



**Centres at:** ★ MUKHERJEE NAGAR ★ MUNIRKA ★ UTTAM NAGAR ★ DILSHAD GARDEN ★ ROHINI ★ BADARPUR BORDER

## SSC MAINS (MATH) MOCK TEST - 4 (SOLUTION)

1. (D) Total no. of marbles kept in 50th box  
= sum of factors of 50  
=  $1 + 2 + 5 + 10 + 25 + 50$   
= 93

2. (C) Let  $x$  be the required number  
and  $a$  be its first part  
so,  $(x - a)$  will be its second part  
Now, A.T.Q,  
 $0.8a = 0.6(x - a) + 3$   
or,  $0.8a + 0.6a = 0.6x + 3$   
or,  $1.4a = 0.6x + 3$

$$\Rightarrow a = \frac{0.6x + 3}{1.4} \quad \text{----- (i)}$$

also

$$0.9a + 6 = 0.8(x - a)$$

$$\text{or, } 0.9a + 0.8a = 0.8x - 6$$

$$\text{or, } 1.7a = 0.8x - 6$$

$$\Rightarrow a = \frac{0.8x - 6}{1.7} \quad \text{----- (ii)}$$

from (i) & (ii) ,

$$\frac{0.6x + 3}{1.4} = \frac{0.8x - 6}{1.7}$$

$$\Rightarrow 1.02x + 5.1 = 1.12x - 8.4$$

$$\Rightarrow 0.1x = 13.5$$

$$\Rightarrow x = \frac{13.5}{0.1} = 135$$

**Alternative method**

$$\frac{4}{5}a = \frac{3}{5}(x - a) + 3$$

$$\Rightarrow \left(\frac{4}{5} + \frac{3}{5}\right)a = \frac{3}{5}x + 3 \quad \text{----- (i)}$$

also  $\frac{9}{10}a + 6 = \frac{4}{5}(x - a)$

$$\Rightarrow \left(\frac{9}{10} + \frac{4}{5}\right)a = \frac{4}{5}x - 6 \quad \text{----- (ii)}$$

from (i) & (ii), we get,

$$\left(\frac{3}{5}x + 3\right) \times \left(\frac{9 + 8}{10}\right) = \left(\frac{4}{5}x - 6\right) \times \left(\frac{4 + 3}{5}\right)$$

$$\text{or, } \frac{51}{50}x + \frac{51}{10} = \frac{28}{25}x - \frac{42}{5}$$

$$\text{or, } \left(\frac{56}{50} - \frac{51}{50}\right)x = \frac{51}{10} + \frac{42}{5}$$

$$\Rightarrow x = \frac{135}{10} \times \frac{50}{5}$$

$$x = 135$$

3. (A) Let the two digit number be  $10y + x$  where  $x > y$

$$\therefore 10x + y - 10y - x = 63$$

$$\Rightarrow 9x - 9y = 63$$

$$\Rightarrow x - y = 7$$

$$\therefore x = 7, 8, 9 \text{ and } y = 0, 1, 2$$

$$\Rightarrow \text{possible values of } x \text{ are } 7, 8, 9$$

4. (A) For every  $n \geq 4$  ;

$n!$  will be divisible by 8

$\Rightarrow$  remainder will be zero

[ because for  $n \geq 4$  , 8 will be a factor of  $n!$  ]

So, remainder of  $1! + 2! + 3! + 4! + \dots + 100!$   
will be equal to the remainder of  $1! + 2! + 3!$   
only

$$1! + 2! + 3! = 1 + 2 + 3 = 9$$

$$\text{and } \frac{9}{8} ; R = 1$$

5. (D) H.C.F. =  $x$  and L.C.M. =  $y$

$$\Rightarrow A \times B = x \times y$$

$$\text{So, } A^3 + B^3 = (A + B)^3 - 3AB(A + B)$$

$$= (x + y)^3 - 3xy(x + y)$$

$$= x^3 + y^3 + 3xy(x + y) - 3xy(x + y)$$

$$= x^3 + y^3$$

6. (A)  $(x)^{\frac{1}{2}} = (y)^{\frac{1}{3}} \Rightarrow (x)^{\frac{1}{1/3}} = (y)^{\frac{1}{1/2}} \Rightarrow (x)^3 = (y)^2$

7. (C) Required average age of 2 persons

$$= \frac{30 + 34 + (8 \times 3)}{2} = 44 \text{ yrs.}$$

8. (\*) Required average age just before the birth of the youngest member

$$= \frac{(10 \times 20) - (10 \times 10)}{10 - 1}$$

$$= \frac{100}{9} = 11.11 \text{ yrs.}$$

9. (C) Weight of first member =  $x$  kg

Weight of second member =  $(x + 2)$

-----

Weight of fifth member =  $(x + 8)$  kg

10. (A) Average speed =  $\frac{\text{Total distance covered}}{\text{Total time taken}}$

$$= \frac{(6 + 8 + 40) \text{ km}}{(15 + 15 + 15) \text{ min}}$$



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$$= \frac{54 \text{ km}}{45 \text{ min}} = \frac{54 \text{ km}}{\frac{45}{60} \text{ hr.}}$$

$$= 72 \text{ km/hr.}$$

11. (C) Age of the captain  
 $= (11 \times 30) - ((5 \times 29) + (5 \times 27))$   
 $= (330 - 280) \text{ yrs.}$   
 $= 50 \text{ yrs.}$

12. (B)  $(2m + 4b) \times 10 = (4m + 5b) \times 6$   
 $\Rightarrow 20m + 40b = 24m + 30b$   
 $\Rightarrow 4m = 10b \Rightarrow 2m = 5b$   
 So,  $5b = 2 \times 40$

$$\Rightarrow b = \frac{2 \times 40}{5} = 16$$

$$\therefore \text{Required ratio} = 40 : 16 = 5 : 2$$

13. (B) **In case I.**  
 Let the number of shirts of brand B be  $x$ .  
 Let the cost of a shirt of brand B be ₹ 1  
 $\therefore$  Original cost  $= 4 \times 2 + x = ₹ (8 + x)$   
**In case II.**

$$4x + 2x = (8 + x) \times \frac{140}{100} = (8 + x) \times \frac{7}{5}$$

$$\Rightarrow 20 + 10x = 56 + 7x$$

$$\Rightarrow 10x - 7x = 56 - 20 = 36$$

$$\Rightarrow 3x = 36 \Rightarrow x = 12$$

$$\therefore \text{Required ratio} = 4 : 12 = 1 : 3$$

14. (C) Half the sum = 18

$$\Rightarrow \text{total sum} = 36$$

$$\Rightarrow \text{Nos. will be } 6, 12 \text{ and } 18$$

$$\text{So, ratio of squares} = 6^2 : 12^2 : 18^2$$

$$= 36 : 144 : 324$$

15. (B) A.T.Q,

$$\frac{A}{6} = \frac{J}{4} = \frac{2}{5}R$$

$$\Rightarrow A : J : R$$

$$= 6 : 4 : \frac{5}{2}$$

$$= 12 : 8 : 5$$

$$\Rightarrow \text{Apoorva's share}$$

$$= \frac{12}{(12 + 8 + 5)} \times 2250$$

$$= \text{Rs. } 1080$$

16. (A) S.P. at 20% profit = Rs. 9/litre

$$\Rightarrow \text{Cost of mixture} = \frac{9}{120} \times 100 = \text{Rs. } 7.5/\text{litre}$$

Now, let the ratio of milk and water in the mixture =  $x : y$

$$\Rightarrow \frac{(10 \times x) + (0 \times y)}{x + y} = 7.5$$

$$\Rightarrow 10x = 7.5(x + y)$$

$$\Rightarrow 2.5x = 7.5y$$

$$\Rightarrow x = 3y$$

$$\Rightarrow x : y = 3 : 1$$

17. (D) Ratio of equivalent capitals of A, B and C for 1 month

$$= (40500 \times 6 + 45000 \times 6) : (45000 \times 12)$$

$$: (60000 \times 6 + 45000 \times 6)$$

$$= (405 + 450) : (450 \times 2) : (600 + 450)$$

$$= 855 : 900 : 1050$$

$$= 171 : 180 : 210$$

$$= 57 : 60 : 70$$

$$\text{Sum the ratios} = 57 + 60 + 70 = 187$$

$$\text{Required difference} = \frac{70 - 57}{187} = 56100$$

$$= \frac{13}{187} \times 56100 = ₹ 3900$$

18. (A) Let the cost price of 1 orange = Re. 1.

$$\therefore \text{C.P. of 1 banana} = \text{Rs. } \frac{3}{4}$$

$$\text{and C.P. of 1 apple} = \text{Rs. } \frac{3}{2}$$

New prices:

$$1 \text{ orange} = \text{Re. } 1.1$$

$$1 \text{ banana} = \frac{3}{4} \times \frac{110}{100} = \text{Rs. } 0.825$$

$$1 \text{ apple} = \frac{3}{2} \times \frac{110}{100} = \text{Rs. } 1.65$$

$\therefore$  Original price of (4 bananas + 2 apples + 3 oranges)

$$= \text{Rs. } (3 + 3 + 3) = \text{Rs. } 9$$

New price of (4 banana + 2 apples + 3 oranges)

$$= \text{Rs. } (4 \times 0.825 + 2 \times 1.65 + 3 \times 1.1)$$

$$= \text{Rs. } (3.3 + 3.3 + 3.3) = 9.9$$

$\therefore$  Percentage increase

$$= \frac{9.9 - 9}{9} \times 100 = 10\%$$

19. (A) Let the no. be  $x$

$$\Rightarrow \% \text{ change}$$

$$= \frac{\text{original result} - \text{changed result}}{\text{original result}} \times 100\%$$

$$= \frac{5x - \frac{x}{5}}{5x} \times 100\%$$

$$= \frac{25x - x}{25x} \times 100\%$$

$$= \frac{24x}{25x} \times 100\% = 96\%$$



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20. (C) 20% decrease in price

⇒ 25% increase in consumption

(when expenditure is constant)

⇒ increased amount of sugar = 25% of 20kg  
= 5 kg

⇒ Total amount now of sugar = (20 + 5) kg  
= 25 kg

21. (C) Votes got by Rahul Gandhi

= (100-10)% of  $\frac{4}{5}$  of total voters

= 90% of  $\frac{4}{5}$  of total voters

=  $\frac{9}{10} \times \frac{4}{5}$  of total voters

=  $\frac{18}{25}$  of total voters

= 216 voters ----- (i)

Now, Votes got by Varun Gandhi

= (100-20)% of  $\left(1 - \frac{4}{5}\right)^{th}$  of the total voters

= 80% of  $\frac{1}{5}^{th}$  of total voters

=  $\frac{4}{5} \times \frac{1}{5}$  of total voters

=  $\frac{4}{25}$  of total voters

=  $\frac{216}{18} \times 4 = 48$  voters

So, total no. of votes polled = (216 + 48) votes  
= 264 votes

22. (C) 10% reduction in price

⇒ 11.11% increase in quantity

(when expenditure is constant)

A.T.Q,

11.11% of original amount of wheat = 50 gm

⇒ Original amount (ie. 100%) of wheat

= (50 × 9) gm

= 450 gm

23. (A) C.P. of each book sold by publisher

=  $\frac{70,000}{2000 - 400}$

= ₹ 43.75

S.P. of each book sold by publisher

= (100-30)% of ₹ 75

= ₹ 52.5

So, % gain =  $\frac{52.5 - 43.75}{43.75} \times 100\%$

(∵ S.P. > C.P.)

= 20% gain

24. (C) If the C.P. of wrist watch be ₹ x then

C.P. of wall clock = ₹ (390 - x)

So,  $\frac{x \times 10}{100} + \frac{(390 - x) \times 15}{100} = 51.50$

⇒  $10x + 5850 - 15x = 5150$

⇒  $5x = 5850 - 5150 = 700$

⇒  $x = \frac{700}{5} = ₹ 140$

∴ C.P. of wall clock = 390 - 140 = ₹ 250

∴ Required difference = 250 - 140 = ₹ 110

25. (A)

∴ (40 - 20)% = Re1

So,  $120\% = \frac{1}{20} \times 120 = ₹ 6$

26. (B) Required Marked price

=  $210 \times \frac{120}{100} \times \frac{100}{(100 - 12.5)}$

=  $210 \times \frac{120}{87.5}$

= ₹ 288

27. (D) Let the C.P. = x

So, S.P. in 1st case = 1.05x

now, C.P. in 2nd case = 0.95x

and S.P. in 2nd case = 1.05x - 2

Now, A.T.Q.  $0.95x \times 1.1 = 1.05x - 2$

or,  $1.045x = 1.05x - 2$

⇒  $1.05x - 1.045x = 2$

⇒  $0.005x = 2$

⇒  $x = \frac{2}{0.005} = 400$

28. (C) Discount on ₹ 36000 =  $\frac{3600 \times 7}{100} = ₹ 2520$

Discount on first ₹ 20,000 =  $\frac{20000 \times 8}{100}$   
= ₹ 1600

Discount on next ₹ 10,000 =  $\frac{10,000 \times 5}{100}$   
= ₹ 500

∴ Discount on remaining ₹ 6,000

= 2520 - (1600 + 500) = ₹ 420

∴ Required percent =  $\frac{420 \times 100}{6000} = 7\%$

29. (B) Net discount given by A

=  $\left(5 + 25 - \frac{5 \times 25}{100}\right)\% = 28.75\%$

& Net discount given by B



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$$= \left( 16 + 12 - \frac{16 \times 12}{100} \right) \% = 26.08\%$$

⇒ A is giving more discount

⇒ it is more profitable to purchase the fan from A.

30.(C) Single equivalent discount =  $\left( p + q - \frac{pq}{100} \right) \%$

31. (A) Required ratio =  $(15 \times 22) : (11 \times 25)$   
 $= 330 : 275$   
 $= 6 : 5$

32. (D) Let Rs.  $x$  = quarterly payment given,  
 $r = 16\%$  per annum  
 So, rate of interest per quarter

$$= \frac{16}{4} = 4\% \text{ per quarter}$$

Also,

No. of quarters in 2 years =  $4 \times 2$   
 $= 8$  quarters

So,

$$8x + (7 + 6 + 4 + 3 + 2 + 1) \times 4\% \text{ of } x = 2280$$

or,  $8x + \left( \frac{7 \times 8}{2} \right) \times 4\% \text{ of } x = 2280$

$$\left[ \because 1 + 2 + 3 + \dots + n = \frac{n(n+1)}{2} \right]$$

or,  $8x + 112\% \text{ of } x = 2280$

or,  $800\% \text{ of } x + 112\% \text{ of } x = 2280$

⇒  $912\% \text{ of } x = 2280$

So,  $x = \frac{2280 \times 100}{912} = ₹ 250$

**Direct Method:-**

Quarterly Payment

$$= \frac{100 \times 2280}{100 \times 8 + \frac{4 \times 8 \times 7}{2}}$$

$$= \frac{100 \times 2280 \times 2}{1600 + 224} = 250$$

33. (D) Let  $x$  be the required annual payment.  
 So, also,  $r = 10\%$  p.a. and  $t = 3$  years

$$\left[ 1 \xrightarrow{+10\%} 1.1 \right]$$

So,  $(1 + 1.1 + 1.21)x = 3310 \times (1.1)^3$

or,  $3.31x = 3310 \times 1.331$

$$x = \frac{3310 \times 1.331}{3.31}$$

= Rs. 1331

**Direct Method:-**

$$\text{Annual payment} = \frac{3310}{\left( \frac{10}{11} + \frac{100}{121} + \frac{1000}{1331} \right)}$$

$$= \frac{3310 \times 1331}{(1210 + 1100 + 1000)}$$

$$= 1331$$

34.(C)  $A = P \left( 1 + \frac{R}{100} \right)^T$

$$\Rightarrow 3 = 1 \left( 1 + \frac{R}{100} \right)^3$$

On squaring both sides,

$$9 = 1 \left( 1 + \frac{R}{100} \right)^6$$

35. (A) Cash price of refrigerator

$$= 1500 + \left( 1020 \times \frac{10}{11} \right) + \left( 1003 + \frac{100}{121} \right)$$

$$+ \left( 990 \times \frac{1000}{1331} \right)$$

$$= 1500 + \left\{ \frac{(10200 \times 121) + (100300 \times 11) + 990000}{1331} \right\}$$

$$= 1500 + \left( \frac{1234200 + 1103300 + 990000}{1331} \right)$$

$$= 1500 + \frac{3327500}{1331}$$

$$= 1500 + 2500$$

$$= 4000$$

**Alternative Method:-**

Cash price of refrigerator

$$= 1500 + \frac{1020}{1.1} + \frac{1003}{(1.1)^2} + \frac{990}{(1.1)^3}$$

$$= 1500 + \frac{1020}{1.1} + \frac{1003}{1.21} + \frac{990}{1.331}$$

$$= 1500 + 2500$$

$$= 4000$$

36. (D) When B works normally then days taken by B to complete the work

$$= \frac{20 \times 12}{20 - 12} \text{ days}$$

$$= 30 \text{ days}$$

Now, If B does the work only half a day daily

⇒ B will take twice the total days to complete the whole work alone

⇒ Now No. of days taken by B

$$= (30 \times 2) \text{ days}$$

$$= 60 \text{ days}$$

So,



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Now days taken by (A + B) together to do the

$$\text{whole work} = \frac{20 \times 60}{20 + 60} = 15 \text{ days}$$

37.(A) Let time taken by B in completing the work = x day

∴ Time taken by A (x - 10) days

$$\therefore \frac{1}{x} + \frac{1}{x-10} = \frac{1}{12}$$

$$\Rightarrow \frac{x-10+x}{x(x-10)} = \frac{1}{12}$$

$$\Rightarrow 24x - 120 = x^2 - 10x$$

$$\Rightarrow x^2 - 34x + 120 = 0$$

$$\Rightarrow x^2 - 30x - 4x + 120 = 0$$

$$\Rightarrow x(x-30) - 4(x-30) = 0$$

$$\Rightarrow (x-4)(x-30) = 0$$

$$\Rightarrow x - 30 \text{ because } x \neq 4$$

38. (C) Let days taken by A to do the whole work = x days

So, days taken by B to do the whole work = (x - 5) days

and, days taken by C to do the whole work = (x - 9) days

Now, ATQ,

Days taken by (A + B) together to do the whole work

= Days taken by C alone to do the whole work

$$\Rightarrow \frac{x(x-5)}{x+(x-5)} = x-9$$

$$\text{or, } x^2 - 5x = (x-9)(2x-5)$$

$$\text{or, } x^2 - 5x = 2x^2 - 5x - 18x + 45$$

$$\text{or, } x^2 - 18x + 45 = 0$$

$$\text{or, } x^2 - 15x - 3x + 45 = 0$$

$$\text{or, } x(x-15) - 3(x-15) = 0$$

$$\text{or, } (x-3)(x-15) = 0 \Rightarrow x = 3 \text{ or } 15$$

but x = 3 is not possible as x - 5 or x - 9 will become negative.

So, x = 15 days

39.(B) Time  $\propto \frac{1}{\text{cross-sectional area of the pipe}}$

$$\text{Time} \propto \frac{1}{\frac{\pi}{4} d^2}$$

$$\text{Time} \propto \frac{1}{d^2}$$

$$\therefore \frac{t_2}{t_1} = \frac{(d_1)^2}{(d_2)^2}$$

$$\text{So, } t_2 = t_1 \left( \frac{d_1}{d_2} \right)^2$$

$$t_1 = 40 \text{ minutes, } d_1 = d, d_2 = 2d$$

$$\therefore t_2 = 40 \left( \frac{d}{2d} \right)^2$$

$$t_2 = 40 \left( \frac{1}{2} \right)^2$$

$$t_2 = 10 \text{ minutes}$$

⇒ time taken by a pipe of diameter 2d for doing the same job = 10 minutes

40.(C) Let the capacity of the tank be x gallons. Quantity of water filled in the tank in 1 minute when all the pipes A, B and C are

$$\text{opened simultaneously} = \frac{x}{20} + \frac{x}{24} - 3$$

$$\text{According to the question, } \frac{x}{20} + \frac{x}{24} - 3 = \frac{x}{15}$$

$$\Rightarrow \frac{x}{20} + \frac{x}{24} - \frac{x}{15} = 3$$

$$\Rightarrow \frac{6x + 5x - 8x}{120} = 3$$

$$\Rightarrow 3x = 3 \times 120$$

$$\Rightarrow x = \frac{3 \times 120}{3} = 120 \text{ gallons}$$

41. (B) Let speed of car = x km/hr.

Here, Distance covered by the car in 27 minutes = Distance covered by the sound in (28 minutes 30 seconds - 27 minutes)

$$\Rightarrow x \text{ km/hr} \times \left( \frac{27}{60} \right) \text{ hr.}$$

$$= \left( 330 \times \frac{18}{5} \text{ km/hr} \right) \times \left( \frac{1.5}{60} \text{ hr} \right)$$

$$\Rightarrow x = 330 \times \frac{18}{5} \times \frac{1.5}{60} \times \frac{60}{27} = 66$$

$$\Rightarrow \text{Speed of car} = 66 \text{ km/hr.}$$

42. (D) In the race between Sonu and Monu.

Distance travelled by Sonu and Monu in same time = 600 mtr. & (600 - 60)mtr = 600 mtr. & 540 mtr.

⇒ In the same time, Ratio of distance travelled by Sonu & Monu = 10 : 9

Similarly,

In the same time, Ratio of distance travelled by Monu & Bablu = 500 : (500 - 25) = 500 : 475 = 20 : 19

So,

In the same time, Ratio of distance travelled by Sonu, Monu & Bablu



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$$= 10 \times 20 : 9 \times 20 : 9 \times 19$$

$$= 200 : 180 : 171$$

⇒ When Sonu travels 200 m, Bablu will travel 171 m

So, When Sonu travels 400 m, Bablu will travel 342 m

⇒ In 400 m race between Sonu & Bablu, Required No. of metres by which Sonu will win the race

$$= 400 \text{ m} - 342 \text{ m}$$

$$= 58 \text{ m}$$

43. (A) Let  $x$  = length of the faster train (in mtr.)

$$\text{So, } 36 \text{ seconds} = \frac{x+10}{(40-20) \text{ kmph}}$$

$$\Rightarrow x = 36 \text{ second} \times 20 \times \frac{5}{18} \text{ m/sec}$$

$$= 200 \text{ mtr.}$$

44. (A) Speed of boat in still water =  $\frac{S_{\text{down}} + S_{\text{up}}}{2}$

$$= \frac{x+y}{2} = 0.5(x+y)$$

45.(C) Expression

$$= 4 + 44 + 444 + \dots \text{ to } n \text{ terms}$$

$$= 4(1 + 11 + 111 + \dots \text{ to } n \text{ terms})$$

$$= \frac{4}{9}(9 + 99 + 999 + \dots \text{ to } n \text{ terms})$$

$$= \frac{4}{9}[(10-1) + (100-1) + (1000-1) + \dots \text{ to } n \text{ terms}]$$

$$= \frac{4}{9}[(10 + 10^2 + 10^3 + \dots \text{ to } n \text{ terms}) - n]$$

$$= \frac{4}{9}[10(1 + 10 + 10^2 + \dots \text{ to } n \text{ terms}) - n]$$

$$= \frac{40}{9} \left( \frac{10^n - 1}{9} \right) - \frac{4}{9}n$$

$$[\because 1 + 10 + 10^2 + \dots \text{ to } n \text{ terms} = \frac{10^n - 1}{9}]$$

$$= \frac{40}{81}(10^n - 1) - \frac{4}{9}n$$

46. (B)  $180 = 2 \times 2 \times 3 \times 3 \times 5$

$$a^3b = abc$$

$$\Rightarrow a^2 = bc$$

$$\therefore a^3b = abc = 180 = 1^2 \times 180 \times 1$$

$$\Rightarrow 1^3 \times 180$$

$$\Rightarrow c = 1$$

47. (C)  $a + b + c = 0$

$$\Rightarrow b + c = -a$$

On squaring both sides, we get

$$(b + c)^2 = a^2$$

$$\Rightarrow b^2 + c^2 = 2bc = a^2$$

$$\Rightarrow a^2 + b^2 + c^2 + 2bc = 2a^2$$

$$\Rightarrow a^2 + b^2 + c^2 = 2a^2 - 2bc$$

$$= 2(a^2 - bc)$$

$$\therefore \frac{a^2 + b^2 + c^2}{a^2 - bc} = \frac{2(a^2 - bc)}{a^2 - bc} = 2$$

48. (D)  $(a-1)\sqrt{2} + 3 = b\sqrt{2} + a$

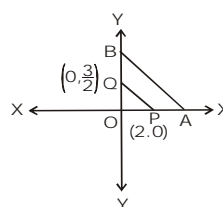
$$\Rightarrow a = 3 : a - 1 = b$$

$$\Rightarrow 3 - 1 : b \Rightarrow b = 2$$

$$\therefore a + b = 3 + 2 = 5$$

49.(B)  $OP = 2$

$$OQ = \frac{3}{2}$$



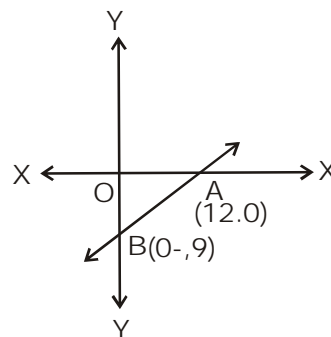
$$\therefore PQ = \sqrt{OP^2 + OQ^2}$$

$$= \sqrt{2^2 + \left(\frac{3}{2}\right)^2}$$

$$= \sqrt{4 + \frac{9}{4}}$$

$$= \sqrt{\frac{16+9}{4}} = \sqrt{\frac{25}{4}} = \frac{5}{2} = 2.5 \text{ cm}$$

50.(A)



Putting  $x = 0$  in  $9x - 12y = 108$ , we get,  $y = -9$

Putting  $y = 0$  in  $9x - 12y = 108$ , we get,  $x = 12$

$$\therefore OA = 12, OB = 9$$

$$\therefore AB = \sqrt{OA^2 + OB^2}$$

$$= \sqrt{12^2 + 9^2}$$

$$= \sqrt{144 + 81}$$

$$= \sqrt{225}$$

$$= 15 \text{ units}$$



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51. (A)  $\left(x + \frac{1}{x}\right)^2 = 3$

$$\Rightarrow x + \frac{1}{x} = \sqrt{3}$$

On cubing both sides.

$$x^3 + \frac{1}{x^3} + 3\left(x + \frac{1}{x}\right) = 3\sqrt{3}$$

$$\Rightarrow x^3 + \frac{1}{x^3} = 3\sqrt{3} - 3\sqrt{3} = 0$$

$$\Rightarrow x^6 + 1 = 0$$

$$\therefore x^{206} + x^{200} + x^{90} + x^{84} + x^{18} + x^{12} + x^6 + 1$$

$$= x^{200}(x^6 + 1) + x^{84}(x^6 + 1) + x^{12}(x^6 + 1) + (x^6 + 1) = 0$$

52. (A)  $\frac{\sqrt{7}}{\sqrt{16+6\sqrt{7}} - \sqrt{16-6\sqrt{7}}}$

$$= \frac{\sqrt{7}}{\sqrt{9+7+2 \times 3 \times \sqrt{7}} - \sqrt{9+7-2 \times 3 \times \sqrt{7}}}$$

$$= \frac{\sqrt{7}}{\sqrt{(3)^2 + (\sqrt{7})^2 + 2 \times 3 \times \sqrt{7}} - \sqrt{(3)^2 + (\sqrt{7})^2 - 2 \times 3 \times \sqrt{7}}}$$

$$= \frac{\sqrt{7}}{\sqrt{(3+\sqrt{7})^2} - \sqrt{(3-\sqrt{7})^2}}$$

$$= \frac{\sqrt{7}}{\sqrt{(3+\sqrt{7})} - \sqrt{(3-\sqrt{7})}} = \frac{\sqrt{7}}{2\sqrt{7}} = \frac{1}{2}$$

53. (B)  $\frac{2x^2 + 3xy + 2y^2}{2x^2 - 3xy + 2y^2} = \frac{2(x^2 + y^2 + 2xy) - xy}{2(x^2 + y^2 - 2xy) + xy}$

$$= \frac{2(x+y)^2 - xy}{2(x-y)^2 + xy} = \frac{2 \times (6)^2 - 1}{2 \times (4\sqrt{2})^2 + 1} = \frac{2 \times 36 - 1}{2 \times 32 + 1}$$

$$= \frac{71}{65}$$

$$\left[ \begin{aligned} \because x &= \frac{\sqrt{2}+1}{\sqrt{2}-1} \text{ and } xy = 1 \Rightarrow y = \frac{1}{x} = \frac{\sqrt{2}-1}{\sqrt{2}+1} \\ \Rightarrow x+y &= \frac{\sqrt{2}+1}{\sqrt{2}-1} + \frac{\sqrt{2}-1}{\sqrt{2}+1} = 6 \\ \text{and } x-y &= \frac{\sqrt{2}+1}{\sqrt{2}-1} - \frac{\sqrt{2}-1}{\sqrt{2}+1} = 4\sqrt{2} \end{aligned} \right.$$

54. (D)  $\frac{x}{2a} = \frac{2b}{a+b}$

Apply C & D,

$$\frac{x+2a}{x-2a} = \frac{a+3b}{b-a} \quad \dots (1)$$

Again,

$$\frac{x}{2b} = \frac{2a}{a+b}$$

Apply C & D,

$$\frac{x+2b}{x-2b} = \frac{3a+b}{a-b} \quad \dots (2)$$

Now,

$$\frac{x+2a}{x+2b} + \frac{x+2b}{x-2b} = \frac{a+3b}{-(a-b)} + \frac{3a+b}{a-b}$$

$$= \frac{-a-3b+3a+b}{a-b}$$

$$= \frac{2a-2b}{a-b} = 2$$

55. (C)  $\left(\frac{1}{\cos \theta} + \frac{1}{\cot \theta}\right) \left(\frac{1}{\cos \theta} - \frac{1}{\cot \theta}\right)$

$$= \left(\frac{1}{\cos \theta} + \frac{\sin \theta}{\cos \theta}\right) \left(\frac{1}{\cos \theta} - \frac{\sin \theta}{\cos \theta}\right)$$

$$= \left(\frac{1+\sin \theta}{\cos \theta}\right) \left(\frac{1-\sin \theta}{\cos \theta}\right)$$

$$= \frac{1-\sin^2 \theta}{\cos^2 \theta} = \frac{\cos^2 \theta}{\cos^2 \theta} = 1$$

56. (C)  $\frac{9}{\operatorname{cosec}^2 \theta} + 4 \cos^2 \theta + \frac{5}{1+\tan^2 \theta}$

$$= 9 \sin^2 \theta + 4 \cos^2 \theta + \frac{5}{\sec^2 \theta}$$

$$= 5 \sin^2 \theta + 4 \sin^2 \theta + 4 \cos^2 \theta + 5 \cos^2 \theta$$

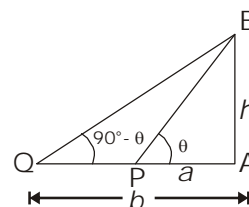
$$= 5(\sin^2 \theta + \cos^2 \theta) + 4(\sin^2 \theta + \cos^2 \theta)$$

$$= (5 \times 1) + (4 \times 1)$$

$$= 5 + 4$$

$$= 9$$

57. (A)



here,  $h$  = height of tower AB

$$\tan \theta = \frac{h}{a} \quad \dots (i)$$

$$\tan(90^\circ - \theta) = \frac{h}{b}$$



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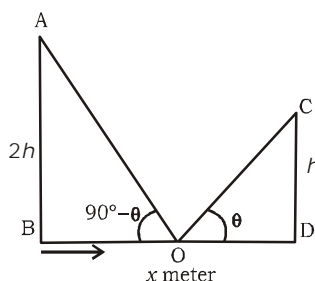
$$\text{or, } \cot \theta = \frac{h}{b}$$

$$\Rightarrow \tan \theta = \frac{b}{h} \text{ ----- (ii)}$$

from (i) and (ii),

$$\frac{h}{a} = \frac{b}{a} \Rightarrow h = \sqrt{ab}$$

58.(A) CD = h metre, AB = 2h metre



$$OB = OD = \frac{x}{2} \text{ metre}$$

From  $\triangle OCD$ ,

$$\tan \theta = \frac{h}{\frac{x}{2}} = \frac{2h}{x} \text{ ----- (i)}$$

From  $\triangle OAB$ ,

$$\tan (90^\circ - \theta) = \frac{AB}{BO}$$

$$\Rightarrow \cot \theta = \frac{2h}{\frac{x}{2}} = \frac{4h}{x} \text{ ----- (ii)}$$

Multiplying both equations,

$$\tan \theta \cdot \cot \theta = \frac{2h}{x} \times \frac{4h}{x}$$

$$\Rightarrow x^2 = 8h^2$$

$$\Rightarrow h = \frac{x}{2\sqrt{2}} \text{ meter}$$

59. (C)  $\tan 2\theta \cdot \tan 3\theta = 1$

$$\Rightarrow \tan 3\theta = \frac{1}{\tan 2\theta} = \cot 2\theta$$

$$\Rightarrow \tan 3\theta = \tan (90^\circ - 2\theta)$$

$$\Rightarrow 3\theta = 90^\circ - 2\theta \Rightarrow 5\theta = 90^\circ$$

$$\Rightarrow \theta = 18^\circ$$

$$\therefore 2\cos^2 \frac{5\theta}{2} - 1 = 2\cos^2 45^\circ - 1$$

$$= 2 \times \frac{1}{2} - 1 = 0$$

$$60.(B) \sin 17^\circ = \frac{x}{y}$$

$$\cos 17^\circ = \sqrt{1 - \sin^2 17^\circ}$$

$$= \sqrt{1 - \frac{x^2}{y^2}} = \sqrt{\frac{y^2 - x^2}{y^2}}$$

$$= \sqrt{\frac{y^2 - x^2}{y^2}}$$

$$\therefore \sec 17^\circ = \frac{y}{\sqrt{y^2 - x^2}}$$

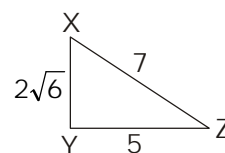
$$\sin 73^\circ = \sin (90^\circ - 17^\circ) = \cos 17^\circ$$

$$\therefore \sec 17^\circ = \sin 73^\circ$$

$$= \frac{y}{\sqrt{y^2 - x^2}} = \frac{\sqrt{y^2 - x^2}}{y}$$

$$= \frac{y^2 - y^2 + x^2}{y\sqrt{y^2 - x^2}} = \frac{x^2}{y\sqrt{y^2 - x^2}}$$

61.(B)



$$XZ - YZ = 2 \text{ ----- (i)}$$

$$\Rightarrow XY^2 + YZ^2 = XZ^2$$

$$\Rightarrow (2\sqrt{6})^2 = XZ^2 - YZ^2$$

$$\Rightarrow 24 = (XZ - YZ)(XZ + YZ)$$

$$\Rightarrow XZ + YZ = 12 \text{ ----- (ii)}$$

Adding both the equations,

$$2 \times Z = 14 \Rightarrow XZ = 7 \therefore YZ = 7 - 2 = 5$$

$$\therefore \sec X = \frac{7}{2\sqrt{6}}$$

$$\tan X = \frac{5}{2\sqrt{6}}$$

$$\therefore \sec X + \tan X = \frac{7}{2\sqrt{6}} + \frac{5}{2\sqrt{6}} = \frac{12}{2\sqrt{6}} = \sqrt{6}$$

62. (A) Angles of triangle

$$\Rightarrow (a - d)^\circ, a^\circ, (a + d)^\circ$$

$$\therefore a - d + a + a + d = 180^\circ$$

$$\Rightarrow 3a = 180^\circ \Rightarrow a = 60^\circ$$

$$\therefore \frac{a - d}{a + d} = \frac{60}{\pi} = \frac{60}{180} = \frac{1}{3}$$

$$\Rightarrow \frac{60 - d}{60 + d} = \frac{1}{3}$$

$$\Rightarrow 180 - 3d = 60 + d$$

$$\Rightarrow 4d = 120^\circ \Rightarrow d = 30^\circ$$

$$a - d = 60^\circ - 30^\circ = 30^\circ$$

$$a = 60^\circ$$

$$a + d = 60^\circ + 30^\circ = 90^\circ$$





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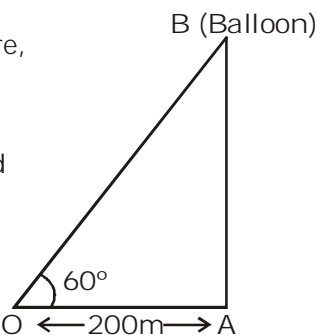
So, Angles of triangle are  $30^\circ, 60^\circ$  and  $90^\circ$

63. (A)

In the given figure, after leaving the point A, balloon reach to point B vertically upward in 1.5 min

Here, O  $\rightarrow$  the observer

So,  $\angle BOA = 60^\circ$  (Observer)



$$\Rightarrow \tan 60^\circ = \frac{AB}{OA}$$

$$\Rightarrow AB = OA \tan 60^\circ = 200 \times \sqrt{3} \text{ m}$$

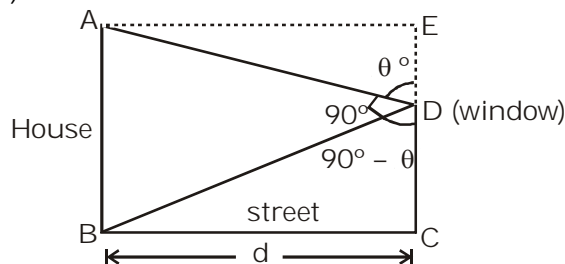
So, speed of the balloon

$$= \frac{\text{distance}}{\text{time}}$$

$$= \frac{AB}{\text{time to reach from A to B}}$$

$$= \frac{200\sqrt{3} \text{ m}}{\frac{1.5}{60} \text{ sec}} = 3.87 \text{ m/sec.}$$

64. (C)



Here,

AB  $\rightarrow$  height of the house  
& CD  $\rightarrow$  height of the window

So, ATQ,

$$\angle ADB = 90^\circ$$

Also,

here, line AD makes an angle  $\theta^\circ$  with the vertical line DE.

$$\Rightarrow \angle ADE = \theta^\circ \text{ also, } \Rightarrow \angle BDC = 90^\circ - \theta$$

In  $\triangle BCD$ ,

$$\tan(90^\circ - \theta) = \frac{BC}{CD} = \frac{d}{CD} \text{ or, } \cot \theta = \frac{d}{CD}$$

$$\Rightarrow CD = \frac{d}{\cot \theta} = d \tan \theta$$

also,

In  $\triangle ADE$ ,

$$\tan \theta = \frac{AE}{DE} = \frac{d}{DE} \Rightarrow DE = \frac{d}{\tan \theta} = d \cot \theta$$

So, the height of the house,

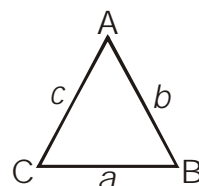
$$AB = CD + DE$$

$$= d(\tan \theta + \cot \theta)$$

$$= d \left( \frac{\sin \theta}{\cos \theta} + \frac{\cos \theta}{\sin \theta} \right) = d \left( \frac{1}{\cos \theta \times \sin \theta} \right)$$

$$= d \sec \theta \operatorname{cosec} \theta$$

65. (A)



Let ABC is a  $\Delta$  and a, b & c are the lengths of BC, CA & AB respectively.

$$\therefore \sin A : \sin B : \sin C = 1 : 1 : \sqrt{2}$$

**By sine formula:**

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$\Rightarrow a : b = \sin A : \sin B \text{ \& } b : c = \sin B : \sin C$$

$$\Rightarrow a : b : c = 1 : 1 : \sqrt{2}$$

$$\text{Let } a = x, b = x \text{ \& } c = \sqrt{2} x$$

ATQ,

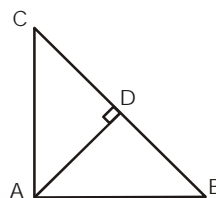
$$\begin{aligned} c^2 : (a^2 + b^2) &= (\sqrt{2}x)^2 : (x^2 + x^2) \\ &= 2x^2 : 2x^2 \\ &= 1 : 1 \end{aligned}$$

66. (B) In  $\Delta$ s ACD and ABC.

$$\angle CDA = \angle CAB = 90^\circ$$

$$\therefore \angle C \text{ is common.}$$

$$\therefore \triangle ACD \sim \triangle ABC$$



$$\therefore \frac{\triangle ACD}{\triangle ABC} = \frac{AC^2}{BC^2}$$

$$\Rightarrow \frac{10}{40} = \frac{9^2}{BC^2}$$

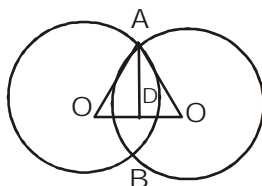
$$\Rightarrow BC^2 = 4 \times 9^2$$

$$\therefore BC = 2 \times 9 = 18 \text{ cm}$$



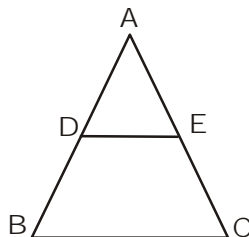
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67.(B)



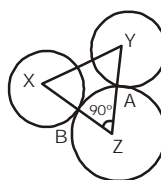
$$\begin{aligned} OD &= \sqrt{15^2 - 12^2} \\ &= \sqrt{225 - 144} \\ &= \sqrt{81} = 9 \\ OD &= \sqrt{13^2 - 12^2} \\ &= \sqrt{169 - 144} = \sqrt{25} = 5 \\ \therefore OO' &= 9 + 5 = 14 \text{ cm} \end{aligned}$$

68. (B)



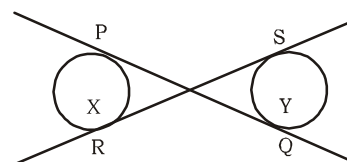
$$\begin{aligned} DE &\parallel BC \\ \angle ADE &= \angle ABC \\ \angle AED &= \angle ACB \\ \therefore \triangle ADE &\sim \triangle ABC \\ \therefore \frac{\square BDEC}{\triangle ADE} &= \frac{1}{1} \\ \Rightarrow \frac{\square BDEC}{\triangle ADE} + 1 &= 1 + 1 \\ \Rightarrow \frac{\triangle ABC}{\triangle ADE} &= 2 = \frac{AB^2}{AD^2} \\ \Rightarrow \frac{AB}{AD} &= \sqrt{2} \\ \Rightarrow \frac{AB}{AD} - 1 &= \sqrt{2} - 1 \\ \Rightarrow \frac{BD}{AD} &= \sqrt{2} - 1 \\ \Rightarrow \frac{AD}{BD} &= \frac{1}{\sqrt{2} - 1} \\ AD : BD &= 1 : \frac{1}{\sqrt{2} - 1} \end{aligned}$$

69.(B)  $XZ = r + 9$  &  $YZ = r + 2$



$$\begin{aligned} \therefore XY^2 &= XZ^2 + YZ^2 \\ \Rightarrow 17^2 &= (r+9)^2 + (r+2)^2 \\ \Rightarrow 289 &= r^2 + 18r + 81 + r^2 + 4r + 4 \\ \Rightarrow 2r^2 + 22r + 85 - 289 &= 0 \\ \Rightarrow 2r^2 + 22r - 204 &= 0 \\ \Rightarrow r^2 + 11r - 102 &= 0 \\ \Rightarrow r^2 + 17r - 6r - 102 &= 0 \\ \Rightarrow r(r+17) - 6(r+17) &= 0 \\ \Rightarrow (r-6)(r+17) &= 0 \\ \Rightarrow r &= 6 \text{ cm} \end{aligned}$$

70.(A)



Length of transverse tangent

$$\begin{aligned} &= \sqrt{XY^2 - (r_1 + r_2)^2} \\ \Rightarrow 8 &= \sqrt{XY^2 - 9^2} \\ \Rightarrow 64 &= XY^2 - 81 \\ \Rightarrow XY^2 &= 64 + 81 = 145 \\ \Rightarrow XY &= \sqrt{145} \end{aligned}$$

71. (C)  $\therefore AB$  is diameter

$$\begin{aligned} \Rightarrow \angle ADB &= 90^\circ \\ \text{also } DO &\perp AB \text{ at 'O', the centre of the circle.} \\ \therefore \triangle ADO &\cong \triangle BDO \text{ (by SAS cong. Rule)} \\ \Rightarrow AD &= DB \text{ (by CPCT)} \\ \therefore \angle DAB &= \angle ABD = 45^\circ \\ \text{But } \angle ACD &= \angle ABD \text{ (angles in the same segment of a circle)} \\ &= 45^\circ \end{aligned}$$

72. (A)  $\angle CAD = \angle CBD$  (Angles in the same segment of a circle)  
 $= 60^\circ$

$$\begin{aligned} \text{Now } \angle BAD &= \angle BAC + \angle CAD \\ &= 30^\circ + 60^\circ = 90^\circ \end{aligned}$$

$$\begin{aligned} \text{Now } \angle BAD + \angle BCD &= 180^\circ \\ (\because \square ABCD &\text{ is cyclic}) \end{aligned}$$

$$\begin{aligned} \Rightarrow 90^\circ + \angle BCD &= 180^\circ \\ \Rightarrow \angle BCD &= 180^\circ - 90^\circ = 90^\circ \end{aligned}$$

73. (A) Perimeter of the rope

$$\begin{aligned} &= 3 \times \left(\frac{1}{3} \text{ of circumference of a circle}\right) + \\ &\quad 3 \times \text{diameter of a circle} \end{aligned}$$



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$$= 3 \times \frac{1}{3} \times 2\pi + 3 \times 2$$

$$= 2\pi + 6$$

74. (A)  $\therefore DC \parallel AB$  (given)

$\Rightarrow \triangle AOB \sim \triangle COD$  (by AA similarity)

$$\Rightarrow \frac{ar(\triangle AOB)}{ar(\triangle COD)} = \frac{AB^2}{DC^2}$$

$$= \frac{(3DC)^2}{DC^2} = \frac{9DC^2}{DC^2} = \frac{9}{1}$$

75. (B) In the given figure,  $\triangle ABC$  is a right angle triangle, where  $\angle B = 90^\circ$

AE, BD and CF are the 3 medians

Now, AB = 12 cm, BC = 9 cm & AC = 15 cm

So, here,

$$BD = \frac{1}{2} AC \Rightarrow BD^2 = \frac{1}{4} AC^2$$

$$\Rightarrow AE^2 + CF^2 = \frac{5}{4} AC^2$$

also,

$$\Rightarrow BD^2 + AE^2 + CF^2 = \left(\frac{1}{4} + \frac{5}{4}\right) AC^2$$

$$= \frac{6}{4} AC^2 = \frac{6}{4} \times 225 = 337.5 \text{ cm}$$

76. (A) Let x unit be the side of the square.

its diagonal =  $\sqrt{2}$  x unit

$A_1$  : Area of the square =  $x^2$  sq. unit

$A_2$  : Area of the equilateral  $\Delta$  described on the diagonal of the square.

$$= \frac{\sqrt{3}}{4} \times (\sqrt{2}x)^2 \text{ sq. unit}$$

$$= \frac{\sqrt{3}}{4} \times 2x^2 \text{ sq. unit}$$

$$\Rightarrow \frac{A_2}{A_1} = \frac{\frac{\sqrt{3}}{4} \times 2x^2}{x^2} = \frac{\sqrt{3}}{2}$$

$$\Rightarrow A_2 : A_1 = \sqrt{3} : 2$$

77. (A)  $d_m$  : diameter of the moon

$d_e$  : diameter of the earth

$$\text{Case I, } \therefore d_m = \frac{1}{4} d_e$$

Let r unit be the radius of the earth.

$$\text{then, } d_m = \frac{1}{4} 2r = \frac{r}{2} \text{ unit}$$

$$R_m : \text{radius of the moon} = \frac{\frac{r}{2}}{2} = \frac{r}{4} \text{ unit}$$

$$\frac{V_e}{V_m} = \frac{\frac{4}{3}\pi r^3}{\frac{4}{3}\pi \left(\frac{r}{4}\right)^3} = 64 : 1$$

78. (B) Perimeter =  $2(l + b)$

$$P = 2(l + w)$$

$$\frac{P}{2} - w = l$$

its area =  $l \times b$

$$k = \left(\frac{P}{2} - w\right) \times w$$

$$\Rightarrow 2k = Pw - 2w^2$$

$$\Rightarrow 2w^2 - Pw + 2k = 0$$

79. (C) Volume of the ice-cream in cylindrical

$$\text{container} = \pi r^2 h = \frac{22}{7} \times 6 \times 6 \times 15 \text{ cm}^3$$

Let r cm be the radius of the cone,

its height = 4r cm

Volume of 1 cone with hemispherical top

$$= \frac{1}{3} \pi r^2 h + \frac{2}{3} \pi r^3$$

$$= \frac{1}{3} \pi r^2 \times 4r + \frac{2}{3} \pi r^3$$

$$= \frac{4}{3} \pi r^3 + \frac{2}{3} \pi r^3$$

$$= \frac{6}{3} \pi r^3 = 2\pi r^3$$

$$V. \text{ of 10 such cones} = 10 \times 2\pi r^3 \text{ cm}^3$$

ATQ,

$$\frac{22}{7} \times 6 \times 6 \times 15 = 10 \times 2\pi r^3$$

$$\frac{22}{7} \times 6 \times 6 \times 15 = 10 \times 2 \times \frac{22}{7} \times r^3$$

$$\Rightarrow r^3 = \frac{6 \times 6 \times 15}{10 \times 2} = \frac{6 \times 6 \times 6}{2 \times 2 \times 2}$$

$$\Rightarrow r = \frac{6}{2} \text{ cm} = 3 \text{ cm}$$

80. (\*) figure is not getting matched with the question asked.



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81. (A) Area of rectangular field =  $\frac{1000}{\frac{1}{4}} \text{ m}^2$   
 $= 4000 \text{ m}^2$

∴ breadth = 50 m

∴ Length =  $\frac{4000}{50} = 80 \text{ m}$

New length of field =  $(80+20) \text{ m} = 100 \text{ m}$

New area =  $100 \times 50 = 5000 \text{ sq. m}$

∴ Required expenditure =  $\left(5000 \times \frac{1}{4}\right) = 1250$

82. (C) Increase in water level

$$= \frac{\text{Volume of sphere}}{\text{Area of base of cylinder}}$$

$$= \frac{\frac{4}{3} \pi r^2}{\pi r^2} = \frac{4}{3} r = \frac{4}{3} \times 3.5 = \frac{14}{3} \text{ cm.}$$

∴ Required water level

$$= 7 - \frac{14}{3} = \frac{7}{3} \text{ cm}$$

83. (A) Curved surface of cylinder =  $2 \pi rh$

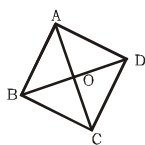
**Case II**

Radius =  $\frac{1}{3}r$  : height =  $6h$

Curved surface =  $2 \pi \times \frac{1}{3}r \times 6h = (2 \pi rh) \times 2$

∴ Increase will be twice.

84. (A) BO = 4 units: OC = 3 units &  $\angle BOC = 90^\circ$



∴ BC =  $\sqrt{4^2 + 3^2} = 5 \text{ units}$

∴ BC<sup>2</sup> = 25 sq. units

85. (A)  $\frac{2}{3} \pi r^3 = 19404$

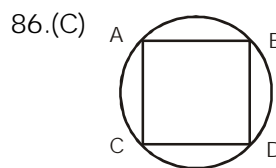
$$\Rightarrow \frac{2}{3} \times \frac{22}{7} \times r^3 = 19404$$

$$\Rightarrow r^3 = \frac{19404 \times 3 \times 7}{2 \times 22} = 9261$$

$$\Rightarrow r = \sqrt[3]{21 \times 21 \times 21} = 21 \text{ cm}$$

∴ Total surface area =  $3 \pi r^2$

$$= 3 \times \frac{22}{7} \times 21 \times 21 = 4158 \text{ sq. cm}$$

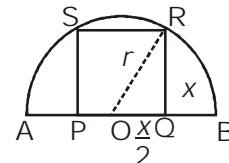


BD = Diagonal = 16 cm

Area of square =  $\frac{1}{2} \times BD^2$

$$= \frac{1}{2} \times 16 \times 16 = 128 \text{ sq. cm.}$$

87. (A) Let 'r' be the radius of the semi-circle and 'x' be the side of the inscribed square.



In  $\triangle OQR$ ,

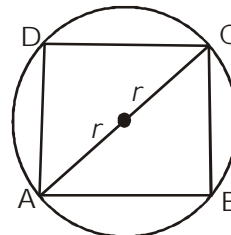
$$r^2 = x^2 + \left(\frac{x}{2}\right)^2$$

$$r^2 = \frac{5}{4} x^2$$

$$\Rightarrow x^2 = \frac{4}{5} r^2$$

∴ Area of the square =  $\frac{4r^2}{5} \text{ sq. unit}$

Again, let 'y' be side of the square inscribed in the circle of same radius.



$$\left[ \begin{aligned} \because 2r &= \sqrt{2}y \\ \Rightarrow y &= \frac{2r}{\sqrt{2}} \end{aligned} \right]$$

Area of the square =  $y^2$

$$= \left(\frac{2r}{\sqrt{2}}\right)^2 \text{ sq. unit}$$

$$= 2r^2 \text{ sq. unit}$$

Required ratio =  $\frac{4r^2}{5} : 2r^2$

$$= 2r^2 \left[ \frac{2}{5} : 1 \right]$$

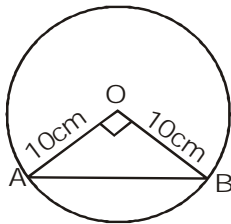
$$= 2r^2 [2 : 5]$$

$$= 2 : 5$$



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88. (A)



Area of the minor segment  
= sector area OABO – area of  $\Delta$  OAB

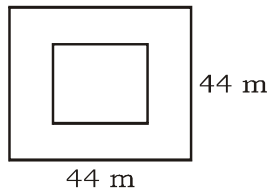
$$= \frac{3.14 \times 10 \times 10 \times 90^\circ}{360^\circ} - \frac{1}{2} \times 10 \times 10$$

$$= \frac{314}{4} - 50 = 78.5 - 50 = 28.5 \text{ cm}^2$$

Area of the major segment  
= area of circle – area of minor segment  
=  $3.14 \times 10 \times 10 - 28.5$   
=  $314 - 28.5 = 285.5 \text{ cm}^2$

$$\therefore \text{Required difference} = 285.5 - 28.5 = 257 \text{ cm}^2$$

89. (C)



Total area of the square field  
=  $(44 \times 44) \text{ m}^2 = 1936 \text{ m}^2$

At the rate of Re. 1 per sq. mtr; the total cost would be Rs. 1936,

but the total cost = Rs. 3536

$$\text{Difference} = \text{Rs. } 3536 - \text{Rs. } 1936 = \text{Rs. } 1600$$

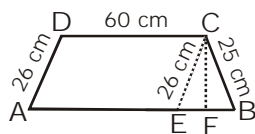
$\Rightarrow$  Rs. 1600 would be the extra cost on the flower bed and as the extra cost on the flower bed is Rs. 1 per sq. mtr.

$$\Rightarrow \text{Area of flower bed} = 1600 \text{ sq. mtr.}$$

$$\Rightarrow \text{Side of flower bed} = \sqrt{1600} \text{ m}^2 = 40 \text{ m}$$

$$\text{So, width of the gravel path} = \frac{44 - 40}{2} = 2 \text{ metre}$$

90. (B)



□ ABCD is a trapezium.

Draw  $CE \parallel DA$  intersecting AB at E.

$\Rightarrow$  □ ABCE is a || gm.

$\Rightarrow DA = CE = 26 \text{ cm.}$

In  $\Delta$  BCE

$$S = \frac{17 + 25 + 26}{2} = \frac{68}{2} = 34$$

$$\text{ar}(\Delta BCE) = \sqrt{34(34 - 17)(34 - 25)(34 - 26)} \text{ cm}^2$$

$$= \sqrt{34 \times 17 \times 9 \times 8}$$

$$= \sqrt{2 \times 17 \times 17 \times 3 \times 3 \times 2 \times 2 \times 2}$$

$$= 2 \times 2 \times 3 \times 17$$

$$= 204 \text{ cm}^2$$

$$\Rightarrow \frac{1}{2} \times BE \times \text{height} = 204$$

$$\text{or, } \frac{1}{2} \times 17 \times CM = 204$$

$$\Rightarrow CM = \frac{204 \times 2}{17} = 24 \text{ cm}$$

$$\text{ar(Trap. ABCD)} = \frac{1}{2} \times (60 + 77) \times 24$$

$$= \frac{1}{2} \times 137 \times 24$$

$$= 1644 \text{ sq. cm.}$$

$$91.(C) \text{ Required number of persons} = 450 + 250 + 150 + 75 + 50 + 25 = 1000$$

$$92.(B) \text{ Required answer} = 250 + 150 = 400$$

$$93.(C) \text{ Required ratio} = 250 : 75 = 10 : 3$$

$$94.(B) \text{ Age group } 15 - 20 \Rightarrow \frac{450}{500} = \frac{9}{10}$$

$$95.(D) \text{ Required percentage} = \frac{25}{500} \times 100 = 5\%$$

$$96. (D) \text{ Expenditure on clothing \& miscellaneous} = (20 + 30)\% \text{ of } 25000 = \text{Rs. } 12500$$

$$97. (C) \text{ Total expenditure} = \frac{15000}{(10 + 20)} \times 100 = \text{Rs. } 50,000$$

$$98. (D) \therefore 360^\circ = 100\%$$

$$\Rightarrow 54^\circ = \frac{54}{3.6} \% = 15\%$$

and among the options the two items having difference of 15% (and hence  $54^\circ$ ) are miscellaneous and Food

$$99. (B) \text{ Required \% age} = \frac{15 - 10}{15} \times 100\%$$

$$= \frac{1}{3} \times 100\% = 33.33\%$$

$$100. (D) 90^\circ = \frac{90}{3.6} \% = 25\%$$

and among the options the two items making central angle of  $90^\circ$ , together, are travelling and entertainment.



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**SSC MAINS (MATHS) MOCK TEST - 4 (ANSWER SHEET)**

- |         |         |         |         |          |
|---------|---------|---------|---------|----------|
| 1. (D)  | 21. (C) | 41. (B) | 61. (B) | 81. (A)  |
| 2. (C)  | 22. (C) | 42. (D) | 62. (A) | 82. (C)  |
| 3. (A)  | 23. (A) | 43. (A) | 63. (A) | 83. (A)  |
| 4. (A)  | 24. (C) | 44. (A) | 64. (C) | 84. (A)  |
| 5. (D)  | 25. (A) | 45. (C) | 65. (C) | 85. (A)  |
| 6. (A)  | 26. (B) | 46. (B) | 66. (B) | 86. (C)  |
| 7. (C)  | 27. (D) | 47. (C) | 67. (B) | 87. (A)  |
| 8. (*)  | 28. (C) | 48. (D) | 68. (B) | 88. (A)  |
| 9. (C)  | 29. (B) | 49. (B) | 69. (B) | 89. (C)  |
| 10. (A) | 30. (C) | 50. (A) | 70. (A) | 90. (B)  |
| 11. (C) | 31. (A) | 51. (A) | 71. (C) | 91. (C)  |
| 12. (B) | 32. (D) | 52. (A) | 72. (A) | 92. (B)  |
| 13. (B) | 33. (D) | 53. (B) | 73. (A) | 93. (C)  |
| 14. (C) | 34. (C) | 54. (D) | 74. (A) | 94. (B)  |
| 15. (B) | 35. (A) | 55. (C) | 75. (B) | 95. (D)  |
| 16. (A) | 36. (D) | 56. (C) | 76. (A) | 96. (D)  |
| 17. (D) | 37. (A) | 57. (A) | 77. (A) | 97. (C)  |
| 18. (A) | 38. (C) | 58. (A) | 78. (B) | 98. (D)  |
| 19. (A) | 39. (B) | 59. (C) | 79. (B) | 99. (B)  |
| 20. (C) | 40. (C) | 60. (B) | 80. (*) | 100. (D) |