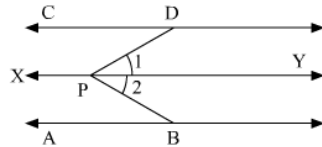




Lines and Angles Ex 8.4 Q11

Answer :

The given figure is:



It is given that $AB \parallel CD$

Let us draw a line XY passing through point P and parallel to AB and CD .

We have $XY \parallel CD$, thus, $\angle CDP$ and $\angle 1$ are alternate interior opposite angles. Therefore,

$$\angle 1 = \angle CDP \quad (i)$$

Similarly, we have $XY \parallel AB$, thus, $\angle ABP$ and $\angle 2$ are alternate interior opposite angles. Therefore,

$$\angle 2 = \angle ABP \quad (ii)$$

On adding (i) and (ii):

$$\angle 1 + \angle 2 = \angle CDP + \angle ABP$$

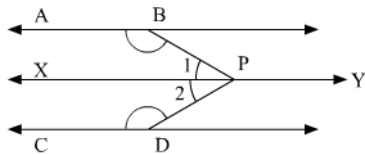
$$\boxed{\angle DPB = \angle CDP + \angle ABP}$$

Hence proved.

Lines and Angles Ex 8.4 Q12

Answer :

The given figure is as follows:



It is given that $AB \parallel CD$

Let us draw a line XY passing through point P and parallel to AB and CD .

We have $XY \parallel CD$, thus, $\angle CDP$ and $\angle 2$ are consecutive interior angles. Therefore,

$$\angle 2 + \angle CDP = 180^\circ \quad (i)$$

Similarly, we have $XY \parallel AB$, thus, $\angle ABP$ and $\angle 1$ are consecutive interior angles. Therefore,

$$\angle 1 + \angle ABP = 180^\circ \quad (ii)$$

On adding equation (i) and (ii), we get:

$$\angle 2 + \angle CDP + \angle 1 + \angle ABP = 180^\circ + 180^\circ$$

$$(\angle 2 + \angle 1) + \angle CDP + \angle ABP = 360^\circ$$

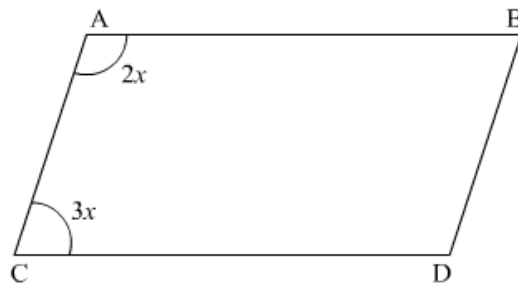
$$\boxed{\angle ABP + \angle BPD + \angle CDP = 360^\circ}$$

Hence proved.

Lines and Angles Ex 8.4 Q13

Answer :

The parallelogram can be drawn as follows:



It is given that

$$\angle A : \angle C = 2 : 3$$

Therefore, let:

$$\angle A = 2x$$

$$\text{and } \angle C = 3x$$

We know that opposite angles of a parallelogram are equal.

Therefore,

$$\angle A = \angle D$$

$$\angle D = 2x$$

Similarly

$$\angle B = 3x$$

Also, if $AB \parallel CD$, then sum of consecutive interior angles is equal to 180° .

Therefore,

$$\angle A + \angle C = 180^\circ$$

$$2x + 3x = 180^\circ$$

$$5x = 180^\circ$$

$$x = \frac{180^\circ}{5}$$

$$x = 36^\circ$$

We have

$$\angle A = 2x$$

$$\angle A = 2(36^\circ)$$

$$\angle A = \boxed{72^\circ}$$

Also,

$$\angle C = 3x$$

$$\angle C = 3(36^\circ)$$

$$\angle C = \boxed{108^\circ}$$

Similarly,

$$\angle D = \boxed{72^\circ}$$

And

$$\angle B = \boxed{108^\circ}$$

Hence, the four angles of the parallelogram are as follows:

$$\angle A = \boxed{72^\circ}, \angle B = \boxed{108^\circ}, \angle C = \boxed{72^\circ} \text{ and } \angle D = \boxed{108^\circ}.$$

***** END *****

