



### Arithmetic Progressions Ex 9.5 Q1

**Answer :**

In the given problem, we need to find the sum of terms for different arithmetic progressions. So, here we use the following formula for the sum of  $n$  terms of an A.P.,

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

Where;  $a$  = first term for the given A.P.

$d$  = common difference of the given A.P.

$n$  = number of terms

(i) 50, 46, 42, ... To 10 terms

Common difference of the A.P. ( $d$ )

$$= a_2 - a_1$$

$$= 46 - 50$$

$$= -4$$

Number of terms ( $n$ ) = 10

First term for the given A.P. ( $a$ ) = 50

So, using the formula we get,

$$S_{10} = \frac{10}{2} [2(50) + (10-1)(-4)]$$

$$= (5) [100 + (9)(-4)]$$

$$= (5) [100 - 36]$$

$$= (5) [64]$$

$$= 320$$

Therefore, the sum of first 10 terms for the given A.P. is **320**.

(ii) 1, 3, 5, 7, ... - 26 To 12 terms.

Common difference of the A.P. ( $d$ )

$$= a_2 - a_1$$

$$= 3 - 1$$

$$= 2$$

Number of terms ( $n$ ) = 12

First term for the given A.P. ( $a$ ) = 1

So, using the formula we get,

$$S_n = \frac{12}{2} [2(1) + (12-1)(2)]$$

$$= (6) [2 + (11)(2)]$$

$$= (6) [2 + 22]$$

$$= (6) [24]$$

$$= 144$$

Therefore, the sum of first 12 terms for the given A.P. is **144**.

(iii)  $3, \frac{9}{2}, 6, \frac{15}{2}, \dots$  To 25 terms.

Common difference of the A.P. ( $d$ ) =  $a_2 - a_1$

$$= \frac{9}{2} - 3$$

$$= \frac{9-6}{2}$$

$$= \frac{3}{2}$$

Number of terms ( $n$ ) = 25

First term for the given A.P. ( $a$ ) = 3

So, using the formula we get,

$$\begin{aligned} S_{25} &= \frac{25}{2} \left[ 2(3) + (25-1) \left( \frac{3}{2} \right) \right] \\ &= \left( \frac{25}{2} \right) \left[ 6 + (24) \left( \frac{3}{2} \right) \right] \\ &= \left( \frac{25}{2} \right) \left[ 6 + \left( \frac{72}{2} \right) \right] \\ &= \left( \frac{25}{2} \right) [6 + 36] \\ &= \left( \frac{25}{2} \right) [42] \\ &= (25)(21) \\ &= 525 \end{aligned}$$

On further simplifying, we get,

$$S_{25} = 525$$

Therefore, the sum of first 25 terms for the given A.P. is **525**.

(iv) 41, 36, 31, ... To 12 terms.

Common difference of the A.P. ( $d$ ) =  $a_2 - a_1$

$$= 36 - 41$$

$$= -5$$

Number of terms ( $n$ ) = 12

First term for the given A.P. ( $a$ ) = 41

So, using the formula we get,

$$\begin{aligned} S_{12} &= \frac{12}{2} [2(41) + (12-1)(-5)] \\ &= (6) [82 + (11)(-5)] \\ &= (6) [82 - 55] \\ &= (6) [27] \\ &= 162 \end{aligned}$$

Therefore, the sum of first 12 terms for the given A.P. is **162**.

(v)  $a + b, a - b, a - 3b, \dots$  To 22 terms.

Common difference of the A.P. ( $d$ ) =  $a_2 - a_1$

$$= (a - b) - (a + b)$$

$$= a - b - a - b$$

$$= -2b$$

Number of terms ( $n$ ) = 22

First term for the given A.P. ( $a$ ) =  $a + b$

So, using the formula we get,

$$\begin{aligned} S_{22} &= \frac{22}{2} [2(a+b) + (22-1)(-2b)] \\ &= (11) [2a + 2b + (21)(-2b)] \\ &= (11) [2a + 2b - 42b] \\ &= (11) [2a - 40b] \\ &= 22a - 440b \end{aligned}$$

Therefore, the sum of first 22 terms for the given A.P. is  $\boxed{22a - 440b}$ .

(vi)  $(x-y)^2, (x^2+y^2), (x+y)^2, \dots$  To  $n$  terms.

Common difference of the A.P.  $(d) = a_2 - a_1$

$$\begin{aligned} &= (x^2 + y^2) - (x-y)^2 \\ &= x^2 + y^2 - (x^2 + y^2 - 2xy) \\ &= x^2 + y^2 - x^2 - y^2 + 2xy \\ &= 2xy \end{aligned}$$

Number of terms  $(n) = n$

First term for the given A.P.  $(a) = (x-y)^2$

So, using the formula we get,

$$S_n = \frac{n}{2} [2(x-y)^2 + (n-1)2xy]$$

Now, taking 2 common from both the terms inside the bracket we get,

$$\begin{aligned} &= \left(\frac{n}{2}\right) [(2)(x-y)^2 + (2)(n-1)xy] \\ &= \left(\frac{n}{2}\right) (2) [(x-y)^2 + (n-1)xy] \\ &= (n) [(x-y)^2 + (n-1)xy] \end{aligned}$$

Therefore, the sum of first  $n$  terms for the given A.P. is  $\boxed{n[(x-y)^2 + (n-1)xy]}$

(vii)  $\frac{x-y}{x+y}, \frac{3x-2y}{x+y}, \frac{5x-3y}{x+y}, \dots$  To  $n$  terms.

Number of terms  $(n) = n$

First term for the given A.P.  $(a) = \left(\frac{x-y}{x+y}\right)$

Common difference of the A.P.  $(d) = a_2 - a_1$

$$\begin{aligned} &= \left(\frac{3x-2y}{x+y}\right) - \left(\frac{x-y}{x+y}\right) \\ &= \frac{(3x-2y) - (x-y)}{x+y} \\ &= \frac{3x-2y-x+y}{x+y} \\ &= \frac{2x-y}{x+y} \end{aligned}$$

So, using the formula we get,

$$\begin{aligned} S_n &= \frac{n}{2} \left[ 2 \left( \frac{x-y}{x+y} \right) + (n-1) \left( \frac{2x-y}{x+y} \right) \right] \\ &= \left( \frac{n}{2} \right) \left[ \left( \frac{2x-2y}{x+y} \right) + \left( \frac{(n-1)(2x-y)}{x+y} \right) \right] \\ &= \left( \frac{n}{2} \right) \left[ \left( \frac{2x-2y}{x+y} \right) + \left( \frac{n(2x-y)-1(2x-y)}{x+y} \right) \right] \\ &= \left( \frac{n}{2} \right) \left[ \left( \frac{2x-2y}{x+y} \right) + \left( \frac{n(2x-y)-2x+y}{x+y} \right) \right] \end{aligned}$$

Now, on further solving the above equation we get,

$$\begin{aligned} &= \left( \frac{n}{2} \right) \left( \frac{2x-2y+n(2x-y)-2x+y}{x+y} \right) \\ &= \left( \frac{n}{2} \right) \left( \frac{n(2x-y)-y}{x+y} \right) \end{aligned}$$

Therefore, the sum of first  $n$  terms for the given A.P. is  $\boxed{\left( \frac{n}{2} \right) \left( \frac{n(2x-y)-y}{x+y} \right)}$ .

(viii)  $-26, -24, -22, \dots$  To 36 terms.

Common difference of the A.P. ( $d$ ) =  $a_2 - a_1$

$$= (-24) - (-26)$$

$$= -24 + 26$$

$$= 2$$

Number of terms ( $n$ ) = 36

First term for the given A.P. ( $a$ ) =  $-26$

So, using the formula we get,

$$\begin{aligned} S_{36} &= \frac{36}{2} [2(-26) + (36-1)(2)] \\ &= (18) [-52 + (35)(2)] \\ &= (18) [-52 + 70] \\ &= (18) [18] \\ &= 324 \end{aligned}$$

Therefore, the sum of first 36 terms for the given A.P. is  $\boxed{324}$ .

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