

Exercise 7B

$$(\cos \theta + \sin \theta) = 1$$

$$(\cos \theta + \sin \theta)^{2} + (\cos \theta - \sin \theta)^{2} = 2(\cos^{2} \theta + \sin^{2} \theta) = 2$$

$$\Rightarrow 1^{2} + (\cos \theta - \sin \theta)^{2} = 2$$

$$\Rightarrow (\cos \theta - \sin \theta)^{2} = 1$$

$$(\cos \theta - \sin \theta) = \pm 1$$

Question 11:

tanA = n tanB and sinA = m sinB

$$\Rightarrow \tan A = \frac{1}{n} \tan A \text{ and } \sin A = \frac{1}{m} \sin A$$

$$\Rightarrow \cot B = \frac{1}{\tan A} \text{ and } \cos e B = \frac{m}{\sin A}$$

$$\therefore \cos e c^2 B - \cot^2 B = 1$$

$$\Rightarrow \frac{m^2}{\sin^2 A} - \frac{n^2}{\tan^2 A} = 1$$

$$\Rightarrow \frac{m^2}{\sin^2 A} - \frac{n^2 \cos^2 A}{\sin^2 A} = 1 \Rightarrow \frac{m^2 - n^2 \cos^2 A}{\sin^2 A} = 1$$

$$\Rightarrow m^2 - n^2 \cos^2 A = \sin^2 A \Rightarrow m^2 - n^2 \cos^2 A = 1 - \cos^2 A$$

$$\Rightarrow m^2 - 1 = n^2 \cos^2 A - \cos^2 A$$

$$\Rightarrow m^2 - 1 = \cos^2 A \left(n^2 - 1\right)$$

$$\Rightarrow \cos^2 A = \frac{\left(m^2 - 1\right)}{\left(n^2 - 1\right)}$$

******* END *******