

Quadratic Equations Ex 8.4 Q4

Answer:

We have been given that,

$$2x^2 + x - 4 = 0$$

Now divide throughout by 2. We get,

$$x^2 + \frac{1}{2}x - 2 = 0$$

Now take the constant term to the RHS and we get

$$x^2 + \frac{1}{2}x = 2$$

Now add square of half of co-efficient of 'x' on both the sides. We have,

$$x^{2} + \frac{1}{2}x + \left(\frac{1}{4}\right)^{2} = \left(\frac{1}{4}\right)^{2} + 2$$
$$x^{2} + \left(\frac{1}{4}\right)^{2} + 2\left(\frac{1}{4}\right)x = \frac{33}{16}$$
$$\left(x + \frac{1}{4}\right)^{2} = \frac{33}{16}$$

Since RHS is a positive number, therefore the roots of the equation exist. So, now take the square root on both the sides and we get

$$x + \frac{1}{4} = \pm \frac{\sqrt{33}}{4}$$
$$x = \frac{-1 \pm \sqrt{33}}{4}$$

Now, we have the values of 'x' as

$$x = \frac{-1 + \sqrt{33}}{4}$$

Also we have.

$$x = \frac{-1 - \sqrt{33}}{4}$$

Therefore the roots of the equation are
$$\boxed{\frac{\sqrt{33}-1}{4}}$$
 and $\boxed{\frac{-1-\sqrt{33}}{4}}$

Quadratic Equations Ex 8.4 Q5

Answer:

We have been given that,

$$2x^2 + x + 4 = 0$$

Now divide throughout by 2. We get,

$$x^2 + \frac{1}{2}x + 2 = 0$$

Now take the constant term to the RHS and we get

$$x^2 + \frac{1}{2}x = -2$$

Now add square of half of co-efficient of 'x' on both the sides. We have,

$$x^{2} + \frac{1}{2}x + \left(\frac{1}{4}\right)^{2} = \left(\frac{1}{4}\right)^{2} - 2$$
$$x^{2} + \left(\frac{1}{4}\right)^{2} + 2\left(\frac{1}{4}\right)x = \frac{-31}{16}$$
$$\left(x + \frac{1}{4}\right)^{2} - 31$$

Since RHS is a negative number, therefore the roots of the equation do not exist as the square of a number cannot be negative.

Therefore the roots of the equation do not exist.

Quadratic Equations Ex 8.4 Q6

Answer:

We have been given that,

$$4x^2 + 4\sqrt{3}x + 3 = 0$$

Now divide throughout by 4. We get,

$$x^2 + \sqrt{3}x + \frac{3}{4} = 0$$

Now take the constant term to the RHS and we get

$$x^2 + \sqrt{3}x = -\frac{3}{4}$$

Now add square of half of co-efficient of 'x' on both the sides. We have,

$$x^{2} + 2\left(\frac{\sqrt{3}}{2}\right)x + \left(\frac{\sqrt{3}}{2}\right)^{2} = \left(\frac{\sqrt{3}}{2}\right)^{2} - \frac{3}{4}$$
$$x^{2} + 2\left(\frac{\sqrt{3}}{2}\right)x + \left(\frac{\sqrt{3}}{2}\right)^{2} = 0$$
$$\left(x + \frac{\sqrt{3}}{2}\right)^{2} = 0$$

Since RHS is a positive number, therefore the roots of the equation exist. So, now take the square root on both the sides and we get

$$x + \frac{\sqrt{3}}{2} = 0$$
$$x = -\frac{\sqrt{3}}{2}$$

Now, we have the values of 'x' as

$$x = -\frac{\sqrt{3}}{2}$$

Also we have,

$$x = -\frac{\sqrt{3}}{2}$$

Therefore the roots of the equation are $\left[-\frac{\sqrt{3}}{2}\right]$ and $\left[-\frac{\sqrt{3}}{2}\right]$