

```
Increasing and Decreasing Functions Ex 17.2 Q1(xvii)
```

We have

$$f(x) = 2x^3 - 24x + 7$$

$$f'(x) = 6x^2 - 24$$

Critical points

$$f'(x)=0$$

$$6x^2 - 24 = 0$$

$$6x^2 = 24$$

$$x^2 = 4$$

$$x = 2, -2$$

Clearly, f'(x) > 0 if x > 2 and x < -2

$$f'(x) < 0 \text{ if } -2 \le x \le 2$$

Thus, f(x) is increasing in  $(-\infty, -2) \cup (2, \infty)$ , decreasing in (-2, 2).

Increasing and Decreasing Functions Ex 17.2 Q1(xviii)

We have 
$$f(x) = \frac{3}{10}x^4 - \frac{4}{5}x^3 - 3x^2 + \frac{36}{5}x + 11$$

Now 
$$f'(x) = 0$$

$$\Rightarrow \frac{6}{5}(x-1)(x+2)(x-3)=0$$

$$\Rightarrow$$
 x = 1, - 2 or 3

The points x = 1, -2 and 3 divide the number line into four disjoint intervals namely,  $(-\infty, -2)$ , (-2, 1), (1, 3) and  $(3, \infty)$ .

Consider the interval  $(-\infty, -2)$ , i.e  $-\infty < x < -2$ 

In this case, we have x - 1< 0, x + 2 < 0 and x - 3 < 0  $\,$ 

$$f'(x) < 0$$
 when  $-\infty < x < -2$ 

Thus, the function f is strictly decreasing in  $\left(-\infty,-2\right)$ 

Consider the interval  $\left(-2,1\right)$ , i.e – 2 < x < 1

In this case, we have x-1<0, x+2>0 and x-3<0

$$\therefore$$
 f'(x) > 0 when - 2 < x < 1

Thus, the function f is strictly increasing in (-2,1)

Now, consider the interval (1,3), i.e 1 < x < 3

In this case, we have x - 1 > 0, x + 2 > 0 and x - 3 < 0

$$\therefore$$
 f(x) < 0 when 1 < x < 3

Thus, the function f is strictly decreasing in (1,3)

Finally consider the interval  $(3, \infty)$ , i.e  $3 < x < \infty$ 

In this case, we have x - 1 > 0, x + 2 > 0 and x - 3 > 0

$$f(x) > 0$$
 when  $x > 3$ 

Thus, the function f is strictly increasing in  $(3, \infty)$ 

Increasing and Decreasing Functions Ex 17.2 Q1(xix)

We have,

$$f\left(x\right) = x^4 - 4x$$

$$f'(x) = 4x^3 - 4$$

Critical points,

$$f'(x) = 0$$

$$\Rightarrow 4(x^3 - 1) = 0$$

$$\Rightarrow x = 1$$

$$\Rightarrow x = 1$$

Clearly, 
$$f'(x) > 0$$
 if  $x > 1$ 

$$f'(x) < 0 \text{ if } x < 1$$

Thus, f(x) increases in  $(1,\infty)$ , decreases in  $(-\infty,1)$ .

Increasing and Decreasing Functions Ex 17.2 Q1(xx)

$$f(x) = \frac{x^4}{4} + \frac{2}{3}x^3 - \frac{5}{2}x^2 - 6x + 7$$

$$f'(x) = x^3 + 2x^2 - 5x - 6$$

Critical points

$$f'(x) = 0$$

$$\Rightarrow x^3 + 2x^2 - 5x - 6 = 0$$

$$\Rightarrow \qquad \left(x+1\right)\left(x+3\right)\left(x-2\right)=0$$

$$\Rightarrow$$
  $x = -1, -3, 2$ 

Clearly, 
$$f'(x) > 0$$
 if  $-3 < x < -1$  and  $x > 2$ 

$$f'(x) < 0 \text{ if } x < -3 \text{ and } -1 < x < 2$$

Thus, f(x) increases in  $(-3,-1) \cup (2,\infty)$ , decreases in  $(-\infty,-3) \cup (-1,2)$ .

\*\*\*\*\*\*\* END \*\*\*\*\*\*\*