# Skew heap

From Wikipedia, the free encyclopedia Jump to: <u>navigation</u>, <u>search</u>

A **skew heap** (or **self-adjusting heap**) is a <u>heap data structure</u> implemented as a <u>binary tree</u>. Skew heaps are advantageous because of their ability to merge more quickly than binary heaps. In contrast with <u>binary heaps</u>, there are no structural constraints, so there is no guarantee that the height of the tree is logarithmic. Only two conditions must be satisfied:

- The general heap order must be enforced
- Every operation (add, remove min, merge) on two skew heaps must be done using a special skew heap merge.

A skew heap is a self-adjusting form of a <u>leftist heap</u> which attempts to maintain balance by unconditionally swapping all nodes in the merge path when merging two heaps. (The merge operation is also used when adding and removing values.)

With no structural constraints, it may seem that a skew heap would be horribly inefficient. However, <u>amortized complexity analysis</u> can be used to demonstrate that all operations on a skew heap can be done in O(log n).[1]

### **Contents**

- 1 Definition
- 2 Operations
  - 2.1 Merging two heaps
  - 2.2 Non-recursive merging
  - 2.3 Adding values
  - 2.4 Removing values
  - 2.5 Implementation
- 3 References
- 4 External links

# **Definition**[ edit ]

Skew heaps may be described with the following recursive definition:

- A heap with only one element is a skew heap.
- The result of *skew merging* two skew heaps and is also a skew heap.

# Operations [edit]

### Merging two heaps [edit]

When two skew heaps are to be merged, we can use a similar process as the merge of two leftist heaps:

- Compare roots of two heaps; let p be the heap with the smaller root, and q be the other heap. Let r be the name of the resulting new heap.
- Let the root of r be the root of p (the smaller root), and let r's right subtree be p's left subtree.
- Now, compute r's left subtree by recursively merging p's right subtree with q.

```
template < class T, class CompareFunction >
SkewNode < T >* CSkewHeap < T, CompareFunction >:: _Merge (SkewNode < T >* root_1, SkewNode < T >* root_2)
{
    SkewNode < T >* firstRoot = root_1;
    SkewNode < T >* secondRoot = root_2;

    if (firstRoot == NULL)
        return secondRoot;

    else if (secondRoot == NULL)
        return firstRoot;

    if (sh_compare -> Less (firstRoot -> key, secondRoot -> key))
{
        SkewNode < T >* tempHeap = firstRoot -> rightNode;
        firstRoot -> rightNode = firstRoot -> leftNode;
        firstRoot -> leftNode = _Merge (secondRoot, tempHeap);
        return firstRoot;
}
else
```

waturn Marga (gagandDoot firstD	200+).
<pre>return _Merge(secondRoot, firstR }</pre>	001);
SkewHeapMerge1.svg	
Before:	
SkewHeapMerge7.svg	
after	
Non-recursive merging[edit]	
Tron-recursive merging[ cuit ]	
Alternatively, there is a non-recursive approach which	h is more wordy, and does require some sorting at the outset.
<ul> <li>subtree.) This will result in a set of trees in whic</li> <li>Sort the subtrees in ascending order based on</li> <li>While there are still multiple subtrees, iteratively</li> </ul>	y recombine the last two (from right to left). has a left child, swap it to be the right child.
SkewHeapMerge1.svg	
SkewHeapMerge2.svg	
SkewHeapMerge3.svg	
SkewHeapMerge4.svg	







## Adding values [edit]

Adding a value to a skew heap is like merging a tree with one node together with the original tree.

## Removing values [edit]

Removing the first value in a heap can be accomplished by removing the root and merging its child subtrees.

#### **Implementation**[ **edit** ]

In many functional languages, skew heaps become extremely simple to implement. Here is a complete sample implementation in Haskell.

```
data SkewHeap a = Empty
                | Node a (SkewHeap a) (SkewHeap a)
singleton :: Ord a => a -> SkewHeap a
singleton x = Node x Empty Empty
union :: Ord a => SkewHeap a -> SkewHeap a -> SkewHeap a
                     `union` t2
Empty
       t.1
t1@ (Node x1 l1 r1) `union` t2@ (Node x2 l2 r2)
                                                  = Node x1 (t2 `union` r1) 11
= Node x2 (t1 `union` r2) 12
 | x1 <= x2
   otherwise
insert :: Ord a => a -> SkewHeap a -> SkewHeap a
insert x heap = singleton x `union` heap
extractMin :: Ord a => SkewHeap a -> Maybe (a, SkewHeap a)
extractMin Empty = Nothing
extractMin (Node x l r) = Just (x, l `union` r)
```

# References [ edit ]

- <u>Sleator</u>, Daniel Dominic; <u>Tarjan</u>, Robert Endre (1986). <u>"Self-Adjusting Heaps"</u>. <u>SIAM Journal on Computing</u> 15 (1): 52–69. doi:10.1137/0215004. <u>ISSN</u> 0097-5397.
- CSE 4101 lecture notes, York University
- 1. <u>http://www.cse.yorku.ca/~andy/courses/4101/lecture-notes/LN5.pdf</u>

# External links [ edit ]

- Animations comparing leftist heaps and skew heaps, York University
- Java applet for simulating heaps, Kansas State University

Retrieved from "<a href="https://en.wikipedia.org/w/index.php?title=Skew\_heap&oldid=638956230" Categories: Binary trees">https://en.wikipedia.org/w/index.php?title=Skew\_heap&oldid=638956230</a>"</a> Categories: Binary trees | Heaps (data structures)

# Navigation menu

#### Personal tools

- Create account
- Log in

## **Namespaces**

- Article
- Talk

#### **Variants**

#### **Views**

- Read
- Edit
- <u>View history</u>

#### More

## Search

Search	Search	Go

## **Navigation**

- Main page
- Contents
- Featured content
- Current events
- Random article
- Donate to Wikipedia
- Wikipedia store

#### Interaction

- Help
- About Wikipedia
- Community portal
- Recent changes
- Contact page

#### **Tools**

- What links here
- Related changes
- Upload file
- Special pages

- Permanent link
- Page information
- Wikidata item
- Cite this page

# Print/export

- Create a book
- Download as PDF
- Printable version

# Languages

- فارسى •
- Српски / srpski
- ไทย
- 中文

\_

## Edit links

- This page was last modified on 20 December 2014, at 21:11.
- Text is available under the <u>Creative Commons Attribution-ShareAlike License</u>; additional terms may apply. By using this site, you agree to the <u>Terms of Use</u> and <u>Privacy Policy</u>. Wikipedia® is a registered trademark of the <u>Wikimedia Foundation</u>, <u>Inc.</u>, a non-profit organization.
- Privacy policy
- About Wikipedia
- <u>Disclaimers</u>
- Contact Wikipedia
- <u>Developers</u>
- Mobile view

