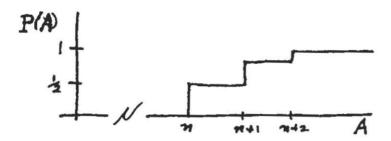
1



6) 
$$\langle f \rangle = 2 f_0(\frac{1}{2}) + f_0(\frac{1}{3}) + 4 f_0(\frac{1}{6}) = f_0(\frac{3}{3} + \frac{1}{3} + \frac{2}{3}) = 2 f_0$$

c) 
$$\langle f^2 \rangle = 4f_0^2(\frac{1}{2}) + f_0^2(\frac{1}{3}) + 16f_0^2(\frac{1}{6}) = f_0^3(\frac{6}{3} + \frac{1}{3} + \frac{8}{3}) = 5f_0^2$$
  
 $Var(f) = \langle f^2 \rangle - \langle f \rangle^2 = (5-4)f_0^2 = \frac{f_0^2}{6}$ 

d) ALL BUT ONE ISOTOPE MUST HAVE A=N.

THE OTHER (C4 CHOICES) MUST HAVE A=N+1

$$\Rightarrow p\left(M = (64n+1)m_0\right) = 64 \cdot \frac{1}{3} \cdot \left(\frac{1}{2}\right)^{63}$$

e) USE THE CENTRAL LIMIT THEOREM

$$p(M) \approx \left(\frac{m_o}{\sqrt{2\pi \operatorname{Var}(M)}} e^{-\frac{(M-LM)^2}{2\operatorname{Var}(M)}^2}\right) \cdot \sum_{i=1}^{\infty} \delta(M-im_o)$$

WHERE 
$$\langle M \rangle = 64 \, m_o \langle A \rangle$$
  
 $Var(M) = 64 \, m_o^2 \, V_{ar}(A)$ 

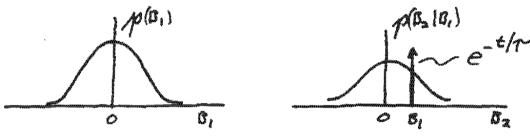
2. a) 
$$p(B_1) = \int_{\infty}^{\infty} p(B_1, B_2) dB_2 = \int_{A \pi 0^2}^{\infty} e^{-t/\tau} = \frac{B_1^2/2\sigma^2}{8^2/2\sigma^2}$$

$$+ \int_{A \pi 0^2}^{\infty} (1 - e^{-t/\tau}) e^{-B_1^2/2\sigma^2} \int_{\sqrt{2\pi\sigma^2}}^{\infty} e^{-B_2^2/2\sigma^2} dB_2$$

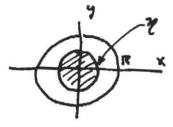
$$= \int_{A \pi 0^2}^{\infty} e^{-B_1^2/2\sigma^2} \int_{NoTe \ THAT \ THIJ \ DOBJ}^{\infty} dB_2$$

$$= \int_{A \pi 0^2}^{\infty} e^{-B_1^2/2\sigma^2} \int_{NoTe \ THAT \ THIJ \ DOBJ}^{\infty} dB_2$$

(b) 
$$p(B_2|B_1) = \frac{p(B_1,B_2)}{p(B_1)} = \frac{e^{-t/\tau} S(B_2-B_1) + (-e^{-t/\tau}) \frac{1}{\sqrt{anc^2}} e^{-\frac{B_2^2}{2}\sigma^2}}{\frac{1}{\sqrt{anc^2}}}$$



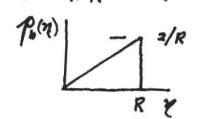
c)  $B_1 + B_2$  ARE NOT S.I. BECAUSE  $p(B_1, B_2) \neq p(B_1) p(B_2)$ NOTE THAT  $p(B_1, B_2)$  DEPENDS ON T BUT  $p(B_1)$  AND  $p(B_2)$  DO NOT.



$$P_{b}(\eta) = (\pi \eta^{2}) \left(\frac{1}{\pi R^{2}}\right) = \eta^{2}/R^{2}$$

$$p(\eta) = \frac{dP(\eta)}{d\eta} = 2\eta/R^2 \quad 0 < \eta < R$$

$$= 0 \quad ELSEWARE$$

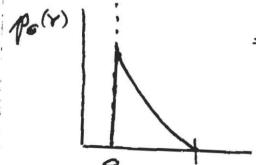


$$P_{\phi}(r) = \int_{a}^{\infty} p(b) db$$

$$p_{\Theta}(r) = \frac{d}{dr} P_{\Theta}(r) = (-1)\left(-\frac{d}{2} \csc^{2}(r/2)\right)\left(\frac{1}{2} \left(\frac{1}{2} \cot(r/2)\right)/R^{2}\right)$$

$$= \frac{d^{2}}{R^{2}} \frac{1}{\sin^{2}(r/2)} \frac{\cos(r/2)}{\sin(r/2)}$$

$$= \frac{1^2}{R^2} \frac{\cos(r/2)}{\sin^3(r/2)}$$



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