

Complex Numbers Ex 13.3 Q1(i)

Let z = -5 + 12i

$$\Rightarrow |z| = \sqrt{(-5)^2 + 12^2}$$
$$= \sqrt{25 + 144}$$
$$= \sqrt{169}$$
$$= 13$$

$$\therefore \sqrt{-5 + 12i} = \pm \left\{ \sqrt{\frac{13 + (-5)}{2}} + i\sqrt{\frac{13 - (-5)}{2}} \right\}$$

$$= \pm \left\{ \sqrt{\frac{8}{2}} + i\sqrt{\frac{18}{2}} \right\}$$

$$= \pm \left\{ 2 + 3i \right\}$$

Complex Numbers Ex 13.3 Q1(ii)

$$let z = -7 - 24i$$

then
$$|z| = \sqrt{(-7)^2 + (-24)^2}$$

= $\sqrt{49 + 576}$
= $\sqrt{625}$
= 25

$$\therefore \sqrt{-7 - 24i} = \pm \left\{ \sqrt{\frac{25 - 7}{2}} - i\sqrt{\frac{25 + 7}{2}} \right\} \quad (\because y < 0)$$

$$= \pm \left\{ \sqrt{\frac{18}{2}} - i\sqrt{\frac{32}{2}} \right\}$$

$$= \pm \left\{ \sqrt{9} - i\sqrt{16} \right\}$$

$$= \pm \left\{ 3 - 4i \right\}$$

Complex Numbers Ex 13.3 Q1(iii)

$$let z = 1 - i$$

then
$$|z| = \sqrt{1^2 + (-1)^2}$$

= $\sqrt{1+1}$
= $\sqrt{2}$

$$\therefore \sqrt{1-i} = \pm \left(\sqrt{\frac{\sqrt{2}+1}{2}} - i \sqrt{\frac{\sqrt{2}-1}{2}} \right) \qquad (v \ y < 0)$$
$$= \pm \left(\sqrt{\frac{\sqrt{2}+1}{2}} - i \sqrt{\frac{\sqrt{2}-1}{2}} \right)$$