# Towards Better Modeling Hierarchical Structure for Self-Attention with Ordered Neurons

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#### Abstract

Recent studies have shown that a hybrid of self-attention networks (SANs) and recurrent neural networks (RNNs) outperforms both individual architectures, while not much is known about why the hybrid models work. With the belief that modeling hierarchical structure is an essential complementary between SANs and RNNs, we propose to further enhance the strength of hybrid models with an advanced variant of RNNs - Ordered Neurons LSTM (ON-LSTM, Shen et al., 2019), which introduces a syntax-oriented inductive bias to perform tree-like composition. Experimental results on the benchmark machine translation task show that the proposed approach outperforms both individual architectures and a standard hybrid model. Further analyses on targeted linguistic evaluation and logical inference tasks demonstrate that the proposed approach indeed benefits from a better modeling of hierarchical structure.

#### 1 Introduction

Self-attention networks (SANs, Lin et al., 2017) have advanced the state of the art on a variety of natural language processing (NLP) tasks, such as machine translation (Vaswani et al., 2017), semantic role labelling (Tan et al., 2018), and language representations (Devlin et al., 2018). However, a previous study empirically reveals that the hierarchical structure of the input sentence, which is essential for language understanding, is not well modeled by SANs (Tran et al., 2018). Recently, hybrid models which combine the strengths of SANs and recurrent neural networks (RNNs) have outperformed both individual architectures on a machine translation task (Chen et al., 2018). We attribute the improvement to that RNNs complement SANs on the representation limitation of hierarchical structure, which is exactly the strength of RNNs (Tran et al., 2018).

Starting with this intuition, we propose to further enhance the representational power of hybrid models with an advanced RNNs variant - Ordered Neurons LSTM (ON-LSTM, Shen et al., 2019). ON-LSTM is better at modeling hierarchical structure by introducing a syntax-oriented inductive bias, which enables RNNs to perform tree-like composition by controlling the update frequency of neurons. Specifically, we stack SANs encoder on top of ON-LSTM encoder (cascaded encoder). SANs encoder is able to extract richer representations from the input augmented with structure context. To reinforce the strength of modeling hierarchical structure, we propose to simultaneously expose both types of signals by explicitly combining outputs of the SANs and ON-LSTM encoders.

We validate our hypothesis across a range of tasks, including machine translation, targeted linguistic evaluation, and logical inference. While machine translation is a benchmark task for deep learning models, the last two tasks focus on evaluating how much structure information is encoded in the learned representations. Experimental results show that the proposed approach consistently improves performances in all tasks, and modeling hierarchical structure is indeed an essential complementary between SANs and RNNs.

The contributions of this paper are:

- We empirically demonstrate that a better modeling of hierarchical structure is an essential strength of hybrid models over the vanilla SANs.
- Our study proves that the idea of augmenting RNNs with ordered neurons (Shen et al., 2019) produces promising improvement on machine translation, which is one potential criticism of ON-LSTM.

<sup>\*</sup>Work done when interning at Tencent AI Lab.

# **Approach**

Partially motivated by Wang et al. (2016) and Chen et al. (2018), we stack a SANs encoder on top of a RNNs encoder to form a cascaded encoder. In the cascaded encoder, hierarchical structure modeling is enhanced in the bottom RNNs encoder, based on which SANs encoder is able to extract representations with richer hierarchical information. Let  $\mathbf{X} = \{\mathbf{x}_1, \dots, \mathbf{x}_N\}$  be the input sequence, the representation of the cascaded encoder is calculated by

$$\mathbf{H}_{\mathrm{RNN}s}^{K} = \mathrm{ENC}_{\mathrm{RNN}s}(\mathbf{X}), \tag{1}$$

$$\mathbf{H}_{\mathrm{RNN}s}^{K} = \mathrm{ENC}_{\mathrm{RNN}s}(\mathbf{X}),$$
 (1)  
 $\mathbf{H}_{\mathrm{SAN}s}^{L} = \mathrm{ENC}_{\mathrm{SAN}s}(\mathbf{H}_{\mathrm{RNN}s}^{K}),$  (2)

where  $Enc_{RNNs}(\cdot)$  is a K-layer RNNs encoder that reads the input sequence, and  $ENC_{SANS}(\cdot)$  is a Llayer SANs encoder that takes the output of RNNs encoder as input.

In this work, we replace the standard RNNs with recently proposed ON-LSTM for better modeling of hierarchical structure, and directly combine the two encoder outputs to build even richer representations, as described below.

**Modeling Hierarchical Structure with Ordered** Neurons ON-LSTM introduces a new syntaxoriented inductive bias - Ordered Neurons, which enables LSTM models to perform tree-like composition without breaking its sequential form (Shen et al., 2019). Ordered neurons enables dynamic allocation of neurons to represent different timescale dependencies by controlling the update frequency of neurons. The assumption behind ordered neurons is that some neurons always update more (or less) frequently than the others, and that order is pre-determined as part of the model architecture. Formally, ON-LSTM introduces novel

ordered neuron rules to update cell state:

$$w_t = \tilde{f}_t \circ \tilde{i}_t, \tag{3}$$

$$\hat{f}_t = f_t \circ w_t + (\tilde{f}_t - w_t), \tag{4}$$

$$\hat{i}_t = i_t \circ w_t + (\tilde{i}_t - w_t), \tag{5}$$

$$c_t = \hat{f}_t \circ c_{t-1} + \hat{i}_t \circ \hat{c}_t, \tag{6}$$

where forget gate  $f_t$ , input gate  $i_t$  and state  $\hat{c}_t$  are same as that in the standard LSTM (Hochreiter and Schmidhuber, 1997). The master forget gate  $f_t$ and the master input gate  $i_t$  are newly introduced to control the erasing and the writing behaviors respectively.  $w_t$  indicates the overlap, and when

the overlap exists  $(\exists k, w_{tk} > 0)$ , the corresponding neurons are further controlled by the standard gates  $f_t$  and  $i_t$ .

An ideal master gate is in binary format such as (0,0,1,1,1), which splits the cell state into two continuous parts: 0-part and 1-part. The neurons corresponding to 0-part and 1-part are updated with more and less frequencies separately, so that the information in 0-part neurons will only keep a few time steps, while the information in 1part neurons will last for more time steps. Since such binary gates are not differentiable, the goal turns to find the splitting point d (the index of the first 1 in the ideal master gate). To this end, Shen et al. (2019) introduced a new activation function:

$$CU(\cdot) = CUMSUM(softmax(\cdot)), \tag{7}$$

where  $softmax(\cdot)$  produces a probability distribution (e.g. (0.1, 0.2, 0.4, 0.2, 0.1)) to indicate the probability of each position being the splitting point d. CUMSUM is the cumulative probability distribution, in which the k-th probability refers to the probability that d falls within the first kpositions. The output for the above example is (0.1, 0.3, 0.7, 0.9, 1.0), in which different values denotes different update frequencies. It also equals to the probability of each position's value being 1 in the ideal master gate. Since this ideal master gate is binary,  $CU(\cdot)$  is the expectation of the ideal master gate.

Based on this activation function, the master gates are defined as

$$\tilde{f}_t = \text{CU}_f(\mathbf{x}_t, \mathbf{h}_{t-1}),$$
 (8)

$$\tilde{i}_t = 1 - CU_i(\mathbf{x}_t, \mathbf{h}_{t-1}),$$
 (9)

where  $\mathbf{x}_t$  is the current input and  $\mathbf{h}_{t-1}$  is the hidden state of previous step.  $CU_f$  and  $CU_i$  are two individual activation functions with their own trainable parameters.

Short-Cut Connection Inspired by previous work on exploiting deep representations (Peters et al., 2018; Dou et al., 2018), we propose to simultaneously expose both types of signals by explicitly combining them with a simple short-cut connection (He et al., 2016).

Similar to positional encoding injection in Transformer (Vaswani et al., 2017), we add the output of the ON-LSTM encoder to the output of SANs encoder:

$$\widehat{\mathbf{H}} = \mathbf{H}_{\text{ON-LSTM}}^K + \mathbf{H}_{\text{SAN}s}^L, \tag{10}$$

#	<b>Encoder Architecture</b>	Para.	BLEU					
Base Model								
1	6L SANS	88M	27.31					
2	6L LSTM	97M	27.23					
3	6L On-Lstm	110M	27.44					
4	6L LSTM + 4L SANS	104M	27.78↑					
5	6L On-LSTM + 4L SANS	123M	28.27↑					
6	3L On-LSTM + 3L SANS	99M	28.21↑					
7	+ Short-Cut	99M	28.37↑					
Big Model								
8	6L SANS	264M	28.58					
9	Hybrid Model + Short-Cut	308M	29.30↑					

Table 1: Case-sensitive BLEU scores on the WMT14 English $\Rightarrow$ German translation task. " $\uparrow$  /  $\uparrow$ ": significant over the conventional self-attention counterpart (p < 0.05/0.01), tested by bootstrap resampling. "6L SANS" is the state-of-the-art Transformer model. "nL LSTM + mL SANS" denotes stacking n LSTM layers and m SANs layers subsequently. "Hybrid Model" denotes "3L ON-LSTM + 3L SANS".

where  $\mathbf{H}_{\text{ON-LSTM}}^K \in \mathbb{R}^{N \times d}$  is the output of ON-LSTM encoder, and  $\mathbf{H}_{\text{SAN}s}^L \in \mathbb{R}^{N \times d}$  is output of SANs encoder.

# 3 Experiments

We chose machine translation, targeted linguistic evaluation and logical inference tasks to conduct experiments in this work. The first and the second tasks evaluate and analyze models as the hierarchical structure is an inherent attribute for natural language. The third task aims to directly evaluate the effects of hierarchical structure modeling on artificial language.

#### 3.1 Machine Translation

For machine translation, we used the benchmark WMT14 English⇒German dataset. were encoded using byte-pair encoding (BPE) with 32K word-piece vocabulary (Sennrich et al., 2016). We implemented the proposed approaches on top of TRANSFORMER (Vaswani et al., 2017) a state-of-the-art SANs-based model on machine translation, and followed the setting in previous work (Vaswani et al., 2017) to train the models, and reproduced their reported results. We tested on both the Base and Big models which differ at hidden size (512 vs. 1024), filter size (2048 vs. 4096) and number of attention heads (8 vs. 16). All the model variants were implemented on the encoder. The implementation details are introduced in Appendix A.1. Table 1 lists the results.

#	Encoder Architecture	Para.	BLEU
1	$3L \text{ ON-LSTM} \rightarrow 3L \text{ SANs}$	99M	28.21
2	$3L SANS \rightarrow 3L ON-LSTM$	99M	27.39
3	8L LSTM	102.2M	27.25
4	10L SANs	100.6M	27.76

Table 2: Results for encoder strategies. Case-sensitive BLEU scores on the WMT14 English $\Rightarrow$ German translation task. "A  $\rightarrow$  B" denotes stacking B on the top of A. The model in Row 1 is the hybrid model in Table 1.

**Baselines** (Rows 1-3) Following Chen et al. (2018), the three baselines are implemented with the same framework and optimization techniques as used in Vaswani et al. (2017). The difference between them is that they adopt SANS, LSTM and ON-LSTM as basic building blocks respectively. As seen, the three architectures achieve similar performances for their unique representational powers.

Hybrid Models (Rows 4-7) We first followed Chen et al. (2018) to stack 6 RNNs layers and 4 SANs layers subsequently (Row 4), which consistently outperforms the individual models. This is consistent with results reported by Chen et al. (2018). In this setting, the ON-LSTM model significantly outperforms its LSTM counterpart (Row 5), and reducing the encoder depth can still maintain the performance (Row 6). We attribute these to the strength of ON-LSTM on modeling hierarchical structure, which we believe is an essential complementarity between SANs and RNNs. In addition, the Short-Cut connection combination strategy improves translation performances by providing richer representations (Row 7).

Stronger Baseline (Rows 8-9) We finally conducted experiments on a stronger baseline – the TRANSFORMER-BIG model (Row 8), which outperforms its TRANSFORMER-BASE counterpart (Row 1) by 1.27 BLEU points. As seen, our model consistently improves performance over the stronger baseline by 0.72 BLEU points, demonstrating the effectiveness and universality of the proposed approach.

Assessing Encoder Strategies We first investigate the encoder stack strategies on different stack orders. From Table 2, to compare with the proposed hybrid model, we stack 3-layers ON-LSTM on the top of 3-layers SANs (Row 2). It performs worse than the strategy in the proposed hybrid model. The result support the viewpoint that the

Task	S	O	Hybrid + Short-Cut						
Task	Final	Final	$\mathbf{H}_O$	$\mathbf{H}_{S}$	Final				
Surface Tasks									
SeLen	92.71	90.70	91.94	89.50	89.86				
WC	81.79	76.42	90.38	79.10	80.37				
Āvg	87.25	83.56	91.16	84.30	85.12				
Syntactic Tasks									
TrDep	44.78	52.58	51.19	52.55	53.28				
ToCo	84.53	86.32	86.29	87.92	87.89				
BShif	52.66	82.68	81.79	82.05	81.90				
Avg	60.66	73.86	73.09	74.17	74.36				
Semantic Tasks									
Tense	84.76	86.00	83.88	86.05	85.91				
SubN	85.18	85.44	85.56	84.59	85.81				
ObjN	81.45	86.78	85.72	85.80	85.38				
SoMo	49.87	49.54	49.23	49.12	49.92				
CoIn	68.97	72.03	72.06	72.05	72.23				
Āvg	74.05	75.96	75.29	75.52	75.85				

Table 3: Performance on the linguistic probing tasks of evaluating linguistics embedded in the learned representations. "S" and "O" denote the SAN and ON-LSTM baseline models. " $\mathbf{H}_O$ " and " $\mathbf{H}_S$ " are respectively the outputs of the ON-LSTM encoder and the SAN encoder in the hybrid model, and "Final" denotes the final output exposed to decoder.

SANs encoder is able to extract richer representations if the input is augmented with sequential context (Chen et al., 2018).

Moreover, to dispel the doubt that whether the improvement of hybrid model comes from the increasement of parameters. We investigate the 8-layers LSTM and 10-layers SANs encoders (Rows 3-4) which have more parameters compared with the proposed hybrid model. The results show that the hybrid model consistently outperforms these model variants with less parameters and the improvement should not be due to more parameters.

#### 3.2 Targeted Linguistic Evaluation

To gain linguistic insights into the learned representations, we conducted probing tasks (Conneau et al., 2018) to evaluate linguistics knowledge embedded in the final encoding representation learned by model, as shown in Table 3. We evaluated SANs and proposed hybrid model with Short-Cut connection on these 10 targeted linguistic evaluation tasks. The tasks and model details are described in Appendix A.2.

Experimental results are presented in Table 3. Several observations can be made here. The proposed hybrid model with short-cut produces more

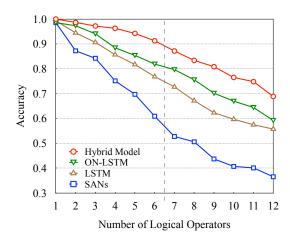


Figure 1: Accuracy of logical inference when training on logic data with at most 6 logical operators in the sequence.

informative representation in most tasks ("Final" in "S" vs. in "Hybrid+Short-Cut"), indicating that the effectiveness of the model. The only exception are surface tasks, which is consistent with the conclusion in Conneau et al. (2018): as a model captures deeper linguistic properties, it will tend to forget about these superficial features. Short-cut further improves the performance by providing richer representations (" $\mathbf{H}_S$ " vs. "Final" in "Hybrid+Short-Cut"). Especially on syntactic tasks, our proposed model surpasses the baseline more than 13 points (74.36 vs. 60.66) on average, which again verifies that ON-LSTM enhance the strength of modeling hierarchical structure for self-attention.

#### 3.3 Logical Inference

We also verified the model's performance in the logical inference task proposed by Bowman et al. (2015). This task is well suited to evaluate the ability of modeling hierarchical structure. Models need to learn the hierarchical and nested structures of language in order to predict accurate logical relations between sentences (Bowman et al., 2015; Tran et al., 2018; Shen et al., 2019). The artificial language of the task has six types of words {a, b, c, d, e, f} in the vocabulary and three logical operators {or, and, not}. The goal of the task is to predict one of seven logical relations between two given sentences. These seven relations are: two entailment types  $(\Box, \Box)$ , equivalence  $(\equiv)$ , exhaustive and non-exhaustive contradiction  $(\land, \mid)$ , and semantic independence  $(\#, \smile)$ .

We evaluated the SANS, LSTM, ON-LSTM and

proposed model. We followed Tran et al. (2018) to use two hidden layers with Short-Cut connection in all models. The model details and hyperparameters are described in Appendix A.3.

Figure 1 shows the results. The proposed hybrid model outperforms both the LSTM-based and the SANs-based baselines on all cases. Consistent with Shen et al. (2019), on the longer sequences ( $\geq 7$ ) that were not included during training, the proposed model also obtains the best performance and has a larger gap compared with other models than on the shorter sequences ( $\leq 6$ ), which verifies the proposed model is better at modeling more complex hierarchical structure in sequence. It also indicates that the hybrid model has a stronger generalization ability.

#### 4 Related Work

Improved Self-Attention Networks Recently, there is a large body of work on improving SANs in various NLP tasks (Yang et al., 2018; Wu et al., 2018; Yang et al., 2019a,b; Guo et al., 2019; Wang et al., 2019a; Sukhbaatar et al., 2019), as well as image classification (Bello et al., 2019) and automatic speech recognition (Mohamed et al., 2019) tasks. In these works, several strategies are proposed to improve the utilize SANs with the enhancement of local and global information. In this work, we enhance the SANs with the On-Lstm to form a hybrid model (Chen et al., 2018), and thoroughly evaluate the performance on machine translation, targeted linguistic evaluation, and logical inference tasks.

Structure Modeling for Neural Networks in NLP Structure modeling in NLP has been studied for a long time as the natural language sentences inherently have hierarchical structures (Chomsky, 1965; Bever, 1970). With the emergence of deep learning, tree-based models have been proposed to integrate syntactic tree structure into Recursive Neural Networks (Socher et al., 2013), LSTMs (Tai et al., 2015), CNNs (Mou et al., 2016). As for SANs, Hao et al. (2019a), Ma et al. (2019) and Wang et al. (2019b) enhance the SANs with neural syntactic distance, multigranularity attention scope and structural position representations, which are generated from the syntactic tree structures.

Closely related to our work, Hao et al. (2019b) find that the integration of the recurrence in SANs encoder can provide more syntactic structure fea-

tures to the encoder representations. Our work follows this direction and empirically evaluates the structure modelling on the related tasks.

#### 5 Conclusion

In this paper, we adopt the ON-LSTM, which models tree structure with a novel activation function and structured gating mechanism, as the RNNs counterpart to boost the hybrid model. We also propose a modification of the cascaded encoder by explicitly combining the outputs of individual components, to enhance the ability of hierarchical structure modeling in a hybrid model. Experimental results on machine translation, targeted linguistic evaluation and logical inference tasks show that the proposed models achieve better performances by modeling hierarchical structure of sequence.

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## **A Supplemental Material**

#### A.1 Machine Translation

We conducted experiments on the widely-used WMT14 English⇒German dataset¹ consisting of about 4.56M sentence pairs. We used newstest2013 and newstest2014 as development set and test set respectively. We applied byte pair encoding (BPE) toolkit² with 32K merge operations. The case-sensitive NIST BLEU score (Papineni et al., 2002) is used as the evaluation metric. All models were trained on eight NVIDIA Tesla P40 GPUs where each was allocated with a batch size of 4096 tokens.

For Base model, it has embedding size and hidden size of 512, filter size of 2048 and attention heads of 8. Compared with Base model, Big model has embedding size and hidden size of 1024, filter size of 4096 and attention heads of 16. For both Base and Big models, the number of encoder and decoder layer is 6, all types of dropout rate is 0.1. Adam (Kingma and Ba, 2015) is used with  $\beta_1 = 0.9$ ,  $\beta_2 = 0.98$  and  $\epsilon = 10^{-9}$ . The learning rate is 1.0 and linearly warms up over the first 4,000 steps, then decreases proportionally to the inverse square root of the step number. Label smoothing is 0.1 during training (Szegedy et al., 2016). All the results we reported are based on the individual models without using the averaging model or ensemble.

## A.2 Targeted Linguistic Evaluation

We conducted 10 probing tasks<sup>3</sup> to study what linguistic properties are captured by the encoders (Conneau et al., 2018). A probing task is a classification problem that focuses on simple linguistic properties of sentences. 'SeLen' predicts the length of sentences in terms of number of words. 'WC' tests whether it is possible to recover information about the original words given its sentence embedding. 'TrDep' checks whether an encoder infers the hierarchical structure of sentences. In 'ToCo' task, sentences should be classified in terms of the sequence of top constituents immediately below the sentence node. 'BShif' tests whether two consecutive tokens within the sentence have been inverted. 'Tense' asks for the tense of the main-clause verb. 'SubN' focuses on

the number of the main clause's subject. 'ObjN' tests for the number of the direct object of the main clause. In 'SoMo', some sentences are modified by replacing a random noun or verb with another one and the classifier should tell whether a sentence has been modified. 'CoIn' contains sentences made of two coordinate clauses. Half of sentences are inverted the order of the clauses and the task is to tell whether a sentence is intact or modified.

Each of our probing model consists a pretrained encoder of model variations from machine translation followed by a MLP classifier (Conneau et al., 2018). The mean of the encoding layer is served as the sentence representation passed to the classifier. The MLP classifier has a dropout rate of 0.3, a learning rate of 0.0005 with Adam optimizer and were trained for 250 epochs.

#### A.3 Logical Inference

We used the artificial data<sup>4</sup> described in Bowman et al. (2015). The train/dev/test dataset ratios are set to 0.8/0.1/0.1 with the number of logical operations range from 1 to 12. We followed Tran et al. (2018) to implement the architectures: premise and hypothesis sentences are encoded in fixed-size vectors, which are concatenated and fed to a three layer feed-forward network for classification of the logical relation. For LSTM based models, we took the last hidden state of the top layer as a fixed-size vector representation of the sentence. For the hybrid and SANs models, we used two trainable queries to obtain the fixed-size representation.

In our experiments, both word embedding size and hidden size are set to 256. All models have two layers, a dropout rate of 0.2, a learning rate of 0.0001 with Adam optimizer, and were trained for 100 epochs. Especially, for hybrid model, we stacked one ON-LSTM layer and one SANs layer subsequently. Short-Cut connection between layers is added into all models for fair comparison.

<sup>&</sup>lt;sup>1</sup>http://www.statmt.org/wmt14/translation-task.html

<sup>&</sup>lt;sup>2</sup>https://github.com/rsennrich/subword-nmt

<sup>&</sup>lt;sup>3</sup>https://github.com/facebookresearch/SentEval/tree/master/data/probing

<sup>&</sup>lt;sup>4</sup>https://github.com/sleepinyourhat/vector-entailment