

Indefinite Integrals Ex 19.30 Q1

Let
$$\int \frac{2x+1}{(x+1)(x-2)} = \frac{A}{(x+1)} + \frac{B}{(x-2)}$$

$$\Rightarrow 2x + 1 = A(x - 2) + B(x + 1)$$

Put *x* = 2

$$\Rightarrow 5 = 3B \Rightarrow B = \frac{5}{3}$$

Put x = -1

$$\Rightarrow -1 = -3A \Rightarrow A = \frac{1}{3}$$

So,

$$\int \frac{2x+1}{(x+1)(x-2)} dx = \frac{1}{3} \int \frac{dx}{x+1} + \frac{5}{3} \int \frac{dx}{x-2}$$
$$= \frac{1}{3} \log|x+1| + \frac{5}{3} \log|x-2| + c$$

Thus,

$$I = \frac{1}{3} \log |x + 1| + \frac{5}{3} \log |x - 2| + c$$

Indefinite Integrals Ex 19.30 Q2

Let
$$\int \frac{1}{x(x-2)(x-4)} dx = \frac{A}{x} + \frac{B}{x-2} + \frac{C}{x-4}$$

$$\Rightarrow 1 = A(x-2)(x-4) + B(x)(x-4) + Cx(x-2)$$

Put x = 0

$$\Rightarrow 1 = 8A \Rightarrow A = \frac{1}{8}$$

Put x = 2

$$\Rightarrow 1 = -4B \qquad \Rightarrow \qquad B = -\frac{1}{4}$$

Put x = 4

$$\Rightarrow 1 = 8C \Rightarrow C = \frac{1}{8}$$

So,

$$\int \frac{1}{x(x-2)(x-4)} dx = \frac{1}{8} \int \frac{dx}{x} + \left(-\frac{1}{4}\right) \int \frac{dx}{x-2} + \frac{1}{8} \int \frac{dx}{x-4}$$
$$= \frac{1}{8} \log|x| - \frac{1}{4} \log|x-2| + \frac{1}{8} \log|x-4| + c$$
$$= \frac{1}{8} \log\left|\frac{x(x-4)}{(x-2)^2}\right| + c$$

Thus,

$$I = \frac{1}{8} \log \left| \frac{x \left(x - 4 \right)}{\left(x - 2 \right)^2} \right| + c$$

Indefinite Integrals Ex 19.30 Q3

Let
$$I = \int \frac{x^2 + x - 1}{x^2 + x - 6} dx$$

$$= \int 1 + \frac{5}{x^2 + x - 6} dx$$

$$\Rightarrow I = \int dx + \int \frac{5dx}{(x+3)(x-2)} ----(1)$$
Let $\frac{5}{(x+3)(x-2)} = \frac{A}{x+3} + \frac{B}{x-2}$

$$\Rightarrow 5 = A(x-2) + B(x+3)$$
Put $x = 2$

$$\Rightarrow 5 = 5B \Rightarrow B = 1$$
Put $x = -3$

$$\Rightarrow 5 = -5A \Rightarrow A = -1$$

$$\therefore I = \int dx + \int \frac{-dx}{x+3} + \int \frac{dx}{x-2}$$

$$I = \int \frac{dx}{x+3} + \int \frac{dx}{x-2} + \int \frac{dx}{x-2} = x - \log|x+3| + \log|x-2| + c$$

Hence,

$$I = x - \log |x + 3| + \log |x - 2| + c$$

Indefinite Integrals Ex 19.30 Q4

Let
$$I = \int \frac{3 + 4x - x^2}{(x + 2)(x - 1)} dx$$

$$= \int -1 + \frac{5x + 1}{(x + 2)(x - 1)} dx$$

$$\Rightarrow I = -\int dx + \int \frac{5x + 1}{(x + 2)(x - 1)} dx ----(1)$$
Let $\frac{5x + 1}{(x + 2)(x - 1)} = \frac{A}{x + 2} + \frac{B}{x - 1}$

$$\Rightarrow 5x + 1 = A(x - 1) + B(x + 2)$$

$$\Rightarrow \qquad 5x+1=A\left(x-1\right)+B\left(x+2\right)$$

Put x = 1

$$\Rightarrow \qquad 6 = 3B \Rightarrow \qquad B = 2$$

Put
$$x = -2$$

$$\Rightarrow$$
 $-9 = -3A \Rightarrow A = 3$

$$I = -\int dx + 3\int \frac{dx}{x+2} + 2\int \frac{dx}{x-1}$$

$$I = -x + 3\log|x + 2| + 2\log|x - 1| + c$$

Indefinite Integrals Ex 19.30 Q5

Let
$$I = \int \frac{x^2 + 1}{x^2 - 1} dx$$

$$= \int 1 + \frac{2}{x^2 - 1} dx$$

$$= \int dx + \int \frac{2dx}{(x + 1)(x - 1)}$$

$$= \int dx + \int \frac{-1}{x + 1} + \frac{1}{x - 1} dx$$

$$= x - \log|x + 1| + \log|x - 1| + c$$

$$I = x + \log \left| \frac{x - 1}{x + 1} \right| + c$$

****** END ******