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# Finger tree

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*For the binary search tree, see [finger search tree](#).*

A **finger tree** is a [purely functional data structure](#) used in efficiently implementing other functional data structures. A finger tree gives [amortized constant time](#) access to the "fingers" (leaves) of the tree, where data is stored, and also stores in each internal node the result of applying some [associative operation](#) to its descendants. This "summary" data stored in the internal nodes can be used to provide the functionality of data structures other than trees. For example, a [priority queue](#) can be implemented by labeling the internal nodes by the minimum priority of its children in the tree, or an indexed list/array can be implemented with a labeling of nodes by the count of the leaves in their children.

Finger trees can provide amortized  $O(1)$  pushing, reversing, popping,  $O(\log n)$  append and split; and can be adapted to be indexed or ordered sequences. And like all functional data structures, it is inherently [persistent](#); that is, older versions of the tree are always preserved.

They have since been used in the [Haskell](#) core libraries (in the implementation of *Data.Sequence*), and an implementation in [OCaml](#) exists<sup>[1]</sup> which was derived from a proven-correct [Coq](#) specification;<sup>[2]</sup> and a [C# implementation of finger trees](#)<sup>[3]</sup> was published in 2008; the [Yi text editor](#) specializes finger trees to finger strings for efficient storage of buffer text. Finger trees can be implemented with or without<sup>[3]</sup> [lazy evaluation](#), but laziness allows for simpler implementations.

They were first published in 1977 by [Leonidas J. Guibas](#),<sup>[4]</sup> and periodically refined since (e.g. a version using [AVL trees](#),<sup>[5]</sup> non-lazy finger trees, simpler 2-3 finger trees,<sup>[6]</sup> B-Trees and so on)

## See also

- [Monoid](#)

## References

- ↑ [Caml Weekly News](#)<sup>[?]</sup>
- ↑ [Matthieu Sozeau :: Dependent Finger Trees in Coq](#)<sup>[?]</sup>
- ↑ Kaplan, H.; [Tarjan, R. E.](#) (1995), "Persistent lists with catenation via recursive slow-down", *Proceedings of the Twenty-Seventh Annual ACM Symposium on the Theory of Computing*, pp. 93–102.
- ↑ [Guibas, L. J.](#); McCreight, E. M.; Plass, M. F.; Roberts, J. R. (1977), "A new representation for linear lists", *Conference Record of the Ninth Annual ACM Symposium on Theory of Computing*, pp. 49–60.
- ↑ [Tsakalidis, A. K.](#) (1985), "AVL-trees for localized search", *Information and Control* **67** (1-3): 173–194, doi:10.1016/S0019-9958(85)80034-6<sup>[?]</sup>.
- ↑ Hinze, Ralf; Paterson, Ross (2006), "Finger Trees: A Simple General-purpose Data Structure" <sup>[?]</sup> (PDF), *Journal of Functional Programming* **16** (2): 197–217, doi:10.1017/S0956796805005769<sup>[?]</sup>.

## External links

- <http://www.soi.city.ac.uk/~ross/papers/FingerTree.html><sup>[?]</sup>
- <http://hackage.haskell.org/packages/archive/EdisonCore/1.2.1.1/doc/html/Data-Edison-Concrete-FingerTree.html><sup>[?]</sup>
- [Example of 2-3 trees in C#](#)<sup>[?]</sup>
- [Example of Hinze/Paterson Finger Trees in Java](#)<sup>[?]</sup>
- [Example of Hinze/Paterson Finger Trees in C#](#)<sup>[?]</sup>
- ["Monoids and Finger Trees in Haskell"](#)<sup>[?]</sup>
- ["Finger tree library for Clojure"](#)<sup>[?]</sup>
- ["Finger tree in Scalaz"](#)<sup>[?]</sup>
- ["Verified Finger Trees in Isabelle/HOL"](#)<sup>[?]</sup>

v · t · e

**Tree data structures**

[hide]

**Search trees**  
(dynamic sets/associative arrays)

2–3 · 2–3–4 · AA · (a,b) · AVL · B · B+ · B\* · B<sup>x</sup> · (Optimal) Binary search · Dancing · HTree · Interval · Order statistic · (Left-leaning) Red-black · Scapegoat · Splay · T ·

	Treap · UB · Weight-balanced
<b>Heaps</b>	Binary · Binomial · Fibonacci · Leftist · Pairing · Skew · Van Emde Boas
<b>Tries</b>	Hash · Radix · Suffix · Ternary search · X-fast · Y-fast
<b>Spatial data partitioning trees</b>	BK · BSP · Cartesian · Hilbert R · <i>k</i> -d (implicit <i>k</i> -d) · M · Metric · MVP · Octree · Priority R · Quad · R · R+ · R* · Segment · VP · X
<b>Other trees</b>	Cover · Exponential · Fenwick · <b>Finger</b> · Fusion · Hash calendar · iDistance · K-ary · Left-child right-sibling · Link/cut · Log-structured merge · Mørkle · PQ · Range · SPQR · Top



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