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## Shortest common supersequence problem

From Wikipedia, the free encyclopedia (Redirected from Shortest common supersequence)

In computer science, the **shortest common supersequence problem** is a problem closely related to the longest common subsequence problem. Given two sequences  $\mathbf{X} = < x_1,...,x_m >$  and  $\mathbf{Y} = < y_1,...,y_n >$ , a sequence  $\mathbf{U} = < u_1,...,u_k >$  is a common supersequence of  $\mathbf{X}$  and  $\mathbf{Y}$  if  $\mathbf{U}$  is a supersequence of both  $\mathbf{X}$  and  $\mathbf{Y}$ . In other words, a shortest common supersequence of strings  $\mathbf{x}$  and  $\mathbf{y}$  is a shortest string  $\mathbf{z}$  such that both  $\mathbf{x}$  and  $\mathbf{y}$  are subsequences of  $\mathbf{z}$ .

A shortest common supersequence (scs) is a common supersequence of minimal length. In the shortest common supersequence problem, the two sequences **X** and **Y** are given and the task is to find a shortest possible common supersequence of these sequences. In general, an scs is not unique.

For two input sequences, an scs can be formed from a longest common subsequence (lcs) easily. For example, if  $\mathbf{X}[1..m] = abcbdab$  and  $\mathbf{Y}[1..n] = bdcaba$ , the lcs is  $\mathbf{Z}[1..r] = bcba$ . By inserting the non-lcs symbols while preserving the symbol order, we get the scs:  $\mathbf{U}[1..t] = abdcabdab$ .

It is quite clear that r+t=m+n for two input sequences. However, for three or more input sequences this does not hold. Note also, that the lcs and the scs problems are not dual problems.

For the more general problem of finding a string, **S** which is a superstring of a set of strings  $S_1, S_2, ..., S_l$ , the problem is NP-Complete .<sup>[1]</sup> Also, good approximations can be found for the average case but not for the worst case.<sup>[2][3]</sup>

## References [edit]

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## External links [edit]

Dictionary of Algorithms and Data Structures: shortest common supersequence 

Categories: Problems on strings | Combinatorics | Formal languages | Dynamic programming

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