

Quadratic Equations Ex 8.6 Q7

Answer:

The given quadric equation is $(b-c)x^2+(c-a)x+(a-b)=0$, and roots are real

Then prove that 2b = a + c.

Here,

$$a = (b-c), b = (c-a)$$
 and, $c = (a-b)$

As we know that $D = b^2 - 4ac$

Putting the value of a = (b-c), b = (c-a) and c = (a-b)

$$D = b^2 - 4ac$$

$$=(c-a)^2-4\times(b-c)\times(a-b)$$

$$=c^2-2ca+a^2-4(ab-b^2-ca+bc)$$

$$=c^2-2ca+a^2-4ab+4b^2+4ca-4bc$$

$$=c^2+2ca+a^2-4ab+4b^2-4bc$$

$$= a^2 + 4b^2 + c^2 + 2ca - 4ab - 4bc$$

As we know that
$$(a^2 + 4b^2 + c^2 + 2ca - 4ab - 4bc) = (a + c - 2b)^2$$

$$D = \left(a + c - 2b\right)^2$$

The given equation will have real roots, if D = 0

$$(a+c-2b)^2=0$$

Square root both side we get

$$\sqrt{\left(a+c-2b\right)^2}=0$$

$$a+c-2b=0$$

$$a+c=2b$$

Hence

$$2b = a + c$$

Quadratic Equations Ex 8.6 Q8

Answer:

The given quadric equation is $(a^2+b^2)x^2-2(ac+bd)x+(c^2+d^2)=0$, and roots are real Then prove that $\frac{a}{b}=\frac{c}{d}$. Here, $a=(a^2+b^2), b=-2(ac+bd) \text{ and, } c=(c^2+d^2)$ As we know that $D=b^2-4ac$ Putting the value of $a=(a^2+b^2), b=-2(ac+bd) \text{ and, } c=(c^2+d^2)$ $D=b^2-4ac=\{-2(ac+bd)\}^2-4\times(a^2+b^2)\times(c^2+d^2)=4(a^2c^2+2abcd+b^2d^2)-4(a^2c^2+a^2d^2+b^2c^2+b^2d^2)=4a^2c^2+8abcd+4b^2d^2-4a^2c^2-4a^2d^2-4b^2c^2-4b^2d^2=-4a^2d^2-4b^2c^2-2abcd$ The given equation will have real roots, if D=0 $-4(a^2d^2+b^2c^2-2abcd)=0$ $(a^2d^2+b^2c^2-2abcd)=0$

Square root both sides we get,

$$ad - bc = 0$$

$$ad = bc$$

$$\frac{a}{b} = \frac{c}{d}$$

 $(ad)^2 + (bc)^2 - 2(ad)(bc) = 0$

 $(ad - bc)^2 = 0$

Hence $\frac{a}{b} = \frac{c}{d}$

Quadratic Equations Ex 8.6 Q9

Answer:

The given equations are

$$ax^2 + 2bx + c = 0$$
 (1)

$$bx^2 - 2\sqrt{ac}x + b = 0 \quad \dots \quad (2)$$

Roots are simultaneously real

Then prove that $b^2 = ac$

Let D_1 and D_2 be the discriminants of equation (1) and (2) respectively,

Then.

$$D_1 = \left(2b\right)^2 - 4ac$$

$$=4b^2-4ac$$

And

$$D_2 = \left(-2\sqrt{ac}\right)^2 - 4 \times b \times b$$

$$=4ac-4b^2$$

Both the given equation will have real roots, if $D_1 \ge 0$ and $D_2 \ge 0$

$$4b^2 - 4ac \ge 0$$

$$4b^2 \ge 4ac$$

$$b^2 \ge ac \dots (3)$$

$$4ac - 4b^2 \ge 0$$

$$4ac \ge 4b^2$$

$$ac \ge b^2 \dots (4)$$

From equations (3) and (4) we get

$$b^2 = ac$$

Hence,
$$b^2 = ac$$

******* END ******