

Exercise 6

Question 1:

On substituting the value of various T-ratios, we get sin60° cos30° + cos60° sin30°

$$= \frac{\sqrt{3}}{2} \times \frac{\sqrt{3}}{2} + \frac{1}{2} \times \frac{1}{2} = \frac{3}{4} + \frac{1}{4} = \frac{4}{4} = 1$$

Question 2:

On substituting the value of various T-ratios, we get sin60° cos30° - cos60° sin30°

$$= \frac{1}{2} \times \frac{\sqrt{3}}{2} - \frac{\sqrt{3}}{2} \times \frac{1}{2}$$
$$= \frac{\sqrt{3}}{4} - \frac{\sqrt{3}}{4}$$
$$= 0$$

Question 3:

On substituting the value of various T-ratios, we get $\cos 45^{\circ} \cos 30^{\circ} + \sin 40^{\circ} \sin 30^{\circ}$

$$=\frac{1}{\sqrt{2}}\times\frac{\sqrt{3}}{2}+\frac{1}{\sqrt{2}}\times\frac{1}{2}=\frac{\sqrt{3}}{2\sqrt{2}}+\frac{1}{2\sqrt{2}}=\frac{\sqrt{3}+1}{2\sqrt{2}}$$

Question 4:

On substituting the value of various T-ratios, we get $2\cos^2 60^\circ + 3\sin^2 45^\circ - 3\sin^2 30^\circ + 2\cos^2 90^\circ$

$$= 2 \times \left(\frac{1}{2}\right)^2 + 3 \times \left(\frac{1}{\sqrt{2}}\right)^2 - 3 \times \left(\frac{1}{2}\right)^2 + 2\left(0\right)^2$$
$$= \frac{1}{2} + \frac{3}{2} - \frac{3}{4} \Rightarrow \frac{2+6-3}{4} = \frac{5}{4}$$

Question 5:

On substituting the value of various T-ratios, we get $\cot^2 30^\circ - 2\cos^2 30^\circ - \frac{3}{4} \sec^2 45^\circ + \frac{1}{4} \csc^2 30^\circ$

$$= \left(\sqrt{3}\right)^2 - 2 \times \left(\frac{\sqrt{3}}{2}\right)^2 - \frac{3}{4} \times \left(\frac{\sqrt{2}}{1}\right)^2 + \frac{1}{4} \times \left(2\right)^2$$

$$= 3 - 2 \times \frac{3}{4} - \frac{3}{4} \times 2 + \frac{1}{4} \times 4$$

$$= 3 - \frac{3}{2} - \frac{3}{2} + 1$$

$$= \frac{6 - 3 - 3 + 2}{2}$$

$$= \frac{2}{3} = 1$$

********* END *******