

## Combinations Ex 17.1 Q18

 $^{n}C_{4}$ ,  $^{n}C_{5}$ , and  $^{n}C_{6}$  are in A.P

$$C_5 - C_4 = C_6 - C_5$$

$$\frac{n!}{5!(n-5)!} - \frac{n!}{4!(n-4)!} = \frac{n!}{6!(n-6)!} - \frac{n!}{6!(n-5)!}$$

$$\Rightarrow \frac{n!}{4!(n-5)!} \left[ \frac{1}{5} - \frac{1}{n-4} \right] = \frac{n!}{5!(n-6)!} \left[ \frac{1}{6} - \frac{1}{n-5} \right]$$

$$\Rightarrow \qquad \frac{1}{n-5} \left[ \frac{n-4-5}{5(n-4)} \right] = \frac{1}{5} \left[ \frac{n-5-6}{6(n-5)} \right]$$

$$\Rightarrow \frac{n-9}{n-4} = \frac{n-11}{6}$$

$$\Rightarrow$$
 6n - 54 =  $n^2$  - 15n + 44

$$\Rightarrow n^2 - 21n + 98 = 0$$

$$n = 7.14$$

n is 7 or 14

Combinations Ex 17.1 Q19

We have 
$$\alpha = {m \choose 2} = \frac{m(m-1)}{2} {n \choose 2} = \frac{n!}{r!(n-r)!}$$

Now  ${n \choose 2} = \frac{\alpha (\alpha - 1)}{2}$ 

$$= \frac{\left(\frac{m(m-1)}{2}\right) \left(\frac{m(m-1)}{2} - 1\right)}{2}$$

$$= \frac{m(m-1)(m^2 - m - 2)}{2 \times 2 \times 2} = \frac{m(m-1)(m+1)(m-2)}{8}$$

$$= \frac{m(m-1)(m+1)(m-2)}{4 \times 2}$$

multiplying with 3, numerator and denominator to make 4:

Or 
$$= \frac{m(m+1)m(m-1)(m-2)}{4 \cdot 3 \cdot 2 \cdot 1}$$
$$= \frac{3(m+1)m(m-1)(m-2)}{4!}$$
$$= 3 \cdot {}^{m+1}C_4 \qquad \left( \cdot \cdot \cdot {}^{n}C_r = \frac{n!}{r!(n-r)!} \right)$$

Combinations Ex 17.1 Q20(i)

$${}^{n}C_{r} = \frac{n!}{r!(n-r)!}$$

$${}^{n}C_{r-1} = \frac{n!}{(r-1)!(n-r+1)!}$$

$$\frac{{}^{n}C_{r}}{{}^{n}C_{r-1}} = \frac{n!(r-1)!(n-r+1)!}{r!(n-r)!n!}$$

$$= \frac{(r-1)!(n-r+1) \times (n-r)!}{r_{2} \times (r-1)!(n-r)!}$$

$$= \frac{n-r+1}{r}$$

Hence Proved

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