



### Differentiation Ex 11.2 Q67

Given,  $y = e^x \cos x$

Differentiating with respect to  $x$ ,

$$\begin{aligned}
 \frac{dy}{dx} &= \frac{d}{dx} (e^x \cos x) \\
 &= e^x \frac{d}{dx} \cos x + \cos x \frac{d}{dx} e^x && \text{[Using product rule]} \\
 &= e^x (-\sin x) + e^x \cos x \\
 &= e^x (\cos x - \sin x) \\
 &= \sqrt{2}e^x \left( \frac{\cos x}{\sqrt{2}} - \frac{\sin x}{\sqrt{2}} \right) && \text{[Multiplying and dividing by } \sqrt{2}] \\
 &= \sqrt{2}e^x \left( \cos \frac{\pi}{4} \cos x - \sin \frac{\pi}{4} \sin x \right)
 \end{aligned}$$

$$\frac{dy}{dx} = \sqrt{2}e^x \cos \left( x + \frac{\pi}{4} \right).$$

### Differentiation Ex 11.2 Q68

Given,  $y = \frac{1}{2} \log \left( \frac{1 - \cos 2x}{1 + \cos 2x} \right)$

$$\Rightarrow y = \frac{1}{2} \log \left( \frac{2 \sin^2 x}{2 \cos^2 x} \right) \quad \left[ \begin{array}{l} \text{Since, } 1 - \cos 2x = 2 \sin^2 x, \\ 1 + \cos 2x = 2 \cos^2 x \end{array} \right]$$

$$\Rightarrow y = \frac{1}{2} \log (\tan^2 x)$$

$$\Rightarrow y = \frac{2}{2} \log \tan x \quad \left[ \text{Since, } \log a^b = b \log a \right]$$

$$\Rightarrow y = \log \tan x$$

Differentiate it with respect to  $x$ ,

$$\begin{aligned}
 \frac{dy}{dx} &= (\log \tan x) \\
 &= \frac{1}{\tan x} \times \frac{d}{dx} (\tan x) && \text{[Using chain rule]} \\
 &= \frac{\sec^2 x}{\tan x} \\
 &= \frac{1}{\cos^2 x \times \frac{\sin x}{\cos x}} \\
 &= \frac{1}{\sin x \cos x} \\
 &= \frac{2}{2 \sin x \cos x} \\
 &= \frac{2}{\sin 2x} && \left[ \text{Since, } \frac{1}{\sin x} = \operatorname{cosec} x \right]
 \end{aligned}$$

So,

$$\frac{dy}{dx} = 2 \operatorname{cosec} 2x.$$

### Differentiation Ex 11.2 Q69

Here,  $y = x \sin^{-1} x + \sqrt{1 - x^2}$

Differentiating with respect to  $x$ ,

$$\begin{aligned}\frac{dy}{dx} &= \frac{d}{dx} \left[ x \sin^{-1} x + \sqrt{1 - x^2} \right] \\ &= \frac{d}{dx} (x \sin^{-1} x) + \frac{d}{dx} (\sqrt{1 - x^2}) \\ &= \left[ x \frac{d}{dx} \sin^{-1} x + \sin^{-1} x \frac{d}{dx} (x) \right] + \frac{1}{2\sqrt{1 - x^2}} \frac{d}{dx} (1 - x^2)\end{aligned}$$

[Using product rule and chain rule]

$$\begin{aligned}&= \left[ \frac{x}{\sqrt{1 - x^2}} + \sin^{-1} x \right] - \frac{2x}{2\sqrt{1 - x^2}} \\ &= \frac{x}{\sqrt{1 - x^2}} + \sin^{-1} x - \frac{x}{\sqrt{1 - x^2}} \\ &= \sin^{-1} x\end{aligned}$$

So,

$$\frac{dy}{dx} = \sin^{-1} x.$$

Differentiation Ex 11.2 Q70

Here,  $y = \sqrt{x^2 + a^2}$

Differentiating with respect to  $x$ ,

$$\begin{aligned}\frac{dy}{dx} &= \frac{d}{dx} (\sqrt{x^2 + a^2}) \\ &= \frac{1}{2\sqrt{x^2 + a^2}} \frac{d}{dx} (x^2 + a^2) && \text{[Using chain rule]} \\ &= \frac{1}{2\sqrt{x^2 + a^2}} \times (2x) \\ &= \frac{x}{\sqrt{x^2 + a^2}}\end{aligned}$$

$$\frac{dy}{dx} = \frac{x}{y} \quad \left[ \text{Since } \sqrt{x^2 + a^2} = y \right]$$

$$\Rightarrow y \frac{dy}{dx} = x$$

$$\Rightarrow y \frac{dy}{dx} - x = 0.$$

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