

# Find the smallest number whose digits multiply to a given number n

Given a number 'n', find the smallest number 'p' such that if we multiply all digits of 'p', we get 'n'. The result 'p' should have minimum two digits.

Examples:

```
Input:  n = 36
```

```
Output: p = 49
```

```
// Note that 4*9 = 36 and 49 is the smallest such number
```

```
Input:  n = 100
```

```
Output: p = 455
```

```
// Note that 4*5*5 = 100 and 455 is the smallest such number
```

```
Input:  n = 1
```

```
Output: p = 11
```

```
// Note that 1*1 = 1
```

```
Input:  n = 13
```

```
Output: Not Possible
```

For a given n, following are the two cases to be considered.

**Case 1:  $n < 10$**  When n is smaller than n, the output is always n+10. For example for n = 7, output is 17. For n = 9, output is 19.

**Case 2:  $n \geq 10$**  Find all factors of n which are between 2 and 9 (both inclusive). The idea is to start searching from 9 so that the number of digits in result are minimized. For example 9 is preferred over 33 and 8 is preferred over 24.

Store all found factors in an array. The array would contain digits in non-increasing order, so finally print the array in reverse order.

Following is C implementation of above concept.

```
#include<stdio.h>
```

```
// Maximum number of digits in output
```

```
#define MAX 50
```

```
// prints the smallest number whose digits multiply to n
```

```
void findSmallest(int n)
```

```
{
```

```
    int i, j=0;
```

```
    int res[MAX]; // To store digits of result in reverse
```

```
    // Case 1: If number is smaller than 10
```

```
    if (n < 10)
```

```
    {
```

```
        printf("%d", n+10);
```

```
        return;
```

```
    }
```

```
    // Case 2: Start with 9 and try every possible digit
```

```
    for (i=9; i>1; i--)
```

```
    {
```

```
        // If current digit divides n, then store all
```

```
        // occurrences of current digit in res
```

```
        while (n%i == 0)
```

```
        {
```

```
            n = n/i;
```

```
            res[j] = i;
```

```
            j++;
```

```
        }
```

```
    }
```

```
    // If n could not be broken in form of digits (prime
```

```
    // are greater than 9)
```

```
    if (n > 10)
```

```
    {
```

```
        printf("Not possible");
```

```
        return;
```

```
    }
```

```
    // Print the result array in reverse order
```

```
    for (i=j-1; i>=0; i--)
```


```
        printf("%d", res[i]);
```

```
}
```

```
// Driver program to test above function
```

```
int main()
```

```
{  
    findSmallest(7);  
    printf("\n");  
  
    findSmallest(36);  
    printf("\n");  
  
    findSmallest(13);  
    printf("\n");  
  
    findSmallest(100);  
    return 0;  
}
```



Output:

```
17  
49  
Not possible  
455
```