

Indefinite Integrals Ex 19.9 Q30

Let $\log \sin x = t$

$$\Rightarrow \frac{1}{\sin x} \cdot \cos x \, dx = dt$$

$$\therefore \cot x \, dx = dt$$

$$\Rightarrow \int \cot x \log \sin x \, dx = \int t \, dt$$

$$= \frac{t^2}{2} + C$$

$$= \frac{1}{2} (\log \sin x)^2 + C$$

Indefinite Integrals Ex 19.9 Q31

Let
$$I = \int \sec x \cdot \log (\sec x + \tan x) dx - - - - (i)$$

Let
$$\log(\sec x + \tan x) = t$$
 then,
 $d[\log(\sec x + \tan x)] = dt$

$$\Rightarrow \sec x \, dx = dt \qquad \left[\because \frac{d}{dx} \left(\log \left(\sec x + \tan x \right) \right) = \sec x \right]$$

Putting $\log(\sec x + \tan x) = t$ and $\sec x dx = dt$ in equation (i), we get

$$I = \int t \, dt$$

$$= \frac{t^2}{2} + c$$

$$= \frac{1}{2} \left[\log \left(\sec x + \tan x \right) \right]^2 + c$$

$$I = \frac{1}{2} \left[\log \left(\sec x + \tan x \right) \right]^2 + c$$

Indefinite Integrals Ex 19.9 Q32

Let
$$I = \int \cos e c x \log (\cos e c x - \cot x) dx - - - - - (i)$$

Let
$$\log(\cos ecx - \cot x) = t$$
 then,
 $dx [\log(\cos ecx - \cot x)] = dt$

$$\Rightarrow \quad \csc x \, dx = dt \qquad \qquad \left[\because \qquad \frac{d}{dx} \left(\log \left(\csc x - \cot x \right) \right) = \csc x \right]$$

Putting $\log(\cos ec x - \cot x) = t$ and $\csc x dx = dt$ in equation (i), we get

$$I = \int t dt$$
$$= \frac{t^2}{2} + c$$

$$I = \frac{1}{2} \left[\log \left(\csc x - \cot x \right) \right]^2 + c$$

Indefinite Integrals Ex 19.9 Q33

Let
$$I = \int x^3 \cos x^4 dx - - - - - (i)$$

Let
$$x^4 = t$$
 then,
 $dx(x^4) = dt$

$$\Rightarrow$$
 $4x^3 dx = dx$

$$\Rightarrow 4x^3 dx = dt$$

$$\Rightarrow x^3 = \frac{dt}{4}$$

Putting $x^4 = t$ and $x^3 dx = \frac{dt}{4}$ in equation (i), we get

$$I = \int \cos t \frac{dt}{4}$$
$$= \frac{1}{4} \sin t + c$$

$$I = \frac{1}{4} \sin x^4 + c$$

Indefinite Integrals Ex 19.9 Q34

Let
$$I = \int x^3 \sin x^4 dx - - - - - (i)$$

Let
$$x^4 = t$$
 then, $d(x^4) = dt$

$$\Rightarrow$$
 $4x^3 dx = dt$

$$\Rightarrow 4x^3 dx = dt$$

$$\Rightarrow x^3 = \frac{dt}{4}$$

Putting
$$x^4 = t$$
 and $x^3 dx = \frac{dt}{4}$ in equation (i), we get

$$I = \int \sin t \frac{dt}{4}$$
$$= \frac{1}{4} \int \sin t \, dt$$
$$= -\frac{1}{4} \cos t + c$$
$$= -\frac{1}{4} \cos x^4 + c$$

$$I = -\frac{1}{4}\cos x^4 + c$$

********* END *******