

A second advantage of digital computing machines is that they are not restricted in their applications to any particular type of problem. The differential analyzer is by far the most general type of analogue machine yet produced, but it is conceptually limited in its scope. It can be made to deal with almost any kind of ordinary differential equation, but it is hardly able to deal with partial differential equations at all, and certainly cannot manage large numbers of linear simultaneous equations, or the sums of polynomials. With its digital machines however it is almost literally true that they are able to tackle any computing problem. A good working rule is that the machine be made to do any job that could be done by a human computer, and will do it in one ten-thousandth of the time. This time estimate is fairly reliable, except in cases where the job is ~~unusually~~ too trivial and straightforward to be worth while giving to the machine.

Some years ago I was researching on what might be described as an investigation of the theoretical possibilities and limitations of digital computing machines. I considered a type of machine which had a central ~~machine~~ mechanism, and an infinite memory which was contained on an infinite tape. This type of machine appeared to be sufficiently general. One of my conclusions was that the idea of a 'rule of thumb' process and a 'machine process' were synonymous. The expression 'machine process' here of course means one which could be carried out by ^{the} type of machine I was considering. It was essential in these theoretical considerations that the memory should be infinite. It can easily be shown that otherwise the machine can only execute ~~finite~~ operations. Machines such as the ACE are ~~very~~ ^{practical} examples of this type of machine. There is at least a very close analogy.

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Digital computing machines all have a central mechanism or control and some very extensive form of memory. The memory does not have to be infinite, but it certainly needs to be very large. In general the movement of the memory as an input to tape is instantaneous - a mechanical machine, because of the large amount of time which is liable to be spent in shifting up and down the tape to reach the point at which a particular piece of information required - the request is stored. Thus a program might easily need a storage of a million entries, and if each entry were equally likely to be the next required the average journey up the tape would be through a million entries, and this would be intolerable. One needs some form of memory with which any required entry can be reached at short notice. This difficulty occurs in need to store the Egyptian hieroglyphs which were written on numerous scrolls. It must have been a very awkward looking up references in them, and the method of arrangement of written matter in books which can be opened at any point is greatly to be preferred. The way that storage of a million entries on scrolls is somewhat impossible. It takes a considerable time to find a given entry. Memory in book form is much more rapid, and is certainly highly suitable when it is to be read by the human eye. We could even imagine a computing machine that was made to work with a memory based on books. It would not be very easy but would be immensely preferable to the infinite machine long ago. Let us for the sake of argument suppose that the difficulties involved in using books as a memory were overcome, that is to say that mechanical devices for finding the right book and opening it at the right page, etc. etc. had been developed, built in the use of human hands and eyes. The information contained in the books would still be rather inaccessible because of the time occupied in the mechanical motions. One cannot turn a page over very quickly without tearing it, and so on. ~~and so on. It is not possible to have a book~~

in so much book transportation, and so it is that the energy involved would be very great. Thus if we moved one book every millisecond and each was moved ten ~~xxxx~~ metres and weighed ~~xxxx~~ ^{100 grams}, and if the kinetic energy were wasted each time we should consume 10^{10} watts, about half the country's power consumption. If we are to have a really fast machine then, we must have our information, or at any rate a part of it, in a more accessible form than can be obtained with books. It seems that this can only be done at the expense of convenience and economy, e.g. ~~xxxxxxxxx~~ by cutting the pages out of the books, and putting each one in to a separate reading mechanism. Some of the methods of storage which are being developed at the present time are not unlike this.

If one wishes to go to the extreme of accessibility in storage mechanisms one is liable to find that ~~xxxxxxxxxxxx~~ it is gained at the price of an intolerable loss of convenience and economy. For instance the most accessible known form of storage is that provided by the valve flip-flop or Jordan Eccles trigger circuit. This enables one to store one digit, capable of two values, and uses two thermionic valves. To store the content of an ordinary novel by such means would cost many millions of pounds. We clearly need some economical method of storage which is more accessible than paper, film etc, but more economical in space and money than the straightforward use of valves. Another desirable feature is that it should be possible to record into the memory from within the computing machine, and this should be possible whether or not the storage already contains something, i.e. the storage should be erasable.

There are

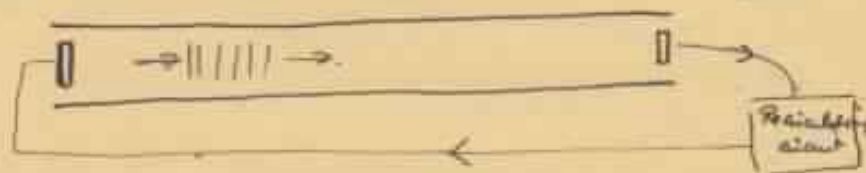
Three main types of storage which have been developed recently and have these properties in greater or lesser degree. Magnetic ~~xxxx~~ wire is very compact, is erasable, and can be recorded on from within the machine, and is moderately accessible. There is storage in the form of charge patterns on the screen of a cathode ray tube. This is probably the ultimate solution. It could be ^{eventually} as accessible as the Jordan Eccles circuit.

4th 1/2

to transport a book every 1111-1111, and

A third possibility is provided by acoustic delay lines. They give greater accessibility than the magnetic wire, though less than the C.R.T type. The accessibility is adequate for most purposes. Their chief advantage is that they are already a going concern. It is intended that the main memory of the ADE shall be provided by acoustic delay lines, consisting of mercury tanks.

The idea of using acoustic delay lines as memory units is due I believe to Robert of Philadelphia University, who was the chief engineer ~~xxxxxx~~ chiefly responsible for the Eniac. The idea is to store the information ~~xxxxxx~~ in the form of compression waves travelling along a column of mercury. Liquids and solids will transmit sound of surprisingly high frequency, and it is quite feasible to put as many as 10¹⁰ pulses into a single 5' tank.



or the information what they represent. A train of pulses may be regarded as stored in the mercury whilst it is travelling through it. If the information is not required when the train emerges it ~~will~~ can be fed back into the column again and again until such time as it is required. This requires a 'recirculating circuit' to read the signal as it emerges from the tank and amplify it and feed it in again. If this were done with a simple amplifier it is clear that the characteristics of both the ~~in~~ tank and the ~~out~~ amplifier would have to be extremely good to permit the signal to pass through even as many as ten times. Actually the recirculating circuit does something slightly different. What it does may perhaps be best expressed in terms of point set topology.

The sparks may be conveyed into the mercury by a pyro. electric
crystal, and also detached at the far end by another
quantity crystal.

Let the plane of the diagram represent the space of all possible signals. I do not of course wish to imply that this is two dimensional. Let the function f be defined for arguments in this signal space and have values in it. In fact let $f(s)$ represent the effect on the signal s when it is passed through the tank and the recirculating mechanism. Then a necessary and sufficient condition that the tank can be used as a storage which will distinguish between N different signals is that ~~there~~ there must be N sets E_1, \dots, E_N such that, if F_r is a set of ~~points~~ ^{points} ~~in~~ E_r

$$f(F_r) \supset f(s) \in E_r$$

~~where~~ F_r is a set of points



It is clearly sufficient for us here only then to ensure that the signals initially fed in belong to one or other of the sets E_r and it will remain in the set after any number of recirculations, without any danger of confusion. It is necessary for suppose s_1, \dots, s_m are signals which can be fed into the machine at any time and read out later without fear of confusion. Suppose that signals distant less than ϵ are liable to be confused. Then for each m, n, r, p $f^r(s_m)$ is distant more than ϵ from $f^p(s_n)$ provided $m \neq n$. We may then take E_m to be the set of points $f^r(s_m)$. These sets ~~will~~ satisfy (a) and are distant ϵ at least apart.

Let E_r be the set of signals which could be obtained from s_r by successive applications of f and shifts of distance not more than ϵ . Then the set E_r is a set, one that is infinite, and by applying a shift of distance ϵ or less to $f(E_r)$ we obtain

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We assume however that owing to the small quantity of
material any loss to give any part within a week of receipt of
4/6)

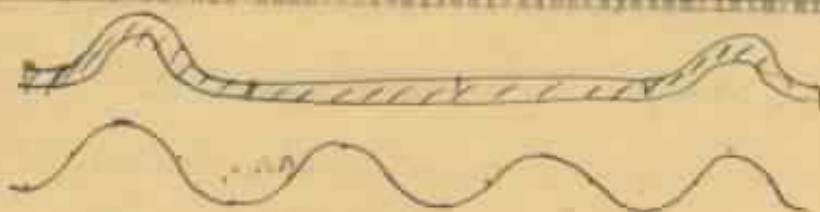
(Sd)

In the case of a mercury delay line used for $N = 16$ the set would consist of all continuous signals within the shaded area.



One of the sets would consist of all continuous signals lying in the region below. It would represent the signal 1001.

~~For order to put such a recirculation system into effect it~~



In order to put such a recirculation system into effect it is essential that a clock signal be supplied to the memory system so that it will be able to distinguish the times when a pulse if any should be present. It would for instance be natural to supply a timing sine wave as shown above to the recirculator.

P.T.O.

The importance of a clock to the ~~recirculation~~ ^{recirculation} process ^{in delay lines} can be illustrated by an interesting little theorem. Suppose that instead of the condition $f \in E, \sup |f(s) - 0| < \epsilon$ we impose a stronger one, viz $f(s) \rightarrow c$ if $s \in E$, i.e. there are ideal forms of the distinguishable signals, and each admissible signal converges towards the ideal form after recirculating. Then we can show that ~~that~~ unless there is a clock the ideal signals are all constants. For let U_α represent a shift of origin, i.e. $U_\alpha s(t) = s(t + \alpha)$. Then since there is no clock the properties of the recirculator are the same at all times and f therefore commutes with U_α at limit. Then $f U_\alpha(c_r) = U_\alpha f(c_r) = U_\alpha c_r$ for $f(c_r) = c_r$ since c_r is an ideal signal. But this means that $U_\alpha(c_r)$ is an ideal signal, and therefore for sufficiently small α must

The idea of a process of with the properties we
 have described is every common one in connection with
 strange devices. It is known as 'regression' of strange
 It is always present in some form, but sometimes
 the regression is ^{c. i. u. n. e.} naturally ^{occurring} and ~~does not need to be~~
 no precaution have to be taken. In other cases
~~it is~~ ^{to require care in process} special precaution have to be taken ^{or else}
 the regression will fade.

be c , since the ideal signals are discrete. Then for any β and sufficiently large n , β/n will be sufficiently small and $U_{\beta/n}(c) = c$. But then by iteration $U_{\beta/n}^*(c) = U_{\beta/n}(c) = c$. i.e. $c(t+\beta) = c(t)$. This means that the ideal signal c is a constant.

We might say that the clock enables us to introduce a discreteness into time, so that time can be regarded as a succession of instants instead of as a continuous flow. A digital machine must essentially deal with discrete objects, and in the case of the ACE this is made possible by the use of a clock. All other digital computing machines that I know of do the same. One can think up ways of avoiding it, but they are very awkward. I should mention that the use of the clock in the ACE is not confined to the realisation of the program, but is used in almost every part.

It may be as well to mention some figures connected with the mercury delay line as we shall use it. We shall use five foot tubes, with a diameter of half an inch. Each of these will enable us to store 10^4 binary digits. The unit I have used here to describe storage capacity is self-explanatory. A unit of storage capacity has a capacity of a binary digit if it can remember any sequence of a digit each being a 0 or a 1. The storage capacity is also the logarithm to the base 2 of the number of different signals which can be remembered, i.e. $\log_2 N$. The digits will be placed at a time interval of one microsecond, so that the time taken for the waves to travel down the tube is just over a millisecond. The velocity is about one and a half kilometres per second. The delay in writing for a given piece of information is about half a millisecond. In practice this is reduced to an effective 250 us.

The full storage capacity of the AGC available on Hg delay lines will be about 200,000 binary digits. This is probably comparable with the memory capacity of a minnow.

I have spent a considerable time in this lecture on this question of memory, because I believe that the provision of proper storage is the key to the problem of the digital computer, and certainly if there are to be persuaded to show any sort of genuine intelligence much larger capacities than are yet available must be provided. In my opinion this problem of making memory available at reasonably short notice is much more important than that of doing over it as much as multiplication at high speed. Speed is necessary if the machine is to work fast enough for the machine to be commercially valuable, but a large storage capacity is necessary if it is to be capable of anything more than rather trivial operations. The storage capacity is therefore the more fundamental requirement.

theoretical

Let us now return to the analogy of the computing machine with an infinite tape. It can be shown that a single special machine of that type can be made to do the work of all. It could in fact be made to work as a model of any other machine.

is

The special machine may be called the universal machine; it works in the following quite simple manner. When we have decided what machine we wish to imitate we write a description of it on the tape of the universal machine. This description is written in a code which we call its own machine code. In which it might find itself. The universal machine has only to keep looking at this description in order to find out what it should do at each stage. Thus the complexity of the machine to be imitated is concentrated in the tape and does not appear in the universal machine proper in any way.

If we take the properties of the universal machine in combination with the fact that the machine processes and acts on thought processes are autonomous we may say that the universal machine is an autonomous machine which can be made to imitate any other machine.

instructions, and he goes to the rule of thumb process. This feature is essential to all digital computing machines such as the ACE. They are in fact universal versions of the universal machine. There is a sort of central pool of electronic equipment, and a large memory. When any particular problem has to be handled the appropriate instructions for the computing process involved are stored in the memory of the ACE and it is then set up for carrying out that process.

I have now indicated the main strategic ideas behind digital computing machinery, and will now follow it up with the very briefest description of the ACE. It will be divided for the sake of argument into the following parts:

Memory
Control
Arithmetic part
Input and Output

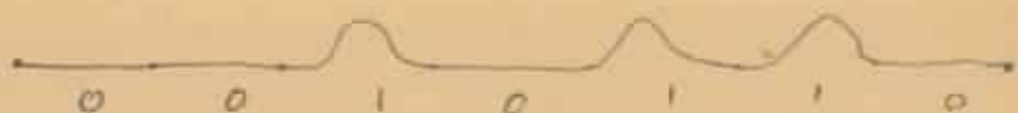
I have already said enough about the memory and will only repeat that in the ACE the memory will consist mainly of mercury. 200 delay lines each holding 1024 binary digits. The purpose of the control is to take the right instructions from the memory, and then it they mean, and arrange for them to be carried out. It is understood that a sort of code is assigned to each 'word' or 'instruction' which has been laid down, whereby ~~various~~ combinations of any 20 binary digits ~~are described~~ ^{are defined} over time. The circuit of the control is made in accordance with the code, so that the right effect is produced. To a large extent we have also allowed the circuit to determine the code, i.e. we have not just thought up the code 'best code' and then found a circuit to put it into effect, but have often ~~taken~~ simplified the circuit as the demands of the code. It is also quite difficult to think about the code entirely in abstracto without any kind of circuit.

The arithmetic part of the machine is the part concerned with addition, multiplication and the other operations which it seems worthwhile to do by means of special circuitry rather than through the simple facilities provided by the control. The distinction between control and arithmetic part is a rather hazy one, but at any rate it is clear that the machine should at least have an adder and a multiplier, even if they turn out in the end to be part of the control. ~~Furthermore, it is necessary to~~ This is a point at which I should mention that ~~the machine~~ ~~the machine~~ ~~is over the~~ ~~machine~~ in the binary scale, ~~even with two multipliers.~~ Inputs from externally provided data are in decimal, and so are outputs intended for human eyes rather than for later recalculation by the ACE. This is the first qualification. The second is that, in spite of the intention of binary working there can be no bar on decimal working of a kind, because of the relation of the ACE to the universal machine. Binary working is the most natural thing to do with any large scale computer. It is much easier to work in the scale of two than any other, because it is so easy to produce mechanisms which have two positions of stability: the two positions may then be regarded as representing 0 and 1. Examples are given as diagrams. Jordan-Kelly circuit, 1947, page



if one is concerned with a small scale calculating machine (or there is at least one serious objection to binary working.

For practical use it will be necessary to build a converter to transform numbers from the binary form to the decimal and back. This may well be a larger undertaking than the binary calculator. With the large scale machines this amount of extra weight. In the first place a converter would become a relatively small piece of apparatus, and in the second it would not really be necessary. This last statement sounds quite paradoxical, but it is a simple consequence of the fact that these machines can be made to do any rule of thumb process by remembering suitable instructions. In a machine it can be made to do binary-decimal conversion, by the use of the AND the provision of the converter involved no more than adding two extra delay lines to the memory. This situation is very typical of what happens with the AEC. There are very many little details which have to be taken care of, and which, according to normal engineering practice would require special circuits. We are able to deal with these points without modification of the machine itself, by using extra words, occasionally resulting in feeding in appropriate instructions.

[illegible]

Let us now look at what the process of binary addition is like. In ordinary decimal addition we always begin from the right, and the same naturally applies to binary. We have to do this because we cannot tell whether to carry unless we have already dealt with the less significant columns. The same applies with electronic addition, and therefore it is convenient to use the convention that if a sequence of pulses is coming down a line, then the least significant pulse always comes first. This has the unfortunate result that we must either write the least significant digit on the left in our binary numbers or else make time flow from right to left in our diagrams. As the latter alternative would involve writing from right to left as well as adding in that way, we have decided to put the least significant bit on the left. Now let us do a typical addition. Let us write the summands and the addends.

$$\begin{array}{r}
 \text{Carry} \\
 A \quad 0 \ 1 \ 1 \ 0 \ 1 \ 1 \ 0 \ 0 \ 1 \ 0 \ 1 \text{ ---} \\
 B \quad 0 \ 1 \ 1 \ 1 \ 0 \ 1 \ 0 \ 0 \ 1 \ 1 \text{ ---} \\
 \hline
 0 \ 1 \ 0 \ 0 \ 1 \ 1 \ 0 \ 0 \ 0
 \end{array}$$

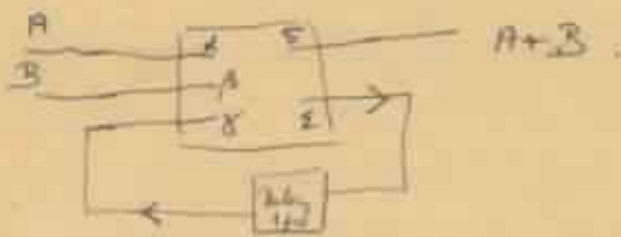
Note that I can do the addition only looking at a small part of the data. To do the addition electronically we need to produce a circuit with three inputs and two outputs.

| Inputs | | Outputs | |
|------------------------|-----|---------|-----|
| Addend A | x | Sum | S |
| Addend B | y | Carry | E |
| Carry from last column | z | | |

This circuit must be such that

| | | | | | | |
|-------------------------------|---|---|----------|---|-------|---|
| if no. of its on inputs is | { | 0 | Then sum | 0 | and | 0 |
| | | 1 | is | 1 | carry | 0 |
| | | 2 | | 0 | is | 1 |
| | | 3 | | 1 | is | 1 |

It is very easy to produce a voltage proportional to the number of pulses on the inputs, and one then merely has to provide a circuit which will discriminate between four different levels and put out the appropriate sum and carry digits. I will not attempt to describe such a circuit; it can be quite simple. When we are given the circuit we merely have to connect it up with feedback and it is an adder. Thus:



It will be seen that we have made use of the fact that the step process is used in addition with each digit, and also the fact that the properties of the electrical circuit are invariant under time shifts, at any rate if these are multiples of the clock period. It might be said that we have made use of the isomorphism between the group of time shifts and the multiplicative group of real numbers to simplify our construction, though I doubt if any other applications of this principle could be found.

It will be seen that with such an adder the addition is broken down into the most elementary steps possible, such as adding one and one. Each of these operations is a microsecond, our numbers will normally consist of 32 binary digits, so that two of them can be added in 50 microseconds. Likewise we shall do multiplications in the form of a number of consecutive additions of one and one or one and zero etc.

or thereabouts.
There are 1024 such additions to be done in a multiplication of one 32 digit number by another, so that one might expect a multiplication to take about a millisecond. Actually the multiplier to be used on ACE will take rather over two milliseconds. This may sound rather long, when the unit operation is only a microsecond, but it actually seems that the machine is fairly well balanced in this respect, i.e. the multiplication time is not a really serious bottleneck.

Feature 2 Computers always spend just as long in writing numbers down and deciding what to do next as they do in actual multiplications, and it is just the same with the ACE. A great deal of time is spent in getting numbers in and out of storage and deciding what to do next. To complete the four elementary processes, subtraction is done by complementation and addition, and division is done by the use of the iteration formula

$$u_n = u_{n-1} + u_{n-1}(1 - au_{n-1})$$

which converges to a^{-1} provided $|1 - au_0| < 1$. The error is squared at each step, so that the convergence is very rapid. This process is of course programmed, i.e. the only extra operation required is the delay line required for storing the relevant instructions.

Leaving on from the arithmetic part there remains the input and output. For this purpose we have chosen Hollerith card equipment. We are able to obtain this without having to do any special development work. The speeds obtainable are not very impressive compared with the speeds at which the electronic equipment works, but they are quite sufficient for all cases where the calculation is long and the result concise: the interesting cases in fact.

It might be said that there would be a difficulty in converting the information provided at the slow speeds necessary to the Hollerith equipment to the high speeds required with the AEC, but it is really quite easy. The Hollerith speeds are for many purposes so slow as to be counted zero or stop, and the problem reduces to the simple one of converting a six number of statically given digits into a stream of pulses. This can be done by means of a form of electronic accumulator.

16a and
16b.

Now let us give a picture of the general use of the machine.
Let us begin with some problem which has been brought in
by a customer. It will first go to the problem prescription
section where it is arranged to see whether it is suitable
form and self-consistent, and - very rough checking procedure
made out, then goes to the solution prescription section. For
let us suppose for example that the problem was to find
tabulate solutions of the equation

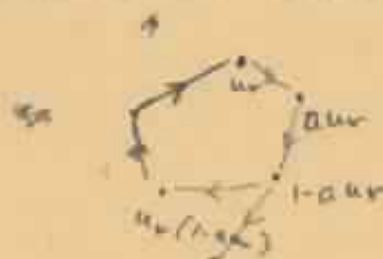
$$y'' + xy' = \sqrt{x} \quad (*)$$

with initial conditions $x=y=0, y'=a$. This would be regarded as an exercise in solving the equation

$$y'' = F(x, y, y')$$

for which one would have instructions & also "look-up" arranged.
One would need also a table to compute the function $F(x,y,z)$
(in this case $F(x,y,z) = \bar{J}_0(r) - xz$) which
would mainly involve a table to produce $\bar{J}_0(r)$, and this
one might expect to get off the shelf. A few additional
details about the boundary conditions and the maximum
digital length of the ord would have to be dealt with, but
much of this detail would be found on the shelf, say like
the table for obtaining $\hat{\bar{J}}_0(r)$. The instructions for the
job would therefore consist of a considerable number taken
off the shelf together with a few made up specially for the
job in question.

Before leaving the outline of the description of the machine I should mention ~~two~~ ~~particular~~ ~~some~~ of the practical situations that are met with in programming. ~~Examples~~ ~~like~~ ~~of~~ ~~the~~ ~~following~~ ~~kind~~ ~~are~~ ~~illustrated~~ ~~by~~ ~~the~~ ~~examples~~ ~~of~~ ~~the~~ ~~following~~ ~~kind~~ I can illustrate two of them in connection with the ~~the~~ calculation of the residues I described above. One of them is the idea of the iterative cycle. Each time that we go from u_r to u_{r+1} , we apply the same sequence of operations, and it will therefore be absolutely the same if we use the same instructions. Thus we go round a round - cycle of instructions: -



It looks however as if we were in a case of getting stuck in this cycle, and unable to get out. This the solution of this difficulty involves another technical idea that of 'discrimination' deciding when to do next 'mostly' i.e. of ~~making discrimination~~ according to the results of that the machine itself, instead of according to data available to the programmer. In this case we include a discrimination in each cycle, which takes us out of the cycle when the value of $|1 - a_4|$ is sufficiently small. It is like an oscillation over a hysteresis, and taking permission to lead after each cycle. This is a very simple idea, but is of the utmost importance. The idea of the iterative cycle of two functions will also have been seen to be rather fundamental when it is realized that the majority of the instructions in the machine must be obeyed a great number of times. If now the whole memory were occupied by instructions, none of it being used for numbers or other data, and if each instruction were obeyed once only, but took the longest possible time, the machine could give answers for only a few cases.

Another important idea is that of construction and then obeying it. This can be used amongst other things for discrimination. In the example ~~which~~ ^{I have just taken} for instance we could ~~calculate a quantity which was~~ ^{if} ~~if~~ $|1 - a_2|$ was less than $\epsilon/31$ and ~~otherwise~~. By adding this quantity to the instruction that is obeyed at the following point the instruction can be completely altered in its effect when finally $|1 - a_2|$ is reduced to sufficiently small dimensions.

Probably the most important idea involved in the instruction table is that of ^{standard} subsidiary tables. ~~Various~~ Certain processes are used repeatedly in all sorts of different connections, and we wish to use the same instructions, from the same part of the memory every time. Thus we may use interpolation for the calculation of a great number of different functions, but we shall always use the same ~~interpolation~~ instruction table for interpolation. We have only to think out how this is to be done once, and forget that how it is done. Each time we want to do an interpolation we have only to remember the memory address where this table is kept, and make the appropriate reference in the instruction table which is using the interpolation. We might be ~~instruction~~ if for instance ~~we~~ ^{we} ~~were~~ ^{were} asked to calculate for fixed values of $J_0(x)$ and use the interpolation table in this way. We should then say that the interpolation table was a subsidiary to the table for calculating $J_0(x)$. There is thus a sort of hierarchy of tables. ~~The~~ The interpolation table might be regarded as taking its orders from the J_0 table, and reporting its answers back to it. The current analogy is however not a very good one, as there are many more masters than servants, and many masters have to share the same servants.

Return to
p. 16.

these had all been assembled and checked they would be taken to the input mechanism, which is simply a Hollerith card reader. They would be put into the card holder and a button pressed to start the cards moving through. It must be remembered that initially there are no instructions in the machine, and once normal facilities are therefore not available, the first few cards that pass in have therefore to be carefully thought out to deal with this situation. When are the initial input cards and are always the same. When they have passed in a set of initial instruction tables will have been set out in the machine, including sufficient to see if the machine carried the essential work of cards that have been prepared for the job we are doing. When this has been done there are various possibilities as to what happens next. Depending on the way the job has been programmed, the machine may have been made to might go straight on through, and carry out the job, punching or printing all the answers required, and stopping when all of this has been done. But more probably it will have been arranged that the machine stops as soon as the instruction tables have been set in. This allows for the possibility of checking the content of the memories is correct, and for a number of variations of procedure. It is clearly a suitable means for a break. We might also make a number of other breaks. For instance ~~then~~ we might be interested in certain particular values of the parameter a , ~~values~~ which were experimentally obtained figures, and it would then be convenient to pause after each parameter value, and feed the next parameter value in from another card. Or one might prefer to have the cards all ready in the holder and let the machine take them in as it wanted them. One can do as one wishes, but one must make up one's mind. Each time the machine ceases in

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this way a "word" or sequence of 25 binary digits is
displayed on each bulb. This word indicates the reason
for stopping. I have already mentioned two possible reasons.
~~Furthermore~~ A large class of further possible reasons is
provided by the checks. ~~Furthermore~~ The program is
done in such a way that the AGE is frequently investigated
identities which should be satisfied if all is as it should be.
Whenever one of these checks fails the machine stops and
displays a word which describes what check has failed.

It will be seen that the possibilities as to what goes
wrong are immense. Use of our diffinition will be the
maintenance of an appropriate discipline, so that we do
not lose track of what we are doing. We shall need a number of
efficient librarian types to keep us in order.

need not always be explicit, i.e. one need not know that in such a form that we can tell, before the circuit starts, and using only pencil and paper, how big the error will be. The error calculation may be a serious part of the ADB's duties. To an extent it may be possible to replace the estimator of error by statistical estimates obtained by repeating the job, ^{several times} and doing the rounding off differently each time, controlling it by some random element, some electronic roulette wheel. Such statistical estimates are however less much in doubt, are useful in ^{machine} form, and give no indication of what can be done if it turns out that the errors are intolerably large. The statistical method can only help the analyst, not replace him.

Analysis is just one of the purposes for which we shall need good machines. Roughly speaking there are two in connection with the ADB will be divided into its masters and its servants. The masters will be the instructions which for it, thinking up design and design work of writing it. Its servants will feed it with cards as it calls for them. They will put right any parts that go wrong. They will assemble data that it requires. In fact the servants will take the place of links. As time goes on the calculator itself will ~~not~~ take over the functions both of masters and of servants. The servants will be replaced by much smaller and electrical links and hence more so. On night for instance provide ~~continuous~~ ^{continuous} curves followers to enable data to be taken direct from curves instead of having to be read off values and much slower speed. The masters are likely to get replaced because as soon as any technique becomes available it is introduced it becomes possible to devise a system of instruction tables which will enable the electronic machines to do it for itself. It may happen however that the masters will refuse to do this. They may be unwilling to let their jobs be stolen from them in this way. In that case they would surround the whole of their work with mystery and

make anyone, laughed in well known ribaldry, whenever
any American machine was made. I think that a reaction
of this kind is a very real danger. This is a priority
issue in principle
leads to the question with as to how far it is possible for
a machine to simulate human activities. I will
return to this later, when I have discussed the effects of
these machines on mathematics a little further.

I expect that digital computing machines will eventually stimulate a considerable interest in symbolic logic and mathematical philosophy. The language in which one communicates with these machines, i.e. the language of instruction tables, forms a sort of symbolic logic. The machine interprets whatever is told it in a quite definite manner without any sense of humor or sense of proportion. Unless in communication with it one says exactly what one means, trouble is bound to result. Ideally one could communicate with these machines in any language provided it was an exact language, i.e. in principle one should be able to communicate in any symbolic logic, provided that the machines were given instruction tables which would enable it to interpret that logical system. This should mean that there will be much more practical sense for logical systems than there has been in the past. As regards mathematical philosophy, since the machines will be doing more and more mathematics themselves, the ~~human~~ interpretative nature of activity of the human intellect will be driven further and further into the philosophical questions of what can in principle be done etc.

21xJm

Some attempts will probably be made to get the machines to
do actual manipulations of mathematical formulae. ^{To do so} ~~these~~ will
require the development of a special logical system for the
purpose. This system should resemble normal mathematical
procedure as closely as possible, but at the
same time should be as unambiguous as possible.

It has been said that computing machines can only carry out the processes that they are instructed to do. This is certainly true in the sense that if they do something other than what they were instructed then they have just made some mistake. It is also true that ~~the instruction~~ ~~the instruction~~ the instruction to constructing these machines in the first instance is to treat them as slaves, giving them only jobs which have been thought out in detail. The user of the machine fully understands what is going on at all the time. The first of the modern machines have only been made in this way. But is it necessary that they should always be used in such a manner? ~~For instance, one might~~ ^{let us suppose we have} set up a machine with certain initial instruction tables, we constructed that these tables might on occasion, if some serious error, modify those tables. One can imagine that after the machine had been operating for some time, the instructions would have altered out of all recognition, but nevertheless still be such that one would have to admit that the machine was still doing some worthwhile calculations. For this it might still be possible to construct a machine designed when the machine was first set up, but in a much more efficient manner. In such a case one would have to admit that ~~far~~ the progress of the machine had not been forgotten when its original instructions were put in. It would be like a pupil who had learnt much from his master, but had added much more by his own work. When this happens I feel that one is obliged to regard the machine as showing intelligence. ~~For instance, one might~~ ^{if one can} provide a reasonably large memory capacity it should be possible to begin to experiment on these lines. The memory capacity of the human brain is probably of the order of ten thousand million ^{binary} digits. But most of this is probably used in remembering visual impressions, and other comparatively useless work. One might reasonably hope to be able to make some use of progress with a few million digits, especially if one confined one's investigations to some rather

limited field such as the game of chess. I would probably be quite easy to find instructions which would enable the machine to win against an even an player. Indeed Shannon of Bell Telephone Laboratories tells me that he has won some playing by rule of thumb: the skill of his opponent is not tested. But I would not consider such a victory very significant. What we need is a machine that can learn from experience. The real utility of letting the machine play the game instructions provides the machine for this, ~~that~~ but this of course does not get us very far.

It might be argued that there is a fundamental contradiction in the idea of a machine with intelligence. It is certainly true that 'looking like a machine', has become synonymous with lack of adaptability. But ~~this is~~ the reason for this is obvious. Machines in the past have had very little store, and there has been no question of the machine having any direction. The argument might however be put into a more expressive form. 'It has for instance been shown that with certain logical systems there ~~cannot~~ can be no machine which will distinguish provable formulae of the system from unprovable, i.e. that there is no test that the machine can apply which will divide propositions with certainty into these two classes. Thus if ~~the~~ machine is made for this purpose it must in some way fail to give an answer. On the other hand if a mathematician is confronted with such a problem he would search around & find new methods of proof, so that he might eventually be able to reach a decision about any given formula. This would be the argument. Against it I would say that fair play must be given to the machine. Instead of it sometimes giving no answer we could arrange that it gives occasional wrong answers. But the human mathematician would likewise make blunders when trying out new techniques. ~~But~~ It is easy for an intelligent man to make blunders as well as mistakes and give him another chance, but the machine would be allowed no mercy. In other words then, if a machine is expected to

be infallible, it must also be intelligent. There are several mathematical theorems which say almost exactly that. But these theorems say nothing about how much intelligence may be displayed if a machine makes no pretence of infallibility. To continue the way also for 'fair play for when testing their [the machines]'. A human mathematician ~~must~~ has always undergone an extensive training. This training may be regarded as not unlike putting information tables into a machine. One must therefore not expect a machine to do a very great deal of building up of information tables on its own. It can do very much in the body of knowledge, why should we expect more of a machine? Putting the same point differently, the machine must be allowed to have contact with human beings in order that it may adapt itself to their standards. The way of doing this may perhaps be rather difficult for this purpose, as the work of the machine must be ~~will~~ automatically provide this contact.