THERMODYNAMICS AND STATISTICAL PHYSICS

Formulas and constants

Thermodynamic functions and relations

$$H = E + pV$$

$$F = E - TS$$

$$G = E - TS + pV$$

$$\left(\frac{\partial E}{\partial S}\right)_{V} = T$$

$$\left(\frac{\partial E}{\partial V}\right)_{c} = -1$$

$$\left(\frac{\partial H}{\partial S}\right) = T$$

$$\left(\frac{\partial E}{\partial S}\right)_V = T$$
 $\left(\frac{\partial E}{\partial V}\right)_S = -p$ $\left(\frac{\partial H}{\partial S}\right)_p = T$ $\left(\frac{\partial H}{\partial p}\right)_S = V$

$$\left(\frac{\partial F}{\partial T}\right)_{xx} = -S$$

$$\left(\frac{\partial F}{\partial V}\right)_{T} = -p$$

$$\left(\frac{\partial F}{\partial T}\right)_V = -S$$
 $\left(\frac{\partial F}{\partial V}\right)_T = -p$ $\left(\frac{\partial G}{\partial T}\right)_p = -S$

$$\left(\frac{\partial G}{\partial p}\right)_T = V$$

Maxwell relations

$$\left(rac{\partial T}{\partial V}
ight)_S = -\left(rac{\partial p}{\partial S}
ight)_V$$

$$\left(\frac{\partial T}{\partial p}\right)_S = \left(\frac{\partial V}{\partial S}\right)_S$$

$$\left(\frac{\partial S}{\partial V}\right)_T = \left(\frac{\partial p}{\partial T}\right)_V$$

$$\left(\frac{\partial T}{\partial V}\right)_S = -\left(\frac{\partial p}{\partial S}\right)_V \qquad \left(\frac{\partial T}{\partial p}\right)_S = \left(\frac{\partial V}{\partial S}\right)_p \qquad \left(\frac{\partial S}{\partial V}\right)_T = \left(\frac{\partial p}{\partial T}\right)_V \qquad \left(\frac{\partial S}{\partial p}\right)_T = -\left(\frac{\partial V}{\partial T}\right)_p$$

Specific heat

$$c_V = rac{1}{
u} \left(rac{dQ}{dT}
ight)_V \qquad \qquad c_p = rac{1}{
u} \left(rac{dQ}{dT}
ight)_p$$

$$c_p = \frac{1}{\nu} \left(\frac{dQ}{dT} \right)_r$$

Entropy

$$S = k \ln \Omega$$

$$S = -k \sum_{r} P_r \ln P_r$$

$$S = -k \sum_{r} P_r \ln P_r$$
 $S = k(\ln Z + \beta \overline{E})$

Partition functions

$$Z = \sum_{r} e^{-oldsymbol{eta} oldsymbol{E}_{r}}$$

$$\mathcal{Z} = \sum_{m{r}} e^{-m{eta} E_{m{r}} - m{lpha} N_{m{r}}}$$

$$Z = \sum_{r} e^{-eta E_r}$$
 $\qquad \qquad Z = \sum_{r} e^{-eta E_r - lpha N_r}$ $\qquad \qquad \ln Z = lpha N \pm \sum_{r} \ln \left(1 \pm e^{-eta \epsilon_r - lpha}
ight)$

Clausius-Clapeyron equation

$$\frac{dp}{dT} = \frac{\Delta S}{\Delta V}$$

$$rac{dp}{dT} = rac{\Delta S}{\Delta V} \qquad \qquad rac{dp}{dT} = rac{L_{12}}{T \; \Delta V}$$

Fermi energy ($\mu = -kT\alpha$)

$$\mu_j = -T \left(\frac{\partial S}{\partial N_j} \right)_{E,V,N} \qquad \mu_j = \left(\frac{\partial E}{\partial N_j} \right)_{S,V,N} \qquad \mu_j = \left(\frac{\partial F}{\partial N_j} \right)_{T,V,N} \qquad \mu_j = -\left(\frac{\partial G}{\partial N_j} \right)_{T,\eta,N}$$

$$\mu_j = \left(rac{\partial E}{\partial N_j}
ight)_{S.V.N}$$

$$\mu_j = \left(rac{\partial F}{\partial N_j}
ight)_{T,V,N}$$

$$\mu_j = -\left(rac{\partial G}{\partial N_j}
ight)_{T,p,N}$$

Stefan-Boltzmann law

$$\mathcal{P}=a\sigma T^4=arac{\pi^2k^4}{60c^2\hbar^3}T^4$$

Stirlings formula

$$\ln N! = N \ln N - N + rac{1}{2} \ln(2\pi N) + ...$$

Integrals

$$\int_0^\infty x^n e^{-ax} dx = rac{n!}{a^{n+1}}$$
 $\int_0^\infty x^{2n+1} e^{-ax^2} dx = rac{n!}{2a^{n+1}}$ $\int_0^\infty x^{2n} e^{-ax^2} dx = rac{(2n-1)!!}{2(2a)^n} \sqrt{rac{\pi}{a}}$

The gamma function

$$\Gamma(t) = \int_0^\infty x^{t-1} e^x dx$$
 $\Gamma(t+1) = t\Gamma(t)$

Value of some integrals

Physical constants

$$c = 2.997925 \cdot 10^8 \text{ m/s}$$

$$e = 1.6022 \cdot 10^{-19} \text{ C}$$

$$h = 6.6262 \cdot 10^{-34} \text{ Js} = 4.1357 \cdot 10^{-15} \text{ eVs}$$

$$\hbar = 1.0546 \cdot 10^{-34} \text{ Js} = 0.65821 \cdot ^{-15} \text{ eVs}$$

$$m_e = 0.91094 \cdot 10^{-30} \text{ kg} = 0.51100 \text{ MeV/c}^2$$

$$m_p = 1.6726 \cdot 10^{-27} \text{ kg} = 938.27 \text{ MeV/c}^2$$

$$m_n = 1.6605 \cdot 10^{-27} \text{ kg} = 931.48 \text{ MeV/c}^2$$

$$N_A = 6.0221 \cdot 10^{23} \text{ mole}^{-1}$$

$$R = 8.314 \text{ JK}^{-1} \text{ mole}^{-1}$$

$$k_B = 1.38066 \cdot 10^{-23} \text{ J/K} = 8.61739 \cdot 10^{-5} \text{ eV/K}$$

$$\sigma = 5.6697 \cdot 10^{-8} \text{ Jm}^{-2} \text{s}^{-1} \text{K}^{-4}$$