

Count numbers that don't contain 3

Given a number n , write a function that returns count of numbers from 1 to n that don't contain digit 3 in their decimal representation.

Examples:

Input: $n = 10$

Output: 9

Input: $n = 45$

Output: 31

// Numbers 3, 13, 23, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 43 contain digit 3.

Input: $n = 578$

Output: 385

Solution:

We can solve it recursively. Let $\text{count}(n)$ be the function that counts such numbers.

'msd' --> the most significant digit in n

'd' --> number of digits in n .

$\text{count}(n) = n$ if $n < 3$

$\text{count}(n) = n - 1$ if $3 \leq n < 10$

$\text{count}(n) = \text{count}(\text{msd}) * \text{count}(10^{(d-1)} - 1) +$
 $\text{count}(\text{msd}) +$
 $\text{count}(n \% (10^{(d-1)}))$
 if $n > 10$ and msd is not 3

$\text{count}(n) = \text{count}(\text{msd} * (10^{(d-1)} - 1))$
 if $n > 10$ and msd is 3

Let us understand the solution with $n = 578$.

$\text{count}(578) = 4 * \text{count}(99) + 4 + \text{count}(78)$

The middle term 4 is added to include numbers 100, 200, 400 and 500.

Let us take $n = 35$ as another example.

$\text{count}(35) = \text{count}(3 * 10 - 1) = \text{count}(29)$

```
#include <stdio.h>
```

```
/* returns count of numbers which are in range from 1 to
```

```
as a digit */
int count(int n)
{
    // Base cases (Assuming n is not negative)
    if (n < 3)
        return n;
    if (n >= 3 && n < 10)
        return n-1;

    // Calculate 10^(d-1) (10 raise to the power d-1) where d is
    // number of digits in n. po will be 100 for n = 578
    int po = 1;
    while (n/po > 9)
        po = po*10;

    // find the most significant digit (msd is 5 for 578)
    int msd = n/po;

    if (msd != 3)
        // For 578, total will be 4*count(10^2 - 1) + 4 + count(578)
        return count(msd)*count(po - 1) + count(msd) + count(n - msd*po);
    else
        // For 35, total will be equal to count(29)
        return count(msd*po - 1);
}

// Driver program to test above function
int main()
{
    printf ("%d ", count(578));
    return 0;
}
```

Output:

385