1. a)
$$C_V \sim (CLASSICAL RESOLT) \times (\frac{FRACTION OF}{ELECTRONS INFLOEMED}) = (\frac{3}{4}Nk)(\frac{kT}{E_F})$$

$$\propto T \Rightarrow \underline{M=1} \quad IN \quad C_V = VVT$$

a)
$$\frac{dI}{dI} = \frac{dI}{dI} \frac{dE}{dI} = -4\pi R^2 \sigma T^4 / r (\frac{4}{3}\pi R^3) T$$

 $\frac{dI}{dI} = -\frac{3\sigma}{4R} T^3$

SOLUTION (NOT REQUIRED)

$$-\frac{dT}{T^{3}} = \frac{30}{7R} dt$$

$$-\int_{T_{0}}^{T(t)} \frac{dT}{T^{3}} = \frac{30}{7R} t = \frac{1}{2} \left(T(t)^{2} - T_{0}^{-2} \right)$$

$$T^{2}(t) = T_{0}^{-2} + \frac{60}{7R} t = \frac{1}{T_{0}^{2}} \left(1 + \frac{60T_{0}^{2}}{7R} t \right)$$

$$T(t)/T_{0} = \left(1 + t/T \right)^{-1/2}$$

$$D(\vec{k}) = \frac{1}{2V/L_y} \qquad D(\vec{k}) = \frac{1}{2V/L_y} = \frac{A}{(2\pi)^2} \quad \forall \quad \vec{k}$$

$$|\vec{k}_y\rangle \qquad 50/N \qquad 3 \quad 2AV \quad 3W$$

= 2
$$\mathbb{D}(\vec{k})$$
 $n'k^2 = \frac{2A\pi}{(2\pi)^2}$ $\frac{2me}{k^2}$

$$\int h_{x} D(\epsilon) = \frac{d\#}{d\epsilon} = \frac{Am}{n \hbar^{2}}$$

c)
$$N = \int_{0}^{\epsilon_{F}} D(\epsilon) d\epsilon = \left(\frac{Am}{r \hbar^{2}}\right) \epsilon_{F} \implies \epsilon_{F} = \frac{r \pi \hbar^{2}}{m} \frac{N}{A}$$

$$E = \int_{0}^{\epsilon_{f}} \epsilon D(\epsilon) d\epsilon = () \pm \epsilon_{f}^{2} = \pm N \epsilon_{f}$$

$$E_{\text{Electron Ger}} = \frac{\gamma r h^2}{2m} \frac{N^2}{4 \pi R^2} = \frac{h^2}{8m} \frac{N^2}{R^2}$$

$$M = \mu_0 \left(\frac{2 \mu_0 H}{2 \pi \kappa^2} \right)$$

$$= \frac{\mu_0^2 H m}{\pi \kappa^2} 4 \pi R^2$$

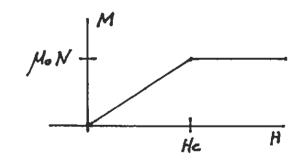
$$= \frac{\mu_0^2 H m}{\pi \kappa^2} 4 \pi R^2$$

$$D_0^{(6)} \qquad D_1^{(6)} \qquad M = \frac{4 m \mu_0^2 R^2}{\pi^2} H$$

$$M = \mu_0 (2 \mu_0 H) \frac{A m}{2 \pi R^2}$$

$$= \frac{\mu_0^2 H m}{\pi K^2} 4 \pi R^2$$

$$M = \frac{4m\mu_0^2 R^2}{L^2} H \qquad M < \mu_0 N$$



$$\frac{4m\mu_0^2R^2Hc}{\hbar^2} = \mu_0N$$

$$Hc = \frac{N\hbar^2}{4mR^2No}$$

3. a)
$$\langle \mu \rangle = \iint p(\theta, e) \left[\mu_0 \cos \theta \right] d\Omega$$

But $\frac{d\mathbb{Z}_1}{d\eta} = \iint \cos \theta e^{\frac{\eta}{\eta}\cos \theta} d\Omega$

$$= \frac{\mathbb{Z}_1}{\rho_0} \iint \left[\mu_0 \cos \theta \right] p(\theta, e) d\Omega = \frac{\mathbb{Z}_1}{\rho_0} \langle \mu \rangle$$

Thus $M = N \langle \mu \rangle = \frac{N \mu_0}{\mathbb{Z}_1} \frac{d\mathbb{Z}_1}{d\eta}$

b) $M = N \mu_0 \frac{\eta}{\sinh(\eta)} \left[\frac{1}{\eta} \cosh(\eta) - \frac{1}{\eta^2} \sinh(\eta) \right]$
 $M = \mu \mu_0 \left[\coth(\eta) - \frac{1}{\eta} \right]$

c) lim M(7) = NHO (37) = NHO HEAT

IIM N/40 M(7) = N/40 (1- HT) FOR LOW T

N/40 M(T)

T

N/40 T

d) CURIE LAW => M = # FOR HIGHT YES

ENERCY GAP => e^D/AT LEADING T DEP, AT LOW T

NO BECAUSE THERE IS NO GAP

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