

# ml(linear regression)

September 15, 2025

## 0.0.1 1. Reading and Understanding the Data

```
[1]: import warnings
warnings.filterwarnings('ignore')
```

Import the libraries

```
[3]: import numpy as np
import pandas as pd
import matplotlib as plt
from sklearn import linear_model
import matplotlib.pyplot as plt
import seaborn as sns
%matplotlib inline
```

Read and Understanding the Data

```
[10]: # Read the given CSV file, and view some sample records
df=pd.read_csv('day.csv')
df
```

```
[10]:
```

|     | instant | dteday     | season | yr | mnth | holiday | weekday | workingday | \ |
|-----|---------|------------|--------|----|------|---------|---------|------------|---|
| 0   | 1       | 01-01-2018 | 1      | 0  | 1    | 0       | 1       | 1          |   |
| 1   | 2       | 02-01-2018 | 1      | 0  | 1    | 0       | 2       | 1          |   |
| 2   | 3       | 03-01-2018 | 1      | 0  | 1    | 0       | 3       | 1          |   |
| 3   | 4       | 04-01-2018 | 1      | 0  | 1    | 0       | 4       | 1          |   |
| 4   | 5       | 05-01-2018 | 1      | 0  | 1    | 0       | 5       | 1          |   |
| ..  | ...     | ...        | ...    | .. | ...  | ...     | ...     |            |   |
| 725 | 726     | 27-12-2019 | 1      | 1  | 12   | 0       | 5       | 1          |   |
| 726 | 727     | 28-12-2019 | 1      | 1  | 12   | 0       | 6       | 0          |   |
| 727 | 728     | 29-12-2019 | 1      | 1  | 12   | 0       | 0       | 0          |   |
| 728 | 729     | 30-12-2019 | 1      | 1  | 12   | 0       | 1       | 1          |   |
| 729 | 730     | 31-12-2019 | 1      | 1  | 12   | 0       | 2       | 1          |   |

|   | weathersit | temp      | atemp    | hum     | windspeed | casual | registered | \ |
|---|------------|-----------|----------|---------|-----------|--------|------------|---|
| 0 | 2          | 14.110847 | 18.18125 | 80.5833 | 10.749882 | 331    | 654        |   |
| 1 | 2          | 14.902598 | 17.68695 | 69.6087 | 16.652113 | 131    | 670        |   |
| 2 | 1          | 8.050924  | 9.47025  | 43.7273 | 16.636703 | 120    | 1229       |   |
| 3 | 1          | 8.200000  | 10.60610 | 59.0435 | 10.739832 | 108    | 1454       |   |

|     |     |           |          |         |           |     |      |
|-----|-----|-----------|----------|---------|-----------|-----|------|
| 4   | 1   | 9.305237  | 11.46350 | 43.6957 | 12.522300 | 82  | 1518 |
| ..  | ... | ...       | ...      | ...     | ...       | ... | ...  |
| 725 | 2   | 10.420847 | 11.33210 | 65.2917 | 23.458911 | 247 | 1867 |
| 726 | 2   | 10.386653 | 12.75230 | 59.0000 | 10.416557 | 644 | 2451 |
| 727 | 2   | 10.386653 | 12.12000 | 75.2917 | 8.333661  | 159 | 1182 |
| 728 | 1   | 10.489153 | 11.58500 | 48.3333 | 23.500518 | 364 | 1432 |
| 729 | 2   | 8.849153  | 11.17435 | 57.7500 | 10.374682 | 439 | 2290 |

|     |      |
|-----|------|
|     | cnt  |
| 0   | 985  |
| 1   | 801  |
| 2   | 1349 |
| 3   | 1562 |
| 4   | 1600 |
| ..  | ...  |
| 725 | 2114 |
| 726 | 3095 |
| 727 | 1341 |
| 728 | 1796 |
| 729 | 2729 |

[730 rows x 16 columns]

```
[9]: df.columns
```

```
[9]: Index(['instant', 'dteday', 'season', 'yr', 'mnth', 'holiday', 'weekday',
         'workingday', 'weathersit', 'temp', 'atemp', 'hum', 'windspeed',
         'casual', 'registered', 'cnt'],
         dtype='object')
```

```
[11]: #Determining the number of rows and columns
df.shape
```

```
[11]: (730, 16)
```

```
[13]: #summary of all the numeric columns in the dataset
df.describe()
```

```
[13]:
```

|       | instant    | season     | yr         | mnth       | holiday    | weekday \  |
|-------|------------|------------|------------|------------|------------|------------|
| count | 730.000000 | 730.000000 | 730.000000 | 730.000000 | 730.000000 | 730.000000 |
| mean  | 365.500000 | 2.498630   | 0.500000   | 6.526027   | 0.028767   | 2.995890   |
| std   | 210.877136 | 1.110184   | 0.500343   | 3.450215   | 0.167266   | 2.000339   |
| min   | 1.000000   | 1.000000   | 0.000000   | 1.000000   | 0.000000   | 0.000000   |
| 25%   | 183.250000 | 2.000000   | 0.000000   | 4.000000   | 0.000000   | 1.000000   |
| 50%   | 365.500000 | 3.000000   | 0.500000   | 7.000000   | 0.000000   | 3.000000   |
| 75%   | 547.750000 | 3.000000   | 1.000000   | 10.000000  | 0.000000   | 5.000000   |
| max   | 730.000000 | 4.000000   | 1.000000   | 12.000000  | 1.000000   | 6.000000   |

|       | workingday | weathersit | temp       | atemp      | hum        | windspeed \ |
|-------|------------|------------|------------|------------|------------|-------------|
| count | 730.000000 | 730.000000 | 730.000000 | 730.000000 | 730.000000 | 730.000000  |
| mean  | 0.690411   | 1.394521   | 20.319259  | 23.726322  | 62.765175  | 12.763620   |
| std   | 0.462641   | 0.544807   | 7.506729   | 8.150308   | 14.237589  | 5.195841    |
| min   | 0.000000   | 1.000000   | 2.424346   | 3.953480   | 0.000000   | 1.500244    |
| 25%   | 0.000000   | 1.000000   | 13.811885  | 16.889713  | 52.000000  | 9.041650    |
| 50%   | 1.000000   | 1.000000   | 20.465826  | 24.368225  | 62.625000  | 12.125325   |
| 75%   | 1.000000   | 2.000000   | 26.880615  | 30.445775  | 72.989575  | 15.625589   |
| max   | 1.000000   | 3.000000   | 35.328347  | 42.044800  | 97.250000  | 34.000021   |

|       | casual      | registered  | cnt         |
|-------|-------------|-------------|-------------|
| count | 730.000000  | 730.000000  | 730.000000  |
| mean  | 849.249315  | 3658.757534 | 4508.006849 |
| std   | 686.479875  | 1559.758728 | 1936.011647 |
| min   | 2.000000    | 20.000000   | 22.000000   |
| 25%   | 316.250000  | 2502.250000 | 3169.750000 |
| 50%   | 717.000000  | 3664.500000 | 4548.500000 |
| 75%   | 1096.500000 | 4783.250000 | 5966.000000 |
| max   | 3410.000000 | 6946.000000 | 8714.000000 |

```
[15]: #Datatypes of each column
df.info()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 730 entries, 0 to 729
Data columns (total 16 columns):
#   Column          Non-Null Count  Dtype
---  -
0   instant         730 non-null    int64
1   dteday          730 non-null    object
2   season          730 non-null    int64
3   yr              730 non-null    int64
4   mnth            730 non-null    int64
5   holiday         730 non-null    int64
6   weekday         730 non-null    int64
7   workingday      730 non-null    int64
8   weathersit       730 non-null    int64
9   temp            730 non-null    float64
10  atemp           730 non-null    float64
11  hum             730 non-null    float64
12  windspeed       730 non-null    float64
13  casual          730 non-null    int64
14  registered       730 non-null    int64
15  cnt             730 non-null    int64
dtypes: float64(4), int64(11), object(1)
memory usage: 91.4+ KB
```

```
[17]: #Checking missing values
df.isnull().sum()
```

```
[17]: instant      0
      dteday      0
      season      0
      yr          0
      mnth        0
      holiday      0
      weekday      0
      workingday   0
      weathersit    0
      temp        0
      atemp       0
      hum         0
      windspeed    0
      casual      0
      registered   0
      cnt         0
      dtype: int64
```

## 1 2.Data Visualisation

```
[21]: df.drop(columns=['dteday'],inplace=True)
      df
```

```
[21]:
```

|     | instant | season | yr | mnth | holiday | weekday | workingday | weathersit | \ |
|-----|---------|--------|----|------|---------|---------|------------|------------|---|
| 0   | 1       | 1      | 0  | 1    | 0       | 1       | 1          | 2          |   |
| 1   | 2       | 1      | 0  | 1    | 0       | 2       | 1          | 2          |   |
| 2   | 3       | 1      | 0  | 1    | 0       | 3       | 1          | 1          |   |
| 3   | 4       | 1      | 0  | 1    | 0       | 4       | 1          | 1          |   |
| 4   | 5       | 1      | 0  | 1    | 0       | 5       | 1          | 1          |   |
| ..  | ...     | ...    | .. | ...  | ...     | ...     | ...        |            |   |
| 725 | 726     | 1      | 1  | 12   | 0       | 5       | 1          | 2          |   |
| 726 | 727     | 1      | 1  | 12   | 0       | 6       | 0          | 2          |   |
| 727 | 728     | 1      | 1  | 12   | 0       | 0       | 0          | 2          |   |
| 728 | 729     | 1      | 1  | 12   | 0       | 1       | 1          | 1          |   |
| 729 | 730     | 1      | 1  | 12   | 0       | 2       | 1          | 2          |   |

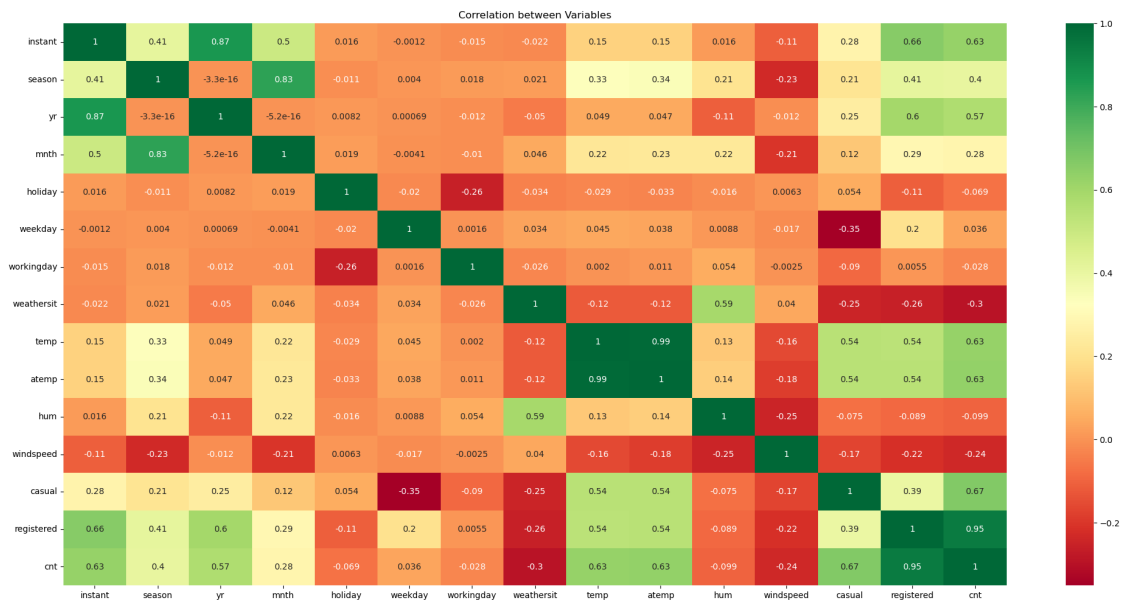
  

|     | temp      | atemp    | hum     | windspeed | casual | registered | cnt  |
|-----|-----------|----------|---------|-----------|--------|------------|------|
| 0   | 14.110847 | 18.18125 | 80.5833 | 10.749882 | 331    | 654        | 985  |
| 1   | 14.902598 | 17.68695 | 69.6087 | 16.652113 | 131    | 670        | 801  |
| 2   | 8.050924  | 9.47025  | 43.7273 | 16.636703 | 120    | 1229       | 1349 |
| 3   | 8.200000  | 10.60610 | 59.0435 | 10.739832 | 108    | 1454       | 1562 |
| 4   | 9.305237  | 11.46350 | 43.6957 | 12.522300 | 82     | 1518       | 1600 |
| ..  | ...       | ...      | ...     | ...       | ...    | ...        |      |
| 725 | 10.420847 | 11.33210 | 65.2917 | 23.458911 | 247    | 1867       | 2114 |

|     |           |          |         |           |     |      |      |
|-----|-----------|----------|---------|-----------|-----|------|------|
| 726 | 10.386653 | 12.75230 | 59.0000 | 10.416557 | 644 | 2451 | 3095 |
| 727 | 10.386653 | 12.12000 | 75.2917 | 8.333661  | 159 | 1182 | 1341 |
| 728 | 10.489153 | 11.58500 | 48.3333 | 23.500518 | 364 | 1432 | 1796 |
| 729 | 8.849153  | 11.17435 | 57.7500 | 10.374682 | 439 | 2290 | 2729 |

[730 rows x 15 columns]

```
[23]: plt.figure(figsize=(25, 12))
sns.heatmap(df.corr(), cmap='RdYlGn', annot = True)
plt.title("Correlation between Variables")
plt.show()
```



```
[25]: df['season']=df.season.map({1: 'spring', 2: 'summer',3:'fall', 4:'winter' })
df['mnth']=df.mnth.map({1: 'Jan',2:'Feb',3:'Mar',4:'Apr',5:'May',6:'June',7:
    ↪ 'July',8:'Aug',9:'Sep',10:'Oct',11:'Nov',12:'Dec'})
df['weathersit']=df.weathersit.map({1: 'Clear',2:'Mist + Cloudy',3:'Light
    ↪ Snow',4:'Snow + Fog'})
df['weekday']=df.weekday.map({0: 'Sun',1: 'Mon',2: 'Tue',3: 'Wed',4: 'Thu',5: 'Fri',6:
    ↪ 'Sat'})
df
```

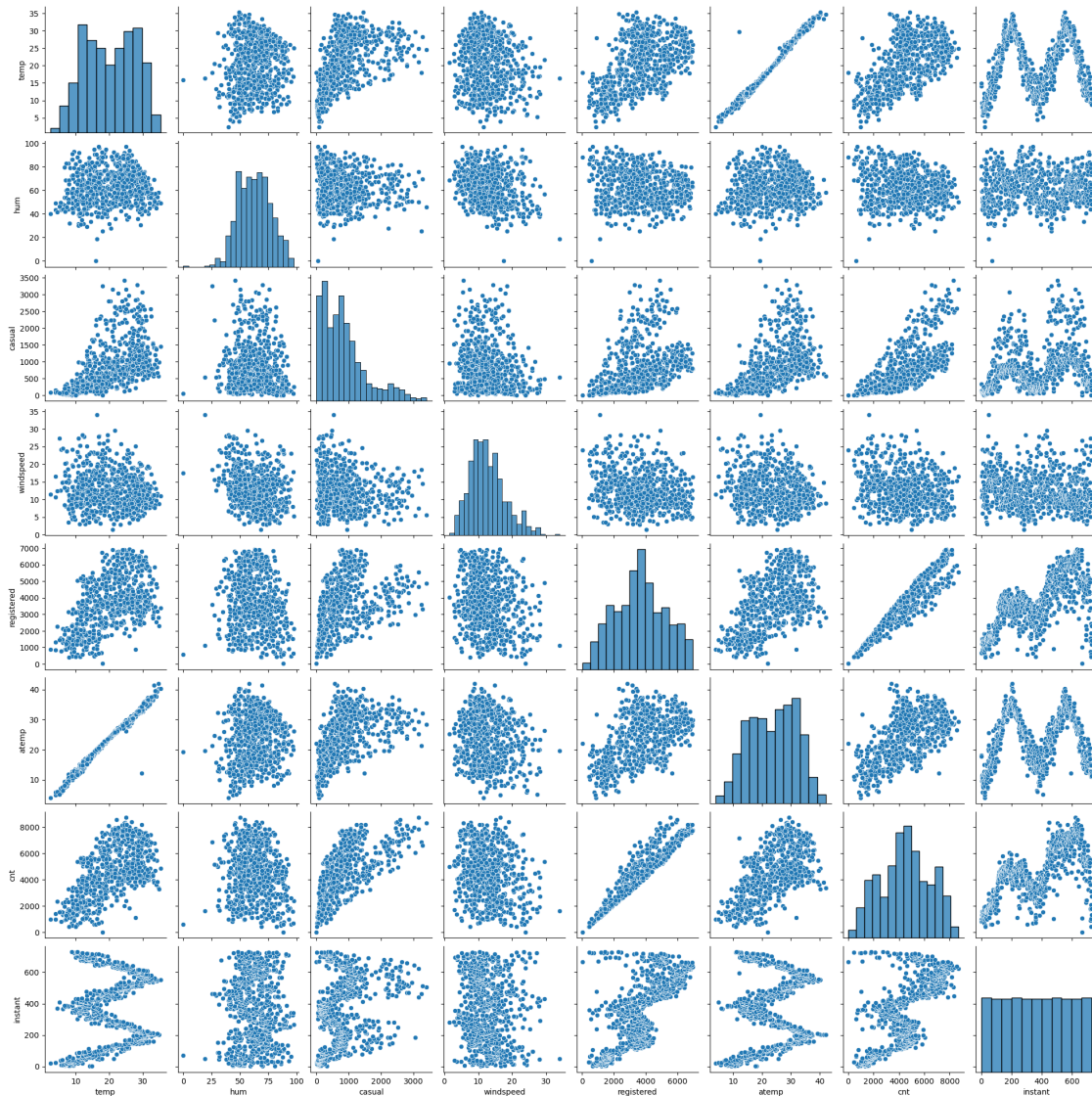
```
[25]:      instant  season  yr  mnth  holiday  weekday  workingday  weathersit  \
0          1   spring   0   Jan          0     Mon           1  Mist + Cloudy
1          2   spring   0   Jan          0     Tue           1  Mist + Cloudy
2          3   spring   0   Jan          0     Wed           1         Clear
3          4   spring   0   Jan          0     Thu           1         Clear
4          5   spring   0   Jan          0     Fri           1         Clear
```

|     |     |        |    |     |     |     |     |               |
|-----|-----|--------|----|-----|-----|-----|-----|---------------|
| ..  | ... | ...    | .. | ... | ... | ... | ... | ...           |
| 725 | 726 | spring | 1  | Dec | 0   | Fri | 1   | Mist + Cloudy |
| 726 | 727 | spring | 1  | Dec | 0   | Sat | 0   | Mist + Cloudy |
| 727 | 728 | spring | 1  | Dec | 0   | Sun | 0   | Mist + Cloudy |
| 728 | 729 | spring | 1  | Dec | 0   | Mon | 1   | Clear         |
| 729 | 730 | spring | 1  | Dec | 0   | Tue | 1   | Mist + Cloudy |

|     | temp      | atemp    | hum     | windspeed | casual | registered | cnt  |
|-----|-----------|----------|---------|-----------|--------|------------|------|
| 0   | 14.110847 | 18.18125 | 80.5833 | 10.749882 | 331    | 654        | 985  |
| 1   | 14.902598 | 17.68695 | 69.6087 | 16.652113 | 131    | 670        | 801  |
| 2   | 8.050924  | 9.47025  | 43.7273 | 16.636703 | 120    | 1229       | 1349 |
| 3   | 8.200000  | 10.60610 | 59.0435 | 10.739832 | 108    | 1454       | 1562 |
| 4   | 9.305237  | 11.46350 | 43.6957 | 12.522300 | 82     | 1518       | 1600 |
| ..  | ...       | ...      | ...     | ...       | ...    | ...        | ...  |
| 725 | 10.420847 | 11.33210 | 65.2917 | 23.458911 | 247    | 1867       | 2114 |
| 726 | 10.386653 | 12.75230 | 59.0000 | 10.416557 | 644    | 2451       | 3095 |
| 727 | 10.386653 | 12.12000 | 75.2917 | 8.333661  | 159    | 1182       | 1341 |
| 728 | 10.489153 | 11.58500 | 48.3333 | 23.500518 | 364    | 1432       | 1796 |
| 729 | 8.849153  | 11.17435 | 57.7500 | 10.374682 | 439    | 2290       | 2729 |

[730 rows x 15 columns]

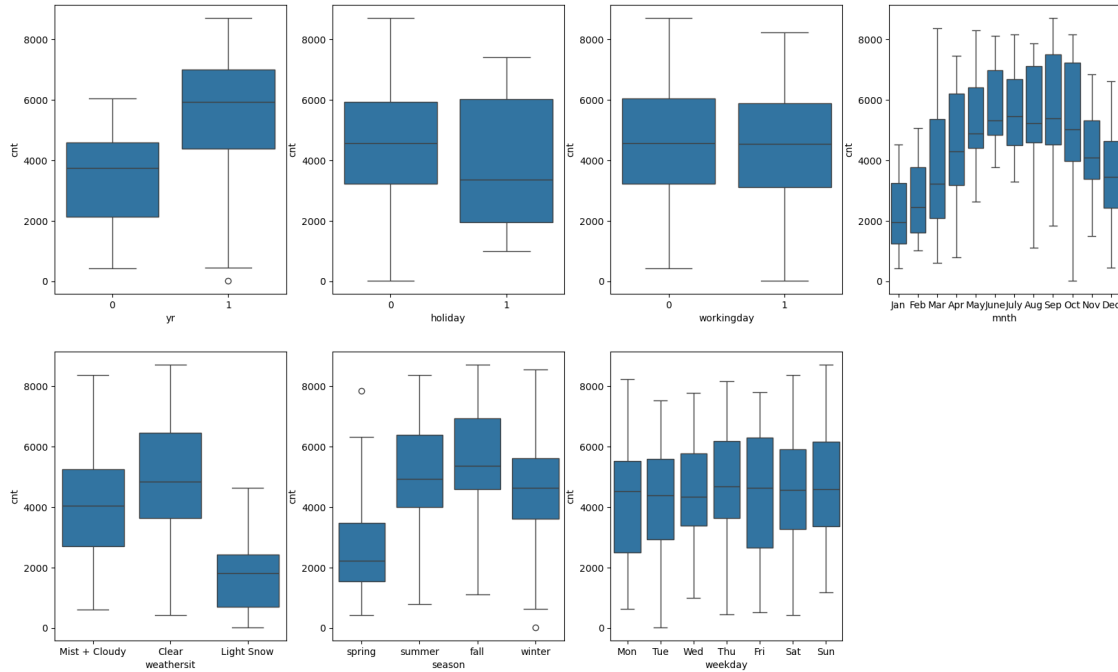
```
[27]: #Pairplot for numeric variables
sns.
    pairplot(df, vars=['temp', 'hum', 'casual', 'windspeed', 'registered', 'atemp', 'cnt', 'instant'])
plt.show()
```



[28]: *##Relationship between categorical and continuous variable*

```
plt.figure(figsize=(20, 12))
plt.subplot(2,4,1)
sns.boxplot(x = 'yr', y = 'cnt', data =df)
plt.subplot(2,4,2)
sns.boxplot(x = 'holiday', y = 'cnt', data = df)
plt.subplot(2,4,3)
sns.boxplot(x = 'workingday', y = 'cnt', data = df)
plt.subplot(2,4,4)
sns.boxplot(x = 'mnth', y = 'cnt', data = df)
plt.subplot(2,4,5)
sns.boxplot(x = 'weathersit', y = 'cnt', data = df)
plt.subplot(2,4,6)
```

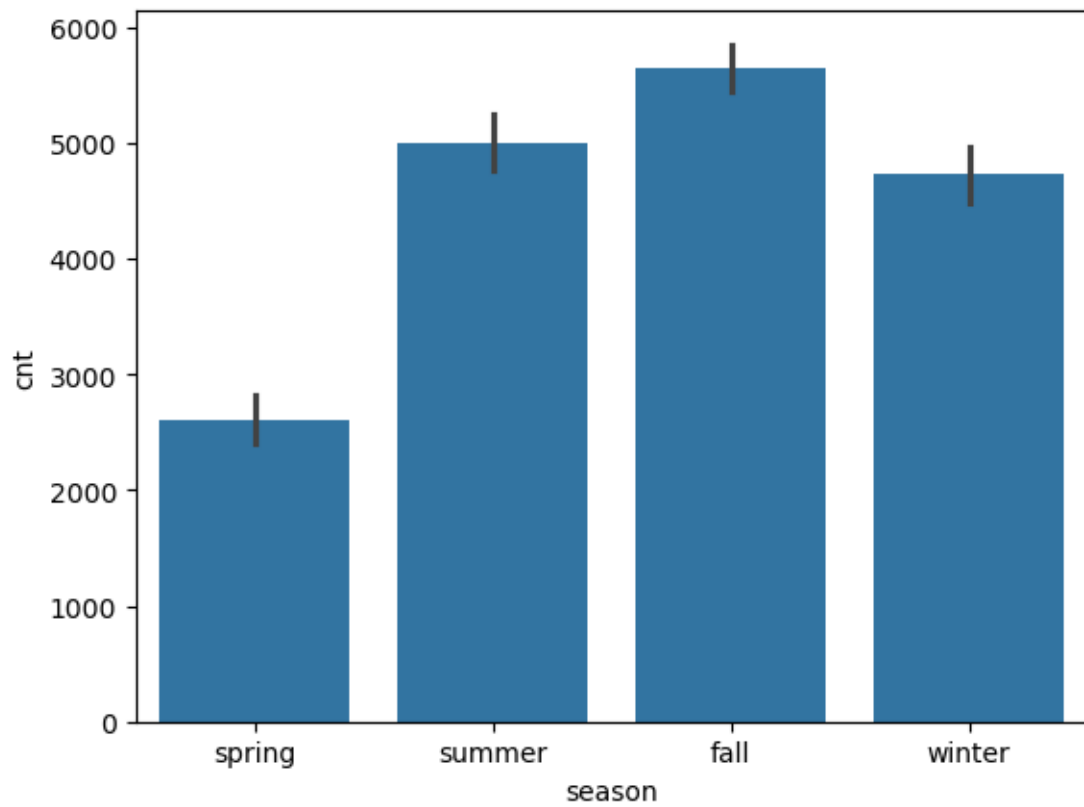
```
sns.boxplot(x = 'season', y = 'cnt', data = df)
plt.subplot(2,4,7)
sns.boxplot(x = 'weekday', y = 'cnt', data = df)
plt.show()
```



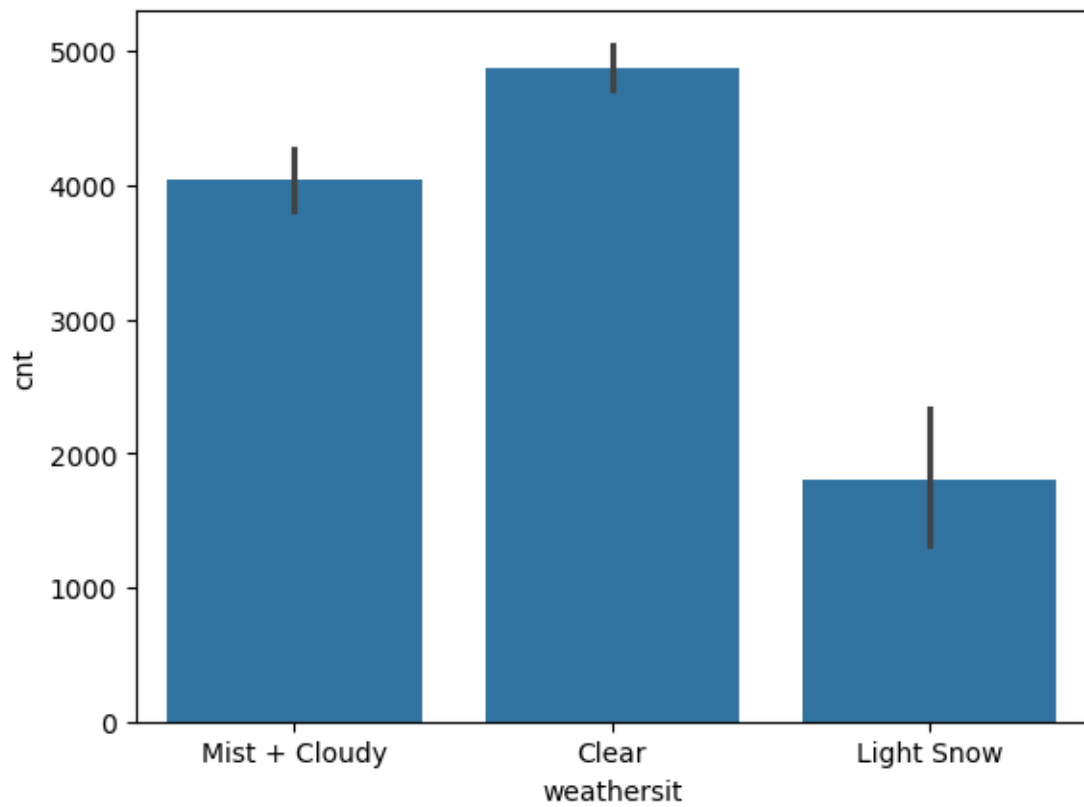
[29]: *#Barplot to see relation between season and count of bike rentals*  

```
sns.barplot(x='season',y='cnt',data=df)
plt.show()
```

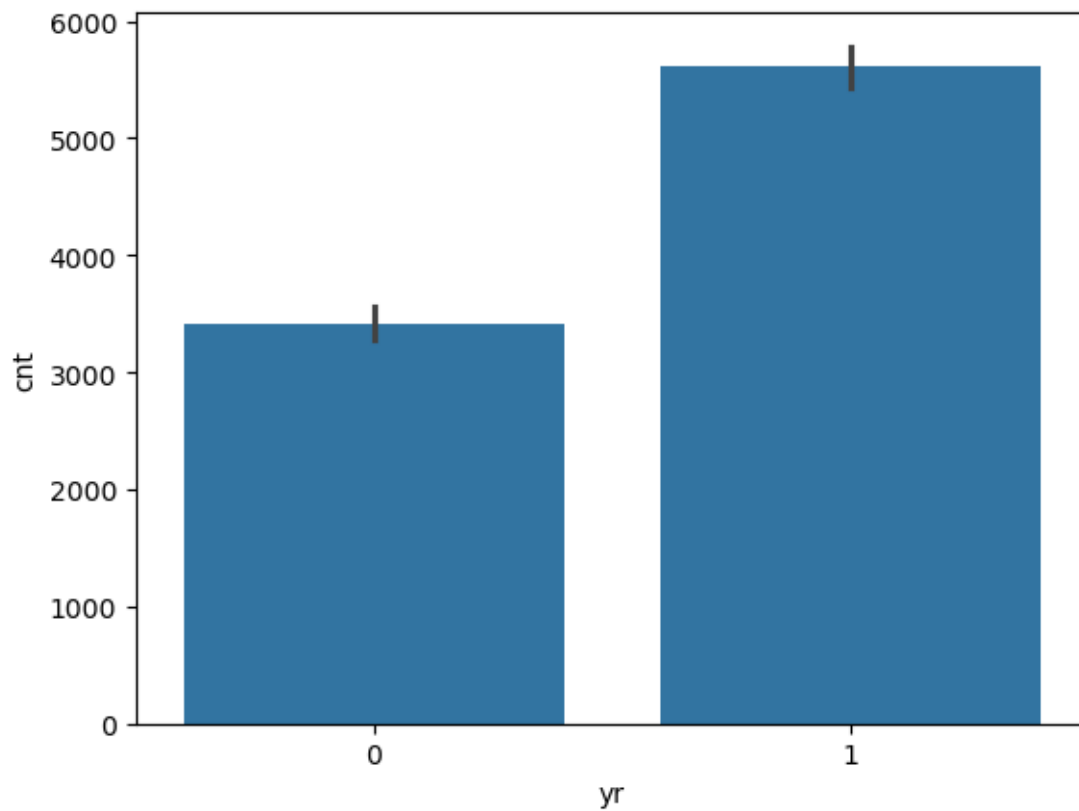




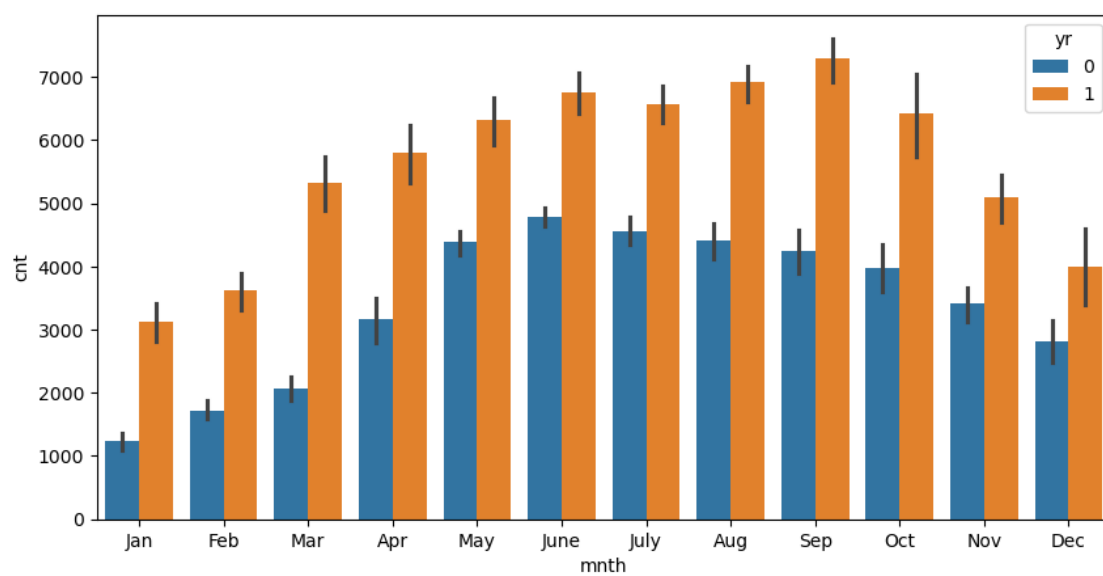
```
[33]: #Relation between weather and count of bike rentals
sns.barplot(x='weathersit',y='cnt',data=df)
plt.show()
```



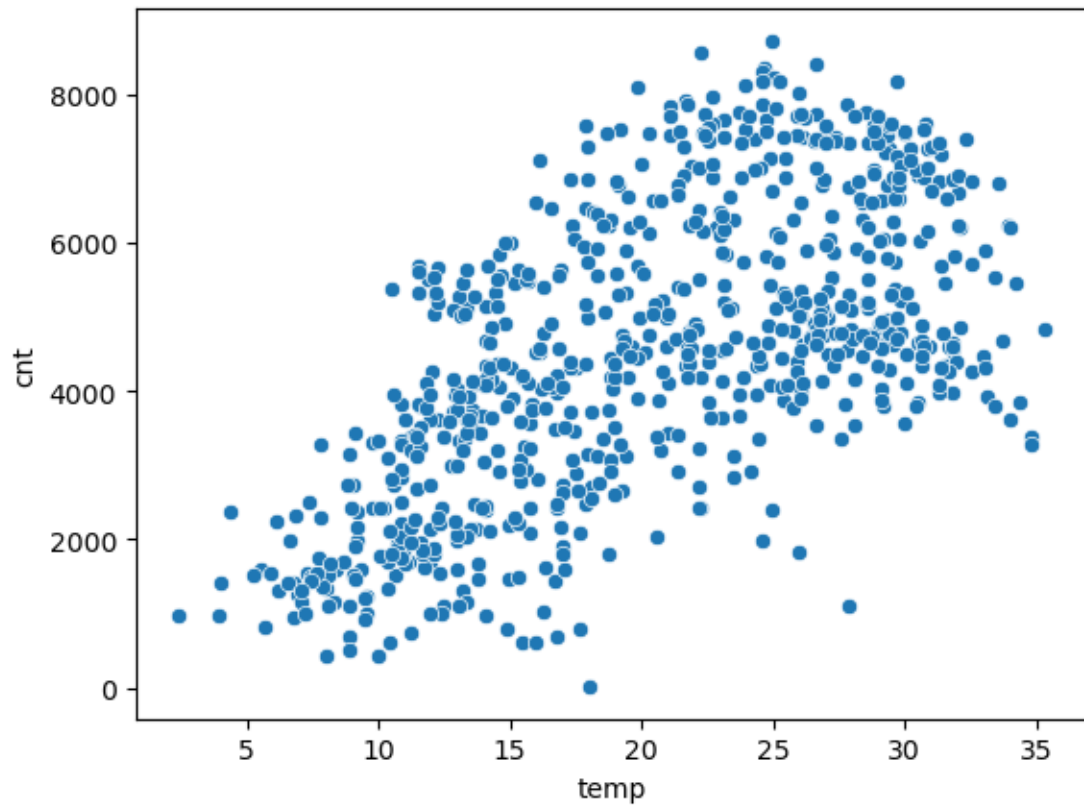
```
[21]: #Relation between Year and count of bike rentals
sns.barplot(x='yr',y='cnt',data=df)
plt.show()
```



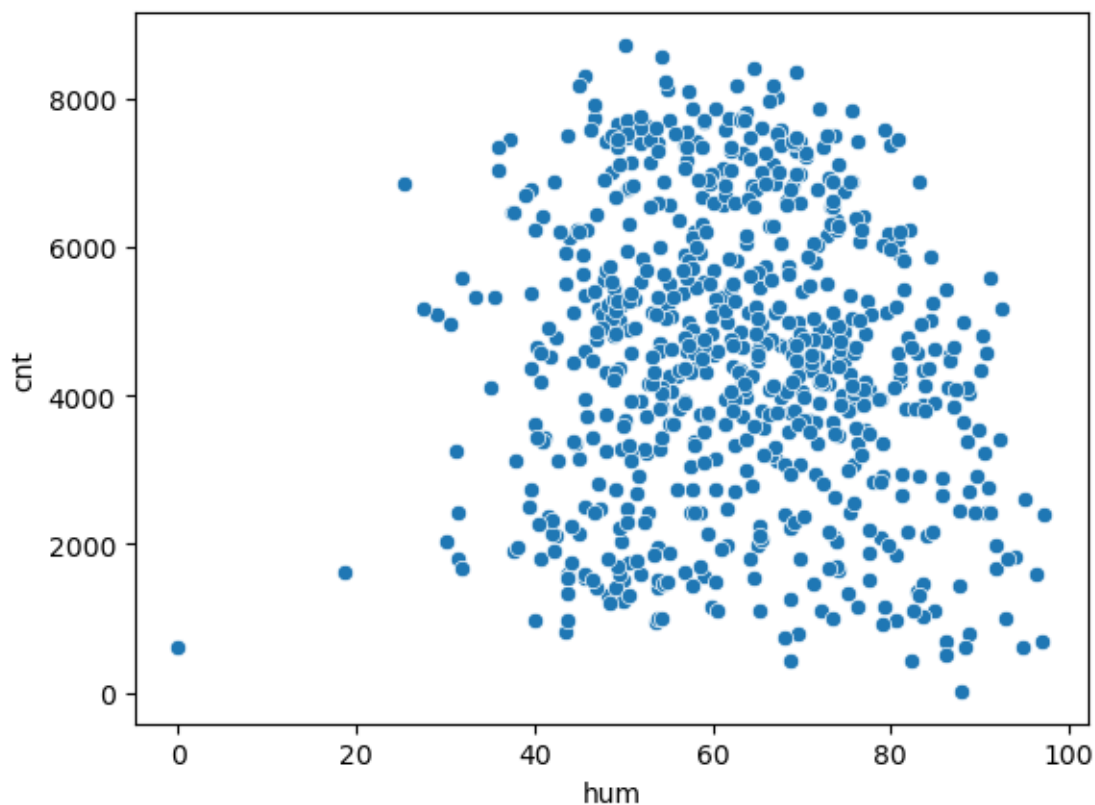
```
[35]: plt.figure(figsize=(10,5))
sns.barplot(x='mnth',y='cnt',hue='yr',data=df)
plt.show()
```



```
[37]: #scatter plot for temperature to count
sns.scatterplot(x='temp',y='cnt' ,data=df)
plt.show()
```



```
[24]: sns.scatterplot(x='hum', y='cnt',data=df)
plt.show()
```



```
[39]: #drop unnecessary columns
df.drop(['instant', 'atemp', 'casual', 'registered'], axis=1, inplace=True)
df
```

```
[39]:
```

|     | season | yr | mnth | holiday | weekday | workingday | weathersit    | temp      | \ |
|-----|--------|----|------|---------|---------|------------|---------------|-----------|---|
| 0   | spring | 0  | Jan  | 0       | Mon     | 1          | Mist + Cloudy | 14.110847 |   |
| 1   | spring | 0  | Jan  | 0       | Tue     | 1          | Mist + Cloudy | 14.902598 |   |
| 2   | spring | 0  | Jan  | 0       | Wed     | 1          | Clear         | 8.050924  |   |
| 3   | spring | 0  | Jan  | 0       | Thu     | 1          | Clear         | 8.200000  |   |
| 4   | spring | 0  | Jan  | 0       | Fri     | 1          | Clear         | 9.305237  |   |
| ..  | ...    | .. | ...  | ...     | ...     | ...        | ...           | ...       |   |
| 725 | spring | 1  | Dec  | 0       | Fri     | 1          | Mist + Cloudy | 10.420847 |   |
| 726 | spring | 1  | Dec  | 0       | Sat     | 0          | Mist + Cloudy | 10.386653 |   |
| 727 | spring | 1  | Dec  | 0       | Sun     | 0          | Mist + Cloudy | 10.386653 |   |
| 728 | spring | 1  | Dec  | 0       | Mon     | 1          | Clear         | 10.489153 |   |
| 729 | spring | 1  | Dec  | 0       | Tue     | 1          | Mist + Cloudy | 8.849153  |   |

|   | hum     | windspeed | cnt  |
|---|---------|-----------|------|
| 0 | 80.5833 | 10.749882 | 985  |
| 1 | 69.6087 | 16.652113 | 801  |
| 2 | 43.7273 | 16.636703 | 1349 |

```

3    59.0435  10.739832  1562
4    43.6957  12.522300  1600
..      ...      ...      ...
725  65.2917  23.458911  2114
726  59.0000  10.416557  3095
727  75.2917   8.333661  1341
728  48.3333  23.500518  1796
729  57.7500  10.374682  2729

```

[730 rows x 11 columns]

```
[41]: df.dtypes
```

```

[41]: season      object
      yr          int64
      mnth        object
      holiday      int64
      weekday      object
      workingday    int64
      weathersit     object
      temp         float64
      hum          float64
      windspeed     float64
      cnt          int64
      dtype: object

```

## 2 3.Data Preparation

```

[43]: # Get the dummy variables for month, season, weathersit, weekday and Let's
      ↪ drop the first column from using 'drop_first = True'pd.get_dummies(bike.
      ↪ season,drop_first=True)
mnths=pd.get_dummies(df.mnth,drop_first=True,dtype=int)
weekdays=pd.get_dummies(df.weekday,drop_first=True,dtype=int)
weathersit=pd.get_dummies(df.weathersit,drop_first=True,dtype=int)
seasons=pd.get_dummies(df.season,drop_first=True,dtype=int)

```

```

[29]: # Add the results to the original bike dataframe
df=pd.concat([mnths,weekdays,weathersit,seasons,df],axis=1)
df

```

```

[29]:
      Aug  Dec  Feb  Jan  July  June  Mar  May  Nov  Oct  ...  yr  mnth  \
0        0    0    0    1    0    0    0    0    0    0  ...  0   Jan
1        0    0    0    1    0    0    0    0    0    0  ...  0   Jan
2        0    0    0    1    0    0    0    0    0    0  ...  0   Jan
3        0    0    0    1    0    0    0    0    0    0  ...  0   Jan
4        0    0    0    1    0    0    0    0    0    0  ...  0   Jan

```

```

..    ...    ...    ...    ...    ...    ...    ...    ...    ...    ...    ...    ...
725    0    1    0    0    0    0    0    0    0    0    0    ...    1    Dec
726    0    1    0    0    0    0    0    0    0    0    0    ...    1    Dec
727    0    1    0    0    0    0    0    0    0    0    0    ...    1    Dec
728    0    1    0    0    0    0    0    0    0    0    0    ...    1    Dec
729    0    1    0    0    0    0    0    0    0    0    0    ...    1    Dec

```

```

    holiday weekday workingday    weathersit    temp    hum \
0         0     Mon         1  Mist + Cloudy  14.110847  80.5833
1         0     Tue         1  Mist + Cloudy  14.902598  69.6087
2         0     Wed         1      Clear    8.050924  43.7273
3         0     Thu         1      Clear    8.200000  59.0435
4         0     Fri         1      Clear    9.305237  43.6957
..    ...    ...    ...    ...    ...    ...
725    0     Fri         1  Mist + Cloudy  10.420847  65.2917
726    0     Sat         0  Mist + Cloudy  10.386653  59.0000
727    0     Sun         0  Mist + Cloudy  10.386653  75.2917
728    0     Mon         1      Clear    10.489153  48.3333
729    0     Tue         1  Mist + Cloudy    8.849153  57.7500

```

```

    windspeed    cnt
0    10.749882   985
1    16.652113   801
2    16.636703  1349
3    10.739832  1562
4    12.522300  1600
..    ...    ...
725    23.458911  2114
726    10.416557  3095
727     8.333661  1341
728    23.500518  1796
729    10.374682  2729

```

[730 rows x 33 columns]

```

[45]: # Drop 'season', 'month', 'weekday', 'weathersit' as we have created the dummies_
      ↪ for it
df.drop(['season', 'mnth', 'weekday', 'weathersit'], axis = 1, inplace = True)
df

```

```

[45]:    yr  holiday  workingday    temp    hum  windspeed    cnt
0     0         0           1  14.110847  80.5833  10.749882   985
1     0         0           1  14.902598  69.6087  16.652113   801
2     0         0           1   8.050924  43.7273  16.636703  1349
3     0         0           1   8.200000  59.0435  10.739832  1562
4     0         0           1   9.305237  43.6957  12.522300  1600
..    ..    ...    ...    ...    ...    ...    ...

```

```

725    1          0          1  10.420847  65.2917  23.458911  2114
726    1          0          0  10.386653  59.0000  10.416557  3095
727    1          0          0  10.386653  75.2917   8.333661  1341
728    1          0          1  10.489153  48.3333  23.500518  1796
729    1          0          1   8.849153  57.7500  10.374682  2729

```

[730 rows x 7 columns]

```

[47]: #Number of rows and columns
df.shape

```

```

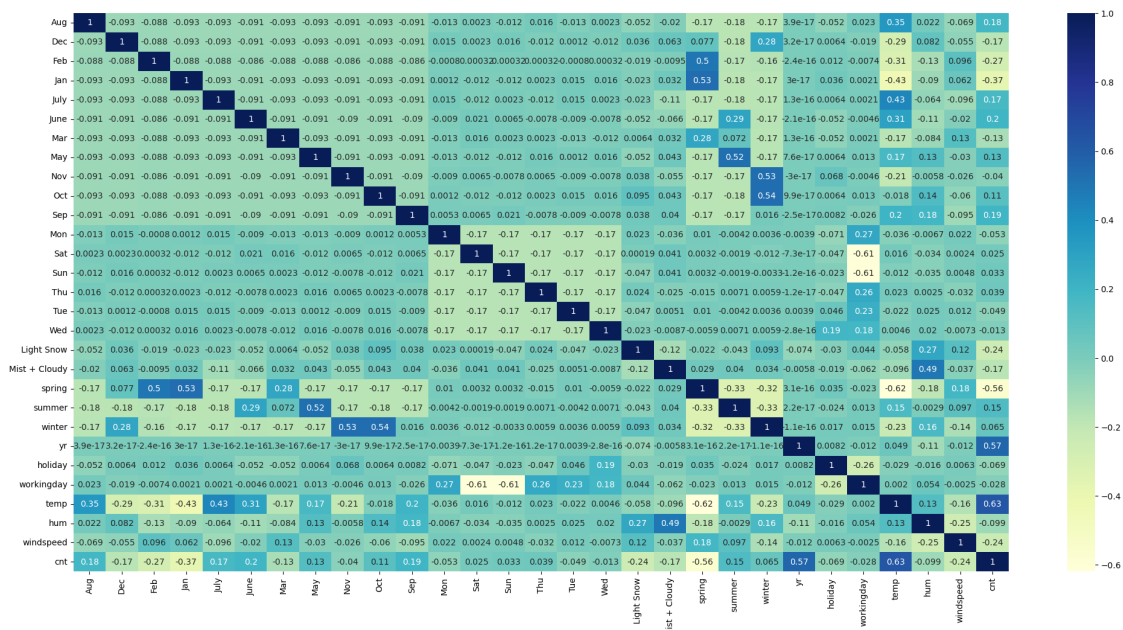
[47]: (730, 7)

```

```

[32]: #Now lets check the correlation between variables again
#Heatmap to see correlation between variables
plt.figure(figsize=(25, 12))
sns.heatmap(df.corr(), cmap='YlGnBu', annot = True)
plt.show()

```



### 3 4.Splitting the Data into Training and Testing Sets

```

[34]: from sklearn.model_selection import train_test_split
# We specify this so that the train and test data set always have the same
rows, respectively
df_train, df_test = train_test_split(df, train_size = 0.7, random_state = 100)

```



```
[35]: #Rows and columns after split
print(df_train.shape)
print(df_test.shape)
```

(510, 29)

(220, 29)

### Rescaling the Features(min-max scaling)

```
[37]: from sklearn.preprocessing import MinMaxScaler
```

```
[38]: #Instantiate an object
scaler = MinMaxScaler()

#Create a list of numeric variables
num_vars=['temp','hum','windspeed','cnt']

#Fit on data
df_train[num_vars] = scaler.fit_transform(df_train[num_vars])
df_train
```

```
[38]:
```

|     | Aug | Dec | Feb | Jan | July | June | Mar | May | Nov | Oct | ... | spring | summer | \ |
|-----|-----|-----|-----|-----|------|------|-----|-----|-----|-----|-----|--------|--------|---|
| 576 | 0   | 0   | 0   | 0   | 1    | 0    | 0   | 0   | 0   | 0   | ... | 0      | 0      |   |
| 426 | 0   | 0   | 0   | 0   | 0    | 0    | 1   | 0   | 0   | 0   | ... | 1      | 0      |   |
| 728 | 0   | 1   | 0   | 0   | 0    | 0    | 0   | 0   | 0   | 0   | ... | 1      | 0      |   |
| 482 | 0   | 0   | 0   | 0   | 0    | 0    | 0   | 0   | 0   | 0   | ... | 0      | 1      |   |
| 111 | 0   | 0   | 0   | 0   | 0    | 0    | 0   | 0   | 0   | 0   | ... | 0      | 1      |   |
| ..  | ... | ... | ... | ... | ...  | ...  | ... | ... | ... | ... | ... | ...    | ...    |   |
| 578 | 1   | 0   | 0   | 0   | 0    | 0    | 0   | 0   | 0   | 0   | ... | 0      | 0      |   |
| 53  | 0   | 0   | 1   | 0   | 0    | 0    | 0   | 0   | 0   | 0   | ... | 1      | 0      |   |
| 350 | 0   | 1   | 0   | 0   | 0    | 0    | 0   | 0   | 0   | 0   | ... | 0      | 0      |   |
| 79  | 0   | 0   | 0   | 0   | 0    | 0    | 1   | 0   | 0   | 0   | ... | 0      | 1      |   |
| 520 | 0   | 0   | 0   | 0   | 0    | 1    | 0   | 0   | 0   | 0   | ... | 0      | 1      |   |

|     | winter | yr | holiday | workingday | temp     | hum      | windspeed | cnt      |
|-----|--------|----|---------|------------|----------|----------|-----------|----------|
| 576 | 0      | 1  | 0       | 1          | 0.815169 | 0.725633 | 0.264686  | 0.827658 |
| 426 | 0      | 1  | 0       | 0          | 0.442393 | 0.640189 | 0.255342  | 0.465255 |
| 728 | 0      | 1  | 0       | 1          | 0.245101 | 0.498067 | 0.663106  | 0.204096 |
| 482 | 0      | 1  | 0       | 0          | 0.395666 | 0.504508 | 0.188475  | 0.482973 |
| 111 | 0      | 0  | 0       | 0          | 0.345824 | 0.751824 | 0.380981  | 0.191095 |
| ..  | ...    | .. | ...     | ...        | ...      | ...      | ...       | ...      |
| 578 | 0      | 1  | 0       | 1          | 0.863973 | 0.679690 | 0.187140  | 0.832835 |
| 53  | 0      | 0  | 0       | 1          | 0.202618 | 0.435939 | 0.111379  | 0.218017 |
| 350 | 1      | 0  | 0       | 1          | 0.248216 | 0.577930 | 0.431816  | 0.312586 |
| 79  | 0      | 0  | 0       | 1          | 0.462664 | 0.759870 | 0.529881  | 0.236424 |
| 520 | 0      | 1  | 0       | 1          | 0.600225 | 0.632030 | 0.359599  | 0.802922 |

[510 rows x 29 columns]

```
[39]: #Checking numeric variables(min and max) after scaling
df_train.describe()
```

```
[39]:
```

|       | Aug        | Dec        | Feb        | Jan        | July       | June \     |
|-------|------------|------------|------------|------------|------------|------------|
| count | 510.000000 | 510.000000 | 510.000000 | 510.000000 | 510.000000 | 510.000000 |
| mean  | 0.096078   | 0.084314   | 0.066667   | 0.088235   | 0.076471   | 0.076471   |
| std   | 0.294988   | 0.278131   | 0.249689   | 0.283915   | 0.266010   | 0.266010   |
| min   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   |
| 25%   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   |
| 50%   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   |
| 75%   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   |
| max   | 1.000000   | 1.000000   | 1.000000   | 1.000000   | 1.000000   | 1.000000   |

|       | Mar        | May        | Nov        | Oct ...    | spring \   |
|-------|------------|------------|------------|------------|------------|
| count | 510.000000 | 510.000000 | 510.000000 | 510.000000 | 510.000000 |
| mean  | 0.098039   | 0.084314   | 0.086275   | 0.084314   | 0.243137   |
| std   | 0.297660   | 0.278131   | 0.281045   | 0.278131   | 0.429398   |
| min   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   |
| 25%   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   |
| 50%   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   |
| 75%   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   |
| max   | 1.000000   | 1.000000   | 1.000000   | 1.000000   | 1.000000   |

|       | summer     | winter     | yr         | holiday    | workingday | temp \     |
|-------|------------|------------|------------|------------|------------|------------|
| count | 510.000000 | 510.000000 | 510.000000 | 510.000000 | 510.000000 | 510.000000 |
| mean  | 0.247059   | 0.247059   | 0.507843   | 0.025490   | 0.711765   | 0.537440   |
| std   | 0.431725   | 0.431725   | 0.500429   | 0.157763   | 0.453386   | 0.225858   |
| min   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   |
| 25%   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.339853   |
| 50%   | 0.000000   | 0.000000   | 1.000000   | 0.000000   | 1.000000   | 0.542596   |
| 75%   | 0.000000   | 0.000000   | 1.000000   | 0.000000   | 1.000000   | 0.735215   |
| max   | 1.000000   | 1.000000   | 1.000000   | 1.000000   | 1.000000   | 1.000000   |

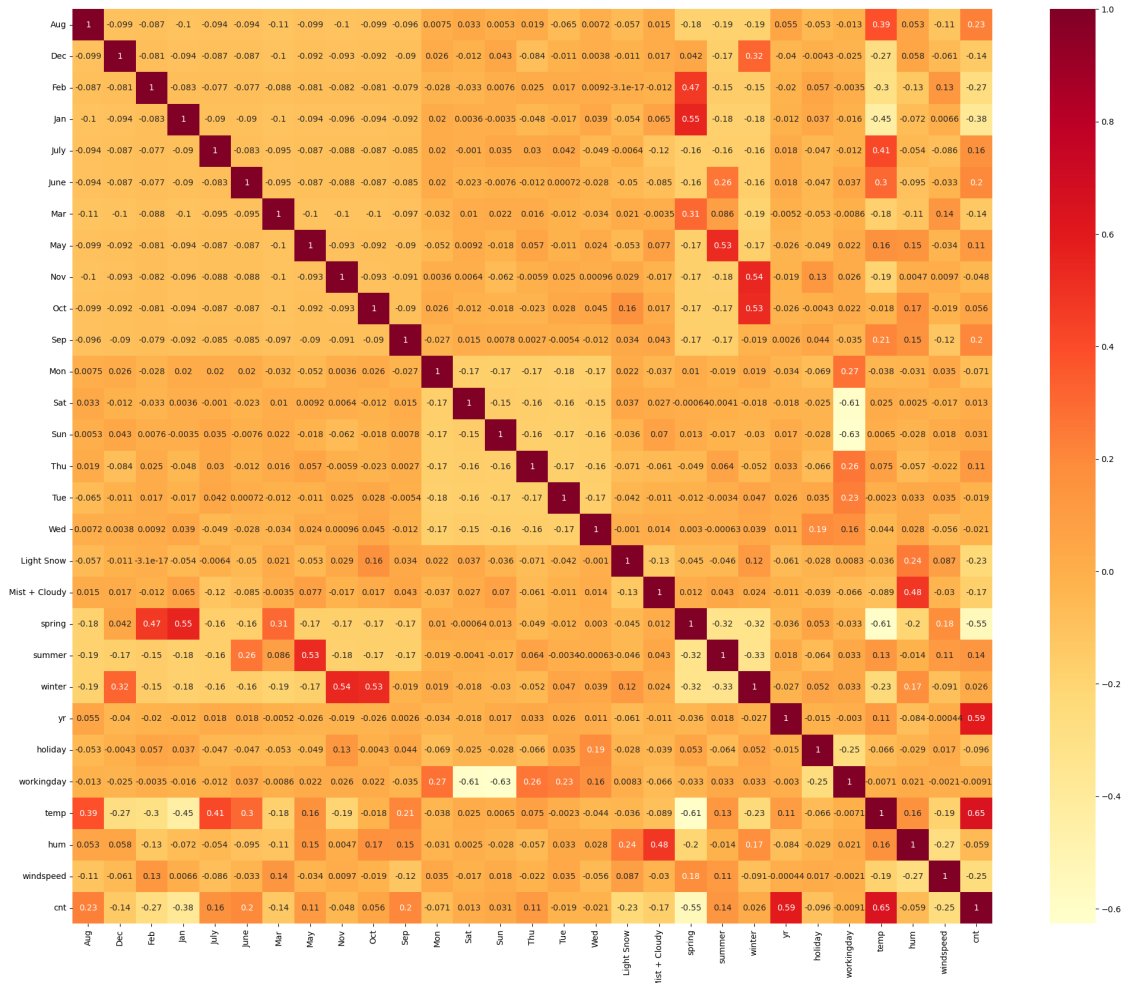
|       | hum        | windspeed  | cnt        |
|-------|------------|------------|------------|
| count | 510.000000 | 510.000000 | 510.000000 |
| mean  | 0.650480   | 0.320883   | 0.513499   |
| std   | 0.145846   | 0.169803   | 0.224421   |
| min   | 0.000000   | 0.000000   | 0.000000   |
| 25%   | 0.538643   | 0.199179   | 0.356420   |
| 50%   | 0.653714   | 0.296763   | 0.518638   |
| 75%   | 0.754830   | 0.414447   | 0.684710   |
| max   | 1.000000   | 1.000000   | 1.000000   |

[8 rows x 29 columns]

```
[40]: # Let's check the correlation coefficients to see which variables are highly
      ↪correlated after scaling
```

```
#Little to no multicollinearity among predictors
```

```
plt.figure(figsize=(25, 20))
sns.heatmap(df_train.corr(),cmap='YlOrRd',annot = True)
plt.show()
```



```
[41]: #Divide the data into X and y
y_train =df_train.pop('cnt')
x_train = df_train
```

## 4 5.Building a linear model

RFE(Recursive feature elimination)

```
[44]: from sklearn.feature_selection import RFE
from sklearn.linear_model import LinearRegression
```

```
[45]: # Running RFE with the output number of the variable equal to 15
lm = LinearRegression()
lm = LinearRegression()
rfe = RFE(lm,n_features_to_select=15)
rfe = rfe.fit(x_train, y_train)
```

```
[46]: #List of variables selected
list(zip(x_train.columns,rfe.support_,rfe.ranking_))
```

```
[46]: [('Aug', False, 9),
      ('Dec', True, 1),
      ('Feb', False, 2),
      ('Jan', True, 1),
      ('July', True, 1),
      ('June', False, 11),
      ('Mar', False, 14),
      ('May', False, 8),
      ('Nov', True, 1),
      ('Oct', False, 12),
      ('Sep', True, 1),
      ('Mon', False, 7),
      ('Sat', False, 4),
      ('Sun', False, 5),
      ('Thu', False, 13),
      ('Tue', False, 6),
      ('Wed', False, 10),
      ('Light Snow', True, 1),
      ('Mist + Cloudy', True, 1),
      ('spring', True, 1),
      ('summer', True, 1),
      ('winter', True, 1),
      ('yr', True, 1),
      ('holiday', True, 1),
      ('workingday', False, 3),
      ('temp', True, 1),
      ('hum', True, 1),
      ('windspeed', True, 1)]
```

```
[47]: #Columns where RFE support is True
col = x_train.columns[rfe.support_]
col
```

```
[47]: Index(['Dec', 'Jan', 'July', 'Nov', 'Sep', 'Light Snow', 'Mist + Cloudy',
        'spring', 'summer', 'winter', 'yr', 'holiday', 'temp', 'hum',
        'windspeed'],
        dtype='object')
```

```
[48]: #Columns where RFE support is False
x_train.columns[~rfe.support_]

[48]: Index(['Aug', 'Feb', 'June', 'Mar', 'May', 'Oct', 'Mon', 'Sat', 'Sun', 'Thu',
        'Tue', 'Wed', 'workingday'],
        dtype='object')

[49]: # Creating X_test dataframe with RFE selected variables
x_train_rfe = x_train[col]

[50]: # Adding a constant variable
import statsmodels.api as sm
x_train_rfe = sm.add_constant(x_train_rfe)

[51]: # Running the linear model
lm = sm.OLS(y_train,x_train_rfe).fit()

[52]: print(lm.summary())
```

```

                                OLS Regression Results
=====
Dep. Variable:                  cnt      R-squared:                  0.845
Model:                        OLS      Adj. R-squared:              0.840
Method:                    Least Squares  F-statistic:                  179.4
Date:                Sat, 06 Jul 2024    Prob (F-statistic):          8.15e-189
Time:                23:08:44             Log-Likelihood:              514.19
No. Observations:                510      AIC:                        -996.4
Df Residuals:                    494      BIC:                        -928.6
Df Model:                        15
Covariance Type:                nonrobust
=====
=
                                coef      std err          t      P>|t|      [0.025
0.975]
-----
-
const                0.3197      0.036      8.859      0.000      0.249
0.391
Dec                 -0.0355      0.018     -2.024      0.043     -0.070
-0.001
Jan                 -0.0434      0.018     -2.393      0.017     -0.079
-0.008
July                -0.0553      0.018     -3.030      0.003     -0.091
-0.019
Nov                 -0.0387      0.019     -2.057      0.040     -0.076
-0.002
Sep                 0.0755      0.017      4.466      0.000      0.042
0.109

```

|               |         |       |        |       |        |
|---------------|---------|-------|--------|-------|--------|
| Light Snow    | -0.2465 | 0.026 | -9.331 | 0.000 | -0.298 |
| -0.195        |         |       |        |       |        |
| Mist + Cloudy | -0.0543 | 0.010 | -5.194 | 0.000 | -0.075 |
| -0.034        |         |       |        |       |        |
| spring        | -0.0613 | 0.021 | -2.881 | 0.004 | -0.103 |
| -0.019        |         |       |        |       |        |
| summer        | 0.0423  | 0.015 | 2.761  | 0.006 | 0.012  |
| 0.072         |         |       |        |       |        |
| winter        | 0.1019  | 0.018 | 5.656  | 0.000 | 0.067  |
| 0.137         |         |       |        |       |        |
| yr            | 0.2304  | 0.008 | 28.487 | 0.000 | 0.215  |
| 0.246         |         |       |        |       |        |
| holiday       | -0.0911 | 0.026 | -3.557 | 0.000 | -0.141 |
| -0.041        |         |       |        |       |        |
| temp          | 0.4815  | 0.037 | 13.005 | 0.000 | 0.409  |
| 0.554         |         |       |        |       |        |
| hum           | -0.1622 | 0.038 | -4.291 | 0.000 | -0.236 |
| -0.088        |         |       |        |       |        |
| windspeed     | -0.1887 | 0.026 | -7.315 | 0.000 | -0.239 |
| -0.138        |         |       |        |       |        |

```
=====
Omnibus:                66.656    Durbin-Watson:                2.025
Prob(Omnibus):           0.000    Jarque-Bera (JB):           161.040
Skew:                    -0.682    Prob(JB):                   1.07e-35
Kurtosis:                5.392    Cond. No.                   20.8
=====
```

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
[53]: #Drop the constant term B0
x_train_rfe = x_train_rfe.drop(['const'], axis=1)
```

```
[54]: # Calculate the VIFs for the new model
from statsmodels.stats.outliers_influence import variance_inflation_factor
vif = pd.DataFrame()
x = x_train_rfe
vif['Features'] = x.columns
vif['VIF'] = [variance_inflation_factor(x.values, i) for i in range(x.shape[1])]
vif['VIF'] = round(vif['VIF'], 2)
vif = vif.sort_values(by = "VIF", ascending = False)
vif
```

```
[54]:      Features      VIF
13      hum  30.89
12      temp  17.79
```

```

14      windspeed  4.72
7        spring  4.37
9        winter  4.06
8        summer  2.82
6  Mist + Cloudy  2.32
10         yr    2.09
3         Nov    1.85
1         Jan    1.75
2         July   1.59
0         Dec    1.56
4         Sep    1.41
5    Light Snow  1.28
11        holiday 1.06

```

```
[55]: #drop July
x_train_new1 = x_train_rfe.drop(["July"], axis = 1)
```

```
[56]: #Build a model
x_train_lm1 = sm.add_constant(x_train_new1)
lm1 = sm.OLS(y_train,x_train_lm1).fit()
print(lm1.summary())
```

#### OLS Regression Results

```

=====
Dep. Variable:          cnt      R-squared:                0.842
Model:                  OLS      Adj. R-squared:           0.838
Method:                 Least Squares      F-statistic:         188.5
Date:                   Sat, 06 Jul 2024    Prob (F-statistic):     5.38e-188
Time:                   23:08:45           Log-Likelihood:        509.49
No. Observations:       510              AIC:                  -989.0
Df Residuals:           495              BIC:                  -925.5
Df Model:                14
Covariance Type:        nonrobust
=====

```

```

=====
=
              coef      std err          t      P>|t|      [0.025
0.975]
-----
-
const          0.3083      0.036      8.520      0.000      0.237
0.379
Dec           -0.0364      0.018     -2.062      0.040     -0.071
-0.002
Jan           -0.0461      0.018     -2.526      0.012     -0.082
-0.010
Nov           -0.0385      0.019     -2.029      0.043     -0.076
-0.001
Sep            0.0900      0.016      5.512      0.000      0.058
=====

```

|               |         |       |        |       |        |
|---------------|---------|-------|--------|-------|--------|
| 0.122         |         |       |        |       |        |
| Light Snow    | -0.2496 | 0.027 | -9.378 | 0.000 | -0.302 |
| -0.197        |         |       |        |       |        |
| Mist + Cloudy | -0.0540 | 0.011 | -5.119 | 0.000 | -0.075 |
| -0.033        |         |       |        |       |        |
| spring        | -0.0490 | 0.021 | -2.328 | 0.020 | -0.090 |
| -0.008        |         |       |        |       |        |
| summer        | 0.0582  | 0.015 | 4.006  | 0.000 | 0.030  |
| 0.087         |         |       |        |       |        |
| winter        | 0.1143  | 0.018 | 6.457  | 0.000 | 0.079  |
| 0.149         |         |       |        |       |        |
| yr            | 0.2312  | 0.008 | 28.372 | 0.000 | 0.215  |
| 0.247         |         |       |        |       |        |
| holiday       | -0.0899 | 0.026 | -3.484 | 0.001 | -0.141 |
| -0.039        |         |       |        |       |        |
| temp          | 0.4642  | 0.037 | 12.586 | 0.000 | 0.392  |
| 0.537         |         |       |        |       |        |
| hum           | -0.1546 | 0.038 | -4.066 | 0.000 | -0.229 |
| -0.080        |         |       |        |       |        |
| windspeed     | -0.1880 | 0.026 | -7.229 | 0.000 | -0.239 |
| -0.137        |         |       |        |       |        |

|                |        |                   |          |
|----------------|--------|-------------------|----------|
| Omnibus:       | 73.786 | Durbin-Watson:    | 2.063    |
| Prob(Omnibus): | 0.000  | Jarque-Bera (JB): | 177.909  |
| Skew:          | -0.751 | Prob(JB):         | 2.33e-39 |
| Kurtosis:      | 5.473  | Cond. No.         | 20.7     |

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
[57]: #Drop the constant term B0
x_train_lm1 = x_train_lm1.drop(['const'], axis=1)
```

```
[58]: # Calculate the VIFs for the new model
vif = pd.DataFrame()
x = x_train_new1
vif['Features'] = x.columns
vif['VIF'] = [variance_inflation_factor(x.values, i) for i in range(x.shape[1])]
vif['VIF'] = round(vif['VIF'], 2)
vif = vif.sort_values(by = "VIF", ascending = False)
vif
```

```
[58]:      Features      VIF
12      hum  30.88
11      temp  16.35
```



```

13      windspeed  4.72
6        spring  4.25
8        winter  3.90
7        summer  2.50
5  Mist + Cloudy  2.32
9            yr  2.09
2          Nov  1.84
1          Jan  1.74
0          Dec  1.55
3          Sep  1.31
4    Light Snow  1.28
10         holiday  1.06

```

```

[59]: #Drop humidity
x_train_new2 = x_train_lm1.drop(["hum"], axis = 1)

```

```

[60]: #Build a model
x_train_lm2 = sm.add_constant(x_train_new2)
lm2 = sm.OLS(y_train,x_train_lm2).fit()
print(lm2.summary())

```

#### OLS Regression Results

```

=====
Dep. Variable:          cnt    R-squared:                0.837
Model:                  OLS    Adj. R-squared:           0.832
Method:                 Least Squares    F-statistic:        195.6
Date:                  Sat, 06 Jul 2024    Prob (F-statistic):    1.23e-185
Time:                  23:08:45    Log-Likelihood:        501.12
No. Observations:      510    AIC:                  -974.2
Df Residuals:          496    BIC:                  -915.0
Df Model:              13
Covariance Type:       nonrobust
=====

```

```

=

```

|        | coef    | std err | t      | P> t  | [0.025 |
|--------|---------|---------|--------|-------|--------|
| 0.975] |         |         |        |       |        |
| -----  |         |         |        |       |        |
| -      |         |         |        |       |        |
| const  | 0.2379  | 0.032   | 7.373  | 0.000 | 0.174  |
| 0.301  |         |         |        |       |        |
| Dec    | -0.0434 | 0.018   | -2.429 | 0.015 | -0.078 |
| -0.008 |         |         |        |       |        |
| Jan    | -0.0522 | 0.018   | -2.824 | 0.005 | -0.089 |
| -0.016 |         |         |        |       |        |
| Nov    | -0.0393 | 0.019   | -2.040 | 0.042 | -0.077 |
| -0.001 |         |         |        |       |        |
| Sep    | 0.0823  | 0.016   | 4.994  | 0.000 | 0.050  |
| 0.115  |         |         |        |       |        |

|                         |         |       |         |       |        |
|-------------------------|---------|-------|---------|-------|--------|
| Light Snow<br>-0.244    | -0.2926 | 0.025 | -11.803 | 0.000 | -0.341 |
| Mist + Cloudy<br>-0.061 | -0.0787 | 0.009 | -8.994  | 0.000 | -0.096 |
| spring<br>-0.018        | -0.0597 | 0.021 | -2.814  | 0.005 | -0.101 |
| summer<br>0.078         | 0.0496  | 0.015 | 3.400   | 0.001 | 0.021  |
| winter<br>0.133         | 0.0988  | 0.018 | 5.628   | 0.000 | 0.064  |
| yr<br>0.251             | 0.2350  | 0.008 | 28.586  | 0.000 | 0.219  |
| holiday<br>-0.039       | -0.0907 | 0.026 | -3.460  | 0.001 | -0.142 |
| temp<br>0.496           | 0.4248  | 0.036 | 11.755  | 0.000 | 0.354  |
| windspeed<br>-0.109     | -0.1591 | 0.025 | -6.263  | 0.000 | -0.209 |

|                |        |                   |          |
|----------------|--------|-------------------|----------|
| Omnibus:       | 73.264 | Durbin-Watson:    | 2.057    |
| Prob(Omnibus): | 0.000  | Jarque-Bera (JB): | 179.059  |
| Skew:          | -0.742 | Prob(JB):         | 1.31e-39 |
| Kurtosis:      | 5.495  | Cond. No.         | 18.8     |

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
[61]: #Drop the constant
x_train_lm2=x_train_lm2.drop(['const'],axis=1)
```

```
[62]: # Calculate the VIFs for the new model
vif = pd.DataFrame()
x = x_train_new2
vif['Features'] = x.columns
vif['VIF'] = [variance_inflation_factor(x.values, i) for i in range(x.shape[1])]
vif['VIF'] = round(vif['VIF'], 2)
vif = vif.sort_values(by = "VIF", ascending = False)
vif
```

```
[62]:
```

|    | Features  | VIF  |
|----|-----------|------|
| 12 | windspeed | 4.66 |
| 11 | temp      | 3.88 |
| 8  | winter    | 2.77 |
| 6  | spring    | 2.76 |
| 9  | yr        | 2.07 |

```

7      summer  1.91
2      Nov    1.81
1      Jan    1.65
5  Mist + Cloudy  1.56
0      Dec    1.46
3      Sep    1.25
4  Light Snow  1.09
10     holiday  1.06

```

```
[63]: #Drop the windspeed column
x_train_new3=x_train_lm2.drop(['windspeed'],axis=1)
```

```
[64]: # Adding a constant variable
x_train_lm3 = sm.add_constant(x_train_new3)
lm3 = sm.OLS(y_train,x_train_lm3).fit()
print(lm3.summary())
```

#### OLS Regression Results

```

=====
Dep. Variable:          cnt      R-squared:                0.824
Model:                  OLS      Adj. R-squared:           0.820
Method:                 Least Squares      F-statistic:         193.7
Date:                  Sat, 06 Jul 2024      Prob (F-statistic):    1.25e-178
Time:                  23:08:45      Log-Likelihood:       481.71
No. Observations:      510      AIC:                  -937.4
Df Residuals:          497      BIC:                  -882.4
Df Model:              12
Covariance Type:       nonrobust
=====

```

```

=====
=
              coef      std err          t      P>|t|      [0.025
0.975]
-----
-
const          0.1761      0.032      5.525      0.000      0.114
0.239
Dec          -0.0337      0.018     -1.827      0.068     -0.070
0.003
Jan          -0.0355      0.019     -1.870      0.062     -0.073
0.002
Nov          -0.0413      0.020     -2.068      0.039     -0.081
-0.002
Sep           0.0878      0.017      5.144      0.000      0.054
0.121
Light Snow   -0.3070      0.026    -11.980      0.000     -0.357
-0.257
Mist + Cloudy -0.0772      0.009     -8.510      0.000     -0.095
-0.059

```

|         |         |       |        |       |        |
|---------|---------|-------|--------|-------|--------|
| spring  | -0.0712 | 0.022 | -3.248 | 0.001 | -0.114 |
| -0.028  |         |       |        |       |        |
| summer  | 0.0417  | 0.015 | 2.761  | 0.006 | 0.012  |
| 0.071   |         |       |        |       |        |
| winter  | 0.1024  | 0.018 | 5.623  | 0.000 | 0.067  |
| 0.138   |         |       |        |       |        |
| yr      | 0.2338  | 0.009 | 27.407 | 0.000 | 0.217  |
| 0.251   |         |       |        |       |        |
| holiday | -0.0930 | 0.027 | -3.419 | 0.001 | -0.146 |
| -0.040  |         |       |        |       |        |
| temp    | 0.4482  | 0.037 | 12.018 | 0.000 | 0.375  |
| 0.522   |         |       |        |       |        |

|                |        |                   |          |
|----------------|--------|-------------------|----------|
| Omnibus:       | 78.127 | Durbin-Watson:    | 2.049    |
| Prob(Omnibus): | 0.000  | Jarque-Bera (JB): | 204.916  |
| Skew:          | -0.764 | Prob(JB):         | 3.18e-45 |
| Kurtosis:      | 5.703  | Cond. No.         | 18.1     |

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
[65]: #Drop constant
x_train_lm3=x_train_lm3.drop(['const'],axis=1)
```

```
[66]: # Calculate the VIFs for the new model
vif = pd.DataFrame()
x = x_train_new3
vif['Features'] = x.columns
vif['VIF'] = [variance_inflation_factor(x.values, i) for i in range(x.shape[1])]
vif['VIF'] = round(vif['VIF'], 2)
vif = vif.sort_values(by = "VIF", ascending = False)
vif
```

```
[66]:
```

|    | Features      | VIF  |
|----|---------------|------|
| 11 | temp          | 2.93 |
| 8  | winter        | 2.64 |
| 9  | yr            | 2.07 |
| 6  | spring        | 2.01 |
| 2  | Nov           | 1.79 |
| 1  | Jan           | 1.64 |
| 7  | summer        | 1.63 |
| 5  | Mist + Cloudy | 1.56 |
| 0  | Dec           | 1.46 |
| 3  | Sep           | 1.25 |
| 4  | Light Snow    | 1.07 |

10 holiday 1.06

```
[67]: #Drop Nov
x_train_new4= x_train_lm3.drop(['Nov'], axis=1)
```

```
[68]: #Build a model
x_train_lm4=sm.add_constant(x_train_new4)
lm4=sm.OLS(y_train,x_train_lm4).fit()
print(lm4.summary())
```

#### OLS Regression Results

```
=====
Dep. Variable:          cnt      R-squared:            0.822
Model:                  OLS      Adj. R-squared:       0.818
Method:                 Least Squares      F-statistic:      209.6
Date:                  Sat, 06 Jul 2024      Prob (F-statistic):  7.02e-179
Time:                  23:08:45      Log-Likelihood:      479.53
No. Observations:      510      AIC:                -935.1
Df Residuals:          498      BIC:                -884.2
Df Model:              11
Covariance Type:       nonrobust
=====
```

```
=

```

|               | coef    | std err | t       | P> t  | [0.025 |
|---------------|---------|---------|---------|-------|--------|
| 0.975]        |         |         |         |       |        |
| -----         |         |         |         |       |        |
| -             |         |         |         |       |        |
| const         | 0.1583  | 0.031   | 5.141   | 0.000 | 0.098  |
| 0.219         |         |         |         |       |        |
| Dec           | -0.0185 | 0.017   | -1.088  | 0.277 | -0.052 |
| 0.015         |         |         |         |       |        |
| Jan           | -0.0303 | 0.019   | -1.605  | 0.109 | -0.067 |
| 0.007         |         |         |         |       |        |
| Sep           | 0.0935  | 0.017   | 5.532   | 0.000 | 0.060  |
| 0.127         |         |         |         |       |        |
| Light Snow    | -0.3029 | 0.026   | -11.819 | 0.000 | -0.353 |
| -0.253        |         |         |         |       |        |
| Mist + Cloudy | -0.0764 | 0.009   | -8.402  | 0.000 | -0.094 |
| -0.059        |         |         |         |       |        |
| spring        | -0.0629 | 0.022   | -2.909  | 0.004 | -0.105 |
| -0.020        |         |         |         |       |        |
| summer        | 0.0473  | 0.015   | 3.177   | 0.002 | 0.018  |
| 0.077         |         |         |         |       |        |
| winter        | 0.0924  | 0.018   | 5.247   | 0.000 | 0.058  |
| 0.127         |         |         |         |       |        |
| yr            | 0.2336  | 0.009   | 27.296  | 0.000 | 0.217  |
| 0.250         |         |         |         |       |        |
| holiday       | -0.0997 | 0.027   | -3.681  | 0.000 | -0.153 |

|        |        |       |        |       |       |
|--------|--------|-------|--------|-------|-------|
| -0.047 |        |       |        |       |       |
| temp   | 0.4687 | 0.036 | 12.991 | 0.000 | 0.398 |
| 0.540  |        |       |        |       |       |

```
=====
```

|                |        |                   |          |
|----------------|--------|-------------------|----------|
| Omnibus:       | 71.781 | Durbin-Watson:    | 2.066    |
| Prob(Omnibus): | 0.000  | Jarque-Bera (JB): | 175.328  |
| Skew:          | -0.728 | Prob(JB):         | 8.47e-39 |
| Kurtosis:      | 5.477  | Cond. No.         | 17.4     |

```
=====
```

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
[69]: #Drop constant
x_train_lm4= x_train_lm4.drop(['const'], axis=1)
```

```
[70]: # Calculate the VIFs for the new model
vif = pd.DataFrame()
x =x_train_new4
vif['Features'] = x.columns
vif['VIF'] = [variance_inflation_factor(x.values, i) for i in range(x.shape[1])]
vif['VIF'] = round(vif['VIF'], 2)
vif = vif.sort_values(by = "VIF", ascending = False)
vif
```

```
[70]:
```

|    | Features      | VIF  |
|----|---------------|------|
| 10 | temp          | 2.93 |
| 8  | yr            | 2.07 |
| 5  | spring        | 2.00 |
| 7  | winter        | 1.67 |
| 1  | Jan           | 1.64 |
| 6  | summer        | 1.63 |
| 4  | Mist + Cloudy | 1.56 |
| 0  | Dec           | 1.29 |
| 2  | Sep           | 1.23 |
| 3  | Light Snow    | 1.07 |
| 9  | holiday       | 1.04 |

```
[71]: #Drop holiday
x_train_new5=x_train_lm4.drop(['holiday'], axis=1)
```

```
[72]: #Building a model
x_train_lm5= sm.add_constant(x_train_new5)
lm5=sm.OLS(y_train,x_train_lm5).fit()
print(lm5.summary())
```

OLS Regression Results

```

=====
Dep. Variable:          cnt    R-squared:                0.818
Model:                  OLS    Adj. R-squared:           0.814
Method:                  Least Squares    F-statistic:           223.6
Date:                    Sat, 06 Jul 2024    Prob (F-statistic):      3.56e-177
Time:                    23:08:45    Log-Likelihood:         472.68
No. Observations:        510    AIC:                    -923.4
Df Residuals:            499    BIC:                    -876.8
Df Model:                 10
Covariance Type:         nonrobust
=====

```

```

=
              coef      std err          t      P>|t|      [0.025
0.975]
-----
-
const          0.1552      0.031      4.980      0.000      0.094
0.216
Dec           -0.0163      0.017     -0.951      0.342     -0.050
0.017
Jan           -0.0305      0.019     -1.594      0.112     -0.068
0.007
Sep            0.0898      0.017      5.259      0.000      0.056
0.123
Light Snow    -0.2987      0.026    -11.520      0.000     -0.350
-0.248
Mist + Cloudy -0.0747      0.009     -8.120      0.000     -0.093
-0.057
spring        -0.0654      0.022     -2.992      0.003     -0.108
-0.022
summer         0.0474      0.015      3.147      0.002      0.018
0.077
winter         0.0893      0.018      5.013      0.000      0.054
0.124
yr             0.2339      0.009     27.004      0.000      0.217
0.251
temp          0.4708      0.037     12.890      0.000      0.399
0.543
=====

```

```

=====
Omnibus:          77.027    Durbin-Watson:          2.024
Prob(Omnibus):    0.000    Jarque-Bera (JB):       188.651
Skew:             -0.777    Prob(JB):               1.08e-41
Kurtosis:         5.542    Cond. No.                17.4
=====

```

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
[73]: #Drop the constant
x_train_lm7=x_train_lm5.drop(['const'],axis=1)
```

```
[74]: # Calculate the VIFs for the new model
vif = pd.DataFrame()
x = x_train_new5
vif['Features'] = x.columns
vif['VIF'] = [variance_inflation_factor(x.values, i) for i in range(x.shape[1])]
vif['VIF'] = round(vif['VIF'], 2)
vif = vif.sort_values(by = "VIF", ascending = False)
vif
```

```
[74]:
```

|   | Features      | VIF  |
|---|---------------|------|
| 9 | temp          | 2.93 |
| 8 | yr            | 2.07 |
| 5 | spring        | 1.98 |
| 7 | winter        | 1.65 |
| 1 | Jan           | 1.64 |
| 6 | summer        | 1.63 |
| 4 | Mist + Cloudy | 1.56 |
| 0 | Dec           | 1.29 |
| 2 | Sep           | 1.23 |
| 3 | Light Snow    | 1.07 |

```
[75]: #Drop temp for the lm4 model
x_train_new6=x_train_lm4.drop(['temp'], axis=1)
```

```
[76]: #Building a model
x_train_lm6= sm.add_constant(x_train_new6)
lm6=sm.OLS(y_train,x_train_lm6).fit()
print(lm6.summary())
```

```

OLS Regression Results
=====
Dep. Variable:          cnt      R-squared:                0.762
Model:                  OLS      Adj. R-squared:           0.757
Method:                 Least Squares      F-statistic:           159.9
Date:                   Sat, 06 Jul 2024    Prob (F-statistic):      1.40e-148
Time:                   23:08:45           Log-Likelihood:         405.10
No. Observations:       510             AIC:                   -788.2
Df Residuals:           499             BIC:                   -741.6
Df Model:                10
Covariance Type:        nonrobust
=====
=

```

|        | coef | std err | t | P> t | [0.025 |
|--------|------|---------|---|------|--------|
| 0.975] |      |         |   |      |        |

```

-----

```



```

-
const          0.5337    0.012    43.522    0.000    0.510
0.558
Dec            -0.0673    0.019    -3.521    0.000    -0.105
-0.030
Jan            -0.0989    0.021    -4.720    0.000    -0.140
-0.058
Sep            0.0763    0.019     3.917    0.000    0.038
0.115
Light Snow     -0.3223    0.030   -10.896    0.000    -0.380
-0.264
Mist + Cloudy  -0.0839    0.010    -7.994    0.000    -0.104
-0.063
spring         -0.2722    0.017   -16.342    0.000    -0.305
-0.239
summer         -0.0562    0.015    -3.863    0.000    -0.085
-0.028
winter         -0.0632    0.015    -4.235    0.000    -0.093
-0.034
yr              0.2459    0.010    25.009    0.000    0.227
0.265
holiday        -0.1053    0.031    -3.363    0.001    -0.167
-0.044
=====
Omnibus:                49.619   Durbin-Watson:                2.006
Prob(Omnibus):           0.000   Jarque-Bera (JB):           119.252
Skew:                    -0.512   Prob(JB):                   1.27e-26
Kurtosis:                5.136   Cond. No.                   8.36
=====

```

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

## 5 6.Residual Analysis of the train data

```

[77]: #X_train_lm5=sm.add_constant(X_train_lm5)
      #X_train_lm5.columns
      x_train_lm5

```

```

[77]:      const  Dec  Jan  Sep  Light Snow  Mist + Cloudy  spring  summer  winter  \
576    1.0    0    0    0          0          0    0    0    0
426    1.0    0    0    0          0          1    1    0    0
728    1.0    1    0    0          0          0    1    0    0
482    1.0    0    0    0          0          1    0    1    0
111    1.0    0    0    0          0          1    0    1    0
..      ...  ...  ...  ...      ...      ...  ...  ...  ...

```

|     |     |   |   |   |   |   |   |   |   |
|-----|-----|---|---|---|---|---|---|---|---|
| 578 | 1.0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 53  | 1.0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| 350 | 1.0 | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 1 |
| 79  | 1.0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 0 |
| 520 | 1.0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 0 |

|     | yr | temp     |
|-----|----|----------|
| 576 | 1  | 0.815169 |
| 426 | 1  | 0.442393 |
| 728 | 1  | 0.245101 |
| 482 | 1  | 0.395666 |
| 111 | 0  | 0.345824 |
| ..  | .. | ...      |
| 578 | 1  | 0.863973 |
| 53  | 0  | 0.202618 |
| 350 | 0  | 0.248216 |
| 79  | 0  | 0.462664 |
| 520 | 1  | 0.600225 |

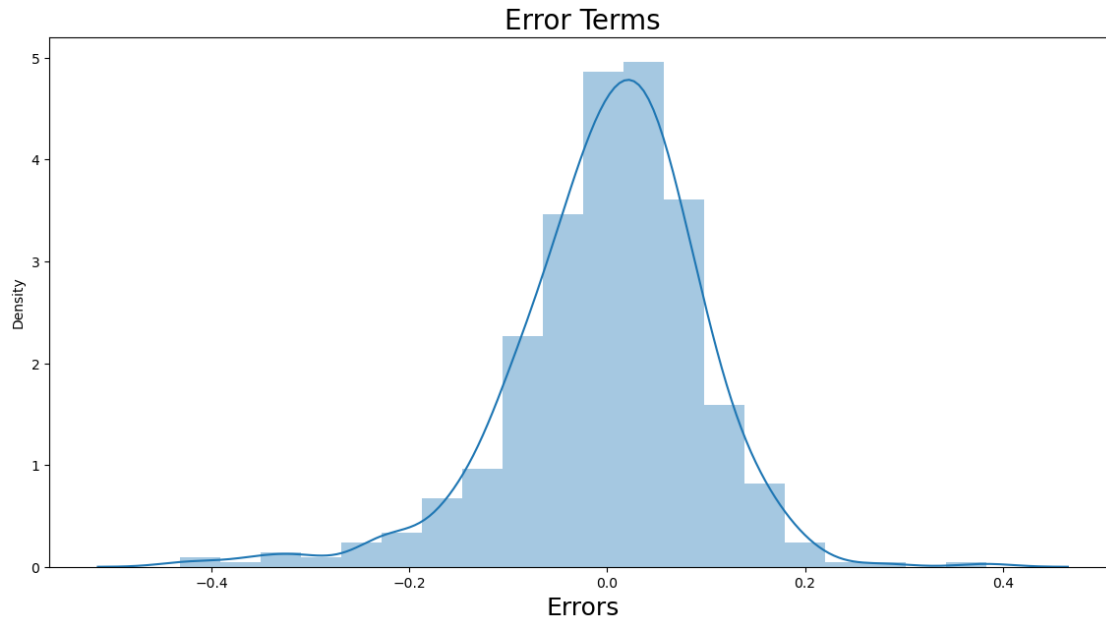
[510 rows x 11 columns]

```
[78]: #y train predicted
y_train_pred = lm5.predict(x_train_lm5)
```

```
[79]: # Plot the histogram of the error terms

fig = plt.figure()
plt.figure(figsize=(14,7))
sns.distplot((y_train - y_train_pred), bins = 20)
plt.title('Error Terms', fontsize = 20)           # Plot heading
plt.xlabel('Errors', fontsize = 18)               # X-label
plt.show()
```

<Figure size 640x480 with 0 Axes>



## 6 7.Making Predictions

```
[81]: #Create a list of numeric variables
num_vars=['temp', 'hum', 'windspeed', 'cnt']

#Fit on data
df_test[num_vars] = scaler.transform(df_test[num_vars])
df_test.head()
```

```
[81]:
```

|     | Aug | Dec | Feb | Jan | July | June | Mar | May | Nov | Oct | ... | spring | summer | \ |
|-----|-----|-----|-----|-----|------|------|-----|-----|-----|-----|-----|--------|--------|---|
| 184 | 0   | 0   | 0   | 0   | 1    | 0    | 0   | 0   | 0   | 0   | ... | 0      | 0      |   |
| 535 | 0   | 0   | 0   | 0   | 0    | 1    | 0   | 0   | 0   | 0   | ... | 0      | 1      |   |
| 299 | 0   | 0   | 0   | 0   | 0    | 0    | 0   | 0   | 0   | 1   | ... | 0      | 0      |   |
| 221 | 1   | 0   | 0   | 0   | 0    | 0    | 0   | 0   | 0   | 0   | ... | 0      | 0      |   |
| 152 | 0   | 0   | 0   | 0   | 0    | 1    | 0   | 0   | 0   | 0   | ... | 0      | 1      |   |

|     | winter | yr | holiday | workingday | temp     | hum      | windspeed | cnt      |
|-----|--------|----|---------|------------|----------|----------|-----------|----------|
| 184 | 0      | 0  | 1       | 0          | 0.831783 | 0.657364 | 0.084219  | 0.692706 |
| 535 | 0      | 1  | 0       | 1          | 0.901354 | 0.610133 | 0.153728  | 0.712034 |
| 299 | 1      | 0  | 0       | 0          | 0.511964 | 0.837699 | 0.334206  | 0.303382 |
| 221 | 0      | 0  | 0       | 1          | 0.881625 | 0.437098 | 0.339570  | 0.547400 |
| 152 | 0      | 0  | 0       | 0          | 0.817246 | 0.314298 | 0.537414  | 0.569029 |

```
[5 rows x 29 columns]
```

```
[82]: #Dividing into X_test and y_test
y_test =df_test.pop('cnt')
x_test =df_test
x_test.describe()
```

```
[82]:
```

|       | Aug        | Dec        | Feb        | Jan        | July       | June \     |
|-------|------------|------------|------------|------------|------------|------------|
| count | 220.000000 | 220.000000 | 220.000000 | 220.000000 | 220.000000 | 220.000000 |
| mean  | 0.059091   | 0.086364   | 0.100000   | 0.077273   | 0.104545   | 0.095455   |
| std   | 0.236333   | 0.281541   | 0.300684   | 0.267633   | 0.306665   | 0.294512   |
| min   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   |
| 25%   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   |
| 50%   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   |
| 75%   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   |
| max   | 1.000000   | 1.000000   | 1.000000   | 1.000000   | 1.000000   | 1.000000   |

|       | Mar        | May        | Nov        | Oct ...    | Mist + Cloudy \ |
|-------|------------|------------|------------|------------|-----------------|
| count | 220.000000 | 220.000000 | 220.000000 | 220.000000 | 220.000000      |
| mean  | 0.054545   | 0.086364   | 0.072727   | 0.086364   | 0.318182        |
| std   | 0.227609   | 0.281541   | 0.260281   | 0.281541   | 0.466833        |
| min   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000        |
| 25%   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000        |
| 50%   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000        |
| 75%   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 1.000000        |
| max   | 1.000000   | 1.000000   | 1.000000   | 1.000000   | 1.000000        |

|       | spring     | summer     | winter     | yr         | holiday    | workingday \ |
|-------|------------|------------|------------|------------|------------|--------------|
| count | 220.000000 | 220.000000 | 220.000000 | 220.000000 | 220.000000 | 220.000000   |
| mean  | 0.254545   | 0.263636   | 0.236364   | 0.481818   | 0.036364   | 0.640909     |
| std   | 0.436599   | 0.441609   | 0.425817   | 0.500809   | 0.187620   | 0.480828     |
| min   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000     |
| 25%   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000     |
| 50%   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 0.000000   | 1.000000     |
| 75%   | 1.000000   | 1.000000   | 0.000000   | 1.000000   | 0.000000   | 1.000000     |
| max   | 1.000000   | 1.000000   | 1.000000   | 1.000000   | 1.000000   | 1.000000     |

|       | temp       | hum        | windspeed  |
|-------|------------|------------|------------|
| count | 220.000000 | 220.000000 | 220.000000 |
| mean  | 0.558718   | 0.638221   | 0.313293   |
| std   | 0.233187   | 0.148694   | 0.159584   |
| min   | 0.046591   | 0.261915   | -0.042808  |
| 25%   | 0.355429   | 0.529197   | 0.198843   |
| 50%   | 0.558172   | 0.625590   | 0.300126   |
| 75%   | 0.755981   | 0.743798   | 0.402718   |
| max   | 0.984424   | 1.002146   | 0.807474   |

[8 rows x 28 columns]

```
[83]: #Columns
x_train_new5.columns

[83]: Index(['Dec', 'Jan', 'Sep', 'Light Snow', 'Mist + Cloudy', 'spring', 'summer',
        'winter', 'yr', 'temp'],
        dtype='object')
```

```
[84]: # Now let's use our model to make predictions.

# Creating X_test_new dataframe by dropping variables from X_test
x_test_new = x_test[x_train_new5.columns]

# Adding a constant variable
x_test_new1 = sm.add_constant(x_test_new)
x_test_new1.head()
```

```
[84]:
```

|     | const | Dec | Jan | Sep | Light Snow | Mist + Cloudy | spring | summer | winter | \ |
|-----|-------|-----|-----|-----|------------|---------------|--------|--------|--------|---|
| 184 | 1.0   | 0   | 0   | 0   | 0          | 1             | 0      | 0      | 0      |   |
| 535 | 1.0   | 0   | 0   | 0   | 0          | 0             | 0      | 1      | 0      |   |
| 299 | 1.0   | 0   | 0   | 0   | 0          | 1             | 0      | 0      | 1      |   |
| 221 | 1.0   | 0   | 0   | 0   | 0          | 0             | 0      | 0      | 0      |   |
| 152 | 1.0   | 0   | 0   | 0   | 0          | 0             | 0      | 1      | 0      |   |

|     | yr | temp     |
|-----|----|----------|
| 184 | 0  | 0.831783 |
| 535 | 1  | 0.901354 |
| 299 | 0  | 0.511964 |
| 221 | 0  | 0.881625 |
| 152 | 0  | 0.817246 |

```
[85]: # Making predictions
y_pred = lm5.predict(x_test_new1)
```

### Finding R-squared and Adjusted R-Squared for Test set

```
[86]: #Evaluate R-square for test
from sklearn.metrics import r2_score
r2_score(y_test,y_pred)
```

```
[86]: 0.8099204382008233
```

```
[87]: #Adjusted R^2
#adj r2=1-(1-R2)*(n-1)/(n-p-1)

#n =sample size , p = number of independent variables

Adj_r2=1-(1-0.8115083)*(11-1)/(11-1-1)
print(Adj_r2)
```

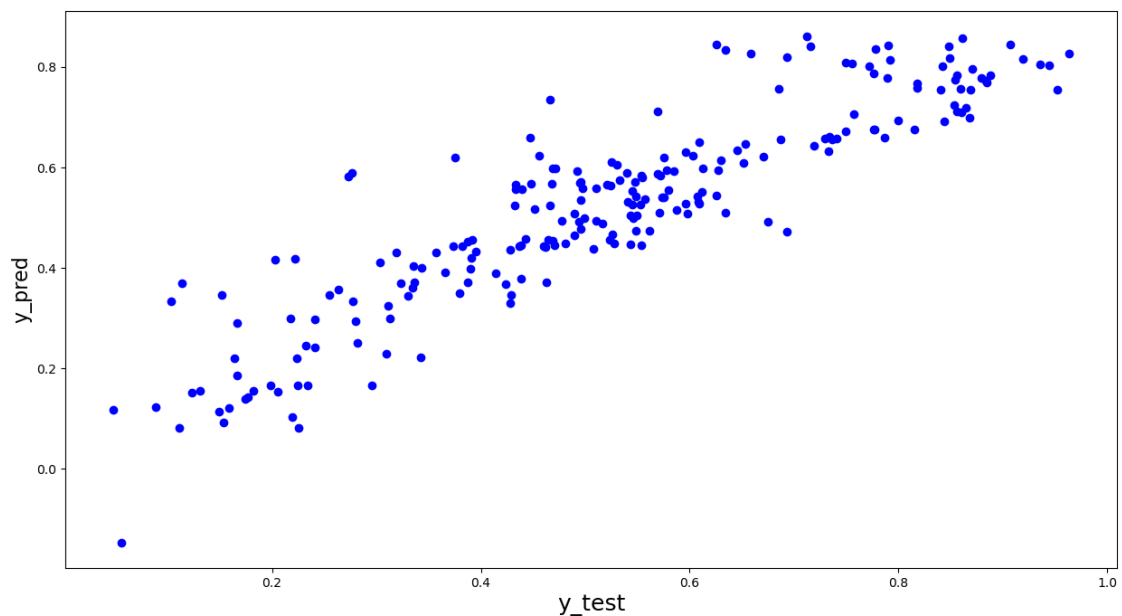
0.7905647777777778

## 7 8.Model Evaluation

```
[88]: # Plotting y_test and y_pred to understand the spread.
fig = plt.figure()
plt.figure(figsize=(15,8))
plt.scatter(y_test,y_pred,color='blue')
fig.suptitle('y_test vs y_pred', fontsize=20)           # Plot heading
plt.xlabel('y_test', fontsize=18)                     # X-label
plt.ylabel('y_pred', fontsize=16)                     # Y-label
```

```
[88]: Text(0, 0.5, 'y_pred')
```

<Figure size 640x480 with 0 Axes>



```
[89]: #Regression plot
plt.figure(figsize=(15,8))
sns.regplot(x=y_test, y=y_pred, ci=68, fit_reg=True, scatter_kws={"color": "blue"}, line_kws={"color": "red"})

plt.title('y_test vs y_pred', fontsize=20)           # Plot heading
plt.xlabel('y_test', fontsize=18)                     # X-label
plt.ylabel('y_pred', fontsize=16)                     # Y-label
plt.show()
```

