

COV-ELM classifier: An Extreme Learning Machine based identification of COVID-19 using Chest X-Ray Images

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Abstract

Coronaviruses constitute a family of virus that gives rise to respiratory diseases. Coronavirus disease 2019 (COVID-19) is an infectious disease caused by a newly discovered coronavirus also termed as Severe acute respiratory syndrome coronavirus 2 (SARS-CoV-2). Due to its rapid spread, WHO has declared COVID-19 outbreak a pandemic on 11th March 2020. Reverse transcription-polymerase chain reaction (RT-PCR) test is popularly used worldwide for the detection of COVID-19. However, due to the high false-negative rate of RT-PCR test, chest X-ray (CXR) imaging is emerging as a feasible alternative for the detection of COVID-19. In this work, we propose a multiclass classification model COV-ELM, based on the extreme learning machine which classifies the CXR images into one of the three classes, namely COVID-19, normal, and pneumonia. The choice of ELM in this work has been motivated by its significantly short training time as compared to conventional gradient-based learning algorithms. After some preprocessing, we extract a pool of features based on texture and frequency. This pool of features serves as an input to the ELM and a 10-fold cross-validation method is employed to evaluate the proposed model. For experimentation, we use chest X-ray (CXR) images from three publicly available sources. The results of applying COV-ELM on test data are quite promising. The COV-ELM achieved a macro average F1-score of 0.95 and the overall sensitivity of 0.94 ± 0.02 at 95% confidence interval. When compared to state-of-the-art machine learning algorithms, the COV-ELM is found to outperform in a three-class classification scenario. The main advantage of COV-ELM is that its training time being quite low, as bigger and diverse datasets become available, it can be quickly retrained as compared to its gradient-based competitor models.

Keywords: COVID-19, Extreme Learning Machine, chest X-rays, Pneumonia viral, Pneumonia bacterial.

1. Introduction

Coronavirus disease 2019 (COVID-19), known to originate from Wuhan City in Hubei Province, China is a contagious infection resulting in respiratory illness in most cases. COVID-19 is caused by a novel coronavirus, widely recognized as severe acute respiratory syndrome coronavirus 2 (SARS-CoV-2; previously known as

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2019-nCoV) [1]. As COVID-19 outbreak has become a global health emergency, on March 11, 2020, the WHO declared COVID-19 a global pandemic [2].

The Reverse transcription-polymerase chain reaction (RT-PCR) test has been used popularly for detection of SARS-CoV-2. Although COVID-19 may be asymptomatic in several instances, it has been reported that even many symptomatic cases showing characteristics of COVID-19 were not diagnosed by RT-PCR test [3]. Thus, due to the high false-negative rate of RT-PCR test which may be up to 67% in early days of contracting the infection, it has to be supplemented with other means of monitoring the clinical features of a subject. This limitation associated with RT-PCR test is shifting the research focus on the analysis of Chest X-ray images. Chest X-ray is the most common method of examining common respiratory and lung infections for fast and cost-effective diagnosis [4, 5]. Though several research groups are working in this direction [6, 7, 8, 9], they are struggling with the challenge to distinguish COVID-19 patients against those suffering from other forms of pneumonia [10]. In this paper, the Extreme Learning Machine (ELM) classifier is preferred over conventional gradient-based learning algorithms due to its faster convergence with the least number of tunable parameters involved in the network.

Several research groups have recently applied some well known deep neural networks like AlexNet (also known as 'ImageNet') [11], VGGNet [12], GoogLeNet [13], ResNet [14], and the variations of these networks for the classification of COVID-19 on chest X-ray images [7, 8, 9]. ImageNet has 60 million parameters and 650,000 neurons, trained through the dataset of 1.2 million images, which took almost a week on two NVIDIA GTX 580 3GB GPUs [11]. VGGNet has 144 million parameters and greater depth compared to ImageNet but it converges in fewer epochs due to regularization, smaller filter sizes, and pre-initialization of certain layers [12]. GoogLeNet [13] utilizes a 22- layer deep network for 1.2 million images in training set, 50,000 in validation set, and 100,000 images in testing set. ResNet trained 23 million parameters to achieve good generalization performance on CIFAR-10 dataset [15] using 50 thousand images for training and another 10 thousand for testing [14].

Khan et al. [7] proposed a deep convolutional neural network (DCNN) model to automate the detection of COVID-19 based on chest X-ray images. The model is based on Xception architecture [16] pre-trained on ImageNet [11] and achieved an overall accuracy of 89.6%. Mahmud et al. [8] proposed a DCNN model using a variation in dilation rate to extract distinguishing features from chest X-ray images and achieved an accuracy of 90.2% for multi-class classification (COVID-19/Normal/Pneumonia). They also used Gradient-weighted Class Activation Mapping (Grad-CAM) to visualize the abnormal regions in CXR scans. Wang et al. [9] developed a computer-aided screening tool for detection of COVID-19 from CXR images based on an already-trained network on ImageNet, tuned with the Adam optimizer, and achieved 91% sensitivity for the COVID-19 class. Basu et al. [17] used domain extension transfer learning (DETL) framework comprising 12 layers. They used an already trained network on National Institutes of Health (NIH) CXR image dataset [4] (comprising 108,948 frontal view X-ray images of 32,717 unique patients) which was fine-tuned for COVID-19 dataset to obtain an overall accuracy $95.3\% \pm 0.02$ on 5-fold cross-validation. Rajaraman et al. [18] iteratively

pruned the task-specific models (VGG-16, VGG-19, and Inception-V3) by pruning 2% of the neurons in each convolutional layer and retrained the model to obtain a macro averaged F1-score of 0.99.

Khuzani et al. [10] used multilayer neural networks (MLNN) to distinguish the CXR images of COVID-19 patients from other forms of pneumonia. They extracted a set of spatial and frequency domain features from X-ray images. Based on the evaluation of extracted features, they concluded that the while Fast Fourier Transform (FFT) features were best suited in detecting the COVID-19, the normal class was best determined by gray level difference method (GLDM). Principal Component Analysis (PCA) was applied to generate an optimized set of synthetic features that served as input to an MLNN to distinguish COVID-19 images from the non-COVID-19 ones with an accuracy of 94% .

It is evident from the above discussion that so far the research groups have mainly focused on the use of deep neural networks which require millions of parameters and the optimal choice of hyper-parameters. However, it is well known that the training of a deep neural network is a time-consuming task even on high-performance computing platforms. Therefore, in order to improve the computational efficiency of the classification models, in this work we have proposed the use of a single hidden layer feed-forward neural network (SLFN) known as extreme learning machine (ELM) [19, 20]. The ELM is a batch learning algorithm proposed by Huang et al. [19] and has been used extensively in different domains like ECG signal classification [21] and identification of arrhythmia disease [22]. The ELM and its variants have also been applied in applications such as fingerprint identification [23], lung cancer detection [24], image and video watermarking [25, 26], and 3D object recognition [27]. The applicability of ELM in various domains is due to its fast learning, good generalization performance, and ease of implementation. The main contribution of this paper is to explore successfully the feasibility of applying ELM in the diagnosis of COVID-19 using CXR images. The rest of the paper is organized as follows: section 2 presents a review of ELM, section 3 gives the dataset description followed by the detailed methodology, outcomes of the experiments and analysis of the results have been discussed in section 4, finally, the conclusions and scope of future work are discussed in section 5.

2. Extreme Learning Machine

Extreme Learning Machine (ELM) was proposed by Huang et al. as an efficient alternative to the backpropagation algorithm for single-layer feed-forward networks (SNFN) [19]. It is a fast learning algorithm with good generalization performance as compared to other traditional feed-forward networks. An ELM works by initializing a set of weights randomly and computing the output weights analytically by Moore Penrose Matrix Inverse [28].

Fig. 1 depicts the overall ELM architecture and the details of its functioning are provided in algorithm 1. Given a training set $(x_j, t_j), x_j \in \mathbf{R}^n, t_j \in \mathbf{R}^m$ for $j = 1, 2, \dots, N$, where the pairs (x_j, t_j) denote the training vectors and the corresponding target values, following [19], the standard ELM having L nodes is modeled as:

$$\sum_{i=1}^L \beta_i g_i(a_i \cdot x_j + b_i) = t_j \quad (1)$$

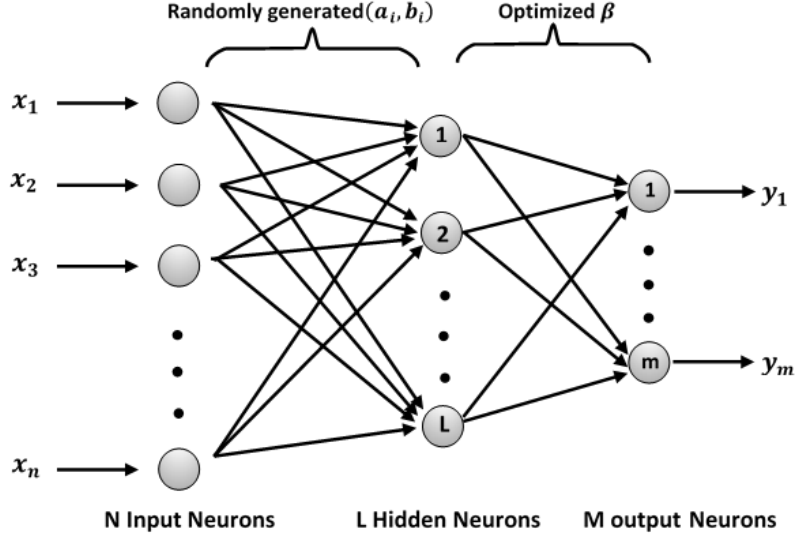


Figure 1: ELM Architecture: The ELM network comprises an input layer, a hidden layer, and an output layer

In Equation 1, a_i denotes the weight vector that connects the input layer to the i^{th} hidden node and b_i denotes the corresponding bias. Further, β_i denotes the weight vector connecting the i^{th} hidden node and the output neurons. The above N equations may also be represented as:

$$G\beta = T \quad (2)$$

The form of the hidden layer output matrix G , mentioned in Equation 2, is given in Equation 3. The form of vectors β and T is given in equation 4.

$$G = \begin{bmatrix} g(a_1.x_1 + b_1) & \dots & g(a_L.x_1 + b_L) \\ \vdots & \dots & \vdots \\ g(a_1.x_N + b_1) & \dots & g(a_L.x_N + b_L) \end{bmatrix}_{N \times L} \quad (3)$$

$$\beta = \begin{bmatrix} \beta_1^T \\ \vdots \\ \beta_L^T \end{bmatrix}_{L \times m} \quad \text{and} \quad T = \begin{bmatrix} t_1^T \\ \vdots \\ t_N^T \end{bmatrix}_{N \times m} \quad (4)$$

The solution of the above system of linear equations is obtained using Moore-Penrose generalized inverse (Equation 5).

$$\beta = G^\dagger T \quad (5)$$

In Equation 5, $G^\dagger = (G^T G)^{-1} G^T$ denotes the Moore-Penrose generalized inverse [28] of matrix G .

Algorithm 1 ELM Algorithm

Input:

Training set: $(x_j, t_j), x_j \in \mathbf{R}^n, t_j \in \mathbf{R}^m$ for $j = 1, 2, \dots, N$

Activation function: $g: \mathbf{R} \rightarrow \mathbf{R}$

Number of hidden nodes: L

Output:

Optimized weight matrix: β

1. Randomly assign hidden node parameters $(a_i, b_i), i = 1, 2, \dots, L$;
 2. Compute the hidden-layer output matrix G ;
 3. Compute output weight vector $\beta = G^\dagger T$
-

Huang et al. [29] argue that ELM outperforms the conventional learning algorithms in terms of learning speed, and in most of the cases shows better generalization capability than the conventional gradient-based learning algorithms such as backpropagation where the weights are adjusted with a non-linear relationship between the input and the output [28]. They further stated that ELM can compute the desired weights of the network in a single step in comparison to classical methods.

3. Material and Methods

In this section, we present a list of CXR image datasets used for experimentation in this work, followed by details of the proposed methodology.

3.1. Dataset Description

In the present work, we have used the following publicly available CXR datasets for COVID-19, Normal, and Pneumonia.

- COVID-19 Image Data Collection [6]. It comprises 760 samples, COVID-19: 538, ARDS: 14, Other Diseases: 222.
- COVID-19 Radiography Database (Kaggle) [30]. It comprises 2905 samples, COVID-19: 219, Normal: 1341, Viral Pneumonia: 1345.
- Mendeley Chest X-ray Images [31]. It comprises 5856 samples, Pneumonia (Viral and Bacterial) : 4273, Normal:1583.

In this work, we only consider the CXR images in a frontal view, namely Poster anterior (PA) and Erect anteroposterior (AP). The first two databases in the above list comprise 520 such images. For the training purpose, we have used these images alongwith 520 CXR images of normal and pneumonia cases from COVID-19 Radiography Database (Kaggle) [30] and Mendeley Chest X-ray Images [31].

3.2. Preprocessing

Due to diversity in the CXR image collection, they are resized and subjected to min-max normalization [32] to ensure uniformity. Further, to enhance the local contrast in the CXRs, Contrast Limited Adaptive Histogram Equalization (CLAHE), a variant of adaptive histogram equalization is applied. Fig. 2 depicts the preprocessing steps for the CXR image dataset, which includes resizing, normalization, and CLAHE [33] applied in sequence.

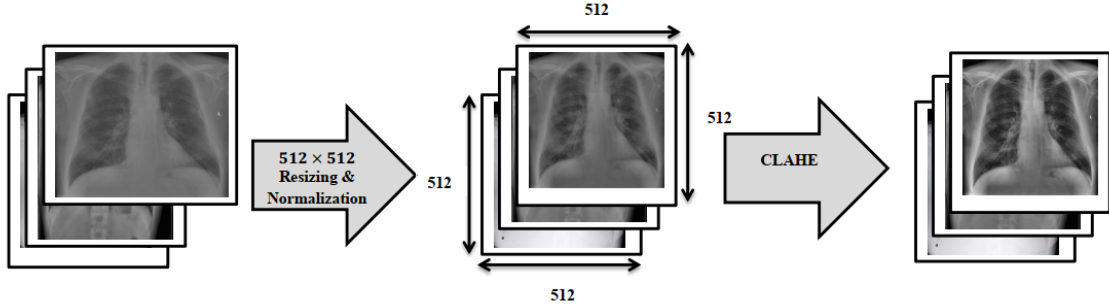


Figure 2: Preprocessing: Image Resizing, Normalization, and Contrast Limited Adaptive Histogram Equalization (CLAHE).

3.3. Feature Extraction

Texture plays a significant role in classifying images or identifying the region of interest (ROI) in an image [34]. In this work, we consider four groups of texture features in a CXR image. The first group of features is directly generated from the preprocessed image of 512×512 . These include area, mean, standard deviation, skewness, kurtosis, energy, entropy, max, min, mean absolute deviation, median, range, root mean square, and uniformity. Remaining texture features are obtained by applying gray-level co-occurrence matrix (GLCM) [35, 36], histogram of oriented gradients (HOG) [37, 38, 39], and gray-level difference matrix (GLDM) [40, 10]. Apart from texture features, the use of frequency features also plays an important role in developing efficient classifiers in medical imaging [41, 42, 43]. In the present work, the frequency features are extracted using Fast Fourier Transform (FFT) and Discrete Wavelet Transform (DWT). Zargari et al. [44] used the aforementioned statistical features for predicting chemotherapy response in ovarian cancer patients. Drawing inspiration from their work, we computed these features for FFT map and three-level (LL3) DWT coefficients to generate a vector of frequency features. Finally, a vector of features is obtained by concatenating textural feature vector of length (140) with the frequency vector of length (28) to generate a vector of size 168 for the CXR images.

3.4. COV-ELM

In this work, we use extreme learning machine (ELM) discussed in section 2 to develop an ELM classifier (COV-ELM) for detection of COVID-19 in CXR images. Based on experimentation, we used L2-normalized radial basis function (rbf-l2) activation function. We also experimented with different number of neurons in the hidden layer. Using 10-fold cross-validation, we observed that with increase in the number of neurons in the hidden layer, accuracy increases up to $L = 140$ neurons, and the highest 10-fold cross-validation accuracy of 94.10% was reached when the number of hidden neurons was $L = 350$. Experimenting with different seeds, we found the peak accuracy was reached for the number of hidden neurons in the range 350 to 380, but without any further increase in 10-fold cross-validation accuracy. So, for further experiments, we fixed the number of hidden neurons as $L = 350$.

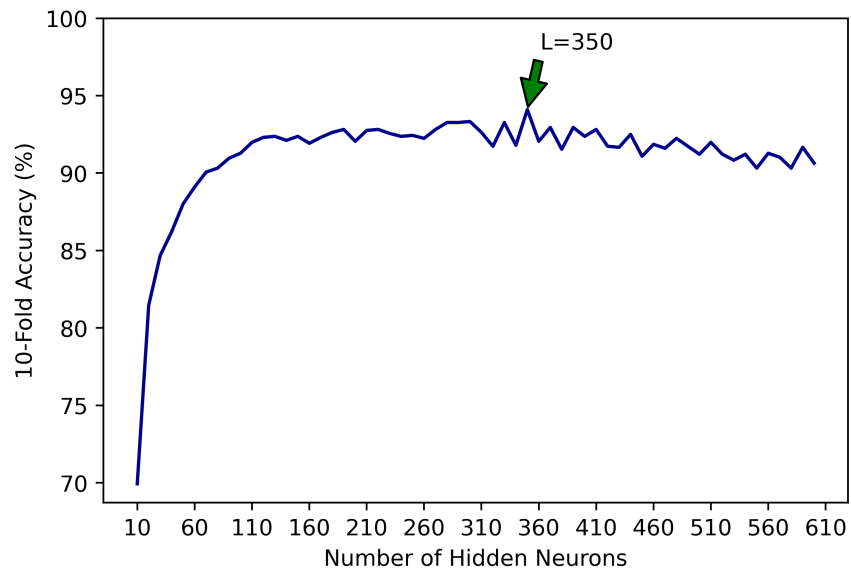


Figure 3: Effect of the increase in the number of hidden neurons (L) on 10-fold cross-validation accuracy. Accuracy increases with increase in L upto $L = 140$, and witnessed highest 10-fold cross-validation accuracy of 94.10% at $L = 350$

Boxplot in Figure 4 depicts the variation in sensitivity value. It is evident from the results that the texture features scores over frequency features. We also examined the influence of a combined set of features (168) on the classification process. It may be noted that the model yields median sensitivity of 0.945 using the combined set of features which scores over the median sensitivity values considering the frequency and texture features separately, exhibiting 0.90 and 0.93 respectively.

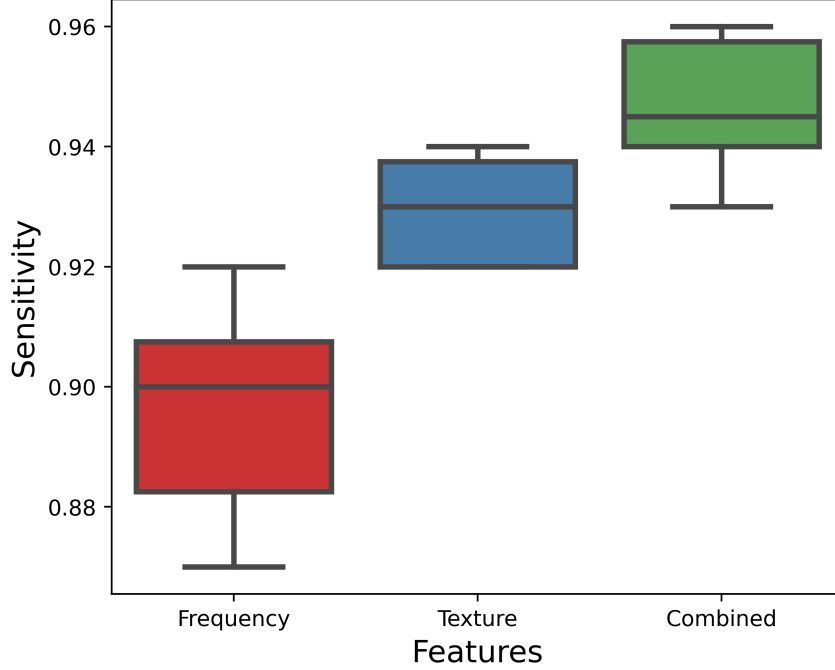


Figure 4: Boxplot for sensitivity (recall) values using frequency features, texture features, and combined set of frequency and texture features. The combined set of features depicts the median sensitivity of 0.945 which scores over the median values considering frequency and texture features separately.

4. Results and Discussion

We have carried out all the experiments using Python 3.6.9 on the NVIDIA Tesla K80 GPU. To evaluate the performance of the proposed method for the three-class classification problem, we trained the model on the CXR dataset using 10-fold cross-validation. Following Handy and Till [45], we depict the receiver operating characteristic (ROC) curves for each of the three classes, namely COVID-19, Normal, and Pneumonia for one fold (please see in Figure 5). It is apparent from the ROC curves that AUC is near unity for all three classes which shows a good generalization performance of COV-ELM.

To evaluate the performance of the proposed classifier, we carried out a 10-fold cross-validation. Fig. 6 depicts the confusion matrix and the heatmap for 10-fold cross-validation. The results of the 10-fold cross-validation are summarized in a confusion matrix (Figure 6(a)). It shows that out of 380 COVID-19 patients, 364 were correctly identified, three were misclassified as normal and thirteen were labeled as pneumonia. Similarly, pneumonia and normal subjects were also labeled by the system quite accurately. Thus, we obtained an overall accuracy of 94.40% and a high recall rate of 95.78%, 95.53%, and 92.41% for COVID-19, Normal, and Pneumonia classes respectively. The macro average of f1-score is 0.95 as depicted in the heatmap (Fig. 6(b)). As shown in Table 1, COV-ELM identified COVID-19, Normal, and Pneumonia classes with sensitivity 0.96 ± 0.04 , 0.96 ± 0.01 , and 0.92 ± 0.03 respectively at 95% confidence interval.

To establish the effectiveness of our approach, the COV-ELM is compared with the state-of-the-art machine

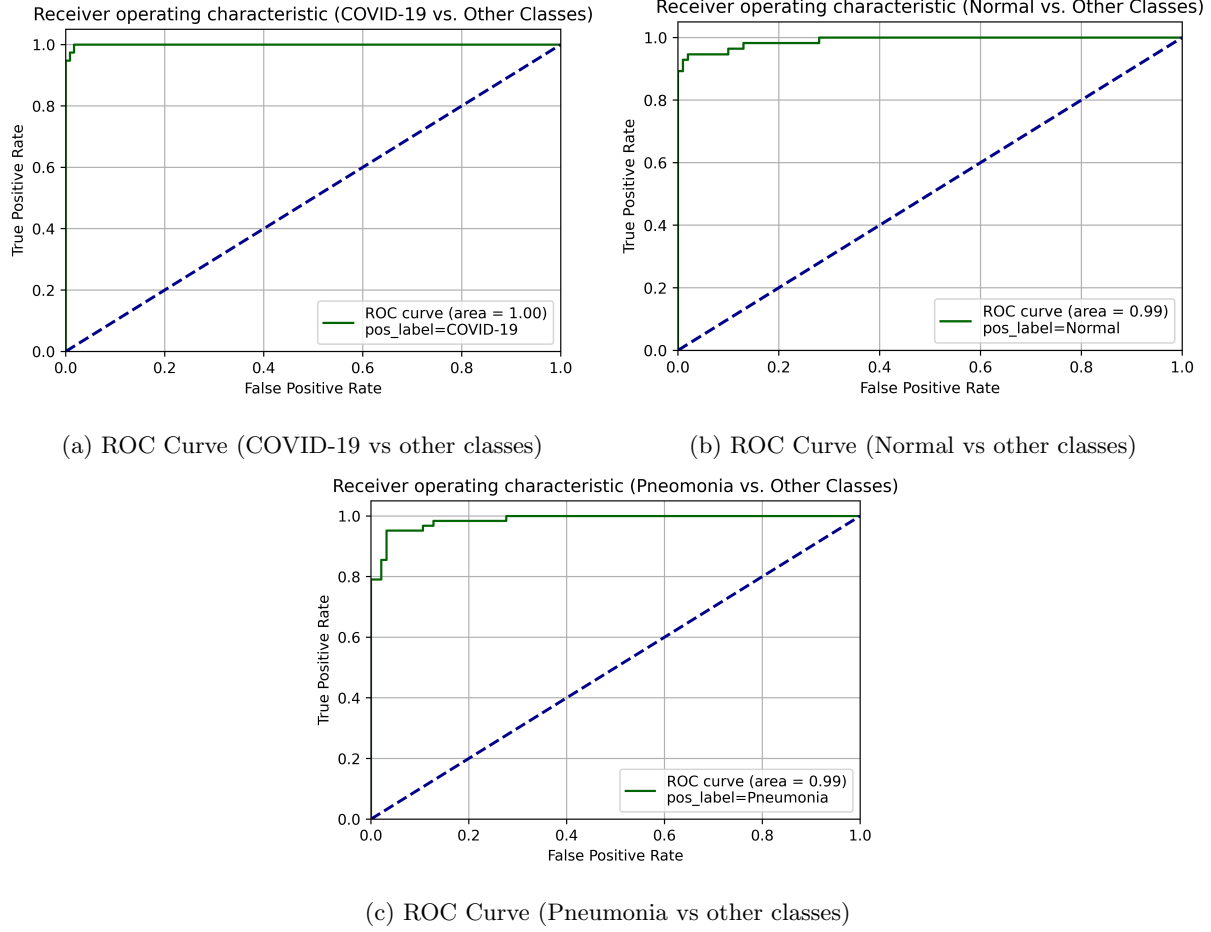
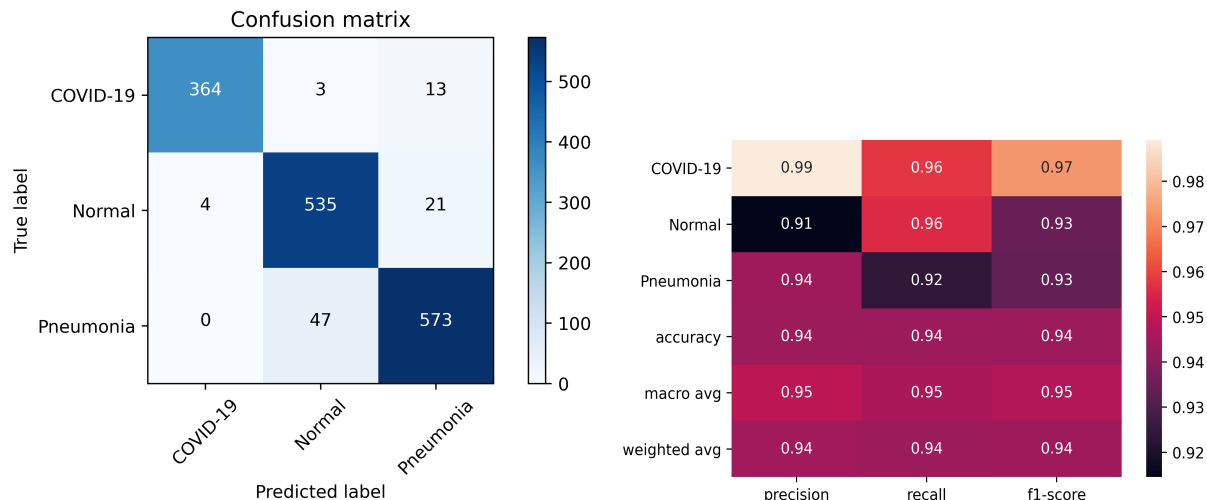


Figure 5: AUC is near unity for each of the three classes namely COVID-19, Normal, and Pneumonia in one vs all setting.

Table 1: Sensitivity (Recall) values for COVID-19, Normal, and Pneumonia at 95% confidence interval.

Sensitivity at 95% CI		
COVID-19	Normal	Pneumonia
0.96 ± 0.04	0.96 ± 0.01	0.92 ± 0.03

learning algorithms, namely support vector classifier (SVC) using rbf and linear kernels, gradient boosting classifier (GBC), random forest ensemble (RBE), artificial neural networks (ANN), decision tree classifier (DTC), and voting classifier (VC) ensemble of (logistic regression (LR), SVC, and GBC) in terms of sensitivity at 95% confidence interval (CI) (please see Table 2). It is clear that COV-ELM has higher sensitivity as compared to its competitors. It is evident from the table that the proposed approach achieves sensitivity of 0.94 ± 0.02 and scores over other state-of-the-art classifiers .



(a) Confusion matrix summarizing number of instances (b) Heatmap summarizing performance metrics: precision, recall and f1-score correctly classified across diagonal elements.

Figure 6: The classification error in classifying COVID-19, Normal, and Pneumonia is 3.68%, 4.46%, and 7.58% respectively and the macro average of f1-score is 0.95.

Table 2: Comparison of COV-ELM with other state-of-the-art classifiers in terms of sensitivity value at 95% confidence interval.

Classifier	Sensitivity
ELM (L=350, rbf-l2)	0.94 ± 0.02
GBC (learning rate=1.0)	0.91 ± 0.05
SVC (C=1.0, kernel='rbf')	0.86 ± 0.06
SVC (C=1.0, kernel='linear')	0.90 ± 0.05
RBE (min_samples_split=2)	0.89 ± 0.05
ANN (23,747 Parameters)	0.85 ± 0.08
DTC (min_samples_leaf=1)	0.82 ± 0.07
VC (LR, SVC, GBC)	0.89 ± 0.05

5. Conclusions

The current research is focused on the accurate diagnosis of COVID-19 with a high sensitivity. In this direction, the paper evaluates the applicability of ELM as a classifier. We use a combination of texture (Spatial, GLDM, HOG, AND GLDM) and frequency features (FFT and DWT) for classification of COVID-19 patients against pneumonia and normal patients. The proposed model has been evaluated using CXR images from three publicly available sources. Opposed to deep neural network which require millions of parameters for training, the number of parameters in ELM is considerably less, compared to a conventional neural network requiring thousands of parameters. We found that the 10-fold cross-validation accuracy increases with an increase in the number of hidden neurons 140, then it stabilizes more or less, finally reaching the

peak accuracy of 94.10% at 350 hidden neurons. The proposed method achieved a macro average f1-score of 0.95 in a three-class classification scenario and an overall accuracy 94.40%. The COV-ELM outperforms other competitive machine learning algorithms with a sensitivity of $0.94\% \pm 0.02$ at 95% confidence interval. The training time of COV-ELM being quite low, compared to its gradient-based competitor models, it can be quickly trained on bigger and diverse datasets that may become available in future. As part of future work, we will like to investigate whether segmentation of lung region could help improving the classification results.

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