







6.896 2/18/04 Theorem A(N) = A\* 45,5 Proof. (Induction on k) Claim: ais = 1 iff 3 path i > j in orig graph only going through nodes 1,2,...,k.  $(\Rightarrow)$  Easy. Case 2. (3) through 1,..., k-1 au(k+1) =

(ase 2. (3) k through 1,..., k-1 ack (k-1) =

time on M-M ( ) Case 1. is j through 1, ..., k-1 X O(N) time on N=N mesh. Idea: Same computation as G.E.  $a_{ij}^{(k)} = a_{ii}^{(k-1)} - a_{ik}^{(k-1)} a_{k}^{(k-1)}$ Also, shortest paths: aij = Sweight of edge from i to j a\*; = weight of min-weight path from i to j'. sum edge weights aij = min (aij), aik + akj Homework min spanning thee Use thm: An edge i -> i with weight air belongs to MST iff I path from i to j with every edge having weight < air.

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