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### SSC (T-II) 2013, MTP - 16 (SOLUTION)

1. (A) Unit digits in  $(7)^4 = 1$ , therefore unit digit in  $(7^4)^8$  i.e.  $7^{32}$  will be 1.

Hence, unit digits in  $(7)^{35}$   
 $= 1 \times 7 \times 7 \times 7 = 3$

Again, unit digit in  $(3)^4 = 1$

Therefore, unit digit in the expansion of  $(3^4)^{17}$   
 $= (3)^{68} = 1$

∴ Unit digit in the expansion of  $(3)^{71}$   
 $= 1 \times 3 \times 3 \times 3 = 7$

and unit digit in the expansion of  $(11)^{35}$   
 $= 1$

∴ Unit digit in the product of  
 $7^{35} \times 3^{71} \times 11^{55} = 1$

2. (C)  $a = \frac{1}{100}$ ,  $b = \frac{1}{5}$ ,  $c = \frac{1}{10}$

or  $a = 0.01$ ,  $b = 0.2$ ,  $c = 0.1$

∴  $b > c > a$

3. (A) Product of the numbers

$$\begin{aligned} &= \text{HCF} \times \text{LCM} \\ &= 21 \times 4641 \\ &= 21 \times 3 \times 7 \times 13 \times 17 \\ &= 3 \times 7 \times 3 \times 7 \times 13 \times 17. \end{aligned}$$

i.e. 273 and 357.

4. (A) Let the number be  $x$ .

$$\therefore x = 765k + 42$$

$$\Rightarrow 17 \times 45K + 17 \times 2 + 8$$

$$\Rightarrow 17(45K + 2) + 8$$

$$\Rightarrow \text{Remainder} = 8$$

5. (B) Distance traversed by the extremity of the

$$\text{minute-hand in one hour} = 2 \times \frac{22}{7} \times 10$$

Distance traversed by the extremity of the minute-hand in 3 days and 5 hour, i.e. in 77 hours

$$= 2 \times \frac{22}{7} \times 10 \times 77$$

$$= 22 \times 220 = 4840 \text{ cm}$$

Distance traversed by the hour-hand in 12 hour

$$= 2 \times \frac{22}{7} \times 7 = 44 \text{ cm}$$

Distance traversed by the hour-hand in 77 hour

$$= \frac{44}{12} \times 7 = \frac{11 \times 77}{3} = \frac{847}{3} = 282.33 \text{ cm}$$

Reqd. difference =  $4840 - 282.33$   
 $= 4557.67 \text{ cm}$

6. (D) The series obtained

$$\begin{aligned} &= 4 \times 2 + 3, 4 \times 5 + 3, 4 \times 8 + 3, 4 \times 11 + 3 \dots \\ &= 11, 23, 35, \dots \end{aligned}$$

$$7. (A) \frac{\frac{1}{2} \div \frac{1}{2} \times \frac{1}{2}}{\frac{1}{2} + \frac{1}{2} \times \frac{1}{2}} = \frac{\frac{1}{2} \times 2 \times \frac{1}{2}}{\frac{3}{4}} = \frac{1}{2} \times \frac{4}{3} = \frac{2}{3}$$

8. (C) Let  $a_1$ ,  $d_1$  represent the 1st term and common difference of  $AP_1$ .

and  $a_2$ ,  $d_2$  represent the 1st term and common difference of  $AP_2$ .

ATQ,

$$\begin{aligned} \frac{S_n}{S_n} &= \frac{\frac{n}{2}[2a_1 + (n-1)d_1]}{\frac{n}{2}[2a_2 + (n-1)d_2]} \end{aligned}$$

$$\frac{7n+1}{4n+27} = \frac{2a_1 + (n-1)d_1}{2a_2 + (n-1)d_2} \dots\dots (i)$$

$$\text{Now, } \frac{a_{11}}{b_{11}} = \frac{a_1 + 10d_1}{a_2 + 10d_2} = \frac{2a_1 + 30d_1}{2a_2 + 30d_2}$$

$$= \frac{2a_1 + (21-1)d_1}{2a_2 + (21-1)d_2}$$

$$= \frac{S_{21}}{S_{21}}$$

$$= \frac{7 \times 21 + 1}{4 \times 21 + 27}$$

$$= \frac{148}{111} \text{ Ans.}$$

9. (B)  $S_n = 0.4 + 0.44 + 0.444 + \dots$  to  $n$  terms  
 $= 4[0.1 + 0.11 + 0.111 + \dots$  to  $n$  terms

$$= \frac{4}{9} [0.9 + 0.99 + 0.999 + \dots \text{ to } n \text{ terms}]$$

$$= \frac{4}{9} \left[ \frac{9}{10} + \frac{99}{100} + \frac{999}{1000} + \dots \text{ to } n \text{ term} \right]$$

$$= \frac{4}{9} \left( 1 - \frac{1}{10} \right) + \left( 1 - \frac{1}{100} \right) + \left( 1 - \frac{1}{1000} \right) + \dots + \left( 1 - \frac{1}{10^n} \right)$$

$$= \frac{4}{9} \left[ (1 + 1 \dots + n \text{ times}) - \left( \frac{1}{10} + \frac{1}{100} + \frac{1}{1000} + \dots + \frac{1}{10^n} \right) \right]$$

$$= \frac{4}{9} \left[ n - \frac{\frac{1}{10} \left\{ 1 - \left( \frac{1}{10} \right)^n \right\}}{1 - \frac{1}{10}} \right] \therefore S_n = \frac{a(1-r^n)}{(1-r)}$$



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$$= \frac{4}{9} \left[ n - \frac{\frac{1}{10} \left( 1 - \frac{1}{10^n} \right)}{\frac{9}{10}} \right]$$

$$= \frac{4}{9} \left[ n - \frac{1}{9} \left( 1 - \frac{1}{10^n} \right) \right]$$

$$= \frac{4}{9} \left[ 9n - 1 + \frac{1}{10^n} \right] \text{ Ans.}$$

10. (C) Number of women who have either nose studs or ear right =  $(15 - 3) = 12$

∴ Number of those who have both nose studs and ear rings =  $(8 + 7) - 12 = 3$

11. (C) Ashok's present age =  $26 - 6 = 20$  yrs

∴ Pradeep's present age =  $20 \times \frac{3}{4} = 15$  yrs]

12. (A) Let the number of girls =  $x$

∴ boys =  $x - 2$

According to question:-

$$x + x - 2 = 52$$

$$\therefore x = 27$$

∴ No. of bags = 25

Again:-

Let average no. of girls =  $y$  kg

$$42 \times 25 + 27xy = 52 \times 52$$

$$\therefore y = \frac{52 \times 52 - 42 \times 25}{27}$$

$$= 61.25 \sim 61 \text{ kg (Approx.)}$$

13. (D) Wrong calculated marks

$$= 35 \times 75$$

$$= \frac{2520 - 36 + 86}{35} = \frac{2570}{35} = 73.42$$

14. (C) If a container contains  $y$  units of liquid and  $x$  units of liquids is taken out. If this operation is repeated  $n$  times. The final quantity of the liquid in the container is

$$y \left( 1 - \frac{x}{y} \right)^n$$

$$\therefore 24 = 54 \left( 1 - \frac{x}{54} \right)^2$$

$$\Rightarrow \left( 1 - \frac{x}{54} \right)^2 = \frac{24}{54} = \frac{4}{9}$$

$$\Rightarrow \left( 1 - \frac{x}{54} \right) = \frac{2}{3}$$

$$\Rightarrow \frac{x}{54} = \frac{1}{3}$$

$$\Rightarrow x = 18 \text{ l}$$

15. (C) Let the quantity of pure milk be  $x$  l.

If 5 l of water is added to it, then,

Cost of  $(5 + x)$  l

$$= \text{Rs. } (3x + 5)$$

$$\therefore \text{Profit} = \text{Rs. } 15$$

$$\text{Given, } 20\% \text{ of } 3x = 15$$

$$\Rightarrow \frac{3x}{5} = 15$$

$$\Rightarrow x = 25 \text{ l}$$

16. (D) Let the amount be Rs.  $x$  and rate is  $r\%$ .

Then, Simple interest

$$\frac{x \times r}{100} = 25$$

$$\Rightarrow x \times r = 2500$$

For true discount

$$\frac{(x - 20) \times r}{100} = 20$$

$$\Rightarrow \frac{x \times r - 20r}{100} = 20$$

$$\Rightarrow xr - 20r = 2000$$

From Eqs. (i) and (ii), we get

$$2500 - 20r = 2000$$

$$\Rightarrow r = 25\%$$

From Eq. (i)

$$x \times 25 = 2500$$

$$\Rightarrow x = 100$$

17. (\*) Let the CP price of pen = Rs. 1

$$\text{CP of 40 pen} = 36 \times 1 = \text{Rs. } 36$$

$$\therefore \text{Selling price of 40 pen} = 40 - 3\% \text{ of } 40$$

$$= 40 - \frac{3}{100} \times 40$$

$$= \frac{400 - 12}{10}$$

$$= \text{Rs. } 38.80$$

$$\therefore \% \text{ profit} = \left[ \frac{38.80 - 36}{36} \right] \times 100$$

$$= \frac{280}{36} = \frac{70}{9} = 7\frac{7}{9} \%$$

18. (C) Length of bridge = 1000 m

Length of train = 500 m

$$\text{Total length} = 1000 + 500 = 1500 \text{ m}$$

$$\text{Speed of train} = \frac{1500}{1000} \times \frac{60}{2} = 45 \text{ km/h}$$

19. (B) Distance (D) = Speed (S) × Time (T)

$$\therefore D = 4 \times \left( T \times \frac{15}{60} \right)$$

$$\Rightarrow D = 4T + 1$$



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$$\text{and } D = 6 \left( T - \frac{10}{60} \right)$$

$$D = 6T - 1$$

Solving eq<sup>ns</sup>. (i) and (ii),

$$T = 1 \text{ h}$$

$$D = 4 \times 1 + 1 = 5 \text{ km}$$

20. (D) It is clear from the question that when A covers 500m, B covers 400 m i.e., A takes a lead of 100 m in every 500 m of distance. Therefore, a lead of 400 m will be taken in travelling a distance of 2000 m or in other words A passes B after every 2000m. Hence, total number of such pass

$$= \frac{5000}{2000} = \frac{5}{2} = 2 \frac{1}{2} \text{ times}$$

21. (C) Let three numbers A, B and C are Rs.  $12x$ ,  $15x$  and  $25x$  respectively.

$$\therefore 12x + 15x + 25x = 312$$

$$\Rightarrow x = \frac{312}{52} = 6$$

$$\begin{aligned} \therefore \text{Required ratio} &= \frac{15 \times 6 - 12 \times 6}{25 \times 6 - 15 \times 6} \\ &= \frac{3 \times 6}{10 \times 6} \\ &= \frac{3}{10} = 3 : 10 \end{aligned}$$

### **SHORTCUT METHOD:-**

There is no need to calculate the value of  $x$ .

$$\begin{aligned} \text{Required ratio} &= \frac{15x - 12x}{25x - 15x} \\ &= \frac{3x}{10x} = \frac{3}{10} = 3 : 10 \end{aligned}$$

22. (B) Ratio of investment of Sita, Gita and Rita is  $(5000 \times 3 + 7000 \times 9) : (4000 \times 1 + 3000 \times 11) : (7000 \times 11)$

$$= 78000 : 37000 : 77000$$

$$= 78 : 37 : 77$$

$\therefore$  Share of Rita in profit

$$= \frac{77}{78 + 37 + 77} \times 1218 = \text{Rs. } 488.47$$

23. (A) Let the speed of man and current be  $x$  km/h and  $y$  km/h respectively.

Then,

$$\frac{30}{x-y} + \frac{44}{x+y} = 10 \quad \dots (i)$$

$$\text{and } \frac{40}{x-y} + \frac{55}{x+y} = 13 \quad \dots (ii)$$

Solving eq<sup>ns</sup>. (i) and (ii),

$$y = 3 \text{ km/h}$$

24. (C) Let the tap can fill the cistern in  $x$  h.

$$\therefore \frac{x \times 8}{x-8} = 12$$

$$\Rightarrow 8x = 12x - 96$$

$$\Rightarrow x = 24 \text{ h}$$

$\therefore$  Capacity of cistern

$$= 24 \times 60 \times 6 = 8640 \text{ l}$$

25. (A) Part of the cistern filled in 3 min

$$= \frac{3}{12} + \frac{3}{16} = \frac{21}{48} = \frac{7}{16}$$

Let remaining  $\frac{9}{16}$  part was filled in  $x$  min

$$\text{Then, } \frac{x}{12} \times \frac{7}{8} + \frac{x}{16} \times \frac{5}{6} = \frac{9}{16}$$

$$\Rightarrow x \left( \frac{7+5}{96} \right) = \frac{9}{16}$$

$$\Rightarrow x = \frac{9}{16} \times \frac{96}{12} = 4.5 \text{ min}$$

26. (A) Ratio of efficiencies of the three persons

$$\begin{aligned} &= \frac{24}{6} : \frac{24}{8} : \frac{24}{3} = \left( \frac{24}{6} + \frac{24}{8} \right) \\ &= 4 : 3 : 1 \end{aligned}$$

$$\therefore \text{Boy's share} = \frac{1}{(4+3+1)} \times 600 = \text{Rs. } 75$$

27. (A) Let the cost price of geyser be Rs.  $x$ , then,  $x \times 1.1 \times 1.15 \times 1.25 = 1265$

$$\begin{aligned} x &= \frac{1265}{1.58125} \\ &= \text{Rs. } 800 \end{aligned}$$

28. (B) Let his increased income be  $x$ . Then,

$$\begin{aligned} (x - 1200) \times \frac{80}{100} \times \frac{12}{100} &= x \times \frac{80}{100} \times \frac{10}{100} \\ \Rightarrow 12x - 14400 &= 10\% \\ x &= \text{Rs. } 7200 \end{aligned}$$

29. (D) Let the present value of what A owes to B be Rs.  $x$ .

Then,

$$x + \frac{x \times 14 \times 3}{2 \times 100} = 1573$$

$$\Rightarrow x + \frac{21}{100}x = 1573$$

$$\Rightarrow \frac{121x}{100} = 1573$$

$$\therefore x = \text{Rs. } 1300$$

Let  $y$  be the present value of what B owes A.

$$\text{Then, } y + y \times \frac{1}{2} \times \frac{14}{100} = \text{Rs. } 1444.50$$



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$$\Rightarrow y + \frac{7}{100}y = \text{Rs. } 1444.50$$

$$\Rightarrow y = \frac{1444.50 \times 100}{107} = \text{Rs. } 1350$$

Hence, B pay Rs. 50 to A.

30. (A) Let the amount given at 4% per annum be Rs.  $x$ .

$\therefore$  Amount given at 5% per annum =  $(1200 - x)$

$$\frac{x \times 4 \times 2}{100} + \frac{(1200 - x) \times 5 \times 2}{100} = 110$$

$$\Rightarrow \frac{-2x + 12000}{100} = 110$$

$$\Rightarrow x = \text{Rs. } 500$$

$$\text{Also, } (1200 - x) = 1200 - 500 = \text{Rs. } 700$$

31. (A) Let money invested at 5% be Rs.  $x$ .

$$\therefore \frac{x \times 1 \times 5}{100} + \frac{(10000 - x) \times 1 \times 8}{100} = 688.25$$

$$\Rightarrow 5x - 8x + 80000 = 68825$$

$$\Rightarrow 3x = 11175$$

$$\Rightarrow x = \text{Rs. } 3725$$

32. (C) Let principal amount be Rs. 100.

$$\text{Then, SI} = \frac{100 \times 20 \times 3}{100} = \text{Rs. } 60$$

$$\text{and CI} = 100 \left( 1 + \frac{20}{100} \right)^3 - 100$$

$$= 100 \times \left( \frac{6}{5} \right)^3 - 100 = \frac{364}{5}$$

$$\therefore \text{CI} - \text{SI} = \frac{364}{5} - 60 = \frac{64}{5}$$

If difference is Rs.  $\frac{64}{5}$ , Principal = Rs. 100

If difference is Rs. 48,

$$\text{Principal} = \frac{100 \times 5}{64} \times 48 = \text{Rs. } 375$$

$$33. (C) \quad \frac{P \left( 1 + \frac{r}{100} \right)^2}{\left( P + \frac{Pr}{100} \right)} = \frac{6}{5}$$

$$\Rightarrow \left( 1 + \frac{r}{100} \right) = \frac{6}{5}$$

$$\Rightarrow r = 20\%$$

34. (D) Train with a speed of 54 km/h passes the man in 20s.

$$\therefore \text{Length of the train} = 54 \times \frac{5}{18} \times 20 = 300 \text{ m}$$

Let the length of platform be  $x$  m.

$$\text{Then, } (300 + x) = 54 \times \frac{5}{18} \times 36$$

$$x = 540 - 300 = 240 \text{ m}$$

$$35. (A) \text{ Length of train} = 12 \times 15 = 180 \text{ m}$$

$$\text{Time} = 18 \text{ s}$$

$$\text{Speed} = \frac{180}{18} = 10 \text{ m/s}$$

$$\text{New distance} = 15 \times 10 = 150 \text{ m}$$

$$\therefore \text{Required time} = \frac{150}{10} = 15 \text{ s}$$

36. (B) Let the CP of the pen and book be Rs.  $x$  and Rs.  $y$  respectively.

$$\therefore 0.95x + 1.15y = (x + y) + 7$$

$$\Rightarrow 0.15y - 0.05x = 7 \quad \dots (i)$$

$$\text{and } 1.05x + 1.1y = (x + y) + 13$$

$$\Rightarrow 0.05x + 0.1y = 13 \quad \dots (ii)$$

Solving Eqs. (i) and (ii), we get

$$y = \text{Rs. } 80$$

37. (D) Let the cost price of articles be Rs.  $x$ .

Then, selling price of article =  $0.88x$ .

Marked price of article

$$= \frac{0.88}{80} \times 100 \times x = 1.1x$$

New selling price of article =  $1.045x$

$$\therefore \text{Profit per cent} = \frac{1.045x - x}{x} \times 100 = 4.5\%$$

38. (A) Let the time of meet =  $t$  h

$$\longleftrightarrow 450 \text{ km} \longleftrightarrow$$

$$A \xrightarrow{\quad} \xrightarrow{\quad} \xrightarrow{\quad} B$$

$$15 \text{ km/h}$$

$$20 \text{ km/h}$$

Now,

$$15 \left( t - \frac{20}{60} \right) + 20t = 450$$

$$\Rightarrow t = 13 \text{ h}$$

$$\text{Distance from A} = 15 \left( 13 + \frac{1}{3} \right) = 190 \text{ km}$$

39. (A) Speed of Ramesh =  $3x$  km/hr

Speed of Suresh =  $4x$  km/hr

Let the distance =  $D$

ATQ,

$$\frac{D}{3x} - \frac{D}{4x} = \frac{1}{2}$$

$$\Rightarrow \frac{D \left( \frac{1}{12} \right)}{x} = \frac{1}{2}$$

$$\Rightarrow D = 6x$$

$$\text{Time of Ramesh} = \frac{D}{3x} = \frac{6x}{3x} = 2 \text{ h}$$

$$\text{Time of Suresh} = \frac{D}{4x} = \frac{6x}{4x} = 1.5 \text{ h}$$



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40.(\*) Work done by A & B in 16 days =  $\frac{16}{30} = \frac{8}{15}$

Remaining work =  $1 - \frac{8}{15} = \frac{7}{15}$

$\therefore \frac{7}{15}$  work is done by B alone in 44 days.

$\therefore$  1 work is done by B alone in

$$= \frac{\frac{44}{7}}{\frac{7}{15}} = \frac{44 \times 15}{7} = 94.29 \text{ days}$$

41. (C)  $SP = \frac{70}{700} MP$

SP For Tarun = Rs. 8750

Labelled price =  $\frac{125}{100} \times \frac{70}{100} MP = 8750$

$\Rightarrow MP = \text{Rs. } 10000$

42. (A) Let the CP of the article be Rs.  $x$ .

Then,

$$SP = x \times 1.12 \times 1.1$$

Given,  $x \times 1.12 \times 1.1 = 616$

$$\Rightarrow x = \frac{616}{1.232} = \text{Rs. } 500$$

43. (B) Let CP = Rs.  $x$  and SP = Rs.  $y$ .

$\Rightarrow y \times 7\% = x \times 8\%$

and  $y \times 9\% = x \times 10\% + 1$

and  $\frac{9}{100} \times y = \frac{10}{100} \times x + 1$

$\Rightarrow 7y = 8x$

and  $9y = 10x + 100$

$\Rightarrow 9 \times \frac{8x}{7} = 10x + 100$

$\Rightarrow x = \text{Rs. } 350$

44. (B) Let the numbers be  $3x$  and  $4x$ .

Then,

$$16x^2 = 8 \times (9x)^2 - 224$$

$\Rightarrow 16x^2 = 72x^2 - 224$

$\Rightarrow 56x^2 = 224$

$\Rightarrow x^2 = 4$

$\Rightarrow x = 2$

Hence, numbers are 6, 8.

45. (A)  $P = \frac{x^2 - 36}{x^2 - 49} = \frac{(x-6)(x+6)}{(x-7)(x+7)}$

$Q = \frac{x+6}{x+7}$

$$\therefore \frac{P}{Q} = \frac{\frac{(x-6)(x+6)}{(x-7)(x+7)}}{\frac{(x+6)}{(x+7)}} = \frac{x-6}{x-7}$$

46. (B)  $S_n = pn + qn^2$

$$S_{n-1} = p(n-1) + q(n-1)^2$$

$$= pn - p + qn^2 - 2qn + q$$

$$a_n = S_n - S_{n-1}$$

$$= pn + qn^2 - (pn - p + qn^2 - 2qn + q)$$

$$= p + 2qn - q$$

Common difference

$$= a_2 - a_1$$

$$= (p + 4q - q) - (p + 2q - q)$$

$$= 2q \text{ Ans.}$$

47. (C)  $a, b$  and  $c$  are in GP and  $a^{\frac{1}{x}} = b^{\frac{1}{y}} = c^{\frac{1}{z}}$ .

Let,  $a^{\frac{1}{x}} = b^{\frac{1}{y}} = c^{\frac{1}{z}} = k$

$\therefore a = k^x$

$b = k^y$

$c = k^z$

Now:-

$b^2 = ac$  [ $a, b$  and  $c$  are in G.P.]

or,  $(k^y)^2 = k^{x+z}$

$\therefore 2y = x + z$

48. (C)

	Spirit	Water
Vessel 1	0.5	0.5
	1	1
Vessel 2	0.75	0.25
	3	1

$$\frac{\text{Spirit}}{\text{Water}} = \frac{\frac{1}{2} \times 2 + \frac{3}{4} \times 3}{\frac{1}{2} \times 2 + \frac{1}{4} \times 3} = \frac{13}{7}$$

49. (C)  $\frac{y}{x-z} = \frac{y+x}{z}$

$\Rightarrow yz = xy + x^2 - yz - xz \quad \dots (i)$

Also,  $\frac{x}{y} = \frac{y}{x-z}$

$\Rightarrow x^2 - xz = y^2 \quad \dots (ii)$

Using Eqs. (i) and (ii), we get

$yz = xy - yz + y^2$

$\Rightarrow 2yz = xy + y^2$

$\therefore 2z = x + y \quad \dots (iii)$

Only option (C) satisfies the Eq. (iii).

50. (A) CP =  $x$  (say)

34% of CP = 26% of SP

$\frac{34}{26}x = \frac{17}{13}x = SP$

$$\% \text{ profit} = \frac{17x - 13x}{13x} \times 100$$

$$= 30.77\%$$



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51. (B) Given roots are real and equal.

$$\begin{aligned} \therefore B^2 - 4AC &= 0 \\ \Rightarrow [-2(a^2 - bc)]^2 - 4(c^2 - ab)(b^2 - ac) &= 0 \\ \Rightarrow 4(a^4 + b^2c^2 - 2a^2bc - c^2b^2 + ac^3 + ab^3 - a^2bc) &= 0 \\ \Rightarrow 4a(a^3 + b^3 + c^3 - 3abc) &= 0 \\ \Rightarrow a^3 + b^3 + c^3 &= 3abc \end{aligned}$$

52. (B)  $\frac{a^{1/2} + a^{-1/2}}{1-a} + \frac{(1-a^{-1/2})}{1+\sqrt{a}}$

$$\Rightarrow \frac{2}{(1-\sqrt{a})(1+\sqrt{a})} + \frac{1-a^{-1/2}}{(1+\sqrt{a})}$$

$$\Rightarrow \frac{2+(1-\sqrt{a})(1-a^{-1/2})}{1-a}$$

$$\Rightarrow \frac{2+1-a^{-1/2}-a^{-1/2}+1}{1-a}$$

$$\Rightarrow \frac{2+2-(a^{-1/2}+a^{1/2})}{1-a}$$

$$\Rightarrow \frac{2+2-2}{1-a} = \frac{2}{1-a}$$

53. (A) Both the expressions are divided by  $(x-2)$ .  
Hence  $f_1(2) = f_2(2)$ .

( $\therefore$  Both remainders are same)

$$\Rightarrow p \times (2)^4 - 3(2)^3 + 20 = 4(2)^2 + 7(2) - p$$

$$\Rightarrow 16p - 24 + 20 = 16 + 14 - p$$

$$\Rightarrow 17p = 34$$

$$\therefore p = 2$$

Hence, the value of 'p' is 2.

54. (A)  $x^{a^3+b^3+3ab(a+b)} = (2^5)^{25}$

$$\Rightarrow x^{(a+b)^3} = 2^{125}$$

$$\Rightarrow x^{5^3} = 2^{5^3}$$

$$\Rightarrow x = 2$$

55. (A) Joining point O to three vertices A, B and C.

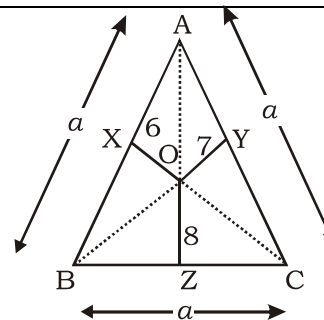
Now,

Area of  $(\triangle OBC + \triangle OCA + \triangle OAB) = \text{area of } \triangle ABC$ .

$$\Rightarrow \frac{1}{2}(a \times 8 + a \times 7 + a \times 6) = \frac{\sqrt{3}}{4} a^2 = \frac{21a}{2}$$

$$a = \frac{42}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}}$$

$$\therefore a = 14\sqrt{3}$$



$\Rightarrow$  Hence, area of triangle ABC.

$$= \frac{\sqrt{3}}{4} a^2$$

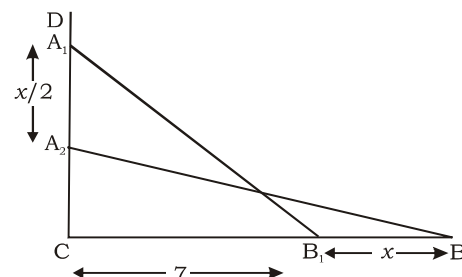
$$= \frac{\sqrt{3}}{4} (14\sqrt{3})^2 \text{ m}^2$$

$$= 254.6 \text{ m}^2$$

56. (D) Let  $A_1B_1$  be the ladder placed against the wall.

$A_1B_1 = \text{length of ladder} = 25 \text{ m}$

$B_1C = 7 \text{ m}$



Now, ladder foot is drawn out from  $B_1$  to  $B_2$  such that  $B_1B_2 = x \text{ m}$ , then the top of the ladder comes down from  $A_1$  to  $A_2$  and  $A_1A_2$

$$= \frac{x}{2} \text{ m (as per question),}$$

So,  $A_1B_1 = A_2B_2 = 25 \text{ m}$  and  $A_2C = Y$  (say)

In  $\triangle A_1B_1C$

$$A_1C = \sqrt{(A_1B_1)^2 - (B_1C)^2}$$

$$\Rightarrow A_1A_2 + A_2C = \sqrt{25^2 - 7^2}$$

$$\Rightarrow \frac{x}{2} + Y = 24 \quad \dots (i)$$

In  $\triangle A_2B_2C$

$$(A_2C)^2 + (B_2C)^2 = A_2B_2^2$$

$$\Rightarrow Y^2 + (x+7)^2 = 25^2$$

$$\Rightarrow \left(24 - \frac{x}{2}\right)^2 + (x+7)^2 = 25^2 \quad [\text{from (i)}]$$

$$\Rightarrow 576 + \frac{x^2}{2} - 24x + x^2 + 49 + 14x = 625$$



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$$\Rightarrow \frac{5x^2}{4} = 10x$$

$$\Rightarrow x = 8 \text{ m}$$

57. (C) Let the circumference of outer circle

$$C_1 = 62.832 \text{ m}$$

circumference of inner circle

$$C_2 = 37.6992 \text{ m}$$

The area between two circles =  $A_1 - A_2 = ?$

Here, using the correlation formula for circumference and area.

$$A = \frac{C^2}{4\pi}$$

$$\Rightarrow A_1 - A_2 = \frac{C_1^2}{4\pi} - \frac{C_2^2}{4\pi}$$

$$\Rightarrow A_1 - A_2 = \frac{C_1^2 - C_2^2}{4\pi}$$

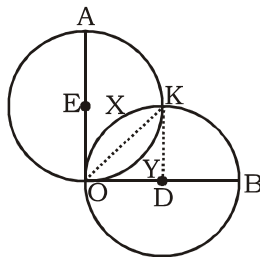
$$\Rightarrow A_1 - A_2 = \frac{(C_1 - C_2)(C_1 + C_2)}{4\pi}$$

$$\Rightarrow A_1 - A_2 =$$

$$\frac{(62.832 + 37.6992)(62.832 - 37.6992)}{4 \times 3.1416}$$

$$\Rightarrow A_1 - A_2 = 201 \text{ m}^2$$

58. (A)



Let AOB be one quadrant of a circle radius.

$$OA = OB = 10 \text{ m}$$

Two circles OKB and OKA are made on the above radii as diameter. So, if E and D are centres.

$$OD = BD = OE = EA = 5 \text{ m}$$

Since two circles are equal, K will be midpoint of arc AKO and OKB.

$$\Rightarrow \angle KDO = 90^\circ$$

$$\Rightarrow OK = 5\sqrt{2}$$

Area common to both circle = 2 × area of segment OXK (or OYK)

Using the formula, for central angle =  $90^\circ$

$$\begin{aligned} \text{Area of segment OXK} &= 0.285 \times r^2 \\ &= 0.285 \times 5^2 \\ &= 7.13 \text{ m}^2 \end{aligned}$$

Area common to both circle

$$\begin{aligned} &= 2 \times 7.13 \\ &= 14.26 \text{ m}^2 \end{aligned}$$

59. (B) Let A = 2 pens are red.

B = 2 pens are blue.

$$\text{than } P(A) = \frac{5}{9} \times \frac{4}{8} = \frac{20}{72} = \frac{5}{18}$$

$$P(B) = \frac{4}{9} \times \frac{3}{8} = \frac{12}{72} = \frac{1}{6}$$

Now, A and B are mutually exclusive events. Hence,

$$P(\text{selecting either 2 red pens or blue pens}) = P(A + B) = P(A) + P(B)$$

$$= \frac{5}{18} + \frac{1}{6} = \frac{4}{9}$$

Hence, the required probability is  $\frac{4}{9}$ .

60. (B)  $\sec^2 \theta \operatorname{cosec}^2 \theta - [\tan^2 \theta + \cot^2 \theta]$

$$= (1 + \tan^2 \theta) (1 + \cot^2 \theta) - [\tan^2 \theta + \cot^2 \theta]$$

$$[\text{since } \sec^2 \theta = 1 + \tan^2 \theta]$$

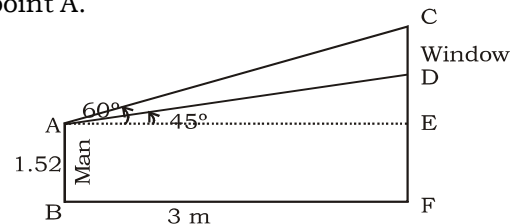
$$= 1 + \tan^2 \theta + \cot^2 \theta + \tan^2 \theta \cot^2 \theta - \tan^2 \theta - \cot^2 \theta$$

$$= 1 + 1$$

$$= 2$$

Hence, the required value is 2.

61. (B) Let AB be the man standing outside a house which has a window CD. C (top point) and D (bottom point) of window are viewed from point A.



$$\left. \begin{aligned} \angle CAE &= 60^\circ \\ \angle DAE &= 45^\circ \end{aligned} \right\} \text{ Given}$$

In right  $\triangle DAE$ ,

$$\tan 45^\circ = \frac{DE}{AE} = \frac{DE}{3}$$

$$\Rightarrow DE = 3 \tan 45^\circ = 3 \text{ m}$$

In right  $\triangle CAE$ ,

$$\tan 60^\circ = \frac{DE}{AE} = \frac{CD + DE}{AE} = \frac{CD + 3}{AE}$$

$$\Rightarrow \sqrt{3} = \left( \frac{CD}{3} + 1 \right)$$

Therefore, the length of the window is 2.2 m.

$$62. (C) \quad (1 - \sin^2 A) = \frac{0.8}{\sec A}$$

$$\Rightarrow \cos^2 A \cdot \sec A = 0.8$$

$$\Rightarrow \cos A = 0.8 = \frac{4}{5}$$





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$$\Rightarrow \sin A = \frac{3}{5}$$

$$\Rightarrow \tan A = \frac{3}{4}$$

$$\text{So, } \tan A + \frac{1}{\cos A} = \frac{3}{4} + \frac{5}{4} = \frac{8}{4} = 2$$

63. (A)  $\tan \theta = 3 \cot \theta$

$$\Rightarrow \tan \theta = \frac{3}{\tan \theta}$$

$$\Rightarrow \tan^2 \theta = 3$$

$$\Rightarrow \tan \theta = \pm \sqrt{3}$$

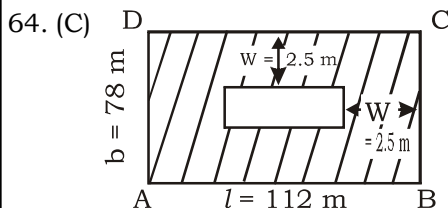
Since  $\theta$  is an acute angle  $\Rightarrow \theta = 60^\circ$

$$\text{Now, } \sin^2 \theta + \operatorname{cosec}^2 \theta - \frac{1}{2} \cot^2 \theta$$

$$= \sin^2 60^\circ + \operatorname{cosec}^2 60^\circ - \frac{1}{2} \cot^2 60^\circ$$

$$= \left(\frac{\sqrt{3}}{2}\right)^2 + \left(\frac{2}{\sqrt{3}}\right)^2 - \frac{1}{2} \times \left(\frac{1}{\sqrt{3}}\right)^2$$

$$= \frac{3}{4} + \frac{4}{3} - \frac{1}{6} = \frac{23}{12}$$



Let ABCD be a rectangular grass plot which has a gravel path of width =  $W = 2.5$  m (shaded portion)

length of plot =  $l = 112$  m

breadth of plot =  $b = 78$  m

Here, the path is inside the rectangular plot.

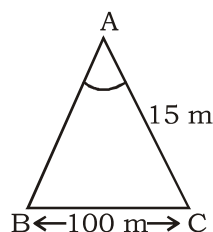
Using the formula:-

$$\begin{aligned} &= 2W(l + b - 2W) \\ &= 2 \times 2.5(112 + 78 - 2 \times 2.5) \\ &= 925 \text{ m}^2 \end{aligned}$$

Now, cost of construction the path

$$= 925 \times 3.40 = \text{Rs. } 3145$$

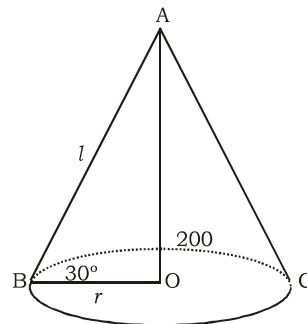
65. (A)



Since the triangle is an equilateral, so each angle =  $60^\circ = \theta$ ,  $r = 15$

$$\begin{aligned} \therefore \text{area of sector} &= \frac{\theta}{360^\circ} \times \pi r^2 \\ &= \frac{60^\circ}{360} \times \frac{22}{7} \times 225 \\ &= 117.85 \text{ m}^2. \end{aligned}$$

66. (D)



Let ABCO be the right cone whose slant height =  $l = AB = AC$

height =  $h = 200$  m

In  $\triangle ABO$ ,  $\angle ABO = 30^\circ$

$$\sin 30^\circ = \frac{200}{l}$$

$$\Rightarrow l = 200 \times 2 = 400 \text{ m}$$

$$\left[ \sin 30^\circ = \frac{1}{2} \right]$$

$$\cos 30^\circ = \frac{r}{l}$$

$$\Rightarrow r = l \cos 30^\circ = 400 \times \frac{\sqrt{3}}{2} = 200\sqrt{3} \text{ m}$$

$$\left[ \cos 30^\circ = \frac{\sqrt{3}}{2} \right]$$

Now,

Area of curved surface =  $\pi rl$

$$\begin{aligned} &= \frac{22}{7} \times 200 \times \sqrt{3} \times 400 \\ &= 435312 \text{ m}^2. \end{aligned}$$

67. (A) Let, the side of equilateral triangle is ' $a$ ' m.

$$\text{Area (A)} = \frac{\sqrt{3}}{4} a^2 \text{ m}^2$$

$$\Rightarrow \text{Cost of paving} = 10 \times \frac{\sqrt{3}}{4} a^2 \text{ rupees}$$

Similarly, perimeter ( $P$ ) =  $3a$  m

$\Rightarrow$  Cost of fencing =  $25 \times a$  rupees

According to the question,

$$10 \times \frac{\sqrt{3}}{4} a^2 = 25 \times 3a$$

$$\Rightarrow a = 10\sqrt{3}$$



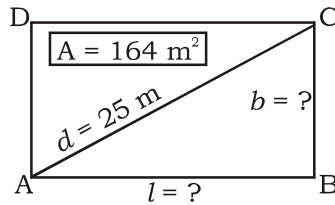


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$$\Rightarrow a = 17.32 \text{ m}$$

Hence, the side of the equilateral triangle is 17.32 m.

68. (C)



Let ABCD is a rectangle whose  
diagonal =  $d = 25 \text{ m}$   
area =  $A = 168 \text{ m}^2$   
length =  $l = ?$   
breadth =  $b = ?$

Using the correlation formula

$$(l + b)^2 = d^2 + 2A \quad [\text{Refer 12.4}]$$

$$\text{and } (l + b)^2 = d^2 - 2A$$

$$\Rightarrow (l + b)^2 = (25)^2 - 2 + 168$$

$$l + b = 31 \quad \text{(i)}$$

Similarly,

$$\Rightarrow (l + b)^2 = (25)^2 - 2 \times 168$$

$$l - b = 17 \quad \text{(ii)}$$

From (i) and (ii)

$$l = 24 \text{ m} = \text{length of the rectangle}$$

$$b = 7 \text{ m} = \text{breadth of the rectangle}$$

69. (A) The given points A, B and C are collinear.  
So, these area of the triangle formed by these points will be zero.

$$\Rightarrow (m + 1)(3 - 2m) + (2m + 1)(2m - 1) + (2m + 2)(1 - 3) = 0$$

$$\Rightarrow 2m^2 - 3m - 2 = 0$$

$$\Rightarrow 2m^2 - 4m + m - 2 = 0$$

$$\Rightarrow 2m(m - 2) + 1(m - 2) = 0$$

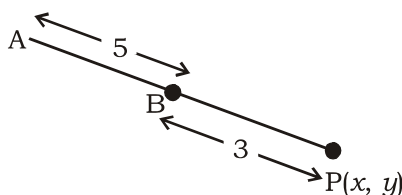
$$\Rightarrow (2m + 1)(m - 2) = 0$$

$$m = -\frac{1}{2} \text{ or } m = 2$$

70. (B) Let  $P(x, y)$  be the required point dividing the line AB externally in the ratio 5 : 3.

$$\Rightarrow \frac{AB}{BP} = \frac{5}{3} = \frac{1}{m} \text{ (say)}$$

Using the formula (section)



$$x = \frac{lx_2 - mx_1}{l - m}$$

$$\text{where } x_1 = 2, x_2 = -3$$

$$\Rightarrow x = \frac{5 \times -3 - 3 \times 2}{5 - 3} = -\frac{21}{2} = -10.5$$

$$\text{and } y = \frac{ly_2 - my_1}{l - m}$$

$$\text{where, } y_1 = -3, y_2 = 7$$

$$y = \frac{5 \times 7 - 3 \times (-3)}{5 - 3} = 22$$

Hence, the required point P is  $(-10.5, 22)$ .

71. (D) Using :-

$$d_1^2 + d_2^2 = 2(a^2 + b^2)$$

$$\Rightarrow a^2 + b^2 = \frac{1}{2} [(10)^2 + (17.78)^2] = 208 \dots \text{(i)}$$

$$\text{and } 2(a + b) = 40 \text{ (given)}$$

$$\Rightarrow a + b = 20$$

..... (ii)

From (i) and (ii), we have

$$a = 12, b = 8$$

72. (B) Let ABCD be a rhombus whose

$$\text{perimeter} = p = 36 \text{ m}$$

$$\text{area} = A = 72 \text{ m}^2$$

$$\text{perimeter } p = 4 \times a$$

$$\Rightarrow 36 = 4a$$

$$\Rightarrow a = 9 \text{ m}$$

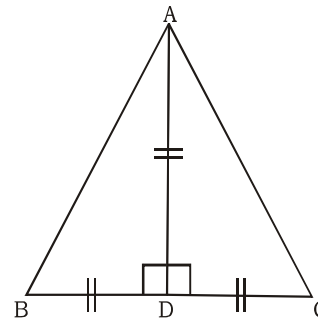
$$\text{Area, } A = a \times h$$

$$\Rightarrow 72 = 9 \times h$$

$$\Rightarrow h = \frac{72}{9} \text{ m}$$

$$h = 8 \text{ m}$$

73. (C)



Given that:-

$$\frac{BD}{DA} = \frac{DA}{DC} \quad \dots \text{(i)}$$

$$= DA^2 = BD \times DC \quad \dots \text{(ii)}$$

In right triangle AOB and AOC:-

$$AB^2 = AD^2 + BD^2 \quad \dots \text{(i)}$$

$$\text{and, } AC^2 = AD^2 + DC^2 \quad \dots \text{(ii)}$$

Adding (A) and (B):-

$$\begin{aligned} AB^2 + AC^2 &= 2AD^2 + DC^2 \\ &= 2 \times BD \times DC + BD^2 + DC^2 \\ &\quad [\text{from (ii)}] \end{aligned}$$

Thus in  $\triangle ABC$ ;

$$AB^2 + AC^2 = BC^2$$

Hence,  $\triangle ABC$  is a right angled at A.



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74. (D) Use length of the rope

$$= \frac{\pi d n}{2} (2n + 1)$$

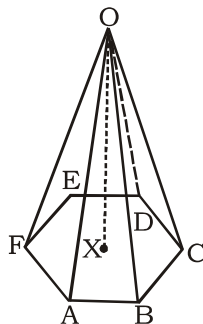
Where  $d = 2 \text{ cm}$

$$n = 140$$

$$\text{length} = \frac{3.14 \times 2 \times 140 [281]}{2}$$

$$= 1236.40 \text{ m}$$

75. (C) Let ABCDEF be a regular hexagonal pyramid whose base



ABCDEF is a regular hexagon.

If  $a =$  each side of regular hexagon,

then,  $6a = 30$

$$\Rightarrow a = 5 \text{ m}$$

height of pyramid =  $OX = h = 20 \text{ m}$

$$\text{Volume (V)} = \frac{1}{3} Ah$$

$$= \frac{1}{3} \times 6 \times \left( \frac{\sqrt{3}}{4} a^2 \right) \times 20$$

$$= 10\sqrt{3}a^2$$

$$= 10\sqrt{3} \times 5^2$$

$$= 250 \times 1.732 \text{ m}^3$$

$$= 433 \text{ m}^3$$

76. (B) It is given that

$S = 2.5 k$ , where  $k$  stands for curved surface area.

$$\Rightarrow 2\pi r(h + r) = 2.5(2\pi rh)$$

$$\Rightarrow \frac{h+r}{h} = 2.5$$

$$\Rightarrow 7 + r = 2.5 \times 7 \quad [\text{since } h = 7 \text{ cm}]$$

$$\Rightarrow r = 10.5 \text{ cm}$$

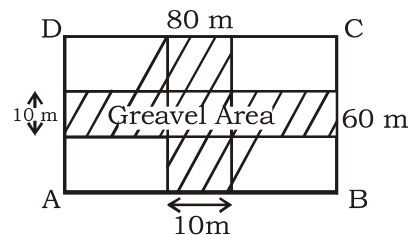
Now,

$$\text{Volume } V = \pi r^2 h$$

$$= \frac{22}{7} \times (10.5)^2 \times 7$$

$$= 2425.5 \text{ cm}^3$$

77. (A)



Let ABCD be a rectangular grass plot

whose length =  $l = 80 \text{ m}$

breadth =  $b = 60 \text{ m}$

Two roads of width  $W = 10 \text{ m}$  (shaded part) are crossing each other at the middle of plot.

$$\begin{aligned} \text{Area of roads} &= W(l + b - W) \\ &= 10(80 + 60 - 10) \text{ m}^2 \\ &= 1300 \text{ m}^2 \end{aligned}$$

Cost of gravelling the roads

$$= \text{rate of gravelling / m}^2 \times \text{area of roads}$$

$$= \text{Rs. } 2 \times 1300$$

$$= \text{Rs. } 2600$$

78. (C) Let  $r =$  radius of hemisphere bowl

$$\Rightarrow 2\pi r = 176$$

$$\Rightarrow r = 28 \text{ cm}$$

Volume of the quantity in hemispherical

$$\text{punch bowl} = \frac{1}{2} \times \frac{2}{3} \pi r^3$$

$$= \frac{1}{3} \pi \times 28^3 \text{ cm}^3$$

Volume of the bowl in which food is to be

$$\text{served} = \frac{2}{3} \pi \times 2^3 \text{ cm}^3.$$

No. of persons served

$$\begin{aligned} &= \frac{\frac{1}{3} \pi \times 28^3}{\frac{2}{3} \pi \times 2^3} \\ &= 1372 \end{aligned}$$

$$79. (D) \quad 3^{x^2 - xy + y^2} = 81 = 3^4$$

$$\Rightarrow x^2 - xy + y^2 = 4 \quad \dots (i)$$

$$\text{and } 2^{x^3 + y^3} = 256 = 2^8$$

$$\Rightarrow x^3 + y^3 = 8 \quad \dots (ii)$$

Dividing (ii) by (i)  $x + y = 2$

80. (B) The given equation is

$$c + \frac{d-y}{y} = e - 1 + \frac{f}{y}$$

$$\Rightarrow c + \frac{d}{y} - \frac{y}{y} = e - 1 + \frac{f}{y}$$

$$\Rightarrow c + \frac{d}{y} - 1 = e - 1 + \frac{f}{y}$$



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$$\Rightarrow \frac{d}{y} - \frac{f}{y} = e - c$$

$$\Rightarrow \frac{d-f}{y} = e - c$$

$$\Rightarrow y = \frac{d-f}{e-c}$$

81. (B) The given equation is

$$bx^2 - ax + \log_2 m^y = 0$$

Now,

$$\text{Sum of the roots} = x_1 + x_2$$

$$= \frac{-a}{b}$$

$$= \frac{a}{b} \quad \dots (i)$$

The given relation is

$$x_1^2 - x_2^2 = a^2$$

$$\Rightarrow (x_1 + x_2)(x_1 - x_2) = a^2$$

$$\Rightarrow \frac{a}{b} (x_1 - x_2) = a^2$$

[From equation (i)]

$$\Rightarrow x_1 - x_2 = ab \quad \dots (ii)$$

From equation (i) and equation (ii)

$$x_1 = \frac{1}{2} \left[ \frac{a}{b} + ab \right] = \frac{a(b^2 + 1)}{2b}$$

$$x_2 = \frac{1}{2} \left[ \frac{a}{b} - ab \right] = \frac{a(1 - b^2)}{2b}$$

Hence, the roots are

$$= \frac{a}{2b} (b^2 + 1), \frac{a}{2b} (1 - b^2)$$

82. (\*) The given expression is

$$= (\sqrt{k+l})^2 + (\sqrt{m})^2 + (\sqrt{n})^2 + 2\sqrt{m}\sqrt{k+l} - 2\sqrt{n}\sqrt{m} - 2\sqrt{n}\sqrt{k+l}$$

$$= [\sqrt{k+l} + \sqrt{m} - \sqrt{n}]^2$$

So, the square root of the given expressions

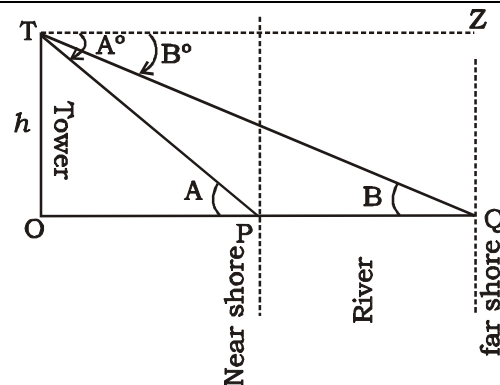
$$= \pm [\sqrt{k+l} + \sqrt{m} - \sqrt{n}]$$

$$83. (C) \frac{\cos(180^\circ + 75^\circ) + \tan(360^\circ - 75^\circ)}{2\cot(90^\circ + 75^\circ) - 2\sin(360^\circ + 90^\circ - 75^\circ)}$$

$$= \frac{-\cos 75^\circ - \tan 75^\circ}{-2\tan 75^\circ - 2\cos 75^\circ} = \frac{1}{2}$$

84. (D) Let OT = height of tower =  $h$  metres

PQ = width of the river



Where P = point of the near shore to tower.

Q = point of the far shore to the tower.

$\angle ZTA = A^\circ$  (angle of depression)

$\angle ZTQ = B^\circ$  (angle of depression)

Then,  $\angle ZTA = \angle TPO = A^\circ$

$\angle ZTQ = \angle TQO = B^\circ$

Now,

$$\text{In } \triangle TOP, \tan A = \frac{h}{OP}$$

$$\Rightarrow OP = h \cot A \quad \dots (i)$$

$$\text{In } \triangle TQO, \tan B = \frac{h}{OQ}$$

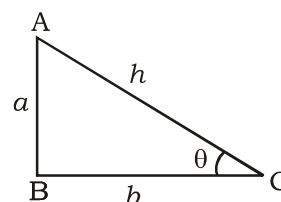
$$= \frac{h}{OP + OQ}$$

$$\Rightarrow OP + PQ = h \cot B \quad \dots (ii)$$

From (i) and (ii),

$$PQ = h(\cot B - \cot A)$$

85. (C)



$$h^2 = a^2 + b^2$$

since,  $a$  and  $h$  are consecutive integers,

$$h = a + 1$$

$$\Rightarrow (a + 1)^2 = a^2 + b^2$$

$$\Rightarrow b^2 = 2a + 1$$

$$\Rightarrow a = \frac{b^2 - 1}{2}$$

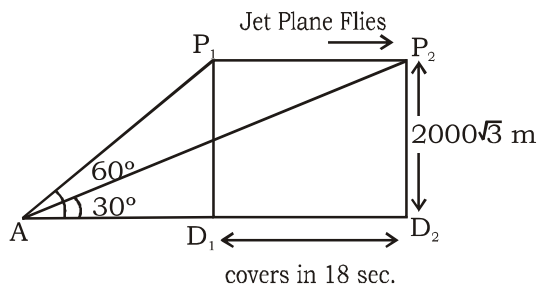
$$\Rightarrow h = \frac{b^2 + 1}{2}$$

$$\text{So, } \sin \theta = \frac{a}{h} = \frac{b^2 - 1}{b^2 + 1}$$



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86. (A)



In  $\triangle AP_1D_1$ ,

$$\tan 60^\circ = \frac{P_1D_1}{AD_1} = \frac{2000\sqrt{3}}{AD_1}$$

$$\sqrt{3} = \frac{2000\sqrt{3}}{AD_1}$$

$$\Rightarrow AD_1 = 2000 \text{ m}$$

In  $\triangle AP_2D_2$ ,

$$\tan 30^\circ = \frac{P_2D_2}{AD_2} = \frac{2000\sqrt{3}}{AD_2}$$

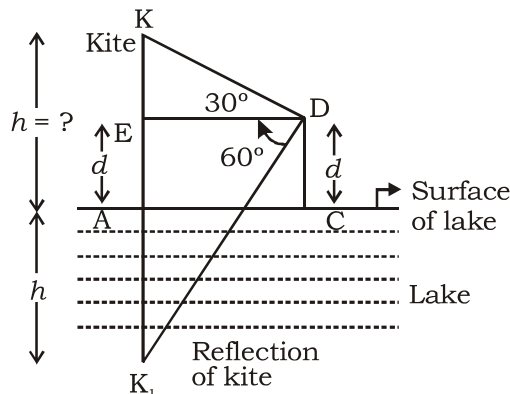
$$\frac{1}{\sqrt{3}} = \frac{2000\sqrt{3}}{AD_2}$$

$$\Rightarrow AD_2 = 6000 \text{ m}$$

$$\therefore D_1D_2 = 6000 - 2000 = 4000 \text{ m}$$

$$\begin{aligned} \text{Speed of the Jet} &= \frac{4000}{18} \times \frac{18}{5} \\ &= 800 \text{ km/h} \end{aligned}$$

87. (C)



Let  $K_1$  be the reflection of kite  $K$ .

Then  $AK = h$  (say)  $= AK_1$

$D$  is a point above the surface  $AC$  of the lake such that  $CD = d = AE$

Then, In  $\triangle KED$ ,

$$\tan 30^\circ = \frac{KE}{ED} = \frac{h-d}{ED} \quad \dots (i)$$

In  $\triangle K_1ED$ ,

$$\tan 60^\circ = \frac{K_1E}{ED} = \frac{h+d}{ED} \quad \dots (ii)$$

Dividing (i) by (ii), ( $ED$  get cancelled)

$$\Rightarrow \frac{1}{3} = \frac{h-d}{h+d} \Rightarrow h = 2d$$

88. (B) Let the no. of sides of the polygon  $= n$

So, there are  $n$  interior angles which are in A.P.

Now,

Sum of  $n$  interior angles

$$= S_n = \frac{n}{2} [2a + (n-1)d]$$

Where,

$$a = 120^\circ$$

$$d = 5$$

$$\therefore S_n = \frac{n}{2} [2 \times 120^\circ + (n-1)5^\circ] \quad \dots (i)$$

But, also, using the formula,

Sum of interior angles for  $n$ -sided

polygon  $= (2n-4) \times 90^\circ$

From (1) and (2)

$$(2n-4) \times 90^\circ = \frac{n}{2} [2 \times 120^\circ + (n-1)5^\circ]$$

$$\Rightarrow n^2 - 25n + 144 = 0$$

$$\Rightarrow (n-16)(n-9) = 0$$

$$n = 16 \text{ or } 9$$

16<sup>th</sup> interior angle

$$= a + (n-1)d, \text{ where } a = 120^\circ, n = 16$$

$$= 120 + (16-1) \times 5$$

$$= 195^\circ, \text{ which is greater than } 180^\circ.$$

Since no interior angle of a regular polygon can exceed  $180^\circ$ .

So,  $n = 16$  is not valid.

Hence, no. of sides of the polygon is 9.

89. (A) Volume of earth dug out

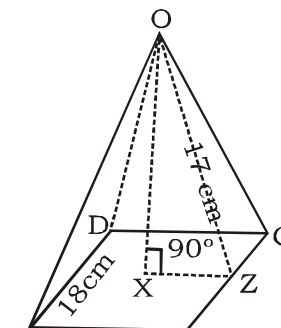
$$= \pi r^2 h = \frac{22}{7} \times \left(\frac{3.5}{2}\right)^2 \times 12 = 115.5 \text{ m}^3$$

The earth dug out is exactly spread to form a platform of height  $h$  m.

$$\Rightarrow 115.5 = 10.5 \times 8 \times h$$

$$\Rightarrow h = 1.375 \text{ m}$$

90. (C)



$AB = 24 \text{ cm}$

Let  $OABCD$  be the right pyramid whose

$AB = DC = 24 \text{ cm}$

$BC = AD = 18 \text{ cm}$

If  $Z$  is the mid point of side  $BC$ , then  $OZ =$  slant height  $= l = 17 \text{ cm}$



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In  $\Delta OXZ$ ,  $\angle X = 90^\circ$

$$\Rightarrow OX = \text{height} = \sqrt{OZ^2 - XZ^2}$$

$$\Rightarrow h = \sqrt{17^2 - \left(\frac{DC}{2}\right)^2}$$

$$\Rightarrow h = \sqrt{17^2 - 12^2}$$

$$\Rightarrow h = 12.04 \text{ cm}$$

Now,

$$\text{Volume} = \frac{1}{3} Ah$$

$$= \frac{1}{3} \times 24 \times 18 \times 12.04$$

$$= 1733.76 \text{ cm}^3$$

$$= 1733.5 \text{ cm}^3 (\text{approx.})$$

	September	October
	<b>Total sales</b> $= \frac{1560}{13} \times 100$ $= 12000$	<b>Total sales</b> $= \frac{2250}{15} \times 100$ $= 15000$
A	$12000 \times \frac{3}{100} = 360$	$15000 \times \frac{5}{100} = 750$
B	$12000 \times \frac{13}{100} = 1560$	$15000 \times \frac{15}{100} = 2250$
C	$12000 \times \frac{22}{100} = 2640$	$15000 \times \frac{25}{100} = 3750$
D	$12000 \times \frac{25}{100} = 3000$	$15000 \times \frac{20}{100} = 3000$
E	$12000 \times \frac{17}{100} = 2040$	$15000 \times \frac{10}{100} = 1500$
F	$12000 \times \frac{8}{100} = 960$	$15000 \times \frac{13}{100} = 1950$
G	$12000 \times \frac{12}{100} = 1440$	$15000 \times \frac{12}{100} = 1800$

91. (A) Required difference

$$\left(12000 \times \frac{D+C}{100}\right) - \left(15000 \times \frac{A+E}{100}\right)$$

$$\left(12000 \times \frac{25+22}{100}\right) - \left(15000 \times \frac{5+10}{100}\right)$$

$$= 5640 - 2250 = 3390$$

92. (B) There is only one absolute decrease i.e. E.

93. (D)  $A + B = 360 + 1560 = 1920$  i.e.

approximately equal to F type of tyres in

October i.e. 1950.

94. (B) Required difference

$$= (750 + 2250 + 3750 + 1950 + 1800)$$

$$- (360 + 1560 + 2640 + 960 + 1440)$$

$$= 10500 - 6960 = 3540$$

[Note : D and E decreasing in sales]

95. (D) Number of tyres D and E sold in September

$$= 3000 + 2040 = 5040$$

Number of tyres D and E sold in October

$$= 3000 + 1500 = 4500$$

Required percentage

$$= \frac{5040}{4500} \times 100 = 112\%$$

96. (C) Leather goods turnover in Tanzania

$$= 40 \times \frac{25}{100} = \$ 10 \text{ million}$$

Leather goods turnover in Africa

$$= 30 \text{ million}$$

Rest of Africa turnover for leather goods

$$= \$ 30 \text{ million} - 10 \text{ million}$$

$$= \$ 20 \text{ million}$$

$$\text{Required percentage} = \frac{20}{30} \times 100$$

$$= 66.67\% = 67\%$$

97. (C) Jewellery items turnover in Tanzania

$$= 40 \times \frac{20}{100} = \$ 8 \text{ million}$$

Jewellery items turnover in Africa

$$= \$ 10 \text{ million}$$

$\therefore$  Jewellery items turnover in rest of Africa

$$= \$ 10 \text{ million} - \$ 8 \text{ million}$$

$$= \$ 2 \text{ million}$$

Garments items turnover in Tanzania

$$= 40 \times \frac{30}{100} = \$ 12 \text{ million}$$

Garments items turnover in Africa

$$= \$ 40 \text{ million}$$

$\therefore$  Garments items turnover in rest of Africa

$$= 40 - 12 = \$ 28 \text{ million}$$

Total of Jewellery items and Garments

items turnover in rest of Africa

$$= 2 + 28 = \$ 30 \text{ million}$$

Turnover from Tanzania from Electrical and leather goods

$$= 40 \times \frac{10}{100} + 40 \times \frac{25}{100}$$

$$= 4 + 10 = \$ 14 \text{ million}$$

$$\text{Ratio} = \frac{30}{14} = 2.14 : 1$$

98. (B) Turnover from Tanzania for Electrical goods and Handicraft together

$$= 40 \times \frac{10}{100} + 40 \times \frac{15}{100}$$



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$= 4 + 6 = \$ 10$  million  
Turnover of Garment in Tanzania

$$= 40 \times \frac{30}{100} = \$ 12 \text{ million}$$

Turnover of Garment in Africa  
 $= \$ 40$  million

Turnover from rest of Africa for Garments  
 $= \$ 40 \text{ million} - \$ 12 \text{ million}$   
 $= \$ 28 \text{ million}$

According to question,  
 $28 \times x = 10$

$$\therefore x = \frac{10}{28} = 0.36 \text{ times}$$

99. (D) Turnover from Jewellery and Garments together from Tanzania

$$= 40 \times \frac{20}{100} + 40 \times \frac{30}{100}$$
$$= \$ 20 \text{ million}$$

Turnover from the rest of Africa for Electrical and Leather goods together

$$= (15 + 30) - \left( 40 \times \frac{10 + 25}{100} \right)$$

$$= 45 - 14 = \$ 31 \text{ million}$$

Required percentage

$$= \frac{20}{31} \times 100 = 65\%$$

100. (C) Turnover from rest of Africa for Electrical

$$\text{goods} = 15 - 40 \times \frac{10}{100}$$
$$= \$ 11 \text{ million}$$

$$\text{Now, } 11 \times \frac{120}{100} = \$ 13.2 \text{ million}$$

Turnover from Tanzania for handicrafts

$$\text{items} = 40 \times \frac{15}{100} = \$ 6 \text{ million}$$

$$\therefore \text{Required ratio} = \frac{6}{13.2}$$
$$= 6 : 13$$



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**SSC MAINS (MATHS) MOCK TEST -16 (ANSWER SHEET)**

- |       |       |       |       |        |
|-------|-------|-------|-------|--------|
| 1. A  | 21. C | 41. C | 61. B | 81. B  |
| 2. C  | 22. B | 42. A | 62. C | 82. *  |
| 3. A  | 23. A | 43. B | 63. A | 83. C  |
| 4. A  | 24. C | 44. B | 64. C | 84. D  |
| 5. B  | 25. A | 45. A | 65. A | 85. C  |
| 6. D  | 26. A | 46. B | 66. D | 86. A  |
| 7. A  | 27. A | 47. C | 67. A | 87. C  |
| 8. C  | 28. B | 48. C | 68. C | 88. B  |
| 9. B  | 29. D | 49. C | 69. A | 89. A  |
| 10. C | 30. A | 50. A | 70. B | 90. C  |
| 11. C | 31. A | 51. B | 71. D | 91. A  |
| 12. A | 32. C | 52. B | 72. B | 92. B  |
| 13. D | 33. C | 53. A | 73. C | 93. D  |
| 14. C | 34. D | 54. A | 74. D | 94. B  |
| 15. C | 35. A | 55. A | 75. C | 95. D  |
| 16. D | 36. B | 56. D | 76. B | 96. C  |
| 17. * | 37. D | 57. C | 77. A | 97. C  |
| 18. C | 38. A | 58. A | 78. C | 98. B  |
| 19. B | 39. A | 59. B | 79. D | 99. D  |
| 20. D | 40. * | 60. B | 80. B | 100. C |