## **Problem Set 3**

Due: In class on Wednesday, February 25. Starred problems are optional.

**Problem 3-1.** Show how to divide an N-bit number by the constant 3 in  $O(\lg N)$  time using O(N) hardware.

**Problem 3-2.** A spanning tree of a graph is the tree formed by a subset of the edges of the graph such that all vertices in the graph are contained in the tree. A minimum spanning tree of an edge-weighted graph is a spanning tree of minimum weight, where the weight of the tree is defined to be the sum of the weights of the edges in the tree. Argue that a minimum spanning tree for a graph with N vertices can be computed in O(N) time on an  $N \times N$  mesh. You may assume that the graph is given as an  $N \times N$  adjacency matrix of edge weights, and that all edge weights are distinct.

**Problem 3-3.** \* Consider the division circuit based on the Chinese Remainder Theorem which was presented in class. The circuit computes the first N bits of 1/x, where x is an N-bit number, in  $O(\lg N)$  time. As presented, how much hardware does this circuit require asymptotically? Try to reduce the asymptotic hardware requirements without giving up the  $O(\lg N)$  time. You may either restrict yourself to combinational implementations or use any fixed-connection network.