

Quadratic Equations Ex 8.7 Q19

Answer:

Let one numbers be x then other (16-x).

Then according to question

$$\frac{1}{x} + \frac{1}{(16 - x)} = \frac{1}{3}$$

$$\frac{16 - \cancel{x} + \cancel{x}}{x(16 - x)} = \frac{1}{3}$$

$$\frac{16}{(16x - x^2)} = \frac{1}{3}$$

By cross multiplication

$$16x - x^{2} = 48$$

$$x^{2} - 16x + 48 = 0$$

$$x^{2} - 12x - 4x - 48 = 0$$

$$x(x-12) - 4(x-12) = 0$$

$$(x-12)(x-4) = 0$$

$$(x-12) = 0$$

$$x = 12$$

$$(x-4) = 0$$
$$x = 4$$

Since, x being a number,

Therefore,

When x = 12 then

$$16 - x = 16 - 12$$

= 4

Thus, two consecutive number be either 4,12

Quadratic Equations Ex 8.7 Q20

Answer:

Let the required number be 3x and (3x+3)

Then according to question

$$(3x)(3x+3) = 270$$

$$9x^2 + 9x - 270 = 0$$

$$9(x^2+x-30)=0$$

$$x^2 + x - 30 = 0$$

$$x^2 + x - 30 = 0$$

$$x^2 - 5x + 6x - 30 = 0$$

$$x(x-5)+6(x-5)=0$$

$$(x-5)(x+6)=0$$

$$(x-5)=0$$

$$x = 5$$

Quadratic Equations Ex 8.7 Q21

Answer:

Let a numbers be x and its reciprocal is $\frac{1}{x}$

Then according to question

$$x + \frac{1}{x} = \frac{17}{4}$$

$$\frac{x^2+1}{x} = \frac{17}{4}$$

By cross multiplication

$$4x^2 + 4 = 17x$$

$$4x^2 - 17x + 4 = 0$$
$$4x^2 - 17x + 4 = 0$$

$$4x^2 - x - 16x + 4 = 0$$

$$x(4x-1)-4(4x-1)=0$$

$$(4x-1)(x-4)=0$$

$$(4x-1)=0$$

$$x = \frac{1}{4}$$

Or

$$(x-4)=0$$

$$x = 4$$

Thus, two consecutive number be either

$$4 \text{ or } \frac{1}{4}$$

******* END ******