

An ISO 9001: 2008 Certified Company

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### MOCK TEST PAPER - 12 (T-II) 2013 (SOLUTION)

1. (B) 
$$\frac{1}{\sqrt{1} + \sqrt{2}} + \frac{1}{\sqrt{2} + \sqrt{3}} + \frac{1}{\sqrt{3} + \sqrt{4}} + \dots$$

$$\frac{1}{\sqrt{120} + \sqrt{121}}$$

$$= \frac{(\sqrt{2} - \sqrt{1})}{(\sqrt{2}^2 - \sqrt{1}^2)} + \frac{(\sqrt{3} - \sqrt{2})}{(\sqrt{3}^2 - \sqrt{2}^2)} + \frac{(\sqrt{4} - \sqrt{3})}{(\sqrt{4}^2 - \sqrt{3}^2)}$$

.... + 
$$\frac{(\sqrt{121} - \sqrt{120})}{(\sqrt{121}^2 - \sqrt{120}^2)}$$

$$= (\sqrt{2} - \sqrt{1}) + \sqrt{3} - \sqrt{2}) + \sqrt{4} - \sqrt{3})$$
$$+ \dots (\sqrt{120} - \sqrt{119}) + (\sqrt{121} - \sqrt{120})$$

$$=$$
  $-\sqrt{1}$  +  $\sqrt{121}$  = 11 - 1 = **10 Ans.**

2. (A) 
$$\frac{\sqrt{5}}{2} - \frac{10}{\sqrt{5}} + \sqrt{125} = \frac{\sqrt{5}}{2} - \frac{10}{\sqrt{5}} + \frac{5\sqrt{5}}{1}$$

$$= \frac{5 - 20 + 10 \times 5}{2\sqrt{5}} = \frac{35}{2 \times 2236} = \frac{35}{4.472}$$

#### = 7 826 Ans

3. (D) 
$$\left(\frac{-1}{216}\right)^{-2/3} \Rightarrow \left(\frac{-1}{6^3}\right)^{-2/3} = \left(-\frac{1}{6}\right)^{-2}$$

= 
$$(-6)^2$$
 = **36 Ans.**

- 4. (C) Required measurement
  - = HCF of 403 kg, 434 kg and 465 kg
  - = 31 kg Ans.
- 5. (C) Let R = Age of Randheer,

So, ATQ, 
$$\frac{R-6}{18} = A$$

Given, Mahesh = 5 yrs

$$\Rightarrow \qquad \text{Anup} \qquad = (5-2) \text{ yrs} = 3 \text{ yrs}$$

 $\therefore$  R = 18 × 3 + 6 = **60 yrs Ans** 

- 6. (B) Let *x* be the number of buffaloes and *y* be the number of ducks.
  - Then, total number of legs = 4x + 2y and total number of heads = x + y

So, 
$$4x + 2y = 2(x + y) + 24$$
  
 $\Rightarrow 2x = 24$ 

$$\Rightarrow$$
  $x = 12 \text{ Ans.}$ 

- 7. (A) Cost of 9 lemons =  $4 \times 48$  paise
  - = 144 paise
  - = cost of 4 mangoes

- So, cost of 3 mangoes =  $\frac{144}{4} \times 3$ 
  - = 108 paise
  - = Cost of 5 apples
- $\Rightarrow$  Cost of 9 oranges = 108 paise
- $\Rightarrow$  Cost of 1 orange =  $\frac{108}{9}$

#### = 12 paise Ans.

- 8. (A) Sum of digits from numbers 1 to 10 = 46, Sum of digits from numbers 11 to 20 = 56
  - &Sum of digits from numbers 21 to 29 = 63
  - $\Rightarrow$  Sum of digits of the given numbers = 46 + 56 + 63 = 165

Again,

Sum of digits of the number 165 = 1 + 6 + 5 = 12Now, when 12 is divided by 9, we get remainder = **3 Ans.** 

9. (A) Let x be the number.

Then calculation done by the student

$$=\frac{x+12}{6}=112$$

$$\rightarrow$$
  $r = 660$ 

So, the correct answer =  $\frac{660}{6}$  + 12

#### = 122 Ans

10. (D) Let x be the number of students and w be their average weight. ATQ,

$$\frac{xw+50}{x+1} = w+1$$

Again, 
$$\frac{xw + 50 + 50}{x + 2} = w + 1.5$$

 $\Rightarrow 1.5x + 2w = 97 \qquad \dots$ 

From equations (i) and (ii),

we get, 
$$w = 47 \text{ Ans}$$

11. (A) Let x be the first number

$$\Rightarrow \frac{x + (x + 1) + (x + 2) + (x + 3) + (x + 4)}{5} = 41$$

or, 
$$5x + 10 = 205$$

$$5x = 195$$
$$x = 39$$

- So, Product of A and E =  $x \times (x + 4)$ 
  - $= 39 \times 43$ 
    - = 1677 Ans.



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12. (A) Let Sunil, Sumant and Surat get ₹ x, ₹ y and ₹ z respectively.

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So, 
$$\frac{x \times 5 \times 1}{100} = \frac{y \times 5 \times 2}{100} = \frac{z \times 5 \times 3}{100}$$

$$\Rightarrow$$
  $x = 2y = 3z$ 

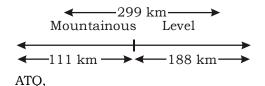
$$\Rightarrow$$
  $x: y: z = 6:3:2$ 

∴ Required difference = 
$$\frac{6-2}{6+3+2} \times 7700$$

#### = ₹ 2800 Ans

13. (C) Let the speed of train on level terrain = x km/h

So, the speed of train through mountainous terrain = (x - 10)km/h



$$\frac{188}{x} + \frac{111}{x - 10} = 7$$

$$\Rightarrow \frac{188x - 1880 + 111x}{x(x - 10)} = 7$$

$$\Rightarrow$$
  $7x^2 - 369x + 1880 = 0$ 

$$\Rightarrow$$
  $x = 47 \text{ km/h Ans.}$ 

14. (D) TV 65% (25%) 40% Newspaper

Number of people who either watch TV or read newspaper = 65% + 40% - 25% = 80%

⇒ Number of people who neither watch TV nor read newspaper.

$$= (100 - 80)\%$$

#### = 20% Ans.

15. (D) Let required amount of second solution to be added = x L So,

$$\frac{15 \times 20 + 5 \times x}{20 + x} = 10$$

$$\Rightarrow 300 + 5x = 20 + 10x$$

$$\Rightarrow x = \frac{100}{5} = 20L \text{ Ans.}$$

16. (A) Milk in mixture

$$= 6 \times \frac{25}{100} + 4 \times \frac{30}{100} = \frac{270}{100}$$

Required percentage = 
$$\frac{270 \times (6+4)}{100}$$

#### = 27% Ans.

17. (B) Let x be the total score in the innings.

So, the highest score = 
$$\frac{2}{9}x$$

And, the next highest score

= 
$$\frac{2}{9}$$
 of the remaining runs

$$=\frac{2}{9}\left(x-\frac{2}{9}x\right)$$

So, ATQ, 
$$\frac{2}{9}x - \frac{2}{9}\left(x - \frac{2}{9}x\right) = 8$$

$$\Rightarrow x - x + \frac{2}{9}x = \frac{8 \times 9}{2}$$

$$\Rightarrow \qquad x = \frac{8 \times 9 \times 9}{2 \times 2}$$

= 162 Ans.

18. (B) 
$$(13 + 22 + 33 + ... 153) - (1 + 2 + 3 + ... + 15)$$

$$= 15 \times \frac{(13+153)}{2} - \frac{15\times16}{2}$$

= 1245 - 120

= 1125 Ans.

19. (B) Let total marks be 100.

So, the minimum marks required to be pass = 40% of 100 = 40 marks

ATQ, Marks obtained by A = 
$$40 - 40 \times \frac{10}{100}$$

= 36 marks

&, Marks obtained by B = 
$$36 - \frac{100}{9} \times \frac{36}{100}$$

$$= 36 - 4$$

So, Marks obtained by C

$$= (36 + 32) - (36 + 32) \times \frac{700}{17 \times 100}$$

$$= 68 - 28 = 40$$
 marks Ans.

20. (B) Let  $\forall x$  be the monthly salary of Mohan. ATQ,

$$\frac{4x}{10} + \frac{6x}{10} \times \frac{50}{100} + \frac{3x}{10} \times \frac{30}{100} + \text{saving} = x$$

$$\Rightarrow \frac{4x}{10} + \frac{3x}{10} + \frac{9x}{100} + 630 = x$$

$$\Rightarrow 630 = \frac{100x - 70x - 9x}{100}$$



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$$\Rightarrow$$
 630 =  $\frac{21x}{100}$ 

 $\Rightarrow$  x = ₹ 3000 Ans

21. (B)  $\cdot$  the total number of men employed = 50 So, total number of wommen employed = 100 & total number of children employed = 150 Now, let the men, women and children wages are 6x, 3x and 2x respectively.

$$\Rightarrow 50 \times 6x + 100 \times 3x + 150 \times 2x = 4500$$

or, 900x = 4500

$$\Rightarrow$$
  $x = 5$ 

- ∴ Per day wages paid to a man, a woman and a child are ₹ 30, ₹ 15 and ₹ 10.
- ∴ Weekly wages paid to a man, a woman and a child are ₹210, ₹105 and ₹70 Ans.
- 22. (B) Let the present and last year salaries of Mahesh and Suresh are x, x' and y, y' respectively.

$$\frac{x'}{y'} = \frac{3}{5}, \frac{x'}{x} = \frac{2}{3}$$

and 
$$\frac{y'}{y} = \frac{4}{5}$$

$$\therefore \frac{\frac{x'}{x}}{\frac{y'}{y}} = \frac{\frac{2}{3}}{\frac{4}{5}}$$

$$\Rightarrow \frac{x'}{y'} \times \frac{y}{x} = \frac{10}{12}$$

$$\Rightarrow \frac{3}{5} \times \frac{y}{x} = \frac{10}{12}$$

$$\Rightarrow \frac{y}{x} = \frac{50}{36}$$

Also, 
$$x + y = 43000$$

$$\Rightarrow x + \frac{50}{36}x = 43000$$

⇒ 
$$x = \frac{43000 \times 36}{86} = ₹ 18000 Ans.$$

23. (D) Actual amount to be paid

$$= 20000 \times \left(1 + \frac{10}{100}\right)^3$$

**=** ₹ 26620

Amount that Rohit have to pay now

$$=20000\left(1+\frac{10}{100}\right)^2\left(1+\frac{15}{100}\right)$$

= ₹ 27830

So, required extra amount

= ₹ 1210 Ans.

24. (A) Let the value of second rate of interest be x% and equal amounts be P each. So, ATQ,

$$P \times \left(1 + \frac{5}{100}\right)^6 = P \times \left(1 + \frac{x}{100}\right)^3$$

$$\Rightarrow \qquad \left(1 + \frac{5}{100}\right)^2 = \left(1 + \frac{x}{100}\right)$$

$$\Rightarrow \frac{105 \times 105}{100 \times 100} = \frac{100 + x}{100}$$

$$\Rightarrow$$
 110.25 = 100 + x

$$x = 10\frac{1}{4}$$
 % Ans

25. (B) Upstream speed = 2 km/h

Downstream speed =  $\frac{1}{10} \times 60 = 6 \text{km/h}$ 

.. Speed in stationary water

$$=\frac{2+6}{2}=4 \text{ km/h}$$

 $\therefore$  Required time =  $\frac{5}{4}$  = 1 hr 15 min Ans.

26. (D) Let the man went up stream for x km.

 $\Rightarrow$  He turned back downstream for (x-2) km.

So, 
$$\frac{x}{(4.5-1.5)} + \frac{x-2}{(4.5+1.5)} = 2 \text{ h } 10 \text{ min}$$

$$\Rightarrow \frac{2x+x-2}{6} = 2\frac{1}{6} \text{ hour}$$

$$\Rightarrow$$
 3x-2 = 13

$$\Rightarrow$$
  $x = 5 \text{ km Ans.}$ 

27. (A) Let x% be the other discount.

So, 
$$65 \times \frac{90}{100} \times \frac{(100 - x)}{100} = 56.16$$

$$\Rightarrow 100 - x = \frac{56.16 \times 100 \times 100}{65 \times 90}$$

$$\Rightarrow$$
 100 –  $x = 96$ 

$$x = 4\%$$
 Ans.

28. (A) Let cost price of the article =  $\forall x$ . So,

$$x \times \frac{117.5}{100} + 11.55 = x \times \frac{92}{100} \times \frac{130}{100}$$



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 $\Rightarrow x = \frac{11.55}{(0.92 \times 130 - 117.5)} \times 100$ 

#### = ₹ 550 Ans.

29. (B) 12.5% of profit = 
$$\frac{12.5}{100}$$
 × 880 = ₹ 110

Remaining  $\stackrel{?}{=}$  770 is divided in the ratio = 5000: 6000 = 5: 6

Profit to Anu = 
$$\frac{5}{11} \times 770 + 110$$
  
= ₹ 460

Profit to Bimla = 
$$\frac{6}{11} \times 770$$
  
= ₹ 420

Required profits are ₹ 460 and ₹ 420 Ans.

30. (B) Ratio to capitals = 
$$\frac{1}{3}$$
 :  $\frac{2}{3}$  = 1 : 2

Ratio of profits 
$$=$$
  $\frac{3}{5}$  :  $\frac{2}{5}$   $=$  3 : 2

Let Y's money was used for x months.

$$(1 \times 9) : (2 \times x) = 3 : 2$$

$$\Rightarrow x = 3$$
 months Ans.

31. (B) A's 1 day work = 
$$\frac{1}{40}$$

So, A's 5 day work = 
$$\frac{1}{40} \times 5 = \frac{1}{8}$$

So, remaining work= 
$$1 - \frac{1}{8} = \frac{7}{8}$$

.. B completed the remaining work in 21 days

So, 1 day's work of B = 
$$\frac{7}{8 \times 21} = \frac{1}{24}$$

$$\Rightarrow$$
 Both (A + B)'s 1 day work =  $\frac{1}{40} + \frac{1}{24}$ 

$$= \frac{3+5}{120} = \frac{8}{120} = \frac{1}{15}$$

Hence, both complete the work in 15 days. Ans.

- 32. (D) Let (A + B) together complete the work in x hours.
  - $\Rightarrow$  A completes the work in (x + 8) days.

& B completes the work in 
$$\left(x + \frac{9}{2}\right)$$
 days.

Using formula, 
$$\frac{(x+8)\left(x+\frac{9}{2}\right)}{2x+\frac{25}{2}} = x$$

$$\Rightarrow x^2 + 8x + \frac{9}{2}x + 36 = 2x^2 + \frac{25}{2}x$$

$$\Rightarrow x^2 = 36 \Rightarrow x = 6$$
 days Ans.

[\* Read days as hours]

33. (C) Let the present population of male and female be x and y respectively.

ATQ, 
$$x + y = 5500$$

and 
$$\frac{111x}{100} + \frac{120y}{100} = 6330$$

$$\Rightarrow$$
 111 $x$  + 120 $y$  = 633000

From equations (i) and (ii), we get

y = 2500 Ans.

34. (C) Let the ouput be x and percentage be a. Then.

$$\therefore x \times \left(1 + \frac{a}{100}\right)^2 = 2x$$

$$\Rightarrow 1 + \frac{a}{100} = \sqrt{2}$$

$$\Rightarrow \frac{a}{100} = \sqrt{2} - 1$$

$$\Rightarrow$$
  $a = (\sqrt{2} - 1) \times 100\%$ 

= 100(
$$\sqrt{2}$$
 - 1)% Ans.

35. (A) Let the cost of the product =  $\sqrt[3]{x}$ . So, ATQ,

$$x \times \frac{110}{100} \times \frac{115}{100} \times \frac{125}{100} = 1265$$

$$\Rightarrow x = 1265 \times \frac{100}{110} \times \frac{100}{115} \times \frac{100}{125}$$

### = ₹ 800 Ans.

36. (C) Total work = 124 × 120 = 14880 men-days Work completed in 64 days

$$= \frac{2}{3} \times 14880 \text{ men-days}$$

Remaining work for remaining 60 days = (14880 – 9920) men-days = 4960 men-days

Now, 
$$: \frac{M_1 D_1}{W_1} = \frac{M_2 D_2}{W_2}$$

$$\therefore \quad \frac{120 \times 64}{9920} = \frac{M_2 \times 60}{4960}$$

$$\Rightarrow$$
  $M_2 = 64$ 

.. Number of workmen who can be reduced = 120 - 64 = 56 Ans.

37. (C) Till 3 pm, part of tank filled

$$=\frac{2}{8}+\frac{1}{12}=\frac{1}{4}+\frac{1}{12}=\frac{4}{12}=\frac{1}{3}$$
 part



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∴ Remaining part =  $1 - \frac{1}{3} = \frac{2}{3}$ 

Now, let *x* be the time taken by all three pipes work to fill the remaining part of tank

$$\left(\frac{1}{8} + \frac{1}{12} - \frac{1}{6}\right)x = \frac{2}{3}$$

$$\Rightarrow \frac{(6+4-8)x}{48} = \frac{2}{3}$$

$$\Rightarrow \frac{2x}{48} = \frac{2}{3} \Rightarrow x = 16 \text{ hour}$$

Hence, the tank will be filled at 1 pm + 16 hour = **5 am. Ans.** 

38. (D) Let leakage alone can empty the full cistern in x h.

Then, 
$$\frac{\frac{9}{2} \times x}{x - \frac{9}{2}} = 5$$

$$\Rightarrow \frac{9}{2}x = 5x - \frac{45}{2}$$

$$\Rightarrow \frac{1}{2}x = \frac{45}{2} \Rightarrow 45 \text{ h Ans.}$$

39. (D) ATQ, original (prime) cost of article = ₹ 6.

⇒ Original raw material cost = ₹ 2

So, New cost of raw material = 
$$2 \times \frac{12}{5}$$

= ₹ 4.80 Also, original manufacturing expenses

= (6-2) = ₹ 4

So, new manufacturing expenses

$$=4 \times \frac{5}{4} = \text{?}5$$

- $\Rightarrow$  New cost of article = 4.80 + 5
  - = ₹ 9.80 Ans
- 40. (A) Let the shares of Anita, Bindu and Champa are 11x, 18x and 24x respectively.

So, 
$$1105 = 11x + 10 + 18x + 20 + 24x + 15$$

$$\Rightarrow$$
 1105 = 53 $x$  + 45

$$\Rightarrow x = 20$$

: Amount received by Champa

$$= 24x + 15$$

$$= 24 \times 20 + 15$$

41. (A) Total marks got by the students in 8 subjects =  $8 \times 57 = 696$  Total marks got by the student in

6 subjects =  $6 \times 85 = 510$ 

⇒ Remaining marks in 2 subjects

Let the highest marks be x, then the second highest marks will be x - 2.

$$x + x - 2 = 186$$

$$\Rightarrow$$
 2x = 188

$$\Rightarrow$$
  $x = 94$ 

- ⇒ Highest marks = **94 Ans.**
- 42. (C) Total score of first three friends

$$= 15 \times 3 = 45$$

and total score of last three friends

$$= 16 \times 3 = 48$$

: Total score of four friends

Score of first friend

$$= 64 - 48 = 16$$

So, required percentage

= 
$$\frac{16}{48} \times 100\%$$
 = 33 $\frac{1}{3}$ % Ans.

43. (B) When a value is first increased and then decreased by the same percentage, then the initial value is always decreased by

$$\frac{x^2}{100}$$
%. (irrespective of initial value)

So, loss percent = 
$$\frac{(15)^2}{100}$$
 = **2.25% Ans.**

44. (B) Let rate of population increase = R\% per annum

So, 
$$4800 = 3600 \left[ 1 + \frac{R}{100} \right]^3$$

$$\Rightarrow \frac{4}{3} = \left[1 + \frac{R}{100}\right]^3 \qquad \dots (i)$$

Now, the population after 3 years

$$=4800\left[1+\frac{R}{100}\right]^3$$

$$=4800 \times \frac{4}{3}$$

= 6400 Ans.

45. (D) Let the two numbers are x and y. Then,

their AM = 
$$\frac{x+y}{2}$$
 = 5

$$\Rightarrow x + y = 10 \qquad \dots (i)$$

and their GM= 
$$\sqrt{xy}$$
 = 4

$$\Rightarrow$$
  $xy = 16$ 

Now, 
$$(x-y)^2 = (x+y)^2 - 4xy$$
  
= 100 - 64 = 36

or, 
$$x - y = 6$$
 ... (ii)



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From equations (i) and (ii),

$$x = 8 \text{ and } y = 2$$

So, the required numbers are 2 & 8 Ans.

46. (B) Let the first term and common term of the AP be *a* and *d* respectively.

ATQ, 
$$(a + 5d) + (a + 14d) = (a + 6d) + (a + 9d) + (a + 11d)$$

- $\Rightarrow$  2a + 19d = 3a + 26d
- $\Rightarrow a + 7d = 0$
- $\Rightarrow$  8th term is **0.** Ans.
- 47. (A) Let M stands for Mohan and R stands for Ram.

**Case : I** 
$$(M + 30) = 2(R - 30)$$
  
 $M - 2R = -90$  ... (i)

**Case : II** 
$$(R + 10) = 3(M - 10)$$
  
  $R - 3M = -40$  ... (ii

Solving Eqs. (i) and (ii), we get

M = 7 34 and 7 62 Ans.

48. (B) Given,

$$\frac{x}{2x+y+z} = \frac{y}{x+2y+z} = \frac{z}{x+y+2z} = a$$

$$x = a(2x + y + z), y = a(x + 2y + z)$$
$$z = a(x + y + 2z)$$

$$\Rightarrow x + y + z = a(4x + 4y + 4z)$$

$$\Rightarrow$$
  $4a = 1 \Rightarrow a = \frac{1}{4}$  Ans.

49. (C) Roots of a quadratic equation

$$ax^2 + bx + c = 0$$
 are real if  $b^2 - 4ac \ge 0$ 

Option (a):  $3x^2 - 4x + 5 = 0$ 

$$b^2 - 4ac = (-4)^2 - 4(3)(5)$$
$$= -44 < 0$$

Hence, roots are not real.

Option (b):  $x^2 + x + 4 = 0$ 

$$b^2 - 4ac = (1)^2 - 4(1)(4)$$
$$= 1 - 16 = -15 < 0$$

Hence, roots are not real.

Option (c): (x-1)(2x-5) = 0

$$\Rightarrow$$
  $x = 1 \text{ and } x = \frac{5}{2} > 0$ 

#### Hence, roots are real.

Option (d): 
$$2x^2 - 3x + 4 = 0$$
  
 $b^2 - 4ac = (-3)^2 - 4(2)(4)$   
 $= 9 - 32 = -23 < 0$ .

Hence, roots are not real. Ans.

50. (C) 
$$2x^2 - 7xy + 3y^2 = 0$$

$$2\left(\frac{x}{y}\right)^2 - 7\left(\frac{x}{y}\right) + 3 = 0$$

$$\therefore \frac{x}{y} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$
$$= \frac{7 \pm \sqrt{49 - 24}}{2 \times 2}$$
$$= \frac{7 \pm 5}{4} = 3, \frac{1}{2}$$

$$\therefore \frac{x}{y} = \frac{3}{1}$$
 and  $\frac{x}{y} = \frac{1}{2}$  Ans.

- 51. (A) Let  $f(x) = 2x^3 ax^2 (2a 3)x + 2$ 
  - $\therefore$  (x + 1) is a factor of the above expression,
    - $\therefore$  Remainder f(-1) = 0

$$\Rightarrow f(-1) = 2(-1)^3 - \alpha(-1)^2 - (2\alpha - 3) \times -1 + 2 = 0$$

$$\Rightarrow$$
  $-2-a+2a-3+2=0$ 

$$\Rightarrow$$
  $a-3=0$ 

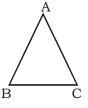
$$a = 3$$
 Ans.

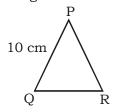
52. (B) Let the common base be x m.

Then, area of triangle = area of parallelogram.

$$\therefore \frac{1}{2} \times x \times \text{Altitude} = x \times 100$$

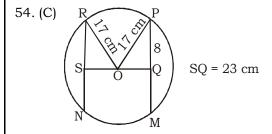
- Altitude = 200 m Ans.
- 53. (D) For two similar triangles ABC and PQR.





$$\frac{AB}{PQ} = \frac{36}{24}$$

⇒ AB = 
$$\frac{36}{24}$$
 × 10 = **15 cm Ans**



In 
$$\triangle$$
 PQO,  
 $(17)^2 = (8)^2 + (OQ)^2$   
 $\therefore (OQ)^2 = 289 - 64 = 225$   
 $OQ = 15$   
 $\therefore OS = 23 - 15 = 8$   
Now in  $\triangle$  ORS,

$$(RS)^2 = (17)^2 - (8)^2$$
$$= 289 - 64 = 225$$



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∴ RS = 15 cm

Hence, length of other chord

$$= 15 \times 2 = 30$$
 cm Ans.

55. (D) Let the three points be  $A\left(0,\frac{8}{3}\right)$ , B(1, 3) and C(82, 30)

Then, AB = 
$$\sqrt{(1-0)^2 + \left(3 - \frac{8}{3}\right)^2} = \frac{\sqrt{10}}{3}$$

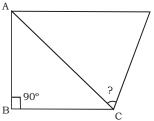
BC = 
$$\sqrt{(82-1)^2 + (30-3)^2}$$
  
=  $\sqrt{6561 + 729}$   
=  $\sqrt{7290} = 27\sqrt{10}$ 

CA = 
$$\sqrt{(82-0)^2 + \left(30 - \frac{8}{3}\right)^2}$$
  
=  $\sqrt{\frac{10 \times (82)^2}{9}} = \frac{82}{3}\sqrt{10}$ 

Now, AB + BC = 
$$\frac{\sqrt{10}}{3}$$
 +  $27\sqrt{10}$  =  $\frac{82\sqrt{10}}{3}$ 

Since, AB + BC = AC, it means points A, B and C are collinear. Ans.

56. (A) Given,  $AD^2 = AB^2 + BC^2 + CD^2$ 



In ∆ABC,

$$AC^2 = AB^2 + BC^2$$
$$AD^2 = AC^2 + CD^2$$

 $\Rightarrow$   $\angle C = 90^{\circ} Ans.$ 

57. (A) Let the length and breadth of a cuboid be 8x cm and 7x cm respectively.

Volume of cuboid =  $l \times b \times h$ 

$$\Rightarrow$$
 1120 = 8 $x \times 7x \times 5$ 

$$\Rightarrow \qquad x^2 = \frac{1120}{8 \times 7 \times 5} = 4$$

$$\Rightarrow x = 2$$

:. Length and breadth of a cuboid are 16 cm and 14 cm by 2 cm.

#### Hence, length exceeds its breadth by 2 cm. Ans.

58. (C) Let length and breadth of blackboard be x m and (x - 8) m respectively. ATQ,  $x \times (x - 8) = (x + 7)(x - 12)$ 

$$\Rightarrow \qquad x^2 - 8x = x^2 - 5x - 84$$

$$\Rightarrow \qquad x = \frac{84}{3} = 28 \text{ cm}$$

Length = 28 cm

Breadth = 
$$x - 8 = 20 \text{ m Ans.}$$

59. (C) Let the outer radius of pipe be r.

$$= \pi \times 28 \times (r^2 - 8^2)$$

$$1496 = \pi \times 28 \times (r^2 - 8^2)$$

$$\Rightarrow r^2 - 64 = \frac{1496}{28 \times 22} \times 7$$

$$28 \times 22$$

$$\Rightarrow r^2 = 17 + 64 = 81$$

$$\Rightarrow r = 9 \text{ cm Ans.}$$

60. (D) Let dimensions of the rectangular stone be 3x, 2x, x respectively.

$$\Rightarrow$$
 3 $x \times 2x \times x = 10368$ 

$$6x^3 = 10368$$

$$x^3 = 1728$$

$$x = 12$$

: Dimensions are 36 dm, 24 dm, 12 dm.

: Entire surface area of a stone.

$$= 2(lb + bh + hl)$$

$$= 2(36 \times 24 + 24 \times 12 + 12 \times 36)$$

$$= 2(864 + 288 + 432)$$

$$= 3168 \, dm^2$$

: Total cost of polishing

$$= 3168 \times 0.02$$

61. (A) Total area of two parks

$$= \pi (8^2 + 6^2) = 100 \pi$$

Area of bigger park

$$= \pi \times 100$$

$$\pi \times r^2 = \pi \times 100$$

$$r^2 = 100$$

$$\therefore$$
  $r = 10 \text{ m Ans}$ 

62. (D) Total area of playground

$$= 750 \times 2 \pi rh$$

$$= 750 \times 2 \times \frac{22}{7} \times \frac{70}{2} \times 150$$

$$= 2475 \times 10^4 \text{ cm}^2$$

$$= 2475 \text{ m}^2$$

 $\therefore$  Total cost of levelling = 2475 × 2

= ₹ 4950 Ans.

63. (C) Since AD bisects  $\angle A$ .

$$\Rightarrow \frac{AB}{AC} = \frac{BD}{DC}$$

$$\Rightarrow \frac{6}{9} = \frac{x}{8-x}$$

$$\Rightarrow$$
 9x = 48 - 6x

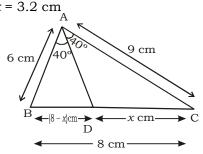
$$\Rightarrow x = \frac{48}{15}$$



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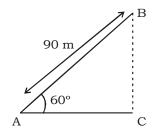
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 $\therefore$  x = 3.2 cm



 $\therefore$  DC = 8 - 3.2 = **4.8** cm Ans.

64. (A)



Let AB be the string.

$$\frac{BC}{AB} = \sin 60^{\circ}$$

$$\Rightarrow$$
 BC = 90 ×  $\frac{\sqrt{3}}{2}$  = 45  $\sqrt{3}$  m Ans.

65. (D) 
$$\cos^6 x + \sin^6 x + 3\sin^2 x \cos^2 x$$
  
= $(\cos^2 x)^3 + (\sin^2 x)^3 + 3\sin^2 x \cos^2 x (\sin^2 x + \cos^2 x)$   
=  $(\cos^2 x + \sin^2 x)^3$   
= **1 Ans.**

66. (A) Given, 
$$a \sec \theta + b \tan \theta = 1$$
 ... (i)

and, 
$$a^2 \sec^2 \theta - b^2 \tan^2 \theta = 5$$
 ... (ii)

From Eqs. (i) and (ii),

$$a \sec \theta - b \tan \theta = 5$$
 ... (iii)

From Eqs. (i) and (iii),

$$a \sec \theta = 3$$
 ... (iv)

b tan 
$$\theta = -2$$
 ... (v)

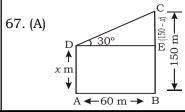
From Eq. (iv),

$$a^2 \sec^2 \theta = 9$$

$$a^2(1 + \tan^2 \theta) = 9$$

$$\Rightarrow \qquad a^2 \left(1 + \frac{4}{b^2}\right) = 9$$

$$\Rightarrow$$
  $a^2b^2 + 4a^2 = 9b^2$  Ans



Let the height of the shorter tower be x m. Then, from  $\triangle$  CDE,

----<u>----</u>

$$\tan 30^{\circ} = \frac{(150 - x)}{60}$$

$$\frac{1}{\sqrt{3}} = \frac{150 - x}{60}$$

$$\therefore \qquad (150 - x) = \frac{60}{\sqrt{3}} = 2\sqrt{3}$$

$$x = 150 - 20\sqrt{3}$$

= 116 m (approx) Ans.

68. (D) 
$$x = 2 + 2^{2/3} + 2^{1/3}$$

The value of x is greater than 2, let us try it for x = 2 and 3.

For 
$$x = 2$$
,  $x^3 - 6x^2 + 6x = -4$ 

For 
$$x = 3$$
,  $x^3 - 6x^2 + 6x = -9$ 

$$x^3 - 6x^2 + 6x < 0$$
 for  $x = 2$  and 3

Hence, option (d) is the answer. Ans.

69. (A) 
$$t-2 = \sqrt[3]{4} + \sqrt[3]{2}$$

$$(t-2)^3 = 4 + 2 + 3\sqrt[3]{4}\sqrt[3]{2}(\sqrt[3]{4} + \sqrt[3]{2})$$

$$\Rightarrow t^3 - 2^3 - 3 \times 2 \times t(t-2) = 6 + 6t - 12$$

$$\Rightarrow$$
  $t^3 - 6t^2 + 6t - 2 = 0$  Ans.

70. (B) Sum of roots = 
$$a + b = 6$$

Product of roots = 
$$a \times b = 6$$

Now, 
$$a^2 + b^2 = (a + b)^2 - 2ab$$

$$= 36 - 12 = 24$$
 Ans.

71. (A) Using AM 
$$\geq$$
 GM

$$\therefore \frac{3^x + 3^{-x}}{2} \ge \sqrt{3^x \cdot 3^{-x}}$$

$$\Rightarrow 3^{x} + 3^{-x} > 2$$
 Ans.

72. (B) 
$$a + b + c = 0$$

$$\Rightarrow a^2 = (b + c)^2$$
 or  $a = -b - c$ 

: Given expression

$$\frac{a^2}{a^2-bc} + \frac{b^2}{b^2-ca} + \frac{c^2}{c^2-ab}$$

$$= \frac{(b+c)^2}{(b+c)^2 - bc} + \frac{b^2}{b^2 + c(b+c)} + \frac{c^2}{c^2 + b(b+c)}$$

$$= \frac{(b+c)^2}{h^2+c^2+hc} + \frac{b^2}{h^2+c^2+hc} + \frac{c^2}{c^2+h^2+hc}$$

$$= \frac{b^2 + c^2 + 2bc + b^2 + c^2}{b^2 + c^2 + bc} = \frac{2(b^2 + c^2 + bc)}{b^2 + c^2 + bc}$$

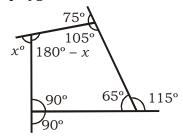
= 2 Ans.



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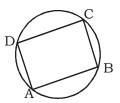
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73. (C) Sum of all the exterior angles of the polygon is 360°.



$$x + 75^{\circ} + 90^{\circ} + 115^{\circ} = 360^{\circ}$$
  
 $x = 80^{\circ} \text{ Ans.}$ 

74. (B)



Given 
$$\angle A = 2 \angle C$$
  
Also,  $\angle A + \angle C = 180^{\circ}$   
(:  $\Box$  ABCD is cyclic)

Now, 
$$\angle B - \angle D = \frac{1}{3} \angle A = 40^{\circ}$$
  
 $\angle B = 110^{\circ}$   
 $\angle D = 70^{\circ}$ 

Minimum difference between any two angles is 10°. Ans.

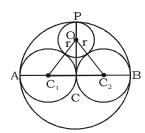
75. (C) Given, 
$$\angle$$
 OBC =  $\angle$  OCB = 37°

[... Angles opposite to equal sides of a triangle are equal]

$$\angle \text{COB} = 180^{\circ} - (37^{\circ} + 37^{\circ})$$
  
= 106°

:. 
$$\angle BAC = \frac{1}{2} \angle COB = \frac{106^{\circ}}{2}$$
  
= **53° Ans.**

76. (C) In  $\triangle OC_1C_2$ ,

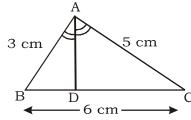


$$(OC_1)^2 = (OC)^2 + (CC_1)^2$$
  
 $\Rightarrow (r+1)^2 = (PC - OP)^2 + 1$ 

$$\Rightarrow (r+1)^2 = (2-r)^2 + 1 \Rightarrow r^2 + 1 + 2r = 4 + r^2 - 4r + 1$$

$$\Rightarrow$$
  $r = \frac{2}{3}$  Ans.

77. (B) 
$$\frac{BD}{AB} = \frac{DC}{AC}$$



$$\therefore \quad \frac{BD}{DC} = \frac{3}{5}$$

$$\therefore$$
 BD : DC = 3 : 5

Now, BD = 
$$\frac{3}{(3+5)} \times 6$$

$$=\frac{18}{8}=\frac{9}{4}=$$
 **2.25 cm Ans.**

78. (C) Area of four walls = 
$$2h(l + b)$$
  
  $l = 2b$  and  $h = 4$  m

$$\Rightarrow$$
  $b = \frac{120}{24} = 5 \text{ and } l = 10$ 

$$\therefore$$
 Area of floor =  $l \times b = 10 \times 5 = 50 \text{ m}^2 \text{Ans.}$ 

New length of rectangle =  $\frac{3}{2}$ L

Initial breadth of rectangle = B

New breadth of rectangle =  $\frac{1}{3}$ B

Initial Area =  $L \times B$ 

New Area = 
$$\frac{3}{2}L \times \frac{1}{3}B = \frac{1}{2}LB$$

## Hence, change in area is $\frac{1}{2}$ . Ans.

80. (D) Let water in the tank is h deep.

$$\therefore 3 \times \frac{3}{2} \times h = 8 \times 2.5$$

$$\Rightarrow h = \frac{8 \times 2.5 \times 2}{3 \times 3} =$$
 **4.44 ft Ans.**

81. (A) Let the water level rises by x m.

$$\Rightarrow$$
 90 × 40 ×  $x$  = 150 × 8

$$\Rightarrow x = \frac{150 \times 8}{90 \times 40} = 0.3333 \text{ m}$$

= 33.33 cm Ans.



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82. (B) Curved Surface Area of 50 pillars

$$= 50 \times 2 \times 3.14 \times \frac{50}{2} \times 400$$

 $= 314 \times 10^4$  sq. cm. = 314 sq. cm.

 $\therefore$  Labour charges = 314 × 0.50

83. (A) Total surface area of remaining solid

= curved surface area of the cylinder + area of base + curved surface area of cone

$$=2\pi rh+\pi r^2+\pi rl$$

$$= 2 \pi \times 8 \times 15 + \pi (8)^{2} + \pi \times 8 \times 17$$

$$= 240 \pi + 64 \pi + 136 \pi$$

- = 440  $\pi$  cm<sup>2</sup> Ans.
- 84. (C) Let the breadth and height of *b* and *h* respectively.

Then, 
$$70 \times 2.2 = 14 \times b$$

$$\Rightarrow$$
  $b = 11 \text{ m}$ 

Also, 
$$14 \times b \times h = 70 \times 11$$

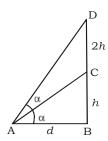
$$h = \frac{70 \times 11}{14 \times 11} =$$
**5m Ans.**

85. (B) Total cost of plastering inner surface

$$= 2 \times \frac{22}{7} \times \frac{7}{2} \times 22.5 \times 3$$

= ₹ 1485 Ans.

86. (C)



Let BC = h be the height of the pillar, then CD = 2h

∴ Also, let  $\angle$  BAC =  $\angle$  CAD =  $\alpha$  and AB = d In  $\triangle$  ABC,

$$\tan \alpha = \frac{h}{d}$$

and in  $\triangle$  ABD,

$$\tan 2\alpha = \frac{3h}{d}$$

$$\Rightarrow \frac{2\tan\alpha}{1-\tan^2\alpha} = \frac{3h}{d}$$

$$\Rightarrow \frac{\frac{2h}{d}}{1 - \left(\frac{h}{d}\right)^2} = \frac{3h}{d}$$

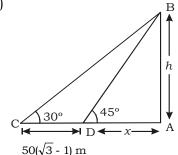
$$\Rightarrow \frac{2}{3} = 1 - \left(\frac{h}{d}\right)^2 \Rightarrow \frac{h}{d} = \frac{1}{\sqrt{3}}$$
 Ans.

87. (D) Given,

$$\frac{\sin A}{\cos A} = \frac{4}{7}$$

$$\therefore \frac{7\frac{\sin A}{\cos A} - 3}{7\frac{\sin A}{\cos A} + 2} = \frac{7 \times \frac{4}{7} - 3}{7 \times \frac{4}{7} + 2} = \frac{4 - 3}{4 + 2} = \frac{1}{6}$$

88. (C)



Distance travelled in 2h, CD =  $50(\sqrt{3} - 1)$  m Let AB be the building and its height be h and AD be x.

$$\frac{h}{x} = \tan 45^{\circ}$$
  $\therefore h = x$  .... (i)

$$\frac{h}{x+50(\sqrt{3}-1)}$$
 = tan 30°

$$\Rightarrow h = \frac{x}{\sqrt{3}} + \frac{50(\sqrt{3} - 1)}{\sqrt{3}}$$
 .... (ii)

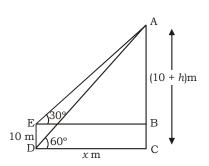
From eqs. (i) and (ii),

$$\Rightarrow h - \frac{h}{\sqrt{3}} = \frac{50(\sqrt{3} - 1)}{\sqrt{3}}$$

$$\Rightarrow h(\sqrt{3}-1) = 50(\sqrt{3}-1)$$

$$\Rightarrow$$
  $h = 50 \text{ m Ans.}$ 

89. (B) Let AB = h m and DC = EB = x m





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Here, pole DE = 10 m

AC = tower = 10 + h

In  $\triangle$  AEB, we have

$$\tan 30^{\circ} = \frac{AB}{EB} = \frac{1}{\sqrt{3}} = \frac{h}{x}$$
 ... (i)

$$\Rightarrow$$
  $x = \sqrt{3}h$ 

In  $\triangle$  ACD, we have,

$$\tan 60^{\circ} = \frac{AC}{CD} = \frac{10+h}{x}$$

$$\Rightarrow \qquad \sqrt{3} = \frac{10+h}{x}$$

$$\therefore \qquad x = \frac{10+h}{\sqrt{3}} \qquad \dots \text{ (ii)}$$

From eqs. (i) and (ii), we get

$$\sqrt{3} h = \frac{10+h}{\sqrt{3}}$$

$$\Rightarrow$$
 3h = 10 + h

$$\Rightarrow \qquad h = 5 \text{ cm}$$

$$h = 5 \text{ cm}$$

$$AC = 10 + h = 15 \text{ m Ans.}$$

[Remember the result in the above : height of tower = 1.5 height of the pole

90. (C) When x = 0

$$\sin x + \csc x = 0 + \infty = \infty$$

When 
$$x = \frac{\pi}{2}$$

$$\sin x + \csc x = 1 + 1 = 2$$

.: When

$$2 \le \sin x + \csc x < \infty$$

Hence,  $\sin x + \csc x \ge 2$  Ans.

91. (C)

Year	Total Sales of all company	Cumulative Sales		
1986	44.50	44.50		
1987	46.00	90.50		
1988	57.00	147.50		
1989	82.00	229.50		
1990	138.00	367.50		

Required ratio = 
$$\frac{90.50}{367.50} = \frac{181}{735} = \frac{1}{4}$$
 **Ans**

92. (A) Average sales of Celia

$$=\frac{18.50+15+16.5+14.5+50}{5}$$

$$=\frac{114.50}{5}$$
 = 22.90 Ans.

93 (A) Growth rate for

Alpha = 
$$\frac{25-20}{20} \times 100 = 25\%$$

Baron = 
$$\frac{15.00 - 11.50}{11.50} \times 100 = 30.43\%$$

Celia = 
$$\frac{50-14.5}{14.5} \times 100 = 244.8\%$$

Dowby = 
$$\frac{48-36}{36} \times 100 = 33.33\%$$

#### Growth is least for Alpha. Ans.

For the year 1986, total sales = 44.594. (B) For the year 1987, total sales = 46 For two years show the closest sales.

95. (A) Required ratio =  $\frac{50}{2}$  = **25** : **1** Ans.

96. (A)	C		who joined = 8550	Candidate who completed MBA = 5700			
		MDA -		IVIDA - 5700			
	A	8550 ×	$\frac{22}{100}$ = 1881	5700 ×	$\frac{18}{100} = 1026$		
	В	8550 ×	$\frac{15}{100}$ = 1282	5700 ×	$\frac{17}{100} = 969$		
	С	8550 ×	$\frac{10}{100}$ = 855	5700 ×	$\frac{13}{100} = 741$		
	D	8550 ×	$\frac{17}{100}$ = 1454	5700 ×	$\frac{16}{100} = 912$		
	Е	8550 ×	$\frac{8}{100} = 684$	5700 ×	$\frac{9}{100} = 513$		
	F	8550 ×	$\frac{12}{100}$ = 1026	5700 ×	$\frac{15}{100} = 855$		
	G	8550 ×	$\frac{16}{100} = 1368$	5700 ×	$\frac{12}{100} = 684$		

Required percentage of

$$A = \frac{1026}{1881} \times 100 = 54.55\%$$

$$B = \frac{969}{1282} \times 100 = 75.59\%$$

$$C = \frac{741}{855} \times 100 = 86.67\%$$

$$D = \frac{912}{1454} \times 100 = 62.72\%$$

$$E = \frac{513}{684} \times 100 = 75\%$$

$$F = \frac{855}{1026} \times 100 = 83.33\%$$

$$G = \frac{684}{1368} \times 100 = 50\%$$

97. (C) Required percentage = 75% Ans. (See solution of last question)

98. (B) Required ratio =  $\frac{684}{1368}$  = **1** : **2** Ans.

Required percentage

$$=\frac{969+741}{1282+855}\times100$$

$$= \frac{1710}{2137} \times 100 = 80\% \text{ Ans.}$$

100. (C) Required difference

$$= (A + D) - (C + E)$$

[Completed – joined]  
= 
$$(1026 + 912) - (855 + 684)$$

- = 1938 1539
- = 399 Ans.



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## SSC MAINS (MATHS) MOCK TEST -12 (ANSWER SHEET)

1.	В	21.	В	41.	Α	61.	Α	8	81.	Α
2.	Α	22.	В	42.	C	62.	D	8	82.	В
3.	D	23.	D	43.	В	63.	C	8	83.	A
4.	C	24.	Α	44.	В	64.	Α	8	84.	C
5.	C	25.	В	45.	D	65.	D	8	85.	В
6.	В	26.	D	46.	В	66.	Α	8	86.	C
7.	Α	27.	Α	47.	Α	67.	Α	8	87.	D
8.	Α	28.	Α	48.	В	68.	D	8	88.	C
9.	Α	29.	В	49.	C	69.	Α	8	89.	В
10.	D	30.	В	50.	C	70.	В	(	90.	C
11.	Α	31.	В	51.	Α	71.	Α	(	91.	C
12.	Α	32.	D	52.	В	72.	В	(	92.	A
13.	C	33.	C	53.	D	73.	C	(	93.	A
14.	D	34.	C	54.	C	74.	В	(	94.	В
15.	D	35.	Α	55.	D	75.	C	(	95.	A
16.	Α	36.	C	56.	Α	76.	C	(	96.	A
17.	В	37.	C	57.	Α	77.	В	(	97.	C
18.	В	38.	D	58.	C	78.	C	(	98.	В
19.	В	39.	D	59.	C	79.	C	(	99.	D
20.	В	40.	Α	60.	D	80.	D		100.	C