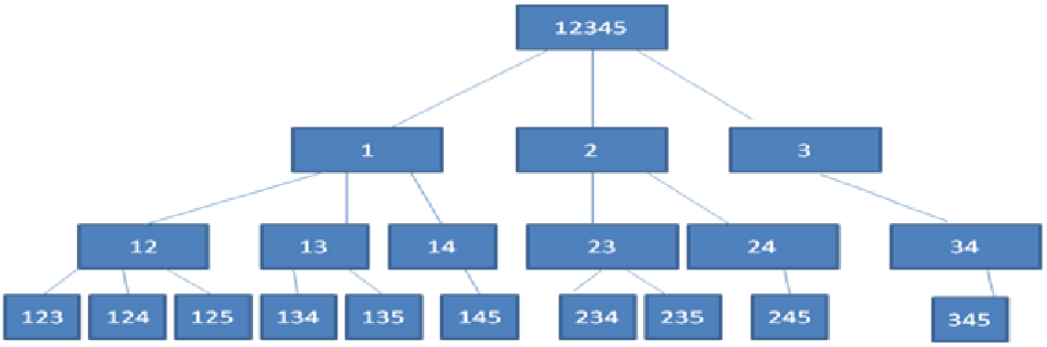
Print all possible combinations of r elements in a given array of size n

Given an array of size n, generate and print all possible combinations of r elements in array. For example, if input array is {1, 2, 3, 4} and r is 2, then output should be {1, 2}, {1, 3}, {1, 4}, {2, 3}, {2, 4} and {3, 4}.

Following are two methods to do this.

Method 1 (Fix Elements and Recur)
We create a temporary array 'data[]' which stores all outputs one by one. The idea is to start from first index (index = 0) in data[], one by one fix elements at this index and recur for remaining indexes. Let the input array be {1, 2, 3, 4, 5} and r be 3. We first fix 1 at index 0 in data[], then recur for remaining indexes, then we fix 2 at index 0 and recur. Finally, we fix 3 and recur for remaining indexes. When number of elements in data[] becomes equal to r (size of a combination), we print data[].

Following diagram shows recursion tree for same input.



Following is C++ implementation of above approach.

```
// Program to print all combination of size r in an arra
#include <stdio.h>
void combinationUtil(int arr[], int data[], int start, i

// The main function that prints all combinations of siz
// in arr[] of size n. This function mainly uses combina
void printCombination(int arr[], int n, int r)
{
    // A temporary array to store all combination one by
    int data[r];

    // Print all combination using temprary array 'data[
    combinationUtil(arr, data, 0, n-1, 0, r);
```

```
}

/* arr[]  ---> Input Array
   data[] ---> Temporary array to store current combinat
   start & end ---> Staring and Ending indexes in arr[]
   index  ---> Current index in data[]
   r ---> Size of a combination to be printed */
void combinationUtil(int arr[], int data[], int start, i
{
    // Current combination is ready to be printed, print
    if (index == r)
    {
        for (int j=0; j<r; j++)
            printf("%d ", data[j]);
        printf("\n");
        return;
    }

    // replace index with all possible elements. The con
    // "end-i+1 >= r-index" makes sure that including on
    // at index will make a combination with remaining e
    // at remaining positions
    for (int i=start; i<=end && end-i+1 >= r-index; i++)
    {
        data[index] = arr[i];
        combinationUtil(arr, data, i+1, end, index+1, r)
    }
}

// Driver program to test above functions
int main()
{
    int arr[] = {1, 2, 3, 4, 5};
    int r = 3;
    int n = sizeof(arr)/sizeof(arr[0]);
    printCombination(arr, n, r);
}
```

Output:

```
1 2 3
1 2 4
1 2 5
1 3 4
1 3 5
1 4 5
```

```
2 3 4
2 3 5
2 4 5
3 4 5
```

How to handle duplicates?

Note that the above method doesn't handle duplicates. For example, if input array is {1, 2, 1} and r is 2, then the program prints {1, 2} and {2, 1} as two different combinations. We can avoid duplicates by adding following two additional things to above code.

1) Add code to sort the array before calling combinationUtil() in printCombination()

2) Add following lines at the end of for loop in combinationUtil()

```
        // Since the elements are sorted, all occurrences of an element
        // must be together
        while (arr[i] == arr[i+1])
             i++;
```

See **this** for an implementation that handles duplicates.

Method 2 (Include and Exclude every element)

Like the above method, We create a temporary array data[]. The idea here is similar to Subset Sum Problem. We one by one consider every element of input array, and recur for two cases:

1) The element is included in current combination (We put the element in data[] and increment next available index in data[])

2) The element is excluded in current combination (We do not put the element and do not change index)

When number of elements in data[] become equal to r (size of a combination), we print it.

This method is mainly based on Pascal's Identity, i.e. $^{n}C_{r} = {}^{n-1}C_{r} + {}^{n-1}C_{r-1}$

Following is C++ implementation of method 2.

```
// Program to print all combination of size r in an arra
```

```
#include<stdio.h>
void combinationUtil(int arr[],int n,int r,int index,int
```

```
// The main function that prints all combinations of siz
// in arr[] of size n. This function mainly uses combina
void printCombination(int arr[], int n, int r)
{
    // A temporary array to store all combination one by
    int data[r];

    // Print all combination using temprary array 'data[
    combinationUtil(arr, n, r, 0, data, 0);
}

/* arr[]  ---> Input Array
   n      ---> Size of input array
   r      ---> Size of a combination to be printed
   index  ---> Current index in data[]
   data[] ---> Temporary array to store current combinat
   i      ---> index of current element in arr[]     */
void combinationUtil(int arr[], int n, int r, int index,
{
    // Current cobination is ready, print it
    if (index == r)
    {
        for (int j=0; j<r; j++)
            printf("%d ",data[j]);
        printf("\n");
        return;
    }

    // When no more elements are there to put in data[]
    if (i >= n)
        return;

    // current is included, put next at next location
    data[index] = arr[i];
    combinationUtil(arr, n, r, index+1, data, i+1);

    // current is excluded, replace it with next (Note t
    // i+1 is passed, but index is not changed)
    combinationUtil(arr, n, r, index, data, i+1);
}
```

```
// Driver program to test above functions
int main()
{
    int arr[] = {1, 2, 3, 4, 5};
    int r = 3;
```

```
    int n = sizeof(arr)/sizeof(arr[0]);
    printCombination(arr, n, r);
    return 0;
}
```

Output:

```
1 2 3
1 2 4
1 2 5
1 3 4
1 3 5
1 4 5
2 3 4
2 3 5
2 4 5
3 4 5
```

How to handle duplicates in method 2?

Like method 1, we can following two things to handle duplicates.

1) Add code to sort the array before calling combinationUtil() in printCombination()

2) Add following lines between two recursive calls of combinationUtil() in combinationUtil()

```
        // Since the elements are sorted, all occurrences of an element
        // must be together
        while (arr[i] == arr[i+1])
             i++;
```

See **this** for an implementation that handles duplicates.