

Division of Algebraic Expressions Ex 8.5 Q2

Answer:

$$\begin{split} &\left(ii\right) \, \frac{3y^3 + 5y^2 + 5y + 2}{y - 2} \\ &= \frac{3y^2(y - 2) + 11y(y - 2) + 27(y - 2) + 56}{y - 2} \\ &= \frac{(y - 2)(3y^2 + 11y + 27) + 56}{y - 2} \\ &= \left(3y^2 + 11y + 27\right) + \frac{56}{y - 2} \end{split}$$

- : Remainder = 56
- \therefore (y-2) is not a factor of $3y^3 + 5y^2 + 5y + 2$.

$$\begin{pmatrix}
\text{iii} & \frac{4x^4 + ^2 + 15}{4x^2 - 5} \\
&= \frac{x^2(4x^2 - 5) + 3(4x^2 - 5) + 30}{4x^2 - 5} \\
&= \frac{(4x^2 - 5)(x^2 + 3) + 30}{4x^2 - 5} \\
&= (x^2 + 3) + \frac{30}{4x^2 - 5}$$

: Remainder = 30

Therefore, $(4x^2 - 5)$ is not a factor of $4x^4 + 7x^2 + 15$

$$\begin{array}{l} \text{(iv)} \quad \frac{3z^2 - 13z + 4}{4 - z} \\ = \frac{3z^2 - 12z - z + 4}{4 - z} \\ = \frac{3z(z - 4) - 1(z - 4)}{4 - z} \\ = \frac{(z - 4)(3z - 1)}{4 - z} \\ = \frac{(4 - z)(1 - 3z)}{4 - z} \\ = 1 - 3z \end{array}$$

: Remainder = 0

 \therefore (4-z) is a factor of $3z^2 - 13z + 4$.

$$\begin{split} \left(V\right) & \frac{10a^2 - 9a - 5}{2a - 3} \\ &= \frac{5a(2a - 3) + 3(2a - 3) + 4}{2a - 3} \\ &= \frac{(2a - 3)(5a + 3) + 4}{2a - 3} \\ &= (5a + 3) + \frac{4}{2a - 3} \end{split}$$

: Remainder = 4

 \therefore (2a-3) is not a factor of $10a^2 - 9a - 5$.

(vi)
$$\frac{8y^{2}-2y+1}{4y+1}$$

$$= \frac{2y(4y+1)-1(4y+1)+2}{4y+1}$$

$$= \frac{(4y+1)(2y-1)+2}{4y+1}$$

$$= (2y-1) + \frac{2}{4y+1}$$

 \therefore Remainder = 2

$$\therefore (4y+1) \text{ is not } a \text{ factor of } 8y^2 - 2y+1.$$

******* END ******