



**Q4. Simplify:**

**(i)**  $(a^2 - b^2)^2$

**(ii)**  $(2x+5)^2 - (2x-5)^2$

**(iii)**  $(7m-8n)^2 + (7m+8n)^2$

**(iv)**  $(4m+5n)^2 + (5m+4n)^2$

**(v)**  $(2.5p-1.5q)^2 - (1.5p-2.5q)^2$

**(vi)**  $(ab+bc)^2 - 2ab^2c$

**(vii)**  $(m^2 - n^2m)^2 + 2m^3n^2$

**Ans: (i)**  $(a^2 - b^2)^2$

$$= (a^2)^2 - 2 \times a^2 \times b^2 + (b^2)^2$$

[Using identity  $(a-b)^2 = a^2 - 2ab + b^2$ ]

$$= a^4 - 2a^2b^2 + b^4$$

**(ii)**  $(2x+5)^2 - (2x-5)^2$

$$= (2x)^2 + 2 \times 2x \times 5 + (5)^2 - [(2x)^2 - 2 \times 2x \times 5 + (5)^2]$$

[Using identities  $(a+b)^2 = a^2 + 2ab + b^2$  and

$(a-b)^2 = a^2 - 2ab + b^2$ ]

$$= 4x^2 + 20x + 25 - [4x^2 - 20x + 25]$$

$$= 4x^2 + 20x + 25 - 4x^2 + 20x - 25$$

$$= 40x$$

$$\textbf{(iii)} \quad (7m - 8n)^2 + (7m + 8n)^2$$

$$= (7m)^2 - 2 \times 7m \times 8n + (8n)^2$$

$$+ [(7m)^2 + 2 \times 7m \times 8n + (8n)^2]$$

$$\text{[Using identities } (a+b)^2 = a^2 + 2ab + b^2 \text{ and}$$

$$(a-b)^2 = a^2 - 2ab + b^2 \text{ ]}$$

$$= 49m^2 - 112mn + 64n^2 + [49m^2 + 112mn + 64n^2]$$

$$= 49m^2 - 112mn + 64n^2 + 49m^2 + 112mn + 64n^2$$

$$= 98m^2 + 128n^2$$

$$\textbf{(iv)} \quad (4m + 5n)^2 + (5m + 4n)^2$$

$$= (4m)^2 + 2 \times 4m \times 5n + (5n)^2 + (5m)^2 + 2 \times 5m \times 4n + (4n)^2$$

$$= (4m)^2 + 2 \times 4m \times 5n + (5n)^2 + (5m)^2 + 2 \times 5m \times 4n + (4n)^2$$

$$[\text{Using identity } (a+b)^2 = a^2 + 2ab + b^2]$$

$$= 16m^2 + 40mn + 25n^2 + 25m^2 + 40mn + 16n^2$$

$$= 16m^2 + 25m^2 + 40mn + 40mn + 25n^2 + 16n^2$$

$$= 41m^2 + 80mn + 41n^2$$

$$\text{(v)} \quad (2.5p - 1.5q)^2 - (1.5p - 2.5q)^2$$

$$= (2.5p)^2 - 2 \times 2.5p \times 1.5q + (1.5q)^2 - [(1.5p)^2 - 2 \times 1.5p \times 2.5q + (2.5q)^2]$$

$$[\text{Using identity } (a-b)^2 = a^2 - 2ab + b^2]$$

$$= 6.25p^2 - 7.50pq + 2.25q^2 - [2.25p^2 - 7.50pq + 6.25q^2]$$

$$= 6.25p^2 - 7.50pq + 2.25q^2 - 2.25p^2 + 7.50pq - 6.25q^2$$

$$= 4p^2 - 4q^2$$

$$\text{(vi)}$$

$$(ab + bc)^2 - 2ab^2c = (ab)^2 + 2 \times ab \times bc + (bc)^2 - 2ab^2c$$

$$[\text{Using identity } (a+b)^2 = a^2 + 2ab + b^2]$$

$$= a^2b^2 + 2ab^2c + b^2c^2 - 2ab^2c$$

$$= a^2b^2 + b^2c^2$$

$$\text{(vii)} \quad (m^2 - n^2m)^2 + 2m^3n^2$$

$$= (m^2)^2 - 2 \times m^2 \times n^2 m + (n^2 m)^2 + 2m^3 n^2$$

$$[\text{Using identity } (a-b)^2 = a^2 - 2ab + b^2]$$

$$= m^4 - 2m^3 n^2 + n^4 m^2 + 2m^3 n^2$$

$$= m^4 + n^4 m^2$$

**Q5.** Show that:

$$\text{(i)} \quad (3x+7)^2 - 84x = (3x-7)^2$$

$$\text{(ii)} \quad (9p-5q)^2 + 180pq = (9p+5q)^2$$

$$\text{(iii)} \quad \left(\frac{4}{3}m - \frac{3}{4}n\right)^2 + 2mn = \frac{16}{9}m^2 + \frac{9}{16}n^2$$

$$\text{(iv)} \quad (4pq+3q)^2 - (4pq-3q)^2 = 48pq^2$$

$$\text{(v)} \quad (a-b)(a+b) + (b-c)(b+c) + (c-a)(c+a) = 0$$

$$\text{Ans: (i) L.H.S.} = (3x+7)^2 - 84x$$

$$= (3x)^2 + 2 \times 3x \times 7 + (7)^2 - 84x$$

$$[\text{Using identity } (a+b)^2 = a^2 + 2ab + b^2]$$

$$= 9x^2 + 42x + 49 - 84x$$

$$= 9x^2 - 42x + 49$$

$$= (3x-7)^2 [\because (a-b)^2 = a^2 - 2ab + b^2]$$

$$= \text{R.H.S.}$$

$$\text{(ii) L.H.S.} = (9p - 5q)^2 + 180pq$$

$$= (9p)^2 - 2 \times 9p \times 5q + (5q)^2 + 180pq$$

$$[\text{Using identity } (a - b)^2 = a^2 - 2ab + b^2]$$

$$= 81p^2 - 90pq + 25q^2 + 180pq$$

$$= 81p^2 + 90pq + 25q^2$$

$$= (9p + 5q)^2 [\because (a + b)^2 = a^2 + 2ab + b^2]$$

$$\text{(iii) L.H.S.} = \left(\frac{4}{3}m - \frac{3}{4}n\right)^2 + 2mn$$

$$= \left(\frac{4}{3}m\right)^2 - 2 \times \frac{4}{3}m \times \frac{3}{4}n + \left(\frac{3}{4}n\right)^2 + 2mn$$

$$[\text{Using identity } (a - b)^2 = a^2 - 2ab + b^2]$$

$$= \frac{16}{9}m^2 - 2mn + \frac{9}{16}n^2 + 2mn$$

$$= \frac{16}{9}m^2 + \frac{9}{16}n^2$$

$$= \text{R.H.S.}$$

$$\text{(iv) L.H.S.} = (4pq + 3q)^2 - (4pq - 3q)^2$$

$$= (4pq)^2 + 2 \times 4pq \times 3q + (3q)^2 - [(4pq)^2 - 2 \times 4pq \times 3q + (3q)^2]$$

$$[\text{Using identities } (a + b)^2 = a^2 + 2ab + b^2 \text{ and}$$

$$(a - b)^2 = a^2 - 2ab + b^2]$$

$$= 16p^2q^2 + 24pq^2 + 9q^2 - [16p^2q^2 - 24pq^2 + 9q^2]$$

$$= 16p^2q^2 + 24pq^2 + 9q^2 - 16p^2q^2 + 24pq^2 - 9q^2$$

$$= 48pq^2$$

$$= \text{R.H.S.}$$

$$\text{(v) L.H.S.} =$$

$$(a - b)(a + b) + (b - c)(b + c) + (c - a)(c + a)$$

$$= a^2 - b^2 + b^2 - c^2 + c^2 - a^2$$

$$[\text{Using identity } (a - b)(a + b) = a^2 - b^2]$$

$$= 0$$

$$= \text{R.H.S.}$$

**Q6.** Using identities, evaluate:

**(i)**  $71^2$

**(ii)**  $99^2$

**(iii)**  $102^2$

**(iv)**  $998^2$

**(v)**  $5.2^2$

**(vi)**  $297 \times 303$

**(vii)**  $78 \times 82$

**(viii)**  $8.9^2$

**(ix)**  $1.05 \times 9.5$

**Ans: (i)**  $71^2 = (70+1)^2$

$$= (70)^2 + 2 \times 70 \times 1 + (1)^2$$

[Using identity  $(a+b)^2 = a^2 + 2ab + b^2$ ]

$$= 4900 + 140 + 1 = 5041$$

**(ii)**  $99^2 = (100-1)^2$

$$= (100)^2 - 2 \times 100 \times 1 + (1)^2$$

$$[\text{Using identity } (a-b)^2 = a^2 - 2ab + b^2]$$

$$= 10000 - 200 + 1 = 9801$$

$$\text{(iii)} \quad 102^2 = (100+2)^2$$

$$= (100)^2 + 2 \times 100 \times 2 + (2)^2$$

$$[\text{Using identity } (a+b)^2 = a^2 + 2ab + b^2]$$

$$= 10000 + 400 + 4 = 10404$$

$$\text{(iv)} \quad 998^2 = (1000-2)^2$$

$$= (1000)^2 - 2 \times 1000 \times 2 + (2)^2$$

$$[\text{Using identity } (a-b)^2 = a^2 - 2ab + b^2]$$

$$= 1000000 - 4000 + 4 = 996004$$

$$\text{(v)} \quad 5.2^2 = (5+0.2)^2$$

$$= (5)^2 + 2 \times 5 \times 0.2 + (0.2)^2$$

$$[\text{Using identity } (a+b)^2 = a^2 + 2ab + b^2]$$

$$= 25 + 2.0 + 0.04 = 27.04$$

$$\text{(vi)} \quad 297 \times 303$$

$$= (300 - 3) \times (300 + 3)$$

$$= (300)^2 - (3)^2$$

$$[\text{Using identity } (a-b)(a+b) = a^2 - b^2]$$

$$= 90000 - 9 = 89991$$

$$\textbf{(vii)} \quad 78 \times 82 = (80 - 2) \times (80 + 2)$$

$$= (80)^2 - (2)^2$$

$$[\text{Using identity } (a-b)(a+b) = a^2 - b^2]$$

$$= 6400 - 4 = 6396$$

$$\textbf{(viii)} \quad 8.9^2 = (8 + 0.9)^2$$

$$= (8)^2 + 2 \times 8 \times 0.9 + (0.9)^2$$

$$[\text{Using identity } (a+b)^2 = a^2 + 2ab + b^2]$$

$$= 64 + 14.4 + 0.81 = 79.21$$

$$\textbf{(ix)} \quad 1.05 \times 9.5 = (10 + 0.5) \times (10 - 0.5)$$

$$= (10)^2 - (0.5)^2$$

$$[\text{Using identity } (a-b)(a+b) = a^2 - b^2]$$

$$= 100 - 0.25 = 99.75$$



**Q7.** Using  $a^2 - b^2 = (a + b)(a - b)$ , find

**(i)**  $51^2 - 49^2$

**(ii)**  $(1.02)^2 - (0.98)^2$

**(iii)**  $153^2 - 147^2$

**(iv)**  $12.1^2 - 7.9^2$

**Ans: (i)**  $51^2 - 49^2 = (51 + 49)(51 - 49)$

[Using identity  $(a - b)(a + b) = a^2 - b^2$ ]

$= 100 \times 2 = 200$

**(ii)**  $(1.02)^2 - (0.98)^2$

$= (1.02 + 0.98)(1.02 - 0.98)$

[Using identity  $(a - b)(a + b) = a^2 - b^2$ ]

$= 2.00 \times 0.04 = 0.08$

**(iii)**  $153^2 - 147^2 = (153 + 147)(153 - 147)$

[Using identity  $(a - b)(a + b) = a^2 - b^2$ ]

$= 300 \times 6 = 1800$

**(iv)**  $12.1^2 - 7.9^2 = (12.1 + 7.9)(12.1 - 7.9)$

[Using identity  $(a - b)(a + b) = a^2 - b^2$ ]

$= 20.0 \times 4.2 = 84.0 = 84$

**Q8.** Using  $(x+a)(x+b) = x^2 + (a+b)x + ab$ , find

**(i)**  $103 \times 104$

**(ii)**  $5.1 \times 5.2$

**(iii)**  $103 \times 98$

**(iv)**  $9.7 \times 9.8$

**Ans: (i)**  $103 \times 104 = (100 + 3) \times (100 + 4)$

$$= (100)^2 + (3+4) \times 100 + 3 \times 4$$

[Using identity  $(x+a)(x+b) = x^2 + (a+b)x + ab$ ]

$$= 10000 + 7 \times 100 + 12$$

$$= 10000 + 700 + 12 = 10712$$

**(ii)**  $5.1 \times 5.2 = (5 + 0.1) \times (5 + 0.2)$

$$= (5)^2 + (0.1+0.2) \times 5 + 0.1 \times 0.2$$

[Using identity  $(x+a)(x+b) = x^2 + (a+b)x + ab$ ]

$$= 25 + 0.3 \times 5 + 0.02$$

$$= 25 + 1.5 + 0.02 = 26.52$$

**(iii)**  $103 \times 98 = (100 + 3) \times (100 - 2)$

$$= (100)^2 + (3-2) \times 100 + 3 \times (-2)$$

[Using identity  $(x+a)(x+b) = x^2 + (a+b)x + ab$ ]

$$= 10000 + (3-2) \times 100 - 6$$

$$= 10000 + 100 - 6 = 10094$$

**(iv)**  $9.7 \times 9.8 = (10 - 0.3) \times (10 - 0.2)$

$$= (10)^2 + \{(-0.3) + (-0.2)\} \times 10 + (-0.3) \times (-0.2)$$

[Using identity  $(x+a)(x+b) = x^2 + (a+b)x + ab$ ]

$$= 100 + \{-0.3 - 0.2\} \times 10 + 0.06$$

$$= 100 - 0.5 \times 10 + 0.06$$

$$= 100 - 5 + 0.06 = 95.06$$

\*\*\*\*\* END \*\*\*\*\*

