0$$

$$\Rightarrow$$
  $x = 10$ 

Also,

$$\frac{d^2p}{dx^2} = \frac{-3}{2} < 0$$

x = 10 is the point of local maxima

Hence, the daily output should be 10 radio sets.

\*\*\*\*\*\*\* END \*\*\*\*\*\*