



Sets Ex 1.6 Q4(i)

i. Let  $x \in B$ . Then

$$\Rightarrow x \in B \cup A$$

$$\Rightarrow x \in A \cup B$$

$$\therefore B \subset (A \cup B)$$

Sets Ex 1.6 Q4(ii)

ii. Let  $x \in A \cap B$ . Then

$$\Rightarrow x \in A \text{ and } x \in B$$

$$\Rightarrow x \in B$$

$$\therefore (A \cap B) \subset B$$

Sets Ex 1.6 Q4(iii)

iii. Let  $x \in A \subset B$ . Then

$$\Rightarrow x \in B$$

Let and  $x \in A \cap B$

$$\Leftrightarrow x \in A \text{ and } x \in B$$

$$\Leftrightarrow x \in A \text{ and } x \in A \quad (\because A \subset B)$$

$$\therefore (A \cap B) = A$$

Sets Ex 1.6 Q5

(i)

In order to show that the following four statements are equivalent, we need to show that  $(1) \Rightarrow (2)$ ,  $(2) \Rightarrow (3)$ ,  $(3) \Rightarrow (4)$  and  $(4) \Rightarrow (1)$

We first show that  $(1) \Rightarrow (2)$

We assume that  $A \subset B$ , and use this to show that  $A - B = \emptyset$

Now  $A - B = \{x \in A : x \notin B\}$ . As  $A \subset B$ ,

$\therefore$  Each element of  $A$  is an element of  $B$ ,

$$\therefore A - B = \emptyset$$

Hence, we have proved that  $(1) \Rightarrow (2)$ .

(ii)

We now show that  $(2) \Rightarrow (3)$

So assume that  $A - B = \emptyset$

To show:  $A \cup B = B$

$$\because A - B = \emptyset$$

$\therefore$  Every element of  $A$  is an element of  $B$

[ $\because A - B = \emptyset$  only when there is some element in  $A$  which is not in  $B$ ]

So  $A \subset B$  and therefore  $A \cup B = B$

So  $(2) \Rightarrow (3)$  is true.

(iii)

We now show that  $(3) \Rightarrow (4)$

Assume that  $A \cup B = B$

To show:  $A \cap B = A$

$\because A \cup B = B$

$\therefore A \subset B$  and so  $A \cap B = A$

So  $(3) \Rightarrow (4)$  is true.

(iv)

Finally we show that  $(4) \Rightarrow (1)$ , which will prove the equivalence of the four statements.

So, assume that  $A \cap B = A$

To show:  $A \subset B$

$\because A \cap B = A$ , therefore  $A \subset B$ , and so  $(4) \Rightarrow (1)$  is true.

Hence,  $(1) \Leftrightarrow (2) \Leftrightarrow (3) \Leftrightarrow (4)$ .

\*\*\*\*\* END \*\*\*\*\*