

A suffix array is a sorted array of all suffixes of a given string. The definition is similar to Suffix Tree which is compressed trie of all suffixes of the given text.

Let the given string be "banana".

0 banana		5 a
1 anana	Sort the Suffixes	3 ana
2 nana	----->	1 anana
3 ana	alphabetically	0 banana
4 na		4 na
5 a		2 nana

The suffix array for "banana" is {5, 3, 1, 0, 4, 2}

We have discussed **Naive algorithm** for construction of suffix array. The Naive algorithm is to consider all suffixes, sort them using a $O(n \log n)$ sorting algorithm and while sorting, maintain original indexes. Time complexity of the Naive algorithm is $O(n^2 \log n)$ where n is the number of characters in the input string.

In this post, a **$O(n \log n)$ algorithm** for suffix array construction is discussed. Let us first discuss a $O(n * \log n * \log n)$ algorithm for simplicity. The idea is to use the fact that strings that are to be sorted are suffixes of a single string.

We first sort all suffixes according to first character, then according to first 2 characters, then first 4 characters and so on while the number of characters to be considered is smaller than $2n$. The important point is, if we have sorted suffixes according to first 2^i characters, then we can sort suffixes according to first 2^{i+1} characters in $O(n \log n)$ time using a $n \log n$ sorting algorithm like Merge Sort. This is possible as two suffixes can be compared in $O(1)$ time (we need to compare only two values, see the below example and code).

The sort function is called $O(\log n)$ times (Note that we increase number of characters to be considered in powers of 2). Therefore overall time complexity becomes $O(n \log n \log n)$. See <http://www.stanford.edu/class/cs97si/suffix-array.pdf> for more details.

Let us build suffix array the example string "banana" using above algorithm.

Sort according to first two characters Assign a rank to all suffixes using ASCII value of first character. A simple way to assign rank is to do "str[i] - 'a'" for i th suffix of strp[]

Index	Suffix	Rank
0	banana	1
1	anana	0
2	nana	13
3	ana	0
4	na	13
5	a	0

For every character, we also store rank of next adjacent character, i.e., the rank of character at str[i + 1] (This is needed to sort the suffixes according to first 2 characters). If a character is last character, we store next rank as -1

Index	Suffix	Rank	Next Rank
0	banana	1	0
1	anana	0	13
2	nana	13	0
3	ana	0	13

4	na	13	0
5	a	0	-1

Sort all Suffixes according to rank and adjacent rank. Rank is considered as first digit or MSD, and adjacent rank is considered as second digit.

Index	Suffix	Rank	Next Rank
5	a	0	-1
1	anana	0	13
3	ana	0	13
0	banana	1	0
2	nana	13	0
4	na	13	0

Sort according to first four character

Assign new ranks to all suffixes. To assign new ranks, we consider the sorted suffixes one by one. Assign 0 as new rank to first suffix. For assigning ranks to remaining suffixes, we consider rank pair of suffix just before the current suffix. If previous rank pair of a suffix is same as previous rank of suffix just before it, then assign it same rank. Otherwise assign rank of previous suffix plus one.

Index	Suffix	Rank	
5	a	0	[Assign 0 to first]
1	anana	1	(0, 13) is different from previous
3	ana	1	(0, 13) is same as previous
0	banana	2	(1, 0) is different from previous
2	nana	3	(13, 0) is different from previous
4	na	3	(13, 0) is same as previous

For every suffix `str[i]`, also store rank of next suffix at `str[i + 2]`. If there is no next suffix at `i + 2`, we store next rank as -1

Index	Suffix	Rank	Next Rank
5	a	0	-1
1	anana	1	1
3	ana	1	0
0	banana	2	3
2	nana	3	3
4	na	3	-1

Sort all Suffixes according to rank and next rank.

Index	Suffix	Rank	Next Rank
5	a	0	-1
3	ana	1	0
1	anana	1	1
0	banana	2	3
4	na	3	-1
2	nana	3	3

```
// C++ program for building suffix array of a given text
#include <iostream>
#include <cstring>
#include <algorithm>
using namespace std;
```

```

// Structure to store information of a suffix
struct suffix
{
    int index; // To store original index
    int rank[2]; // To store ranks and next rank pair
};

// A comparison function used by sort() to compare two suffixes
// Compares two pairs, returns 1 if first pair is smaller
int cmp(struct suffix a, struct suffix b)
{
    return (a.rank[0] == b.rank[0])? (a.rank[1] < b.rank[1] ?1: 0):
        (a.rank[0] < b.rank[0] ?1: 0);
}

// This is the main function that takes a string 'txt' of size n as an
// argument, builds and return the suffix array for the given string
int *buildSuffixArray(char *txt, int n)
{
    // A structure to store suffixes and their indexes
    struct suffix suffixes[n];

    // Store suffixes and their indexes in an array of structures.
    // The structure is needed to sort the suffixes alphabetically
    // and maintain their old indexes while sorting
    for (int i = 0; i < n; i++)
    {
        suffixes[i].index = i;
        suffixes[i].rank[0] = txt[i] - 'a';
        suffixes[i].rank[1] = ((i+1) < n)? (txt[i + 1] - 'a'): -1;
    }

    // Sort the suffixes using the comparison function
    // defined above.
    sort(suffixes, suffixes+n, cmp);

    // At this point, all suffixes are sorted according to first
    // 2 characters. Let us sort suffixes according to first 4
    // characters, then first 8 and so on
    int ind[n]; // This array is needed to get the index in suffixes[]
                // from original index. This mapping is needed to get
                // next suffix.
    for (int k = 4; k < 2*n; k = k*2)
    {
        // Assigning rank and index values to first suffix
        int rank = 0;
        int prev_rank = suffixes[0].rank[0];
        suffixes[0].rank[0] = rank;
        ind[suffixes[0].index] = 0;

        // Assigning rank to suffixes
        for (int i = 1; i < n; i++)
        {
            // If first rank and next ranks are same as that of previous
            // suffix in array, assign the same new rank to this suffix
            if (suffixes[i].rank[0] == prev_rank &&
                suffixes[i].rank[1] == suffixes[i-1].rank[1])
            {
                prev_rank = suffixes[i].rank[0];
                suffixes[i].rank[0] = rank;
            }
            else // Otherwise increment rank and assign
            {
                prev_rank = suffixes[i].rank[0];
                suffixes[i].rank[0] = ++rank;
            }
            ind[suffixes[i].index] = i;
        }

        // Assign next rank to every suffix
    }
}

```

```

    for (int i = 0; i < n; i++)
    {
        int nextindex = suffixes[i].index + k/2;
        suffixes[i].rank[1] = (nextindex < n)?
                               suffixes[ind[nextindex]].rank[0]: -1;
    }

    // Sort the suffixes according to first k characters
    sort(suffixes, suffixes+n, cmp);
}

// Store indexes of all sorted suffixes in the suffix array
int *suffixArr = new int[n];
for (int i = 0; i < n; i++)
    suffixArr[i] = suffixes[i].index;

// Return the suffix array
return suffixArr;
}

// A utility function to print an array of given size
void printArr(int arr[], int n)
{
    for (int i = 0; i < n; i++)
        cout << arr[i] << " ";
    cout << endl;
}

// Driver program to test above functions
int main()
{
    char txt[] = "banana";
    int n = strlen(txt);
    int *suffixArr = buildSuffixArray(txt, n);
    cout << "Following is suffix array for " << txt << endl;
    printArr(suffixArr, n);
    return 0;
}

```

Output:

```

Following is suffix array for banana
5 3 1 0 4 2

```

Note that the above algorithm uses standard sort function and therefore time complexity is $O(n \log n \log n)$. We can use Radix Sort here to reduce the time complexity to $O(n \log n)$.