

Total Orbital Angular Momentum

C: $2p^2$ $\begin{array}{|c|c|c|} \hline \uparrow & \uparrow & \\ \hline \end{array}$ or $\begin{array}{|c|c|c|} \hline \uparrow\downarrow & & \\ \hline \end{array}$

Clebsch-Gordan Series: $L = \ell_1 + \ell_2, \ell_1 + \ell_2 - 1, \dots, |\ell_1 - \ell_2|$

$L = |M_L|_{\max}$

$2p^2$: $1 + 1, \dots, |1 - 1| = 2, 1, 0$

$2p^2$: D, P, S

L	0	1	2	3	4	5
Term	S	P	D	F	G	H

$M_L = \Sigma m_\ell$			$M_L = \Sigma m_\ell$		
+1	0	-1			
$\begin{array}{ c c c } \hline \uparrow\downarrow & & \\ \hline \end{array}$			2		
$\begin{array}{ c c c } \hline \uparrow & \downarrow & \\ \hline \end{array}$			1		
$\begin{array}{ c c c } \hline \uparrow & & \downarrow \\ \hline \end{array}$			0		
$\begin{array}{ c c c } \hline & \uparrow\downarrow & \\ \hline \end{array}$			0		
$\begin{array}{ c c c } \hline & \uparrow & \downarrow \\ \hline \end{array}$			-1		
$\begin{array}{ c c c } \hline & & \uparrow\downarrow \\ \hline \end{array}$			-2		
${}^1D + {}^1S$					

+1	0	-1	
$\begin{array}{ c c c } \hline \uparrow & \uparrow & \\ \hline \end{array}$			1
$\begin{array}{ c c c } \hline \uparrow & & \uparrow \\ \hline \end{array}$			0
$\begin{array}{ c c c } \hline & \uparrow & \uparrow \\ \hline \end{array}$			-1
3P			

Singlets: $L = |M_L|_{\max} = 2$ for a 1D with $M_L = 2, 1, 0, -1, -2$, leaving $M_L = 0$ to give a 1S term.

Triplets: $L = |M_L|_{\max} = 1$ for a 3P with $M_L = 1, 0, -1$.

These diagrams don't take into account electron indistinguishability. Schematically for example:

$$\begin{array}{|c|c|c|} \hline \uparrow\downarrow & & \\ \hline \end{array} \sim \frac{1}{\sqrt{2}} \left(\begin{array}{|c|c|c|} \hline \uparrow & \downarrow & \\ \hline \end{array} - \begin{array}{|c|c|c|} \hline \downarrow & \uparrow & \\ \hline \end{array} \right) \quad \text{and all electrons take their turns in } p_x, p_y, \text{ and } p_z.$$

In addition, all degenerate configurations mix as linear combinations (e.g. all the $M_L = 0$ configurations).

configuration: $d^1 p^1$					for which $\ell_1 = 2$ and $\ell_2 = 1$					$L = 2+1, \dots, 2-1 = 3, 2, 1$ or F, D, P				
+2	+1	0	-1	-2	+2	+1	0	-1	-2	+2	+1	0	-1	-2
\uparrow						\uparrow						\uparrow		

overall: 3,2,2,1,1,1,0,0,0,-1,-1,-1,-2,-2,-3

leaving: 2,1,1,0,0,-1,-1,-2

leaving: 1,0,-1

$L = |M_L|_{\max} = 3$ with $M_L = 3, 2, 1, 0, -1, -2, -3$

$L = |M_L|_{\max} = 2$ with $M_L = 2, 1, 0, -1, -2$

$L = |M_L|_{\max} = 1$ with $M_L = 1, 0, -1$

Degenerate individual configurations combine in the final terms and electron indistinguishability is maintained in the final spin-orbitals, through the use of Slater determinants.