

Lecture Notes in Computer Science

Edited by G. Goos and J. Hartmanis

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Kathleen Jensen
Niklaus Wirth

PASCAL
User Manual and Report



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PREFACE

This manual is directed to those who have previously acquired some programming skill. The intention is to provide a means of learning Pascal without outside guidance. It is based on The Programming Language Pascal (Revised Report) [1]--the basic definition of Pascal and concise reference manual for the experienced Pascal programmer.

The linear structure of a book is by no means ideal for introducing a language, whether it be a formal or natural one. Nevertheless, it is recommended to follow the given organization, paying particular attention to the example programs, and then to reread those sections causing difficulties. One may wish, however, to reference chapter 12 if troubles arise concerning the input and output conventions of the programs.

The manual was prepared as a file on a computer, that is, as a sequence of characters of a single type font. This is very convenient for the purposes of updating; unfortunately, it is sometimes a bit awkward to read. The reader is asked to be indulgent with the absence of sub- and superscripts (e.g. m raised to the power n is denoted by $m**n$).

Chapters 0--12 define the language Pascal and serve as a standard for both the implementor and the programmer. The implementor must regard the task of recognizing Standard Pascal as the minimum requirement of his system, while the programmer who intends his programs to be transferable from one installation to another should use only features described as Standard Pascal. On the other hand, any implementation may (and usually does) go beyond the minimum. Chapters 13 and 14 document the implementation of Pascal on the CDC 6000 machine. Chapter 13 describes the additional features of the language PASCAL 6000, whereas chapter 14 is devoted to the use of the compiler and the system under the operating system SCOPE.

The efforts of many go into this manual, and we especially thank the members of the Institut fuer Informatik, ETH Zurich, and John Larmouth, Rudy Schild, Olivier Lecarme, and Pierre Desjardins for their criticism, suggestions, and encouragement. Our implementation of Pascal--which made this manual both possible and necessary--is the work of Urs Ammann, aided by Helmut Sandmayr.

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June 1974

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INTRODUCTION

Much of the following text assumes the reader has a minimal grasp of computer terminology and a "feeling" for the structure of a program. The purpose of this section is to spark that intuition.

```
{ program 0.1
assuming annual inflation rates of 7, 8, and 10 per cent.
find the factor by which the frank, dollar, pound
sterling, mark, or guilder will have been devalued in
1, 2, ... n years.}
```

```
program inflation(output);
```

```
const n = 10;
var i : integer; w1,w2,w3 : real;
begin i := 0; w1 := 1.0; w2 := 1.0; w3 := 1.0;
repeat i := i+1;
  w1 := w1 * 1.07;
  w2 := w2 * 1.08;
  w3 := w3 * 1.10;
  writeln(i,w1,w2,w3)
until i=n
end.
```

1	1.070000000000e+00	1.080000000000e+00	1.100000000000e+00
2	1.144900000000e+00	1.166400000000e+00	1.210000000000e+00
3	1.225043000000e+00	1.259712000000e+00	1.331000000000e+00
4	1.310796010000e+00	1.360488960000e+00	1.464100000000e+00
5	1.402551730700e+00	1.469328076800e+00	1.610510000000e+00
6	1.500730351849e+00	1.586874322944e+00	1.771561000000e+00
7	1.605781476478e+00	1.713824268779e+00	1.948717100000e+00
8	1.718186179832e+00	1.850930210282e+00	2.143588810000e+00
9	1.838459212420e+00	1.999004627104e+00	2.357947691000e+00
10	1.967151357290e+00	2.158924997273e+00	2.593742460100e+00

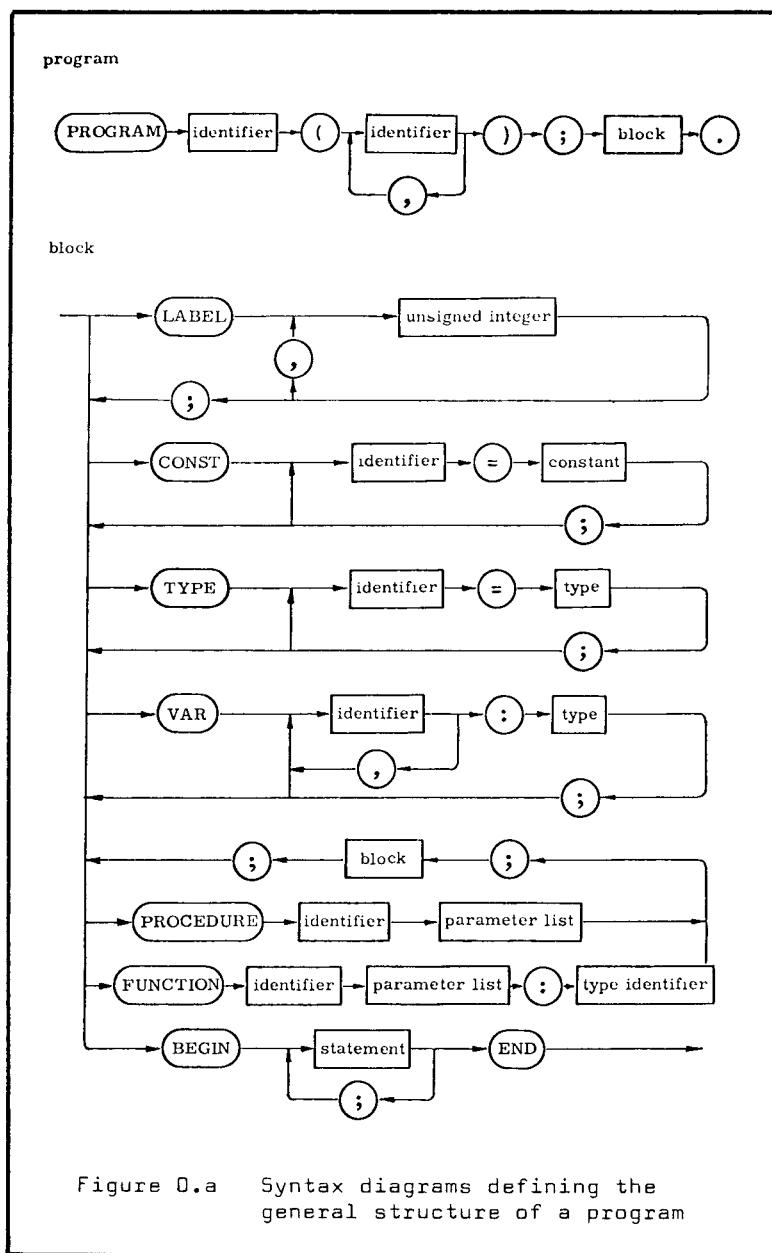
An algorithm or computer program consists of two essential parts, a description of actions which are to be performed, and a description of the data, which is manipulated by these actions. Actions are described by so-called statements, and data is described by so-called declarations and definitions.

The program is divided into a heading and a body, called a block. The heading gives the program a name and lists its parameters. (These are (file) variables and represent the arguments and results of the computation. See chapter 13.) The file "output" is a compulsory parameter. The block consists of six sections, where any except the last may be empty. In the required order they are:

```
<label declaration part>
<constant definition part>
<type definition part>
<variable declaration part>
<procedure and function declaration part>
<statement part>
```

The first section lists all labels defined in this block. The second section defines synonyms for constants; i.e. it introduces identifiers that may later be used in place of those constants. The third contains type definitions; and the fourth, variable definitions. The fifth section defines subordinate program parts (i.e. procedures and functions). The statement part specifies the actions to be taken.

The above program outline is more precisely expressed in a syntax diagram. Starting at the diagram named program, a path through the diagram defines a syntactically correct program. Each box references a diagram by that name, which is then used to define its meaning. Terminal symbols (those actually written in a Pascal program) are in rounded enclosures. (See appendix D for the full syntax diagram of Pascal.)

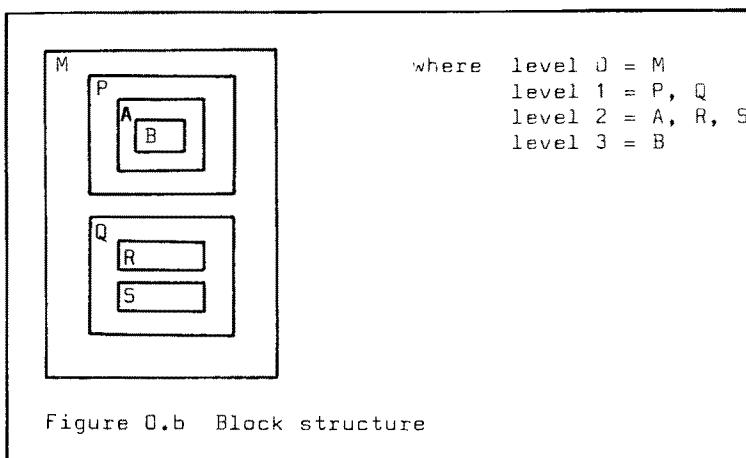


An alternative formulation of a syntax is the traditional Backus-Naur Form, where syntactic constructs are denoted by English words enclosed between the angular brackets < and >. These words are suggestive of the nature or meaning of the construct. A sequence of constructs (1 or more elements) enclosed by the meta-brackets { and } imply their repetition zero or more times. (For the BNF of Pascal, see appendix D.) As an example, the construct <program> of figure 0.a is defined by the following formulas, called "productions":

```
<program> ::= <program heading> <block> .
<program heading> ::= program <identifier> ( <file identifier>
                                              { . <file identifier>} ) :
<file identifier> ::= <identifier>
```

Each procedure (function) has a structure similar to a program; i.e. each consists of a heading and a block. Hence, procedures may be declared (nested) within other procedures. Labels, constant synonyms, type, variable, and procedure declarations are local to the procedure in which they are declared. That is, their identifiers have significance only within the program text which constitutes the procedure declaration and which is called the scope of these identifiers. Since procedures may be nested, so may scopes. Objects which are declared in the main program, i.e. not local to some procedure, are called global and have significance throughout the entire program.

Since blocks may be nested within other blocks by procedure and function declarations, one is able to assign a level of nesting to each. If the outermost program-defined block (e.g. the main program) is called level 0, then a block defined within this block would be of level 1; in general, a block defined in level *i* would be of level (*i*+1). Figure 0.b illustrates a block structure.



In terms of this formulation, the scope or range of validity of an identifier *x* is the entire block in which *x* is defined, including those blocks defined in the same block as *x*. (For this example, note that all identifiers must be distinct. Section 3.e discusses the case where identifiers are not necessarily distinct.)

objects defined in block	are accessible in blocks
M	M,P,A,B,Q,R,S
P	P,A,B
A	A,B
B	B
Q	Q,R,S
R	R
S	S

For programmers acquainted with ALGOL, PL/I, or FORTRAN, it may prove helpful to glance at Pascal in terms of these other languages. For this purpose, we list the following characteristics of Pascal:

1. Declaration of variables is mandatory.
2. Certain key words (e.g. begin, end, repeat) are "reserved" and cannot be used as identifiers. In this manual they are underlined.
3. The semicolon (:) is considered as a statement separator, not a statement terminator (as e.g. in PL/I).
4. The standard data types are those of whole and real numbers, the logical values, and the (printable) characters. The basic data structuring facilities include the array, the record (corresponding to COBOL's and PL/I's "structure"), the set, and the (sequential) file. These structures can be combined and nested to form arrays of sets, files of records, etc. Data may be allocated dynamically and accessed via pointers. These pointers allow the full generality of list processing. There is a facility to declare new, basic data types with symbolic constants.
5. The set data structure offers facilities similar to the PL/I "bit string".
6. Arrays may be of arbitrary dimension with arbitrary bounds; the array bounds are constant. (i.e. There are no dynamic arrays.)
7. As in FORTRAN, ALGOL, and PL/I, there is a go to statement. Labels are unsigned integers and must be declared.
8. The compound statement is that of ALGOL, and corresponds to the DO group in PL/I.
9. The facilities of the ALGOL switch and the computed go to of FORTRAN are represented by the case statement.
10. The for statement, corresponding to the DO loop of FORTRAN, may only have steps of 1 (up) or -1 (downto) and is executed only as long as the value of the control variable lies within the limits. Consequently, the controlled statement may not be executed at all.

11. There are no conditional expressions and no multiple assignments.
12. Procedures and functions may be called recursively.
13. There is no "own" attribute for variables (as in ALGOL).
14. Parameters are called either by value or by reference; there is no call by name.
15. The "block structure" differs from that of ALGOL and PL/I insofar as there are no anonymous blocks, i.e. each block is given a name, and thereby is made into a procedure.
16. All objects--constants, variables, etc.--must be declared before they are referenced. The following two exceptions are however allowed:
 - 1) the type identifier in a pointer type definition (chapter 10)
 - 2) procedure and function calls when there is a forward reference (chapter 11).

Upon first contact with Pascal, many tend to bemoan the absence of certain "favorite features". Examples include an exponentiation operator, concatenation of strings, dynamic arrays, arithmetic operations on Boolean values, automatic type conversions, and default declarations. These were not oversights, but deliberate omissions. In some cases their presence would be primarily an invitation to inefficient programming solutions; in others, it was felt that they would be contrary to the aim of clarity and reliability and "good programming style". Finally, a rigorous selection among the immense variety of programming facilities available had to be made in order to keep the compiler relatively compact and efficient--efficient and economical for both the user who writes only small programs using few constructs of the language and the user who writes large programs and tends to make use of the full language.

1
NOTATION AND VOCABULARY

The basic vocabulary consists of basic symbols classified into letters, digits, and special symbols. The special symbols are operators and delimiters:

+	:	(<u>and</u>	<u>end</u>	<u>nil</u>	<u>set</u>
-)	<u>array</u>	<u>file</u>	<u>not</u>	<u>then</u>
*	=	[<u>begin</u>	<u>for</u>	<u>of</u>	<u>to</u>
/	<>]	<u>case</u>	<u>function</u>	<u>or</u>	<u>type</u>
:=	<	{	<u>const</u>	<u>goto</u>	<u>packed</u>	<u>until</u>
.	<=	}	<u>div</u>	<u>if</u>	<u>procedure</u>	<u>var</u>
.	>=	↑	<u>do</u>	<u>in</u>	<u>program</u>	<u>while</u>
:	>	..	<u>downto</u>	<u>label</u>	<u>record</u>	<u>with</u>
			<u>else</u>	<u>mod</u>	<u>repeat</u>	

Word-delimiters (or reserved words) are normally underlined in the hand-written program to emphasize their interpretation as single symbols with fixed meaning. The programmer may not use these words in a context other than that explicit in the definition of Pascal; in particular, these words may not be used as identifiers. They are written as a sequence of letters (without surrounding escape characters).

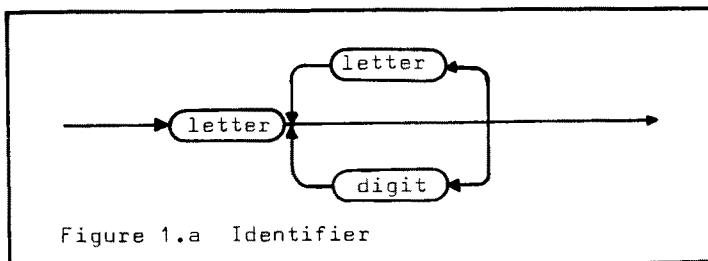
The construct:

{<any sequence of symbols not containing "{}">>}

may be inserted between any two identifiers, numbers, or special symbols. It is called a comment and may be removed from the program text without altering its meaning. The symbols { and } do not occur otherwise in the language, and when appearing in syntactic descriptions, they denote meta-symbols like | and ::=.

(On systems where the curly brackets are unavailable, the character pairs {*} and {*} are used in their place.)

Identifiers are names denoting constants, types, variables, procedures, and functions. They must begin with a letter, which may be followed by any combination and number of letters and digits. Although an identifier may be very long, implementations may impose a limit as to how many of these characters are significant. Implementations of Standard Pascal will always recognise the first 8 characters of an identifier as significant. That is, identifiers denoting distinct objects should differ in their first 8 characters.



examples of legal identifiers:

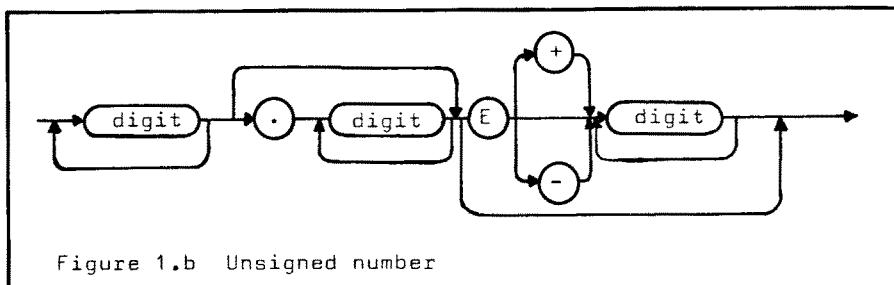
```
sum      root3     pi      h4g      x
thisisaverylongbutneverthelesslegalidentifier
thisisaverylongbutprobablythesameidentifierasabove
```

illegal identifiers:

```
3rd      array     level.4      root-3
```

Certain identifiers, called standard identifiers, are predefined (e.g. sin, cos). In contrast to the word-delimiters (e.g. array), one is not restricted to this definition and may elect to redefine any standard identifier, as they are assumed to be declared in a hypothetical block surrounding the entire program block.

Decimal notation is used for numbers. The letter E preceding the scale factor is pronounced as "times 10 to the power of". The syntax of unsigned numbers is summarized in figure 1.b.



Note that if the number contains a decimal point, at least one digit must precede and succeed the point. Also, no comma may occur in a number.

unsigned numbers:

```
3      03      6272844      0.6      5E-8      49.22E+08      1E 10
```

incorrectly written numbers:

3,487.159 XII .6 E 10 5.E-16

Blanks, ends of lines, and comments are considered as separators. An arbitrary number of separators may occur between any two consecutive Pascal symbols with the following exception: no separators may occur within identifiers, numbers, or special symbols. However, at least one separator must occur between any pair of consecutive identifiers, numbers, or word symbols.

Sequences of characters enclosed by single quote marks are called strings. To include a quote mark in a string, one writes the quote mark twice.

examples of strings:

'a' ';' '3' 'begin' 'don''t'
' this string has 33 characters '

2
THE CONCEPT OF DATA

Data is the general expression describing all that is operated on by the computer. At the hardware and machine code levels, all data are represented as sequences of binary digits (bits). Higher level languages allow one to use abstractions and to ignore the details of representation--largely by developing the concept of data type.

A data type defines the set of values a variable may assume. Every variable occurring in a program must be associated with one and only one type. Although data types in Pascal can be quite sophisticated, each must be ultimately built from unstructured types. An unstructured type is either defined by the programmer, and then called a declared scalar type, or one of the four standard scalar types--integer, real, Boolean, or char.

A scalar type is characterized by the set of its distinct values, upon which a linear ordering is defined. The values are denoted by identifiers in the definition of the type (see chapter 5).

A. The type Boolean

A Boolean value is one of the logical truth values denoted by the predefined identifiers false and true.

The following logical operators yield a Boolean value when applied to Boolean operands: (Appendix B summarizes all operators.)

<u>and</u>	logical conjunction
<u>or</u>	logical disjunction
<u>not</u>	logical negation

Each of the relational operators (=, <>, <=, <, >, >=, in) yields a Boolean value. Furthermore, the type Boolean is defined such that false < true. Hence, it is possible to define each of the 16 Boolean operations using the above logical and relational operators. For example, if p and q are Boolean values, one can express

implication	as	p <= q
equivalence	as	p = q
exclusive OR	as	p <> q

Standard Boolean functions--i.e. standard functions which yield a Boolean result--are: (Appendix A summarizes all standard functions.)

```
odd(x)      true if the integer x is odd, false otherwise
eoln(f)     end of a line, explained in chapter 9
eof(f)      end of file, explained in chapter 9
```

B. The type integer

A value of type integer is an element of the implementation-defined subset of whole numbers.

The following arithmetic operators yield an integer value when applied to integer operands:

```
*   multiply
div divide and truncate (i.e. value is not rounded)
mod a mod b = a - ((a div b)*b)
+   add
-   subtract
```

The relational operators =, <>, <, <=, >=, > yield a Boolean result when applied to integer operands. <> denotes inequality.

Four important standard functions yielding integer results are:

```
abs(x)      the result is the absolute value of x.
sqr(x)      the result is x squared.
trunc(x)    x is a real value; the result is its whole part.
            (The fractional part is discarded. Hence
            trunc(3.7)=3 and trunc(-3.7)=-3)
round(x)    x is a real value; the result is the rounded
            integer. round(x) means for x>=0 trunc(x+0.5), and
            for x<0 trunc(x-0.5)
```

Notes: abs and sqr yield an integer result only when their argument is also of type integer. If i is a variable of type integer, then

succ(i) yields the "next" integer, and
pred(i) yields the preceding integer

This is, however, more clearly expressed by the expressions
i+1 and i-1

There exists an implementation-dependent standard identifier maxint. If a and b are integer expressions, the operation:

a qq b

is guaranteed to be correctly implemented when:

```
abs(a or b)  <= maxint,
abs(a)        <= maxint, and
abs(b)        <= maxint
```

C. The type real

A value of type real is an element of the implementation-defined subset of real numbers.

As long as at least one of the operands is of type real (the other possibly being of type integer) the following operators yield a real value:

```
*   multiply
/   divide (both operands may be integers, but
           the result is always real)
+   add
-   subtract
```

Standard functions when accepting a real argument yield a real result:

```
abs(x)      absolute value
sqr(x)      x squared
```

Standard functions with real or integer argument and real result:

```
sin(x)      trigonometric functions
cos(x)
arctan(x)
ln(x)       natural logarithm
exp(x)      exponential function
sqrt(x)     square root
```

Warning: although real is included as a scalar type, it cannot always be used in the same context as the other scalar types. In particular, the functions pred and succ cannot take real arguments, and values of type real cannot be used when indexing arrays, nor in controlling for statements, nor for defining the base type of a set.

D. The type char

A value of type char is an element of a finite and ordered set of characters. Every computer system defines such a set for the purpose of communication. These characters are then available on the input and output equipment. Unfortunately, there does not

exist one standard character set; therefore, the definition of the elements and their ordering is strictly implementation dependent.

The following minimal assumptions hold for the type char, independent of the underlying implementation:

- The character set includes
1. the alphabetically ordered set of capital Latin letters A...Z
 2. the numerically ordered and contiguous set of the decimal digits 0...9
 3. the blank character.

A character enclosed in apostrophes (single quotes) denotes a constant of this type.

examples:

'*' 'G' '3' ' ' 'X'

(To represent an apostrophe, one writes it twice.)

The two standard functions `ord` and `chr` allow the mapping of the given character set onto a subset of natural numbers--called the ordinal numbers of the character set--and vice versa; `ord` and `chr` are called transfer functions.

`ord(c)` is the ordinal number of the character `c` in the underlying ordered character set. (also see section 5.A)

`chr(i)` is the character value with the ordinal number `i`.

One sees immediately that `ord` and `chr` are inverse functions, i.e.

`chr(ord(c)) = c` -and- `ord(chr(i)) = i`

Furthermore, the ordering of a given character set is defined by
 $c_1 < c_2 \text{ iff } \text{ord}(c_1) < \text{ord}(c_2)$

This definition can be extended to each of the relational operators: `=`, `<>`, `<`, `<=`, `>=`, `>`. If `R` denotes one of these operators, then

`c1 R c2` iff `ord(c1) R ord(c2)`

When the argument of the standard functions `pred` and `succ` is of type `char`, the functions can be defined as:

`pred(c) = chr(ord(c)-1)`
`succ(c) = chr(ord(c)+1)`

Note: The predecessor (successor) of a character is dependent upon the underlying character set and is undefined if one does not exist.

THE PROGRAM HEADING AND THE DECLARATION PART

Every program consists of a heading and a block. The block contains a declaration part, in which all objects local to the program are defined, and a statement part, which specifies the actions to be executed upon these objects.

```
<program> ::= <program heading> <block> .
<block> ::= <label declaration part>
           <constant definition part>
           <type definition part>
           <variable declaration part>
           <procedure and function declaration part>
           <statement part>
```

A. Program heading

The heading gives the program a name (not otherwise significant inside the program) and lists its parameters, through which the program communicates with the environment (see chapter 13.B.1).

```
<program heading> ::= program <identifier> ( <file identifier>
                                              { . <file identifier> } ) ;
```

B. Label declaration part

Any statement in a program may be marked by prefixing the statement with a label followed by a colon (making possible a reference by a goto statement). However, the label must be defined in the label declaration part before its use. The symbol label heads this part, which has the general form:

```
label <label> { . <label> } ;
```

A label is defined to be an unsigned integer, and consists of at most 4 digits.

example:

```
label 3,18;
```

C. Constant definition part

A constant definition introduces an identifier as a synonym for a constant. The symbol const introduces the constant definition part, which has the general form:

```
const <identifier> = <constant>; { <identifier> = <constant>; }
```

where a constant is either" a number, a constant identifier (possibly signed), or a string.

The use of constant identifiers generally makes a program more readable and acts as a convenient documentation aid. It also allows the programmer to group machine or example dependent quantities at the beginning of the program where they can be easily noted and/or changed. (Thereby aiding the portability and modularity of the program.)

As an example, consider the following program:

```
{ program 3.1
example of constant definition part }

program convert(output);

const addin = 32; mulby = 1.8; low = 0; high = 39;
separator = '-----';
var degree : low..high;
begin
writeln(separator);
for degree := low to high do
begin write(degree,'c',round(degree*mulby + addin),'f');
  if odd(degree) then writeln
end;
writeln;
writeln(separator)
end.
```

0c	32f	1c	34f
2c	36f	3c	37f
4c	39f	5c	41f
6c	43f	7c	45f
8c	46f	9c	48f
10c	50f	11c	52f
12c	54f	13c	55f
14c	57f	15c	59f
16c	61f	17c	63f
18c	64f	19c	66f
20c	68f	21c	70f
22c	72f	23c	73f
24c	75f	25c	77f
26c	79f	27c	81f
28c	82f	29c	84f
30c	86f	31c	88f
32c	90f	33c	91f
34c	93f	35c	95f
36c	97f	37c	99f
38c	100f	39c	102f

D. Type definition part

A data type in Pascal may be either directly described in the variable declaration or referenced by a type identifier. Provided are not only several standard type identifiers, but also a mechanism, the type definition, for creating new types. The symbol type introduces a program part containing type definitions. The definition itself determines a set of values and associates an identifier with the set. The general form is:

```
type <identifier> = <type>; {<identifier> = <type>;}
```

Examples of type definitions are found in the subsequent chapters.

E. Variable declaration part

Every variable occurring in a statement must be declared in a variable declaration. This declaration must textually precede any use of the variable.

A variable declaration associates an identifier and a data type with a new variable by simply listing the identifier followed by its type. The symbol var heads the variable declaration part. The general form is:

```
var <identifier> {, <identifier>} : <type>;
{<identifier> {, <identifier>} : <type>;}
```

example:

```
var root1,root2,root3: real;
      count,i: integer;
      found: Boolean;
      filler: char;
```

This identifier/type association is valid throughout the entire block containing the declaration, unless the identifier is redefined in a subordinate block. Suppose a block B is nested within block A. (i.e. declared within the scope of and hence subordinate to A, as in figure 0.b) It is possible to declare an identifier in B that is already declared in A. This has the effect of associating that identifier with a variable local to B--not available to A--which may be of any type. The latter definition is then valid throughout the scope of B, unless redeclared in a block subordinate to B. It is not allowed to declare a single identifier more than once within the same level and scope. Hence the following is always incorrect.

```
var a : integer;
      a : real;
```

F. Procedure and function declaration part

Every procedure or function must be defined (or announced) before its use. Procedure and function declarations are treated in chapter 11. Procedures are subroutines and are activated by procedure statements. Functions are subroutines that yield a result value, and therefore can be used as constituents of expressions.

THE CONCEPT OF ACTION

Essential to a computer program is action. That is, a program must do something with its data--even if that action is the choice of doing nothing! Statements describe these actions. Statements are either simple (e.g. the assignment statement) or structured.

A. The assignment statement

The most fundamental of statements is the assignment statement. It specifies that a newly computed value be assigned to a variable. The form of an assignment is:

```
<variable> := <expression>
```

where `:=` is the assignment operator, not to be confused with the relational operator `=`. The statement "`a := 5`" is pronounced "the current value of `a` is replaced with the value 5", or simply, "`a becomes 5`".

The new value is obtained by evaluating an expression consisting of constant or variable operands, operators, and function designators. (A function designator specifies the activation of a function. Standard functions are listed in Appendix A; user defined functions are explained in chapter 11.) An expression is a rule for calculating a value where the conventional rules of left to right evaluation and operator precedence are observed. The operator `not` (applied to a Boolean operand) has the highest precedence, followed by the multiplying operators (`*, ./, div, mod, and`), then the adding operators (`+, -, or`), and of lowest precedence, the relational operators (`=, <>, <, <=, >, >=, in`). Any expression enclosed within parentheses is evaluated independent of preceding or succeeding operators.

examples:

<code>2 * 3-4 * 5</code>	$= (2*3) - (4*5) = -14$
<code>15 div 4 * 4</code>	$= (15 \text{ div } 4)*4 = 12$
<code>80/5/3</code>	$= (80/5)/3 = 5.333$
<code>4/2 *3</code>	$= (4/2)*3 = 6.000$
<code>sqrt(sqr(3)+11*5)</code>	$= 8.000$

The syntax of Appendix D reflects the exact rules of precedence. The reader is recommended to reference it whenever in doubt.

Boolean expressions have the property that their value may be known before the entire expression has been evaluated. Assume for example, that `x=0`. Then

`(x>0) and (x<10)`

is already known to be false after computation of the first

factor, and the second need not be evaluated. The rules of Pascal neither require nor forbid the evaluation of the second part in such cases. This means that the programmer must assure that the second factor is well-defined, independent of the value of the first factor. Hence, if one assumes that the array a has an index ranging from 1 to 10, then the following example is in error!

```
x := 0;
repeat x := x+1 until (x>10) or (a[x]=0)
```

(Note that if no $a[i] = 0$, the program will refer to an element $a[11]$.)

Direct assignment is possible to variables of any type, except files. However, the variable (or the function) and the expression must be of identical type, with the exception that if the type of the variable is real, the type of the expression may be integer. (If a subrange type is involved, its associated scalar type determines the validity of the assignment; see section 5.8.)

```
examples of assignments:
root1 := pi*x/y
root1 := -root1
root3 := (root1 + root2)*(1.0 + y)
found := y>z
count := count + 1
degree := degree + 10
sqrpr := sqr(pr)
y := sin(x) + cos(y)
```

B. The compound statement

The compound statement specifies that its component statements be executed in the same sequence as they are written. The symbols begin and end act as statement brackets. Note that the "body" of a program has the form of a compound statement.

```
{ program 4.1
the compound statement }

program beginend(output);

var sum : integer;
begin
  sum := 3+5;
  writeln(sum,-sum)
end.
```

Pascal uses the semicolon to separate statements, not to terminate statements; i.e. the semicolon is NOT part of the statement. The explicit rules regarding semicolons are reflected in the syntax of Appendix D. If one had written a semicolon after the second statement, then an empty statement (implying no action) would have been assumed between the semicolon and the symbol end. This does no harm, for an empty statement is allowable at this point. Misplaced semicolons can, however, cause troubles--note the example in section 4.D.

C. Repetitive statements

Repetitive statements specify that certain statements be repeatedly executed. If the number of repetitions is known beforehand (before the repetitions are begun), the for statement is usually the appropriate construct to express the situation; otherwise, the repeat or while statement should be used.

C.1 The while statement

The while statement has the form:

```
while <expression> do <statement>
```

The expression controlling the repetition must be of type Boolean. It is evaluated before each iteration, so care must be taken to keep the expression as simple as possible.

```
{ program 4.2
compute h(n) = 1 + 1/2 + 1/3 + ... + 1/n }

program egwhile(input, output);

var n : integer; h : real;
begin read(n); write(n);
h := 0;
while n>0 do
begin h := h + 1/n; n := n-1
end;
writeln(h)
end.
```

```
10 2.928968253968e+00
```

The statement executed by the while statement (a compound statement in the above case) is repeated until the expression becomes false. If its value is false at the beginning, the

statement is not executed at all.

C.2 The repeat statement

The repeat statement has the form:

```
repeat <statement> { .. <statement>} until <expression>
```

The sequence of statements between the symbols `repeat` and `until` is executed at least once. Repeated execution is controlled by the Boolean expression, which is evaluated after every iteration.

```

{ program 4.3
compute h(n) = 1 + 1/2 + 1/3 + ... + 1/n }

program egrepeat(input, output);

var n : integer; h : real;
begin  read(n); write(n);
       h := 0;
       repeat h := h + 1/n;  n := n-1
       until n=0;
       writeln(h)
end.

```

10 2.928968253968e+00

The above program performs correctly for $n > 0$. Consider what happens if $n \leq 0$. The while-version of the same program is correct for all n , including $n = 0$.

Note that it is a sequence of statements that the repeat statement executes; a bracketing pair begin...end would be redundant (but not incorrect).

C.3 The for statement

The `for` statement indicates that a statement be repeatedly executed while a progression of values is assigned to the control variable of the `for` statement. It has the general form:

```
{ program 4.4
compute h(n) = 1 + 1/2 + 1/3 + ... + 1/n }

program egfor(input, output);

var i,n : integer; h : real;
begin read(n); write(n);
h := 0;
for i := n downto 1 do h := h + 1/i;
writeln(h)
end.
```

10 2.928968253968e+00

```
{ program 4.5
compute the cosine using the expansion:
cos(x) = 1 - x**2/(2*1) + x**4/(4*3*2*1) - ... }
```

```
program cosine(input, output);

const eps = 1e-14;
var x,sx,s,t:real;
i,k,n :integer;
begin read(n);
for i := 1 to n do
begin read(x); t := 1; k := 0; s := 1; sx := sqr(x);
while abs(t) > eps*abs(s) do
begin k := k + 2; t := -t*sx/(k*(k-1));
s := s+t
end;
writeln(x,s,k div 2)
end
end.
```

1.534622222233e-01	9.882477647614e-01	5
3.333333333333e-01	9.449569463147e-01	6
5.000000000000e-01	8.775825618904e-01	7
1.000000000000e+00	5.403023058681e-01	9
3.141592653590e+00	-1.000000000000e+00	14

The control variable, the initial value, and the final value must be of the same scalar type (excluding type real), and must not be altered by the for statement. The initial and final values are evaluated only once. If in the case of to (downto) the initial value is greater (less) than the final value, the for statement is not executed. The final value of the control variable is left undefined upon normal exit from the for statement.

A for statement of the form:

```
for v := e1 to e2 do S
```

is equivalent to the sequence of statements:

```
if e1<=e2 then
begin v := e1; S; v := succ(v); S; ...; v := e2; S
end
{at this point, v is undefined}
```

and a for statement of the form:

```
for v := e1 downto e2 do S
```

is equivalent to the statement:

```
if e1>=e2 then
begin v := e1; S; v := pred(v); S; ...; v := e2; S
end
{at this point, v is undefined}
```

As a final example consider the following program.

```
{ program 4.6
compute 1 - 1/2 + 1/3-...+1/9999 - 1/10000 . 4 ways.
 1) left to right, in succession
 2) left to right, all pos and neg terms, then subtract
 3) right to left in succession
 4) right to left, all pos and neg terms, then subtract}

program summing(output);

var s1,s2p,s2n,s3,s4p,s4n,lrp,lrn,rlp,rln : real;
  i : integer;
begin s1 := 0; s2p := 0; s2n := 0; s3 := 0; s4p := 0; s4n := 0;
  for i := 1 to 5000 do
  begin
    lrp := 1/(2*i-1); { pos terms, left to right }
    lrn := 1/(2*i); { neg terms, left to right}
    rlp := 1/(10001-2*i); { pos terms, right to left}
    rln := 1/(10002-2*i); {neg terms, right to left }
    s1 := s1 + lrp - lrn;
    s2p := s2p + lrp; s2n := s2n + lrn;
    s3 := s3 + rlp - rln;
    s4p := s4p + rlp; s4n := s4n + rln
  end;
  writeln(s1,s2p-s2n);
  writeln(s3,s4p-s4n)
end.
```

```
6.930971830595e-01 6.930971830612e-01
6.930971830599e-01 6.930971830601e-01
```

Why do the four "identical" sums differ?

D. Conditional statements

A conditional statement, an if or case statement, selects a single statement of its component statements for execution. The if statement specifies that a statement be executed only if a certain condition (Boolean expression) is true. If it is false, then either no statement or the statement following the symbol else is executed.

D.1 The if statement

The two forms for an if statement are:

```
if <expression> then <statement>
(or)
if <expression> then <statement> else <statement>
```

The expression between the symbols if and then must be of type Boolean. Note that the first form may be regarded as an abbreviation of the second when the alternative statement is the empty statement. Caution: there is never a semicolon before an else! Hence, the text:

```
if p then begin S1; S2; S3 end; else S4
```

is incorrect. Perhaps even more deceptive is the text:

```
if p then; begin S1; S2; S3 end
```

Here, the statement controlled by the if is the empty statement, between the then and the semicolon; hence, the compound statement following the if statement will always be executed.

The syntactic ambiguity arising from the construct:

```
if <expression-1> then if <expression-2> then <statement-1>
else <statement-2>
```

is resolved by interpreting the construct as equivalent to

```
if <expression-1> then
begin if <expression-2> then <statement-1>
else <statement-2>
end
```

The reader is further cautioned that a carelessly formulated if statement can be very costly. Take the example where one has n-mutually exclusive conditions, c1...cn, each instigating a

distinct action, s_i . Let $P(c_i)$ be the probability of c_i being true, and say that $P(c_i) \geq P(c_j)$ for $i < j$. Then the most efficient sequence of if clauses is:

```
if c1 then s1
else if c2 then s2
else ...
else if c(n-1) then s(n-1) else sn
```

The fulfillment of a condition and the execution of its statement completes the if statement, thereby bypassing the remaining tests.

If "found" is a variable of type Boolean, another frequent abuse of the if statement can be illustrated by:

```
if a=b then found := true else found := false
```

A much simpler statement is:

```
found := a=b
```

```

{ program 4.7
  write roman numerals }

program roman(output);

var x,y : integer;
begin y := 1;
repeat x := y; write(x,' ');
  while x>=1000 do
    begin write('m'); x := x-1000 end;
    if x>=500 then
      begin write('d'); x := x-500 end;
    while x>=100 do
      begin write('c'); x := x-100 end;
    if x>=50 then
      begin write('l'); x := x-50 end;
    while x>=10 do
      begin write('x'); x := x-10 end;
    if x>=5 then
      begin write('v'); x := x-5 end;
    while x>=1 do
      begin write('i'); x := x-1 end;
    writeln; y := 2*y
  until y>5000
end.

```

```

1 i
2 ii
4 iiiii
8 viiii
16 xvii
32 xxxii
64 lxxxxi
128 cxxxviii
256 cclvi
512 dxii
1024 mxxiiii
2048 mmxxxxviii
4096 mmmmlxxxxvi

```

Notice again that it is only one statement that is controlled by an if clause. Therefore, when more than one action is intended, a compound statement is necessary.

The next program raises a real value x to the power y , where y is a non-negative integer. A simpler, and evidently correct version is obtained by omitting the inner while statement: the result z is then obtained through y multiplications by x . Note the loop invariant: $z*(u**e)=x**y$. The inner while statement leaves z and $u**e$ invariant, and obviously improves the efficiency of the algorithm.

```

{ program 4.8
exponentiation with natural exponent }

program exponentiation(input, output);

var e,y: integer; u,x,z: real;
begin  read(x,y); write(x,y);
z := 1; u := x; e := y;
while e>0 do
begin {z*u**e = x**y, e>0}
  while not odd(e) do
    begin e := e div 2; u := sqr(u)
    end;
  e := e-1; z := u*z
end;
writeln(z) {z = x**y}
end.

```

```

2.000000000000e+00          7  1.280000000000e+02

```

The following program plots a real-valued function $f(x)$ by letting the X-axis run vertically and then printing an asterisk in positions corresponding to the coordinates. The position of the asterisk is obtained by computing $y=f(x)$, multiplying by a scale factor s , rounding the product to the next integer, and then adding a constant h and letting the asterisk be preceded by that many blank spaces.

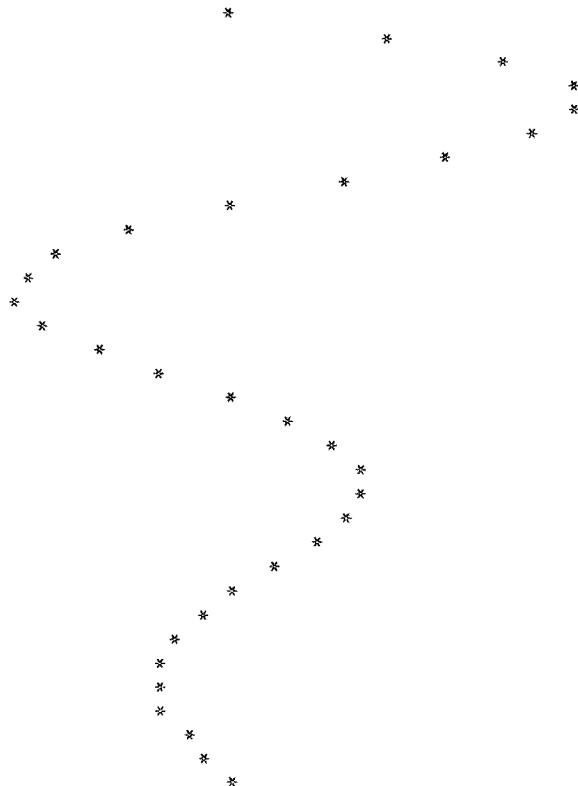
```

{ program 4.9
graphic representation of a function
f(x) = exp(-x) * sin(2*pi*x) }

program graph1(output);

const d = 0.0625; {3/16, 16 lines for interval [x,x+1]}
  s = 31; {31 character widths for interval [y,y+1]}
  h = 34; {character position of x-axis}
  c = 6.28318; {2*pi} lim = 32;
var x,y : real; i,n : integer;
begin x := 0;
  for i := 1 to lim do
    begin y := exp(-x)*sin(c*x); n := round(s*y) + h;
      repeat write(' '); n := n-1
      until n=0;
      writeln('*');
      x := x+d
    end
end.

```



D.2 The case statement

The case statement consists of an expression (the selector) and a list of statements, each being labelled by a constant of the type of the selector. The selector type must be a scalar type, excluding the type real. The case statement selects for execution that statement whose label is equal to the current value of the selector; if no such label is listed, the effect is undefined. Upon completion of the selected statement, control goes to the end of the case statement. The form is:

```
case <expression> of
  <case label list> : <statement>;
  ...
  <case label list> : <statement>
end
```

```
examples: (assume var i: integer; ch: char;)
case i of
  0: x := 0;           case ch of
  1: x := sin(x);    'a', 'g', 'd': ch := succ(ch);
  2: x := cos(x);    'z', 'e': ch := pred(ch);
  3: x := exp(x);    'f', 'g': {null case}
  4: x := ln(x)
end
```

Notes: "Case labels" are not ordinary label (see section 4.E) and cannot be referenced by a goto statement. Their ordering is arbitrary; however, labels must be unique within a given case statement.

Although the efficiency of the case statement depends on the implementation, the general rule is to use it when one has several mutually exclusive statements with similar probability of selection.

E. The goto statement

A **goto** statement is a simple statement indicating that further processing should continue at another part of the program text, namely at the place of the label.

```
goto <label>
```

Each label (an unsigned integer that is at most 4 digits) must appear in a label declaration prior to its occurrence in the program body. The scope of a label L declared in a block A is the entire text of block A. That is, one statement in the statement part of A may be prefixed with L:. Then any other statement within the whole of block A may reference L in a goto statement.

```

example (program fragment):

label 1; {block A}
  ...
procedure B; {block B}
  label 3;
begin
  3: writeln('error');
  ...
  goto 3
  ...
  goto 1

end; {block B}

begin {block A}
  ...
  1: writeln(' test fails')
    {a "goto 3" is not allowed in block A}
end

```

Warning: The effect of jumps from outside of a structured statement into that statement is not defined. Hence, the following examples are incorrect. (Note that compilers do not necessarily indicate an error.)

Illegal examples:

- a) for i:= 1 to 10 do
 begin S1;
 3: S2
 end;
 goto 3
- b) if p then goto 3;
 ...
 if q then 3: S
- c) procedure P
 begin ...
 3: S
 end;
 begin ...
 goto 3
 end.

A goto statement should be reserved for unusual or uncommon situations where the natural structure of an algorithm has to be broken. A good rule is to avoid the use of jumps to express regular iterations and conditional execution of statements, for such jumps destroy the reflection of the structure of computation in the textual (static) structure of the program. Moreover, the lack of correspondence between textual and computational (static and dynamic) structure is extremely detrimental to the clarity of the program and makes the task of

verification much more difficult. The presence of goto's in a Pascal program is often an indication that the programmer has not yet learned "to think" in Pascal (as this is a necessary construct in other programming languages).

5
SCALAR AND SUBRANGE TYPES

A. Scalar types

The basic data types in Pascal are the scalar types. Their definition indicates an ordered set of values by enumerating the identifiers which denote the values.

```
type <type identifier> = ( <identifier> {, <identifier>} ) ;  
  
example:  
type color = (white,red,blue,yellow,purple,green,  
               orange,black);  
sex = (male,female);  
day = (mon,tues,wed,thur,fri,sat,sun);  
operators = (plus,minus,times,divide);  
  
illegal example:  
type workday = (mon,tues,wed,thur,fri,sat);  
               free = (sat,sun);  
(for the type of sat is ambiguous)
```

The reader is already acquainted with the standard type Boolean defined as:

```
type Boolean = (false, true);
```

This automatically implies the standard identifiers false and true and specifies that false<true.

The relational operators =, <>, <, <=, >=, and >, are applicable on all scalar types provided both comparands are of the same types. The order is determined by the sequence in which the constants are listed.

Standard functions with arguments of scalar types are:

succ(x)	e.g. succ(blue) = yellow	the successor of x
pred(x)	pred(blue) = red	the predecessor of x
ord(x)	ord(blue) = 2	the ordinal number of x

The ordinal number of the first constant listed is 0, ord(x) = ord(pred(x)) + 1.

Assuming that c and c1 are of type color (above), b is of type Boolean, and s1..sn are arbitrary statements, then the following are meaningful statements:

```

for c := black downto red do s1
  while (c1<>c) and b do s1
    if c>white then c := pred(c)
    case c of
      red,blue,yellow: s1;
      purple: s2;
      green,orange: s3;
      white,black: s4
    end
  end

```

B. Subrange types

A type may be defined as a subrange of any other already defined scalar type--called its associated scalar type. The definition of a subrange simply indicates the least and the largest constant value in the subrange, where the lower bound must be less than the upper bound. A subrange of the type real is not allowed.

```
type <type identifier> = <constant> .. <constant>;
```

Semantically, a subrange type is an appropriate substitution for the associated scalar type in all definitions. Furthermore, it is the associated scalar type which determines the validity of all operations involving values of subrange types. For example, given the declaration:

```
var a: 1..10; b: 0..30; c:20..30;
```

The associated scalar type for a, b, and c is integer. Hence the assignments

```
a := b; c := b; b:= c;
```

are all valid statements, although their execution may sometimes be infeasible. The phrase "or subrange thereof" is therefore assumed to be implied throughout this text and is not always mentioned (as it is in the Revised Report.)

example:

```
type days = (mon,tues,wed,thur,fri,sat,sun); {scalar type}
workd = mon..fri; {subrange of days}
index = 0..63; {subrange of integer}
letter = 'a'..'z'; {subrange of char}
```

Subrange types provide the means for a more explanatory statement of the problem. To the implementor they also suggest an opportunity to conserve memory space and to introduce validity checks upon assignment at run-time. (For an example with subrange types, see program 6.3.)

STRUCTURED TYPES IN GENERAL--THE ARRAY IN PARTICULAR

Scalar and subrange types are unstructured types. The other types in Pascal are structured types. As structured statements were compositions of other statements, structured types are compositions of other types. It is the type(s) of the components and--most importantly--the structuring method that characterize a structured type.

An option available to each of the structuring methods is an indication of the preferred internal data representation. A type definition prefixed with the symbol packed signals the compiler to economize storage requirements, even at the expense of additional execution time and a possible expansion of the code, due to the necessary packing and unpacking operations. It is the user's responsibility to realize if he wants this trade of efficiency for space. (The actual effects upon efficiency and savings in storage space are implementation dependent, and may, in fact, be nil.)

The array type

An array type consists of a fixed number of components (defined when the array is introduced) where all are of the same type, called the component or base type. Each component can be explicitly denoted and directly accessed by the name of the array variable followed by the so-called index in square brackets. Indices are computable; their type is called the index type. Furthermore, the time required to select (access) a component does not depend upon the value of the selector (index); hence the array is termed a random-access structure.

The definition of an array specifies both the component type and the index type. The general form is:

```
type A = array[T1] of T2;
```

where A is a new type identifier; T1 is the index type and is a scalar type (where types integer and real are not allowable index types); and T2 is any type.

examples of variable declarations -and- sample assignments

memory : array[0..max] of integer	memory[i+j] := x
sick : array[days] of Boolean	sick[mon] := true

(Of course these examples assume the definition of the auxiliary identifiers.)

```

{ program part 6.1
  find the largest and smallest number in a given list }

program minmax(input, output);

const n = 20;
var u,v,min,max : integer;
      a : array[1..n] of integer;
begin
  {assume that at this point in the program, array a
   contains the values: 35 68 94 7 88 -5 -3 12 35 9
   -6 3 0 -2 74 88 52 43 5 4}

  min := a[1]; max := min; i := 2;
  while i < n do
  begin u := a[i]; v := a[i+1];
    if u>v then
      begin if u>max then max := u;
              if v<min then min := v
      end else
      begin if v>max then max := v;
              if u<min then min := u
      end;
    i := i+2
  end;
  if i=n then
    if a[n]>max then max := a[n]
    else if a[n]<min then min := a[n];
  writeln(max,min)
end.

```

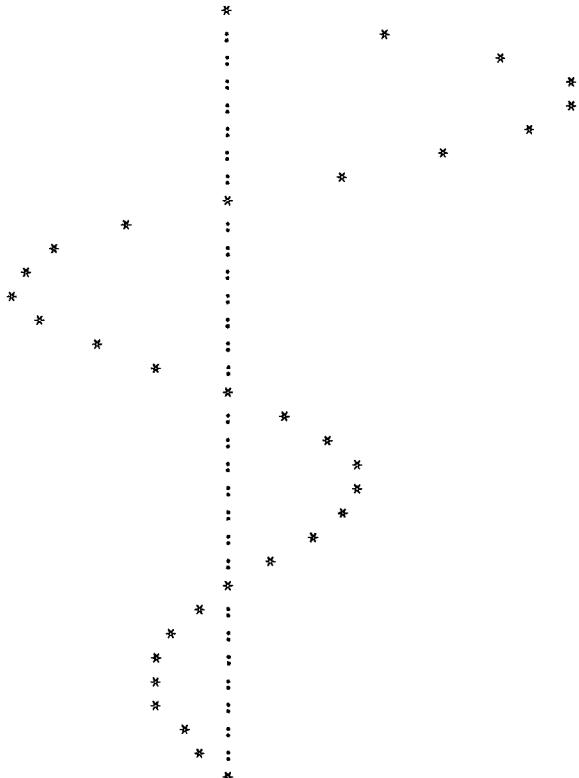
```

{ program 6.2
  extend program 4.9 to print x-axis }

program graph2(output);

const d = 0.0625; {1/16, 16 lines for interval [x,x+1]}
  s = 31; {31 character widths for interval [y,y+1]}
  maxl = 67; {max length of line}
  hl = 34; {character position of x-axis}
  c = 6.28318; {2*pi} lim = 32;
var x,y : real; i,n : integer;
  a : array[0..maxl] of char;
begin x := 0;
  for i := 0 to maxl do a[i] := ' ';
  for i := 1 to lim do
    begin a[hl] := ':';
      y := exp(-x)*sin(c*x); n := round(s*y) + hl;
      a[n] := '*';
      writeln(a);
      a[n] := ' '; x := x + d
    end
  end
end.

```



(Consider how one would extend program 6.2 to print more than one function--both with and without the use of an array.)

Since T2 may be of any type, the components of arrays may be structured. In particular, if T2 is again an array, then the original array A is said to be multidimensional. Hence, the declaration of a multidimensional array M can be so formulated:

```
var M : array[a..b] of array[c..d] of T;  
and  
M[i][j]
```

then denotes the jth component (of type T) of the ith component of M.

For multidimensional arrays, it is customary to make the convenient abbreviations:

```
var M : array[a..b,c..d] of T;  
and  
M[i,j]
```

We may regard M as a matrix and say that M[i,j] is the jth component (in the jth column) of the ith component of M (of the ith row of M).

This is not limited to two dimensions, for T can again be a structured type. In general, the (abbreviated) form is:

```
type <type identifier> =  
    array[<index type> {, <index type>}] of <component type> ;
```

If n index types are specified, the array is said to be n-dimensional, and a component is denoted by n index expressions.

```

{ program 6.3
  matrix multiplication }

program matrixmul(input, output);

const m = 4; p = 3; n = 2;
var i : 1..m; j : 1..n; k : 1..p;
  s : integer;
  a : array[1..m,1..p] of integer;
  b : array[1..p,1..n] of integer;
  c : array[1..m,1..n] of integer;
begin {assign initial values to a and b}
  for i := 1 to m do
    begin for k := 1 to p do
      begin read(s); write(s); a[i,k] := s
      end;
      writeln
    end;
    writeln;
    for k := 1 to p do
      begin for j := 1 to n do
        begin read(s); write(s); b[k,j] := s
        end;
        writeln
      end;
      writeln;
    {multiply a * b}
    for i := 1 to m do
      begin for j := 1 to n do
        begin s := 0;
          for k := 1 to p do s := s + a[i,k]*b[k,j];
          c[i,j] := s; write(s)
        end;
        writeln
      end;
      writeln
    end.
  writeln
end.

```

1	2	3
-2	0	2
1	0	1
-1	2	-3
-1	3	
-2	2	
2	1	
1	10	
6	-4	
1	4	
-9	-2	

Strings were defined earlier as sequences of characters enclosed

in single quote marks (chapter 1). Strings consisting of a single character are the constants of the standard type char (chapter 2); those of n characters ($n > 1$), are defined as constants of the type defined by:

packed array[1..n] of char

Assignment ($:=$) is possible between operands of identical array types. The relational operators $=$, $<$, $<=$, and $>=$ are applicable on operands of identical packed character arrays, where the underlying character set determines the ordering.

Access to individual components of packed arrays is often costly, and the programmer is advised to pack or unpack a packed array in a single operation. This is possible through the standard procedures pack and unpack. Letting A be an array variable of type

array[m..n] of T

and Z be a variable of type

packed array[u..v] of T

where $(n-m) \geq (v-u)$, then

pack(A,i,Z) means for j := u to v do
 $Z[j] := A[j-u+i]$

and

unpack(Z,A,i) means for j := u to v do
 $A[j-u+i] := Z[j]$

where j denotes an auxiliary variable not occurring elsewhere in the program.

7
RECORD TYPES

The record types are perhaps the most flexible of data constructs. Conceptually, a record type is a template for a structure whose parts may have quite distinct characteristics. For example, assume one wishes to record information about a person. Known are the name, the social security number, sex, date of birth, number of dependents, and marital status. Furthermore, if the person is married or widowed, the date of the (last) marriage is given; if divorced, one knows the date of the (most recent) divorce and whether this is the first divorce or not; and if single, given is whether an independent residency is established. All of this information can be expressed in a single "record".

More formally, a record is a structure consisting of a fixed number of components, called **fields**. Unlike the array, components are not constrained to be of identical type and cannot be directly indexed. A type definition specifies for each component its type and an identifier, the **field identifier**, to denote it. The scope of a field identifier is the smallest record in which it is defined. In order that the type of a selected component be evident from the program text (without executing the program), the record selector consists of constant field identifiers rather than a computable value.

To take a simple example, assume one wishes to compute with complex numbers of the form $a+bi$, where a and b are real numbers and i is the square root of -1 . There is no standard type "complex". However, the programmer can easily define a record type to represent complex numbers. This record would need two fields, both of type real, for the real and imaginary parts. The syntax necessary to express this is:

```
<record type> ::= record <field list> end
<field list> ::= <fixed part> | <fixed part> ; <variant part> |
                  <variant part>
<fixed part> ::= <record section> {; <record section>}
<record section> ::= <field identifier> {, <field identifier>} :
                      <type> | <empty>
```

Applying these rules, one can state the following definition and declaration:

```
type complex = record re,im : real
                           end;
var x : complex;
```

where **complex** is a type identifier, **re** and **im** are identifiers of fields, and **x** is a variable of type **complex**. Consequently, **x** is a record made up of two components or fields.

Likewise, a variable representing a date can be defined as:

```
date = record mo:(jan,feb,mar,apr,may,june,
                  july,aug,sept,oct,nov,dec);
           day: 1..31;
           year: integer
         end
```

a toy as:

```
toy = record kind:(ball,top,boat,doll,blocks
                  game,model,book);
           cost: real;
           received: date;
           enjoyed: (alot,some,alittle,none);
           broken,lost: Boolean
         end
```

or a homework assignment as:

```
assignment = record subject:(history,language,lit,
                      math,psych,science);
           assigned: date;
           grade: 0..4;
           weight: 1..10
         end
```

To reference a record component, the name of the record is followed by a point, and the respective field identifier. For example, the following assigns 5+3i to x:

```
x.re := 5;
x.im := 3
```

If the record is itself nested within another structure, the naming of the record variable reflects this structure. For example, assume one wishes to record the most recent small pox vaccination for each member in the family. A possibility is to define the members as a scalar, and then the dates in an array of records:

```
type family= (father,mother,child1,child2,child3);
var vaccine: array[family] of date;
```

An update might then be recorded as:

```
vaccine[child3].mo := apr;
vaccine[child3].day := 23;
vaccine[child3].year := 1973
```

Note: the type "date" also includes, for instance, a 31st April.

```

{ program 7.1
operations on complex numbers }

program complex(output);

const fac = 4;
type complex = record re,im : integer end;
var x,y : complex;
n : integer;
begin
  x.re := 2; x.im := 7;
  y.re := 6; y.im := 3;
  for n := 1 to 4 do
    begin
      writeln(' x = ',x.re:3,x.im:3, ' y = ',y.re:3,y.im:3);
      {x + y}
      writeln(' sum = ',x.re + y.re:3,
              x.im + y.im:3);
      {x * y}
      writeln(' product = ',x.re*y.re - x.im*y.im:3,
              x.re*y.im + x.im*y.re:3);
      writeln;
      x.re := x.re + fac; x.im := x.im - fac;
    end
  end.

```

x = 2 7 y = 6 3
sum = 8 10
product = -9 48

x = 6 3 y = 6 3
sum = 12 6
product = 27 36

x = 10 -1 y = 6 3
sum = 16 2
product = 63 24

x = 14 -5 y = 6 3
sum = 20 -2
product = 99 12

The syntax for a record type also makes provisions for a variant part, implying that a record type may be specified as consisting of several variants. This means that different variables, although said to be of the same type, may assume structures which differ in a certain manner. The differences may consist of a different number and different types of components.

Each variant is characterised by a list, in parentheses, of declarations of its pertinent components. Each list is labelled by one or more labels, and the set of lists is preceded by a case clause specifying the data type of these labels (i.e. the

type according to which the variants are discriminated). As an example, assume the existence of a

```
type maritalstatus = (married, widowed, divorced, single)
```

Then one can describe persons by data of the

```
type person =
  record <attributes or fields common to all persons> ;
    case maritalstatus of
      married: (<fields of married persons only>) ;
      single:  (<fields of single persons only>) ;
      .....
  end
```

Usually, a component (field) of the record itself indicates its currently valid variant. For example, the above defined person record is likely to contain a common field

```
ms : maritalstatus
```

This frequent situation can be abbreviated by including the declaration of the discriminating component--the so-called tag field--in the case clause itself, i.e. by writing

```
case ms: maritalstatus of
```

The syntax defining the variant part is:

```
<variant part> ::= case <tag field> <type identifier> of
  <variant> {; <variant>}
<variant> ::= <case label list> : ( <field list> ) | 
  <empty>
<case label list> ::= <case label> {, <case label>}
<case label> ::= <unsigned constant>
<tag field> ::= <identifier> : | <empty>
```

It is helpful to "outline" the information about a person, before defining it as a variant record structure.

```
I. Person
A. name (last, first)
B. social security number (integer)
C. sex (male, female)
D. date of birth (month, day, year)
E. number of dependents (integer)
F. marital status
  if married,widowed
    a. date of marriage (month, day, year)
  if divorced
    a. date of divorce (month, day, year)
    b. first divorce (false, true)
  if single
    a. independent residency (false,true)
```

Figure 7.a is a corresponding picture of two "sample" people with different attributes.

	woodyard	(A)	robertsman
	edward		nicolas
	845680539		627259003
	male		male
(B)	aug 30 1941		mar 15 1932
(C)	1		4
(D)	single		divorced
(E)			feb 23 1972
(F)	true		false

Figure 7.a Two sample people

A record defining "person" can now be formulated as:

```

type alfa = packed array[1..10] of char;
status = (married,widowed,divorced,single);
date = record mo :(jan,feb,mar,apr,may,jun,
                  july,aug,sept,oct,nov,dec);
           day : 1..31;
           year : integer
         end;
person = record
           name : record first,last: alfa
           end;
           ss : integer;
           sex : (male,female);
           birth : date;
           depdts : integer;
           case ms : status of
             married,widowed : (mdate: date);
             divorced : (ddate: date;
                           firstd: Boolean);
             single : (indepdt : Boolean)
           end; {person}

```

Warnings:

1. All field names must be distinct--even if they occur in different variants.
2. If the field list for a label L is empty, the form is:
L : ()
3. A field list can have only one variant part and it must succeed the fixed part(s). (However, a variant part may itself contain variants. Hence, it is possible to have nested variants.)

Referencing a record component is essentially a simple linear reconstruction of the outline. As example, assume a variable p of type person and "create" the first of the model people.

```
p.name.last := 'woodyard
p.name.first := 'edward
p.ss := 845680539;
p.sex := male;
p.birth.mo := aug;
p.birth.day := 30;
p.birth.year := 1941;
p.depdt := 1;
p.ms := single;
p.indepdt := true
```

A. The with statement

The above notation can be a bit tedious, and the user may wish to abbreviate it using the with statement. The with clause effectively opens the scope containing the field identifiers of the specified record variable, so that the field identifiers may occur as variable identifiers. (Thereby providing an opportunity for the compiler to optimize the qualified statement.) The general form is:

```
with <record variable> {, <record variable>} do <statement>
```

Within the component statement of the with statement one denotes a field of a record variable by designating only its field identifier (without preceding it with the notation of the entire record variable).

The with statement below is equivalent to the preceding series of assignments:

```
with p.name,birth do
begin last := 'woodyard ';
  first := 'edward ';
  ss := 845680539;
  sex := male;
  mo := aug;
  day := 30;
  year := 1941;
  depdt := 1;
  ms := single;
  indepdt := true
end {with}
```

Likewise,

```
var currdate : date;
...
with currdate do
  if mo=dec then
    begin mo := jan; year := year+1
    end
  else mo := succ(mo)
```

is equivalent to

```
var currdate : date;
...
if currdate.mo=dec then
  begin currdate.mo := jan;
    currdate.year := currdate.year+1
  end
else currdate.mo := succ(currdate.mo)
```

And the following accomplishes the vaccine update exampled earlier:

```
with vaccine[child3] do
  begin mo := apr; day := 23; year := 1973
  end
```

No assignments may be made by the qualified statement to any elements of the record variable list. That is, given:

with r do S

r must not contain any variables subject to change by S; for example:

```
with a[i] do
  begin ...
    i := i+1
  end
```

is not allowed.

The form:

with r1, r2, ..., rn do S

is equivalent to

```
with r1 do
  with r2 do
  ....
  with rn do S
```

Whereas:

```
var a : array[2..8] of integer;
  a : 2..8;
```

is NOT allowed, for the definition of a is ambiguous.

```
var a : integer;
  b : record a: real; b: Boolean
    end;
```

IS allowed, for the notation for the integer a is easily distinguishable from the real "b.a". Likewise, the record variable b is distinguishable from the Boolean "b.b". Furthermore, within the qualified statement S of

```
with b do S
```

both "b" and "b.b" reference the Boolean "b.b".

8
THE SEI TYPES

A set type defines the set of values that is the powerset of its base type, i.e. the set of all subsets of values of the base type, including the empty set. The base type must be a scalar or subrange type.

```
type <identifier> = set of <base type>;
```

The base type of a set must be a scalar type; however, implementations of Pascal may define limits for the size of sets, which can be quite small (e.g. the number bits in a word).

Sets are built up from their elements by set constructors (denoted by <set> in the syntax). They consist of the enumeration of the set elements, i.e. of expressions of the base type, which are separated by commas and enclosed by set brackets [and]. Accordingly, [] denotes the empty set.

```
<set> ::= [ <element list> ]
<element list> ::= <element> {, <element>} | <empty>
<element> ::= <expression> | <expression> .. <expression>
```

The form m..n denotes the set of all elements i of the base type such that $m \leq i \leq n$. If $m > n$, [m..n] denotes the empty set.

Examples of set constructors:

```
[13]
[i+j,i-j]
['A'..'Z','0'..'9']
```

The following operators are applicable on all objects with set structure:

```
+ union
* intersection
- set difference (e.g. A-B denotes the set of all elements of A that are not also elements of B.)
```

Relational operators applicable to set operands are:

```
= <> test on (in)equality
<= >= test on set inclusion
in set membership. The first operand is a scalar type,
the second is of its associated set type; the result
is true when the first is an element of the second,
otherwise false.
```

examples of declarations	-and-	assignments
<u>type</u> primary = (red,yellow,blue); color = <u>set of</u> primary;		hue1 := [red]; hue2 := []; hue2 := hue2 + [succ(red)]
<u>var</u> hue1,hue2 : color;		
<u>var</u> ch: char;		chset1 := ['d','a','g'];
chset1,chset2: <u>set of</u> 'a'..'z';		chset2 := ['a'..'z']-[ch]
<u>var</u> opcode : <u>set of</u> 0..7;		add := [2,3] <= opcode
add : Boolean;		

Set operations are relatively fast and can be used to eliminate more complicated tests. A simpler test for:

```

if (ch='a')or(ch='b')or(ch='c')or(ch='d')or(ch='z') then s
is:
if ch in ['a'..'d','z'] then s

{ program 8.1
example of set operations }

program setup(output)

type days = (m,t,w,th,fr,sa,su);
    week = set of days;
var wk,work,free : week;
    d : days;

procedure check(s : week); {procedures introduced in chapter 11}
    var d : days;
begin write(' ');
for d := m to su do
    if d in s then write('x') else write('o');
writeln
end; {check}

begin work := []; free := [];
wk := [m..su];
d := sa; free := [d] + free +[su];
check(free);
work := wk - free; check(work);
if free <= wk then write(' o');
if wk >= work then write(' k');
if not(work >= free) then write(' jack');
if [sa] <= work then write(' forget it');
writeln
end.
```

```

oooooxx
xxxxoo
ok jack

```

On program development

Programming--in the sense of designing and formulating algorithms--is in general a complicated process requiring the mastery of numerous details and specific techniques. Only in exceptional cases will there be a single good solution. Usually, so many solutions exist that the choice of an optimal program requires a thorough analysis not only of the available algorithms and computers but also of the way in which the program will most frequently be used.

Consequently, the construction of an algorithm should consist of a sequence of deliberations, investigations, and design decisions. In the early stages, attention is best concentrated on the global problems, and the first draft of a solution may pay little attention to details. As the design process progresses, the problem can be split into subproblems, and gradually more consideration given to the details of problem specification and to the characteristics of the available tools. The terms steplike refinement [2] and structured programming [4] are associated with this approach.

The remainder of this chapter illustrates the development of an algorithm by rewording (to be consistent with Pascal notation) an example C.A.R. Hoare presents in Structured Programming [4, "Notes on Data Structuring"].

The assignment is to generate the prime numbers falling in the range $2..n$, where $n \geq 2$. After a comparison of the various algorithms, that of Eratosthenes' sieve is chosen because of its simplicity (no multiplications or divisions).

The first formulation is verbal.

1. Put all the numbers between 2 and n into the "sieve".
2. Select and remove the smallest number remaining in the sieve.
3. Include this number in the "primes".
4. Step through the sieve, removing all multiples of this number.
5. If the sieve is not empty, repeat steps 2--5.

Although initialization of variables is the first step in the execution of a program, it is often the last in the development process. Full comprehension of the algorithm is a prerequisite for making the proper initializations; updating of these initializations with each program modification is necessary to keep the program running. (Unfortunately, updating is not always sufficient!)

Hoare chooses a set type with elements $2..n$ to represent both the sieve and the primes. The following is a slight variation of the program sketch he presents.

```

const n = 10000;
var sieve,primes : set of 2..n;
  next,j : integer;
begin {initialize}
  sieve := [2..n]; primes := []; next := 2;
  repeat {find next prime}
    while not(next in sieve) do next := succ(next);
    primes := primes + [next];
    j := next;
    while j<=n do {eliminate}
      begin sieve := sieve - [j]; j := j + next
      end
    until sieve=[]
end.

```

As an exercise Hoare makes the assignment to rewrite the program, so that the sets only represent the odd numbers. The following is one proposal. Note the close correlation with the first solution.

```

const n = 5000; {n' = n div 2}
var sieve,primes : set of 2..n;
  next,j,c : integer;
begin {initialize}
  sieve := [2..n]; primes := []; next := 2;
  repeat {find next prime}
    while not(next in sieve) do next := succ(next);
    primes := primes + [next];
    c := 2*next - 1; {c = new prime}
    j := next;
    while j<=n do {eliminate}
      begin sieve := sieve - [j]; j := j+c
      end
    until sieve=[]
end.

```

It is desirable that all basic set operations are relatively fast. Many implementations restrict the maximum size of sets according to their "wordlength", so that each element of the base set is represented by one bit (0 meaning absence, 1 meaning presence). Most implementations would therefore not accept a set with 10,000 elements. These considerations lead to an adjustment in the data representation, as shown in program 8.2.

A large set can be represented as an array of smaller sets such that each "fits" into one word (implementation dependent). The following program uses the second sketch as an abstract model of the algorithm. The sieve and the primes are redefined as arrays of sets; next is defined as a record. The output is left undeveloped.

```

{ program 8.2
  generate the primes between 3..10000 using a
  sieve containing odd integers in this range.}

program primes(output);

const wdlength = 59; {implementation dependent}
  maxbit = 58;
  w = 84; {w = n div wdlength div 2}
var sieve,primes : array[0..w] of set of 0..maxbit;
  next : record word,bit :integer
    end;
  j,k,t,c : integer;  empty : boolean;
begin {initialize}
  for t := 0 to w do
    begin sieve[t] := [0..maxbit]; primes[t] := [] end;
  sieve[0] := sieve[0] - [0]; next.word := 0;
  next.bit := 1; empty := false;

  with next do
  repeat { find next prime }
    while not(bit in sieve[word]) do bit := succ(bit);
    primes[word] := primes[word] + [bit];
    c := 2*bit + 1;
    j := bit; k := word;
    while k<=w do {eliminate}
      begin sieve[k] := sieve[k] - [j];
        k := k + word*2; j := j + c;
        while j>maxbit do
          begin k := k+1; j := j - wdlength
          end
      end;
    if sieve[word]=[] then
      begin empty := true; bit := 0
      end;
    while empty and (word<w) do
      begin word := word+1; empty := sieve[word]=[]
      end
  until empty; {ends with}

end.

```

FILE TYPES

In many ways the simplest structuring method is the sequence. In the data processing profession the generally accepted term to describe a sequence is a sequential file. Pascal uses simply the word file to specify a structure consisting of a sequence of components--all of which are of the same type.

A natural ordering of the components is defined through the sequence, and at any instance only one component is directly accessible. The other components are accessible by progressing sequentially through the file. The number of components, called the length of the file, is not fixed by the file type definition. This is a characteristic which clearly distinguishes the file from the array. A file with no components is said to be empty.

```
type <identifier> = file of <type>;
```

The declaration of every file variable *f* automatically introduces a buffer variable, denoted by *f*↑, of the component type. It can be considered as a window through which one can either inspect (read) existing components or append (write) new components, and which is automatically moved by certain file operators.

The sequential processing and the existence of a buffer variable suggest that files may be associated with secondary storage and peripherals. Exactly how the components are allocated is implementation dependent, but we assume that only some of the components are present in primary store at any one time, and only the component indicated by *f*↑ is directly accessible.

When the window *f*↑ is moved beyond the end of a file *f*, the standard Boolean function *eof(f)* returns the value true, otherwise false. The basic file-handling operators are:

reset(f) resets the file window to the beginning for the purpose of reading, i.e. assigns to *f*↑ the value of the first element of *f*. *eof(f)* becomes false if *f* is not empty; otherwise, *f*↑ is not defined, and *eof(f)* remains true.

rewrite(f) precedes the rewriting of the file *f*. The current value of *f* is replaced with the empty file. *eof(f)* becomes true, and a new file may be written.

get(f) advances the file window to the next component; i.e. assigns the value of this component to the buffer variable *f*↑. If no next component exists, then *eof(f)* becomes true, and the resulting value of *f*↑ is not defined. The effect of *get(f)* is

defined only if `eof(f)` is false prior to its execution.

`put(f)` appends the value of the buffer variable `f↑` to the file `f`. The effect is defined only if prior to execution the predicate `eof(f)` is true. `eof(f)` remains true, and `f↑` becomes undefined.

examples of declarations -and- statements with files

<code>var data : file of integer;</code>	<code>a := sqr(data↑);</code>
<code> a : integer;</code>	<code>get(data)</code>
<code>var club : file of person;</code>	<code>club↑ := p;</code>
<code> p : person;</code>	<code>put(club)</code>

Program parts:

1. Read a file of real numbers and compute their sum `S`.

```
{ program part
  compute sum }

S := 0; reset(f);
while not eof(f) do
  begin S := S + f↑; get(f)
  end
```

2. The following program fragment operates on two files of ordered sequences of integers
`f1,f2, ... ,fm` and `g1,g2, ... ,gn`

such that $f(i+1) \geq f_i$ and $g(i+1) \geq g_i$, for all i,j and merges them into one ordered file `h` such that
 $h(k+1) \geq h(k)$ for $k = 1,2, \dots, (m+n-1)$.

It uses the following variables:
`endfg : Boolean;`
`f,g,h : file of integer`

```

{ program part
  merge f and g into h }

begin reset(f); reset(g); rewrite(h);
  endfg := eof(f) or eof(g);
  while not endfg do
    begin if f↑ < g↑ then
      begin h↑ := f↑; get(f);
        endfg := eof(f)
      end else
        begin h↑ := g↑; get(g);
          endfg := eof(g)
        end;
      put(h)
    end;
  while not eof(g) do
    begin h↑ := g↑; put(h);
      get(g)
    end;
  while not eof(f) do
    begin h↑ := f↑; put(h);
      get(f)
    end
  end
end

```

Files may be local to a program (or local to a procedure) or they may already exist outside the program. The latter are called external files. External files are passed as parameters in the program heading (see chapter 13) into the program.

A. Textfiles

Files whose components are characters are called textfiles. Accordingly, the standard type text is defined as follows:

```
type text = file of char;
```

Texts are usually subdivided into lines. A straight-forward method of indicating the separation of two consecutive lines is by using control characters. For instance, in the ASCII character set the two characters cr (carriage return) and lf (line feed) are used to mark the end of a line. However, many computer installations use a character set devoid of such control characters; this implies that other methods for indicating the end of a line must be employed.

We may consider the type text as being defined over the base type char (containing printable characters only) extended by a (hypothetical) line separator character. This control character cannot be assigned to variables of type char, but can be both

recognized and generated by the following special textfile operators:

```
writeln(x) terminate the current line of the textfile x
readln(x) skip to the beginning of the next line of the
           textfile x ( $x^\dagger$  becomes the first character of the
           next line)
eoln(x)   a Boolean function indicating whether the end of
           the current line in the textfile x has been
           reached. (If true,  $x^\dagger$  corresponds to the position
           of a line separator, but  $x^\dagger$  is a blank.)
```

If f is a textfile and ch a character variable, the following abbreviated notation may be used in place of the general file operators.

abbreviated form	expanded form
<hr/>	
write(f,ch)	$f^\dagger := ch; put(f)$
read(f,ch)	$ch := f^\dagger; get(f)$

The following program schemata use the above conventions to demonstrate some typical operations performed on textfiles.

1. Writing a text y. Assume that P(c) computes a (next) character and assigns it to parameter c. If the current line is to be terminated, a Boolean variable p is set to true; and if the text is to be terminated, q is set to true.

```
rewrite(y);
repeat
  repeat P(c); write(y;c)
  until p;
  writeln(y)
until q
```

2. Reading a text x. Assume that Q(c) denotes the processing of a (next) character c. R denotes an action to be executed upon encountering the end of a line.

```
reset(x);
while not eof(x) do
begin
  while not eoln(x) do
    begin read(x;c); Q(c)
    end;
  R; readln(x)
end
```

3. Copying a text *x* to a text *y*, while preserving the line structure of *x*.

```

reset(x); rewrite(y);
while not eof(x) do
begin {copy a line}
  while not eoln(x) do
    begin read(x,c); write(y,c)
    end;
  readln(x); writeln(y)
end

```

B. The standard files "input" and "output"

The textfiles "input" and "output" usually represent the standard I/O media of a computer installation (such as the card reader and the line printer). Hence, they are the principal communication line between the computer and its human user.

Because these two files are used very frequently, they are considered as "default values" in textfile operations when the textfile *f* is not explicitly indicated. That is

is equivalent to

write(ch)	write(output,ch)
read(ch)	read(input,ch)
writeln	writeln(output)
readln	readln(input)
eof	eof(input)
eoln	eoln(input)

Note: The standard functions reset (rewrite) must not be applied to the file input (output).

Accordingly, for the case where *x* is "input" and *y* is "output", the first two of the program schemata can be expressed as follows: (assume var ch: char)

Writing a text on file "output";

```

repeat
  repeat P(ch); write(ch)
  until p;
  writeln
until q

```

Reading a text from file "input":

```
while not eof do
  begin {process a line}
    while not eoln do
      begin read(ch); Q(ch)
      end;
    R; readln
  end
```

Further extensions of the procedures write and read (for the convenient handling of legible input and output data) are described in chapter 12.

The next two examples of programs show the use of the textfiles input and output. (Consider what changes would be necessary if only get and put, not read and write, are to be used.)

```
{ program 9.1 -- frequency count of letters in input file }

program fcount(input,output);

var ch: char;
  count: array['a'..'z'] of integer;
  letter: set of 'a'..'z';
begin letter := ['a'..'z'];
  for ch := 'a' to 'z' do count[ch] := 0;
  while not eof do
    begin
      while not eoln do
        begin read(ch); write(ch);
          if ch in letter then count[ch] := count[ch]+1
        end;
        writeln; readln
    end
  end.
```

In some installations when a textfile is sent to a printer, the first character of each line is used as a printer control character; i.e. this first character is not printed, but instead interpreted as controlling the paper feed mechanism of the printer. The following conventions are in wide use:

blank	:	feed one line space before printing
'0'	:	feed double space before printing
'1'	:	skip to top of next page before printing
'+'	:	no line feed (overprint)

The following program inserts a blank at the beginning of each line, resulting in normal single space printing.

```
{ program 9.2 -- insert leading blank }

program insert(input,output);

var ch: char;
begin
  while not eof do
    begin write('.');
      while not eoln do
        begin read(ch); write(ch)
        end;
      writeln; readln
    end
  end.
```

If read and write are used without indication of a file parameter, the default convention specifies that the files input and output are assumed; in which case, they must be mentioned in the parameter list of the program heading.

10
POINTER TYPES

A static variable (statically allocated) is one that is declared in a program and subsequently denoted by its identifier. It is called static, for it exists (i.e. memory is allocated for it) during the entire execution of the block to which it is local. A variable may, on the other hand, be generated dynamically (without any correlation to the static structure of the program) by the procedure new. Such a variable is consequently called a dynamic variable.

Dynamic variables do not occur in an explicit variable declaration and cannot be referenced directly by identifiers. Instead, generation of a dynamic variable introduces a pointer value (which is nothing other than the storage address of the newly allocated variable). Hence, a pointer type P consists of an unbounded set of values pointing to elements of a given type T. P is then said to be bound to T. The value nil is always an element of P and points to no element at all.

```
type <identifier> = ↑ <type identifier>;
```

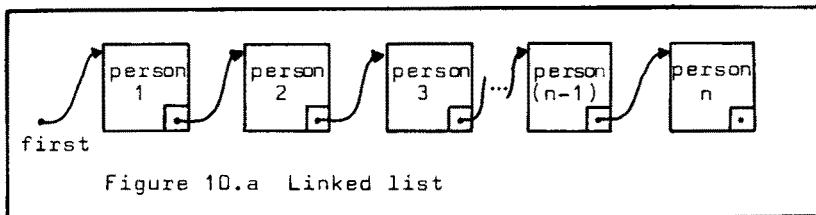
If p is a pointer variable bound to a type T, then p is a reference to a variable of type T, and p↑ denotes that variable.

Pointers are a simple tool for the construction of complicated and flexible data structures. If the type T is a record structure that contains one or more fields of type ↑T, then structures equivalent to arbitrary finite graphs may be built, where the T's represent the nodes, and the pointers are the edges.

As an example, consider the construction of a "data bank"" for a given group of people. Assume the persons are represented by records as defined in chapter 7. One may then form a chain or linked list of such records by adding a field of a pointer type as shown below.

```
type link = ↑person;
...
person = record
  ...
  next : link;
  ...
end;
```

A linked list of n persons can be represented as in figure 10.a.



A variable of type link, called "first" points to the first element of the list. The link of the last person is nil.

If we assume that the file "input" contains n social security numbers, then the following code could have been used to construct the above chain.

```
var first, p: link; i: integer;
    ...
first := nil;
for i := 1 to n do
begin read(s); new(p);
    p^.next := first;
    p^.ss := s;
    first := p
end
```

For purposes of access, one introduces another variable, say pt, of type link and allows it to move freely through the list. To demonstrate selection, assume there is a person with social security number equal to n and access this person. The strategy is to advance pt via link until the desired member is located:

```
pt := first;
while pt^.ss <> n do pt := pt^.next
```

In words this says, "Let pt point to the first element. While the social security number of the member pointed to (referenced) by pt does not equal n , advance pt to the variable indicated by the link (also a pointer variable) of the record which pt currently references." Note in passing that

first¹.next¹.next
accesses the third person.

Note that this simple search statement works only, if one is sure that there is at least one person with security number n on the list. But is this realistic? A check against failing to recognize the end of the list is therefore mandatory. One might first try the following solution:

```
pt := first;
while (pt <> nil) and (pt^.ss <> n) do pt := pt^.next
```

But recall section 4.A. If pt = nil, the variable pt¹, referenced in the second factor of the termination condition,

does not exist at all. The following are two possible solutions which treat this situation correctly:

- (1)

```
pt := first; b := true;
      while (pt <> nil) and b do
          if pt↑.ss = n then b := false else pt := pt↑.next
```
- (2)

```
pt := first;
      while pt <> nil do
          begin if pt↑.ss = n then goto 13;
          pt := pt↑.next
      end
```

To pose another problem, say one wishes to add the sample person to the bank. First a space in memory must be allocated, and a reference created by means of the standard procedure new.

<code>new(p)</code>	allocates a new variable <i>v</i> and assigns the pointer reference of <i>v</i> to the pointer variable <i>p</i> . If the type of <i>v</i> is a record type with variants, then <code>new(p)</code> allocates enough storage to accommodate all variants. The form
<code>new(p.t1, ... ,tn)</code>	can be used to allocate a variable of the appropriate size for the variant with tag field values equal to the constants <i>t1...tn</i> . The tag field values must be listed contiguously and in the order of their declaration. Any trailing tag fields may be omitted. This <u>does not</u> imply assignment to the tag fields.

Warning: if a record variable *p↑* is created by the second form of `new`, then this variable must not change its variant during program execution. Assignment to the entire variable is not allowed; however one can assign to the components of *p↑*.

If *newp* is a variable of type *link* (as defined above), `new(newp)` creates a new variable of type *person* and assigns the reference to *newp*. The value of the new variable is undefined upon allocation. Access is via the pointer.

examples:

```
newp↑.ss := 845680539    assignes a social security number
newp↑ := paul            assigns the record paul to newp↑
```

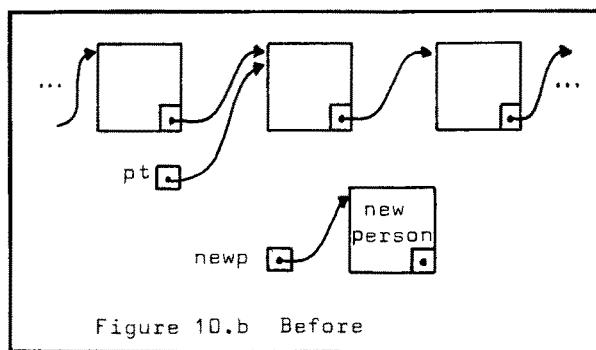
The procedure dispose is the "inverse" of `new` and may have either the form

```
dispose(p)
or
```

```
dispose(p,t1,...tn)
```

relative to which form of new was used to create the variable pointed to by p. Dispose then "erases" the variable referenced by p.

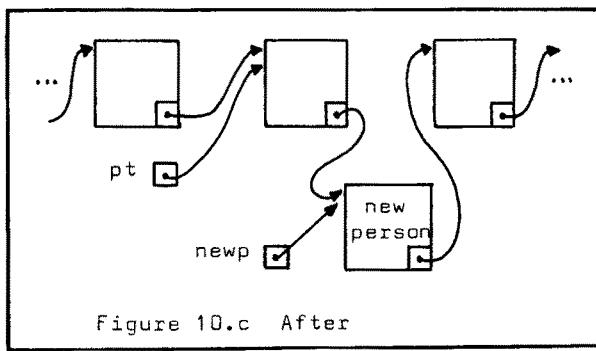
In the next step the new member, referenced by the pointer newp, must be inserted after the member referenced by pt. See figure 10.b.



Insertion is a simple matter of changing the pointers:

```
newp↑ .next := pt↑ .next;
pt↑ .next := newp
```

Figure 10.c illustrates the result.



Deletion of the member following the auxiliary pointer pt is accomplished in the single instruction:

```
pt↑ .next := pt↑ .next↑ .next
```

It is often practical to process a list using 2 pointers--one following the other. In the case of deletion, it is then likely that one pointer--say p1--precedes the member to be deleted, and p2 points to that member. Deletion can then be expressed in the single instruction:

```
p1↑ .next := p2↑ .next
```

One is, however, warned that deletions in this manner will, in most installations, result in the loss of usable (free) store. A possible remedy is the following:

```
p1↑ .next := p2↑ .next;  
dispose(p2)
```

This provides the implementor with the opportunity to mark the store defining the variable referenced by p2 as free. What actually is done may greatly vary among installations; elaborate "garbage collections" may be implemented, or the dispose instruction may simply be ignored.

Linked allocation is the most efficient representation for inserting and deleting elements. Arrays require shifting down (up) of every element below the index in the case of insertion (deletion), and files require complete rewriting.

For an example involving a tree structure instead of a linear list, refer to chapter 11 (program 11.5).

A word to the wise

Pascal provides a wide variety of data structures. It is left to the programmer to evaluate his problem in detail sufficient to determine the structure best suited to express the situation and to evaluate the algorithm. As indicated by the "data bank" example, linked allocation is especially nice for insertion and deletion. If, however, these operations happen infrequently, but instead efficient access is mandatory, then the representation of the data as an array of records is usually more appropriate.

PROCEDURUS AND FUNCTIONS

As one grows in the art of computer programming, one constructs programs in a sequence of refinement steps. At each step the programmer breaks his task into a number of subtasks, thereby defining a number of partial programs. Although it is possible to camouflage this structure, this is undesirable. The concept of the procedure (or subroutine) allows the display of the subtasks as explicit subprograms.

A. Procedures

The procedure declaration serves to define a program part and to associate it with an identifier, so that it can be activated by a procedure statement. The declaration has the same form as a program, except it is introduced by a procedure heading instead of a program heading.

Recall the program part that found the minimum and maximum values in a list of integers. As an extension, say that increments of $j_1..j_n$ are added to $a[1]...a[n]$, then min and max are again computed. The resulting program, which employs a procedure to determine min and max, follows.

```

{ program 11.1
  extend program 6.1 }

program minmax2(input,output);

const n = 20;
var a : array[1..n] of integer;
    i,j : integer;
procedure minmax;
  var i :1..n; u,v,min,max :integer;
begin min := a[1]; max := min; i := 2;
  while i<n do
    begin u := a[i]; v := a[i+1];
      if u>v then
        begin if u>max then max := u;
              if v<min then min := v
            end else
              begin if v>max then max := v;
                    if u<min then min := u
                  end;
      i := i+2
    end;
  if i=n then
    begin if a[n]>max then max := a[n]
          else if a[n]<min then min := a[n];
    writeln(min,max); writeln
  end; {minmax}

begin {read array}
  for i := 1 to n do
    begin read(a[i]); write(a[i]:3)
    end;
  writeln;
  minmax;
  for i := 1 to n do
    begin read(j); a[i] := a[i]+j; write(a[i]:3)
    end;
  writeln;
  minmax
end.

-1 -3  4   7   8 54 23 -5   3   9   9   9 -6 45 79 79   3   1   1   5
      -6           79

44 40  7 15   9 88 15 -4   7 43 12 17 -7 48 59 39   9   7   7 12
      -7           88

```

Although simple, this program illustrates many points:

1. The simplest form of the PROCEDURE HEADING, namely:

```
procedure <identifier>;
```

2. LOCAL VARIABLES. Local to procedure minmax are the variables i, u, v, min, and max. These may be referenced only within the scope of minmax; assignments to these variables have no effect on the program outside the scope of minmax.
3. GLOBAL VARIABLES. Global variables are a, i, and j; They may be referenced throughout the program. (e.g. The first assignment in minmax is min := a[i].)
4. NAME PRECEDENCE. Note that i is the name for both a global and a local variable. These are not the same variable! A procedure may reference any variable global to it, or it may choose to redefine the name. If a variable name is redefined, the new name/type association is then valid for the scope of the defining procedure, and the global variable of that name (unless passed as a parameter) is no longer available within the procedure scope. Assignment to the local i (e.g. i := i+2) has no effect upon the global i; and since i denotes the local variable, the global variable i is effectively inaccessible.

It is a good programming practice to declare every identifier which is not referenced outside the procedure, as strictly local to that procedure. Not only is this good documentation, but it also provides added security. For example, i could have been left as a global variable; but then a later extension to the program which called procedure minmax within a loop controlled by i would cause incorrect computation.

5. The PROCEDURE STATEMENT. In this example the statement, "minmax" in the main program activates the procedure.

Examining the last example in more detail, one notes that minmax is called twice. By formulating the program part as a procedure--i.e. by not explicitly writing this program part twice--the programmer conserves not only his typing time, but also space in memory. The static code is stored only once, and space defining local variables is activated only during the execution of the procedure.

One should not hesitate, however, from formulating an action as a procedure--even when called only once--if doing so enhances the readability. Defining development steps as procedures makes a more communicable and verifiable program.

Often necessary with the decomposition of a problem into subroutines is the introduction of new variables to represent the arguments and the results of the subroutines. The purpose of such variables should be clear from the program text.

The following program extends the above example to compute the minimum and maximum value of an array in a more general sense.

```

{ program 11.2
  extend program 11.1 }

program minmax3(input,output);

const n = 20;
type list = array[1..n] of integer;
var a,b : list;
    i,j,min1,max1,max2 : integer;

procedure minmax(var g:list; var j,k:integer);
  var i :1..n; u,v :integer;
begin j := g[1]; k := j; i := 2;
  while i<n do
    begin u := g[i]; v := g[i+1];
      if u>v then
        begin if u>k then k := u;
          if v<j then j := v
        end else
          begin if v>k then k := v;
            if u<j then j := u
          end;
      i := i+2
    end;
    if i=n then
      if g[n]>k then k := g[n]
      else if g[n]<j then j := g[n];
  end; {minmax}

begin {read array}
  for i := 1 to n do
    begin read(a[i]); write(a[i]:3) end;
  writeln;
  minmax(a,min1,max1);
  writeln(min1,max1,max1-min1); writeln;
  for i := 1 to n do
    begin read(b[i]); write(b[i]:3) end;
  writeln;
  minmax(b,min2,max2);
  writeln(min2,max2,max2-min2);
  writeln(abs(min1-min2),abs(max1-max2)); writeln;
  for i := 1 to n do
    begin a[i] := a[i] + b[i]; write(a[i]:3) end;
  writeln;
  minmax(a,min1,max1);
  writeln(min1,max1,max1-min1)
end.

```

-1	-3	4	7	8	54	23	-5	3	9	9	9	-6	45	79	79	3	1	1	5
							-6		79				85						
45	43	3	8	1	34	-8	1	4	34	3	8	-1	3	-2	-4	6	6	6	7
							-8		45				53						
									2				34						
44	40	7	15	9	58	15	-4	7	43	12	17	-7	48	77	75	9	7	7	12
							-7		88				95						

In program 11.2, one encounters the second form of the procedure heading:

```
procedure <identifier> ( <formal parameter section>
                           {; <formal parameter section>} );
```

The formal parameter section lists the name of each formal parameter followed by its type. It is followed by the declaration part, which introduces the objects local to the procedure.

The labels in the label definition part and all identifiers introduced in the formal parameter part, the constant definition part, the type definition part, the variable, procedure, or function declaration parts are local to the procedure declaration which is called the scope of these objects. They are not known outside their scope. In the case of local variables, their values are undefined at the beginning of the statement part.

Parameters provide a substitution mechanism that allows a process to be repeated with a variation of its arguments. (e.g. minmax is called twice to scan array a and once to scan array b.)

One notes a correspondence between the procedure heading and the procedure statement. The latter contains a list of actual parameters, which are substituted for the corresponding formal parameters that are defined in the procedure declaration. The correspondence is established by the positioning of the parameters in the lists of actual and formal parameters. There exist four kinds of parameters: so-called value parameters, variable parameters, procedure parameters (the actual parameter is a procedure identifier), and function parameters (the actual parameter is a function identifier).

Program 11.2 shows the case of the variable parameter. The actual parameter must be a variable; the corresponding formal parameter must be preceded by the symbol var and represents this actual variable during the entire execution of the procedure. Furthermore, if $x_1..x_n$ are the actual variables that correspond to the formal variable parameters $v_1..v_n$, then $x_1..x_n$ should be distinct variables.

All address calculations are done at the time of the procedure call. Hence, if a variable is a component of an array, its index expression is evaluated when the procedure is called.

To describe the memory allocation pictorially, one could draw an arrow for each variable parameter from the name of the formal parameter to the memory location of the corresponding actual parameter. Any operation involving the formal parameter is then performed directly upon the actual parameter. Whenever the parameter represents a result of the procedure--as is the case with j and k above--it must be defined as a variable parameter.

When no symbol heads the parameter section, the parameter(s) of

this section are said to be value parameter(s). In this case the actual parameter must be an expression (of which a variable is a simple case). The corresponding formal parameter represents a local variable in the called procedure. As its initial value, this variable receives the current value of the corresponding actual parameter (i.e. the value of the expression at the time of the procedure call). The procedure may then change the value of this variable by assigning to it; this cannot, however, affect the value of the actual parameter. Hence, a value parameter can never represent a result of a computation.

The difference in the effects of value and variable parameters is shown in program 11.3.

```
{ program 11.3
procedure parameters }

program parameters(output);
begin
var a,b: integer;
procedure h(x: integer; var y: integer);
begin x := x+1; y := y+1;
writeln(x,y)
end;
begin a := 0; b := 0;
h(a,b);
writeln(a,b)
end.
```

1	1
0	1

In program 11.2 none of the values in array g are altered; i.e. g is not a result. Consequently g could have been defined as a value parameter without affecting the end result. To understand why this was not done, it is helpful to look at the implementation.

A procedure call allocates a new area for each value parameter: this represents the local variable. The current value of the actual parameter is "copied" into this location; exit from the procedure simply releases this storage.

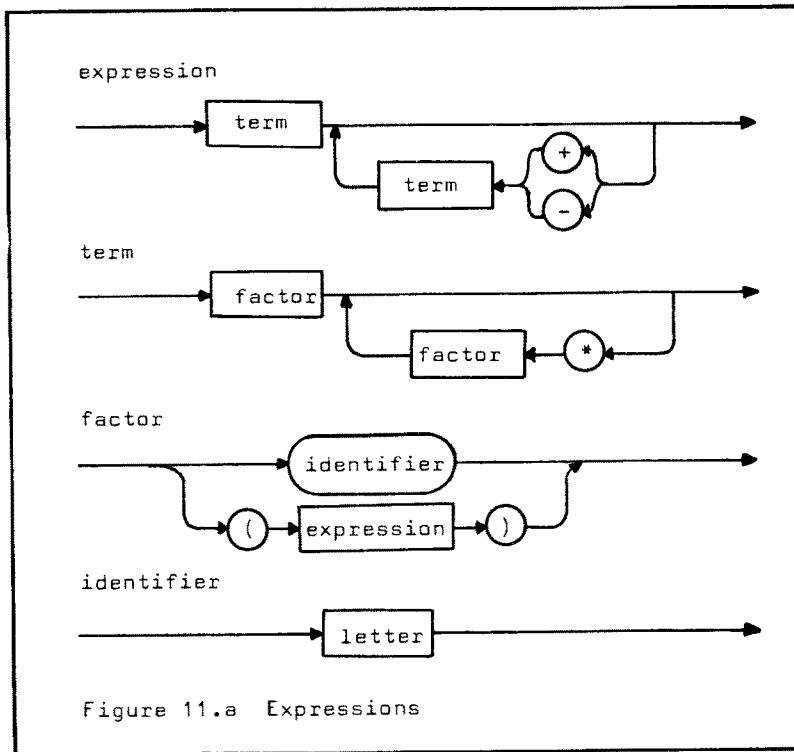
If a parameter is not used to transfer a result of the procedure, a value parameter is generally preferred. The referencing is then quicker, and one is protected against mistakenly altering the data. However in the case where a parameter is of a structured type (e.g. an array), one should be cautious, for the copying operation is relatively expensive, and the amount of storage needed to allocate the copy may be large. Because referencing of each element in the array occurs only once, it is desirable to define the parameter as a variable parameter.

One may change the dimension of the array simply by redefining n. To make the program applicable for an array of reals, one needs only to change the type and variable definitions; the statements are not dependent upon integer data.

The use of the procedure identifier within the text of the procedure itself implies recursive execution of the procedure. Problems whose definition is naturally recursive, often lend themselves to recursive solutions. An example is the following program. Given as data are the symbolic expressions:

```
(a+b)*(c-d)
a+b*c-d
( a + b)* c-d
a+b*(c-d)
a*a*a*a
b+c*(d+c*a*a)*b+a .
```

which are formed according to the syntax of figure 11.a. A period terminates the input.



The task is to construct a program to convert the expressions into postfix form (Polish notation). This is done by constructing an individual conversion procedure for each syntactic construct (expression, term, factor). As these syntactic constructs are defined recursively, their corresponding procedures may activate themselves recursively.

```

{ program 11.4
  conversion to postfix form }

program postfix(input,output);

var ch : char;

procedure find;
begin repeat read(ch)
      until (ch<>' ') and not eoln(input)
end;

procedure expression;
  var op : char;

  procedure term;

    procedure factor;
    begin if ch='(' then
        begin find; expression; {ch = } }
        end else write(ch);
        find
    end; {factor}

    begin factor;
      while ch='*' do
        begin find; factor; write('*')
        end
    end; {term}

    begin term;
      while (ch='+')or(ch='-') do
        begin op := ch; find; term; write(op)
        end
    end; {expression}

  begin find;
    repeat write(' ');
    expression;
    writeln
    until ch='.'
  end.

ab+cd-*  

abc**d-  

ab+c*d-  

abcd-*+  

aa*a*a*  

bcdca*a**+*b**+a+

```

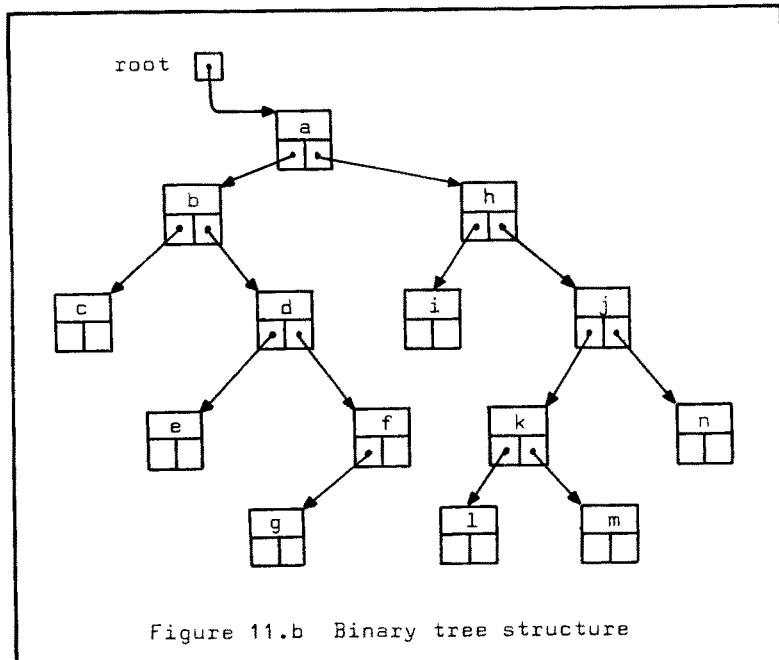
The **binary tree** is a data structure that is naturally defined in recursive terms and processed by recursive algorithms. It consists of a finite set of nodes that is either empty or consists of a node (the root) with two disjoint binary trees.

called the left and right subtrees (6). Recursive procedures for generating and traversing binary trees naturally reflect this mode of definition.

Program 11.5 builds a binary tree and traverses it in pre-, post-, and endorder. The tree is specified in preorder, i.e. by listing the nodes (single letters in this case) starting at the root and following first the left and then the right subtrees so that the input corresponding to figure 11.b is:

```
abc..de..fg...hi..jkl..m..n..
```

where a point signifies an empty subtree.



```

{ program 11.5
  binary tree traversal }

program traversal(input,output);

type ptr = ^node;
      node = record info : char;
                  llink,rlink : ptr
              end;
var root : ptr; ch : char;

procedure preorder(p : ptr);
begin if p<>nil then
    begin write(p^.info);
        preorder(p^.llink);
        preorder(p^.rlink)
    end
end; {preorder}

procedure postorder(p : ptr);
begin if p<>nil then
    begin postorder(p^.llink);
        write(p^.info);
        postorder(p^.rlink)
    end
end; {postorder}

procedure endorder(p : ptr);
begin if p<>nil then
    begin endorder(p^.llink);
        endorder(p^.rlink);
        write(p^.info)
    end
end; {endorder}

procedure enter(var p:ptr);
begin read(ch); write(ch);
  if ch<>'.' then
    begin new(p);
      p^.info := ch;
      enter(p^.llink);
      enter(p^.rlink);
    end
  else p := nil
end;{enter}

begin
  write(' '); enter(root); writeln;
  write(' '); preorder(root); writeln;
  write(' '); postorder(root); writeln;
  write(' '); endorder(root); writeln
end.

```

```

abc..de..fg...hi..jkl..m..n..
abcdefghijklmn
cbedgfaihlkmjn
cegfdbilmknjha

```

The reader is cautioned against applying recursive techniques indiscriminately. Although appearing "clever", they do not always produce the most efficient solutions.

If a procedure P calls a procedure Q and Q also calls P, then either P or Q must be "pre-announced" by a forward declaration (section 11.C).

The standard procedures in Appendix A are predeclared in every implementation of Pascal. Any implementation may feature additional predeclared procedures. Since they are, as all standard objects, assumed to be declared in a scope surrounding the user program, no conflict arises from a declaration redefining the same identifier within the program. The standard procedures get, put, read, write, reset, and rewrite were introduced in chapter 9. Read and write are further discussed in chapter 12.

B. Functions

Functions are program parts (in the same sense as procedures) which compute a single scalar or pointer value for use in the evaluation of an expression. A function designator specifies the activation of a function and consists of the identifier designating the function and a list of actual parameters. The parameters are variables, expressions, procedures, or functions and are substituted for the corresponding formal parameters.

The function declaration has the same form as the program, with the exception of the function heading which has the form:

```
function <identifier> : <result type> ;
-or-
function <identifier> ( <formal parameter section>
{, <formal parameter section>} ) : <result type> ;
```

As in the case of procedures, the labels in the label definition part and all identifiers introduced in the formal parameter part, the constant definition part, the type definition part, the variable, procedure, or function declaration parts are local to the function declaration, which is called the scope of these objects. They are not known outside their scope. The values of local variables are undefined at the beginning of the statement part.

The identifier specified in the function heading names the function. The result type must be a scalar, subrange, or pointer type. Within the function declaration there must be an executed assignment (of the result type) to the function identifier. This assignment "returns" the result of the function.

The examples to date have only dealt with variable and value parameters. Also possible are procedure and function parameters. Both must be introduced by a special symbol; the symbol procedure signals a formal procedure parameter; the symbol function, a formal function parameter. The following program finds a zero of a function by bisection; the function is specified at the time of the call.

```
{ program 11.6
  find zero of a function by bisection }

program bisect(input, output);

const eps =1e-14;
var x,y :real;

function zero(function f: real; a,b: real): real;
  var x,z :real; s :boolean;
begin s := f(a)<0;
repeat x := (a+b)/2.0;
  z := f(x);
  if (z<0)=s then a := x else b := x
until abs(a-b)<eps;
zero := x
end; {zero}

begin {main}
  read(x,y); writeln(x,y,zero(sin,x,y));
  read(x,y); writeln(x,y,zero(cos,x,y))
end.

-1.000000000000e+00 1.000000000000e+00 -7.105427357601e-15
 1.000000000000e+00 2.000000000000e+00 1.570796326795e+00
```

An assignment (occurring in a function declaration) to a non-local variable or to a variable parameter is called a side effect. Such occurrences often disguise the intent of the program and greatly complicate the task of verification. (Some implementations may even attempt to forbid side effects.) Hence, the use of functions producing side effects is strongly discouraged.

As an example, consider program 11.7.

```
{ program 11.7
  test side effect }

program sideeffect(output);

var a,z: integer;
function sneaky(x: integer): integer;
begin z := z-x; {side effect on z}
  sneaky := sqr(x)
end;
begin
  z := 10; a := sneaky(z); writeln(a,z);
  z := 10; a := sneaky(10) * sneaky(z); writeln(a,z);
  z := 10; a := sneaky(z) * sneaky(10); writeln(a,z)
end.
```

```
100          0
 0          0
10000      -10
```

The next example formulates the exponentiation algorithm of program 4.8 as a function declaration.

```

{ program 11.8
  extent program 4.8 }

program expon2(output);
var pi,spi: real;
function power(x:real; y:integer): real; {y>=0}
  var z: real;
begin  z := 1;
  while y>0 do
    begin
      while not odd(y) do
        begin y := y div 2; x := sqr(x)
        end;
      y := y-1; z := x*z
    end;
    power := z
  end; {power}

begin pi := 3.14159;
  writeln(2.0,7,power(2.0,7));
  spi := power(pi,2);
  writeln(pi,2,spi);
  writeln(spi,2,power(spi,2));
  writeln(pi,4,power(pi,4))
end.

```

2.00000000000e+00	7	1.28000000000e+02
3.14159000000e+00	2	9.869587728100e+00
9.869587728100e+00	2	9.740876192266e+01
3.14159000000e+00	4	9.740876192266e+01

The appearance of the function identifier in an expression within the function itself implies recursive execution of the function.

```

{ program 11.9
  recursive formulation of gcd }

program recursivegcd(output);

var x,y,n : integer;

function gcd(m,n: integer):integer;
begin if n=0 then gcd := m
      else gcd := gcd(n,m mod n)
end; {gcd}

procedure try(a,b :integer);
begin writeln(a,b,gcd(a,b))
end;

begin try(18,27);
      try(312,2142);
      try(61,53);
      try(98,868)
end.

```

18	27	9
312	2142	6
61	53	1
98	868	14

Function calls may occur before the function definition if there is a forward reference (section 11.C).

The standard functions of Appendix A are assumed to be predeclared in every implementation of Pascal. Any implementation may feature additional predeclared functions.

C. Remarks

1. Procedure (function) calls may occur before the procedure (function) definition if there is a forward reference. The form is as follows: (Notice that the parameter list and eventual result type are written only in the forward reference.)

```
procedure Q(x: T); forward;
procedure P(y: T);
begin
  Q(a)
end;
procedure Q; {parameters are not repeated}
begin
  P(b)
end;
begin
  P(a);
  Q(b)
end.
```

2. Procedures and functions which are used as parameters to other procedures and functions must have value parameters only. (Consequently, it is not necessary to test at run time whether a parameter is called by value or by address.)
3. A component of a packed structure must not appear as an actual variable parameter. (Consequently, there is no need to pass addresses of partwords, and to test at run time for the internal representation of the actual variable.)

INPUT AND OUTPUT

The problem of communication between man and computer was already mentioned in chapter 9. Both learn to understand through what is termed pattern recognition. Unfortunately, the patterns recognized most easily by man (dominantly those of picture and sound) are very different from those acceptable to a computer (electrical impulses). In fact, the expense of physically transmitting data--implying a translation of patterns legible to man into ones legible to a computer, and vice versa--can be as costly as the processing of the transmitted information. (Consequently, much research is devoted to minimizing the cost by "automatizing" or "automating" more of the translation process.) This task of communication is called input and output handling (I/O).

The human can submit his information via input devices (e.g. key punches, card readers, paper tapes, magnetic tapes, terminals) and receive his results via output devices (e.g. line printers, card and paper tape punches, terminals, visual display units). Common to both--and defined by each individual installation--is a set of legible characters (chapter 2). It is over this character set that Pascal defines the two standard textfile variables (program parameters) input and output (also see chapter 9).

Textfiles may be accessed through the standard file procedures get and put. This can, of course be quite cumbersome as these procedures are defined for single character manipulation. To illustrate, consider one has a natural number stored in a variable x and wishes to print it on the file output. Note that the pattern of characters denoting the decimal representation of the value will be quite different from that denoting the value written as a Roman numeral (see program 4.7). But as one is usually interested in decimal notation, it appears sensible to offer built-in standard transformation procedures that translate abstract numbers (from whatever computer-internal representation is used) into sequences of decimal digits and vice versa.

The two standard procedures read and write are thereby extended to facilitate the analysis and the formation of textfiles. The syntax for calling these procedures is non-standard, for they can be used with a variable number of parameters whose types are not fixed.

A. The procedure read

Let v1,v2, ..., vn denote variables of type char, integer, or real, and let f denote a textfile.

1. read(v1, ..., vn) stands for
read(input,v1, ..., vn)

2. `read(f,v1, ..., vn)` stands for
`begin read(f,v1); ... ; read(f,vn) end`
3. `readln(v1, ..., vn)` stands for
`readln(input,v1, ..., vn)`
4. `readln(f,v1, ..., vn)` stands for
`begin read(f,v1); ... ; read(f,vn); readln(f) end`

The effect is that after `vn` is read (from the textfile `f`), the remainder of the current line is skipped. (However, the values of `v1...vn` may stretch over several lines.)

5. If `ch` is a variable of type `char`, then
`read(f,ch)` stands for

```
begin ch := f↑; get(f) end
```

If a parameter `v` is of type `integer` (or a subrange thereof) or `real`, a sequence of characters, which represents an `integer` or a `real` number according to the Pascal syntax, is read. (Consecutive numbers must be separated by blanks or ends of lines.)

examples:

Read and process a sequence of numbers where the last value is immediately followed by an asterisk. Assume `f` to be a textfile, `x` and `ch` to be variables of types `integer` (or `real`) and `char` respectively.

```
reset(f);
repeat read(f,x,ch);
  P(x)
until ch='*' 
```

Perhaps a more common situation is when one has no way of knowing how many data items are to be read, and there is no special symbol that terminates the list. Two convenient schemata follow. In the first, single items are processed.

```
reset(f); read(f,x);
while not eof(f) do
begin P(x);
  read(f,x)
end
```

Notice that the last call of `read`, which causes `eof(f)` to become true, does not return a defined value for `x`.

The second schema processes n -tuples of numbers:

```

reset(f); read(f,x1);
while not eof(f) do
begin read(f,x2, ..., xn);
  P(x1, ..., xn);
  read(f,x1)
end

```

(For the above schema to function properly, the total number of single items must be a multiple of n.)

B. The procedure write

The procedure write appends character strings (one or more characters) to a textfile. Let p₁, p₂, ..., p_n be parameters of the form defined below (see 5), and let f be a textfile. Then, when writing onto the file f:

1. write(p₁, ..., p_n) stands for
write(output,p₁, ..., p_n)
2. write(f,p₁, ..., p_n) stands for
begin write(f,p₁); ... ; write(f,p_n) end
3. writeln(p₁, ..., p_n) stands for
writeln(output,p₁, ..., p_n)
4. writeln(f,p₁, ..., p_n) stands for
begin write(f,p₁); ... ; write(f,p_n); writeln(f) end

This has the effect of writing p₁, ..., p_n and then terminating the current line of the textfile f.

5. Every parameter p_i must be of one of the forms:

```

e
e : e1
e : e1 : e2

```

where e, e₁, and e₂ are expressions.

6. e is the value to be written and may be of type char, integer, real, Boolean, or it may be a string. In the first case, write(f,c) stands for
f↑ := c; put(f)
7. e₁--called the minimum field width--is an optional control. It must be a natural number and indicates the minimum number of characters to be written. In general, the value e is written with e₁ characters (with preceding blanks). If e₁ is "too small", more space is allocated. (Reals must be written with at least one preceding blank; however, this restriction does not apply to integer values.) If no field length is specified, a default value (implementation dependent) is assumed according to the type of the expression e.

8. e_2 --called the fraction length--is an optional control and is applicable only when e is of type real. It must be a natural number and specifies the number of digits to follow the decimal point. (The number is then said to be written in fixed-point notation.) If no fraction length is specified, the value is printed in decimal floating-point form.
10. If the value e is of type Boolean, then the standard identifier true or false is written.

The purpose of this chapter is to introduce those features that are peculiar to the implementation on the Control Data 6000 computers. The reader is warned that reliance upon any of the characteristics peculiar to PASCAL 6000-3.4 may render his programs unacceptable to other implementations of Pascal. One is, therefore, advised to use only features described as Standard Pascal in the previous chapters whenever possible, and certainly when writing "portable" programs.

The topics of this chapter fall into four categories:

- A) Extensions to the language
- B) Specifications left undefined in the preceding chapters
- C) Restrictions
- D) Additional predefined procedures, functions, and types

A. Extensions to the language Pascal

This section defines non-standard language constructs available on the Pascal 6000-3.4 system. Although they may be oriented toward the particular environment provided by the given operating system, they are described and can be understood in machine independent terms.

A.1 Segmented files

A file can be regarded as being subdivided into so-called segments, i.e. as a sequence of segments, each of which is itself a sequence. PASCAL 6000-3.4 offers a facility to declare a file as being segmented, and to recognize segments and their boundaries. Each segment of such a file is a "logical record" in CDC SCOPE terminology.

```
declaration:  
  <file type> ::= segmented file of <type>
```

```
an example:  
  type T = segmented file of char;
```

The predicate function

```
 eos(x)      returns the value true when the file x is  
              positioned at the end of a segment, otherwise  
              false.
```

The following two standard procedures are introduced:

`putseg(x)` must be called when the generation of a segment of the file `x` has been completed, and

`getseg(x)` is called in order to initiate the reading of the next segment of the file `x`. It assigns to the buffer variable `x†` the first component of that next segment. If no next segment exists, `eof(x)` becomes true; if a next segment exists but is empty, then `eos(x)` becomes true and `x†` is undefined. Subsequent calls of `get(x)` will either step on to the next component or, if it does not exist, cause `eos(x)` to become true.

`Get(x)` must not be called if either `eos(x)` or `eof(f)` is true; `eof(x)` always implies `eos(x)`.

The advantages of a segmented file lie in the possibility of positioning the reading or writing head (relatively) quickly to any segment in the file. For the purposes of reading and (re)writing a segmented file, the standard procedures `getseg` and `rewrite` are extended to accept two arguments.

`getseg(x,n)` initiates the reading of the `n`th segment counting from the current position of the file. `n>0` implies counting segments in the forward direction; `n<0` means counting them backwards; and `n=0` indicates the current segment. Note: `getseg(x,1)` is equivalent to `getseg(x)`.

`rewrite(x,n)` initiates the (re)writing of `x` at the beginning of the `n`th segment counting from the current position. Note: `rewrite(x,1)` is not equivalent to `rewrite(x)`. The latter causes initiation of (re)writing at the very beginning of the entire file.

Since files are organized for sequential (forward) processing, one should not expect `getseg` and `rewrite` to be as efficient for `n<0` as they are for `n>0`.

The following two program schemas, with the parametric statements `W`, `R`, and `S`, show the operations of sequential writing and reading of a segmented file.

Writing a segmented file `x`:

```
rewrite(x);
repeat {generate a segment}
  repeat {generate a component}
    W(x†); put(x)
  until p;
  putseg(x)
until q
```

Note: this schema will never generate an empty file nor an empty segment.

Reading a segmented file x:

```

reset(x);
while not eof(x) do
begin {process a segment}
  while not eos(x) do
    begin {process a component}
      R(x↑); get(x)
    end;
    S; getseg(x)
end

```

The next example shows a procedure that reads a segmented textfile f and copies the first n lines of each segment onto the file output.

```

procedure list;
var i,s: integer;
begin s := 0; reset(f);
  while not eof(f) do
    begin s := s+1; i := 0;
      writeln('segment',s);
      while not eos(f) and (i<n) do
        begin i := i+1; {copy a line}
          while not eoln(f) do
            begin write(f↑); get(f) {next character}
            end;
          writeln; readln(f) {next line}
        end;
        getseg(f) {next segment}
      end
    end
  end
end

```

The standard procedures `read` and `write` can also be applied to segmented textfiles.

A.2 External procedures

PASCAL 6000-3.4 provides a facility to access external procedures, i.e. procedures (functions) that exist outside the user program and have been separately compiled. This enables the Pascal programmer to access program libraries. The declaration of such a procedure consists of a procedure heading followed by the word "extern" or "Fortran".

B. Specifications left undefined in the preceding chapters

B.1 The program heading and external files

A PASCAL file variable is implemented as a file in the CDC operating system. Local files are allocated on disc store or in the Extended Core Store (ECS). Storage is allocated when they are generated and automatically released when the block to which they are local is terminated.

Files that exist outside the program (i.e. before or after program execution) may be made available to the program if they are specified as actual parameters in the program call statement (EXECUTE) of the control card record. They are called external files and are substituted for the formal parameters specified in the program heading. The heading has the following form:

```
program <identifier> ( <program parameter>
                         {, <program parameter>} ) ;
```

where a program parameter is either:

```
<file identifier>      -or-      <file identifier> *
```

The parameters are formal file identifiers; they must be declared as file variables in the main program in exactly the same way as actual local file variables.

Files denoted by the formal parameters input and output have a somewhat special status. The following rules must be noted:

1. The program heading must contain the formal parameter output.
2. Contrary to all other external files, the two formal file identifiers input and output must not be defined in a declaration, because their declaration is automatically assumed to be:

```
var input, output: text;
```

3. The procedures reset and rewrite have no effect if applied to the actual files INPUT and OUTPUT.

example:

```
program P(output, x, y);
           ...
var x,y: text;
```

If an actual parameter in the EXECUTE statement of the control card record is left empty, the corresponding formal parameter in

the program heading is then assumed as the actual "logical file name". For example, when calling a program with the heading:

```
program P(output,f,g);
```

then EXECUTE,(,X,) is equivalent to EXECUTE,P(OUTPUT,X,G). The full specification of the file parameters is recommended because reliance on default values often leads to mistakes that could easily have been avoided.

B.2 Representation of files

In the case of external files it is important to know the representation of files chosen by the PASCAL compiler. Every component of a PASCAL-6000 file occupies an integral number of 60-bit words, with the exception of files with component type char (textfiles). In this case PASCAL files use the "standard" representation imposed by CDC's text file conventions: 10 characters are packed into each word, implying that the procedures put and get include packing and unpacking operations when applied to textfiles. The end of a line is represented by at least 12, right-adjusted zero-bits in a word. Files originating from card decks follow the same general textfile conventions. Note that the operating system removes most (but not necessary all) trailing blanks when reading cards. Hence, such files do not necessarily consist of 80-character "card images".

Files that are not segmented are written as a single "logical record" (in SCOPE terminology). While reading an unsegmented external file, end-of-record marks are ignored [for an exception, see point 3 below]. In segmented files, each segment corresponds to a "logical record". There is no provision to specify a "record level".

Use of external files

1. If an external file is to be read (written), then in the case of non-segmented files, reading (writing) must be initiated by the statement

```
reset(x)      ( rewrite(x) )
```

and in the case of segmented files by

```
reset(x)      ( rewrite(x) ) or  
getseg(x,n)  ( rewrite(x,n) )
```

(This statement is automatically implied for the files denoted by the formal parameters input and output, and must not be specified by the programmer.)

2. Every external file is automatically "opened" by a call of

the OPE routine of the operating system. If this opening is to be restricted to the read function--e.g. in the case of a permanent file without write permission--then this has to be indicated by an asterisk following the file parameter in the program heading. The asterisk itself constitutes no protection against writing on the file.

```
example:
program testdata(output, data*);
  ...
  var data: file of real;
    r: real;
    ...
    r := data↑; get(data)
    ...
  
```

3. If the actual file name INPUT is substituted corresponding to a formal program parameter, say f, then f is the current single logical record of the file INPUT.

B.3 The standard types

INTEGER

The standard identifier maxint is defined as

```
const maxint = 281474976710655; { = 2**48 - 1 }
```

The reader is cautioned, however, that the CDC computer provides no indication of overflow. It is, therefore, the programmer's responsibility to provide a check whenever this might occur.

Actually, the machine is capable of storing integers up to an absolute value of 2**59, but then only the operations of addition (+), subtraction (-), taking the absolute value, multiplication and division by powers of 2 (implemented as shifts), and comparisons are correctly executed in this range (as long as no overflow occurs). In particular, one cannot even print an integer value i when abs(i)>maxint. This does, however, allow the following test:

```
if abs(i) > maxint then write(' too big')
```

REAL

The type real is defined according to CDC 6000 floating point format. Provided is a mantissa with 48 bits, corresponding to 14 decimal digits. The maximum absolute magnitude is 10**322.

CHAR

A value of type **char** is an element in the character set provided by the particular installation. The following 3 versions exist:

- 1) The CDC Scientific 64-character set
- 2) The CDC Scientific 63-character set
- 3) The CDC ASCII 64-character set

Table 13.a lists the available characters and indicates their ordering: **Note**: the CDC specification implies an ordering of the ASCII characters which differs from the International Standard (ISO)!

CDC Scientific Character Set with 64 elements

	Ø	1	2	3	4	5	6	7	8	9
Ø	:	A	B	C	D	E	F	G	H	I
10	J	K	L	M	N	O	P	Q	R	S
20	T	U	V	W	X	Y	Z	Ø	1	2
30	3	4	5	6	7	8	9	+	-	*
40	/	()	\$	=	,	.	≡	[
50]	%	≠	↷	∨	∧	↑	↓	<	>
60	≤	≥	¬	:						

Comments:

- Ø not used in 63-character set version
- 51 : in the 63-character set version
- 48 ' at ETH
- 53 { at ETH
- 57 } at ETH

ASCII Character Set with CDC's ordering

	Ø	1	2	3	4	5	6	7	8	9
Ø	:	A	B	C	D	E	F	G	H	I
10	J	K	L	M	N	O	P	Q	R	S
20	T	U	V	W	X	Y	Z	Ø	1	2
30	3	4	5	6	7	8	9	+	-	*
40	/	()	\$	=	,	.	≠	[
50]	%	"	-	!	&	'	?	<	>
60	@	＼	＾	:						

Figure 13.a CDC character sets

Based upon the above character sets, the following characters are accepted as synonyms for the standard symbol given in the left column:

Standard Pascal	CDC scientific	ASCII
<u>not</u>	~	
<u>and</u>	^	&
<u>or</u>	v	
<u><></u>	#	
<u><=</u>	<	
<u>>=</u>	>	

Figure 13.b: Alternative representation of standard symbols

B.4 The standard procedure "write"

If no minimum field length parameter is specified, the following default values are assumed.

type	default
integer	10
real	22 (where the exponent is always expressed in the form: E \pm 999)
Boolean	10
char	1
a string	length of the string
alfa (see D.1)	10

The end of each line in a textfile f must be explicitly indicated by writeln(f), where writeln(output) may be written simply as writeln. If a textfile is to be sent to a printer, no line may contain more than 136 characters. The first character of each line is interpreted by the printer as a control character and is not printed. The following characters are interpreted to mean

'+'	no line feed (overprinting)
blank	single spacing
'0'	double spacing
'.'	triple spacing
'1'	skip to top of next page before printing

The procedure writeln(x) is used to mark the end of a line on file x. The conventions of the CDC operating system regarding textfile representation are such that this procedure is forced to emit some extra blanks under certain circumstances. Hence,

upon reading, a textfile may contain blanks at the end of lines that were never explicitly written. (Sorry about this!)

C. Restrictions (as of March 1974)

1. The word segmented is reserved.
2. The base type of a set must be either
 - a) a scalar with at most 58 elements (or a subrange thereof)
or
 - b) a subrange with a minimum element greater than or equal to zero, and a maximum element less than or equal to 58.
or
 - c) a subrange of the type char with the maximum element less than or equal to the value chr(58).
3. Standard (built-in) procedures or functions are not accepted as actual parameters. For example, in order to run program 11.6 in PASCAL 6000-3.4, one would have to write auxiliary functions as follows:

```

    ...
function sine(x: real): real;
  begin sine := sin(x)  end;

function cosine(x: real): real;
  begin cosine := cos(x)  end;

function zero(function f: real; a,b: real): real;
  begin ...  end;
  ...

begin
  read(x,y);  writeln(x,y,zero(sine,x,y));
  read(x,y);  writeln(x,y,zero(cosine,x,y))
end.

```

4. It is not possible to construct a file of files; however, records and arrays with files as components are allowed.

D. Additional predefined types, procedures, and functions

D.1 Additional predefined types

The type alfa is predefined by:

```
type alfa = packed array[1..10] of char;
```

(Hence, a value of type alfa is representable in exactly one word.) The constants of this type are strings of exactly 10 characters.

Applicable on operands of type alfa are assignment (:=) and comparison, where = and <> test equality and <, <=, >=, and > test order according to the underlying character set. Alfa values may be printed by the procedure write.

```
{ program 13.1
  alfa values }

program egalfa(output);

var n1,n2: alfa;
begin write(' names: ');
  n1 := 'raymond'; n2 := 'debbby
  if n2 < n1 then writeln(n2,n1)
    else writeln(n1,n2)
end.
```

names: debby raymond

Note: It is not possible to read alfa values directly; instead, the following is suggested:

```
var buf: array[1..10] of char;
a: alfa; i: integer;
...
for i := 1 to 10 do read(buf[i]);
pack(buf,1,a) {accomplishes read(a)}
...
```

D.2 Additional predefined procedures and functions

Procedures

date(a)	assigns to the alfa variable the current date.
halt	terminates the execution of the program and issues a post-mortem dump.
linelimit(f,x)	f is a textfile and x is an integer expression. The effect is to cause the program to be terminated, if more than x lines are asked to be written on file f.
message(x)	the string x is written into the dayfile. (Hence, x should contain at most 40 characters.)
time(a)	assigns to the alfa variable a the current time.
putseg, getseg,	and the extensions to rewrite and reset are

discussed in section 13.A.1.

Functions

card(x)	equals the cardinality of the set x (i.e. the number of elements contained in the set x.)
clock	a function, without parameters, yielding an integer value equal to the central processor time, expressed in milliseconds, already used by the job.
expo(x)	yields an integer value equal to the exponent of the floating-point representation of the real value x.
undefined(x)	a Boolean function. Its value is true when the real value x is "out of range" or "indefinite", otherwise false [7].
eos(x)	(discussed in section 13.A.1)

How to Use the PASCAL 6000-3.4 SystemA. Control statements (for SCOPE 3.4)

A Pascal job usually consists of four steps. First, the Pascal compiler is loaded. The second step is the compilation step, which yields a listing of the source program and the compiled code. In the third step the compiled code, deposited by the compiler on secondary store, is loaded and linked with precompiled routines for input and output handling, which are provided on a "program library" file. Finally, the compiled and loaded code is executed. These four steps are initiated by appropriate orders to the operating system in the form of control statements. The exact form of these statements and their abbreviated forms (loading and execution can often be ordered by a single statement) depend entirely upon the available operating system, and must therefore be specified by the particular installation.

The actual file parameters, which correspond to the formal file identifiers listed in the program heading, must be specified in the statement initiating execution of the compiled program (usually an EXECUTE command).

The compiler itself is also a Pascal program. Its heading is

```
Program Pascal(input,output,lgo);
```

The first formal parameter denotes the file representing the source program to be compiled; the second, the program listing; and the third, the compiled "binary", relocatable code.

The CDC operating systems allow the omission of actual parameters in the control statements. If an actual file name is omitted, the Pascal convention on program parameters specifies that the formal file identifier be used as the actual file name. Hence, the standard files INPUT, OUTPUT, and LGO are automatically assumed as the default files for the source file, the listing, and the relocatable binary code respectively. Note, however, that these roles may be assumed by other files when their names are entered as actual parameters. Note: actual parameters must consist of at most 7 characters.

B. Compiler options

The compiler may be instructed to generate code according to certain options; in particular, it may be requested to insert or omit run-time test instructions. Compiler directives are written as comments and are designated as such by a \$-character as the first character of the comment:

```
{$<option sequence> <any comments> }
```

Example: {\$T+,P+ }

The option sequence is a sequence of instructions separated by commas. Each instruction consists of a letter, designating the option, followed either by a plus (+) if the option is to be activated or a minus (-) if the option is to be passivated, or by a digit (see X and B below).

The following options are presently available:

T include run-time tests that check

- a) all array indexing operations to insure that the index lies within the specified array bounds.
- b) all assignments to variables of subrange types to make certain that the assigned value lies within the specified range.
- c) all divisions to insure against zero divisors
- d) all automatic integer to real conversions to assure that the converted value satisfies:
abs(i) <= maxint
- e) all case statements to insure that the case selector corresponds to one of the specified case labels.

default = T+

P generate the code necessary to write a complete Post-Mortem Dump (see section 14.C.2) in the case of a run-time error.

default = P+

X if a digit n ($0 \leq n \leq 6$) follows the X, pass the first n parameter descriptors in the registers X0 to X(n-1) (the first in X0, the second in X1, etc.). Otherwise pass them in the locations with the addresses B6+3 to B6+n+2.

$n > 0$ reduces the size of the code produced by the compiler and probably also slightly improves the code. However, the programmer must be aware that with $n > 0$, the compiler cannot use the registers X0 to X $\min(n-1, i-2)$ for the passing of the ith parameter. It is therefore possible that for $n > 0$, the compiler gives the message "running out of registers"; where for $n=0$, it would not.

default = X4

E allows the programmer to control the symbols for the entry points to the object code modules (procedures and functions) that he declares in his program.. The following conventions hold:

-- Modules declared as "extern" or "fortran" get an entry point name equal to the procedure identifier cut to the first seven characters.

-- Local modules get an entry point name depending on the value of the E-option (at the moment of analyzing the module name):

E- A unique symbol is generated by the compiler
 E+ The first seven characters of the module name are taken.

Whenever the cut module name is taken (E+ and "extern" or "fortran"), it is the programmers responsibility to avoid the occurrence of duplicate entry point symbols.

default = E-

L controls the listing of the program text.

default = L+

U allows the user to restrict the number of relevant characters in every source line to 72. The remainder of the line is treated as a comment. With U- the number of relevant characters is 120. The rest of the line is then treated as a comment.

default = U-

B used to specify a lower limit for the size of file buffers. If after the B a digit d ($1 \leq d \leq 9$) occurs, the buffer size S, computed by the compiler, is guaranteed to be $S > 128*d$ words.

default = B4

As the compiler instructions may be written anywhere in the program, it is possible to activate the options selectively over specific parts of the program.

C. Error messages

C.1 Compiler

The compiler indicates a detected error by an arrow, pointing to the relevant place in the text, followed by a number, which corresponds to the messages in Appendix E.

C.2 Run-time (Post-Mortem Dump)

When the compiler option P is turned on (i.e. P+), the compiler generates code that can be used to print a readable "dump" in the case that a run-time error occurs. The dump includes the

following information:

- a) the cause of the trap and where it occurred
- b) a description of each of the procedures (functions) that is activated at the time of the trap. These appear in the reverse order of their calls and consist of:
 - 1) the name of the procedure
 - 2) the location of its call
 - 3) a list of the names and values of the local variables and parameters.
- c) the values of the global variables in the main program.

Only variables and parameters of the types integer, real, Boolean, char, and alfa. Pointers are either "nil" or have an octal value (address). For other scalar variables, the ordinal number of their current value is printed. When, for any one procedure, the option P is turned off (P-), then only the procedure name and the location of its call appear in the dump.

In the case of recursive procedure calls, only the last (most recent) three occurrences of each procedure are listed.

References

=====

1. N. Wirth, The Programming Language Pascal, Acta Informatica, 1, 35-63, 1971.
The Programming Language Pascal (Revised Report), Berichte der Fachgruppe Computer-Wissenschaften ETH Zurich, 5, 1973.
2. -----, "Program Development by Stepwise Refinement", Comm. ACM 14, 221-227, April 1971.
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4. O.J. Dahl, E.W. Dijkstra, C.A.R. Hoare, Structured Programming, Academic Press Inc. 1972.
5. C.A.R. Hoare and N. Wirth, "An Axiomatic Definition of the Programming Language Pascal", Acta Informatica, 2, 335-355, 1973.
6. D.E. Knuth, The Art of Computer Programming, vol 1, Fundamental Algorithms, Addison-Wesley, 1968.
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Appendix A
Standard Procedures and Functions

File handling procedures

put(f) appends the value of the buffer variable f^\uparrow to the file f , and is applicable only if prior to execution, $\text{eof}(f)$ is true. $\text{eof}(f)$ remains true, and f^\uparrow becomes undefined.

get(f) advances the current file position to the next component, and assigns the value of this component to the buffer variable f^\uparrow . If no next component exists, then $\text{eof}(f)$ becomes true, and the value of f^\uparrow is undefined. Applicable only if $\text{eof}(f)$ is false prior to its execution.

reset(f) resets the current file position to its beginning for the purpose of reading, i.e. assigns to the buffer variable f^\uparrow the value of the first element of f . $\text{eof}(f)$ becomes false if f is not empty; otherwise, f^\uparrow is undefined and $\text{eof}(f)$ remains true.

rewrite(f) replaces the current value of f with the empty file. $\text{eof}(f)$ becomes true, and a new file may be written.

page(f) instructs the printer to skip to the top of a new page before printing the next line of the textfile f .

read, readln, write, writeln are applicable on textfiles and are discussed in chapter 12.

Dynamic allocation procedure

new(p) allocates a new variable v and assigns the pointer reference of v to the pointer variable p . If the type of v is a record type with variants, the form

new(p,t1,...,tn) can be used to allocate a variable of the variant with tag field values $t1..tn$. The tag field values must be listed contiguously and in the order of their declaration.

dispose(p) returns the dynamic variable v that is referenced by p .

dispose(p,t1,...,tn) returns the dynamic variable v that is referenced by p and was created by the second form of new. (Implementations may

choose to ignore this statement.)

Data transfer procedures

```
pack(a,i,z)      If a is an array variable of type
                  array[m..n] of T
                  and z is a variable of type
                  packed array[u..v] of T
                  where n-m >= v-u, then this is equivalent to
                  for j := u to v do z[j] := a[j-u+i]
                  and
unpack(z,a,i)   is equivalent to
                  for j := u to v do a[j-u+i] := z[j]
                  (In both cases, j denotes an auxiliary variable
                   not occurring elsewhere in the program.)
```

Arithmetic functions

```
abs(x)    computes the absolute value of x. The type of the result
          is the same as that of x, which must be either integer or
          real.

sqr(x)    computes x*x. The type of the result is the same as that
          of x, which must be either integer or real.

sin(x)    for the following, the type of x must be either real or
          integer. The type of the result is always real.

cos(x)
arctan(x)
exp(x)
ln(x)     (natural logarithm)
sqrt(x)   (square root)
```

Predicates (Boolean functions)

```
odd(x)    the type of x must be integer; the result is true if x
          is odd, otherwise false.

eoln(f)   returns the value true when, while reading the textfile
          f, the end of the current line is reached; otherwise,
          false.

eof(f)    returns the value true when, while reading the file f,
          the "end-of-file" is reached; otherwise, false.
```

Transfer functions

trunc(x) x must be of type real; the result is the greatest integer less than or equal to x for $x \geq 0$, and the least integer greater or equal to x for $x < 0$.

round(x) x must be of type real; the result, of type integer, is the value x rounded.
That is, $\text{round}(x) = \text{trunc}(x+0.5)$, for $x \geq 0$
 $\text{trunc}(x-0.5)$, for $x < 0$

ord(x) the ordinal number of the argument x in the set of values defined by the type of x .

chr(x) x must be of type integer, and the result is the character whose ordinal number is x (if it exists).

Further standard functions

succ(x) x is of any scalar type (except real), and the result is the successor value of x (if it exists).

pred(x) x is of any scalar type (except real), and the result is the predecessor value of x (if it exists).

Appendix B
Summary of Operations

<u>operator</u>	<u>operation</u>	<u>type of operand(s)</u>	<u>result type</u>
<code>:=</code>	assignment	any type except file types	---
arithmetic:			
<code>+ (unary)</code>	identity	integer or real	same as operand
<code>- (unary)</code>	sign inversion		
<code>+</code>	addition	integer or real	integer
<code>-</code>	subtraction		or real
<code>*</code>	multiplication		
<code>div</code>	integer division	integer	integer
<code>/</code>	real division	integer or real	real
<code>mod</code>	modulus	integer	integer
relational:			
<code>=</code>	equality	scalar, string,	
<code><></code>	inequality	set, or pointer	
<code><</code>	less than	scalar or string	
<code>></code>	greater than		Boolean
<code><=</code>	less or equal	scalar or string	
<code>-or-</code>			
<code>>=</code>	set inclusion	set	
<code>greater or equal</code>		scalar or string	
<code>-or-</code>			
<code>set inclusion</code>		set	
<code>in</code>	set membership	first operand is any scalar, the second is its set type	
logical:			
<code>not</code>	negation		
<code>or</code>	disjunction	Boolean	Boolean
<code>and</code>	conjunction		
set:			
<code>+</code>	union		
<code>-</code>	set difference	any set type T	T
<code>*</code>	intersection		

Appendix C
Tables

A. Table of standard identifiers

```

Constants:
  false, true, maxint

Types:
  integer, Boolean, real, char, text

Program parameters:
  input, output

Functions:
  abs, arctan, chr, cos, eof, eoln, exp, ln, odd,
  ord, pred, round, sin, sqr, sqrt, succ, trunc

Procedures:
  get, new, pack, page, put, read, readln, reset,
  rewrite, unpack, write, writeln

```

B. Table of word-delimiters (reserved words)

<u>and</u>	<u>end</u>	<u>nil</u>	<u>set</u>
<u>array</u>	<u>file</u>	<u>not</u>	<u>then</u>
<u>begin</u>	<u>for</u>	<u>of</u>	<u>to</u>
<u>case</u>	<u>function</u>	<u>or</u>	<u>type</u>
<u>const</u>	<u>goto</u>	<u>packed</u>	<u>until</u>
<u>div</u>	<u>if</u>	<u>procedure</u>	<u>var</u>
<u>do</u>	<u>in</u>	<u>program</u>	<u>while</u>
<u>downto</u>	<u>label</u>	<u>record</u>	<u>with</u>
<u>else</u>	<u>mod</u>	<u>repeat</u>	

C. Non-standard, predefined identifiers in PASCAL 6000-3.4

```

Types:
  alfa

Functions:
  card, clock, eos, expo, undefined

Procedures:
  data, getseg, halt, linelimit, message, putseg, time

```

Appendix D
Syntax

Backus-Naur Form (BNF)

Note: the following symbols are meta-symbols belonging to the BNF formalism, and not symbols of the language Pascal.

`::= | { }`

The curly brackets denote possible repetition of the enclosed symbols zero or more times. In general,

`A ::= {B}`

is a short form for the purely recursive rule:

`A ::= <empty> | AB`

BNF

```

<program> ::= <program heading> <block> .

<program heading> ::= program <identifier> ( <file identifier>
                                              {, <file identifier> } );

<file identifier> ::= <identifier>

<identifier> ::= <letter> {<letter or digit>}

<letter or digit> ::= <letter> | <digit>

<block> ::= <label declaration part> <constant definition part>
           <type definition part> <variable declaration part>
           <procedure and function declaration part>
           <statement part>

<label declaration part> ::= <empty> |
    label <label> {, <label>} ;

<label> ::= <unsigned integer>

<constant definition part> ::= <empty> |
    const <constant definition> {; <constant definition>} ;

<constant definition> ::= <identifier> = <constant>

<constant> ::= <unsigned number> | <sign> <unsigned number> |
               <constant identifier> | <sign> <constant identifier> |
               <string>

<unsigned number> ::= <unsigned integer> | <unsigned real>
```

```
<unsigned integer> ::= <digit> {<digit>}

<unsigned real> ::= <unsigned integer> . <digit> {<digit>} |
    <unsigned integer> . <digit> {<digit>} E <scale factor> |
    <unsigned integer> E <scale factor>

<scale factor> ::= <unsigned integer> | <sign> <unsigned integer>

<sign> ::= + | -

<constant identifier> ::= <identifier>

<string> ::= ' <character> {<character>} '

<type definition part> ::= <empty> |
    type <type definition> {; <type definition>} ;

<type definition> ::= <identifier> = <type>

<type> ::= <simple type> | <structured type> | <pointer type>

<simple type> ::= <scalar type> | < subrange type> |
    <type identifier>

<scalar type> ::= ( <identifier> {, <identifier>} )

< subrange type> ::= <constant> .. <constant>

<type identifier> ::= <identifier>

<structured type> ::= <unpacked structured type> |
    packed <unpacked structured type>

<unpacked structured type> ::= <array type> | <record type> |
    <set type> | <file type>

<array type> ::= array [ <index type> {, <index type>} ] of
    <component type>

<index type> ::= <simple type>

<component type> ::= <type>

<record type> ::= record <field list> end

<field list> ::= <fixed part> | <fixed part> ; <variant part> |
    <variant part>

<fixed part> ::= <record section> {; <record section>}

<record section> ::= <field identifier> {, <field identifier>} :
    <type> | <empty>

<variant part> ::= case <tag field> <type identifier> of
    <variant> {; <variant>}
```

```

<tag field> ::= <field identifier> : | <empty>
<variant> ::= <case label list> : ( <field list> ) | <empty>
<case label list> ::= <case label> { , <case label>}
<case label> ::= <constant>
<set type> ::= set of <base type>
<base type> ::= <simple type>
<file type> ::= file of <type>
<pointer type> ::= ↑ <type identifier>
<variable declaration part> ::= <empty> |
    var <variable declaration> { ; <variable declaration>} ;
<variable declaration> ::= <identifier> { , <identifier>} : <type>
<procedure and function declaration part> ::= |
    { <procedure or function declaration> ; }
<procedure or function declaration> ::= <procedure declaration> |
    <function declaration>
<procedure declaration> ::= <procedure heading> <block>
<procedure heading> ::= procedure <identifier> : |
    procedure <identifier> ( <formal parameter section>
        { ; <formal parameter section>} ) ;
<formal parameter section> ::= <parameter group> |
    var <parameter group> | function <parameter group> |
    procedure <identifier> { , <identifier>} ;
<parameter group> ::= <identifier> { , <identifier>} :
    <type identifier>
<function declaration> ::= <function heading> <block>
<function heading> ::= function <identifier> : <result type> : |
    function <identifier> ( <formal parameter section>
        { ; <formal parameter section>} ) : <result type> ;
<result type> ::= <type identifier>
<statement part> ::= <compound statement>
<statement> ::= <unlabelled statement> |
    <label> : <unlabelled statement>
<unlabelled statement> ::= <simple statement> |
    <structured statement>
<simple statement> ::= <assignment statement> |

```

```

<procedure statement> | <go to statement> |
<empty statement>

<assignment statement> ::= <variable> := <expression> |
    <function identifier> := <expression>

<variable> ::= <entire variable> | <component variable> |
    <referenced variable>

<entire variable> ::= <variable identifier>

<variable identifier> ::= <identifier>

<component variable> ::= <indexed variable> | <field designator> |
    <file buffer>

<indexed variable> ::= <array variable> [ <expression>
    {, <expression>} ]

<array variable> ::= <variable>

<field designator> ::= <record variable> . <field identifier>

<record variable> ::= <variable>

<field identifier> ::= <identifier>

<file buffer> ::= <file variable> ↑

<file variable> ::= <variable>

<referenced variable> ::= <pointer variable> ↑

<pointer variable> ::= <variable>

<expression> ::= <simple expression> | <simple expression>
    <relational operator> <simple expression>

<relational operator> ::= = | <> | < | <= | >= | > | in

<simple expression> ::= <term> | <sign> <term> |
    <simple expression> <adding operator> <term>

<adding operator> ::= + | - | or

<term> ::= <factor> | <term> <multiplying operator> <factor>

<multiplying operator> ::= * | / | div | mod | and

<factor> ::= <variable> | <unsigned constant> | ( <expression> ) |
    <function designator> | <set> | not <factor>

<unsigned constant> ::= <unsigned number> | <string> |
    <constant identifier> | nil

<function designator> ::= <function identifier> |
    <function identifier> ( <actual parameter>

```

```

    { , <actual parameter>} )

<function identifier> ::= <identifier>

<set> ::= [ <element list> ]

<element list> ::= <element> { , <element>} | <empty>

<element> ::= <expression> | <expression> .. <expression>

<procedure statement> ::= <procedure identifier> |
    <procedure identifier> ( <actual parameter>
    { , <actual parameter>} )

<procedure identifier> ::= <identifier>

<actual parameter> ::= <expression> | <variable> |
    <procedure identifier> | <function identifier>

<go to statement> ::= goto <label>

<empty statement> ::= <empty>

<empty> ::=

<structured statement> ::= <compound statement> |
    <conditional statement> | <repetitive statement> |
    <with statement>

<compound statement> ::= begin <statement> { ; <statement>} end

<conditional statement> ::= <if statement> | <case statement>

<if statement> ::= if <expression> then <statement> |
    <if expression> then <statement> else <statement>

<case statement> ::= case <expression> of <case list element>
    { ; <case list element>} end

<case list element> ::= <case label list> : <statement> |
    <empty>

<case label list> ::= <case label> { , <case label> }

<repetitive statement> ::= <while statement> | <repeat statement> |
    <for statement>

<while statement> ::= while <expression> do <statement>

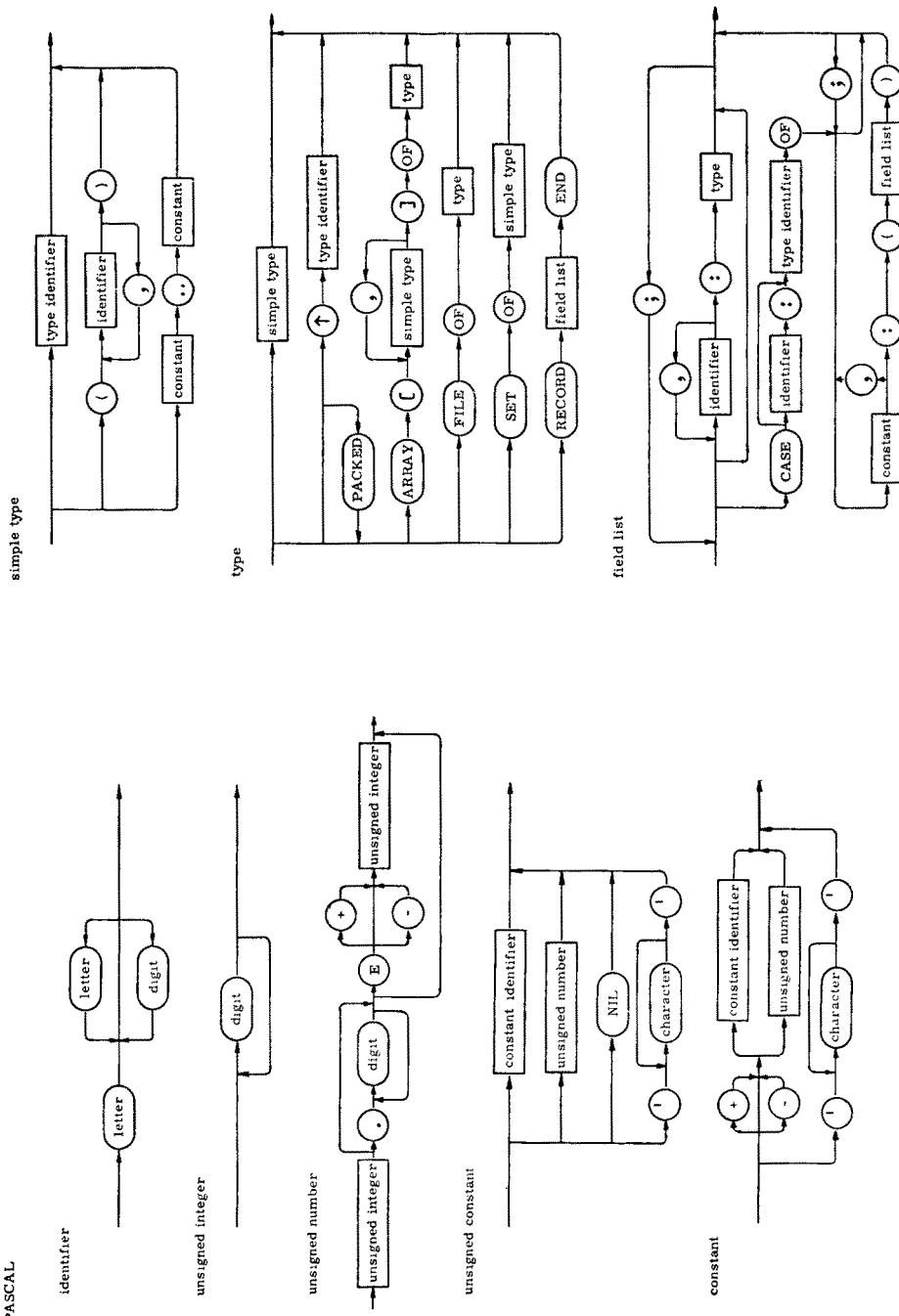
<repeat statement> ::= repeat <statement> { ; <statement>}
    until <expression>

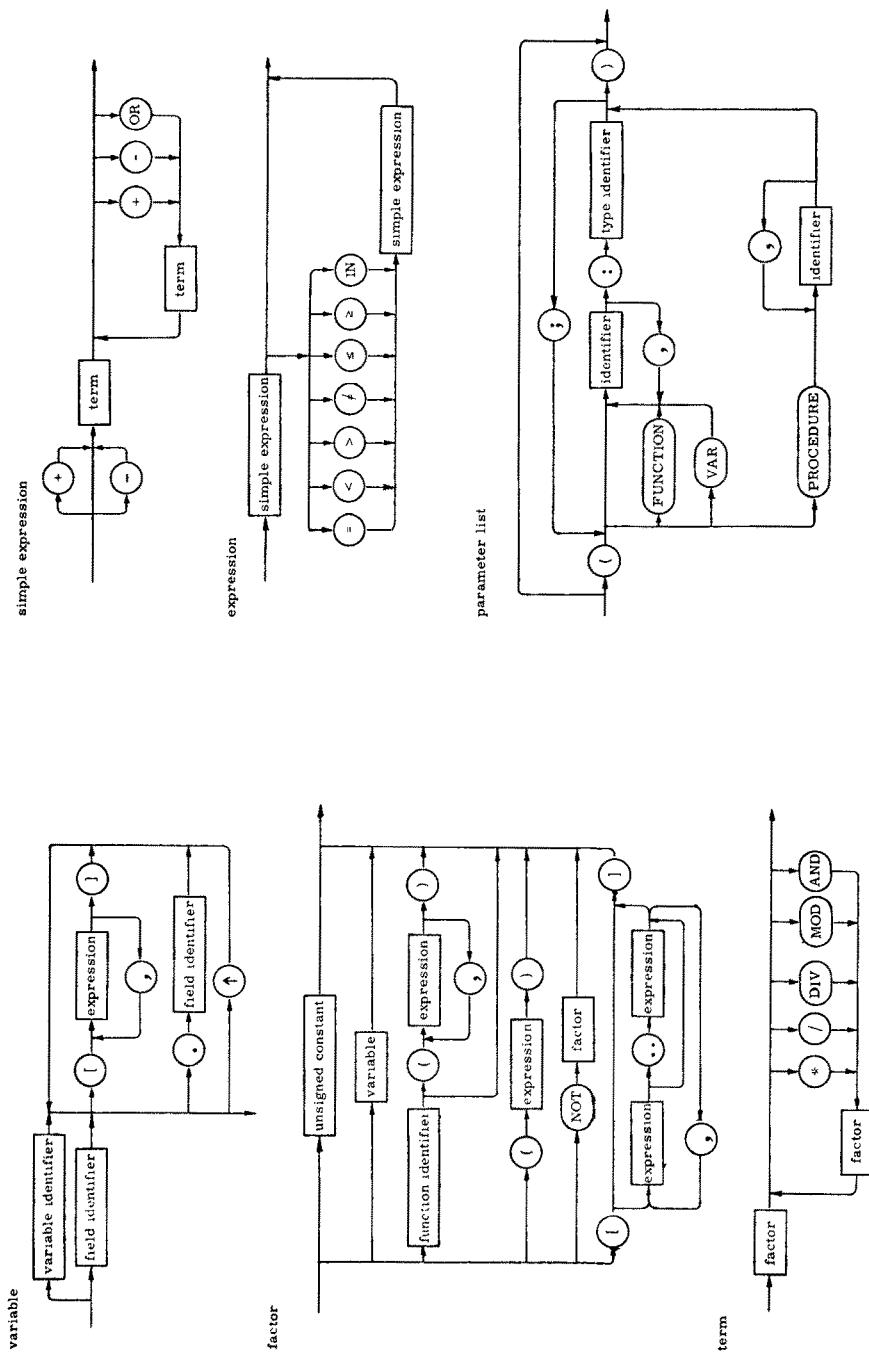
<for statement> ::= for <control variable> := <for list> do
    <statement>

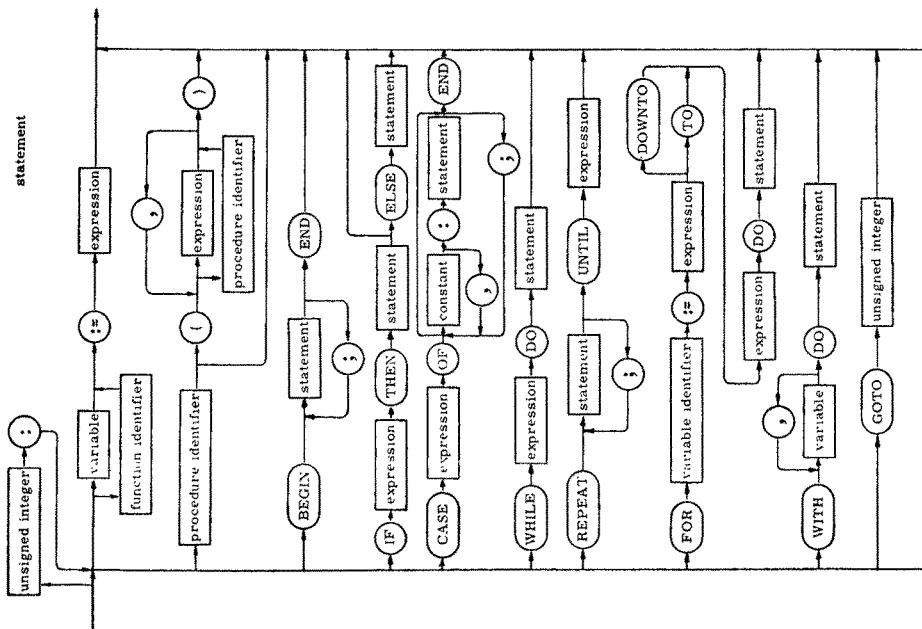
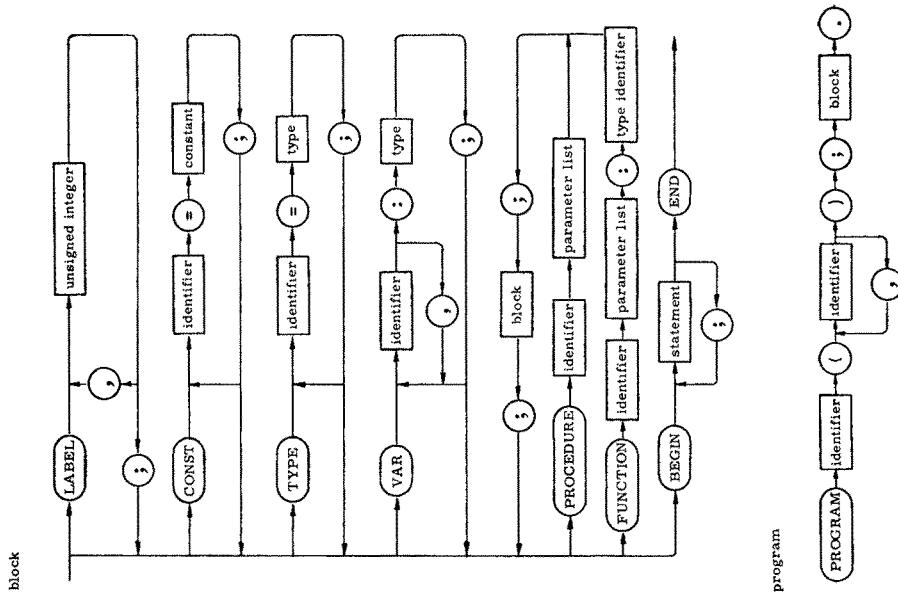
<for list> ::= <initial value> to <final value> |
    <initial value> downto <final value>

```

```
<control variable> ::= <identifier>
<initial value> ::= <expression>
<final value> ::= <expression>
<with statement> ::= with <record variable list> do <statement>
<record variable list> ::= <record variable> {, <record variable>}
```







**Appendix E
Error Number Summary**

```
1: error in simple type
2: identifier expected
3: 'program' expected
4: ')' expected
5: ':' expected
6: illegal symbol
7: error in parameter list
8: 'of' expected
9: '(' expected
10: error in type
11: '[' expected
12: ']' expected
13: 'end' expected
14: ';' expected
15: integer expected
16: '=' expected
17: 'begin' expected
18: error in declaration part
19: error in field-list
20: '.' expected
21: '*' expected

50: error in constant
51: ':=' expected
52: 'then' expected
53: 'until' expected
54: 'do' expected
55: 'to'/'downto' expected
56: 'if' expected
57: 'file' expected
58: error in factor
59: error in variable

101: identifier declared twice
102: low bound exceeds highbound
103: identifier is not of appropriate class
104: identifier not declared
105: sign not allowed
106: number expected
107: incompatible subrange types
108: file not allowed here
109: type must not be real
110: tagfield type must be scalar or subrange
111: incompatible with tagfield type
112: index type must not be real
113: index type must be scalar or subrange
114: base type must not be real
115: base type must be scalar or subrange
116: error in type of standard procedure parameter
117: unsatisfied forward reference
```

118: forward reference type identifier in variable declaration
119: forward declared; repetition of parameter list not allowed
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allowed
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declaration
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```
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303: value to be assigned is out of bounds
304: element expression out of range

398: implementation restriction
399: variable dimension arrays not implemented
```

Appendix F
Programming Examples

```

{ PASCAL 6000-3.4 }

procedure rdr(var f: text; var x: real);
{ read real numbers in 'free format' }
const t48 = 281474976710656;
limit = 56294995342131;
z = 27; { ord('0') }
lim1 = 322; { maximum exponent }
lim2 = -292; { minimum exponent }
type posint = 0..323;
var ch: char; y: real; a,i,e: integer;
s,ss: boolean; { signs }

function ten(e: posint): real; { = 10**e, 0<e<322 }
var i: integer; t: real;
begin i := 0; t := 1.0;
repeat if odd(e) then
  case i of
    0: t := t * 1.0e1;
    1: t := t * 1.0e2;
    2: t := t * 1.0e4;
    3: t := t * 1.0e8;
    4: t := t * 1.0e16;
    5: t := t * 1.0e32;
    6: t := t * 1.0e64;
    7: t := t * 1.0e128;
    8: t := t * 1.0e256
  end ;
  e := e div 2; i := i+1
until e = 0;
ten := t
end;

begin
if eof(f) then
begin message('**tried to read past eos/eof');
halt
end;
{skip leading blanks}
while (f^=' ') and (not eof(f)) do get(f);
if not eof(f) then
begin
ch := f^;
if ch = '-' then
begin s := true; get(f); ch := f^
end else
begin s := false;
if ch = '+' then
begin get(f); ch := f^
end
end
end;

```

```

if not(ch in ['0'..'9']) then
begin message('**digit expected'); halt;
end;
a := 0; e := 0;
repeat if a < limit then a := 10*a + ord(ch)-z
else e := e+1;
get(f); ch := f↑
until not(ch in ['0'..'9']);
if ch = '.' then
begin { read fraction } get(f); ch := f↑;
while ch in ['0'..'9'] do
begin if a < limit then
begin a := 10*a + ord(ch)-z; e := e-1
end;
get(f); ch := f↑
end
end;
if ch = 'e' then
begin { read scale factor } get(f); ch := f↑;
i := 0;
if ch = '-' then
begin ss := true; get(f); ch := f↑
end else
begin ss := false; if ch = '+' then
begin get(f); ch := f↑
end
end;
while ch in ['0'..'9'] do
begin if i<limit then
begin i := 10*i + ord(ch)-z end;
get(f); ch := f↑
end;
if ss then e := e-i else e := e+i;
end;
if e < lim2 then
begin a := 0; e := 0
end else
if e > lim1 then
begin message('**number too large'); halt end;
{ 0 < a < 2**49 }
if a >= t48 then y := ((a+1) div 2) * 2.0
else y := a;
if s then y := -y;
if e < 0 then x := y/ten(-e) else
if e <> 0 then x := y*ten(e) else x := y;
end;
end ;

```

```

{ PASCAL 6000-3.4 }

procedure wre(var f:text; x: real; n: integer);
  { write real number x in n characters }
  const t48 = 281474976710656; { 2**48 }
    realt48 = 2.81474976710656e14;
    z = 27; { ord('0') }
  type posint = 0..323;
  var c,d,e,e0,e1,e2,i: integer;

  function ten(e: posint): real; { 10**e, 0<e<322 }
    var i: integer; t: real;
  begin i := 0; t := 1.0;
    repeat if odd(e) then
      case i of
        0: t := t * 1.0e1;
        1: t := t * 1.0e2;
        2: t := t * 1.0e4;
        3: t := t * 1.0e8;
        4: t := t * 1.0e16;
        5: t := t * 1.0e32;
        6: t := t * 1.0e64;
        7: t := t * 1.0e128;
        8: t := t * 1.0e256
      end;
      e := e div 2; i := i+1
    until e = 0;
    ten := t
  end { ten };

begin { at least 10 characters needed: b+9.9e+999 }
  if undefined(x) then
    begin for i:=1 to n-1 do begin f↑:=''; put(f) end;
      f↑:='u'; put(f)
    end else
    if x=0 then
      begin while n > 1 do
        begin f↑ := '.'; put(f); n:= n-1
        end;
        f↑ := '0'; put(f)
      end else
      begin
        if n <= 10 then n := 3 else n := n-7;
        repeat f↑ := '.'; put(f); n := n-1
        until n <= 14;
        { 2 <= n <= 14 = number of digits to be printed }
        begin { test sign, then obtain exponent }
          if x < 0 then
            begin f↑ := '-'; put(f); x := -x
            end else begin f↑ := '+'; put(f) end;
          e := expo(x) * 77 div 256; { *log(2) }
          if e >= 0 then
            begin e := e+1; x := x/ten(e)
            end else x := x*ten(-e);
          while x < 0.1 do
            begin x := 10.0*x; e := e-1
            end;
        end;
      end;
    end;
end;

```

```

{ 0.1 <= x < 1.0 }
case n of      { rounding }
  2: x := x +0.5e-2;
  3: x := x +0.5e-3;
  4: x := x +0.5e-4;
  5: x := x +0.5e-5;
  6: x := x +0.5e-6;
  7: x := x +0.5e-7;
  8: x := x +0.5e-8;
  9: x := x +0.5e-9;
 10: x := x +0.5e-10;
 11: x := x +0.5e-11;
 12: x := x +0.5e-12;
 13: x := x +0.5e-13;
 14: x := x +0.5e-14
end;
if x >= 1.0 then
  begin x := x * 0.1; e := e+1
  end;
c := trunc(x*real48);
c := 10*c; d := c div t48;
f↑ := chr(d+z); put(f);
f↑ := '.'; put(f);
for i := 2 to n do
begin c := (c - d*t48) * 10; d := c div t48;
  f↑ := chr(d+z); put(f)
end;
f↑ := 'e'; put(f); e := e-1;
if e < 0 then
  begin f↑ := '-'; put(f); e := -e;
  end else begin f↑ := '+'; put(f) end;
e1 := e * 205 div 2048; e2 := e - 10*e1;
e0 := e1 * 205 div 2048; e1 := e1 - 10*e0;
f↑ := chr(e0+z); put(f);
f↑ := chr(e1+z); put(f);
f↑ := chr(e2+z); put(f)
end
end
end { wr } ;

```

INDEX

When a reference in this index is not a section name (e.g. Appendix A), then the reference may be of the following forms:

x1 x1.x2 x1.x2.x3

x1 is always the chapter number. x2 may be a capital letter in which case it may be followed by x3, a number, and refers to a chapter section. When x2 is a small letter, the reference is a figure; when x2 is a number, the reference is a program.

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REPORT

Preface to the Revised Report

The language PASCAL has now been in use for several years, during which considerable experience has been gained through its use, its teaching, and its implementation. Although many reasons suggest that a language should be kept unchanged as soon as it has gained a user community, it would be unwise to ignore this experience and to refrain from making good use of it. This Report therefore describes a revised language which included some changes suggested by the work of the last two years. It is still of the form of the original definition, and in fact the changes are very few and relatively minor. They concern the following subjects :

- Constant parameters are replaced by value parameters (in the sense of Algol 60).
- The class structure is eliminated: pointer variables are bound to a data type instead of a class variable.
- The handling of files is changed such that the buffer variable $f\uparrow$ always has a defined value except when the condition $\text{eof}(f)$ is true.
- Packed records and packed arrays are introduced. As a consequence, the type alfa becomes a special case of a packed character array. The generalization has some consequences on the denotation of strings (formerly called alfa constants).
- Programs require a program heading with external files as parameters.
- All labels require a declaration.

Moreover, there are a few minor syntactic changes, such as the renaming of the powerset structure to set structure.

Implementation efforts on various computers have brought the problem of portability and machine independence of software systems to our closer attention. Many of the above mentioned changes, and also some additional restrictions, were adopted and imposed in the interest of program portability and machine independent definability. They made it possible to define almost the entire language by a set of abstract axioms and rules of inference. Such a rigorous definition is necessary to be able to prove properties of programs. This rigour and machine independence has notably been achieved without sacrifice in the efficiency of program execution.

In order to provide a common base for implementations on various computers, the language defined in this Revised Report is called Standard PASCAL. This standard is defined in terms of the ISO character set.

The chapter on PASCAL for the CDC 6000 computer has been removed

from the Report and replaced by a general chapter on suggested standards for implementation and program interchange. This standard specifies ways to represent programs in terms of available character sets, and lists a number of restrictions on the language with the intent of simplifying implementations. Programs to be used on several computers where PASCAL is available should adhere to this standard.

The two procedures `read` and `write` together with the new procedures `readln`, `writeln`, and `eoln` have been included in the set of standard procedures and are described in a new Chapter 12. They now constitute a binding standard for legible input and output. The latter three are used to control the line structure of text files, and have become necessary, because the Standard language cannot depend on the existence of a line control character (`eol`) in the character set.

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1. Introduction

The development of the language Pascal is based on two principal aims. The first is to make available a language suitable to teach programming as a systematic discipline based on certain fundamental concepts clearly and naturally reflected by the language. The second is to develop implementations of this language which are both reliable and efficient on presently available computers.

The desire for a new language for the purpose of teaching programming is due to my dissatisfaction with the presently used major languages whose features and constructs too often cannot be explained logically and convincingly and which too often defy systematic reasoning. Along with this dissatisfaction goes my conviction that the language in which the student is taught to express his ideas profoundly influences his habits of thought and invention, and that the disorder governing these languages directly imposes itself onto the programming style of the students.

There is of course plenty of reason to be cautious with the introduction of yet another programming language, and the objection against teaching programming in a language which is not widely used and accepted has undoubtedly some justification, at least based on short term commercial reasoning. However, the choice of a language for teaching based on its widespread acceptance and availability, together with the fact that the language most widely taught is thereafter going to be the one most widely used, forms the safest recipe for stagnation in a subject of such profound pedagogical influence. I consider it therefore well worth-while to make an effort to break this vicious circle.

Of course a new language should not be developed just for the sake of novelty; existing languages should be used as a basis for development wherever they meet the criteria mentioned and do not impede a systematic structure. In that sense Algol 60 was used as a basis for Pascal, since it meets the demands with respect to teaching to a much higher degree than any other standard language. Thus the principles of structuring, and in fact the form of expressions, are copied from Algol 60. It was, however not deemed appropriate to adopt Algol 60 as a subset of Pascal; certain construction principles, particularly those of declarations, would have been incompatible with those allowing a natural and convenient representation of the additional features of Pascal.

The main extensions relative to Algol 60 lie in the domain of data structuring facilities, since their lack in Algol 60 was considered as the prime cause for its relatively narrow range of applicability. The introduction of record and file structures should make it possible to solve commercial type problems with Pascal, or at least to employ it successfully to demonstrate such problems in a programming course.

2. Summary of the language

An algorithm or computer program consists of two essential parts, a description of actions which are to be performed, and a description of the data, which are manipulated by these actions. Actions are described by so-called statements, and data are described by so-called declarations and definitions.

The data are represented by values of variables. Every variable occurring in a statement must be introduced by a variable declaration which associates an identifier and a data type with that variable. The data type essentially defines the set of values which may be assumed by that variable. A data type may in Pascal be either directly described in the variable declaration, or it may be referenced by a type identifier, in which case this identifier must be described by an explicit type definition.

The basic data types are the scalar types. Their definition indicates an ordered set of values, i.e. introduces identifiers standing for each value in the set. Apart from the definable scalar types, there exist four standard basic types: Boolean, integer, char, and real. Except for the type Boolean, their values are not denoted by identifiers, but instead by numbers and quotations respectively. These are syntactically distinct from identifiers. The set of values of type char is the character set available on a particular installation.

A type may also be defined as a subrange of a scalar type by indicating the smallest and the largest value of the subrange.

Structured types are defined by describing the types of their components and by indicating a structuring method. The various structuring methods differ in the selection mechanism serving to select the components of a variable of the structured type. In Pascal, there are four basic structuring methods available: array structure, record structure, set structure, and file structure.

In an array structure, all components are of the same type. A component is selected by an array selector, or computable index, whose type is indicated in the array type definition and which must be scalar. It is usually a programmer-defined scalar type, or a subrange of the type integer. Given a value of the index type, an array selector yields a value of the component type. Every array variable can therefore be regarded as a mapping of the index type onto the component type. The time needed for a selection does not depend on the value of the selector (index). The array structure is therefore called a random-access structure.

In a record structure, the components (called fields) are not necessarily of the same type. In order that the type of a selected component be evident from the program text (without executing the program), a record selector is not a computable value, but instead is an identifier uniquely denoting the component to be selected. These component identifiers are

declared in the record type definition. Again, the time needed to access a selected component does not depend on the selector, and the record is therefore also a random-access structure.

A record type may be specified as consisting of several variants. This implies that different variables, although said to be of the same type, may assume structures which differ in a certain manner. The difference may consist of a different number and different types of components. The variant which is assumed by the current value of a record variable may be indicated by a component field which is common to all variants and is called the tag field. Usually, the part common to all variants will consist of several components, including the tag field.

A set structure defines the set of values which is the powerset of its base type, i.e. the set of all subsets of values of the base type. The base type must be a scalar type, and will usually be a programmer-defined scalar type or a subrange of the type integer.

A file structure is a sequence of components of the same type. A natural ordering of the components is defined through the sequence. At any instance, only one component is directly accessible. The other components are made accessible by progressing sequentially through the file. A file is generated by sequentially appending components at its end. Consequently, the file type definition does not determine the number of components.

Variables declared in explicit declarations are called static. The declaration associates an identifier with the variable which is used to refer to the variable. In contrast, variables may be generated by an executable statement. Such a dynamic generation yields a so-called pointer (a substitute for an explicit identifier) which subsequently serves to refer to the variable. This pointer may be assigned to other variables, namely variables of type pointer. Every pointer variable may assume values pointing to variables of the same type T only, and it is said to be bound to this type T. It may, however, also assume the value nil, which points to no variable. Because pointer variables may also occur as components of structured variables, which are themselves dynamically generated, the use of pointers permits the representation of finite graphs in full generality.

The most fundamental statement is the assignment statement. It specifies that a newly computed value be assigned to a variable (or components of a variable). The value is obtained by evaluating an expression. Expressions consist of variables, constants, sets, operators and functions operating on the denoted quantities and producing new values. Variables, constants, and functions are either declared in the program or are standard entities. Pascal defines a fixed set of operators, each of which can be regarded as describing a mapping from the operand types into the result type. The set of operators is subdivided into groups of

1. arithmetic operators of addition, subtraction, sign

inversion, multiplication, division, and computing the remainder.

2. Boolean operators of negation, union (or), and conjunction (and).
3. set operators of union, intersection, and set difference.
4. relational operators of equality, inequality, ordering, set membership and set inclusion. The results of relational operations are of type Boolean.

The procedure statement causes the execution of the designated procedure (see below). Assignment and procedure statements are the components or building blocks of structured statements, which specify sequential, selective, or repeated execution of their components. Sequential execution of statements is specified by the compound statement, conditional or selective execution by the if statement and the case statement, and repeated execution by the repeat statement, the while statement, and the for statement. The if statement serves to make the execution of a statement dependent on the value of a Boolean expression, and the case statement allows for the selection among many statements according to the value of a selector. The for statement is used when the number of iterations is known beforehand, and the repeat and while statements are used otherwise.

A statement can be given a name (identifier), and be referenced through that identifier. The statement is then called a procedure, and its declaration a procedure declaration. Such a declaration may additionally contain a set of variable declarations, type definitions and further procedure declarations. The variables, types and procedures thus declared can be referenced only within the procedure itself, and are therefore called local to the procedure. Their identifiers have significance only within the program text which constitutes the procedure declaration and which is called the scope of these identifiers. Since procedures may be declared local to other procedures, scopes may be nested. Entities which are declared in the main program, i.e. not local to some procedure, are called global. A procedure has a fixed number of parameters, each of which is denoted within the procedure by an identifier called the formal parameter. Upon an activation of the procedure statement, an actual quantity has to be indicated for each parameter which can be referenced from within the procedure through the formal parameter. This quantity is called the actual parameter. There are three kinds of parameters: value parameters, variable parameters, and procedure or function parameters. In the first case, the actual parameter is an expression which is evaluated once. The formal parameter represents a local variable to which the result of this evaluation is assigned before the execution of the procedure (or function). In the case of a variable parameter, the actual parameter is a variable and the formal parameter stands for this variable. Possible indices are evaluated before execution of the procedure (or function). In the case of procedure or function

parameters, the actual parameter is a procedure or function identifier.

functions are declared analogously to procedures. The only difference lies in the fact that a function yields a result which is confined to a scalar or pointer type and must be specified in the function declaration. Functions may therefore be used as constituents of expressions. In order to eliminate side-effects, assignments to non-local variables should be avoided within function declarations.

3. Notation, terminology, and vocabulary

According to traditional Backus-Naur form, syntactic constructs are denoted by English words enclosed between the angular brackets < and > . These words also describe the nature or meaning of the construct, and are used in the accompanying description of semantics. Possible repetition of a construct is indicated by enclosing the construct within metabrackets { and }. The symbol <empty> denotes the null sequence of symbols.

The basic vocabulary of Pascal consists of basic symbols classified into letters, digits, and special symbols.

```
<letter> ::= A|B|C|D|E|F|G|H|I|J|K|L|M|N|O|P|Q|R|S|T|U|V|
           W|X|Y|Z|a|b|c|d|e|f|g|h|i|j|k|l|m|n|o|p|q|r|
           s|t|u|v|w|x|y|z
```

```
<digit> ::= 0|1|2|3|4|5|6|7|8|9
```

```
<special symbol> ::=
    + | - | * | / | = | <> | < | > | <= | >= | ( | ) |
    [ | ] | { | } | := | . | , | : | ; | ' | ^ | div |
    mod | nil | in | or | and | not | if | then | else |
    case | of | repeat | until | while | do | for | to |
    downto | begin | end | with | goto | const | var |
    type | array | record | set | file | function |
    procedure | label | packed | program
```

The construct

```
{<any sequence of symbols not containing ">">}
```

may be inserted between any two identifiers, numbers (cf. 4), or special symbols. It is called a comment and may be removed from the program text without altering its meaning. The symbols { and } do not occur otherwise in the language, and when appearing in syntactic descriptions they are meta-symbols like | and ::= . The symbol pairs (* and *) are used as synonyms for { and }.

4. Identifiers, Numbers, and Strings

Identifiers serve to denote constants, types, variables, procedures and functions. Their association must be unique within their scope of validity, i.e. within the procedure or function in which they are declared (cf. 10 and 11).

```
<identifier> ::= <letter>{<letter or digit>}
<letter or digit> ::= <letter> | <digit>
```

The usual decimal notation is used for numbers, which are the constants of the data types integer and real (see 6.1.2.). The letter E preceding the scale factor is pronounced as "times 10 to the power of".

```
<digit sequence> ::= <digit>{<digit>}
<unsigned integer> ::= <digit sequence>
<unsigned real> ::= <unsigned integer>.<digit sequence> |
    <unsigned integer>.<digit sequence>E<scale factor> |
    <unsigned integer> E <scale factor>
<unsigned number> ::= <unsigned integer> | <unsigned real>
<scale factor> ::= <unsigned integer> |
    <sign><unsigned integer>
<sign> ::= + | -
```

Examples:

```
1      100      0.1      5E-3      87.35E+8
```

Sequences of characters enclosed by quote marks are called strings. Strings consisting of a single character are the constants of the standard type char (see 6.1.2). Strings consisting of n (>1) enclosed characters are the constants of the types (see 6.2.1)

```
packed array [1..n] of char
```

Note: If the string is to contain a quote mark, then this quote mark is to be written twice.

```
<string> ::= '<character>{<character>}'
```

Examples:

```
'A'      ';'      ....
'PASCAL'      'THIS IS A STRING'
```

5. Constant definitions

A constant definition introduces an identifier as a synonym to a constant.

```
<constant identifier> ::= <identifier>
<constant> ::= <unsigned number> | <sign><unsigned number> |
    <constant identifier> | <sign><constant identifier> |
    <string>
<constant definition> ::= <identifier> = <constant>
```

6. Data type definitions

A data type determines the set of values which variables of that type may assume and associates an identifier with the type.

```
<type> ::= <simple type> | <structured type> | <pointer type>
<type definition> ::= <identifier> = <type>
```

6.1. Simple types

```
<simple type> ::= <scalar type> | < subrange type> |
                  <type identifier>
<type identifier> ::= <identifier>
```

6.1.1. Scalar types

A scalar type defines an ordered set of values by enumeration of the identifiers which denote these values.

```
<scalar type> ::= (<identifier> {,<identifier>} )
```

Examples:

```
(red, orange, yellow, green, blue)
(club, diamond, heart, spade)
(Monday, Tuesday, Wednesday, Thursday, Friday,
 Saturday, Sunday)
```

Functions applying to all scalar types (except real) are :

```
succ   the succeeding value (in the enumeration)
pred   the preceding value (in the enumeration)
```

6.1.2. Standard types

The following types are standard in Pascal:

integer	The values are a subset of the whole numbers defined by individual implementations. Its values are the integers (see 4).
real	Its values are a subset of the real numbers depending on the particular implementation. The values are denoted by real numbers (see 4).
Boolean	Its values are the truth values denoted by the identifiers true and false.
char	Its values are a set of characters determined by particular implementations. They are denoted by the characters themselves enclosed within quotes.

6.1.3. Subrange types

A type may be defined as a subrange of another scalar type by indication of the least and the largest value in the subrange. The first constant specifies the lower bound, and must not be greater than the upper bound.

<subrange type> ::= **<constant>** .. **<constant>**

Examples : 1 .. 100
 -10 .. +10
 Monday .. Friday

6.2. Structured types

A structure type is characterised by the type(s) of its components and by its structuring method. Moreover, a structured type definition may contain an indication of the preferred data representation. If a definition is prefixed with the symbol packed, this has no effect on the meaning of a program, but is a hint to the compiler that storage should be economised even at the price of some loss in efficiency of access, and even if this may expand the code necessary for expressing access to components of the structure.

```
<structured type> ::= <unpacked structured type> |  
    packed <unpacked structured type>  
<unpacked structured type> ::= <array type> |  
    <record type> | <set type> | <file type>
```

6.2.1. Array types

An array type is a structure consisting of a fixed number of components which are all of the same type, called the component type. The elements of the array are designated by indices, values belonging to the so-called index type. The array type definition specifies the component type as well as the index type.

```
<array type> ::= array [<index type> { ,<index type>} ] of  
                      <component type>  
<index type> ::= <simple type>  
<component type> ::= <type>
```

If n index types are specified, the array type is called n -dimensional, and a component is designated by n indices.

Examples : `array [1..100] of real`
 `array [1..10, 1..20] of 0..99`
 `array [Boolean] of color`

6.2.2. Record types

A record type is a structure consisting of a fixed number of components, possibly of different types. The record type definition specifies for each component, called a **field**, its type and an identifier which denotes it. The scope of these so-called **field identifiers** is the record definition itself, and they are also accessible within a field designator (cf. 7.2) referring to a record variable of this type.

A record type may have several **variants**, in which case a certain field may be designated as the **tag field**, whose value indicates which variant is assumed by the record variable at a given time. Each variant structure is identified by a case label which is a constant of the type of the tag field.

```

<record type> ::= record <field list> end
<field list> ::= <fixed part> | <fixed part>;<variant part> |
                  <variant part>
<fixed part> ::= <record section> {;<record section>}
<record section> ::=
    <field identifier>{,<field identifier>} : <type> | <empty>
<variant part> ::= case <tag field> <type identifier> of
                  <variant> {;<variant>}
<variant> ::= <case label list> : (<field list>) | <empty>
<case label list> ::= <case label> {,<case label>}
<case label> ::= <constant>
<tag field> ::= <identifier> : | <empty>

```

Examples:

```

record day: 1..31;
        month: 1..12;
        year: integer
end

record name, firstname: alfa;
        age: 0..99;
        married: Boolean
end

record x,y: real;
        area: real;
        case s: shape of
            triangle: (side: real;
                        inclination, angle1, angle2: angle);
            rectangle: (side1, side2: real;
                         skew, angle3: angle);
            circle:   (diameter: real)
end

```

6.2.3. Set types

A set type defines the range of values which is the powerset of its so-called **base type**. Base types must not be structured types. Operators applicable to all set types are:

```

+      union
-      set difference
*      intersection
in      membership

```

The set difference $x - y$ is defined as the set of all elements of x which are not members of y .

```

<set type> ::= set of <base type>
<base type> ::= <simple type>

```

6.2.4. File types

A file type definition specifies a structure consisting of a sequence of components which are all of the same type. The number of components, called the length of the file, is not fixed by the file type definition. A file with 0 components is called empty.

```
<file type> ::= file of <type>
```

Files with component type char are called textfiles, and are a special case insofar as the component range of values must be considered as extended by a marker denoting the end of a line. This marker allows textfiles to be substructured into lines. The type text is a standard type predeclared as

```
type text = file of char
```

6.3. Pointer types

Variables which are declared in a program (see 7.) are accessible by their identifier. They exist during the entire execution process of the procedure (scope) to which the variable is local, and these variables are therefore called static (or statically allocated). In contrast, variables may also be generated dynamically, i.e. without any correlation to the structure of the program. These dynamic variables are generated by the standard procedure new (see 10.1.2.); since they do not occur in an explicit variable declaration, they cannot be referred to by a name. Instead, access is achieved via a so-called pointer value which is provided upon generation of the dynamic variable. A pointer type thus consists of an unbounded set of values pointing to elements of the same type. No operations are defined on pointers except the test for equality.

The pointer value nil belongs to every pointer type; it points to no element at all.

```
<pointer type> ::= ↑<type identifier>
```

Examples of type definitions:

```

color      = (red, yellow, green, blue)
sex        = (male, female)
text       = file of char
shape      = (triangle, rectangle, circle)
card       = array [1..80] of char
alfa       = packed array [1..10] of char
complex   = record re,im: real end
person    = record name, firstname: alfa;
            age: integer;
            married:Boolean;
            father, child, sibling: ↑person;
case s: sex of
            male: (enlisted, bold: Boolean);
            female: (pregnant: Boolean;
                      size: array[1..3] of integer)
end

```

7. Declarations and denotations of variables

Variable declarations consist of a list of identifiers denoting the new variables, followed by their type.

<variable declaration> ::= <identifier>{,<identifier>} : <type>

Every declaration of a file variable f with components of type T implies the additional declaration of a so-called buffer variable of type T. This buffer variable is denoted by f↑ and serves to append components to the file during generation, and to access the file during inspection (see 7.2.3. and 10.1.1.).

Examples:

```

x,y,z: real
u,v: complex
i,j: integer
k: 0..9
p,q: Boolean
operator: (plus, minus, times)
a: array[0..63] of real
b: array[color,Boolean] of complex
c: color
f: file of char
hue1,hue2: set of color
p1,p2: ↑person

```

Denotations of variables either designate an entire variable, a component of a variable, or a variable referenced by a pointer (see 6.3). Variables occurring in examples in subsequent chapters are assumed to be declared as indicated above.

<variable> ::= <entire variable> | <component variable> |
 <referenced variable>

7.1. Entire variables

An entire variable is denoted by its identifier.

```
<entire variable> ::= <variable identifier>
<variable identifier> ::= <identifier>
```

7.2. Component variables

A component of a variable is denoted by the variable followed by a selector specifying the component. The form of the selector depends on the structuring type of the variable.

```
<component variable> ::= <indexed variable> |
    <field designator> | <file buffer>
```

7.2.1. Indexed variables

A component of an n-dimensional array variable is denoted by the variable followed by n index expressions.

```
<indexed variable> ::= 
    <array variable> [<expression> {,<expression>}]
<array variable> ::= <variable>
```

The types of the index expressions must correspond with the index types declared in the definition of the array type.

Examples:

```
a[12]
a[i+j]
b[red,true]
```

7.2.2. Field designators

A component of a record variable is denoted by the record variable followed by the field identifier of the component.

```
<field designator> ::= <record variable>.<field identifier>
<record variable> ::= <variable>
<field identifier> ::= <identifier>
```

Examples:

```
u.re
b[red,true].im
p2^.size
```

7.2.3. File buffers

At any time, only the one component determined by the current file position (read/write head) is directly accessible. This component is called the current file component and is represented by the file's **buffer variable**.

```
<file buffer> ::= <file variable>↑
<file variable> ::= <variable>
```

7.3. Referenced variables

```
<referenced variable> ::= <pointer variable>↑
<pointer variable> ::= <variable>
```

If *p* is a pointer variable which is bound to a type *T*, *p* denotes that variable and its pointer value, whereas *p*↑ denotes the variable of type *T* referenced by *p*.

Examples:

```
p↑.father
p↑.sibling↑.child
```

8. Expressions

Expressions are constructs denoting rules of computation for obtaining values of variables and generating new values by the application of operators. Expressions consist of operands, i.e. variables and constants, operators, and functions.

The rules of composition specify operator **precedences** according to four classes of operators. The operator **not** has the highest precedence, followed by the so-called multiplying operators, then the so-called adding operators, and finally, with the lowest precedence, the relational operators. Sequences of operators of the same precedence are executed from left to right. The rules of precedence are reflected by the following syntax:

```

<unsigned constant> ::= <unsigned number> | <string> |
                        <constant identifier> | nil
<factor> ::= <variable> | <unsigned constant> |
                        <function designator> | <set> | (<expression>) |
                        not <factor>
<set> ::= [ <element list> ]
<element list> ::= <element> {,<element>} | <empty>
<element> ::= <expression> | <expression>..<expression>
<term> ::= <factor> | <term><multiplying operator><factor>
<simple expression> ::= <term> |
                        <simple expression> <adding operator><term> |
                        <adding operator><term>
<expression> ::= <simple expression> |
                        <simple expression><relational operator><simple expression>

```

Expressions which are members of a set must all be of the same type, which is the base type of the set. [] denotes the empty set, and [x..y] denotes the set of all values in the interval x...y.

Examples :

Factors :

```

x
15
(x+y+z)
sin(x+y)
[red,c,green]
[1.5,10..19,23]
not p

```

Terms :

```

x*y
i/(1-i)
p or q
(x<=y) and (y < z)

```

Simple expressions :

```

x+y
-x
hue1 + hue2
i*j + 1

```

Expressions :

```

x = 1.5
p<=q
(i<j) = (j<k)
c in hue1

```

8.1. Operators

If both operands of the arithmetic operators of addition, subtraction and multiplication are of type integer (or a subrange thereof), then the result is of type integer. If one of the operands is of type real, then the result is also of type real.

8.1.1. The operator not

The operator not denotes negation of its Boolean operand.

8.1.2. Multiplying operators

<multiplying operator> ::= * | / | div | mod | and

operator	operation	type of operands	type of result
*	multiplication set intersection	real, integer any set type T	real, integer T
/	division	real, integer	real
<u>div</u>	division with truncation	integer	integer
<u>mod</u>	modulus	integer	integer
<u>and</u>	logical "and"	Boolean	Boolean

8.1.3. Adding operators

<adding operator> ::= + | - | or

operator	operation	type of operands	type of result
+	addition set union	integer, real any set type T	integer, real T
-	subtraction set difference	integer, real any set type T	integer, real T
<u>or</u>	logical "or"	Boolean	Boolean

When used as operators with one operand only, - denotes sign inversion, and + denotes the identity operation.

8.1.4. Relational operators

<relational operator> ::= = | <> | < | <= | >= | > | in

operator	type of operands	result
= <>		
< > =	any scalar or subrange type	Boolean
in	any scalar or subrange type and its set type respectively	Boolean

Notice that all scalar types define ordered sets of values.

The operators <>, <=, >= stand for unequal, less or equal, and greater or equal respectively.

The operators <= and >= may also be used for comparing values of set type, and then denote set inclusion.

If p and q are Boolean expressions, p = q denotes their equivalence, and p <= q denotes implication of q by p. (Note that false < true)

The relational operators = <> < <= > >= may also be used to compare (packed) arrays with components of type char (strings), and then denote alphabetical ordering according to the collating sequence of the underlying set of characters.

8.2. Function designators

A function designator specifies the activation of a function. It consists of the identifier designating the function and a list of actual parameters. The parameters are variables, expressions, procedures, and functions, and are substituted for the corresponding formal parameters (cf. 9.1.2.. 10, and 11).

```
<function designator> ::= <function identifier> |
  <function identifier>(<actual parameter>{,<actual parameter>})
<function identifier> ::= <identifier>
```

Examples: Sum(a,100)
 GCD(147,k)
 sin(x+y)
 eof(f)
 ord(f↑)

9. Statements

Statements denote algorithmic actions, and are said to be executable. They may be prefixed by a label which can be referenced by goto statements.

```

<statement> ::= <unlabelled statement> |
               <label>:<unlabelled statement>
<unlabelled statement> ::= <simple statement> |
                           <structured statement>
<label> ::= <unsigned integer>

```

9.1. Simple statements

A simple statement is a statement of which no part constitutes another statement. The empty statement consists of no symbols and denotes no action.

```

<simple statement> ::= <assignment statement> |
                     <procedure statement> | <goto statement> |
                     <empty statement>
<empty statement> ::= <empty>

```

9.1.1. Assignment statements

The assignment statement serves to replace the current value of a variable by a new value specified as an expression.

```

<assignment statement> ::= <variable> := <expression> |
                           <function identifier> := <expression>

```

The variable (or the function) and the expression must be of identical type, with the following exceptions being permitted:

1. the type of the variable is real, and the type of the expression is integer or a subrange thereof.
2. the type of the expression is a subrange of the type of the variable, or vice-versa.

Examples :

```

x := y + z
p := (1 <= i) and (i < 100)
i := sqr(k) - (i * j)
hue := [blue, succ(c)]

```

9.1.2. Procedure statements

A procedure statement serves to execute the procedure denoted by the procedure identifier. The procedure statement may contain a list of actual parameters which are substituted in place of their corresponding formal parameters defined in the procedure declaration (cf. 10). The correspondence is established by the positions of the parameters in the lists of actual and formal parameters respectively. There exist four kinds of parameters: so-called value parameters, variable parameters, procedure parameters (the actual parameter is a procedure identifier), and function parameters (the actual parameter is a function identifier).

In the case of a value parameter, the actual parameter must be an expression (of which a variable is a simple case). The

corresponding formal parameter represents a local variable of the called procedure, and the current value of the expression is initially assigned to this variable. In the case of a variable parameter, the actual parameter must be a variable, and the corresponding formal parameter represents this actual variable during the entire execution of the procedure. If this variable is a component of an array, its index is evaluated when the procedure is called. A variable parameter must be used whenever the parameter represents a result of the procedure.

Components of a packed structure must not appear as actual variable parameters.

```
<procedure statement> ::= <procedure identifier> |
    <procedure identifier> (<actual parameter>
                           { ,<actual parameter> })
<procedure identifier> ::= <identifier>
<actual parameter> ::= <expression> | <variable> |
    <procedure identifier> | <function identifier>
```

Examples: next
 Transpose(a,n,m)
 Bisect(fct,-1.0,+1.0,x)

9.1.3. Goto statements

A goto statement serves to indicate that further processing should continue at another part of the program text, namely at the place of the label.

```
<goto statement> ::= goto <label>
```

The following restrictions hold concerning the applicability of labels:

1. The scope of a label is the procedure within which it is defined. It is therefore not possible to jump into a procedure.
2. Every label must be specified in a label declaration in the heading of the procedure in which the label marks a statement.

9.2. Structured statements

Structured statements are constructs composed of other statements which have to be executed either in sequence (compound statement), conditionally (conditional statements), or repeatedly (repetitive statements).

```
<structured statement> ::= <compound statement> |
    <conditional statement> | <repetitive statement> |
    <with statement>
```

9.2.1. Compound statements

The compound statement specifies that its component statements are to be executed in the same sequence as they are written. The symbols `begin` and `end` act as statement brackets.

```
<compound statement> ::= begin <statement> { ;<statement>} end
```

Example: `begin z := x ; x := y; y := z end`

9.2.2. Conditional statements

A conditional statement selects for execution a single one of its component statements.

```
<conditional statement> ::=
  <if statement> | <case statement>
```

9.2.2.1. If statements

The if statement specifies that a statement be executed only if a certain condition (Boolean expression) is true. If it is false, then either no statement is to be executed, or the statement following the symbol `else` is to be executed.

```
<if statement> ::= if <expression> then <statement> |
                  if <expression> then <statement> else <statement>
```

The expression between the symbols `if` and `then` must be of type Boolean.

Note:

The syntactic ambiguity arising from the construct

```
if <expression-1> then if <expression-2> then <statement-1>
                      else <statement-2>
```

is resolved by interpreting the construct as equivalent to

```
if <expression-1> then
begin if <expression-2> then <statement-1> else <statement-2>
end
```

Examples:

```
if x < 1.5 then z := x+y else z := 1.5
if p1 <> nil then p1 := p1↑.father
```

9.2.2.2. Case statements

The case statement consists of an expression (the selector) and a list of statements, each being labelled by a constant of the type of the selector. It specifies that the one statement be executed whose label is equal to the current value of the

selector.

```
<case statement> ::= case <expression> of
    <case list element> { ;<case list element>} end
<case list element> ::= <case label list> : <statement> |
    <empty>
<case label list> ::= <case label> { ,<case label> }
```

Examples:

<u>case</u> operator <u>of</u> plus: x := x+y; minus: x := x-y; times: x := x*y <u>end</u>	<u>case</u> i <u>of</u> 1: x := sin(x); 2: x := cos(x); 3: x := exp(x); 4: x := ln(x) <u>end</u>
--	--

9.2.3. Repetitive statements

Repetitive statements specify that certain statements are to be executed repeatedly. If the number of repetitions is known beforehand, i.e. before the repetitions are started, the for statement is the appropriate construct to express this situation; otherwise the while or repeat statement should be used.

```
<repetitive statement> ::= <while statement> |
    <repeat statement> | <for statement>
```

9.2.3.1. While statements

```
<while statement> ::= while <expression> do <statement>
```

The expression controlling repetition must be of type Boolean. The statement is repeatedly executed until the expression becomes false. If its value is false at the beginning, the statement is not executed at all. The while statement

```
while B do S
```

is equivalent to

```
if B then
  begin S:
    while B do S
  end
```

Examples :

```
while a[i] <> x do i := i+1
while i>0 do
begin if odd(i) then z := z*x;
          i := i div 2;
          x := sqr(x)
end
while not eof(f) do
begin P(f↑); get(f)
end
```

9.2.3.2. Repeat statements

```
<repeat statement> ::=  
    repeat <statement> {;<statement>} until <expression>
```

The expression controlling repetition must be of type Boolean. The sequence of statements between the symbols **repeat** and **until** is repeatedly executed (and at least once) until the expression becomes true. The repeat statement

```
repeat S until B
```

is equivalent to

```
begin S;
    if not B then
        repeat S until B
    end
```

Examples :

```
repeat k := i mod j;
          i := j ;
          j := k
until j = 0
repeat P(f↑); get(f)
until eof(f)
```

9.2.3.3. For statements

The for statement indicates that a statement is to be repeatedly executed while a progression of values is assigned to a variable which is called the **control variable** of the for statement.

```

<for statement> ::= 
  for <control variable> := <for list> do <statement>
<for list> ::= <initial value> to <final value> | 
  <initial value> downto <final value>
<control variable> ::= <identifier>
<initial value> ::= <expression>
<final value> ::= <expression>

```

The control variable, the initial value, and the final value must be of the same scalar type (or subrange thereof), and must not be altered by the repeated statement. They cannot be of type real.

A for statement of the form

```
for v := e1 to e2 do S
```

is equivalent to the sequence of statements

```
v := e1; S; v := succ(v); S; ... ; v := e2; S
```

and a for statement of the form

```
for v := e1 downto e2 do S
```

is equivalent to the statement

```
v := e1; S; v := pred(S); S; ... ; v := e2; S
```

Examples:

```

for i := 2 to 100 do if a[i] > max then max := a[i]

for i := 1 to n do
for j := 1 to n do
begin x := 0 ;
  for k := 1 to n do x := x+a[i,k]*b[k,j];
  c[i,j] := x
end

for c := red to blue do Q(c)

```

9.2.4. With statements

```

<with statement> ::= with <record variable list> do <statement>
<record variable list> ::= <record variable>{.<record variable>}

```

Within the component statement of the with statement, the components (fields) of the record variable specified by the with clause can be denoted by their field identifier only, i.e. without preceding them with the denotation of the entire record variable. The with clause effectively opens the scope containing the field identifiers of the specified record variable, so that the field identifiers may occur as variable identifiers.

Example:

```
with date do
if month = 12 then
    begin month := 1; year := year + 1
    end
else month := month+1
```

is equivalent to

```
if date.month = 12 then
    begin date.month := 1; date.year := date.year+1
    end
else date.month := date.month+1
```

No assignments may be made in the qualified statement to any elements of the record variable list. However, assignments are possible to the components of these variables.

10. Procedure declarations

Procedure declarations serve to define parts of programs and to associate identifiers with them so that they can be activated by procedure statements.

```
<procedure declaration> ::= <procedure heading> <block>
<block> ::= <label declaration part>
           <constant definition part><type definition part>
           <variable declaration part>
           <procedure end function declaration part>
           <statement part>
```

The **procedure heading** specifies the identifier naming the procedure and the formal parameter identifiers (if any). The parameters are either value-, variable-, procedure-, or function parameters (cf. also 9.1.2.). Procedures and functions which are used as parameters to other procedures and functions must have value parameters only.

```
<procedure heading> ::= procedure <identifier> ; |
                     procedure <identifier> (<formal parameter section>
                           {<formal parameter section>} ) ;

<formal parameter section> ::=
  <parameter group> |
  var <parameter group>
  function <parameter group> |
  procedure <identifier> {,<identifier>}
<parameter group> ::= <identifier>{,<identifier>} :
  <type identifier>
```

A parameter group without preceding specifier implies that its constituents are value parameters.

The **label declaration part** specifies all labels which mark a

statement in the statement part.

```
<label declaration part> ::= <empty> |
    label <label> { .<label>} ;
```

The constant definition part contains all constant synonym definitions local to the procedure.

```
<constant definition part> ::= <empty> |
    const <constant definition> { ;<constant definition>} ;
```

The type definition part contains all type definitions which are local to the procedure declaration.

```
<type definition part> ::= <empty> |
    type <type definition> { ;<type definition>} ;
```

The variable declaration part contains all variable declarations local to the procedure declaration.

```
<variable declaration part> ::= <empty> |
    var <variable declaration> { ;<variable declaration>} ;
```

The procedure and function declaration part contains all procedure and function declarations local to the procedure declaration.

```
<procedure and function declaration part> ::= |
    {<procedure or function declaration> ;}
<procedure or function declaration> ::= |
    <procedure declaration> | <function declaration>
```

The statement part specifies the algorithmic actions to be executed upon an activation of the procedure by a procedure statement.

```
<statement part> ::= <compound statement>
```

All identifiers introduced in the formal parameter part, the constant definition part, the type definition part, the variable-, procedure or function declaration parts are local to the procedure declaration which is called the scope of these identifiers. They are not known outside their scope. In the case of local variables, their values are undefined at the beginning of the statement part.

The use of the procedure identifier in a procedure statement within its declaration implies recursive execution of the procedure.

Examples of procedure declarations:

```

procedure readinteger (var f: text; var x: integer) ;
var i,j: integer;
begin while f↑ = ' ' do get(f); i := 0;
      while f↑ in ['0'..'9'] do
        begin j := ord(f↑)- ord('0');
          i := 10*i + j;
          get(f)
        end;
      x := i
end;

procedure Bisect(function f: real; a,b: real; var z: real);
var m: real;
begin {assume f(a) < 0 and f(b) > 0 }
  while abs(a-b) > 1E-10*abs(a) do
    begin m := (a+b)/2.0;
      if f(m) < 0 then a := m else b := m
    end;
  z := m
end;

procedure GCD(m,n: integer; var x,y,z: integer);
var a1,a2, b1,b2,c,d,q,r: integer; {m>=0, n>0}
begin {Greatest Common Divisor x of m and n.
      Extended Euclid's Algorithm}
  a1 := 0; a2 := 1; b1 :=1; b2 := 0;
  c := m; d := n;
  while d <> 0 do
    begin {a1*m + b1*n = d, a2*m + b2*n = c,
          gcd(c,d) = gcd(m,n)}
      q := c div d; r := c mod d ;
      a2 := a2 - q*a1; b2 := b2 - q*b1;
      c := d; d := r;
      r := a1; a1 := a2; a2 := r;
      r := b1; b1 := b2; b2 := r
    end;
  x := c; y := a2; z := b2
  { x = gcd(m,n) = y*m + z*n }
end;

```

10.1. Standard procedures

Standard procedures are supposed to be predeclared in every implementation of Pascal. Any implementation may feature additional predeclared procedures. Since they are, as all standard quantities, assumed as declared in a scope surrounding the program, no conflict arises from a declaration redefining the same identifier within the program. The standard procedures are listed and explained below.

10.1.1. File handling procedures

put(f) appends the value of the buffer variable f^\dagger to the file f. The effect is defined only if prior to execution the predicate $\text{eof}(f)$ is true. $\text{eof}(f)$ remains true, and the value of f^\dagger becomes undefined.

get(f) advances the current file position (read/write head) to the next component, and assigns the value of this component to the buffer variable f^\dagger . If no next component exists, then $\text{eof}(f)$ becomes true, and the value of f^\dagger is not defined. The effect of $\text{get}(f)$ is defined only if $\text{eof}(f) = \text{false}$ prior to its execution. (see 11.1.2)

reset(f) resets the current file position to its beginning and assigns to the buffer variable f^\dagger the value of the first element of f. $\text{eof}(f)$ becomes false, if f is not empty; otherwise f^\dagger is not defined, and $\text{eof}(f)$ remains true.

rewrite(f) discards the current value of f such that a new file may be generated. $\text{eof}(f)$ becomes true.

Concerning the textfile procedures `read`, `write`, `readln`, `writeln`, and `page`, see Chapter 12.

10.1.2. Dynamic allocation procedure

new(p) allocates a new variable v and assigns the pointer to v to the pointer variable p. If the type of v is a record type with variants, the form

new(p,t₁,...,t_n) can be used to allocate a variable of the variant with tag field values t₁,...,t_n.

dispose(p) and **dispose(p,t₁,...,t_n)** can be used to indicate that storage occupied by the variable referenced by the pointer p is no longer needed. (Implementations may use this information to retrieve storage, or they may ignore it.)

10.1.3. Data transfer procedures

Let the variables a and z be declared by

```
a: array [m..n] of T
z: packed array [u..v] of T
```

where n-m >= v-u. Then the statement `pack(a,i,z)` means

```
for j := u to v do z[j] := a[j-u+i]
```

and the statement `unpack(z,a,i)` means

```
for j := u to v do a[j-u+i] := z[j]
```

where j denotes an auxiliary variable not occurring elsewhere in the program.

11. Function declarations

Function declarations serve to define parts of the program which compute a scalar value or a pointer value. Functions are activated by the evaluation of a function designator (cf. 8.2) which is a constituent of an expression.

```
<function declaration> ::= <function heading><block>
```

The function heading specifies the identifier naming the function, the formal parameters of the function, and the type of the function.

```
<function heading> ::= function <identifier>:<result type>; |  
    function <identifier> (<formal parameter section>  
    {<formal parameter section>}) : <result type> ;  
<result type> ::= <type identifier>
```

The type of the function must be a scalar, subrange, or pointer type. Within the function declaration there must be at least one assignment statement assigning a value to the function identifier. This assignment determines the result of the function. Occurrence of the function identifier in a function designator within its declaration implies recursive execution of the function.

Examples:

```
function Sqrt(x: real): real;  
var x0,x1: real;  
begin x1 := x; {x>1, Newton's method}  
    repeat x0 := x1; x1 := (x0+ x/x0)*0.5  
    until abs(x1-x0) < eps*x1 ;  
    Sqrt := x0  
end
```

```
function Max(a: vector; n: integer): real;  
var x: real; i: integer;  
begin x := a[1];  
    for i := 2 to n do  
        begin {x = max(a[1],...,a[i-1])}  
            if x < a[i] then x := a[i]  
        end;  
        {x = max(a[1],...,a[n])}  
    Max := x  
end
```

```

function GCD(m,n: integer):integer;
begin if n=0 then GCD := m else GCD := GCD(n,m mod n)
end

function Power(x: real; y: integer): real : {y >= 0}
var w,z: real; i: integer;
begin w := x; z := 1; i := y;
  while i > 0 do
    begin {z*(w**i) = x ** y}
      if odd(i) then z := z*w;
      i := i div 2;
      w := sqr(w)
    end;
    {z = x**y}
  Power := z
end

```

11.1. Standard functions

Standard functions are supposed to be predeclared in every implementation of Pascal. Any implementation may feature additional predeclared functions (cf. also 10.1).

The standard functions are listed and explained below:

11.1.1. Arithmetic functions

<code>abs(x)</code>	computes the absolute value of <code>x</code> . The type of <code>x</code> must be either <code>real</code> or <code>integer</code> , and the type of the result is the type of <code>x</code> .
<code>sqr(x)</code>	computes <code>x**2</code> . The type of <code>x</code> must be either <code>real</code> or <code>integer</code> , and the type of the result is the type of <code>x</code> .
<code>sin(x)</code>	
<code>cos(x)</code>	
<code>exp(x)</code>	the type of <code>x</code> must be either <code>real</code> or <code>integer</code> , and
<code>ln(x)</code>	the type of the result is <code>real</code> .
<code>sqrt(x)</code>	
<code>arctan(x)</code>	

11.1.2. Predicates

<code>odd(x)</code>	the type of <code>x</code> must be <code>integer</code> , and the result is true, if <code>x</code> is odd, and false otherwise.
<code>eof(f)</code>	<code>eof(f)</code> indicates, whether the file <code>f</code> is in the end-of-file status.
<code>eoln(f)</code>	indicates the end of a line in a textfile (see chapter 12).

11.1.3. Transfer functions

`trunc(x)` the real value x is truncated to its integral part.

`round(x)` the real argument x is rounded to the nearest integer.

`ord(x)` x must be of a scalar type (including Boolean and char), and the result (of type integer) is the ordinal number of the value x in the set defined by the type of x .

`chr(x)` x must be of type integer, and the result (of type char) is the character whose ordinal number is x (if it exists).

11.1.4. Further standard functions

`succ(x)` x is of any scalar or subrange type, and the result is the successor value of x (if it exists).

`pred(x)` x is of any scalar or subrange type, and the result is the predecessor value of x (if it exists).

12. Input and output

The basis of legible input and output are textfiles (cf. 6.2.4) that are passed as program parameters (cf. 13) to a PASCAL program and in its environment represent some input or output device such as a terminal, a card reader, or a line printer. In order to facilitate the handling of textfiles, the four standard procedures `read`, `write`, `readln`, and `writeln` are introduced in addition to `get` and `put`. They can be applied to textfiles only; however, these textfiles must not necessarily represent input/output devices, but can also be local files. The new procedures are used with a non-standard syntax for their parameter lists, allowing, among other things, for a variable number of parameters. Moreover, the parameters must not necessarily be of type char, but may also be of certain other types, in which case the data transfer is accompanied by an implicit data conversion operation. If the first parameter is a file variable, then this is the file to be read or written. Otherwise, the standard files `input` and `output` are automatically assumed as default values in the cases of reading and writing respectively. These two files are predeclared as

```
var input, output: text
```

Textfiles represent a special case among file types insofar as texts are substructured into lines by so-called line markers (cf. 6.2.4.). If, upon reading a textfile f , the file position

is advanced to a line marker, that is past the last character of a line, then the value of the buffer variable $f \uparrow$ becomes a blank, and the standard function `eoln(f)` (`end of line`) yields the value true. Advancing the file position once more assigns to $f \uparrow$ the first character of the next line, and `eoln(f)` yields false (unless the next line consists of 0 characters). Line markers, not being elements of type `char`, can only be generated by the procedure `writeln`.

12.1. The procedure read

The following rules hold for the procedure `read`; f denotes a textfile and $v_1 \dots v_n$ denote variables of the types `char`, `integer` (or subrange of `integer`), or `real`.

1. `read(v_1, ..., v_n)` is equivalent to `read(input, v_1, ..., v_n)`
2. `read(f, v_1, ..., v_n)` is equivalent to `read(f, v_1); ...; read(f, v_n)`
3. if v is a variable of type `char`, then `read(f, v)` is equivalent to $v := f \uparrow; get(f)$
4. if v is a variable of type `integer` (or subrange of `integer`) or `real`, then `read(f, v)` implies the reading from f of a sequence of characters which form a number according to the syntax of PASCAL (cf. 4.) and the assignment of that number to v . Preceding blanks and line markers are skipped.

12.2. The procedure readln

1. `readln(v_1, ..., v_n)` is equivalent to `readln(input, v_1, ..., v_n)`
2. `readln(f, v_1, ..., v_n)` is equivalent to

$$\text{read}(f, v_1, \dots, v_n); \text{readln}(f)$$
3. `readln(f)` is equivalent to

$$\text{while not eoln}(f) \text{ do get}(f); \\ \text{get}(f)$$

`Readln` is used to read and subsequently skip to the beginning of the next line.

12.3. The procedure write

The following rules hold for the procedure `write`; f denotes a textfile, $p_1 \dots p_n$ denote so-called write-parameters, e denotes an expression, m and n denote expressions of type `integer`.

1. `write(p_1, ..., p_n)` is equivalent to `write(output, p_1, ..., p_n)`

2. `write(f,p1,...,pn)` is equivalent to

```
    write(f,p1); ... ; write(f,pn)
```

3. The write-parameters p have the following forms:

```
    e:m      e:m:n      e
```

e represents the value to be "written" on the file f, and m and n are so-called field width parameters. If the value e, which is either a number, a character, a Boolean value, or a string requires less than m characters for its representation, then an adequate number of blanks is issued such that exactly m characters are written. If m is omitted, an implementation-defined default value will be assumed. The form with the width parameter n is applicable only if e is of type real (see rule 6).

4. if e is of type char, then

```
    write(f, e:m) is equivalent to
    f↑ := ' ' ; put(f);      (repeated m-1 times)
    f↑ := e ; put(f)
```

Note: the default value for m is in this case 1.

5. If e is of type integer (or a subrange of integer), then the decimal representation of the number e will be written on the file f, preceded by an appropriate number of blanks as specified by m.

6. If e is of type real, a decimal representation of the number e is written on the file f, preceded by an appropriate number of blanks as specified by m. If the parameter n is missing (see rule 3), a floating-point representation consisting of a coefficient and a scale factor will be chosen. Otherwise a fixed-point representation with n digits after the decimal point is obtained.

7. if e is of type Boolean, then the words TRUE or FALSE are written on the file f, preceded by an appropriate number of blanks as specified by m.

8. if e is an (packed) array of characters, then the string e is written on the file f.

12.4. The procedure writeln

1. `writeln(p1,...,pn)` is equivalent to `writeln(output,p1,...,pn)`

2. `writeln(f,p1,...,pn)` is equivalent to `write(f,p1,...,pn); writeln(f)`

3. `writeln(f)` appends a line marker (cf.6.2.4) to the file f.

12.5. Additional procedures

`page(f)` causes skipping to the top of a new page, when the textfile `f` is printed.

13. Programs

A Pascal program has the form of a procedure declaration except for its heading.

```
<program> ::= <program heading> <block> .
<program heading> ::= 
    program <identifier> (<program parameters>) ;
<program parameters> ::= <identifier> {, <identifier>} }
```

The identifier following the symbol `program` is the program name; it has no further significance inside the program. The program parameters denote entities that exist outside the program, and through which the program communicates with its environment. These entities (usually files) are called `external`, and must be declared in the block which constitutes the program like ordinary local variables.

The two standard files `input` and `output` must not be declared (cf. 12), but have to be listed as parameters in the program heading, if they are used. The initialising statements `reset(input)` and `rewrite(output)` are automatically generated and must not be specified by the programmer.

Examples :

```
program copy(f,g);
var f,g: file of real;
begin reset(f); rewrite(g);
  while not eof(f) do
    begin g^ := f^; put(g); get(f)
    end
  end.

program copytext(input,output);
var ch: char;
begin
  while not eof(input) do
    begin
      while not eoln(input) do
        begin read(ch); write(ch)
        end;
      readln; writeln
    end
  end
end.
```

14. A standard for implementation and program interchange

A primary motivation for the development of PASCAL was the need for a powerful and flexible language that could be reasonably efficiently implemented on most computers. Its features were to be defined without reference to any particular machine in order to facilitate the interchange of programs. The following set of proposed restrictions is designed as a guideline for implementors and for programmers who anticipate that their programs be used on different computers. The purpose of these standards is to increase the likelihood that different implementations will be compatible, and that programs are transferable from one installation to another.

1. Identifiers denoting distinct objects must differ over their first 8 characters.
2. Labels consist of at most 4 digits.
3. The implementor may set a limit to the size of a base type over which a set can be defined. (Consequently, a bit pattern representation may reasonably be used for sets.)
4. The first character on each line of printfiles may be interpreted as a printer control character with the following meanings:
 blank : single spacing
 '0' : double spacing
 '1' : print on top of next page

Representations of PASCAL in terms of available character sets should obey the following rules:

5. Word symbols - such as `begin`, `end`, etc. - are written as a sequence of letters (without surrounding escape characters). They may not be used as identifiers.
6. Blanks, ends of lines, and comments are considered as separators. An arbitrary number of separators may occur between any two consecutive PASCAL symbols with the following restriction: no separators must occur within identifiers, numbers, and word symbols.
7. At least one separator must occur between any pair of consecutive identifiers, numbers, or word symbols.

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