

9

TIME, SPEED AND DISTANCE

It is sure and certain that it is one of the most important chapter, which includes various fundamental and logical concepts and therefore most of the problems are complex in their nature. Every year 4-6 problems are generally asked in CAT. Besides CAT almost every aptitude exam contains the questions pertaining to the concepts of TSD.

This chapter includes the following :

- (a) Motion in a straight line
- (b) Circular motion and races
- (c) Problems based on trains, boats, river and clocks etc.

CONCEPT OF MOTION

When a body moves from a point A to another point B at a distance of D , then it requires some time (T) to cover a distance (D) with a particular speed (S).

The relation between T , S and D is as follows:

$$T \times S = D$$

i.e., Time \times Speed = Distance

Therefore, when D is constant,

$$T \propto \frac{1}{S}$$

and when T is constant,

$$D \propto S$$

and when S is constant,

$$D \propto T$$

NOTE This relation of proportionality is very important.

Formulae : Distance = Speed \times Time

EXAMPLE 1 Abhishek drives his bike at the speed of 150 km/h. What is the distance covered by him in 3 hours.

SOLUTION $D = S \times T = 150 \times 3 = 450$ km

EXAMPLE 2 Udai travels half of his journey by train at the speed of 120 km/h and rest half by car at 80 km/h. What is the average speed?

$$\text{Speed} = \frac{\text{Distance}}{\text{Time}}$$

$$\text{Time} = \frac{\text{Distance}}{\text{Speed}}$$

NOTE To solve the problem, all the units involved in the calculation must be uniform i.e., either all of them be in metres and seconds or in kilometres and hours etc.

Conversion of unit:

$$1 \text{ km/h} = \frac{5}{18} \text{ m/s}$$

$$1 \text{ m/s} = \frac{18}{5} \text{ km/h}$$

$$[1 \text{ km} = 1000 \text{ m}, 1 \text{ h} = 60 \text{ min}, 1 \text{ min} = 60 \text{ s}]$$

HINT Try to find these relations by unitary method.

$$1 \text{ mile} = 1609.30 \text{ m} = 1.6093 \text{ km}$$

$$\text{and} \quad 1 \text{ km} = 0.621 \text{ mile}$$

$$1 \text{ yard} = 0.9144 \text{ m}$$

$$\text{and} \quad 1 \text{ m} = 1.0936 \text{ yards}$$

$$\text{and} \quad 1 \text{ m} = 39.4 \text{ inches}$$

$$\text{Average speed} = \frac{\text{Total distance}}{\text{Total time taken}}$$

When distances are equal :

$$\text{Average speed} = \frac{2xy}{x + y} \quad (\text{speeds } x, y)$$

$$\text{and} \quad \text{Average speed} = \frac{3xyz}{xy + yz + zx} \quad (\text{speeds } x, y, z)$$

SOLUTION Let the total distance be $2D$ km, then

Total time = Time taken by train + Time taken by car

$$= \frac{D}{120} + \frac{D}{80}$$

$$\therefore \text{Average speed} = \frac{2D}{\frac{D}{120} + \frac{D}{80}}$$

EXAMPLE 7 Shweta when increases her speed from 24 km/h to 30 km/h she takes one hour less than the usual time to cover a certain distance. What is the distance usually covered by Shweta?

- (a) 160 km (b) 240 km (c) 120 km (d) 90 km

SOLUTION Let the original time be t hours, then

$$24t = 30 \times (t - 1) = D \quad (\text{distance})$$

then $t = 5$

$$\therefore \text{Distance} = 24 \times 5 = 120 \text{ km}$$

Alternatively: Go through options.

$$\begin{array}{l} \frac{120}{24} = 5 \text{ h} \\ \frac{120}{30} = 4 \text{ h} \end{array} \quad \begin{array}{l} \text{1 hour less} \\ \text{ } \end{array}$$

Hence, the option (c) is correct.

Alternatively: Since distance (D) is constant.

$$\text{Therefore, } D = S_1 \times t_1 = S_2 \times t_2$$

It means here we can apply product constancy

$$\begin{array}{ll} \text{Speed} & \text{Time} \\ \frac{1}{4} \uparrow & \frac{1}{5} \downarrow \\ & = 1 \text{ hour} \end{array}$$

$$\therefore \text{Original time taken} = 5 \times 1 = 5 \text{ hours}$$

$$\begin{aligned} \text{Therefore, Distance} &= \text{Original speed} \times \text{Original time} \\ &= 24 \times 5 = 120 \text{ km} \end{aligned}$$

NOTE In the given exercise or in the whole chapter you have to solve maximum problems through product constancy concept described in the chapter of ratio proportion and variation. Solving through product constancy gives faster results.

Alternatively: Let the distance be D , then

$$\frac{D}{24} - \frac{D}{30} = 1$$

$$\Rightarrow D = 120 \text{ km}$$

EXAMPLE 8 Kriplani goes to school at 20 km/h and reaches the school 4 minutes late. Next time, she goes at 25 km/h and reaches the school 2 minutes earlier than the scheduled time. What is the distance of her school?

SOLUTION Increase in speed = 5 km/h

$$\text{Decrease in time} = 6 \text{ min} (4 + 2)$$

By product constancy :

$$\begin{array}{ll} \text{Speed} & \text{Time} \\ \frac{1}{4} \uparrow & \frac{1}{5} \downarrow \\ 4 & 5 \end{array} = 6 \text{ min}$$

$$\text{It means original time} = 30 \text{ min} \quad \left(\because \frac{x}{5} = 6 \Rightarrow x = 30 \right)$$

$$\begin{aligned} \therefore \text{Total distance} &= \text{Original speed} \times \text{Original time} \\ &= 20 \times \frac{30}{60} = 10 \text{ km} \end{aligned}$$

EXAMPLE 9 Amit covers a certain distance with his own speed, but when he reduces his speed by 10 km/h his time duration for the journey increases by 40 hours, while if he increases his speed by 5 km/h from his original speed he takes 10 hours less than the original time taken. Find the distance covered by him.

SOLUTION

$$\left. \begin{array}{l} S \\ -10 \end{array} \right\} \begin{array}{l} T \\ +40 \end{array} \quad \left. \begin{array}{l} 40S - 10T = -400 \\ -10S + 5T = -50 \end{array} \right\} \dots (i)$$

$$\left. \begin{array}{l} S \\ +5 \end{array} \right\} \begin{array}{l} T \\ -10 \end{array} \quad \left. \begin{array}{l} -10S + 5T = -50 \\ 5S - T = 10 \end{array} \right\} \dots (ii)$$

Solving eq. (i) and (ii), we get

$$S = 25 \text{ and } T = 60$$

$$\begin{aligned} \therefore \text{Distance} (D) &= S \times T \\ &= 25 \times 60 = 1500 \text{ km} \end{aligned}$$

where $D \rightarrow$ Distance, $S \rightarrow$ Speed, $T \rightarrow$ Time

‘+’ means increase in value.

and ‘-’ means decrease in value.

Alternatively: Let distance be x km and usual speed be y km/h.

$$\begin{aligned} \frac{x}{(y-10)} - \frac{x}{y} &= 40 \\ \Rightarrow x \left[\frac{10}{y(y-10)} \right] &= 40 \\ \Rightarrow x &= 4y(y-10) \quad \dots (i) \\ \text{and } \frac{x}{y} - \frac{x}{(y+5)} &= 10 \\ \Rightarrow x &= 2y(y+5) \quad \dots (ii) \\ \text{from eq. (i) and (ii)} & \\ 4y(y-10) &= 2y(y+5) \\ 2y-20 &= y+5 \\ y &= 25 \text{ km/h} \\ \therefore x &= 1500 \text{ km} \end{aligned}$$

EXAMPLE 10 A train met with an accident 60 km away from Anantpur station. It completed the remaining journey at $\frac{5}{6}$ th of the

previous speed and reached the Baramula station 1 hour 12 min late. Had the accident taken place 60 km further, it would have been only 1 hour late.

(a) What is the normal speed of the train?

(b) What is the distance between Anantpur and Baramula?

SOLUTION **Case I.** Since the speed is decreased by $\frac{1}{6}$. So, the time will be increased by $1/5$, which is equal to 1 hour 12 minutes.

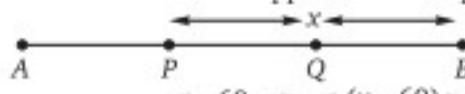
It means the normal time required for this remaining part (x) of the journey is $5 \times 72 \text{ min} = 360 \text{ min} = 6 \text{ h}$.

($\because 1 \text{ h } 12 \text{ min} = 72 \text{ min}$)



P is the place of accident.

Case II. When accident is supposed to be happened at Q .



Since, the speed is decreased by $\frac{1}{6}$, hence, the time will be increased by $\frac{1}{5}$, which is equal to 1 hour, hence the normal time required for this remaining part ($x-60$) of journey = $5 \times 1 = 5$ hours.

Thus, it is clear that when the train runs 60 km of its normal speed it takes 1 hour less, which implies that in 1 hour the train can run 60 km with its normal speed. Thus, the normal speed of the train is 60 km/h.

(b) Since the train requires 6 hours at its normal speed of 60 km/h for the x km. Hence,

$$x = 6 \times 60 = 360 \text{ km}$$

Thus, the total distance = Distance travelled before accident + Distance travelled after accident
 $= 60 \times 1 + 60 \times 6 = 420 \text{ km}$

EXAMPLE 11 *A and B started simultaneously towards each other from P and Q respectively. The distance between P and Q is 600 km and the ratio of speeds of A is to B is 5 : 7. If they meet at a point M:*

RELATIVE MOTION WITH TWO OR MORE BODIES

(i) When two bodies move in the same direction: If the speeds of the two bodies A and B be S_A and S_B , then their relative speed = $S_A - S_B$ or $S_B - S_A$ i.e., in the same direction the relative speed or effective speed between two bodies is the difference of their speeds. (The difference is always considered

EXAMPLE 12 *The distance between two places P and Q is 700 km. Two persons A and B started towards Q and P from P and Q simultaneously. The speed of A is 30 km/h and speed of B is 40 km/h. They meet at a point M which lies on the way from P to Q.*

- How long will they take to meet each other at M?
- What is the ratio of $PM : MQ$?
- What is the distance MQ ?
- What is the extra time needed by A to reach at Q than to reach at P by B?
- What is the ratio of time taken by A and B to reach their respective destinations after meeting at M?
- In how many hours will they be separated by only 560 km before meeting each other.
- How long will it take to separate them by 280 km from each other when they cross M (time to be considered after their meeting)?

SOLUTION



- (i) Since, they are coming towards each other from opposite ends, therefore the relative speed will be the sum of their speeds = $30 + 40 = 70 \text{ km/h}$.

Thus, the required time to meet at M

$$\begin{aligned} &= \text{Time required to cover 700 km (combined)} \\ &= \frac{700}{70} = 10 \text{ h} \end{aligned}$$

Thus in 10 hours they will meet each other at M.

- (ii) The ratio of their distances covered to meet at M

$$= \text{Ratio of their speeds} = 3 : 4$$

(Since, time is constant i.e., same for each)

Thus $PM : MQ = 3 : 4$

$$(iii) MQ = \frac{4}{7} \times 700 = 400 \text{ km}$$

(i) Find the ratio of $PM : QM$.

(ii) Find the distance PM .

SOLUTION (i) Since the time is constant so, the distance covered by A and B is directly proportional to the speeds of A and B .

Hence, $PM : QM = 5 : 7$

(ii) Since, the ratio of their speeds (or their distances covered) is $5 : 7$. Hence, A will cover $\frac{5}{12}$ of the total length.

$$\therefore PM = \frac{5}{12} \times 600 = 250 \text{ km}$$

$$(\text{Similarly } QM = \frac{7}{12} \times 600 = 350 \text{ km})$$

as positive)

(ii) When two bodies move in the opposite direction:

If the speeds of the two bodies A and B be S_A and S_B , then their relative speed = $S_A + S_B$.

i.e., in the opposite direction the relative speed or effective speed between two bodies is the sum of their speeds.

$$(iv) \text{ Time required by } A \text{ to reach at } Q = \frac{700}{30} = \frac{70}{3} \text{ h}$$

$$\text{Time required by } B \text{ to reach at } P = \frac{700}{40} = \frac{70}{4} \text{ h}$$

$$\begin{aligned} \therefore \text{Extra time required by } A &= \frac{70}{3} - \frac{70}{4} \\ &= 70 \times \frac{1}{12} = 5 \text{ h } 50 \text{ min} \end{aligned}$$

$$(v) \text{ Time required by } A \text{ to cover } MQ = \frac{400}{30}$$

$$\text{and time required by } B \text{ to cover } MP = \frac{300}{40}$$

$$\therefore \text{Required ratio} = \frac{400/30}{300/40} = \frac{16}{9}$$

Remember: If speed of A is S_A and speed of B is S_B and A takes t_A time to cover MQ and B takes t_B time to cover MP , then

$$\frac{S_A}{S_B} = \sqrt{\frac{t_B}{t_A}}$$

(vi) It means they have to cover $(700 - 560) = 140 \text{ km}$. Thus, the required time to cover 140 km distance

$$= \frac{140}{70} = 2 \text{ h}$$

(vii) Since in each hour they separate by 70 km from each other. Hence, to separate by 280 km, time required

$$= \frac{280}{70} = 4 \text{ h}$$

EXAMPLE 13 *Two places P and Q are 800 km apart from each other. Two persons start from P towards Q at an interval of 2 hours. Whereas A leaves P for Q before B. The speeds of A and B are 40 km/h and 60 km/h respectively. B overtakes (or catches or meets) A at M, which is on the way from P to Q.*

- (i) How long will B take to overtake?
- (ii) What is the distance from P, where B overtakes A (i.e., PM)?
- (iii) What is the ratio of time taken by A and B to meet at M?
- (iv) What is the extra time required by A to reach at Q?
- (v) How many hours late A will reach at Q than that of B?
- (vi) After how many hours A and B will be separated by 50 km before M, when both are moving?
- (vii) How many hours does B require to advance himself, by 100 km, in comparison to A?

SOLUTION

- (i) Since A moves 2 hours earlier than B at the speed of 40 km/h, so in 2 hours A will cover 80 km. Thus A will be 80 km away from B.

Now, since they are moving in the same direction therefore their relative speed will be $(60 - 40) = 20$ km/h i.e., with respect to A, B moves at 20 km/h. It means either they reduce (or create) the difference of 20 km in each hour between themselves.

Thus, the required time to overtake (or reduce the difference upto zero from 80 km)

$$= \frac{\text{Distance advanced}}{\text{Relative speed}} = \frac{80}{20} = 4 \text{ h}$$

- (ii) The distance between P and M

$$= (\text{Time required to overtake} \times \text{Speed of the faster body}) \\ = 4 \times 60 = 240 \text{ km}$$

Since, B has to move for 4 hours at 60 km/h. Hence, distance covered = 240 km.

- (iii) Time taken by B to reach at M = 4 h

TO AND FRO MOTION IN A STRAIGHT LINE

This concept is just the extension of the previous concepts of relative motion between more than one dynamic (or moving) bodies.

(a) When two bodies start moving towards each other

- (i) To meet each other they cover the distances in the ratio of their individual speeds.
- (ii) If the initial distance (or gaping) between two bodies A and B is D , then A and B together have to cover D unit of distance for the first meeting.
- (iii) For the next number of meeting (e.g., second, third, fourth meeting and so on) both A and B together have to cover $2D$ distance more from the previous meeting i.e., to meet for the fourth time they have to cover together $D + (3 \times 2D) = 7D$ unit of distances. Similarly for seventh meeting they have to cover together $D + (6 \times 2D) = 13D$ units of distance. Thus for each subsequent meeting they have to cover $2D$ distance extra from the previous one.

Time taken by A to reach at M = $(4 + 2) = 6$ h

Thus, the ratio of time taken by A and B = $6 : 4 = 3 : 2$
(Since, A has left 2 hours earlier)

(iv) Time taken by A to reach at Q = $\frac{800}{40} = 20$ h

Time taken by B to reach at Q = $\frac{800}{60} = 13$ h 20 min

Hence, A takes 6 hrs 40 min extra to reach at Q.

(v) Since, A leaves 2 hrs earlier, thus he will reach at Q only 4 hours 40 min late.

Since, A takes 6 hrs 40 min extra to reach at Q.

(vi) When B starts to move towards Q the difference between A and B is 80 km.

The required difference between A and B = 50 km
Hence, they have to reduce it by 30 km.

$$\text{Thus, the required time} = \frac{(80 - 50)}{20} = 1.5 \text{ h} \\ = 1 \text{ h } 30 \text{ min}$$

Thus, after $3/2$ hrs A will be only 50 metres ahead of B.

(vii) When B starts to follow A (towards Q) A was 80 km ahead of B. Also B wants to overtake A and further go ahead of A by 100 km. Thus, the net difference (required) = 180 km.

∴ Required time

$$= \frac{(\text{Distance advanced} + \text{Required difference})}{\text{Relative speed}}$$

$$= \frac{80 + 100}{20} = \frac{180}{20} = 9 \text{ h}$$

Thus, after 9 hrs (when B starts moving) B will be 100 km ahead of A i.e., they will be separated by 100 km from each other after crossing M.

NOTE Individually they will cover the distances in the ratio of their speeds for any number of meeting.
Thus, the total distance covered for the n^{th} meeting = $(2n - 1)D$.

(b) When two bodies start moving towards the same direction

- (i) For the first meeting after they start to move they have to cover $2D$ distance, if the distance between two particular points (or places) be D unit. Since, the faster body reaches the next (or opposite) end first than the slower body and the faster body starts returning before the slower body reaches the same opposite end and thus the two bodies meet somewhere between the two ends covering individually the distances in their respective speeds.

- (ii) For every subsequent meeting they have to cover together $2D$ unit distance more from the previous meeting.

Thus, for n^{th} meeting they have to cover together $(n \times 2D)$ unit of distance.

- (iii) At any point of time the distances covered by the bodies will be equal to the ratio of their speeds.

EXAMPLE 14 The distance between P and Q is 100 m and the speeds of A and B are 20 m/s and 30 m/s respectively. Initially A and B are at P . They move between P and Q . Calculate:

- the distance covered by A in first meeting.
- the time required for the second meeting.
- the distance covered by B to meet for the third time.
- the ratio of distances covered by A and B till the fourth meeting.
- the distance between P and the place of fifth meeting.
- the distance between Q and the point of third meeting.

SOLUTION	Meeting	Total distance covered by A and B together	Distance covered by A	Distance covered by B	Point of meeting from P	Point of meeting from Q	Time (in second)
	1 st	200 m	80 m	120 m	80 m	20 m	4
	2 nd	400 m	160 m	240 m	40 m	60 m	8
	3 rd	600 m	240 m	360 m	40 m	60 m	12
	4 th	800 m	320 m	480 m	80 m	20 m	16
	5 th	1000 m	400 m	600 m	0 m (at P)	100 m	20

- The distance covered by A in the first meeting = 80 m
- Time required for the second meeting = $\frac{400}{50} = 8$ s
- The distance covered by B for the third time meeting = $12 \times 30 = 360$ m
- It is always (for any moment, after the starting of movement) will be in the ratio of their respective speeds.
So, the required ratio of distances covered by A and B = $20 : 30 = 2 : 3$ i.e.,
$$A : B = 20 : 30 = 2 : 3$$
- Since for the fifth meeting they have to cover $50 \times 20 = 1000$ m.
- 60 m.

EXAMPLE 15 The distance between two points P and Q is 100 m. A is initially at P and B is at Q . The speeds of A and B is 20 m/s and 30 m/s. They move between P and Q to and fro :

- Find the time required for the first meeting.
- Distance covered by A till the third meeting.
- Distance covered by B till the fifth meeting.
- The distance between P and the place of fourth meeting.
- The distance between Q and the place of fifth meeting.
- The ratio of distances covered by each one till the third meeting.

SOLUTION	No. of meeting	Distance covered by A and B together	Time (in second)	Distance covered by A	Distance covered by B	Distance between P and point of meeting	Distance between Q and point of meeting
	1 st	100 m	2	40 m	60 m	40 m	60 m
	2 nd	300 m	6	120 m	180 m	80 m	20 m
	3 rd	500 m	10	200 m	300 m	at P	at P
	4 th	700 m	14	280 m	420 m	80 m	20 m
	5 th	900 m	18	360 m	540 m	40 m	60 m

- 2 second $\left(\text{Time} = \frac{100}{50} = 2 \right)$
- 200 m (Distance = Speed \times Time = $20 \times 10 = 200$ m)
- 540 m ($D = 18 \times 30 = 540$ m)
- 80 m
- 60 m
- 2 : 3 always equal to the ratio of respective speeds.

EXAMPLE 16 A and B are two friends. A lives at a place P and B lives at another place Q . Everyday A goes to Q to meet B at 120 km/h. Thus, he takes 3 hours. On a particular day B started to meet A so he moved towards P . On that day A took only 2 hours to meet B on the way instead at Q .

- What is the ratio of speeds of A is to B ?
- What is the speed of B ?

SOLUTION Distance between P and Q = $120 \times 3 = 360$ km

Let the speed of B be S_B , then

$$\text{Time} = \frac{\text{Distance}}{\text{Speed}}$$

$$2 = \frac{360}{(120 + S_B)}$$

$$\Rightarrow S_B = 60 \text{ km/h}$$

Here, A and B are moving towards each other. So, the relative speed will be the sum of the speeds of A and B both.

Therefore, ratio of speeds of $A : B = 2 : 1$.

(i) $2 : 1$

(ii) 60 km/h

NOTE In this case ratio of speeds of

$$A : B = \frac{\text{Actual time required when } B \text{ is also moving}}{\text{Time difference when } B \text{ is also moving}}$$

$$= \frac{(3 - 1)}{1} = \frac{2}{1}$$

EXAMPLE 17 A lives at P and B lives at Q . A usually goes to meet B at Q . He covers the distance in 3 hours at 150 km/h . On a particular day B started moving away from A . While A was moving towards Q thus A took total 5 hours to meet B .

(i) What is the speed of B ?

(ii) What is the ratio of speeds of $A : B$?

SOLUTION

$$\text{Distance} = 3 \times 150 = 450 \text{ km}$$

$$\text{Time} = \frac{\text{Distance}}{\text{Relative speed}}$$

$$5 = \frac{450}{(150 - S_B)} \quad S_B \rightarrow \text{Speed of } B$$

$$\Rightarrow S_B = 60 \text{ km/h}$$

$$\text{Ratio of speeds of } A : B = \frac{150}{60} = \frac{5}{2} = 5 : 2$$

- (i) 60 km/h (ii) $5 : 2$

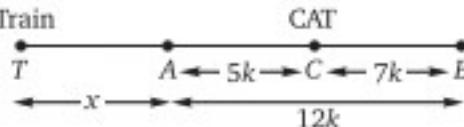
In this case ratio of speeds of

$$A : B = \frac{\text{Actual time required when } B \text{ is also moving}}{\text{Time difference}}$$

$$= \frac{5}{2}$$

EXAMPLE 18 A train approaches a tunnel AB . Inside the tunnel a cat located at a point $i.e.$, $\frac{5}{12}$ of the distance AB measured from the entrance A . When the train whistles, the cat runs. If the cat moves to the entrance of the tunnel A , the train catches the cat exactly at the entrance. If the cat moves to the exit B , the train catches the cat at exactly the exit. The speed of the train is greater than the speed of the cat by what order?

SOLUTION



Let the speed of train be u and the speed of cat be v and train whistles at a point T , x km away from A , then

$$\frac{u}{v} = \frac{x}{5k} = \frac{x + 12k}{7k}$$

$$\Rightarrow 7x = 5(x + 12k)$$

$$\Rightarrow \frac{x}{k} = \frac{30}{1}$$

$$\therefore \frac{u}{v} = \frac{30}{5 \times 1} = \frac{6}{1}$$

$$\text{Alternatively: } \frac{u}{v} = \frac{7k + 5k}{7k - 5k} = \frac{6}{1}$$

NOTE Since time is constant, therefore distances covered by train and cat will be in the ratio of their respective speeds.

CONCEPT BASED ON TRAINS

- When two trains (or bodies) are moving in opposite direction, their relative speed will be equal to the sum of their individual speeds.
- When two trains are moving in the same direction their relative speed will be equal to the difference of their speeds.
- Distance to be covered to cross each other is always equal to the sum of their individual lengths.
- Distance to be covered such as bridge, platform etc.,

is always equal to the sum of the length of train and the length of the particular object such as bridge, platform etc.

- Distance to be covered such as pole, man, tree etc, is always equal to the length of the train only.
- If a man is travelling in a train, then this man has to cover the distance to cross another train is equal to the length of the train which is passing or crossing him. In this case the relative speed of both the trains will be considered.

EXAMPLE 19 A train crosses a tree in 10 seconds. If the length of the train be 150 m , then find the speed of the train.

SOLUTION

$$\text{Distance} = \text{Length of train}$$

$$= \text{Speed of train} \times \text{Time}$$

$$150 = \text{Speed} \times 10$$

$$\Rightarrow \text{Speed} = 15 \text{ m/s}$$

$$\text{Speed} = 15 \times \frac{18}{5} = 54 \text{ km/h}$$

NOTE A train starts to cross a stationary thin object (of inconsiderable thickness) when the engine of the train meets the object and it completes the crossing when the last wagon (or backend) of the train just crosses the object.

EXAMPLE 20 A train crosses a man coming from the opposite direction in 7.5 seconds. If the speed of man be 10 m/s and speed of train is 20 m/s , find the length of the train.

SOLUTION Length of train = Time \times Relative speed

$$= 7.5 \times (10 + 20) = 7.5 \times 30 = 225 \text{ m}$$

EXAMPLE 21 A train of length 250 m crosses a bridge of length 150 m in 20 seconds. What is the speed of train?

SOLUTION (Length of train + Length of bridge)

$$= \text{Speed of train} \times \text{Time}$$

$$(250 + 150) = 20 \times \text{Speed}$$

$$\text{Speed} = \frac{400}{20} = 20 \text{ m/s} = 72 \text{ km/h}$$

EXAMPLE 22 Two trains coming from the opposite sides crosses each other in 10 seconds if the lengths of first train and second train be 125 m and 175 m respectively, also the speed of first train be 36 km/h, find the speed of second train.

SOLUTION Speed of first train = 36 km/h = 10 m/s

$$\text{Now, Time} = \frac{\text{Sum of length of the two trains}}{\text{Sum of their speeds}}$$

$$10 = \frac{125 + 175}{(10 + x)}$$

$$\Rightarrow x = 20 \text{ m/s} = 72 \text{ km/h}$$

EXAMPLE 23 A fast moving superfast express crosses another passenger train in 20 seconds. The speed of faster train is 72 km/hr and speed of slower train is 27 km/h. Also the length of faster train is 100 m, then find the length of the slower train if they are moving in the same direction.

SOLUTION Time = $\frac{\text{Sum of length of the two train}}{\text{Difference in speeds}}$

$$20 = \frac{(100 + x)}{25/2}$$

$$\Rightarrow x = 150 \text{ m}$$

NOTE Relative speed = $(72 - 27) = 45 \text{ km/h}$

$$= 45 \times \frac{5}{18} = \frac{25}{2} \text{ m/s}$$

CONCEPT BASED ON BOATS AND RIVERS (OR STREAMS)

- When the boat and stream (or current) of river move in the same direction, then the relative speed of the boat is the sum of the individual speeds of boat and river. It is known as **downstream speed**.
- When the boat moves against the current of the river (i.e., in opposite direction), then the relative speed of the boat is the difference of the speeds of the boat and stream (of the river). It is known as **upstream speed**. Let the speed of boat in still water be B and speed of current of river be C then,

$$\begin{cases} \text{Downstream speed} = (B + C) \\ \text{Upstream speed} = (B - C) \end{cases} ; \quad B > C$$

$$\begin{cases} \text{Speed of the boat in still water} = \frac{(D + U)}{2} \\ \text{Speed of current (or stream)} = \frac{(D - U)}{2} \end{cases}$$

where $D \rightarrow$ downstream speed of the boat and $U \rightarrow$ upstream speed of the boat

When the distance covered by boat in downstream (i.e., with the flow of water) is same as the distance covered by boat in upstream (against the flow of the water) then,

$$\frac{\text{Time taken by boat in DS}}{\text{Time taken by boat in US}} = \frac{\text{Upstream speed}}{\text{Downstream speed}}$$

DS \rightarrow Downstream, US \rightarrow Upstream

EXAMPLE 24 A boat can move at 5 km/h in still water (i.e., when water is not flowing). The speed of stream of the river is 1 km/h. A boat takes 80 minutes to go from a point A to another point B and return to the same point.

- What is the distance between the two points?
- What is the ratio of downstream speed and upstream speed?
- What is the ratio of time taken in downstream speed to the upstream speed?

SOLUTION Downstream speed of boat = $(5 + 1) = 6 \text{ km/h}$

$$\text{Upstream speed of boat} = (5 - 1) = 4 \text{ km/h}$$

$$\text{Therefore, } \frac{\text{Downstream speed}}{\text{Upstream speed}} = \frac{\text{Upstream time}}{\text{Downstream time}}$$

$$\frac{6}{4} = \frac{3}{2} = \frac{\text{Time taken in upstream direction}}{\text{Time taken in downstream direction}}$$

$$\therefore \text{Time taken in downstream} = \frac{2}{5} \times 80 = 32 \text{ min}$$

$$\text{and time taken in upstream direction} = \frac{3}{5} \times 80 = 48 \text{ min}$$

$$\therefore \text{Distance between two points} = \text{DS speed} \times \text{DS time}$$

$$= \text{US speed} \times \text{US time}$$

where DS \rightarrow Downstream and US \rightarrow Upstream

$$D = \frac{6 \times 32}{60} = 3.2 \text{ km}$$

$$\text{or } D = 4 \times \frac{48}{60} = 3.2 \text{ km}$$

$$(i) 3.2 \text{ km} \quad (ii) 3 : 2 \quad (iii) 2 : 3$$

EXAMPLE 25 A man can row 9 km/h in still water. It takes him twice as long as to row up as to row down. Find the rate of stream of the river.

SOLUTION $\frac{\text{Time taken in upstream}}{\text{Time taken in downstream}} = \frac{2}{1}$

$$\therefore \frac{\text{Downstream speed}}{\text{Upstream speed}} = \frac{2}{1} \quad \text{where } \frac{B + R}{B - R} = \frac{2}{1}$$

$B \rightarrow$ Speed of boat in still water

$R \rightarrow$ Speed of current

$$\Rightarrow \frac{B}{R} = \frac{3}{1} \quad (\text{By componendo and dividendo})$$

$$\Rightarrow \frac{9}{R} = \frac{3}{1} \Rightarrow R = 3 \text{ km/h}$$

RACES

Terminology

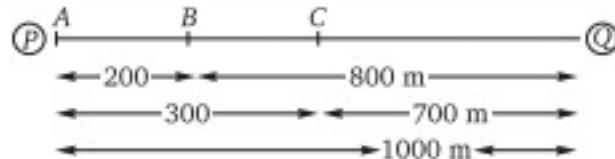
- (i) **Startup or headstart:** When a runner allows to another runner to stay ahead in the same race, then it is said that there is a startup in the race.

For example if A allows B to go ahead before starting the race, then it is said that A gives startup to B and B has the startup. If before starting the race B goes ahead of x metre, then we can say A gives x metre startup to B or B has startup (or headstart) of x metre.

- (ii) **Dead heat:** When the runners reach the finishing line (or the final post) then it is said that these runners finish (or end) the race in dead heat.

EXAMPLE 1 *A can give B a 200 m startup and C a 300 m startup in a race of 1 km. How many metres startup can B give to C in a 1 km race.*

SOLUTION



$$\text{Ratio of speeds of } A : B = 1000 : 800 = 5 : 4$$

$$\text{Ratio of speeds of } A : C = 1000 : 700 = 10 : 7$$

$$\text{Ratio of speeds of } B : C = 800 : 700 = 8 : 7$$

Since, when B moves 8 m, C moves 7 metre. Therefore, when B moves 1000 m, C moves 875 metre. Thus, B can give C a start of $1000 - 875 = 125$ m.

Alternatively: Since C is 12.5% slower than B . So, C will cover 12.5% less distance than B in the same time.

(Since when time is constant, they cover the distances in the ratio of their speeds.)

Thus, in 1000 m (or 1 km) when B runs 1000 m, C will run 125 m less than B .

Hence, B can give a start of 125 m to C in a 1 km race.

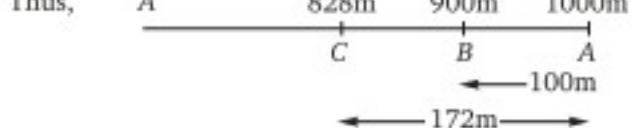
EXAMPLE 2 *In a one km race A gives B a start of 100 m and in a one km race B gives a start of 80 m to C. In a 1 km race who will win and by how much distance from the worst performer between two losers?*

SOLUTION

$$\text{Ratio of speeds of } A : B = 1000 : 900 = 100 : 90$$

$$\text{Ratio of speeds of } B : C = 1000 : 920 = 100 : 92$$

Therefore, when A moves 1000 m, B moves 900 m and when B moves 900 m, C moves 828 m.



Since, C moves 8% less than B in the same time. Thus, C is the worst performer and A will win by him by 172 m.

SOME MORE USEFUL CONCEPTS

- (i) When it is said that A can give B a start of x metre in y metre race, then it means in y metre race B runs x metre less than A in the same time.

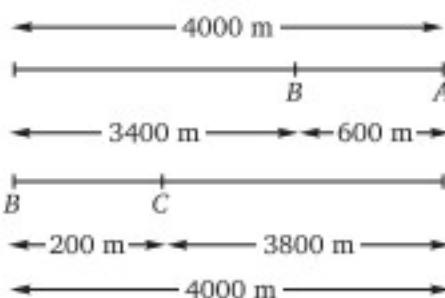
NOTE There is a great difference between 'can' and 'gives'.

- (ii) When A beats B by t seconds in a race of y metre then it means B is the loser and A is the winner and when A reaches the finishing line B is still some distance back to A . Thus B takes t seconds to cover the remaining distance. Hence, we can calculate the speed of loser (B).

- (iii) Throughout the race there is always a certain relationship among runners i.e., they always maintain the ratio of speeds. I think this is the nub of all the problems pertaining to the races. Go ahead...

EXAMPLE 3 *In a 4 km race A wins by 600 m over B. B can give start of 200 m to C in a 4 km race. By how much distance C gets start up so that the race between A and C ends in dead heat in the same race of 4 km?*

SOLUTION



$$\text{Ratio of speeds of } A : B = 4000 : 3400 = 20 : 17$$

$$\text{and} \quad \text{Ratio of speeds of } B : C = 20 : 19$$

$$\therefore \text{Ratio of speeds of } A : B : C = 400 : 340 : 323$$

Therefore, in 4000 m race A run 4000 m, B run 3400 m and C run 3230 m. Thus C can get 770 m start up from A .

EXAMPLE 4 *In a 1500 m race A wins over B by 350 m and in 1500 m race C can give a startup of 250 m to B. By how much distance A give start up to C, so that A beats C by 50 metres?*

SOLUTION

$$\text{Ratio of speeds of } A : B = 1500 : 1150 = 30 : 23$$

$$\text{Ratio of speeds of } B : C = 5 : 6$$

$$\therefore \text{Ratio of speeds of } A : B : C = 150 : 115 : 138$$

So, when A moves 1500 m, B moves 1150 m and C moves 1380 m. Thus C moves 120 m less than A . To win A just by 50 m over C , A should give $120 - 50 = 70$ m startup to C .

EXAMPLE 5 *In a race of 2500 m, A beats B by 500 m and in a race of 2000 m, B beats C by 800 m. By what distance A gives startup to C so that they will end up with dead heat in 3 km race. Also find that by what distance A will win over C in a 1 km race?*

SOLUTION

$$\text{Ratio of speeds of } A : B = 2500 : 2000 = 5 : 4$$

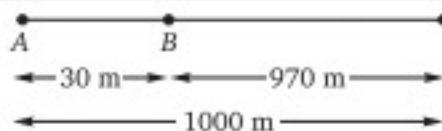
$$\text{Ratio of speeds of } B : C = 5 : 3$$

$$\therefore \text{Ratio of speeds of } A : B : C = 25 : 20 : 12$$

In 3 km race A run 3000 m, B run 2400 m, C run 1440 m, so to end up the race in dead heat A should give C the startup of 1560 m and therefore in 1 km the same will be 520 m.

EXAMPLE 6 A gives B, a start of 30 m or 10 seconds and end up the race of 1 km in dead heat. What is the ratio of speeds of A and B?

SOLUTION



Since, either B has the startup of 30 m or 10 seconds. It means B runs 30 m in 10 seconds. Hence, the speed of B is 3 m/s.

NOTE Don't be confused that A's speed = 3 m/s.

Also, it is very simple when A moves 1000 m, B moves 970 m. Since, the ratio of speeds is equal to the ratio of distances covered by A and B in the same time. Thus, the speed of

$$A : B = 1000 : 970 = 100 : 97$$

EXAMPLE 7 In a 1 km race A wins over B by 80 m or 20 seconds. B can give a start of 100 m to C in 1 km race. Find out that by how much time A will win over C? Also, find the ratio of speeds of B and C.

SOLUTION Ratio of speeds of A : B = 100 : 92

$$\text{Ratio of speeds of } B : C = 10 : 9$$

$$\therefore \text{Ratio of speeds of } A : B : C = 1000 : 920 : 828$$

$$\text{Also, } \text{Speed of } B = \frac{80}{20} = 4 \text{ m/s}$$

$$\text{Therefore, } \text{Speed of } C = 3.6 \text{ m/s}$$

Now, C has to cover 172 m distance in extra time. So, the time taken by C to cover the remaining distance $= \frac{172}{3.6} = 47.77$ s.

$$\begin{aligned} \text{Ratio of speeds of } B : C &= \text{Ratio of distances covered by } B : C \\ &= 1000 : 900 = 10 : 9 \end{aligned}$$

$$\therefore \frac{\text{Speed of } B}{\text{Speed of } C} = \frac{10}{9}$$

EXAMPLE 8 A can win B by 250 m in a 2 km race. What should be the change in distance of startup? So, that B must cover 20% less distance than that by A in the same time.

SOLUTION

$$\frac{\text{Distance covered by } A}{\text{Distance covered by } B} = \frac{5}{4}$$

$$\therefore \frac{\text{Speed of } A}{\text{Speed of } B} = \frac{5}{4}$$

So, when A moves 2000 m, B should move 1600 m. But since initially B moves 1750 m. Therefore the new startup will be increased by 150 m.

EXAMPLE 9 The ratio of speeds of A and B is 4 : 7 and A loses the race by 270 m, then what is the length of the race course?

SOLUTION When B moves 7 m, A moves only 4 m. Hence, A loses the race by 3 m.

Now, since B loses by 3 m in the race of 7 m.

\therefore B will lose 270 m in the race of 630 m.

EXAMPLE 10 The ratio of time taken to run a certain distance by Pythagorus and Hawkins is 4 : 3 and thus Hawkins wins the race by 360 m. What is the distance of race course?

SOLUTION

$$\begin{aligned} \frac{\text{Time taken by Pythagorus}}{\text{Time taken by Hawkins}} &= \frac{4}{3} \\ \frac{\text{Speed of Pythagorus}}{\text{Speed of Hawkins}} &= \frac{3}{4} \\ &= \frac{\text{Distance covered by P}}{\text{Distance covered by H}} \end{aligned}$$

Now, when Hawkins runs 4 m, Pythagorus runs 3 m and thus Hawkins wins by 1 m.

So, when Hawkins wins the race by 1 m, race course is 4 m. when Hawkins wins the race by 360 m, race course is

$$360 \times 4 = 1440 \text{ m}$$

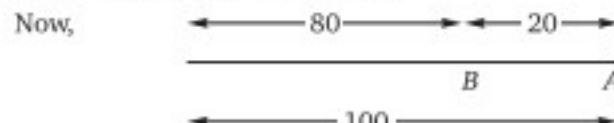
Alternatively : 360 = 25% of the total length of race.

$$\therefore \text{length of race course} = 1440 \text{ m.}$$

EXAMPLE 11 In a race of D km, A wins over B by 0.2 D and in the same length of race B wins over C by 0.25 D. What should be the head-start to C, So that A and C finish the race at the same time.

SOLUTION **Note:** Instead of solving the problem using 'D' as a distance convert it into 100 i. e., suppose D = 100.

(It is just for your convenience.)



$$\text{Now, } \text{Speed of } A : B = 100 : 80 = 5 : 4$$

$$\text{Speed of } B : C = 4 : 3$$

$$\therefore \text{Speed of } A : B : C = 20 : 16 : 12$$

$$= \underline{\underline{100 : 80 : 60}}$$

{40}

So, A can give C a start of 40 m in 100 m race. Therefore, A can give 0.4 D. Start to 'C' in the race of D unit.

EXAMPLE 12 In a 3 km race the speeds of A and B are in the ratio of 6 : 5 and A wins by 10 seconds. What is the time taken by B to finish the race. Also, to end the race in dead heat what per cent of total distance A should give the startup to B?

SOLUTION Ratio of distances covered by A and B when A just reaches the finishing line = 6 : 5.

Thus, B has to cover 500 m distance in extra time and this 500 m distance is covered by B in 10 seconds. So, the speed of B = 50 m/s.

Thus, the total time required by B to complete the 3 km race

$$= \frac{3000}{50} = 60 \text{ s} = 1 \text{ min}$$

Since, B covers 16.66% distance less than A covers in the same time, so A should give 16.66% of the total distance as a startup to B.

EXAMPLE 13 In a 1 km race A gives B a startup of 5 seconds and still wins over B by 15 seconds. The ratio of speeds of A and B is 2 : 1. Find the time taken by A to finish 2.5 km race.

SOLUTION

$$\frac{\text{Speed of } A}{\text{Speed of } B} = \frac{2}{1}$$

$$\frac{\text{Time taken by } A}{\text{Time taken by } B} = \frac{1}{2}$$

$$\frac{t}{(t+20)} = \frac{1}{2}$$

$$\Rightarrow t = 20 \text{ s}$$

Thus, A needs 20 seconds to cover 1 km. Thus, to cover 2.5 km race he needs $20 \times 2.5 = 50$ seconds.

EXAMPLE 14 X can beat Y by 200 m in a race of 2000 m. Y can beat Z by 100 m in a race of 2500 m. By how many metres can X beat Z in a race of 1000 m?

SOLUTION Ratio of speeds of X and Y = 10 : 9 (2000 : 1800)

Ratio of speeds of Y and Z = 25 : 24 (2500 : 2400)

Ratio of speeds of X, Y and Z = 250 : 225 : 216

Since in a race of 250 m, X beats Z by 34 m.

So, in a race of 1000 m, X will beat Z by 136 m.

EXAMPLE 15 In a 6 km race B has 250 m headstart and C has 500 m headstart by A, still A beats C and B by 235 m and 350 m respectively. How many metres startup can B give to C so as to end up the race at the same time with C in the race of 6 km. Also find the ratio of speeds of A : B : C.

SOLUTION When A runs 6000 m, B runs 5400 m only and C runs 5265 m only.

So, when B runs 6000 m, C will run 5850 m. So, B can give 150 m startup to C.

$$\begin{aligned} \text{Ratio of speeds of } A : B : C &= 6000 : 5400 : 5265 \\ &= 1200 : 1080 : 1053 \\ &= 400 : 360 : 351 \end{aligned}$$

EXAMPLE 16 A can run 1 km in 2 min 20 second and B can run the same distance in 3 min. What is the distance travelled by B in the same time as A travels, when they start simultaneously in the race of 4.5 km.

SOLUTION

$$\frac{\text{Time taken by } A}{\text{Time taken by } B} = \frac{140 \text{ s}}{180 \text{ s}} = \frac{7}{9}$$

$$\therefore \frac{\text{Speed of } A}{\text{Speed of } B} = \frac{\text{Distance travelled by } A}{\text{Distance travelled by } B} = \frac{9}{7}$$

$$\text{Therefore, } B \text{ travels } \frac{7}{9} \times 4.5 = 3.5 \text{ km.}$$

EXAMPLE 17 Shahrukh takes 4 min to cover the same distance for which Urmila takes 6 min 30 sec. What is the ratio of distances covered by Shahrukh and Urmila in the race of 2.6 km and by what distance Shahrukh wins over Urmila?

SOLUTION $\frac{\text{Time taken by Shahrukh}}{\text{Time taken by Urmila}} = \frac{240}{390} = \frac{8}{13}$

$$\frac{\text{Distance covered by Shahrukh}}{\text{Distance covered by Urmila}} = \frac{13}{8}$$

Hence, Shahrukh will win the race by 1 km.

EXAMPLE 18 A runs at the speed of $\frac{7}{4}$ times the speed of B. By calculation B finds that she has to run 300 m after A reaches to the winning post. What is the total distance of race?

SOLUTION

$$\frac{\text{Speed of } A}{\text{Speed of } B} = \frac{7}{4}$$

$$\frac{\text{Distance of } A}{\text{Distance of } B} = \frac{7}{4}$$

So, the total distance of race = 700 m.

$$(\because 7x - 4x = 300 \Rightarrow 7x = 700)$$

EXAMPLE 19 Time taken by A is $\frac{5}{7}$ of B's time for the same length of race. The speed of A is 84 m/s and A beats B by 240 m. What is the length of race course?

SOLUTION $\frac{\text{Speed of } A}{\text{Speed of } B} = \frac{\text{Time taken by } B}{\text{Time taken by } A} = \frac{7}{5}$

$$\text{Now since, } 7x - 5x = 240$$

$$\Rightarrow 7x = 840 \text{ m}$$

EXAMPLE 20 In a race of 3000 m, Michal beats Nicholas by 600 m and Nicholas in a race of 2000 m beats Oscar by 600 m. In a 1 km race by how much distance Michal beats Oscar?

SOLUTION Ratio of speeds of M : N : O = 100 : 80 : 56

So, Michal (M) beats Oscar (O) by 440 m in 1 km race.

EXAMPLE 21 In a race of 500 m, President runs at 5 m/s. If president gives chairman a start of 20 m and still beats him by 20 seconds, what is the chairman's speed?

SOLUTION Chairman has to cover only 480 m. He takes total

$$100 + 20 = 120 \text{ s}$$

$$\text{Therefore, speed of chairman} = \frac{480}{120} = 4 \text{ m/s}$$

EXAMPLE 22 In a race of 800 m Dholakiya gives Preetam a start of 200 m and then loses the race by 20 seconds. What is the speed of Preetam and Dholakiya respectively? If the ratio of respective speeds be 3 : 2.

SOLUTION Let the speed of Dholakiya be S_D and speed of Preetam be S_P and let the time taken by Preetam be t second then,

$$\frac{S_D}{S_P} = \frac{\frac{800}{(t+20)}}{\frac{600}{t}} = \frac{2}{3}$$

$$\frac{800}{600} \times \frac{t}{(t+20)} = \frac{2}{3}$$

$$t = 20 \text{ s}$$

$$\therefore \text{Speed of Preetam} = \frac{600}{20} = 30 \text{ m/s}$$

$$\text{and speed of Dholakiya} = \frac{800}{40} = 20 \text{ m/s}$$

EXAMPLE 23 In race of 1 km Sahara gives Birla a startup of 250 m still Sahara wins by 150 m. What is the ratio of speeds of Sahara and Birla?

SOLUTION When Sahara covers 1000 m, Birla covers only 600 m.
So, the ratio of speeds of Sahara and Birla
 $= 1000 : 600 = 5 : 3$

EXAMPLE 24 Priyambda wins the race over Kokilaben by 150 m in a race of 1 km but when she gives a startup of 5 seconds to Kokilaben she wins by 65 m. Find the speed of Kokilaben.

SOLUTION In 5 seconds Kokilaben runs 85 m.
So, the speed of Kokilaben = 17 m/s.

CIRCULAR MOTION

- When the bodies are moving in the opposite direction, their relative speed becomes equal to the sum of their individual speed.
- When two bodies are moving in the same direction their relative speed becomes equal to the difference of the individual speeds.

First Meeting

- Let A and B be two runners. Time taken by them to meet for the first time

$$= \frac{\text{Length of the circular track}}{\text{Relative speed}}$$

EXAMPLE 1 Arjun and Bhishma are running on a circular track of length 600 m (i.e., circumference of the track). Speed of Arjun is 30 m/s and that of Bhishma is 20 m/s. They start from the same point at the same time in the same direction. When will they meet again for the first time?

SOLUTION Time = $\frac{\text{Circumference}}{\text{Relative speed}}$
 $= \frac{600}{10} = 60 \text{ s}$

Actually Arjun (faster one) has to make a lead of 600 m, because when Arjun will be 600 m ahead (or extra distance) of Bhishma, they will be together again as a person when completes the total length (or circumference) it starts retracing the same path and thus Arjun and Bhishma can be together again.

Since, they make a difference (or Arjun makes a lead) of 10 m in 1 second. So, he will create 600 m difference in 60 second.

EXAMPLE 2 In the previous problem if they move in opposite direction, then what is the time taken by them to meet again for the first time?

SOLUTION Time = $\frac{\text{Circumference}}{\text{Relative speed}}$
 $= \frac{600}{50} = 12 \text{ s}$ $(30 + 20 = 50)$

EXAMPLE 3 Arjun and Bhishma run at the speed 30 m/s and 20 m/s respectively on the circular track of 600 m, as its circumference, when would the Arjun and Bhishma meet for the first time at the starting point if they start simultaneously from the same point?

SOLUTION Time taken by Arjun to complete one round

$$= \frac{600}{30} = 20 \text{ s}$$

Time taken by Bhishma to complete one round = $\frac{600}{20} = 30 \text{ s}$

- When there are more than two runners, then suppose A is the fastest runner and A meets B for the first time in t_{AB} seconds/hours and A meets C for the first time in t_{AC} seconds/hours and A meets D for the first time in t_{AD} seconds/hours and so on. Then time taken by all of them to meet for the first time is the LCM of t_{AB}, t_{AC}, t_{AD} etc.

First Meeting at the Starting Point

Let A takes t_A time to complete one round and B takes t_B time and C takes t_C time and so on, then the time taken to meet for the first time at the starting point = LCM of t_A, t_B, t_C etc.

Hence, after every 20 second, Arjun would be at the starting point and after every 30 second, Bhishma would be at the starting point. Thus the time taken by both to be at the starting point again for the first time

$$= \text{LCM of } 20 \text{ and } 30 = 60 \text{ s}$$

Thus, every 60 seconds they would be together at the starting point.

NOTE The required time for the bodies to meet for the first time at the starting point is immaterial to the direction of bodies i.e., whether they move in the same direction or in opposite direction.

EXAMPLE 4 Arjun, Bhishma and Nakul run on the circular path at the speed of 20 m/s, 30 m/s and 50 m/s respectively in the same direction. The circumference of the track (or path) is 600 m.

- When will they be together again for the first time?
- When will they be together again for the first time at the starting point?

SOLUTION (i) Nakul meets Arjun after every $= \frac{600}{(50 - 20)} = 20 \text{ s}$

Nakul meets Bhishma after every $= \frac{600}{(50 - 30)} = 30 \text{ s}$

Therefore, all of the three would meet after every 60 seconds. $(60 = \text{LCM of } 20 \text{ and } 30)$.

Hence, they would all meet for the first time after 60 seconds.

(ii) Arjun takes $\frac{600}{20} = 30 \text{ s}$ to complete one round

Bhishma takes $\frac{600}{30} = 20 \text{ s}$ to complete one round

and Nakul takes $\frac{600}{50} = 12 \text{ s}$ to complete one round

Hence, they would meet for the first time at the starting point after 60 seconds.

HINT $60 = \text{LCM of } 30, 20 \text{ and } 12$.

EXAMPLE 5 A tortoise can complete a full round on the circular track in 8 min, while the rabbit can do the same on the same circular track in 5 min. A, B, C and D are the four consecutive points on the circular track which are equidistant from each other. A is opposite to C and B is opposite to D.

- (i) After how many minutes will they meet together for the first time, when both have started simultaneously from the same point in the same direction?
 - (ii) After how many minutes will they meet together for the first time at the starting point, when both have started simultaneously from the same point in the same direction?
 - (iii) If they start from a point A, simultaneously in the same direction then after how many minutes will they meet at C which is just opposite to A?
 - (iv) If tortoise has a lead of 5 min, when would they meet for the first time, where they have started from the same point in the same direction?

SOLUTION (i) Ratio of time of rabbit and tortoise = 5 : 8

∴ Ratio of the speed of rabbit and tortoise = 8

Let the length of the circular track be 40 m, then the speed of rabbit = 8 m/min and speed of tortoise = 5 m/min.

(40 is the LCM of 8 and 5, taken just for convenience in calculation)

Now, the time when they will be together for the first time

$$= \frac{\text{Circumference}}{\text{Relative speed}} = \frac{40}{3} \text{ min}$$

- (ii) Time taken by rabbit to complete one round = 5 min
 Time taken by tortoise to complete one round = 8 min
 \therefore They will meet at the starting point, for the first time
 $= \text{LCM of 5 and 8} = 40 \text{ min}$

(iii) Rabbit reaches point C in $\frac{20}{8} = 2.5 \text{ min.}$
 Rabbit reaches the same point C in 7.5, 12.5, 17.5, 22.5 min etc. Tortoise reaches after 4 min, 12 min, 20 min, ... etc. They will never meet at C since time cannot coincide as time taken by rabbit is the decimal number and time taken by tortoise is a natural number.

(iv) In 5 min tortoise travels 25 m. Now, rabbit starts chasing tortoise @ 8 m/min.

∴ Time taken by rabbit to overtake tortoise

$$= \frac{25}{(8-5)} = \frac{25}{3} \text{ min}$$

EXAMPLE 6 Alfred and Bernard run on the circular track of 600 m. Speeds of Alfred and Bernard are 30 m/s and 20 m/s respectively. Initially they are diametrically opposite to each other.

- (i) When will they meet for the first time if both move in the same direction?
 (ii) If both of them move in opposite directions, when will they meet for the second time?

SOLUTION (i) Relative speed of Alfred = $30 - 20 = 10$ m/s
Bernard is 300 m ahead in the race.

$$\text{So, time taken by Alfred to catch Bernard} = \frac{300}{10} = 30 \text{ s}$$

- $$\text{(ii) To meet for the second time they have to cover} \\ = 300 + 600 = 900 \text{ m}$$

$$\text{there relative speed} = 30 + 20 = 50 \text{ m/s}$$

(since direction is opposite)

$$\therefore \text{Time taken to meet for the second time} = \frac{900}{50} = 18 \text{ s}$$

EXAMPLE 7 A, B and C run on a circular track of 800 m. Speeds of A, B and C are 20 m/s, 26 m/s and 33 m/s.

- (i) When will they meet for the first time?
 (ii) What is the ratio of distances covered by each one to meet for the first time.

SOLUTION (i) Time taken by C to meet A for the first time

$$= \frac{800}{33 - 20} = \frac{800}{13} \text{ s}$$

Time taken by C to meet B for the first time

$$= \frac{800}{33-26} = \frac{800}{7} \text{ s}$$

$$\text{LCM of } \frac{800}{13} \text{ and } \frac{800}{7} = 800 \text{ s.}$$

Therefore, all of them (i. e., A, B and C) meet after 800 seconds = 13 min 20 sec.

- (ii) The ratio of distances = ratio of speeds
 $= 20 : 26 : 33$

INTRODUCTORY EXERCISE-9.1

CLOCKS

Actually the movement of hour-hand and minute-hand follows the relative motion. The dial of the clock behaves like a circular track and where minute-hand is a faster runner and hour-hand is a slower one.

For better understanding with the clocks, assume 60 minutes shown on the dial as 60 points. Here we give an

EXAMPLE 1 How many times minute-hand coincides with hour-hand in 12 hours?

SOLUTION Time taken by minute-hand to meet hour-hand for the first time $= \frac{60}{55} = \frac{12}{11}$ hours.

(Assume initially both hands are at 12 i.e., 12 O' clock is shown by them.)

Therefore, after every $\frac{12}{11}$ hours minute hand and hour-hand meet each other (or coincide or overtake).

Now, since in $\frac{12}{11}$ hours they coincide 1 time

So, in 12 hours they will coincide

$$= \frac{12}{\frac{12}{11}} = \frac{12}{12} \times 11 = 11 \text{ times}$$

Remember: Between 11 O'clock and 1 O'clock, two hands coincide only one time, that's why they coincide with each other only 11 times in 12 hours.

NOTE In every $\frac{12}{11}$ hours (or $65 \frac{5}{11}$ min) two hands of a clock coincide.

EXAMPLE 2 In 12 hours how many times the two hands of clock will be just opposite to each other i.e., they make a straight line having the difference of 180° between them?

SOLUTION $180^\circ = 30 \text{ points}$

For the first time minute-hand and hour-hand will be separated in $\frac{30}{55} \text{ h} \left(\text{Time} = \frac{\text{Required distance}}{\text{Relative speed}} \right)$ and for every next

time they will take $\frac{60}{55}$ minutes more to occur as opposite to each other.

(Since in $60/55$ hours they complete one round of clock's dial i.e., 60 points undergoing the relative motion, we have total 12 hours.)

$$\begin{aligned} \text{Thus, } & \frac{30}{55} + \frac{60}{55} + \frac{60}{55} + \frac{60}{55} + \dots = 12 \\ \Rightarrow & \frac{30}{55} + \frac{60}{55} + \frac{60}{55} + \dots = \frac{12 \times 55}{55} \\ \Rightarrow & 6 + 12 + 12 + \dots = 12 \times 11 = 132 \\ \Rightarrow & 6 + 12n = 132 \\ \Rightarrow & 12n = 126 \Rightarrow n = 10 \end{aligned}$$

only integral value is admissible.

Thus, total $10 + 1 = 11$ times both hands of a clock will be opposite to each other.

Remember: Between 5 O'clock and 7 O'clock the two hands make 180° angle only one time, that's why they make 180° angle only 11 times in 12 hours, i.e., at exactly 6 O'clock they are 180° apart.

arbitrary new unit of distance as 'point'.

So, minute-hand (MH) runs on the circular track of 60 points at 60 points per hour and hour-hand (HH) runs at 5 points per hour. Now we become familiar with the relative motion of two hands of a clock.

Here, 1 point $= 6^\circ$ and 60 point $= 360^\circ$

also 1 point $= 6^\circ = 1 \text{ min}$

EXAMPLE 3 In 12 hours how many times a minute-hand and hour-hand of a clock makes 90° between them or becomes perpendicular to each other?

SOLUTION $90^\circ = 15 \text{ points}$

This problem can be solved in two parts.

(i) When minute-hand goes ahead of hour-hand.

(ii) When hour-hand goes ahead of minute-hand.

(i) For the first time minute-hand and hour-hand will make 90° (or 15 points) difference in $\frac{15}{55}$ hours.

$$\text{time} = \frac{\text{distance}}{\text{relative speed}}$$

Now, after every $\frac{60}{55}$ hours they will occur at 90° . Since, in every $\frac{60}{55}$ hours they create a difference of 360° or 60 points (as the circumference of dial).

Now, we have 12 hours,

$$\begin{aligned} \therefore & \frac{15}{55} + \frac{60}{55} + \frac{60}{55} + \dots = 12 \text{ h} = 12 \times \frac{55}{55} \\ \Rightarrow & \frac{3}{11} + \frac{12}{11} + \frac{12}{11} + \dots = \frac{12 \times 11}{11} \\ \Rightarrow & \frac{3}{11} + \left(\frac{12}{11} n \right) = \frac{12 \times 11}{11} \\ \Rightarrow & 3 + 12n = 132 \\ \Rightarrow & n = \frac{129}{12} = 10 \end{aligned}$$

(only integral value of n is acceptable)

Therefore, $10 + 1 = 11$ times in 12 hours minute-hand makes 90° angle between the two hands, but when minute hand is ahead of hour-hand.

(ii) For the first time minute-hand and hour-hand will make 90° (or 15 points) difference in $\frac{60 - 15}{55} = \frac{45}{55}$ hours.

Since, in this case minute-hand goes till it appears to be 15 points behind of hour-hand (consider initially they are showing 12 O'clock) then you will see that at 12 : 49 : 05 two hand are making 90° angle between them, while it appears to be hour-hand is ahead of minute-hand.

Now, for every next time after $\frac{60}{55}$ hours they will show the same situation.

we have 12 hours.

$$\text{So, } \frac{45}{55} + \frac{60}{55} + \frac{60}{55} + \frac{60}{55} + \dots = 12 \text{ h} = 12 \times \frac{55}{55}$$

$$\begin{aligned}
 &\Rightarrow \frac{3}{11} + \frac{4}{11} + \frac{4}{11} \dots = \frac{4 \times 11}{11} \\
 &\Rightarrow 3 + 4 + 4 + \dots = 44 \\
 &\Rightarrow 3 + 4n = 144 \\
 &\Rightarrow n = \frac{41}{4} = 10, \text{ consider only integral value.}
 \end{aligned}$$

Thus, total $10 + 1 = 11$ times they will make 90° angle.

Hence, in 12 hours both hands make 90° angle $(11 + 11) = 22$ times in different positions.

Remember: At 3 O'clock and 9 O'clock they are at right angled. Since, except between 2-4 O'clock and 8-10 O'clock in each hour both hands make 90° angle 4 times while in the 2-4 O'clock and 8-10 O'clock two hands makes three-times in every two hour.

EXAMPLE 4 Between 2 O'clock and 3 O'clock when two hands of a clock overlap each other?

SOLUTION To overlap or overtake minute-hand has to reduce the gap of 10 points. Since at 2 O'clock two hands are 10 point apart.

$$\begin{aligned}
 &\therefore \text{Time} = \frac{\text{Distance advanced}}{\text{Relative speed}} \\
 &= \frac{10}{55} \text{ h} = \frac{10}{55} \times 60 \text{ min} \\
 &= 10 \text{ min } 54 \text{ s}
 \end{aligned}$$

Thus, at 2 : 10 : 54 both hands of a clock coincide.

EXAMPLE 5 Between 6 am and 7 am when the two hands of a clock coincide.

SOLUTION Time $= \frac{30}{55} \text{ h} = \frac{30}{55} \times 60 \text{ min} = 32 \text{ min } 43 \text{ s}$
(Distance advanced $= 6 \times 5 = 30$ points)

Thus at 6 : 32 : 43 two hands of a clock coincide.

EXAMPLE 6 Between 11 O'clock and 12 O'clock when will they coincide.

SOLUTION Distance advanced at 11 O'clock = 55 points

Relative speed = 55 point/h

$$\therefore \text{Time} = \frac{55}{55} = 1 \text{ h}$$

Hence, they will coincide at $(11 + 1) = 12$ O'clock.

EXAMPLE 7 Between 3 O'clock and 4 O'clock when will the two hands make 36° angle between them:

- (i) when hour-hand is ahead of minute-hand.
- (ii) when minute-hand is ahead of hour-hand.

SOLUTION (i) $36^\circ = 6$ points

Now, at 3 O'clock two hands are separated by exactly 15 points to which we have to reduce upto 6 points. Thus, we have to reduce $15 - 6 = 9$ points distance, with the relative speed of 55 point/h.

$$\begin{aligned}
 \therefore \text{Time required} &= \frac{9}{55} \text{ h} = \frac{9}{55} \times 60 \\
 &= 9 \text{ min } 49 \text{ s}
 \end{aligned}$$

Thus at 3 : 09 : 49 they are 36° apart from each other.

(ii) At 3 O'clock both hands are 15 points apart so to make them 6 points apart minute-hand has to move for $(15 + 6) = 21$ points, since minute-hand has to go 6 points ahead of hour hand, after crossing the hour-hand.

$$\therefore \text{Time} = \frac{21}{55} \text{ h} = \frac{21}{55} \times 60 \text{ min} = 22 \text{ min } 54 \text{ s}$$

Thus at 3 : 22 : 54, both hands will be 6 points (or 36°) apart from each other.

Did you notice something?

The same angle can be formed in two situations, one when hour-hand is ahead of minute-hand and when minute-hand is ahead of hour-hand.

Thus, you can find the required time by dividing the required difference of points (which you have to either create or reduce) by the relative speed.

EXAMPLE 8 What is the angle between the two hands at 3 : 10 am?

SOLUTION Assume 60th point (i.e., when it is 12 O'clock) as the origin.

Step 1. Find the distance of minute-hand from the origin.

Step 2. Find the distance of hour-hand from the origin.

Step 3. Take the difference between two values obtained in step 1 and step 2.

\therefore **Step 1.** 10 point = 60°

Step 2. $90^\circ + 5^\circ = 95^\circ$ (In 10 min hour-hand moves 5°)

Step 3. $95^\circ - 60^\circ = 35^\circ$

Thus, at 3 : 10 am two hands are 35° apart.

EXAMPLE 9 What is the angle between two hands of a clock at 7 : 35?

SOLUTION **Step 1.** At 7 : 35, minute-hand is $35 \times 6 = 210^\circ$ away from origin.

Step 2. At 7 : 35 hour-hand is $7 \times 30 + 35 \times \frac{1}{2} = 210 + 17.5$

$= 227.5^\circ$ away from the origin.

Step 3. $227.5 - 210 = 17.5^\circ$

Thus at 7 : 35, both hands make 17.5° angle between them.

NOTE A minute-hand moves 6° in one minute while a hour-hand moves $\left(\frac{1}{2}\right)^\circ$ in one minute.

Exercise

LEVEL 1

- 'A' goes 10 km distance with average speed of 6 km/h while rest 20 km he travels with an average speed of 15 km/h. What is the average speed of 'A' **during** the whole journey?
(a) 10 km/h (b) 12 km/h
(c) 13 km/h (d) 14.5 km/h
- A covers half of his distance with 20 km/h and rest with 30 km/h. What is the average speed during the whole journey?
(a) 20 km/h (b) 24 km/h
(c) 25 km/h (d) 26 km/h
- A covers 1/3rd of his journey at the speed of 10 km/h and half of the rest at the speed of 20 km/h and rest at the speed of 30 km/h. What is the average speed of A?
(a) $6\frac{2}{11}$ km/h (b) $16\frac{4}{11}$ km/h
(c) $16\frac{4}{11}$ m/s (d) none of these
- A covers 1/4th of his journey at 20 km/h and 1/3rd of the rest at 25 km/h and half of the rest at 30 km/h and rest at the speed of 40 km/h. What is the average speed of A?
(a) $13\frac{78}{89}$ km/h (b) 12 km/h
(c) $26\frac{86}{89}$ km/h (d) 28 km/h
- A covered half of his journey at 20 km/h and rest at x km/h, then his average speed is 24 km/h. What is the value of x ?
(a) 30 (b) 32
(c) 36 (d) 40
- A man covered half of the distance at $3x$ km/h and rest at $5x$ km/h. What is the average speed of the man?
(a) $4x$ km/h (b) $3.5x$ km/h
(c) $3.75x$ km/h (d) none of these
- A person goes to his office at 1/3rd of the speed at which he returns from his office. If the average speed during the whole trip (i.e., one round) is 12 km/h. What is the speed of the person while he was going to his office?
(a) 10 (b) 6
(c) 8 (d) can't be determined
- A person X starts from Lucknow and another persons Y starts from Kanpur to meet each other. Speed of X is 25 km/h, while speed of Y is 35 km/h. If the distance between Lucknow and Kanpur be 120 km and both X and Y start their journey at the same time, when will they meet?
(a) 1 h later (b) 2 h later
(c) $\frac{1}{2}$ h later (d) 3 h later

- In the above question (no. 8), what is the distance from Lucknow where they meet?
(a) 50 km (b) 60 km
(c) 100 km (d) 80 km

- Two persons A and B started from two different places towards each other. If the ratio of their speeds be 3 : 5, then what is the ratio of distance covered by A and B respectively till the point of meeting?
(a) 1 : 2 (b) 3 : 4
(c) 3 : 5 (d) 5 : 3

Directions for question number 11 to 16: A person P is at X and another person Q is at Y. The distance between X and Y is 100 km. The speed of P is 20 km/h. While the speed of Q is 60 km/h?

- If they first time meet at point Z somewhere between X and Y then the distance between X and Z is :
(a) 20 km (b) 40 km
(c) 25 km (d) 30 km
- If they continue to move to and fro between X and Y then what is the distance covered by P when they meet second time?
(a) 105 km (b) 100 km
(c) 80 km (d) 75 km
- If they continue to move to and fro between X and Y then what is the distance travelled by Q, when they meet each other for the third time?
(a) 375 km (b) 225 km
(c) 350 km (d) 445 km
- If P and Q continue to move between X and Y in the given manner and if they meet for the fourth time at a place M somewhere between X and Y, then the distance between X and M is :
(a) 10 km (b) 90 km
(c) 75 km (d) 25 km
- If P and Q continue to move between X and Y, then the ratio of distances covered by P and Q when they meet for the 5th time?
(a) 1 : 4 (b) 1 : 3
(c) 2 : 3 (d) 3 : 4
- If P and Q continue to move between X and Y, then the distance covered by P and Q together between any two consecutive meeting?
(a) 100 (b) 300
(c) 200 (d) can't be determined

Directions for questions number 17, 18 and 19: A persons P starts his journey from A and another person Q starts his journey from B , towards each other. The speeds of P and Q are 16 km/h and 25 km/h respectively and they meet at point M somewhere between A and B when they start their journey simultaneously.

Directions for questions number 22 to 27: There are two places X and Y , 200 km apart from each other. Initially two persons P and Q both are at ' X '. The speed of P is 20 km/h and speed of Q is 30 km/h. Later on they starts to move to and fro between X and Y .

22. If they starts to move between X and Y , then for the first time when they will meet each other?
 (a) after 12 hours (b) after 24 hours
 (c) after 30 hours (d) after 8 hours

23. If they meet first time at a point M somewhere between X and Y , then what is the distance travelled by P ?
 (a) 160 km (b) 150 km
 (c) 200 km (d) 210 km

24. If they meet second time each other at a point N somewhere between X and Y , then the distance travelled by Q is :
 (a) 240 km (b) 480 km
 (c) 360 km (d) none of these

25. If they meet third time each other at a point C , somewhere between X and Y , then the ratio of distances CX and CY is :
 (a) 3 : 2 (b) 1 : 3
 (c) 2 : 3 (d) 2 : 5

26. If they meet fourth time each other at a point D somewhere between X and Y , then what is the distance between D and X ?
 (a) 75 (b) 80
 (c) 150 (d) 160

27. After starting their race, they meet each other for the n^{th} time at point X , then what is the minimum possible value of n ?
 (a) 1 (b) 2
 (c) 3 (d) 5

2. **Directions for questions number 28 to 33:** A person X started 3 hours earlier at 40 km/h from a place P, then another person Y followed him at 60 km/h, started his journey at 3 O'clock, afternoon.

28. At what time will they meet to each other (or at what time Y will overtake X)?
 (a) 4:30 pm (b) 5 pm
 (c) 6 pm (d) 9 pm

29. At what time the difference between X and Y was 30 km, but before Y overtakes X?
 (a) 6:30 pm (b) 7:30 pm
 (c) 8:75 pm (d) none of these

30. At what time Y will be 30 km ahead of X, after overtaking it?
 (a) 6:45 pm (b) 7:30 pm
 (c) 10:30 pm (d) 8 pm

31. What is the distance travelled by Y to overtake X?
 (a) 180 km (b) 420 km
 (c) 320 km (d) 360 km

32. What distance should Y cover so that he may reach 360km ahead of X?
 (a) 1440 km (b) 1200 km
 (c) 920 km (d) 750 km

33. What is difference in time when X was 30 km ahead of Y and when Y was 30 km ahead of X?
 (a) 2 (b) 3
 (c) 3.5 (d) 4.25

34. A postman goes with a speed of 36 km/h what is the speed of postman in m/s?
 (a) 4.5 m/s (b) 6 m/s
 (c) 10 m/s (d) can't be determined

35. In the above question (no. 34) what is the speed in m/min?
 (a) 325 (b) 432
 (c) 360 (d) 600

36. In the above question (no. 34) what is the speed of postman in mile/h?
 (a) 22.37 (b) 30.08
 (c) 28.30 (d) 38.12

37. A train goes with a speed of 20 m/s. What is the speed of train in km/h?
 (a) 57 km/h (b) 72 km/h
 (c) 80 km/h (d) 120 km/h

38. As per the question (no. 37) what is the speed of train in km/min?
 (a) 1.2 (b) 12
 (c) 1200 (d) 120

39. A is twice fast as B and B is thrice as fast as C. The journey covered by C in 78 minutes will be covered by A in :
 (a) 12 min (b) 13 min
 (c) 15.5 min (d) none of these

40. The ratio of speeds of A is to B is 2 : 3 and therefore A takes 20 minutes less time than B takes. What is the ratio of time taken by A and B?
 (a) 2 : 3 (b) 2 : 5
 (c) 3 : 2 (d) 3 : 5

41. What is the time taken by A (in the above question)?
 (a) 1 h (b) 1.2 h
 (c) 0.6 h (d) 30 min

- (a) 6 s (b) 16 s
(c) 10 s (d) none of these
64. If a train 225 m long passes a telegraphic pole in 9 seconds, then the time taken (in seconds) by it to cross a tunnel 450 m long is :
(a) 8 s (b) 10 s
(c) 27 s (d) none of these
65. A train 350 m long is running at the speed of 36 km/h. If it crosses a tunnel in 1 minute, then the length of the tunnel (in metres) is :
(a) 200 m (b) 250 m
(c) 150 m (d) none of these
66. If a 250 m long train crosses a platform of the same length as that of the train in 25 seconds, then the speed of the train is :
(a) 150 m/s (b) 200 m/s
(c) 20 km/h (d) 72 km/h
67. Sabarmati express takes 18 seconds to pass completely through a station 162 m long and 15 seconds through another station 120 m long. The length of the Sabarmati express is :
(a) 132 m (b) 100 m
(c) 80 m (d) 90 m
68. A train 200 m long travels at the speed of 72 km/h. A man is running at 3.6 km/h in the same direction in which the train is going. The train will pass the man in :
(a) 10 s (b) $12\frac{3}{19}$ s
(c) $10\frac{10}{19}$ s (d) none of these
69. A train 350 m long is moving at the speed of 20 km/h. It will cross a man coming from the opposite direction at the speed of 1 km/h in :
(a) 27 s (b) 35 s
(c) 45 s (d) 60 s
70. The length of Lucknow mail is 120 m and that of Punjab mail is 80 m. These two trains are running in the same direction with velocities of 40 km/h and 50 km/h respectively. The time taken by them to cross each other is :
(a) 8 s (b) 72 s
(c) 11.5 s (d) 12.5 s
71. In the above question if the trains are running in opposite directions. The time taken by them to cross each other is :
(a) 8 s (b) 72 s
(c) 12.5 s (d) none of these
72. A train passes an electric pole in 10 seconds and a platform 120 m long in 18 seconds. Its length in metres is :
(a) 150 m (b) 130 m
(c) 240 m (d) 180 m
73. A 175 m long train crosses a man walking at a speed of 9 km/h in the opposite direction in 10 sec. The speed of the train (in km/h) is :
(a) 45 (b) 54
(c) 72 (d) 68
74. A train of length 100 m takes 1/6 minute to pass over another train 150 m long coming from the opposite direction. If the speed of first train is 60 km/h, the speed of the second train is :
(a) 45 km/h (b) 28 km/h
(c) 30 km/h (d) none of these
75. A train overtakes two girls who are walking in the opposite direction in which the train is going at the rate of 3 km/h and 6 km/h and passes them completely in 36 seconds and 30 seconds respectively. The length of the train (in metres) is :
(a) 120 m (b) 150 m
(c) 125 m (d) none of these
76. A coolie standing on a railway platform observes that a train going in one direction takes 4 seconds to pass him. Another train of same length going in opposite direction takes 5 seconds to pass him. The time taken (in seconds) by the two trains to cross each other will be :
(a) 35 (b) 36.5
(c) $\frac{40}{9}$ (d) none of these
77. Pushpak express leaves Lucknow at 6 am and two hours later another train Bhopal express leaves Lucknow. Both trains arrive Bhopal at 4 pm on the same day. If the difference between their speeds be 10 km/h, what is the average speeds of both the trains over entire route :
(a) 40 km/h (b) $44\frac{4}{9}$ km/h
(c) $42\frac{3}{5}$ km/h (d) none of these
- Directions for question number 78, 79:** Two trains leave Meerut at the difference of 4 hours. The first train leaves at 8 am at 40 km/h and the faster train leaves later at 60 km/h in the same direction.
78. When the faster train will overtake the slower train?
(a) 4 pm (b) 2 pm
(c) 8 pm (d) 6:30 pm
79. What is the distance from Meerut, where one train overtakes another train?
(a) 480 km (b) 420 km
(c) 360 km (d) 250 km
80. The distance between Lucknow and Delhi is 700 km. Rajdhani express starts from Delhi for the Lucknow at 60 km/h. 50 minutes later Lucknow express leaves Lucknow for Delhi on the parallel tracks at 70 km/h. How far from Lucknow will they cross each other?
(a) 250 km (b) 360 km
(c) 350 km (d) 475 km
81. Patna express travels first 560 km in 7 hours and rest 360 km in 9 hours. What is the average speed of the train?
(a) 39 km/h (b) 43 km/h
(c) 63 km/h (d) 57.5 km/h
82. Jammutavi express leaves Jammu for Kanya Kumari at 120 km/h and returns to Jammu at 80 km/h. What is the average speed of the train during the whole journey?
(a) 47.5 km/h (b) 96 km/h
(c) 38 km/h (d) 57.5 km/h
83. In the above question if the total time taken by the train is 25 hours, what is the distance between these two places?
(a) 1365.5 km (b) 1369 km
(c) 1200 km (d) can't be determined

- 101.** Abdul starts in a car from Ahmedabad towards Bangalore. After sometime he realises that he will cover only 75% of the distance in the scheduled time and he therefore doubles his speed immediately and thus manages to reach Bangalore exactly on time. Find the time after which Abdul changed his speed, given that he could have been late by 3 hours if he had not changed his speed :
- (a) 3 h (b) 4 h
(c) 5 h (d) 6 h
- 102.** A man travels the first part of his journey at 20 km/h and the next at 70 km/h, covering the entire journey at an average speed of 50 km/h. What is the ratio of the distance that he covered at 20 km/h to that he covered at 70 km/h?
- (a) 4 : 21 (b) 3 : 22
(c) 1 : 4 (d) 3 : 5
- 103.** Anjali fires two bullets from the same place at an interval of 6 minutes but Bhagwat sitting in a car approaching the place of firing hears the second fire 5 minute 32 seconds after the first firing. What is the speed of car, if the speed of sound is 332 m/s?
- (a) 56 m/s (b) 102 m/s
(c) 28 m/s (d) 32 m/s
- 104.** A car crosses a man walking at 6 km/h. The man can see the things upto 450 m only in one direction due to fog. He sees the car which was going in the same direction for 4.5 minutes. What is the speed of the car?
- (a) 9 km/h (b) 12 km/h
(c) 12.5 km/h (d) 15 km/h
- 105.** A man takes 4 h 20 minutes in walking to a certain place and riding back. If he walk on both sides he loses 1 h. The time he would take by riding both ways is :
- (a) 2 h 20 min (b) 3 h 20 min
(c) 2 h (d) 4 h 40 min
- 106.** A train met with an accident 120 km from station A. It completed the remaining journey at $5/6$ of its previous speed and reached 2 hours late at station B. Had the accident taken place 300 km further, it would have been only 1 hour late? What is the speed of the train?
- (a) 100 km/h (b) 120 km/h
(c) 60 km/h (d) 50 km/h
- 107.** For the above question what is the total distance between A and B ?
- (a) 480 km (b) 520 km
(c) 600 km (d) 720 km
- 108.** The wheel of an engine of 300 cm in circumference makes 10 revolutions in 6 seconds. What is the speed of the wheel (in km/h)?
- (a) 18 (b) 20
(c) 27 (d) 36
- 109.** A man can row downstream at 12 km/h and upstream at 8 km/h. What is the speed of man in still water?
- (a) 12 km/h (b) 10 km/h
(c) 8 km/h (d) 9 km/h
- 110.** A man can row upstream at 15 km/h and downstream at 21 km/h. The speed of water current of the river is :
- (a) 8 km/h (b) 6 km/h
(c) 3 km/h (d) 5 km/h

- 111.** A boat moves downstream at 1 km in 5 minutes and upstream at 1 km in 12 minutes. What is the speed of current?
- (a) 4.5 km/h (b) 3.5 km/h
(c) 2 km/h (d) 2.5 km/h
- 112.** A man rows downstream 60 km and upstream 36 km, taking 4 hours each time. The speed of the man is :
- (a) 15 km/h (b) 16 km/h
(c) 8 km/h (d) 12 km/h
- 113.** A man can row 5 km/h in still water. If the rate of current is 1 km/h, it takes $\frac{5}{4}$ hours to row to a place and back. How far is the place?
- (a) 2 km (b) 2.5 km
(c) 3 km (d) 4 km
- 114.** A man can swim 5 km/h in still water. If the speed of current be 3 km/h, the time taken by him to swim to a place 16 km upstream and back is :
- (a) 8 h (b) 7.5 h
(c) 6.66 h (d) 10 h
- 115.** A boat covers 48 km upstream and 72 km downstream in 12 hours, while it covers 72 km upstream and 48 km downstream in 13 hours. The speed of stream is :
- (a) 2 km/h (b) 2.2 km/h
(c) 2.5 km/h (d) 4 km/h
- 116.** A motor boat takes 2 hours to travel a distance of 9 km downstream and it takes 6 hours to travel the same distance against the current. The speed of the boat in still water and that of the current (in km/h) respectively are :
- (a) 6, 5 (b) 3, 1.5
(c) 8, 5 (d) 9, 3
- 117.** A man can row 15 km/h in still water and he finds that it takes him twice as much time to row up than as to row down the same distance in the river. The speed of the current (in km/h) is :
- (a) 6 km/h (b) 6.5 km/h
(c) 4.5 km/h (d) 5 km/h
- 118.** A motor boat takes 12 hours to go downstream and it takes 24 hours to return the same distance. What is the time taken by boat in still water?
- (a) 15 h (b) 16 h
(c) 8 h (d) 20 h
- 119.** The speed of a boat in upstream is $2/3$ that of downstream. Find the ratio of speed of boat in still water and to the average speed of boat in downstream and upstream?
- (a) $\frac{24}{25}$ (b) $\frac{25}{24}$
(c) $\frac{5}{12}$ (d) none of these
- 120.** The difference between downstream speed and upstream speed is 3 km/h and the total time taken during upstream and downstream is 3 hours. What is the downstream speed, if the downstream and upstream distance are 3 km each?
- (a) 2.5 km/h (b) 4.33 km/h
(c) 4 km/h (d) 3.3 km/h

121. A boat which sails at 10 km/h in still water starts chasing, from 10 km behind, another one which sails at 4 km/h in the upstream direction. After how long will it catchup if the stream is flowing at 2 km/h :

(a) 4 h (b) 2.5 h
(c) 2 h (d) 3.5 h

Directions for question number 122 and 123 : A motor boat went downstream for 120 km and immediately returned. It took the boat 15 hours to complete the round trip. If the speed of the river were twice as high, the trip downstream and back would take 24 hours.

122. What is the speed of the boat in still water?

(a) 20 km/h (b) 18 km/h
(c) 15 km/h (d) 16 km/h

123. What is the speed of the stream?

(a) 3.5 km/h (b) 4 km/h
(c) 6 km/h (d) 8 km/h

124. A boat sails 15 km of a river towards upstream in 5 hours. How long will it take to cover the same distance downstream, if the speed of current is one-fourth the speed of the boat in still water :

(a) 1.8 h (b) 3 h
(c) 4 h (d) 5 h

125. A boat takes 5 hours more while going back in upstream than in downstream. If the distance between two places is 24 km and the speed of boat in still water be 5.5 km/h. What must be the speed of boat in still water so that it can row downstream, 24 km, in 4 hours?

(a) 1.5 km/h (b) 3.5 km/h
(c) 4.5 km/h (d) 3 km/h

126. A boat takes 7 hours to go from P to R, through a midpoint Q, but it takes 8 hours to go from P to Q and then return from Q to P. How long it would take to go from R to P?

(a) 7 h (b) 8 h
(c) 9 h (d) none of these

127. Mallah can row 40 km upstream and 55 km downstream in 13 h and 30 km upstream and 44 km downstream in 10 hours. What is the speed of Mallah in still water?

(a) 6 km/h (b) 12 km/h
(c) 3 km/h (d) 8 km/h

Directions for question number 128-129 : In a kilometre race, A can give B a start of 20 m and also in a half kilometre race C beats A by 50 m.

128. If A, B and C run a 2 km race, what is the difference between the distances covered by the two losers, when the winner finishes the race?

(a) 64 m (b) 36 m
(c) 32 m (d) 58 m

129. B and C run a half km race, who should give a start to the slower runner and of how many metres so that they both finish the race at the same time?

(a) C, 59 m (b) B, 34 m
(c) C, 48 m (d) B, 56 m

130. In a 1600 m race, A beats B by 80 m and C by 60 m. If they run at the same time then by what distance will C beat B in a 400 m race?

(a) $5\frac{15}{77}$ m (b) $5\frac{20}{76}$ m
(c) $15\frac{5}{77}$ m (d) none of these

131. Aman can run a distance in 190 seconds and Shakti can run the same distance in 200 seconds. If they start together, by what distance Aman can beat Shakti in 1 km race?

(a) 48 m (b) 25 m
(c) 24 m (d) 50 m

132. A runs $\frac{7}{4}$ times as fast as B. If A gives B a start of 300 m, how

far must the winning post be if both A and B have to end the race at same time?

(a) 1400 m (b) 700 m
(c) 350 m (d) 210 m

133. A beats B by 100 m in a race of 1200 m and B beats C by 200 m in a race of 1600 m. Approximately by how many metres can A beat C in a race of 9600 m?

(a) 1600 m (b) 1800 m
(c) 1900 m (d) 2400 m

134. In a 1000 m race Ameesha gives a headstart of 100 m to Bipasha and beats her by 200 m. In the same race Ameesha gives a headstart of 100 m to Celina and beats her by 300 m. By how many metres would Bipasha beat Celina in a 50 m race?

(a) 6.66 m (b) 7.143 m
(c) 8 m (d) none of these

135. In a 1000 metres race Ravi gives Vinod a start of 40 m and beats him by 19 seconds. If Ravi gives a start of 30 seconds then Vinod beats Ravi by 40 m. What is the ratio of speed of Ravi to that of Vinod?

(a) 4 : 5 (b) 6 : 5
(c) 3 : 8 (d) 5 : 4

136. In a race, the man who came two places ahead of the last man finished one place ahead of the man who came three places behind the man just ahead of the one who stood second. How many men finished the race?

(a) 6 (b) 5
(c) 4 (d) 8

137. Vinay and Versha run a race with their speeds in the ratio of 5 : 3. They prefer to run on a circular track of circumference 1.5 km. What is the distance covered by Vinay when he passes Versha for the seventh time?

(a) 25.25 km (b) 26.25 km
(c) 132 m (d) none of these

138. A gives both B and C a start of 60 m in a 1500 m race. However, while B finishes with him, C is 15 m behind them when A and B cross the finishing line. How much start can B give C for the 1500 m race course?

(a) $7\frac{6}{23}$ m (b) $15\frac{5}{8}$ m
(c) $7\frac{11}{16}$ m (d) $5\frac{5}{24}$ m

139. In a 600 m race Prabhat has a start of 200 m and the ratio of speeds of Prabhat and Nishith is 4 : 5, then the distance by which Prabhat wins by :

(a) 100 m (b) 80 m
(c) 120 m (d) none of these

LEVEL (2)

Directions for question number 1-4 : Aishwarya is going to cover a distance of 360 km from Ambala to Khandala. The first one-third of the distance she covers on a cycle. The second one-third she covers by an auto-rickshaw and the remaining distance she travels by car. The average speed of the journey by a car is 5 times the average speed by cycle and 20 km/h more than the average speed by auto-rickshaw, but she took 1 hour more by auto-rickshaw than by car.

Ambala is 1080 km and all three meet at the same point on the way, at same time, then at what time did Rani leave Kolkata?

- (a) 7 am (b) 8 am
 (c) 7:30 am (d) 10 am

6. A passenger sitting in a train of length l m, which is running with speed of 60 km/h passing through two bridges, notices that he crosses the first bridge and the second bridge in time intervals which are in the ratio of 7 : 4 respectively. If the length of first bridge be 280 m, then the length of second bridge is :
 (a) 490 m (b) 220 m
 (c) 160 m (d) can't be determined

7. Pathik and Rahi started from two places Andheri and Bhavnagar towards Bhavnagar and Andheri respectively at 8 : 20 am. The speeds of Pathik and Rahi are in the ratio of 4 : 5. They meet at Chandni Chowk, somewhere between Andheri and Bhavnagar, spent some-time together enjoyed coffee and burger and then both started towards their destination at 9 : 27 am. If Pathik reaches Bhavnagar at 10 : 32 am, how much time did they spend together?
 (a) 8 min (b) 12 min
 (c) 15 min (d) can't be determined

8. A train with 120 wagons crosses Arjun who is going in the same direction, in 36 seconds. It travels for half an hour from the time it starts overtaking the Arjun (he is riding on the horse) before it starts overtaking Srikrishna (who is also riding on his horse) coming from the opposite direction in 24 seconds. In how much time (in seconds) after the train has crossed the Srikrishna do the Arjun meets to Srikrishna?
 (a) 3560 sec (b) 3600 sec
 (c) 3576 sec (d) can't be determined

9. Kareena and Shahid start from Kurla and Worli towards Worli and Kurla respectively, at the same time. After they meet at Shantakruz on the way from Kurla to Worli, Kareena reduces her speed by 33.33% and returns back to Kurla and Shahid increases his speed by 33.33% and returns back to Worli. If Kareena takes 2 hours for the entire journey, what is the time taken by Shahid for the entire journey?
- (a) 96 min (b) 84 min
(c) 168 min (d) can't be determined
10. Due to the technical snag in the signal system two trains start approaching each other on the same rail track from two different stations, 240 km away from each other. When the train starts a bird also starts moving to and fro between the two trains at 60 km/h touching each time each train. The bird is initially sitting on the top of the engine of one of the trains and it moves so till these trains collide. If these trains collide one and a half hour after the start, then how many kilometres bird travells till the time of collision of trains?
- (a) 90 km (b) 130 km
(c) 120 km (d) none of these
11. Einstein walks on an escalator at a rate of 5 steps per second and reaches the other end in 10 seconds. While coming back, walking at the same speed he reaches the starting point in 40 seconds. What is the number of steps on the escalator?
- (a) 40 (b) 60
(c) 120 (d) 80
12. A girl while walking diametrically across a semicircular playground, takes 3 minutes less than if she had kept walking round the circular path from A to B. If she walks 60 metres a minute, what is the diameter of the play ground :
- (a) 60 m (b) 48 m
(c) 84 m (d) 315 m
13. Two trains start simultaneously from two stations Howrah and Bandra, respectively towards each other on the same track. The distance between the two stations is 560 km and the speed of trains are 30 and 40 km/h. Simultaneously with the trains, a sparrow sitting on the top of one of the train starts towards the other and reverses its direction on reaching the other train and so on. If the speed of sparrow is 80 km/h then the distance that the sparrow flies before being crushed between the train is :
- (a) 70 km (b) 560 km
(c) 640 km (d) 650 km
14. A surveillance plane is moving between two fixed places Pukhwara and Kargil at 120 km/h. The distance between two places is 600 km. After 18 hour what will be the distance between the Kargil and its position if it is starts moving from Pukhwara?
- (a) 360 km (b) 300 km
(c) 240 km (d) none of these
15. The speed of a car during the second hour of its journey is thrice that in the first hour. Also its third hours speed is the average speed of the first two hours. Had the car travelled at the second hours speed during all the first three hours, then it would have travelled 150 km more. Find the percentage reduction in time in the second case for the first three hours :
- (a) $33\frac{1}{3}\%$ (b) 40%
(c) 25% (d) 50%
16. There are three runners Tom, Dick and Harry with their respective speeds of 10 km/h, 20 km/h and 30 km/h. They are initially at P and they have to run between the two points P and Q which are 10 km apart from each other. They start their race at 6 am and end at 6 pm on the same day. If they run between P and Q without any break, then how many times they will be together either at P and Q during the given time period?
- (a) 5 (b) 7
(c) 4 (d) 12
- Directions for question number 17 and 18 :** Arjun and Srikrishna go by chariot from Mathura to Kurukshetra which is on the way to Hastinapur. Abhimanyu goes from Hastinapur to Kurukshetra. The distance between Mathura to Hastinapur is 700 km and the distance between Hastinapur and Kurukshetra is 300 km. Speed of Arjun and Srikrishna's chariot is 25 km/h and speed of Abhimanyu is 10 km/h. All the three persons start their journey at 10 am. After travelling some miles Srikrishna sees Duryodhan going (by riding on his horse) at 20 km/h to Kurukshetra. Arjun and Srikrishna go ahead meet Abhimanyu and pick him up. Then they return immediately to Kurukshetra and thus all the four reach at the same time.
17. What is the total distance travelled by Arjun?
- (a) 400 (b) 500
(c) 600 (d) can't be determined
18. What is the total time taken to reach Kurukshetra?
- (a) 10 h (b) 15 h
(c) 18 h (d) 24 h
19. Priyanka, Akshay and Salman started out on a journey to watch the newly released movie "Mujhse Shaadi Karogi", which was being shown at wave cine-multiplex. The multiplex was 120 km away from their starting point of journey. Priyanka and Salman went by car at the speed of 50 km/h, while Akshay travelled by Tonga (horse cart) at 10 km/h. After a certain distance Salman got off and travelled the rest distance by another Tonga at 10 km/h, while Priyanka went back for Akshay and reached the destination at the same time that Salman arrived. The number of hours required for the trip was :
- (a) 4 h (b) 5 h
(c) 4.8 h (d) can't be determined
- Directions for question number 20 and 21 :** Ajai and Kajol start towards each other at the same time from Barabanki and Fatehpur for their destinations Fatehpur and Barabanki respectively which are 300 km apart. They meet each other 120 km away from Barabanki.
20. Shahrukh starts from Barabanki to Fatehpur, 1 hour after Ajai starts. Shahrukh meets Kajol 1.5 hours after Shahrukh starts. If the speed of Shahrukh is atleast 20 km/h faster than the speed of Kajol.
- Which of the following statements is true?

- (a) The minimum possible speed of Ajai is 45 km/h
 - (b) The maximum possible speed of Ajai is 45 km/h
 - (c) The minimum possible speed of Kajol is 60 km/h
 - (d) The maximum possible speed of Kajol is 60 km/h

21. What is the minimum speed of Shahrukh to overtake Ajai, before he meets Kajol? (Use the data from previous question, if necessary)

Directions for question number 22-24 : Raghupati goes at a speed of 60 km/h. Raghav goes at a speed of 36 km/h. Raja Ram can go from Azamgarh to Barelley in 2 hours. The distance between Azamgarh to Barelley is equal to the distance between Azamgarh to Chandoli. Raghav takes the same time travelling from Barelley to Azamgarh as from Barelley to Chandoli at his regular speed which is twice the speed of Raja Ram.

22. What is the distance between Azamgarh and Chandoli?

23. How much time will Raghupati take to complete a round trip of the three cities?

24. If Raghupati and Raja Ram travel towards each other from Barelley and Chandoli respectively, how far from Barelley will they meet each other?

- (a) $\frac{60}{13}$ (b) $27 \frac{9}{13}$ km
 (c) $37 \frac{9}{13}$ (d) $\frac{360}{9}$

Directions for question number 25-26 : Mohan, Namit and Pranav travel from Shantipur to Hulchulpur. They have a two seater bike which can be driven by only Mohan. It is known that due to very stringent traffic rules only two persons can ride at a time. Hulchulpur is 180 km away from Shantipur. All of them can walk at 6 km/h, but reach to Hulchulpur simultaneously also they started their journey simultaneously.

25. If the speed of the bike is 36 km/h, then what is the total distance that the bike travels?

26. If the speed of the bike is 42 km/h, then what is the shortest possible time in which all three of them can complete the journey?

- (a) $7\frac{1}{3}$ h (b) $9\frac{4}{7}$ h
 (c) $9\frac{3}{7}$ h (d) can't

27. While walking down on the pavements of New York city, I notice that every 20 minute there is a city bus coming in the opposite direction and every 30 minute there is a city bus overtaking me from behind. What is the time gap between one city bus passing a stationary point known as Local Bus Stop beside the route and the immediately next city bus in the same direction passing the same stationary point?

28. Abhinav and Brijesh start from Allahabad and Barabanki respectively with uniform velocities. Abhinav is headed towards Barabanki and Brijesh towards Allahabad and both cities are 600 km apart. Abhinav rests whenever Brijesh is on the move and Brijesh rests whenever Abhinav is on the move. Abhinav's speed is 25 km/h and Brijesh's speed is 30 km/h. If Abhinav starts first and reaches Barabanki in 36 hours, then find the least time that Brijesh would take to reach Barabanki.

29. A man can cross a downstream river by steamer in 40 minutes and same by boat in 1 hour. If the time of crossing the river in upstream direction by steamer is 50% more than downstream time by the steamer and the time required by boat to cross the same river by boat in upstream is 50% more than the time required in downstream by boat. What is the time taken for the man to cross the river downstream by steamer and then return to same place by boat half the way and by steamer the rest of the way?

Directions for question number 30 and 31 : Awadh express and Bokaro express start simultaneously from Lucknow and Jamshedpur towards each other and continuously shuttle between these two places. Every time these trains meet each other, they turn back after exchanging their respective speeds. the initial ratio of their speeds is 2 : 1.

30. What is the number of distinct places at which they will meet?

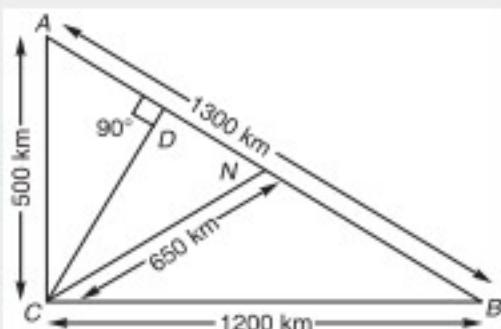
31. Let these two trains first time meet at Patna, then what is the ratio of distances covered by Awadh express and Bokaro express till they meet for the third time at the same place Patna :

32. Mahindra starts a journey for his office, which is in the north east of his home. An hour after starting meets with a minor accident. He takes one hour in resuming his journey. After that he proceeds at $\frac{5}{6}$ th of his former speed and arrives at the office 1 hour 36 minutes late than the scheduled time. Had the accident occurred 80 kms further from the actual place of accident, he would have arrived 1 hour 20 minutes beyond the scheduled time. What is the distance between his office and his home?

33. A soldier fired two bullets at an interval of 335 seconds moving at a uniform speed v_1 . A terrorist who was running ahead of the soldier in the same direction, hears the two shots at an interval of 330 seconds? If the speed of sound is 1188 km/h, then who is the faster and by how much?

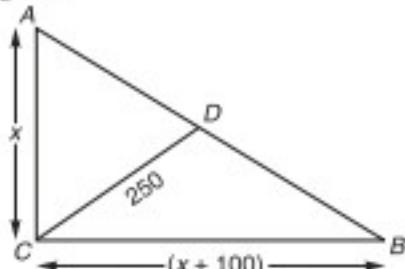
- (a) Soldier, 22 km/h (b) Terrorist, 25 km/h
 (c) Soldier, 18 km/h (d) Terrorist, 20 km/h
34. A hunter fired two shots from the branch of a tree at an interval of 76 seconds. A tiger separating too fast hears the two shots at an interval of 83 seconds. If the velocity of the sound is 1195.2 km/h, then find the speed of tiger?
 (a) 112.8 km/h (b) 100.8 km/h
 (c) 80.16 km/h (d) none of these
35. A man goes to the fair in Funcity with his son and faithful dog. Unfortunately man misses his son which he realises 20 minutes later. The son comes back towards his home at the speed of 20 m/min and man follows him at 40 m/min. The dog runs to the son (child) and comes back to the man (father) to show him the direction of his son. It keeps moving to and fro at 60 m/min between son and father, till the man meets the son. What is the distance travelled by the dog in the direction of the son?
 (a) 800 m (b) 1675 m
 (c) 848 m (d) 1000 m
36. Amarnath express left Amritsar for Gorakhpur. Two hours later Gorakhnath express left from Amritsar to Gorakhpur. Both trains reached Gorakhpur simultaneously. If Amarnath express had started from Amritsar and Gorakhnath express had started from Gorakhpur at the same time and travelled towards each other they would meet in 1 h 20 min. Find the time taken by Amarnath express to travel from Amritsar to Gorakhpur (in hours):
 (a) 2 (b) 4
 (c) 5 (d) 6
37. Akbar and Birbal set out at the same time to walk towards each other respectively from Agra and Banaras 144 km apart. Akbar walks at the constant speed of 8 km/h, while Birbal walks 4 km in the first hour, 5 km in the second hour, 6 km in the third hour and so on. Then the Akbar and Birbal will meet:
 (a) in 6 h
 (b) in 8 h
 (c) midway between Agra and Banaras
 (d) 80 km away from Banaras
38. A tiger is 50 of its own leaps behind a deer. The tiger takes 5 leaps per minute to the deer's 4. If the tiger and the deer cover 8 m and 5 m per leap respectively, what distance will the tiger have to run before it catches the deer?
 (a) 600 m (b) 700 m
 (c) 800 m (d) 1000 m
39. Soniya and Priyanka started from Amethi and Bellari for Bellari and Amethi, which are 645 km apart. They meet after 15 hours. After their meeting, Sonia increased her speed by 3 km/h and Priyanka reduced her speed by 3 km/h, they arrived at Bellari and Amethi respectively at the same time. What is their initial speeds?
 (a) 24 km/h and 30 km/h (b) 25 km/h and 18 km/h
 (c) 18 km/h and 21 km/h (d) 20 km/h and 23 km/h
40. Den Bosch and Eastbourne are two famous cities 300 km apart. Maradona starts from Den Bosch at 8 : 24 am. An hour later Pele starts from Den Bosch. After travelling for 1 hour, Pele reaches Nottingham that Maradona had passed 40 minutes earlier. Nottingham falls on the way from Den Bosch to Eastbourne. If Pele and Maradona just reaches Eastbourne at the same time, what are the speeds of the Maradona and Pele respectively?
 (a) 100 km/h, 125 km/h (b) 60 km/h, 80 km/h
 (c) 60 km/h, 75 km/h (d) 75 km/h, 100 km/h
41. A thief sees a jeep at a distance of 250 m, coming towards him at 36 km/h. Thief takes 5 seconds to realise that there is nothing but the police is approaching him by the jeep and start running away from police at 54 km/h. But police realise after 10 seconds, when the thief starts running away, that he is actually a thief and gives chase at 72 km/h. How long after thief saw police did police catchup with him and what is the distance police had to travel to do so?
 (a) 50 s, 1000 m (b) 65 s, 1150 m
 (c) 65 s, 1300 m (d) 45 s, 1050 m
42. Inspired by the 'Golden quadrilateral project' UP Government recently accomplished a diamond triangular project. Under this project the State Government laid down 6 lane roads connecting three cities Ayodhya, Banaras and Chitrakoot, which are equally separated from each other i. e., in terms of geometry they form an equilateral triangle. Angad and Bajrang start simultaneously from Ayodhya and Banaras respectively, towards Chitrakoot. When Angad covers 100 kms, Bajrang covers such a distance that the distance between Angad and Bajrang makes 90° angle with the road joining Banaras and Chitrakoot. When Bajrang reaches Chitrakoot, Angad is still 150 km away from Chitrakoot. What is the distance between Ayodhya and Banaras?
 (a) 250 km (b) 450 km
 (c) 300 km (d) none of these
43. Two trains Ajanta express and Barouni express simultaneously started on two parallel tracks from Meerut to Nagpur, which are 390 km apart. The ratio of the speed of Ajanta express and Barouni express is 6 : 7. After how long (in kms) travelling, Barouni express exchanges the speed with Ajanta express so that both the trains reach at their destination simultaneously:
 (a) 150 km (b) 190 km
 (c) 210 km (d) can't be determined
44. In a circus there was a leopard and a tiger walking in the two different rings of same radii. There I observed that when leopard moved 3 steps, tiger moved 5 steps in the same time, but the distance traversed by leopard in 5 steps is equal to the distance traversed by tiger in 4 steps. What is the number of rounds that a leopard made when tiger completed 100 rounds?
 (a) 120 (b) 48
 (c) 75 (d) none of these

Directions for question number 45-48 : In the following figure the route is shown which is followed by Professor Jai and Professor Jaya, who are visiting faculty at IIM-A and IIM-B respectively. A, B denote IIM-A and IIM-B respectively and C denotes the residence of Prof. Jai and Prof. Jaya. They leave home for classes at the same time and their driving speeds are $\frac{500}{13}$ km/h and $\frac{1200}{13}$ km/h respectively. Also they finish the classes at the same time to reach home.



The path adopted by Jai and Jaya is $CADC$ and $CBDC$ respectively. Prof. Jai and Prof. Jaya are husband and wife respectively.

45. If both of them start and finish the classes at the same time, then who returned home earlier than other, if no one of them halts for anywhere in the route and they just leave the institution as soon as they finish the lectures?
- Prof. Jai
 - Prof. Jaya
 - Return at the same time
 - Can't be determined
46. In the shown figure N and D denotes Noida and Delhi respectively, who returned home late and by how much time, if Jaya turned from Noida instead of Delhi :
- Jai, 9 h 10 min
 - Jaya, 9 h 50 min
 - Jai, 2 h 55 min
 - Jai, 16 h 10 min
47. In the above question how many per cent time Jaya saved in going via Noida of the total time taken previously :
- 10%
 - 25%
 - 50%
 - 17%
48. If Mrs. Jaya wants to watch the premier show of a movie at Wave Cinema in Noida while returning from institute through BNC. When will she return home given that she spends total time 3 hours at wave cinema?
- at the same time as normal
 - 5 min late than her husband
 - at the same time when her husband returns
 - can't be determined
49. Preetam and Devi start running a race on the given track as shown in figure.



Where AC and BC are mutually perpendicular and CD is the median of triangular paths ABC . BC is 100 km longer than that of AC , again CD is 250 km. The speeds of Preetam and Devi are 30 km/h and 40 km/h, initially and their respective paths of running are $CADC$ and $CBDC$. After how much time they reverse their speeds so that they return C at the same time?

- $\frac{50}{7}$ h
- $\frac{120}{7}$ h
- $\frac{80}{11}$ h
- none of these

Directions for question number 50, 51, and 52 : The markets M_1, M_2, M_3, \dots etc of Vyapaar city are lying besides the circular paths P_1, P_2, P_3, \dots etc. All the circular paths are concentric at centre 'O' and their distances are 1 km, 2 km, 3 km, ... etc from the centre 'O' respectively. At the centre 'O' there is a "Khoob Khao" tiffin agency which supplies the tiffins to all the markets M_1, M_2, M_3, \dots etc. A tiffin carrier starts from 'O' goes directly east of the shop and then on reaching the circular path it moves 1 km in counter clock direction on it. After completing its 1 km distance on P_1 the carrier moves to P_2 in the radial direction. Then it goes 2 km on P_2 . Similarly 3 km on P_3 and 4 km on P_4 etc in counter clock direction moving radially from P_2 to P_3 and P_3 to P_4 etc and motion of the carrier continued in this manner till it reaches exactly in the east direction.

50. After reaching east of the shop it can't move on further than the given distance on the current path. For how many markets can it supply its tiffins directly?
- 4
 - 5
 - 7
 - can't be determined
51. The total distance covered by the carriers in providing the tiffins from centre 'O' to the last point in one way only is :
- 30 km
 - 28 km
 - 35 km
 - none of these
52. The ratio of distances covered on the circular path P_2 to that on the last path, where the carrier reaches directly eastward of its shop is :
- 1 : 1
 - 2 : 7
 - $2 : \pi$
 - none of these

Directions for question number 53-57 : A train enters into a tunnel AB at A and exits at B . A jackal is sitting at O in another by passing tunnel AOB , which is connected to AB at A and B , where OA is perpendicular to OB . A cat is sitting at P inside the tunnel AB making the shortest possible distance between O and P , such that $AO : PB = 30 : 32$. When a train before entering into the tunnel AB makes a whistle (or siren) somewhere before A , the jackal and cat run towards A , they meet with accident (with the train) at the entrance A . Further if the cat moves towards B instead of A it again meets with accident at the exit of the tunnel by the same train coming from the same direction.

53. What is the ratio of speeds of jackal and cat?
- 4 : 3
 - 5 : 3
 - 1 : 1
 - can't be determined
54. The ratio of speeds of jackal is to train is :
- 5 : 1
 - 3 : 5
 - 1 : 5
 - can't be determined
55. If jackal moves towards OPA , it will meet with train at M_1 then AM_1 is :
- 20 km
 - 16 km
 - 10 km
 - can't be determined
56. If jackal moves towards OPB and cat moves towards POA who will not meet with accident with the train?
- Jackal
 - Cat
 - Both (a) and (b)
 - Can't be determined
57. The ratio of time taken by cat and jackal in moving OPA and PBO respectively given that they do not meet with accident :
- 1 : 1
 - 3 : 4
 - 5 : 4
 - none of these

58. A candle of 6 cm long burns at the rate of 5 cm in 5 h and another candle of 8 cm long burns at the rate of 6 cm in 4 h. What is the time required by each candle to remain of equal lengths after burning for some hours, when they start to burn simultaneously with uniform rate of burning?
- (a) 1 h (b) 1.5 h
(c) 2 h (d) none of these
59. Two boats start at the same instant to cross a river W metre wide. The faster boat reaches the other bank and returns back immediately. What are the distances travelled by them when they meet, where the speeds of these boats are b_1 & b_2 ?
- (a) $\frac{2W}{(b_1 + b_2)}, \frac{2W}{(b_1 - b_2)}$
(b) $\frac{2W}{(b_1 + b_2)} b_1$ and $\frac{2W}{(b_1 + b_2)} b_2$
(c) $\frac{W}{(b_1 + b_2)} b_1, \frac{W}{(b_1 + b_2)} b_2$
(d) data insufficient
60. Mariya was travelling in her boat when the wind blew her hat off and the hat started floating back downstream. The boat continued to travel upstream for twelve more minutes before Mariya realized that her hat had fallen off and turned back downstream. She caught up with that as soon as it reached the starting point. Find the speed of river if Mariya's hat flew off exactly 3 km from where she started :
- (a) 5 km/h (b) 6 km/h
(c) 7.5 km/h (d) can't be determined
61. Akbar, Birbal and Chanakya run around a circular track of length 500 m. Akbar and Birbal run with the speeds of 15 m/s and 20 m/s in the same direction respectively and Chanakya being very intelligent run in the opposite direction with a speed of 25 m/s. If all three of them start at the same time, then :
- (a) Akbar meets Chanakya more frequently than Birbal does
(b) Akbar and Chanakya meets as frequently as Birbal and Chanakya
(c) Akbar meets Birbal least frequently
(d) Nothing can be concluded
62. Arun and Barun run with the speeds of 30 m/s and 20 m/s around a circular track of 600 m. They participate in a 3000 m race. What is the distance covered by Arun when he passes Barun for the 5th time?
- (a) 2200 m (b) 2250 m
(c) 2850 m (d) none of these
63. Akkal and Bakkal are running on a circular track of radius 175 metres. Akkal can complete a round in 100 seconds and the speed of Bakkal is twice the speed of Akkal. They started simultaneously towards each other from two points 350 metres diametrically opposite on the circular path. If they first meet at a point they called it love point, which is between the two points P and Q from where they have started their race, after how much time from the start do they meet at love point for the third time?
- (a) $218\frac{2}{5}$ s (b) $216\frac{2}{3}$ s
(c) 221 s (d) none of these
64. Arti and Barkha start swimming towards each other from the deep end and shallow end respectively of a swimming pool in Funcity. They start their swimming simultaneously in the length of 300 m pool. The ratio of their speeds is 1 : 2 respectively. Each swimmer rests for 6 seconds once she reaches the other end and starts swimming back. Where will they meet for the second time in the still water of swimming pool?
- (a) 30 m from the shallow end
(b) at the shallow end
(c) at the deepend
(d) can't be determined
65. A and B runs around a circular track. A beats B by one round or 10 minutes. In this race, they had completed 4 rounds. If the race was only of one round, find the A's time over the course :
- (a) 8 min (b) 7.5 min
(c) 12.5 min (d) 12 min
66. A, B and C participated in a race. A covers the same distance in 49 steps, as B covers in 50 steps and C in 51 steps. A takes 10 steps in the same time as B takes 9 steps and C takes 8 steps. Who is the winner of the race?
- (a) A (b) B
(c) C (d) can't be determined
67. Shambhu drives his car very fast at 360 m/s. Moving ahead for some hours he finds some problem in headlights of the car. So he takes 20 seconds in changing the bulb of the headlight by stopping the car. Mean while he notices that another car which was 400 m back is now 200 m ahead of his car. What is the speed of this car?
- (a) 100 km/h (b) 92 km/h
(c) 108 km/h (d) 300 km/h
68. Two persons start from the opposite ends of a 90 km straight track and run to and fro between the two ends. The speed of first person is 30 m/s and the speed of other is $125/6$ m/s. They continue their motion for 10 hours. How many times they pass each other?
- (a) 10 (b) 9
(c) 12 (d) none of these
69. At what time after 3 : 10 am, the acute angle made by the minute and hour-hand is double to that of at 3 : 10 am, for the first time?
- (a) 4 h 43 min (b) 3 h 48 min
(c) $3\frac{320}{11}$ min (d) none of these
70. If the two incorrect watches are set at 12 : 00 noon at correct time, when will both the watches show the correct time for the first time given that the first watch gains 1 min in 1 hour and second watch loses 4 min in 2 hours :
- (a) 6 pm, 25 days later
(b) 12 : 00 noon, 30 days later
(c) 12 noon, 15 days later
(d) 6 am 45 days later
71. Rajeev and Sanjeev are too close friends. Rajeev's watch gains 1 minute in an hour and Sanjeev's watch loses 2 minutes in an hour. Once they set both the watches at 12 : 00 noon, with my correct watch. When will the two incorrect watches of Rajeev and Sanjeev show the same time together?
- (a) 8 days later (b) 10 days later
(c) 6 days later (d) can't be determined
72. At a railway station a 24 hour watch loses 3 minutes in 4 hours. If it is set correctly on Sunday noon when will the watch show the correct time?
- (a) 6 pm after 40 days (b) 12 noon after 75 days
(c) 12 pm after 100 days (d) 12 noon after 80 days

73. A swiss watch is being shown in a museum which has a very peculiar property. It gains as much in the day as it loses during night between 8 pm to 8 am. In a week how many times will the clock show the correct time?
 (a) 6 times (b) 14 times
 (c) 7 times (d) 8 times
74. A wrist watch which is running 12 minutes late on a Sunday noon is 16 minutes ahead of the correct time at 12 noon on the next Sunday. When is the clock 8 minutes ahead of time?
 (a) Thursday 10 am (b) Friday noon
 (c) Friday 8 pm (d) Tuesday noon
75. A clock loses 2 minutes in an hour and another clock gains 2 minutes in every 2 hours. Both these clocks are set correctly at a certain time on Sunday and both the clocks stop simultaneously on the next day with the time shown being 9 am and 10 : 06 am. What is the correct time at which they stopped?
 (a) 9 : 54 am (b) 9 : 44 pm
 (c) 9 : 46 am (d) 9 : 44 am
76. David sets his watch at 6 : 10 am on Sunday, which gains 12 minutes in a day. On Wednesday if this watch is showing 2 : 50 pm. What is the correct time?
 (a) 1 : 50 pm (b) 2 : 10 pm
 (c) 2 : 30 pm (d) 3 : 30 pm
77. Ramu purchased a second hand Swiss watch which is very costly. In this watch the minute-hand and hour hand coincide

- after every $65 \frac{3}{11}$ minutes. How much time does the watch lose or gain per day?
 (a) 4 min (b) 5 min
 (c) 4 min, 20 sec (d) none of these
78. My watch was 8 minutes behind at 8 pm on Sunday but within a week at 8 pm on Wednesday it was 7 minutes ahead of time. During this period at which time this watch has shown the correct time :
 (a) Tuesday 10 : 24 am
 (b) Wednesday 9 : 16 pm
 (c) It cannot show the correct time during this period
 (d) None of the above
79. Out of the following four choices which does not show the coinciding of the hour hand and minute-hand :
 (a) 3 : 16 : 2 (b) 6 : 32 : 43
 (c) 9 : 59 : 05 (d) 5 : 27 : 16
80. Kumbhakarna starts sleeping between 1 am and 2 am and he wakes up when his watch shows such a time that the two hands (i.e., hour-hand and minute-hand) interchange the respective places. He wakes up between 2 am and 3 am on the same night. How long does he sleep?
 (a) $55 \frac{5}{13}$ min (b) $110 \frac{10}{13}$ min
 (c) $54 \frac{6}{13}$ min (d) none of these

SPEED TEST (TSD)



Directions for question number 1 to 3: Arun took part in a triathlon, an athletic event. He had to swim, run and bicycle to 10 km, 24 km and 30 km, respectively and return the same way. Arun's average speed for the triathlon is 4 km/h. He took a total of 4 min for swimming and 20 min for bicycling in the triathlon.

1. His speed of running is:
 (a) 5 km/min (b) 6 km/min
 (c) 7.5 km/min (d) $\frac{8}{3}$ km/min
2. He finishes race in:
 (a) 16 min (b) 23 min
 (c) 32 min (d) 35 min
3. How much time he took while returning for the bicycle if the time taken for the return of each phase (i.e., each event) is 50% greater than that of taken initially:
 (a) 12 min (b) 11 min
 (c) $11 \frac{1}{9}$ min (d) none of these

Directions for question number 4 to 5: A, B and C start running a race from the same point P in the same direction. A runs around a path which is an equilateral triangle PQX and B runs around a square path PQYZ and C runs on the regular hexagonal path PQRSTU. Where the one side PQ of each path is common.

4. If all of them complete one equal round at the same time then which of the following is true?
 (a) Speed of C is twice that of B
 (b) Speed of A is half that of C
 (c) Speed of B is 50% more than that of A
 (d) none of the above
5. If each of them run at a same constant speed, what is the maximum number of rounds anyone of them would have completed when they meet for the first time?
 (a) 1 (b) 2 (c) 3 (d) 4

Directions for the question number 6 to 9: City X and City Y are connected to a straight road. A and B start moving simultaneously towards each other. After travelling some distance, B takes a 60° turn to his left. Two hours later after B turns, A takes a 60° turn to his right. A travels 60 km after turning, before he meets B. A and B together travel 200 km before turning and they arrive at the meeting point simultaneously.

6. How many hours after turning does A meet B?
 (a) 1 (b) 3 (c) 4 (d) 5
7. What distance does A travel before turning 60 degree to his right?
 (a) 140 km (b) 150 km
 (c) 160 km (d) 170 km
8. If A and B had not turned, after how many hours would they have met?
 (a) $7 \frac{1}{8}$ h (b) $9 \frac{1}{8}$ h (c) $6 \frac{1}{8}$ h (d) $8 \frac{1}{8}$ h
9. What is B's speed?
 (a) 10 km/h (b) 12.5 km/h
 (c) 12 km/h (d) 15 km/h
10. Chetak and Ashwa, two horses, start galloping from Patna to Ranchi which are 80 km apart. The speed of Chetak is 160 km/h and that of Ashwa is 150 km/h. They start galloping simultaneously, from Patna to Ranchi. Chetak reached to Ranchi and returned to Patna but Ashwa returned from Jamshedpur (which is somewhere between Patna and Ranchi) to Patna at the same time. What is the ratio of distances between Patna and Jamshedpur and Jamshedpur and Ranchi?
 (a) 15 : 1 (b) 3 : 25
 (c) 15 : 2 (d) none of these



Answers

INTRODUCTORY EXERCISE-9.1

1 (a)	2. (c)	3. (c)							
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LEVEL-1

1 (a)	2. (b)	3. (b)	4. (c)	5. (a)	6. (c)	7. (c)	8. (b)	9. (a)	10. (c)
11. (c)	12. (d)	13. (a)	14. (d)	15. (b)	16. (c)	17. (b)	18. (c)	19. (b)	20. (c)
21. (b)	22. (d)	23. (a)	24. (b)	25. (c)	26. (d)	27. (d)	28. (d)	29. (b)	30. (c)
31. (d)	32. (a)	33. (b)	34. (c)	35. (d)	36. (a)	37. (b)	38. (a)	39. (b)	40. (c)
41. (a)	42. (b)	43. (b)	44. (c)	45. (c)	46. (c)	47. (c)	48. (b)	49. (a)	50. (b)
51. (b)	52. (a)	53. (b)	54. (c)	55. (c)	56. (c)	57. (a)	58. (b)	59. (d)	60. (b)
61. (a)	62. (c)	63. (c)	64. (c)	65. (b)	66. (d)	67. (d)	68. (c)	69. (d)	70. (a)
71. (a)	72. (a)	73. (b)	74. (c)	75. (b)	76. (c)	77. (b)	78. (c)	79. (a)	80. (c)
81. (d)	82. (b)	83. (c)	84. (c)	85. (b)	86. (d)	87. (b)	88. (b)	89. (d)	90. (c)
91. (c)	92. (b)	93. (d)	94. (d)	95. (c)	96. (b)	97. (a)	98. (b)	99. (b)	100. (a)
101. (d)	102. (a)	103. (c)	104. (b)	105. (b)	106. (c)	107. (d)	108. (a)	109. (b)	110. (c)
111. (b)	112. (d)	113. (c)	114. (d)	115. (a)	116. (b)	117. (d)	118. (b)	119. (b)	120. (b)
121. (b)	122. (b)	123. (c)	124. (b)	125. (b)	126. (c)	127. (d)	128. (b)	129. (a)	130. (a)
131. (d)	132. (b)	133. (c)	134. (b)	135. (b)	136. (b)	137. (b)	138. (b)	139. (a)	140. (c)
141. (c)	142. (d)	143. (d)	144. (d)	145. (b)	146. (a)	147. (b)	148. (d)	149. (a)	150. (c)

LEVEL-2

1 (b)	2. (c)	3. (b)	4. (a)	5. (b)	6. (c)	7. (c)	8. (c)	9. (b)	10. (a)
11. (d)	12. (d)	13. (c)	14. (c)	15. (a)	16. (b)	17. (c)	18. (d)	19. (c)	20. (b)
21. (d)	22. (c)	23. (b)	24. (b)	25. (b)	26. (c)	27. (b)	28. (c)	29. (b)	30. (b)
31. (c)	32. (b)	33. (c)	34. (b)	35. (d)	36. (b)	37. (c)	38. (c)	39. (d)	40. (d)
41. (b)	42. (c)	43. (c)	44. (b)	45. (c)	46. (c)	47. (d)	48. (b)	49. (b)	50. (c)
51. (a)	52. (a)	53. (b)	54. (c)	55. (c)	56. (b)	57. (c)	58. (d)	59. (b)	60. (c)
61. (c)	62. (d)	63. (b)	64. (b)	65. (b)	66. (a)	67. (c)	68. (c)	69. (c)	70. (b)
71. (b)	72. (d)	73. (d)	74. (b)	75. (d)	76. (b)	77. (a)	78. (a)	79. (c)	80. (a)

SPEED TEST-1

1 (b)	2. (c)	3. (b)	4. (b)	5. (d)	6. (b)	7. (a)	8. (d)	9. (c)	10. (a)
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Hints & Solutions

LEVEL (1)

1. Average speed = $\frac{\text{Total distance}}{\text{Total time}} = \frac{10 + 20}{\frac{10}{6} + \frac{20}{15}} = \frac{30}{\left(\frac{90}{30}\right)} = \frac{30}{3} = 10 \text{ km/h}$

2. Average speed (when distances are same) = $\frac{2uv}{u+v} = \frac{2 \times 20 \times 30}{(20+30)} = 24 \text{ km/h}$

where u, v are the different speeds.
(or use the general formula—Total distance/Total time)

3. Average speed = $\frac{3uvw}{uv + vw + uw} = \frac{3 \times 10 \times 20 \times 30}{200 + 600 + 300} = \frac{18000}{1100} = 16 \frac{4}{11} \text{ km/h}$

Alternatively: Suppose the total distance 3 times the LCM of the given speeds, then solve by general formula.

Total distance = 180 km (say)
then Total time = $\frac{60}{10} + \frac{60}{20} + \frac{60}{30} = 6 + 3 + 2 = 11 \text{ h}$
 \therefore Average speed = $\frac{180}{11} = 16 \frac{4}{11} \text{ km/h}$

Alternatively: Suppose the total distance equals to $3x$ km then solve as above.

4. Suppose the total distance equals to 4 times the LCM of the speeds.

\therefore Total distance = 2400 km
 \therefore Total time = $\frac{600}{20} + \frac{600}{25} + \frac{600}{30} + \frac{600}{40} = 30 + 24 + 20 + 15 = 89 \text{ h}$
 \therefore Average speed = $\frac{2400}{89} = 26 \frac{86}{89} \text{ km/h}$

5. $\frac{2 \times 20 \times x}{(20+x)} = 24$
 $\Rightarrow x = 30 \text{ km/h}$

Alternatively: Go through options.

6. Average speed = $\frac{2uv}{u+v} = \frac{2 \times 3x \times 5x}{(3x+5x)} = 3.75x \text{ km/h}$

7. $u = k, v = 3k$
 $\therefore \frac{2uv}{u+v} \Rightarrow \frac{2 \times k \times 3k}{(k+3k)} = 12$
 $\Rightarrow 1.5k = 12$
 $\Rightarrow k = 8 \text{ km/h}$

Alternatively: Go through options.

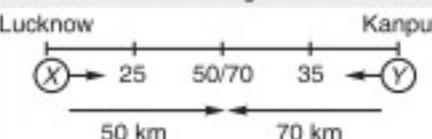
Alternatively: Solve through alligations.

8. Effective speed = $25 + 35 = 60 \text{ km/h}$

Total distance to be covered = 120 km

\therefore Time taken = $\frac{120}{60} = 2 \text{ h}$

HINT Since in each hour X and Y together covers 60 km.

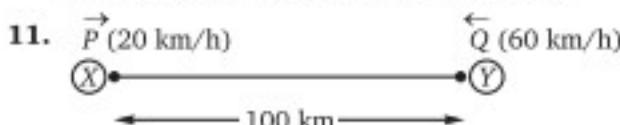


9. Since they take 2 hours to meet each other. Thus in 2 h X is 50 km away from Lucknow.

Alternatively: Both X and Y will cover the respective distances in the ratio of their speeds.

So, distance from Lucknow = $\frac{5}{12} \times 120 = 50 \text{ km}$

10. When time is constant the distances covered by A and B will be in the ratio of their speeds, respectively.



To meet each other they have to cover 100 km distance together and the ratio of distances covered by each one is directly proportional to the ratio of their speeds, respectively. Since the time taken by each one is same (i.e., constant).

Hence, $\frac{XZ}{YZ} = \frac{20}{60} = \frac{1}{3}$

$\therefore XZ = \frac{1}{4} \times 100 = 25 \text{ km}$

12. To meet the second time they have to cover 300 km distance together [for n^{th} time distance = $(2n-1)d$]

Time taken by them to meet each other, for the second time

$$= \frac{300}{80} = 3 \frac{3}{4} \text{ h}$$

Distance covered by P = $20 \times 3 \frac{3}{4} = 75 \text{ km}$

Alternatively: The ratio of distance covered
= Ratio of their speeds

\therefore Distance covered by P = $\frac{1}{4} \times 300 = 75 \text{ km}$

13. The ratio of distances covered by each of them

= Ratio of their respective speeds

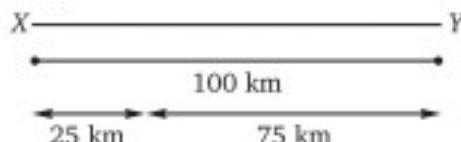
$$\therefore \text{Distance covered by } Q \text{ for the third meeting} = \frac{3}{4} \times 500 \\ = 375 \text{ km}$$

14. Consider the distance travelled by any one of them, then find the distance between X and M , where they meet.

\therefore The distance travelled by P for the fourth meeting

$$= \frac{1}{4} \times 700 = 175 \text{ km}$$

Therefore P will be 75 km from Y . It means P will be 25 km away from X .



15. This is constant for any number of meeting and is equal to the ratio of their speeds. Hence, 1 : 3.

16. It is always twice the length of race course. Hence, between any two consecutive meeting they have to cover total 200 km distance to meet each other for the next meeting.

HINT For the first meeting they will cover 100 km.

For the second meeting they will cover 300 km.

For the third meeting they will cover 500 km.

For the fourth meeting they will cover 700 km and so on.

17. To meet each other they will take equal time since they start their journey simultaneously.

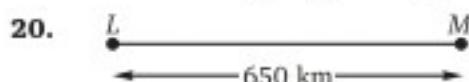
18. To reach their destination the time taken by A and B is equal to the ratio of reciprocal to their speeds. Since when distance is constant time is inversely proportional to the respective speeds.

$$\text{Hence, time taken by } A \text{ and } B = \frac{1}{16} : \frac{1}{25} = 25 : 16$$

$$19. \frac{A's \text{ speed}}{B's \text{ speed}} = \sqrt{\frac{\text{Time taken by } B (t_B)}{\text{Time taken by } A (t_A)}}$$

$$\frac{16}{25} = \sqrt{\frac{t_B}{t_A}}$$

$$\Rightarrow \frac{t_B}{t_A} = \frac{256}{625} \Rightarrow \frac{t_A}{t_B} = \frac{625}{256}$$



(Kamal) (Vimal)
40 km/h 30 km/h

In the first 3 hours Vimal covers 90 km.

So, the rest distance = 560 km

Now, Kamal and Vimal both travels together, towards each other.

$$\text{So, the time} = \frac{\text{Distance}}{\text{Speed}} = \frac{560}{70} = 8 \text{ h}$$

Thus, Vimal travels total = $3 + 8 = 11$ h

Thus, the distance travelled by Vimal = $11 \times 30 = 330$ km

21. The distance covered by Kamal = $8 \times 40 = 320$ km

- 22.



To meet the first time they have to cover $200 \times 2 = 400$ km

$$\text{Now, the time taken to meet each other} = \frac{400}{50} = 8 \text{ h}$$

23. Distance travelled by $P = 20 \times 8 = 160$ km

$$24. \text{Distance travelled by } Q = 30 \times \frac{800}{50} = 480 \text{ km}$$

$$25. \text{Distance travelled by } P = 20 \times \frac{1200}{50} = 480 \text{ km}$$

So, P will be 80 km away from X . Therefore ratio of distances

$$= \frac{80}{120} = \frac{2}{3}$$

$$26. \text{The distance travelled by } P = \frac{1600}{50} \times 20 = 640 \text{ km}$$

Thus, P will be 160 km away from X .

[Since $640 = (200 \times 2) + 240$]

\therefore Distance between D and X is 160 km.

27. This is possible only when the distance covered by P in n round be the multiple of 400.

28. X started at 12 : 00 noon

Y started at 3 pm

$$\text{Required time} = \frac{\text{Distance advanced in 3 h}}{\text{Relative speed}}$$

$$= \frac{40 \times 3}{20} = 6 \text{ h} \quad (20 = 60 - 40)$$

Hence, Y will overtake X at 9 pm. $(3 + 6 = 9)$

$$29. \text{Required time} = \frac{\text{Distance advance} - \text{Required difference}}{\text{Relative speed}}$$

$$= \frac{120 - 30}{20} = \frac{90}{20} = 4.5 \text{ h}$$

Thus, at 7 : 30 pm X and Y will be 30 km apart.

$$30. \text{Required time} = \frac{\text{Distance advanced} + \text{Required difference}}{\text{Relative speed}}$$

$$= \frac{120 + 30}{20} = \frac{150}{20} = 7.5 \text{ h}$$

Thus at 10 : 30 pm X and Y will be 30 km apart.

31. Distance travelled by Y to overtake X

$$= \text{Time taken} \times \text{Speed of } Y$$

$$= 6 \times 60 = 360 \text{ km}$$

Thus, Y will overtake X at a distance of 360 km from P .

32. Required distance

$$= \left(\frac{\text{Distance advanced} + \text{Required difference}}{\text{Relative speed}} \right) \times (\text{Speed of } Y) \\ = \frac{120 + 360}{20} \times 60 = 1440 \text{ km}$$

$$33. \text{Time (when } X \text{ was 30 km ahead of } Y) = \frac{120 - 30}{20} = 4.5 \text{ h}$$

$$\text{Time (when } Y \text{ was 30 km ahead of } X) = \frac{120 + 30}{20} = 7.5 \text{ h}$$

Thus, required difference in time = 3 h

34. Speed = 36 km/h

$$= 36 \times \frac{5}{18} = 10 \text{ m/s}$$

35. Since in 60 minutes postman goes 36000 metre.

$$\text{So in 1 minute postman goes } \frac{36000}{60} = 600 \text{ metre}$$

Thus, his required speed = 600 m/min

36. 1 mile = 1609.3 m = 1.6093 km

$$\therefore 1 \text{ km} = \frac{1}{1.6093} \text{ mile} = 0.6213882 \text{ mile}$$

$$\therefore \text{Required speed} = 36 \times 0.6213882 \text{ mile/h} \\ = 22.37 \text{ mile/h}$$

$$37. \text{Speed} = 20 \text{ m/s} = 20 \times \frac{18}{5} = 72 \text{ km/h}$$

38. In one hour train goes 72 km. So in one minute train will go $\frac{72}{60}$.

$$\therefore \text{Speed} = \frac{6}{5} = 1.2 \text{ km/min}$$

39. The ratio of speeds of A, B, C = 6 : 3 : 1

\therefore The ratio of time taken by A, B, C = 1 : 2 : 6

\therefore Time taken by A = 13 min

40. $A : B$

Speed 2 : 3

Time $3x : 2x$

$$41. \therefore 3x - 2x = 20 \Rightarrow x = 20$$

$$\therefore 3x = 60 \text{ min} = 1 \text{ h}$$

42. Let the original speed be S_1 and time t_1 and distance be D

$$\text{Now, } \frac{D/2}{2t_1} = S_2$$

$$\therefore S_2 = \frac{D}{4t_1} \text{ and } S_1 = \frac{D}{t_1}$$

$$\therefore \frac{S_1}{S_2} = \frac{D/t_1}{D/4t_1} = \frac{4}{1}$$

43. You can go through options to check the required difference.

Alternatively: Required distance

$$= \frac{S_1 S_2}{(S_1 - S_2)} \times \text{Time difference} \\ = \frac{5 \times 8}{3} \times \frac{3}{2} = 20 \text{ km}$$

Alternatively: Take the LCM of distances then solve by unitary method.

$$\therefore \text{LCM of 5, 8} = 40$$

Now, consider 40 km as a distance, then there is a 3 hours difference in 40 km. So, 3/2 hours difference will be in 20 km.

Alternatively: Let x be the distance, then

$$\frac{x}{5} - \frac{x}{8} = \frac{3}{2}$$

$$\Rightarrow x = 20 \text{ km}$$

44. $A : B$

Speed 2 : 3

Time 3 : 2

$\therefore B$ takes 48 minutes so A will take 72 minutes
= 1 h 12 min

45. The ratio of distances = 160 : 140 = 8 : 7

\therefore The ratio of speeds = 8 : 7

$$46. \frac{x}{9} - \frac{x}{10} = \frac{20}{60}$$

$$x = 30 \text{ km}$$

47. Time taken by Abhinav = 4 h

Time taken by Praveen = 3.5 h

For your convenience take the product of times taken by both as a distance.

Then the distance = 14 km

Since, Abhinav covers half of the distance in 2 hours (i.e., at 8 am)

Now, the rest half (i.e., 7 km) will be covered by both Praveen and Abhinav.

$$\text{Time taken by them} = \frac{7}{7.5} = 56 \text{ min}$$

Thus, they will cross each other at 8 : 56 am.

48. 9 km difference arises in the 99 km distance.

\therefore 72 km difference will arise in the 792 km distance.

49. Apply the product constancy concept

$$\begin{array}{ccc} \text{Speed} & & \text{Time} \\ \frac{1}{5} \downarrow & & \frac{1}{4} \uparrow \\ & & = 15 \text{ min} \end{array}$$

$$\text{Since, } \frac{x}{4} = 15 \text{ min} \Rightarrow x = 60 \text{ min} = 1 \text{ h}$$

So, the original (or usual) time = 60 min = 1 h

50. $\begin{array}{ccc} \text{Speed} & & \text{Time} \\ \frac{1}{4} \downarrow & & \frac{1}{3} \uparrow = 2 \text{ h} \end{array}$

$$\Rightarrow \text{Usual time} = 2 \times 3 = 6 \text{ h}$$

$$51. \begin{array}{ccc} \text{Speed} & & \text{Time} \\ \frac{1}{2} \uparrow & & \frac{1}{3} \downarrow = 40 \text{ min} \end{array}$$

$$\Rightarrow \text{Usual time} = 3 \times 40 = 120 \text{ min} = 2 \text{ h}$$

$$52. \begin{array}{ccc} \text{Speed} & & \text{Time} \\ \frac{2}{20} = \frac{1}{10} \downarrow & & \frac{1}{9} \uparrow = 10 \text{ min} \end{array}$$

$$\Rightarrow \text{Usual time} = 9 \times 10 = 90 \text{ min} = \frac{3}{2} \text{ h}$$

$$\therefore \text{Distance travelled} = \text{Speed} \times \text{Time} \\ = 20 \times \frac{3}{2} = 30 \text{ km}$$

53. Increase in speed = 1 km

Change in time = 25 min

$$\begin{array}{ccc} \text{Speed} & & \text{Time} \\ \frac{1}{5} \uparrow & & \frac{1}{6} \downarrow = 25 \end{array}$$

$$\Rightarrow \text{Usual (normal) time} = 6 \times 25 = 150 \text{ min} = \frac{5}{2} \text{ h}$$

$$\therefore \text{Distance} = \text{Normal speed} \times \text{Normal time}$$

$$= 5 \times \frac{5}{2} = 12.5 \text{ km}$$

54. Since, they are 1.5 km apart in each hour.
 \therefore 7.5 km apart they will be in 5 hours.
 (Since, in the same direction speeds are subtracted)
55. In each hour they will be 720 km apart.
 (Since in opposite direction speeds are added)
56. Let the distance = x km and usual rate = y km/h

$$\therefore \frac{x}{y} - \frac{x}{(y+6)} = 4 \text{ h} \quad \dots(\text{i})$$

$$\frac{x}{(y-4)} - \frac{x}{y} = 4 \quad \dots(\text{ii})$$

From Eqs. (i) and (ii), we get

$$\frac{x}{y} - \frac{x}{(y+6)} = \frac{x}{(y-4)} - \frac{x}{y}$$

$$\Rightarrow y = 24$$

Now putting the value of $y = 24$ in Eq (i), we get
 $x = 480$

Alternatively:

$$\begin{array}{l} \begin{array}{c} S \nearrow T \\ +6 \quad -4 \end{array} \Rightarrow -4S + 6T = |-4 \times 6| \\ \begin{array}{c} S \nearrow T \\ -4 \quad +4 \end{array} \Rightarrow 4S - 4T = |-4 \times 4| \end{array}$$

$$\therefore \begin{array}{l} -4S + 6T = 24 \quad \dots(\text{i}) \\ 4S - 4T = 16 \quad \dots(\text{ii}) \end{array}$$

\therefore Solving these two equations, we get

$$\begin{array}{l} T = 20 \quad \text{and} \quad S = 24 \\ \therefore \text{Distance} = \text{Speed} \times \text{Time} \\ = 24 \times 20 = 480 \text{ km} \end{array}$$

57. Let the original speed be x km/h, then

$$\begin{array}{l} \frac{600}{x} - \frac{600}{(x+20)} = 1 \\ \Rightarrow 600 \left(\frac{x+20-x}{x(x+20)} \right) = 1 \\ \Rightarrow x^2 + 120x - 12000 = 0 \\ \Rightarrow (x-120)(x-100) = 0 \\ \Rightarrow x = 100 \quad \text{and} \quad x = 120 \\ \therefore \text{Original speed} = 100 \text{ km/h} \end{array}$$

Alternatively:

$$\begin{array}{l} S_1 \times S_2 = \text{Distance} \times \frac{\text{Difference in speed}}{\text{Difference in time}} \\ = 600 \times \frac{20}{1} = 600 \times 20 = 12000 \end{array}$$

$$\Rightarrow S_1 \times S_2 = 12000$$

$$\therefore S_1 = 100 \quad \text{and} \quad S_2 = 120$$

(Factorise 12000 in such a way that the difference be 20) S_1 is the original speed and S_2 is the changed speed.

58. Very similar to question number 57.

$$180 \times \frac{5}{3} = 60 \times 5$$

$$\begin{array}{l} S_1 \times S_2 = 300 = 15 \times 20 \\ S_1 = 15 \text{ km/h} \end{array}$$

and $S_2 = 20 \text{ km/h}$

$$\text{Alternatively: } S_1 \times (S_1 + 5) = 300$$

$$\Rightarrow S_1 = 15 \text{ km/h}$$

59. Very similar to previous problems

$$t_1 \times t_2 = \text{Distance} \times \frac{\text{Difference in time}}{\text{Difference in speed}}$$

$$\Rightarrow t_1 \times t_2 = 1680 \times \frac{6}{14}$$

$$\Rightarrow t_1 \times t_2 = 120 \times 6 = 720 = 30 \times 24$$

[since $t_2 = (t_1 - 6) \Rightarrow t_1 \times (t_1 - 6) = 720 \Rightarrow t_1 = 30$]

Therefore, usual time = 30 h

$$60. \text{Relative speed} = \frac{\text{Total distance}}{\text{Total time}}$$

$$= \frac{60 + 40}{20} = 5 \text{ m/s}$$

$$\therefore 5 \text{ m/s} = 5 \times \frac{18}{5} = 18 \text{ km/h}$$

Now, Relative speed = 18 km/h

$$= \text{Speed of ambulance} - \text{Speed of school bus}$$

$$18 = 30 - \text{speed of school bus}$$

$$\text{Speed of school bus} = 12 \text{ km/h}$$

$$61. \begin{array}{ccc} \text{Time} & & \text{Speed} \\ \frac{1}{4} \downarrow & & \frac{1}{3} \uparrow \end{array}$$

Since he has to increase his speed by $\frac{1}{3}$ rd of the original speed.

So, the new speed = $15 + 5 = 20 \text{ km/h}$

$$\text{Alternatively: } 15 \times 4 = 3 \times x$$

$$\Rightarrow x = 20 \text{ km/h}$$

$$62. \text{Time (required)} = \frac{\text{Length of train}}{\text{Speed of train}} \quad \left(T = \frac{D}{S} \right)$$

$$= \frac{350}{70} = 5 \text{ s}$$

$$63. \text{Time taken to cross the bridge} = \frac{\text{Total length}}{\text{Speed of train}}$$

$$= \frac{270 + 130}{40} = \frac{400}{40}$$

$$= 10 \text{ s}$$

$$64. \text{Speed of train} = \frac{225}{9} = 25 \text{ s}$$

$$\text{Now, Time taken to cross the tunnel} = \frac{225 + 450}{25} = 27 \text{ s}$$

65. Let the length of the tunnel be x m, then

$$\text{Time} = \frac{\text{Length of train} + \text{Length of tunnel}}{\text{Speed}}$$

$$60 = \frac{350 + x}{10} \quad \left(\text{Speed} = 36 \times \frac{5}{18} = 10 \text{ m/s} \right)$$

$$\Rightarrow x = 250 \text{ m}$$

$$\begin{aligned} \text{66. Speed of train} &= \frac{\text{Length of train} + \text{Length of platform}}{\text{Time}} \\ &= \frac{250 + 250}{25} = 20 \text{ m/s} \\ &= 72 \text{ km/h} \end{aligned}$$

67. Let the length of the Sabarmati express is x metre then,

$$\frac{x + 162}{18} = \frac{x + 120}{15} \quad \text{Speed of train}$$

$$\Rightarrow x = 90 \text{ m}$$

$$\begin{aligned} \text{68. Time} &= \frac{\text{Length of train}}{\text{Relative speed}} \\ &= \frac{200}{19} = 10 \frac{10}{19} \text{ s} \end{aligned}$$

(Relative speed = $72 - 3.6 = 68.4 \text{ km/h} = 19 \text{ m/s}$)

$$\begin{aligned} \text{69. Time} &= \frac{\text{Length of train}}{\text{Relative speed}} \\ &= \frac{350}{35} \times 6 = 60 \text{ s} \end{aligned}$$

(Relative speed = $20 + 1 = 21 \text{ km/h} = 21 \times \frac{5}{18} = \frac{35}{6} \text{ m/s}$)

$$\text{70. Relative speed} = 50 - 40 = 10 \text{ km/h} = \frac{50}{18} \text{ m/s}$$

$$\begin{aligned} \therefore \text{Time taken} &= \frac{\text{Sum of length of the trains}}{\text{Relative speed}} \\ &= \frac{200}{50} \times 18 = 72 \text{ s} \end{aligned}$$

$$\text{71. Relative speed} = 50 + 40 = 90 \text{ km/h}$$

$$= 90 \times \frac{5}{18} = 25 \text{ m/s}$$

$$\therefore \text{Time taken} = \frac{\text{Sum of lengths of train}}{\text{Relative speed}} = \frac{200}{25} = 8 \text{ s}$$

72. Let the length of train be x m, then

$$\frac{x}{10} = \frac{120 + x}{18}$$

$$\Rightarrow x = 150 \text{ m}$$

73. Let the speed of train be x km/h, then

$$\frac{175}{10} = (9 + x) \times \frac{5}{18}$$

$$\Rightarrow x = 54 \text{ km/h}$$

$$\text{74. Relative speed} = \text{Sum of speeds of two trains} = (60 + x)$$

$$\text{Time} = \frac{\text{Sum of length of two trains}}{\text{Relative speed}}$$

$$10 = \frac{250}{(60 + x) \times 5} \times 18$$

$$(60 + x) = 90$$

$$x = 30 \text{ km/h}$$

75. Let the length of the train be x metre, and let the speed of train be y km/h, then

$$x = (y + 3) \frac{5}{18} \times 36 \quad \dots(i)$$

$$\text{and} \quad x = (y + 6) \times \frac{5}{18} \times 30 \quad \dots(ii)$$

From Eq. (i) and (ii), we get

$$(y + 3) \times 36 = (y + 6) \times 30$$

$$y = 12 \text{ km/h}$$

$$\therefore x = (y + 3) \times \frac{5}{18} \times 36$$

$$\text{or} \quad x = 15 \times \frac{5}{18} \times 36$$

$$\text{or} \quad x = 150 \text{ m}$$

76. Let the length of each train be x m, then

$$S_1 = \frac{x}{4} \quad \text{and} \quad S_2 = \frac{x}{5}; \quad S_1 \text{ and } S_2 \text{ are speeds}$$

$$\text{Now, required time} = \frac{2x}{\frac{x}{4} + \frac{x}{5}} = \frac{40}{9} \text{ s}$$

77.

Pushpak	Bhopal
Time \rightarrow	10 : 8
Speed \rightarrow	8 : 10
\Rightarrow	4x : 5x

$$\text{Since, } 5x - 4x = 10$$

$$\Rightarrow 5x = 50 \quad \text{and} \quad 4x = 40$$

$$\therefore \text{Average speed} = \frac{2 \times 40 \times 50}{40 + 50} = 44 \frac{4}{9} \text{ km/h}$$

$$\text{78. Required time} = \frac{\text{Distance advanced}}{\text{Relative speed}} = \frac{4 \times 40}{20} = 8 \text{ h}$$

Thus, the faster train will overtake at 8 pm.

$$\text{79. Required distance} = \text{Time taken in overtaking} \times \text{Faster's speed} = 8 \times 60 = 480 \text{ km from Meerut}$$

80. In 50 minute Rajdhani express can cover 50 km. So, the rest distance = 650 km, which will be jointly covered by both trains.

$$\therefore \text{Time taken} = \frac{650}{(60 + 70)} = 5 \text{ h}$$

$$\text{Distance from Lucknow} = 5 \times 70 = 350 \text{ km}$$

$$\text{81. Average speed} = \frac{\text{Total distance}}{\text{Total time}}$$

$$= \frac{560 + 360}{16} = 57 \frac{1}{2} \text{ h}$$

$$\text{82. Average speed} = \frac{2 \times 80 \times 120}{200} = 96 \text{ km/h}$$

$$\text{83. Distance} = \text{Average speed} \times \text{Average time}$$

$$\text{or} \quad \text{Distance} = 96 \times \frac{25}{2}$$

$$\text{or} \quad \text{Distance} = 1200 \text{ km}$$

$$\text{84. } 50 \times 30 = x \times 20$$

$$\Rightarrow x = 75 \text{ km/h}$$

85. $\frac{S_1}{S_2} = \sqrt{\frac{t_2}{t_1}}$

$$\frac{120}{S_2} = \sqrt{\frac{9}{16}} = \frac{3}{4}$$

$$\Rightarrow S_2 = 160 \text{ km/h}$$

86. $S_1 + S_2 = \frac{240}{4} = 60$

$$S_1 - S_2 = \frac{240}{12} = 20$$

$$\therefore S_1 = 40 \text{ m/s} \text{ and } S_2 = 20 \text{ m/s}$$

$$\therefore S_1 = 40 \times \frac{18}{5} = 144 \text{ km/h}$$

87. Time taken to cross the man = $\frac{\text{Length of the faster train}}{\text{Relative speed}}$

$$18 = \frac{x}{15 \times \frac{5}{18}} \Rightarrow x = 75 \text{ m}$$

88. Suppose the total distance be 300 km (LCM of 50 and 60) then in the first case it takes only 5 hours and in the second case it takes 6 hours.

Thus, in 6 hours trains halts for 1 hour.

Therefore in 1 hour train halts for $1/6$ hour = 10 m

Alternatively: Difference in speeds = 10 km/h

Faster speed = 60 km/h

$$\therefore \text{Required time per hour} = \frac{10}{60} = \frac{1}{6} \text{ h} = 10 \text{ min}$$

89. If the speed of faster horse be f_s and that of slower horse be s_s , then

$$f_s + s_s = \frac{50}{1} = 50$$

and $\frac{50}{s_s} - \frac{50}{f_s} = \frac{5}{6}$

Now, you can go through options.

The speed of slower horse is 20 km/h.

Since, $20 + 30 = 50$

and $\frac{50}{20} - \frac{50}{30} = \frac{5}{6}$

90. Let he walked for x hours, then

$$5x + 25(10 - x) = 17 \times 10$$

$$\Rightarrow x = 4$$

$$\therefore 10 - x = 6 \text{ h}$$

Hence, distance travelled by auto = $25 \times 6 = 150 \text{ km}$.

91. Let the original speed be x km/h then,

$$\frac{36}{(x-6)} + \frac{36}{(x+6)} = 8$$

Now, you can go through options or solve it as follows

$$\frac{(x+6+x-6)}{(x^2-36)} = \frac{8}{36}$$

$$\Rightarrow x = 12 \text{ and } x = -3$$

Thus, the possible value of $x = 12$

\therefore Time taken by faster speed = 2 h

92. Time = $\frac{\text{Distance advanced}}{\text{Relative speed}}$

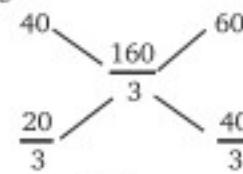
$$2 = \frac{2 \times x}{(30-x)}$$

$$\Rightarrow x = 15 \text{ km/h}$$

93. Prachi travels only for 3 hours, since half an hour she halts at Lucknow.

Now, the average speed (except the halt) = $\frac{160}{3}$ km/h

Therefore, by alligation



$$\Rightarrow 1 : 2$$

Therefore, the ratio of time taken at 40 km/h and at 60 km/h is 1 : 2.

Thus, the distance between Lucknow and Kanpur

$$= 2 \times 60 = 120 \text{ km}$$

94. Let the speed of the faster train be f_s and slower train be s_s , then

$$f_s + s_s = \frac{200 + 250}{18} = 25 \text{ m/s}$$

and $f_s - s_s = \frac{200 + 250}{60} = \frac{450}{60} = 7.5 \text{ m/s}$

$$\therefore f_s = 16.25 \text{ m/s}$$

$$= 16.25 \times \frac{18}{5} = 58.5 \text{ km/h}$$

95. Distance covered in 3 minutes = $3 \times \frac{1000}{60} = 50 \text{ m}$

Now he has to cover (500 + 50) metres in $(30 - 3)$ minutes

$$\therefore \text{New speed} = \frac{550/1000}{27/60} = \frac{11}{9} \text{ km/h}$$

96.

	Anil	Mukesh	
Speed \rightarrow	3	:	4
Time \rightarrow	4	:	3

But $4x - 3x = \frac{1}{2} \text{ h}$

$$\Rightarrow 4x = 2 \text{ h} \text{ and } 3x = 1.5 \text{ h}$$

Now, since Anil doubles the speed so time will be half of the actual time. Hence, new time will be 1 hour.

97. Average speed of Anil and Mukesh = $\frac{3x + 4x}{2} = 28$

$$\Rightarrow x = 8$$

$$\therefore \text{Speed of Sameer} = 3 \times 8 = 24 \text{ km/h}$$

$$\therefore \text{Distance travelled} = 2 \times 24 = 48 \text{ km}$$

98. Let the speed of X and Y be the x km/h and y km/h respectively. Since they meet after 3 hours, so $x + y = 100$. Since, the faster train takes atleast $3 + 2 = 5$ hours to complete the 300 km journey. Hence, minimum possible speed for the slower train = 40 km/h at which speed it will take 7.5 h to complete the journey. $\left(7.5 = \frac{300}{40}\right)$

99. Let the time taken in first third part of the journey be x minutes, then the time required in second third part of the journey is $\frac{3x}{2}$ and in the last third part of the journey time required is $\frac{15x}{8}$.

$$\text{Therefore, } x + \frac{3x}{2} + \frac{15x}{8} = 350 \text{ min}$$

$$\Rightarrow x = 80 \text{ min}$$

100.

Speed	Time
$\frac{1}{5} \downarrow$	$\frac{1}{4} \uparrow$

 = 15 min

$$\text{Therefore usual time} = 4 \times 15 = 60 \text{ min}$$

- Now,

Speed	Time
$\frac{1}{4} \uparrow$	$\frac{1}{5} \downarrow$

 = 12 min

(Since original time = 60 min)

Therefore he will be $15 + 12 = 27$ minutes early in comparison to the previous day.

101. Let the original speed be s km/h and scheduled time = hours

and total distance = D km

$$\text{then } s \times t = \frac{3}{4} D \quad \dots \text{(i)}$$

$$\text{and } s \times (t + 3) = D \quad \dots \text{(ii)}$$

From Eq. (i) and (ii), we get

$$st = \frac{3}{4} [s(t + 3)] \Rightarrow t = 9 \text{ h}$$

and let $s = 1$ km/h, then $D = 12$ km

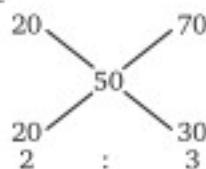
Again, since he doubles his speed after k hours then,

$$s_1 t_1 + s_2 t_2 = D$$

$$1 \times k + 2 \times (9 - k) = 12$$

$$\Rightarrow k = 6 \text{ h}$$

102. By alligation rule



Ratio of time = 2 : 3

∴ Ratio of distances = $2 \times 20 : 3 \times 70 = 4 : 21$

$$\text{Alternatively: } \frac{x}{20} + \frac{y}{70} = \frac{x+y}{50}$$

$$\Rightarrow \frac{76x + 20y}{1400} = \frac{x+y}{50}$$

$$\Rightarrow 42x = 8y \Rightarrow \frac{x}{y} = \frac{4}{21}$$

103. $\frac{(\text{Speed of wind})}{(\text{Speed of car})} = \frac{(\text{Time utilised})}{(\text{Time saved})}$

$$\frac{332}{x} = \frac{332}{28}$$

$$\Rightarrow x = 28 \text{ m/s}$$

$$104. \text{ Time} = \frac{\text{Total distance}}{\text{Relative speed}}$$

$$\frac{4.5}{60} = \frac{450/1000}{x} \Rightarrow x = 6 \text{ km/h}$$

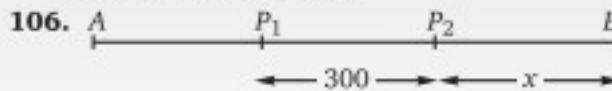
Relative speed = Speed of car - Speed of man

$$6 = x - 6 \\ \Rightarrow x = 12 \text{ km/h}$$

105. $W + R \rightarrow 4 \text{ h } 20 \text{ min}$

$$W + W \rightarrow 5 \text{ h } 20 \text{ min}$$

$$\therefore R + R \rightarrow 3 \text{ h } 20 \text{ min}$$



$P_1 \rightarrow$ Place of accident

$P_2 \rightarrow$ Imaginary place of accident

For the distance x

$$\text{Speed} \quad \text{Time} \\ \frac{1}{6} \downarrow \quad \frac{1}{5} \uparrow = 1 \text{ h}$$

Thus, the usual time required for the distance x km is $5 \times 1 = 5$ hours.

For the distance $(x + 300)$

$$\text{Speed} \quad \text{Time} \\ \frac{1}{6} \downarrow \quad \frac{1}{5} \uparrow = 2 \text{ h}$$

Thus, the usual time required for the distance $(x + 300)$ km is $5 \times 2 = 10$ h.

It means he covers 300 km distance in 5 h

$$\therefore \text{Speed} = \frac{300}{5} = 60 \text{ km/h} \quad (\text{normal speed})$$

107. Since, he can cover x km at 60 km/h in 5 h it means $x = 300$ km.

$$\text{Therefore, total distance} = (120 + 300 + 300) = 720 \text{ km.}$$

108. Circumference means one revolution.

$$\text{Therefore, distance covered in 10 revolutions} = 300 \times 10 \\ = 30 \text{ m}$$

i.e., 30 metre in 6 seconds.

$$\therefore \text{Speed of wheel} = \frac{30}{6} \text{ m/s} = 5 \text{ m/s}$$

$$\therefore 5 \text{ m/s} = 5 \times \frac{18}{5} = 18 \text{ km/h}$$

$$109. \text{ Speed of man in still water} = \frac{S_D + S_U}{2}$$

$$= \frac{12 + 8}{2} = 10 \text{ km/h}$$

$S_D \rightarrow$ Speed in downstream (= Boat + River)

$S_U \rightarrow$ Speed in upstream (= Boat - River)

$$110. \text{ Speed of water current} = \frac{S_D - S_U}{2} = \frac{21 - 15}{2} = 3 \text{ km/h}$$

$$111. S_D = 12 \text{ km/h}$$

$$S_U = 5 \text{ km/h}$$

$$\text{Speed of current} = \frac{12 - 5}{2} = 3.5 \text{ km/h}$$

112. $S_D \rightarrow 15 \text{ km/h}$

$S_U \rightarrow 9 \text{ km/h}$

$$\text{Speed of man} = \frac{15+9}{2} = 12 \text{ km/h}$$

113. Let the required distance be D km, then

$$\frac{D}{6} + \frac{D}{4} = \frac{5}{4}$$

$$D \left(\frac{10}{24} \right) = \frac{5}{4}$$

$$\Rightarrow D = 3 \text{ km}$$

114. $\frac{16}{8} + \frac{16}{2} = 10 \text{ h}$

115. Let the downstream speed be D and upstream speed be U , then

$$\frac{48}{U} + \frac{72}{D} = 12$$

and $\frac{48}{D} + \frac{72}{U} = 13$

$\therefore 48m + 72n = 12 \quad \dots(i)$

and $48n + 72m = 13 \quad \dots(ii)$

Solving Eq. (i) and (ii), we get

$$m + n = \frac{5}{24} \quad \text{and} \quad m - n = \frac{1}{24}$$

$\therefore D = 12 \text{ km/h} \quad \text{and} \quad U = 8 \text{ km/h}$

$\therefore \text{Speed of current} = 2 \text{ km/h}$

116. $D_S = \frac{9}{2} = 4.5 \text{ km/h}$

$$U_S = \frac{9}{6} = 1.5 \text{ km/h}$$

$\therefore \text{Speed of boat in still water} = \frac{4.5 + 1.5}{2} = 3 \text{ km/h}$

and Speed of river in still water $= \frac{4.5 - 1.5}{2} = 1.5 \text{ km/h}$

117. $\frac{D_T}{U_T} = \frac{1}{2} \Rightarrow \frac{D_S}{U_S} = \frac{2}{1} \Rightarrow \frac{B+S}{B-S} = \frac{2}{1} \Rightarrow \frac{B}{S} = \frac{3}{1}$

HINT D_T and U_T are the downstream and upstream times and D_S and U_S are the downstream and upstream speeds. Here we can use componendo and dividendo.

$$\therefore \frac{\text{Speed of boat}}{\text{Speed of stream}} = \frac{3}{1} = \frac{15}{x}$$

$\therefore \text{Speed of stream} = 5 \text{ km/h}$

118. If t_1 and t_2 are the upstream and downstream times. Then time taken in still water is given by

$$\frac{2 \times t_1 \times t_2}{t_1 + t_2} = \frac{2 \times 12 \times 24}{36} = 16 \text{ h}$$

Alternatively: $D = (B + S) \times 12$

and $D = (B - S) \times 24$

where $(B + S)$ is downstream speed

$(B - S)$ is upstream speed

$$\Rightarrow \frac{B+S}{B-S} = \frac{2}{1}$$

$$\Rightarrow \frac{B}{S} = \frac{3}{1} \quad (\text{By componendo and dividendo})$$

Now $D = 4S \times 12 = 48S$

$D = 48S = 16B \quad (\text{Distance} = \text{Time} \times \text{Speed})$

$\therefore \text{Required time} = 16 \text{ h}$

119. $\frac{D_S}{U_S} = \frac{B+S}{B-S} = \frac{3}{2}$

where $B \rightarrow \text{Speed of boat in still water}$

$S \rightarrow \text{Speed of current/stream}$

$$\Rightarrow \frac{2B}{2S} = \frac{5}{1} \quad (\text{By componendo and dividendo})$$

$$\Rightarrow \frac{B}{S} = \frac{5/2}{1/2} \Rightarrow B = \frac{5}{2}$$

$$\text{Average speed of downstream and upstream} = \frac{2 \times 3 \times 2}{3 + 2} = \frac{12}{5}$$

$$\therefore \text{Required ratio} = \frac{5/2}{12/5} = \frac{25}{24}$$

120. Let x be the upstream speed, then the downstream speed will be $(x + 3)$

$$\therefore \frac{3}{x} + \frac{3}{x+3} = 3$$

$$\Rightarrow x^2 + x - 3 = 0$$

$$\Rightarrow x = \frac{-1 + \sqrt{13}}{2}$$

$$= \frac{-1 + 3.6}{2} = 1.3 \text{ km/h}$$

$$\therefore (x + 3) = 4.3 \text{ km/h}$$

121. Upstream speed of first boat = 8 km/h

Upstream speed of second boat = 4 km/h

$\therefore \text{Relative speed} = 4 \text{ km/h}$

$$(\text{Relative speed} = 8 - 4)$$

$$\therefore \text{Required time} = \frac{10}{4} = 2.5 \text{ h}$$

122. Downstream speed = $B + S$

$B \rightarrow \text{Speed of boat}$

Upstream speed = $B - S$

$S \rightarrow \text{Speed of stream}$

$$\therefore \frac{120}{B+S} + \frac{120}{B-S} = 15$$

$$\Rightarrow \frac{B}{B^2 - S^2} = \frac{1}{16} \quad \dots(i)$$

$$\text{Again} \quad \frac{120}{B+2S} + \frac{120}{B-2S} = 24$$

$$\Rightarrow \frac{B}{B^2 - 4S^2} = \frac{1}{10} \quad \dots(ii)$$

From Eq. (i) and (ii), we get

$$B = (B^2 - S^2) 16$$

and $B = (B^2 - 4S^2) 10$

$$\Rightarrow 10B^2 - 40S^2 = 16B^2 - 16S^2$$

$$\Rightarrow \frac{B^2}{S^2} = 9 \Rightarrow \frac{B}{S} = 3$$

i.e., $B : S = 3 : 1$

Now, you can go through options or solve by equations. Since now you know the ratio of speeds of boat and stream. The correct choice is (b).

124. Upstream speed = $B - S$

Downstream speed = $B + S$

$$B - S = \frac{15}{5} = 3 \text{ km/h}$$

Again

$$B = 4S$$

∴

$$B - S = 3 = 3S$$

⇒

$$S = 1 \text{ and } B = 4 \text{ (km/h)}$$

∴

$$B + S = 5 \text{ km/h}$$

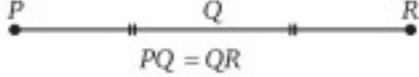
∴ Time during downstream = $\frac{15}{5} = 3 \text{ h}$

125. $\frac{24}{(5.5 - R)} - \frac{24}{(5.5 + R)} = 5$

⇒ $R = 2.5 \text{ km/h}$; $R \rightarrow$ Speed of river/current

Again $(B_2 + R) = \frac{24}{4} = 6$

⇒ $(B_2 + 2.5) = 6 \Rightarrow B_2 = 3.5 \text{ km/h}$

126. 

$P \rightarrow Q \rightarrow R$ (7 h)

It means $P \rightarrow Q$ (3.5 h)

Again $\{P \rightarrow Q \text{ and } Q \rightarrow P\}$ (8 h)

It means $Q \rightarrow P$ (4.5 h)

Therefore $R \rightarrow Q$ (4.5 h)

Thus, from R to P boat will take 9 hours.

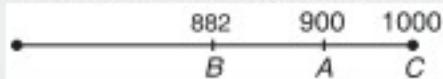
HINT $P \rightarrow R$ (Downstream)
 $R \rightarrow P$ (Upstream)

127. $\frac{40}{(B - S)} + \frac{55}{(B + S)} = 13$

$$\frac{30}{(B - S)} + \frac{44}{(B + S)} = 10$$

HINT Go through options for quicker answer and prefer the value which can help in dividing 44 and 55.

Solutions for question number 128 and 129: B is 2% slow than A and A is 10% slow than C . Therefore, in 1 km race.

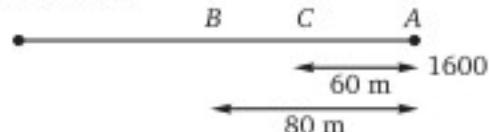


128. Since in 1000 m (1 km) race difference between A and B is 18 m.

So in 2 km race it will be 36 m.

129. In a 1 km race C can give B a start of 118 m. Therefore in a half km race C can give B a start of 59 m.

130. In a 1600 m race



$C \rightarrow 1540, B \rightarrow 1520$

The ratio of speeds of $C : B$ is $77 : 76$. It means in 77 m race C beats B by 1 m. So, in 400 m race C will beat B by

$$400 \times \frac{1}{77} \text{ m} = 5 \frac{15}{77} \text{ m}$$

131.

Aman Shakti

Time 190 200

Speed $20x$ $19x$

∴ $20x = 1000 \text{ m}$

⇒ $x = 50 \text{ m}$

Again $20x - 19x = x = 50 \text{ m}$

So, Aman can beat Shakti by 50 m.

132.

$A : B$

Speed 7 : 4

Time 4 : 7

Distance 4 : 7 (Since distance \propto time)

Now, $7x - 4x = 300$

$3x = 300$

⇒ $x = 100$

∴ $7x = 700$

Thus, the winning post be 700 m away from the starting point.

133. Ratio of speeds of $A : B = 12 : 11$

and ratio of speeds of $B : C = 8 : 7$

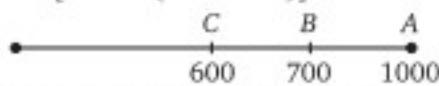
Therefore ratio of speeds of $A : B : C = 96 : 88 : 77$

So in 9600 m race A will beat C by 1900 m.

134. When Ameesha runs 1000 m, then Bipasha runs only 700 m $[1000 - (100 + 200)]$

when Ameesha runs 1000 m, then Celina runs only 600 m $[1000 - (100 + 300)]$

Therefore,



Now, since in 700 m race Bipasha beats Celina by 100 m. So, in 50 m race Bipasha will beat Celina by

$$50 \times \frac{100}{700} = 7.14 \text{ m}$$

Alternatively: Bipasha beats Celina by 14.28% of the distance then in 50 m race Bipasha will beat Celina by 7.14 m.

135.

Distance Time

Case I: Ravi 1000 t_1

Vinod 960 $t_1 + 19$

Case II: Ravi 960 t_2

Vinod 1000 $t_2 + 30$

Therefore, $\frac{1000}{t_1} = \frac{960}{t_2} = \text{Speed of Ravi}$

$$\Rightarrow t_1 = \frac{25}{24} t_2$$

Also $\frac{960}{t_1 + 19} = \frac{1000}{t_2 + 30} = \text{Speed of Vinod}$

$$\therefore (t_2 + 30) 24 = 25 \left[\frac{25}{24} t_2 + 19 \right]$$

$$\Rightarrow 49t_2 = 5880$$

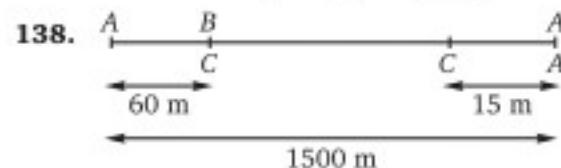
$$\Rightarrow t_2 = 120 \text{ s}$$

$$\therefore \text{Required ratio} = \frac{960/t_2}{1000/t_2 + 30} = \frac{6}{5}$$

137. Since, the speeds of Vinay and Versha are in the ratio of 5 : 3 i.e., when Vinay covers 5 rounds, then Versha covers 3 rounds, but first time Vinay and Versha meet when Vinay completes $2\frac{1}{2}$ round and Versha completes $1\frac{1}{2}$ round.

For Vinay to pass Versha 7th time, Vinay would have completed $7 \times 2\frac{1}{2}$ rounds. Since, each round is $1\frac{1}{2}$ km, the distance covered by Vinay is

$$7 \times 2\frac{1}{2} \times 1\frac{1}{2} = 7 \times \frac{5}{2} \times \frac{3}{2} = 26\frac{1}{4} \text{ km}$$



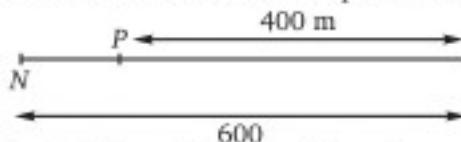
In the same time, when A covers 1500 m, B covers 1440 m and C covers 1425 m.

So, in 1440 m race B can give a start of 15 m.

\therefore In 1500 m race B will give a start of

$$\frac{15}{1440} \times 1500 = 15\frac{5}{8} \text{ m}$$

139. In 600 m race Prabhat can have only start of 120 m. Now since he has more than 200 m start up so he will win the race.



Now, when Prabhat will cover 400 m distance, then in the same time Nishith will cover only 500 m. So, Prabhat will win by 100 m.

140. B is 25% slower than A and C is 20% slower than B.

Therefore in a game of 200 points B can have 150 points and C can have 120 points.

Thus, A can give C 80 points.

141. Since between 11 am and 1 pm and 11 pm and 1 am two hands of a clock coincide only once, each time.

142. Since between 2 am and 3 am (2 pm and 3 pm) and 8 am and 10 am (8 pm and 10 pm) two hands of a clock make 90° angle only 3 times in rest of the each hour two hands make 90° angle 2 times.

143. Since between 5 am and 7 am (5 pm and 7 pm) this happens only once. In rest each of the hours it happens one time.

144. Both (a) and (b) are correct.

Relative speed = Speed of minute-hand

– Speed of hour-hand

$$= 6^\circ - \frac{1}{2}^\circ = 5\frac{1}{2}^\circ$$

$$\text{and } 1 \text{ min} - \frac{1}{12} \text{ min} = \frac{11}{12} \text{ min}$$

145. $\frac{5 \times 30}{11/2} = \frac{300}{11} = 27\frac{3}{11} \text{ min} = 27 \text{ min } 16 \text{ s}$

Therefore, required time = 5 : 27 : 16

146. The angle made by minute-hand = $5 \times 30 = 150^\circ$

The angle made by hour-hand = $2 \times 30 + 25 \times \frac{1}{2} = 72.5^\circ$

Hence, required angle = $150 - 72.5 = 77.5^\circ$

147. $\frac{90^\circ - 30^\circ}{5.5} = \frac{60}{11} \times 2 = \frac{120}{11} = 10\frac{10}{11} \text{ minute}$

$$= 10 \text{ min } 54 \text{ s}$$

\therefore Required time = 3 : 10 : 54

148. $\frac{210}{5.5} = \frac{210}{11} \times 2 = \frac{420}{11} = 38\frac{2}{11} \text{ min} = 38 \text{ min } 11 \text{ s}$

Therefore, required time = 7 : 38 : 11

149. The angle made by minute-hand = 90°

The angle made by hour-hand = $6 \times 30 + 15 \times \frac{1}{2} = 187.5^\circ$

\therefore Required difference = 97.5°

150. $\frac{90 - 35}{5.5} = \frac{55}{11} \times 2 = 10 \text{ min}$

So, the required time = 3 : 10 : 00

Again $\frac{90 + 35}{5.5} = \frac{125}{11} \times 2 = \frac{250}{11} = 22\frac{8}{11} \text{ min}$

$$= 22 \text{ min } 43 \text{ s}$$

LEVEL (2)

1.	Cycle	Auto	Car
Speed	x	$(5x - 20)$	$5x$
Time		$(t + 1)$	t
Distance	120	120	120 (in km)
	$\frac{120}{(5x - 20)} - \frac{120}{5x} = 1$		
\Rightarrow	$x^2 - 4x - 96 = 0$		
\Rightarrow	$x = 12$		
\therefore	Average speed = $\frac{360}{(10 + 3 + 2)} = 24 \text{ km/h}$		

2. Time taken by cycle = $\frac{120}{12} = 10 \text{ h}$

Time taken by auto = $\frac{120}{40} = 3 \text{ h}$

Time taken by car = $\frac{120}{60} = 2 \text{ h}$

Total time = 15 h

3. In last 5 hours she covers 240 km ($120 + 120$)

4. New time = $3 + 3 + 2 = 8 \text{ h}$

Hence, decrease in time = 7 h

(15 – 8)

\therefore Percentage change = $\frac{7}{15} \times 100 = 46.66\%$

5. Time taken to meet Bipasha and Mallika = $\frac{1080}{(60 + 120)} = 6 \text{ h}$

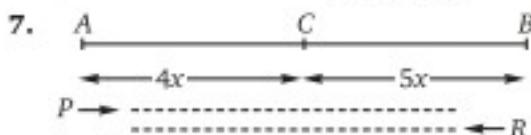
So, in 6 hours Bipasha covers 360 km and this 360 km distance Rani covers in $\frac{360}{90} = 4 \text{ h}$.

Hence, Rani leaves Kolkata 2 hours later than Bipasha i.e., at 8 am. Rani leaves Kolkata.

NOTE The distance 360 covered by Bipasha to meet Mallika can also be calculated by the ratio of their speeds.

6. Note here the length of the train in which passenger is travelling is not considered since we are concerned with the passenger instead of train. So, the length of the bridge will be directly proportional to the time taken by the passenger respectively.

Therefore, $\frac{t_1}{t_2} = \frac{l_1}{l_2}$ $t \rightarrow \text{Time}$
 $\frac{7}{4} = \frac{280}{x}$ $l \rightarrow \text{Length of bridge}$
 $\Rightarrow x = 160 \text{ m}$



Note that the distances covered by them to meet at C are in the direct ratio of their speeds. Therefore

$$AC : BC = 4x : 5x$$

Now, for any particular person (say Pathik) the time required to cover different distances is directly proportional to the different distances. So, time taken by Pathik to cover AC and BC are the ratio of 4 : 5 (excluding staying or halt time at Chandni Chowk).

Thus time required to cover AC is 52 minutes only since he covers BC in 65 minutes.

But since he leaves Chandni Chowk for Bhavnagar at 9 : 27 am i.e., 67 minutes later, when he left Andheri. It means he must have stayed at C for $(67 - 52) = 15$ minutes.

8. Let the length of the train be L metres and speeds of the train Arjun and Srikrishna be R , A and K respectively, then

$$\frac{L}{R - A} = 36 \quad \dots (i)$$

and $\frac{L}{(R + K)} = 24 \quad \dots (ii)$

From eq. (i) and (ii)

$$3(R - A) = 2(R + K)$$

$$\Rightarrow R = 3A + 2K$$

In 30 minutes (i.e., 1800 seconds), the train covers 1800R (distance) but the Arjun also covers 1800A (distance) in the same time.

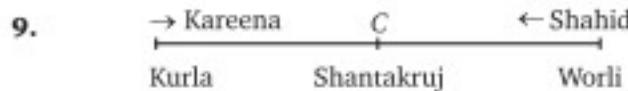
Therefore distance between Arjun and Srikrishna, when the train has just crossed Srikrishna

$$= 1800(R - A) - 24(A + K)$$

$$\therefore \text{Time required} = \frac{1800(R - A) - 24(A + K)}{(A + K)}$$

$$= (3600 - 24) = 3576 \text{ s}$$

$$(\text{Since } R = 3A + 2K)$$



Let the time taken by Kareena in going from C to S is x minutes and the time taken by Shahid in going from Worli to Shantakrui be y min.

Since, the new speed of Kareena is $\frac{2}{3}$, therefore time taken in returning $= \frac{3}{2}x$.

$$\therefore x + \frac{3}{2}x = 120$$

$$\Rightarrow x = 48 \text{ min}$$

$$\text{but } x = y$$

Again since the new speed of Shahid is $\frac{4}{3}$, therefore the time taken in returning $= \frac{3}{4}y$.

$$\therefore \text{Total time} = y + \frac{3}{4}y$$

$$= 48 + 36 = 84 \text{ min}$$

10. Time taken to collide the two trains $= \frac{3}{2} \text{ h}$

So, in $\frac{3}{2} \text{ h}$ bird travels $\frac{3}{2} \times 60 = 90 \text{ km}$

11. Let there be l steps in the escalator and x be the speed (in steps/second) of escalator, then

$$\frac{l}{(5 + x)} = 10 \quad \text{and} \quad \frac{l}{(5 - x)} = 40$$

$$\text{then} \quad \frac{5 + x}{5 - x} = \frac{40}{10} \Rightarrow x = 3$$

$$\therefore \text{Number of steps in the escalator} = l = 8 \times 10 = 80$$

12. Let the radius be r , then difference in the distance

$$= (\pi r - 2r) = r(\pi - 2)$$

$$= r\left(\frac{22}{7} - 2\right) = 60 \times 3$$

$$\Rightarrow 2r = 315 \text{ m}$$

$[\pi r \rightarrow \text{semiperimeter and } 2r \rightarrow \text{diameter}]$

13. Time taken by trains to collide $= \frac{560}{70} = 8 \text{ h}$

In 8 h sparrow will cover $8 \times 80 = 640 \text{ km}$

14.

In 18 h plane will cover $18 \times 120 = 2160 \text{ km}$

Now, $2160 = (600 \times 2) + 600 + 360$

So, the plane will be 360 km away from Kargil it means it will be 240 km ($600 - 360$) away from Pukhwara.

	First hour	Second hour	Third hour	Total
Initial speed	x	$3x$	$2x$	$6x$
New speed	$3x$	$3x$	$3x$	$9x$

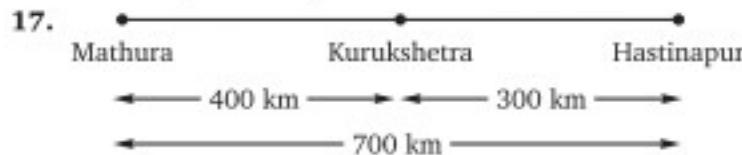
$$\therefore \text{Percentage increase in speed} = \frac{3x}{6x} \times 100 = 50\%$$

Since speed is increased by (50%) $\frac{1}{2}$

Therefore, time will reduce by (33.33%) $\frac{1}{3}$

16. 

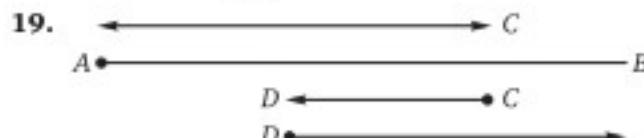
They will be together at every two hours. Therefore in 12 h they will be $(6 + 1) = 7$ times together at P and they will never meet altogether at Q.

17. 

Consider only one person either Arjun or Srikrishna since their speed is same and move together.

Now, the distance covered by Arjun and Abhimanyu is in the ratio of their speeds. So, Arjun will cover 500 km to meet Abhimanyu and thus Arjun has to return back 100 km for Kurukshetra. Therefore, Arjun will cover total 600 km distance.

$$18. \text{ Total time} = \frac{600}{25} = 24 \text{ h}$$

19. 

A is the starting point of journey.

B is the destination.

C \rightarrow where Salman has got off.

D \rightarrow where Priyanka picks up Akshay

Let $AD = l$ and $BC = k$ and $CD = x$

$$\text{then } \frac{CD + DB}{BC} = \frac{50}{10}$$

$$\frac{2x + k}{k} = \frac{5}{1}$$

$$\Rightarrow \frac{x}{k} = \frac{2}{1}$$

$$\text{Again } \frac{AC + CD}{AD} = \frac{50}{10}$$

$$\frac{2x + l}{l} = \frac{5}{1}$$

$$\Rightarrow \frac{x}{l} = \frac{2}{1}$$

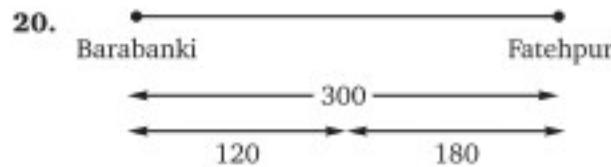
$$\Rightarrow x = 2k = 2l \text{ or } k = l = \frac{x}{2}$$

$$\therefore k + x + l = 120$$

$$\Rightarrow k = 30 \text{ km, } x = 60 \text{ km and } l = 30 \text{ km}$$

$$\begin{aligned} \text{Total distance travelled} &= AC + CD + DB \\ &= l + x + x + x + k = 240 \text{ km} \end{aligned}$$

$$\therefore \text{Time (required)} = \frac{240}{50} = 4.8 \text{ h}$$



Let the speeds of Ajai, Kajol and Shahrukh be x , y and z respectively, then

$$\frac{y}{x} = \frac{180}{120} \Rightarrow x = \frac{2y}{3}$$

Note Kajol is faster since she covers 180 km while Ajai covers only 120 km in the same time.

Shahrukh meets Kajol 1.5 hours after Shahrukh himself starts and 2.5 hours after Kajol starts.

$$\text{Hence, } 2.5y + 1.5z = 300$$

$$\Rightarrow z = \frac{600 - 5y}{3}$$

$$\text{Since } z \geq (y + 20) \Rightarrow \frac{600 - 5y}{3} \geq (y + 20)$$

$$\Rightarrow y \leq 67.5$$

$$\text{or } x \leq 45 \text{ km/h}$$

21. Let t be the time after Kajol starts, when she meets Ajai, then

$$t = \frac{300}{(x + y)}$$

This should be less than 2.5 or $(x + y) > 120$

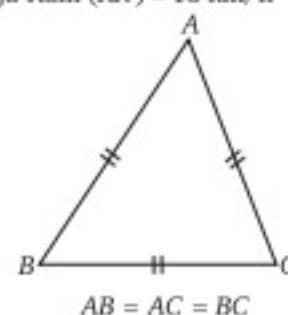
$$\text{Since } y = \frac{3x}{2} \Rightarrow y > 72$$

This ($y > 72$) is greater than 67.5 km/h and hence Shahrukh will always overtake Ajai before he meets Kajol.

22. Speed of Raghupati (R_p) = 60 km/h

Speed of Raghav (R_v) = 36 km/h

Speed of Raja Ram (RR) = 18 km/h



Time taken to cover AB by (RR) is 2 hours

\therefore Time taken to cover AB by Raghav is 1 hour

\therefore Time taken to cover AB by Raghupati = 36 min

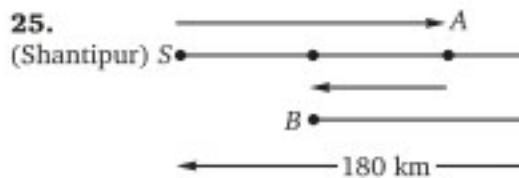
$$\left(t_{RP} : t_{RV} : t_{RR} = \frac{1}{S_{RP}} : \frac{1}{S_{RV}} : \frac{1}{S_{RR}} \right)$$

$t \rightarrow$ Time, $S \rightarrow$ Speed

$$AB = 2 \times 18 = 36 \text{ km}$$

$$23. \text{ Time} = \frac{3 \times 36}{60} = \frac{9}{5} \text{ h} = 1 \text{ h } 48 \text{ min}$$

$$\begin{aligned} 24. \text{ Distance from Barelley} &= \frac{60}{(60 + 18)} \times 36 \\ &= \frac{360}{13} = 27 \frac{9}{13} \text{ km} \end{aligned}$$



Since the speed of bike and walking are different. So, two people partially travelled by bike and rest by walking since all the three persons take equal time to reach the destination. It means initially Mohan will carry either Namit or Pranav to a point A , then this person reach to H by walking and Mohan return to B where he will pick up the third person and reach at H at the same time as the second person.

$$\text{Let } SB = k, AB = x \text{ and } AH = l$$

$$\text{Now, } \frac{SA + AB}{SB} = \frac{36}{6}$$

$$\frac{2x + k}{k} = \frac{6}{1}$$

$$\Rightarrow \frac{x}{k} = \frac{5}{2}$$

$$\text{and } \frac{AB + BH}{AH} = \frac{36}{6}$$

$$\Rightarrow \frac{2x + l}{l} = \frac{6}{1}$$

$$\Rightarrow \frac{x}{l} = \frac{5}{2}$$

$$\therefore x : k : l = 5 : 2 : 2$$

$$\Rightarrow x + k + l = 180$$

$$\Rightarrow x = 100, k = 40 \text{ and } l = 40 \text{ km}$$

$$\text{Total distance travelled by bike} = SA + AB + BH$$

$$= k + 3x + l = 380 \text{ km}$$

$$26. \frac{2x + k}{k} = \frac{42}{6} = \frac{7}{1}$$

$$\Rightarrow \frac{x}{k} = \frac{3}{1}$$

$$\text{Similarly } \frac{x}{l} = \frac{3}{1}$$

$$\therefore x : k : l = 3 : 1 : 1$$

$$\therefore x = 108, k = 36, l = 36 \text{ km}$$

$$\text{Total distance travelled} = k + 3x + l = 396 \text{ km}$$

$$\therefore \text{Required time} = \frac{396}{42} = 9 \frac{3}{7} \text{ h}$$

27. Let the buses leave from both the stations at time intervals of T , then the distance between any two consecutive buses coming opposite to me = the distance between any two consecutive buses coming in the same direction as me = VT . (where V is the velocity of the buses)
Let the speed of walking be W , then

$$\frac{VT}{V + W} = 20 \text{ and } \frac{VT}{V - W} = 30$$

$$\therefore \frac{V + W}{V - W} = \frac{30}{20} = \frac{3}{2}$$

$$\Rightarrow \frac{V}{W} = \frac{5}{1}$$

$$\therefore \frac{VT}{V + W} = 20$$

$$\Rightarrow \frac{5}{6} \times T = 20$$

$$\Rightarrow T = 24 \text{ min}$$

28. Time taken by Abhinav = 36 h

$$\text{Ideal time required by Abhinav} = \frac{600}{25} = 24 \text{ h}$$

It means Abhinav rests for $(36 - 24) = 12$ h

$$\text{Now, the required time for Brijesh} = \frac{600}{30} = 20 \text{ h}$$

But Brijesh utilised those 12 hours in which Abhinav rests, so he needs only $(20 - 12) = 8$ hours extra.

Thus, the total time taken by Brijesh = $36 + 8 = 44$ h

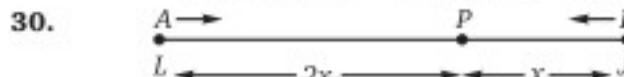
29. Downstream (Steamer) = 40 min

Downstream (Boat) = 60 min

Upstream (Steamer) = 60 min

Upstream (Boat) = 90 min

$$\text{Required time} = 40 + 30 + 45 = 115 \text{ min}$$



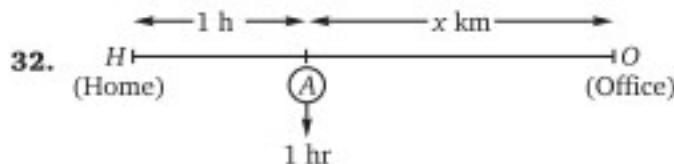
These two trains meet only at P and L i.e., there are only two points.

31. For the first meeting they have to cover only $2x + x = 3x$ distance and for the further meeting for each next meeting they have to cover $6x$ distance together.

Distance covered by A	2x	2x	4x	2x
Distance covered by B	x	4x	2x	4x
Point of meeting	P	L	P	P
Total distance travelled	3x	6x	6x	6x

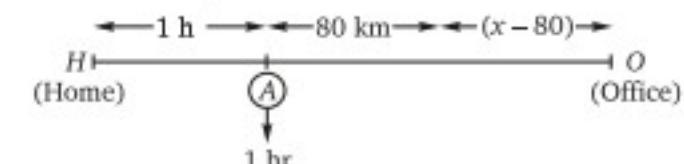
when A and B meet at P for the third time A goes $10x$ and B goes $11x$.

Thus, the required ratio = 10 : 11



$$\begin{array}{ll} \text{Speed} & \text{Time} \\ \frac{1}{6} \downarrow & \frac{1}{5} \uparrow = 36 \text{ min} \end{array}$$

\Rightarrow actual time required to cover x km is $5 \times 36 = 180$ min



$$\begin{array}{ll} \text{Speed} & \text{Time} \\ \frac{1}{6} \downarrow & \frac{1}{5} \uparrow = 20 \text{ min} \end{array}$$

\Rightarrow actual time required for $(x - 80)$ km = $5 \times 20 = 100$ min
It means he can move = $x - (x - 80) = 80$ km in

$$(180 - 80) = 80 \text{ min}$$

It means his actual speed = 60 km/h

Thus, the total distance from his home to his office

$$= 60 \times 1 + 60 \times 3 = 240 \text{ km}$$

NOTE Since 1 hour he lost at the place of accident, so the actual delay due to reduced speed is always 1 hour less than it is found to be in both the cases.
It means due to reduced speed he becomes late only 36 minutes and 20 minutes in respective cases.

33. $\frac{\text{Speed of wind (Sound)}}{\text{Relative speed of soldier and terrorist}} = \frac{\text{Time utilised}}{\text{Difference in time}}$

$$\frac{1188}{x} = \frac{330}{5}$$

$$\Rightarrow x = 18 \text{ km/h}$$

34. In case of increasing gap between two objects.

$$\frac{\text{Speed of sound}}{\text{Speed of tiger}} = \frac{\text{Time utilised}}{\text{Difference in time}}$$

$$\frac{1195.2}{x} = \frac{83}{7}$$

$$\Rightarrow x = 100.8 \text{ km/h}$$

35. In 20 minutes the difference between man and his son

$$= 20 \times 20 = 400 \text{ m}$$

Distance travelled by dog when he goes towards son

$$= \frac{400}{40} \times 60$$

= 600 m and time required is 10 minutes

In 10 minutes the remaining difference between man and son.

$$400 - (20 \times 10) = 200 \text{ m}$$

NOTE Relative speed of dog with child is 40 km/h and the same with man is 100 km/h.

$$\text{Time taken by dog to meet the man} = \frac{200}{100} = 2 \text{ min}$$

In 2 min the remaining distance between child and man

$$200 - (2 \times 20) = 160 \text{ m}$$

Now, the time taken by dog to meet the child again

$$= \frac{160}{40} = 4 \text{ min}$$

In 4 minutes he covers $4 \times 60 = 240 \text{ m}$ distance while going towards the son.

In 4 minute the remaining distance between man and child

$$= 160 - (4 \times 20) = 80 \text{ m}$$

Time required by dog to meet man once again

$$= \frac{80}{100} = 0.8 \text{ min}$$

In 0.8 min remaining distance between man and child

$$= 80 - (0.8 \times 20) = 64 \text{ m}$$

Now, time taken by dog to meet the child again

$$= \frac{64}{40} \times \frac{8}{5} \text{ min}$$

$$\therefore \text{Distance travelled by dog} = \frac{8}{5} \times 60 = 96 \text{ m}$$

Thus, we can observe that every next time dog just go 2/5th of the previous distance to meet the child in the direction of child.

So, we can calculate the total distance covered by dog in the direction of child with the help of GP formula.

$$\text{Here, first term (a)} = 600 \text{ and common ratio (r)} = \frac{2}{5}$$

$$\because \text{Sum of the infinite GP} = \frac{a}{1-r}$$

$$= \frac{600}{1 - \frac{2}{5}} = \frac{600}{3/5} = 1000 \text{ m}$$

36. Let Amarnath express takes x hours, then Gorakhnath express takes $(x - 2)$ hours.

$$\therefore \frac{1}{x} + \frac{1}{(x-2)} = \frac{60}{80}$$

$$\Rightarrow x = 4 \text{ h}$$

37. Distance travelled by them in first hour = 12 km

Distance travelled by them in second hour = 13 km

Distance travelled by them in third hour = 14 km and so on

Thus, in 9 hours they will cover exactly 144 km and in 9 h each will cover half-half the total distance.

$$(8 \times 9 = 72 \text{ and } 4 + 5 + 6 + 7 + 8 + 9 + 10 + 11 + 12 = 72)$$

38. Speed of tiger = 40 m/min

Speed of deer = 20 m/min

Relative speed = $40 - 20 = 20 \text{ m/min}$

Difference in distances = $50 \times 8 = 400 \text{ m}$

$$\therefore \text{Time taken in overtaking (or catching)} = \frac{400}{20} = 20 \text{ min}$$

\therefore Distance travelled in 20 min = $20 \times 40 = 800 \text{ m}$

39. The sum of their speeds = $\frac{615}{15} = 43 \text{ km/h}$

Notice that they are actually exchanging their speeds. Only then they can arrive at the same time at their respective destinations. It means the difference in speeds is 3 km/h.

$$\text{Thus, } x + (x + 3) = 43$$

$$\Rightarrow x = 20 \text{ and } x + 3 = 23$$

The concept is very similar to the case when after meeting each other they returned to their own places of departure. It can be solved through option also.

40. Let Pele covers x km in 1 hour. So Maradona takes $(2 \text{ h} - 40 \text{ min}) = 1 \text{ h } 20 \text{ min}$ to cover x km. Let speed of Maradona and Pele be M and P respectively than

$$x = M \times \frac{4}{3} \text{ and } x = P \times 1$$

$$\Rightarrow \frac{M}{P} = \frac{3}{4}$$

$$\text{Again } \frac{300}{M} - \frac{300}{P} = 1$$

$$\begin{aligned} \Rightarrow \quad & \frac{300}{3k} - \frac{300}{4k} = 1 \\ \Rightarrow \quad & k = 25 \\ \Rightarrow \quad & M = 3k = 75 \text{ km/h} \\ \text{and} \quad & P = 4k = 100 \text{ km/h} \\ \text{(Through option it is very easy to solve.)} \end{aligned}$$

41. Initial speed of police = 10 m/s

Increased speed of police = 20 m/s

Speed of thief = 15 m/s

Initial difference between thief and police = 250 m

After 5 seconds difference between thief and police

$$= 250 - (5 \times 10) = 200 \text{ m}$$

After 10 seconds more the difference between thief and police = $200 + (5 \times 10) = 250$ m.

Now, the time required by police to catch the thief

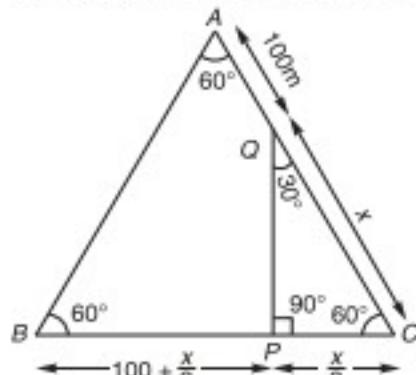
$$= \frac{250}{5} = 50 \text{ s}$$

Distance travelled = $50 \times 20 = 1000$ m

$$\text{Total time} = 50 + 15 = 65 \text{ s}$$

$$\text{Total distance} = 1000 + (15 \times 10) = 1150 \text{ m}$$

42.



$$\begin{aligned} \frac{100 + \frac{x}{2}}{100} &= \frac{100 + x}{(100 + x - 150)} \\ &= \frac{\text{Speed of Bajrang}}{\text{Speed of Angad}} \end{aligned}$$

$$\frac{200 + x}{200} = \frac{(100 + x)}{(x - 50)}$$

$$\Rightarrow (200 + x)(x - 50) = 200(100 + x)$$

$$\Rightarrow x^2 + 150x - 10000 = 20000 + 200x$$

$$\Rightarrow x^2 - 50x - 30000 = 0$$

$$\Rightarrow (x - 200)(x + 150) = 0$$

$$\Rightarrow x = 200 \text{ km}$$

Therefore distance between Ayodhya and Banaras is 300 km since $AB = BC = AC$.

(With the help of trigonometry we can find the value of PC in terms of x i.e., $\cos 60^\circ = \frac{PC}{QC} = \frac{1}{2}$. Hence $PC = \frac{x}{2}$)

43. Basically they will exchange their speeds just after half of the time required for the whole journey. It means after covering 210 km distance they will exchange their speeds.

Check it out graphically for more clarification.

44. The ratio of speeds

= The ratio of distances, when time is constant

∴ The ratio of distances covered by leopard to the tiger = 12 : 25

Again, ratio of rounds made by leopard to the tiger = 12 : 25

Hence, leopard makes 48 rounds, when tiger makes 100 rounds.

45. Length of $DC = \frac{6000}{13}$ (for this, refer geometry section)

Total distance covered in the returning by Jai

$$\begin{aligned} &= AD + CD \\ &= \frac{2500}{13} + \frac{6000}{13} = \frac{8500}{13} \text{ km} \end{aligned}$$

$$\text{Required time} = \frac{8500/13}{500/13} = 17 \text{ h}$$

Total distance covered by Jaya while returning

$$\begin{aligned} &= BD + DC \\ &= \frac{14400}{13} + \frac{6000}{13} \end{aligned}$$

$$\therefore \text{Required time} = \frac{20400/13}{1200/13} = 17$$

Hence, both will reach at the same time.

Alternatively: Since the ratio of speeds is same as that of distances. So, they will take same time to reach the home.

46. The distance of route $ADC = \frac{8500}{13}$

and the distance of route $BNC = 1300$

$$\text{and the time taken by Jai is } \frac{8500/13}{500/13} = 17 \text{ h}$$

$$\text{and the time taken by Jaya is } \frac{1300}{1200/13} = \frac{169}{12} \text{ h} = 14 \frac{1}{12} \text{ h}$$

$$= 14 \text{ h } 05 \text{ min}$$

Hence, option (c) is correct.

47. Time saved in percentage = $\frac{175}{1020} \times 100 = 17.15\%$

48. Husband takes 17 hours and she takes 14 h 05 min + 3h
= 17 h 05 min

So, she becomes late by 05 min than her husband.

49. $x^2 + (x + 100)^2 = (500)^2$ (Using Pythagoras theorem)

$$\Rightarrow x = 300 \text{ km}$$

Now, let they change their speeds after t_1 hours and then the rest time is t_2 then

$$30t_1 + 40t_2 = 800 \quad \dots (i)$$

$$40t_1 + 30t_2 = 900 \quad \dots (ii)$$

Solving Eq. (i) and (ii), we get

$$t_1 = \frac{120}{7} \text{ and } t_2 = \frac{50}{7}$$

50. Since it moves only one radian on every path and it has to move 2π radian to reach directly eastward. Hence, it has to run on more than 6 paths i.e., the last path is 7th one (or P_7)
($\because n \times 1 \text{ radian} \geq 2\pi \text{ radian}$)

$$\Rightarrow n \geq 2\pi$$

or $n = 7$, for integer values

Hence, option (c) is correct.

51. Since it stops directly eastward of the shop so the total distance covered so far

$$= 7 + (1 + 2 + 3 + 4 + 5 + 6 + 2) = 30 \text{ km}$$

NOTE Total radial movement = 7 km

Again on the last path it will move only 2 km.

Actually it has to cover total 2π radian distance but on 6 paths it covers only 6 radian hence the remaining distance which will be covered on the 7th path i.e., $2\pi - 6$

$$= 2 \times \frac{22}{7} - 6 = \frac{2}{7} \text{ radian}$$

But, the radius of the last path (i.e., P_7) = 7 km

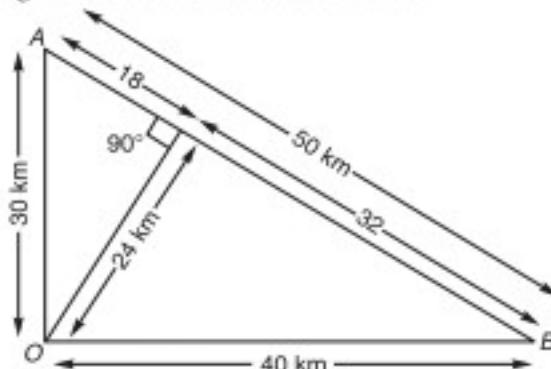
Hence, the distance covered in km = $\frac{2}{7} \times 7 = 2 \text{ km}$

$$\left(\theta = \frac{\text{Arc}}{\text{Radius}} \right)$$

Thus, on the last path it moves only 2 km. Hence, (a) is the correct choice.

52. The ratio of distance covered on P_2 and P_7 = $\frac{2}{2} = \frac{1}{1}$

53. Since it is clear from the statement itself that ΔAOB is a right angle triangle and further OP must be perpendicular to AB then we can find that $AO = 30 \text{ km}$ and $BO = 40 \text{ km}$ by using Pythagoras theorem and its corollaries.



HINT

$$OP^2 = OA^2 - AP^2$$

∴

$$OP^2 = 900 - x^2$$

and

$$OB^2 = OP^2 + BP^2$$

∴

$$OB^2 = 900 - x^2 + 1024$$

and

$$AB^2 = OA^2 + OB^2$$

∴

$$(x + 32)^2 = 900 + 900 - x^2 + 1024$$

∴

$$x = 18 \text{ km}$$

Hence, $AP = 18$, $OA = 30$ and $OB = 40$ and $OP = 24 \text{ km}$

Now, since jackal and cat reaches A at the same time, so the ratio of speeds = ratio of distances covered by them.

$$\therefore \frac{\text{Speed of jackal}}{\text{Speed of cat}} = \frac{30}{18} = \frac{5}{3}$$

54. Again, since jackal and train both arrive at A at the same time and let the train was $x \text{ km}$ away from A, before entering into the tunnels, i.e., when it makes a whistle then the ratio of distances covered by train and jackal.

$$= \frac{x}{30} = \frac{x + 50}{40}$$

$$\Rightarrow x = 150 \text{ km}$$

Thus, the ratio of speeds of Jackal is to train is 1 : 5.

55. Since, when the train arrive at A, the jackal can move 30 km. So, at the time when train is at A the jackal will cover 6 km from P on PA in addition to 24 km at OP. Now, the rest distance at AP is 12 km this remaining distance will be covered by train and jackal according to their respective speeds.

$$\text{So, distance covered by train} = 12 \times \frac{5}{6} = 10 \text{ km}$$

$$\text{and distance covered by jackal} = 12 \times \frac{1}{6} = 2 \text{ km}$$

Hence, jackal will meet with train at M_1 which is 10 km away from A (inside AB).

NOTE It can be solved using options in lesser time.

56. It is obvious from the path of cat that if cat moves in the POA direction it will never meet with accident and now jackal follows the path OPB. Again when the train is at A then jackal will cover 30 km (i.e., 24 (OP) + 6 km on PB).

So, the ratio of distances covered by jackal is to train = ratio of their respective speeds.

Now let the jackal and train meet each other at AB , $(6 + x)$ km away from P towards B, then

$$\frac{x}{24 + x} = \frac{1}{5}$$

$$\Rightarrow 4x = 24 \Rightarrow x = 6$$

Hence, train meets with jackal at $(18 + 6 + 6) = 30 \text{ km}$ away from A.

$$\text{Alternatively: } \frac{150 + 18 + 6 + x}{30 + x} = \frac{5}{1} \Rightarrow x = 6$$

Hence, $18 + 6 + 6 = 30 \text{ km}$.

Thus, option (b) is correct.

57. The ratio of time taken by cat and jackal = $\frac{72/3}{96/5} = \frac{5}{4}$

Hence, option (c) is correct.

58. $(6 - x) = (8 - 1.5x)$

$$\Rightarrow x = 4 \text{ cm}$$

So, it will take 4 hours to burn in such a way that they remain equal in length.

59. Total distance covered by them when they meet = $2W$

$$\text{and} \quad \text{Total time} = \frac{2W}{b_1 + b_2}$$

$$\therefore d_1 = \frac{2W}{(b_1 + b_2)} b_1 \quad \text{and} \quad d_2 = \frac{2W}{(b_1 + b_2)} b_2$$

60. Let the speed of boat be B and that of river be R . In 12 minutes the distance between boat and hat

$$= 12(B - R) + 12R = 12B$$

Now time taken by boat to reach to the hat

$$= \frac{12B}{(B + R) - R} = 12 \text{ min}$$

Total time = 24 min

In 24 minutes had flown off = 3 km

$$\therefore \frac{24}{60} \times R = 3$$

$$\Rightarrow R = 7.5 \text{ km/h}$$

61. Akbar meets Birbal once $\frac{500}{20-15} = 100 \text{ s}$

Birbal meets Chanakya once $\frac{500}{20+25} = 11 \frac{1}{9} \text{ s}$

Akbar meets Chanakya once $\frac{500}{15+25} = 12.5 \text{ s}$

62. Time taken by them to meet $\frac{600}{30-20} = 60 \text{ s}$

Time taken to meet 5th time $= 5 \times 60 = 300 \text{ s}$

Total duration of race $= \frac{3000}{30} = 100 \text{ s}$

So, they will not meet 5th time in the race of 3000 metre.

63. Length of the track $= 2 \times \frac{22}{7} \times 175 = 1100 \text{ m}$

Distance to be covered for the first meeting = 550 m

Speed of Akkal $= \frac{1100}{100} = 11 \text{ m/s}$

Speed of Bakkal $= \frac{1100}{50} = 22 \text{ m/s}$

Time taken from the start of the first meeting

$$= \frac{550}{(11+22)} = \frac{50}{3} \text{ s}$$

Time taken for Akkal and Bakkal to meet again at Love point = LCM of times taken by them to go around the track once.

$$= \text{LCM of } \frac{1100}{11} \text{ and } \frac{1100}{22}$$

$$= \text{LCM of } 100 \text{ and } 50$$

$$= 100 \text{ s}$$

So, the total required time $= \frac{50}{3} + 100 + 100$

$$= \frac{650}{3} = 216 \frac{2}{3} \text{ s}$$

64. Since both rest for 6 seconds so when B is just about to start the journey A reaches there at the shallow end so they meet at they shallow end.

65. B runs around the track in 10 min.

i.e., Speed of B = 10 min per round

$\therefore A$ beats B by 1 round

Time taken by A to complete 4 rounds

$$= \text{Time taken by B to complete 3 rounds}$$

$$= 30 \text{ min}$$

$\therefore A$'s speed $= \frac{30}{4} \text{ min per round}$

$$= 7.5 \text{ min per round}$$

Hence, if the race is only of one round A's time over the course = 7 min 30 sec.

66. The ratio of speeds of A, B, C $= \frac{10}{49} : \frac{9}{50} : \frac{8}{51}$

Hence, A is the fastest.

67. Speed of this car $= \frac{400+200}{20} \times \frac{18}{5} \text{ km/h}$

$$= 108 \text{ km/h}$$

68. The speeds of two persons is 108 km/h and 75 km/h. The first person covers 1080 km in 10 hours and thus he makes 12 rounds. Thus, he will pass over another person 12 times in any one of the direction.

69. Angle between two hands at 3 : 10 am

$$= (90 + 5) - 60 = 35^\circ$$

So, the required angle = 70° , after 3 : 10 am

Total time required to make 70° angle when minute-hand is ahead of hour-hand.

$$= \frac{90+70}{11/2} = \frac{320}{11} \text{ min}$$

So, at 3 h $\frac{320}{11}$ min the required angle will be formed.

Alternatively: Check through options.

70. **For the first watch:** When a watch creates the difference of 12 hours, it shows correct time.

So to create the difference of 12 h required time

$$= \frac{60 \times 12}{24} = 30 \text{ days}$$

For the second watch: To create the difference of 12 h required time

$$= \frac{30 \times 12}{24} = 15 \text{ days}$$

So, after 30 days at the same time both watches show the correct time.

HINT Take the LCM of 30 and 15.

71. To show the same time together the difference between two watches must be 12 h.

Now, since they create 3 min difference in 1 h

So they will create 12 h difference in $\frac{1}{3} \times \frac{12 \times 60}{24}$

$$= 10 \text{ days later}$$

72. To show the correct time again, watch must create 24 h difference. (Since in one round hour-hand covers 24 h.)

So, the required time $= \frac{4}{3} \times \frac{60 \times 24}{24} = 80 \text{ day}$

73. $(n+1)$ times in n days

74. Actually the watch gains $(12+16)$

$$= 28 \text{ min in } 7 \times 24 \times 60 \text{ min.}$$

Thus, it gains 1 min in 360 minutes.

Therefore, it will gain $(12+8)$ min in $\frac{20 \times 360}{60 \times 24} = 5 \text{ day}$

Hence, (b) is the correct choice.

75. Actually they create a difference of 3 min per hour and the two watches are showing a difference of 66 minutes. Thus, they must have been corrected 22 hours earlier.

Now, the correct time can be found by comparing any one of the watch.

Since, second watch gains 1 min in 1 hour so it will must show 22 min extra than the correct time in 22 hours.

Hence, the correct time can be found by subtracting 22 min from 10 : 06.

Hence, (d) is the correct answer.

NOTE For quick answer go through options.

76. Incorrect watch covers 1452 min in 1440 min

So, it will cover 1 min in $\frac{1440}{1452}$ min

$$\begin{aligned} \text{Therefore it will cover 4840 min in } & \frac{1440}{1452} \times 4840 \\ & = 4800 \text{ min} \\ & = 80 \text{ h} \end{aligned}$$

Therefore $80 \text{ h} = 3 \text{ days and } 8 \text{ h.}$

77. You must know that a correct watch coincide just after $65 \frac{5}{11}$ min.

Therefore in every $65 \frac{5}{11}$ hours the watch gains $\frac{2}{11}$.

Hence, in 24 hours it will gain $\frac{2}{11} \times \frac{11}{720} \times 24 \times 60 = 4 \text{ min}$

78. In 72 hours my watch gains $(8 + 7) = 15 \text{ min}$. To show the correct time watch must gain 8 minutes.

Since the watch gains 15 min in $72 \times 60 \text{ min}$.

Therefore, the watch will gain 8 min in $\frac{72 \times 60 \times 8}{15} \text{ min}$

$$= \frac{72 \times 60 \times 8}{15} = 38 \text{ h } 24 \text{ min}$$

Hence, (a) is the correct choice.

80. To exchange the position both hands to cover 360° together.

In one minute, hour-hand moves $\frac{1}{2}^\circ$ and in one minute, minute-hand moves 6° . Let the required time be t min, then

$$\begin{aligned} 6t + \frac{1}{2}t &= 360 \\ \Rightarrow t &= \frac{360}{13} \times 2 = \frac{720}{13} = 55 \frac{5}{13} \text{ min} \end{aligned}$$



8

TIME AND WORK

This chapter is one of the easiest chapter for the students. Even an average student can perform better than in other chapters. There is basically one concept involved in this chapter *i.e.*, concept of efficiency. So most of the problems are very similar in their basic characteristic. Almost every aptitude exam ask the problems from this chapter. On an average 2-3 problems from this chapter have been asked in past years in CAT.

As it is very clear to all of us that the work is directly related with time. As one can say if a particular person or machine works for more time then more work will be done and if it devotes less time then it yields less work *i.e.*, output of a machine or person is directly proportional to time, provided that he/she maintains his/her efficiency during the work.

CONCEPT OF EFFICIENCY

Suppose a person can complete a particular work in 2 days then we can say that each day he does half of the work or 50% work each day. Thus it is clear that his efficiency is 50% per day. Efficiency is generally considered with respect to the time. The time can be calculated either in days, hours, minutes or months etc. So if a person completes his work in 4 days, then his efficiency (per day) is 25%. Since each day he works 1/4th of the total work (*i.e.*, 25% of the total work).

I would like to mention that the calculation of percentage and conversion of ratios and fractions into percentage and vice versa is the prerequisite for this chapter.

Now, if a person can complete a work in n days then his one day's work = $\frac{1}{n}$

and this one day's work in terms of percentage is called his efficiency.

Also if a person can complete $\frac{1}{n}$ work in one day, then he can complete the whole work in n days.

Relation between work of 1 unit of time and percentage efficiency.

A person can complete his work in n days, then his one day's work = $\frac{1}{n}$, his percentage efficiency = $\frac{1}{n} \times 100$

No. of days/hours etc. required to complete the whole work	Work of 1 day/hour	Percentage efficiency
n	$1/n$	$100/n$
1	1/1	100%
2	1/2	50%
3	1/3	$33.33\% = 33\frac{1}{3}\%$
4	1/4	25%
5	1/5	20%
6	1/6	$16.66\% = 16\frac{2}{3}\%$
7	1/7	$14.28\% = 14\frac{2}{7}\%$
8	1/8	12.5%
9	1/9	$11.11\% = 11\frac{1}{9}\%$
10	1/10	10%

This table is very similar to the percentage fraction table given in the chapter of percentage. This table just manifests as a model for efficiency conversion.

Basically for faster and smarter calculation you have to have your percentage calculation very smart.

All the problems of this chapter can be solved through two methods :

1. Unitary method
2. Percentage efficiency

Unitary method is generally obsolete in respect to high level aptitude exam of CAT since it involves typical calculation of LCM each and every time. But when the problems are solved through percentage efficiency it becomes inevitable to save the time which in turn helps to do some more problems within the stipulated time. I admit that initially it might be difficult to solve for those students who are not so good and confident in percentage and fraction calculation, but a little bit of extra Practice will yield an unexpected result in quicker calculations. Now I have some good examples to show you both the methods of solving the same problems.

EXAMPLE 1 A can do a job in 12 days and B can do the same job in 6 days, in how many days working together they can complete the job?

SOLUTION

$$A's \text{ 1 day's work} = \frac{1}{12}$$

$$B's \text{ 1 day's work} = \frac{1}{6}$$

$$\therefore (A + B)'s \text{ 1 day's work} = \frac{1}{12} + \frac{1}{6} = \frac{3}{12} = \frac{1}{4}$$

$$\therefore \text{Time taken by both to finish the whole work} = \frac{1}{\frac{1}{4}} = 4 \text{ days}$$

Alternatively :

$$\text{efficiency of } A = \frac{100}{12} = 8.33\%$$

$$\text{and } \text{efficiency of } B = \frac{100}{6} = 16.66\%$$

$$\text{Combined efficiency of } A \text{ and } B \text{ both} = 8.33 + 16.66 = 25\%$$

$$\therefore \text{Time taken by both to finish the work (working together)} = \frac{100}{25} = 4 \text{ days}$$

NOTE As per my experience, I have found that in this chapter only selected (numerals) numbers are always used and thus there are almost 20 – 25 numbers are frequently used. So one can very easily remember (and calculate) the percentage efficiency but with different combinations to calculate the LCM becomes a very tedious job. Still you can choose your own method, which is comfortable to you.

RELATION BETWEEN EFFICIENCY AND TIME

Efficiency is inversely proportional to the time (i.e., number of days, hours, minutes) etc.

EXAMPLE 1 A takes 16 days to finish a job alone, while B takes 8 days to finish the same job. What is the ratio of their efficiency and who is less efficient?

SOLUTION Since A takes more time than B to finish the same job hence A is less efficient or

$$\text{efficiency of } A = \frac{100}{16} = 6.25\%$$

$$\text{and } \text{efficiency of } B = \frac{100}{8} = 12.5\%$$

$$\text{ratio of efficiency of } A : B = \frac{1}{16} : \frac{1}{8} = 1 : 2$$

Hence, B is twice efficient as A.

EXAMPLE 2 A is thrice efficient as B and A takes 20 days to do a job, then in how many days B can finish the same job?

SOLUTION Ratio of efficiency of $A : B = 3 : 1$

$$\therefore \text{Ratio of required days of } A : B = \frac{1}{3} : \frac{1}{1} = 1 : 3$$

Now since A takes 20 days. So B will take 60 days to finish the same job.

NOTE Ratio of number of days is equal to the ratio of the reciprocals of efficiency and vice-versa.

EXAMPLE 2 A can do a job in 10 days, B can do the same job in 12 days and C can do the same job in 15 days. In how many days they will finish the work together?

SOLUTION

$$A's \text{ 1 day's work} = \frac{1}{10}$$

$$B's \text{ 1 day's work} = \frac{1}{12}$$

$$C's \text{ 1 day's work} = \frac{1}{15}$$

$$(A + B + C)'s \text{ one day's work} = \frac{1}{10} + \frac{1}{12} + \frac{1}{15} = \frac{15}{60} = \frac{1}{4}$$

Since they can complete $\frac{1}{4}$ work in 1 day. So they will finish the whole work in $\frac{1}{\frac{1}{4}} = 4$ days.

Alternatively : A's efficiency = 10%

B's efficiency = 8.33%

C's efficiency = 6.66%

Combined efficiency of A, B and C = $10 + 8.33 + 6.66 = 25\%$

Hence, they will take $\frac{100}{25} = 4$ days to finish the job working together

(Since in one day they complete 25% work)

For example if A is twice efficient as B, it means, A takes half the time to finish the same job as B requires working alone.

EXAMPLE 3 P is thrice as efficient as Q and is therefore able to finish a piece of work in 60 days less than Q. Find the time in which P and Q can complete the work individually.

SOLUTION Efficiency of $P : Q = 3 : 1$

Required number of days of $P : Q = 1 : 3$

i.e., if P requires x days then Q requires $3x$ days

but $3x - x = 60$

$\Rightarrow 2x = 60$

$\Rightarrow x = 30$ and $3x = 90$

Thus P can finish the work in 30 days and Q can finish the work in 90 days.

EXAMPLE 4 A is twice as good a workman as B and is therefore able to finish a piece of work in 30 days less than B. In how many days they can complete the whole work; working together?

SOLUTION Ratio of efficiency = $2 : 1 (A : B)$

Ratio of required time = $1 : 2 (A : B) \Rightarrow x : 2x$

but $2x - x = 30$

$\Rightarrow x = 30$ and $2x = 60$

now efficiency of $A = 3.33\%$

and efficiency of $B = 1.66\%$

Combined efficiency of A and B together = 5%
 \therefore time required by A and B working together to finish the work
 $= \frac{100}{5} = 20$ days.

NOTE

$$\text{Efficiency} \propto \frac{1}{\text{number of time units}}$$

$$\therefore \text{Efficiency} \times \text{time} = \text{constant work}$$

$$\text{Hence} \quad \text{Required time} = \frac{\text{work}}{\text{efficiency}}$$

Whole work is always considered as 1, in terms of fraction and 100%, in terms of percentage.

$$\text{In general, number of day's or hours} = \frac{100}{\text{efficiency}}$$

EXAMPLE 5 *A can do a works in x days while B can do the same work in y days then in how many days will they complete the work, working together?*

CONCEPT OF NEGATIVE WORK

In this case one person works but another destroys it or cancels it. For example Sonu can write 20 pages per hour but his younger sister Rimjhim erases 10 pages per hour which

EXAMPLE 1 *A tub can be filled in 20 minutes but there is a leakage in it which can empty the full tub in 60 minutes. In how many minutes it can be filled?*

$$\begin{aligned} \text{SOLUTION} \quad \text{Filling efficiency} &= 5\% \quad \left(\because 5 = \frac{100}{20} \right) \\ \text{emptying efficiency} &= 1.66\% \quad \left(\because 1.66 = \frac{100}{60} \right) \\ \text{Net efficiency} &= 5 - 1.66 = 3.33\% \\ \therefore \text{Required time to fill the tub} &= \frac{100}{3.33} = 30 \text{ minutes} \end{aligned}$$

**APPLICATION OF INVERSE PROPORTION
(OR PRODUCT CONSTANCY)**

As I have already discussed thoroughly the concept of inverse proportion and product constancy in ratio-proportion and it has been widely used in profit loss chapter also.

Since the efficiency or rate of work done in one unit of time (mentioned) is inversely proportional to the time i.e., if the rate of work done is greater then the time required will be less and if the rate of work done is less then the time required for the

EXAMPLE 1 *If 20 persons can do a piece of work in 7 days then calculate the number of persons required to complete the work in 28 days*

$$\text{SOLUTION} \quad \text{Number of persons} \times \text{days} = \text{work}$$

$$20 \times 7 = 140 \text{ man-days}$$

Now,

$$x \times 28 = 140 \text{ man-days}$$

SOLUTION

$$A's \text{ one day's work} = \frac{1}{x}$$

$$B's \text{ one day's work} = \frac{1}{y}$$

So, both A and B completes $\frac{1}{x} + \frac{1}{y} = \frac{x+y}{xy}$ work in one day.

Now, by Unitary method

$$\frac{x+y}{xy} \text{ work can be completed in 1 day}$$

$\therefore 1$ (means complete) work will be finished in $\frac{1}{\frac{x+y}{xy}} = \frac{xy}{x+y}$ days

$$= \frac{xy}{x+y} \text{ days.}$$

$(\because \text{Required time to complete the work} = \frac{1}{\text{one day's work}})$

Sonu writes.

It means finally Sonu writes 10 pages per hour since each hour his sister erases 10 pages out of 20 written pages. Take another example :

Alternatively : In 1 minute tub is filling $= \frac{1}{20}$

In 1 minute tub is emptying $= \frac{1}{60}$

$$\begin{aligned} \therefore \text{In 1 minute, effective filling of tub} &= \frac{1}{20} - \frac{1}{60} \\ &= \frac{2}{60} = \frac{1}{30} \end{aligned}$$

Since $\frac{1}{30}$ part of tub is filled in 1 minute.

Therefore complete tub will be filled in $\frac{1}{\frac{1}{30}} = 30$ minutes

same amount of work will be more.

This product constancy method is limited to the constant work, if the amount of work gets changed, then it does not work, then we have to take help from the unitary method.

When more than one man/machine work on a particular work/project, the rate of work is calculated as the strength of workers working in a particular time. So the amount of work is defined in terms of man-days or man-hours or man-days-hours.

$$\Rightarrow x = 5$$

Therefore in second case the required number of person is 5.

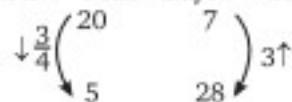
Second Method : Since work is constant, therefore

$$M_1 \times D_1 = M_2 \times D_2 = \text{work done}$$

$$20 \times 7 = M_2 \times 28$$

$$\Rightarrow M_2 = 5$$

Third Method : Men \times days = work, which is constant



Since number of days is increased by 3 times (i.e., 300%). So the number of men will be decreased by $\frac{3}{4}$ times (i.e., 75%)

(remember percentage change graphic)

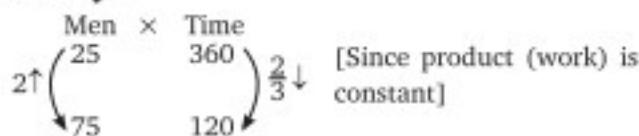
EXAMPLE 2 If 25 men can do a piece of work in 36 days working 10 hours a day, then how many men are required to complete the work working 6 hours a day in 20 days?

SOLUTION $M_1 \times D_1 \times H_1 = M_2 \times D_2 \times H_2$

$$25 \times 36 \times 10 = M_2 \times 20 \times 6$$

$$\Rightarrow M_2 = 75 \text{ persons}$$

Alternatively :



By percentage change graphic, when time is decreased by $\frac{2}{3}$ (i.e., 66.66%), number of men is increased by 2 times (i.e., 200%)

EXAMPLE 3 A contractor employed 30 men to complete the project in 100 days. But later on he realised that just after 25 days only 20% of the work had been completed.

- How many extra days, than the scheduled time are required?
- To complete the work on the scheduled time how many men he has to increase?
- If the amount of work is also increased by 20% of the actual work, then how many extra days are required (in comparison with scheduled time) but the number of men remained constant.
- How many men should be increased so that the work will be completed in 25 days less than the scheduled time.

SOLUTION (a) Men \times days = work done

$$30 \times 25 = 750 = 20\% \text{ of the actual work}$$

Now, the work to be done is 4 times than the work done but the number of days is only 3 times. So he is required 4 times the number of days, thus he has to work for extra 25 days.

$$(b) M_1 D_1 = M_2 D_2$$

$$4(30 \times 25) = M_2 \times 75$$

RELATION BETWEEN EFFICIENCIES

In this case the efficiencies of different persons are different but when they work in a group, so the efficiency of the group is required to know the time taken. For example 3 men can do a work in 4 days while 12 boys can do the same work in 3 days. It means we need $3 \times 4 = 12$ man-days i.e., 12 men can finish the job in 1 day.

$$\Rightarrow M_2 = 40$$

(Since, the work to be done is 4 times of the work done. Hence he requires 4 times man-days.)

Alternatively : Since the new product (i.e., work) is 4 times of the original product (i.e., work). But the new product is being multiplied by 3. Thus to make it 4 times we have to multiply it by $4/3$. Thus without changing number of days we get the new value of number of men which is 40 (being multiplied by $4/3$)

Therefore he has to increase 10 more men.

$$(c) \text{ New work} = 3750 \text{ man-days}$$

$$\text{and} \quad \text{the available number of men} = 30$$

$$\therefore \text{number of days required} = \frac{3750}{30} = 125$$

So, he has to work for extra 50 days where

$$50 = (125 - 75)$$

$$(d) \text{ Work} = 3000 \text{ unit (man days)}$$

$$\text{number of available days} = 50 (75 - 25)$$

$$\therefore \text{number of men required} = \frac{3000}{50} = 60$$

Thus he has to increase $(60 - 30) = 30$ more men.

EXAMPLE 4 16 workers working 6 hours a day can build a wall of length 150 metres, breadth 20 m and height 12 m in 25 days. In how many days 12 workers, working 8 hours a day can build a wall of length 800 m, breadth 15 m and height 6 m.

SOLUTION Here work is the volume of the wall. So the work force should be increased/decreased in the ratio of volume of the work. Therefore

$$\frac{L_1 B_1 H_1}{L_2 B_2 H_2} = \frac{M_1 D_1 T_1}{M_2 D_2 T_2}$$

where L, B, H are length, breadth and height of the wall respectively and M, D, T are men, days and time in hours per day, respectively. 1 indicates the first case, while 2 indicates second case. So the ratio of work force remains constant as the ratio of volume and work.

$$\therefore \frac{150 \times 20 \times 12}{800 \times 15 \times 6} = \frac{16 \times 6 \times 25}{12 \times 8 \times D_2}$$

$$\Rightarrow D_2 = 50$$

hence the required number of days = 50

Please notice that the volume of work becomes twice (in the second case) so the work force will also be twice to the previous work force.

Similarly we need $12 \times 3 = 36$ boys days i.e., 36 boys can finish the same job in 1 day.

Here we can see that to finish the work in only 1 day 12 men are needed while 36 boys are needed. Thus we can conclude that work of 12 men is equal to the work of 36 boys. Therefore efficiency of 12 men is equal to 36 boys i.e., we can say the efficiency of 1 man is equal to 3 boys. Thus a man is thrice efficient as a boy or we can say that a man is two times more efficient than a boy.

EXAMPLE 1 6 boys and 8 women finish a job in 6 days and 14 boys and 10 women finish the same job in 4 days. In how many days working together 1 boy and 1 woman can finish the work?

SOLUTION In this kind of questions we find the work force required to complete the work in 1 day (or given unit of time) then we equate the work force to find the relationship between the efficiencies (or work rate) between the different workers.

$$\text{Therefore } 6B + 8W = 6 \text{ days}$$

$$\Rightarrow 6(6B + 8W) = 1 \text{ day} \quad (\text{inversely proportional})$$

$$\Rightarrow 36B + 48W = 1 \quad (\text{by unitary method})$$

$$\text{Again } 14B + 10W = 4 \text{ days}$$

$$\Rightarrow 56B + 40W = 1$$

So, here it is clear that either we employ 36B and 48W to finish the work in 1 day or 56B and 40W to finish the same job in 1 day. Thus, we can say

$$\Rightarrow 36B + 48W = 56B + 40W$$

$$\Rightarrow 20B = 8W$$

$$\Rightarrow W = 2.5B$$

Thus a woman is 2.5 times as efficient as a boy.

$$\text{Now, since } 36B + 48W = 1$$

$$\Rightarrow 36B + 48 \times (2.5B) = 1$$

$$\Rightarrow 156B = 1$$

i.e., to finish the job in 1 day 156 boys are required or the amount of work is 156 boys-days.

$$\text{Again } 1W + 1B = 2.5B + 1B = 3.5B$$

Now, since 156 boys can finish the job in 1 day

So 1 boy can finish the job in 1×156 days

$$\therefore 3.5 \text{ boys can finish the job in } \frac{1 \times 156}{3.5} = 44 \frac{4}{7} \text{ days}$$

NOTE There is a great difference between 'and' & 'or'

For example 4 men and 8 women can do a piece of work in 10 days : means it is unknown that who is faster or slower (i.e., we don't know the relation between efficiencies of a man and a woman)

Again, 4 men or 8 women can do a piece of work in 10 days : means 4 men are equal to 8 women. Hence a man is twice efficient as a woman.

EXAMPLE 2 6 men and 8 women can do a job in 10 days. In how many days can 5 men and 9 women do the same job?

SOLUTION Since we don't know the relation between work rate (or efficiency) between a man and that of a woman so we can't find the required number of days.

EXAMPLE 3 6 men and 8 women can do a job in 10 days. In how many days can 3 men and 4 women finish the same job working together?

SOLUTION Notice here we don't know the relation of efficiencies but we can solve the problem due to clear relation between the work force.

$$\text{Since } 6M + 8W = 10 \text{ days}$$

$$2(3M + 4W) = 10 \text{ days}$$

$$\Rightarrow (3M + 4W) = 20 \text{ days}$$

Since, the work force has become half of the original force so number of days must be double.

Thus required number of days = 20

EXAMPLE 4 A can complete a work in 12 days, B in 15 days. Find the time taken by them :

- when A and B worked together.
- when A and B worked alternatively started by A.
- when A and B worked alternatively started by B.
- if A started two days later, in comparison to B.
- if B started two days later, in comparison to A.
- if A leaves two days before the actual completion of the work.
- if B leaves two days before the actual completion of the work.
- if A leaves two days before the scheduled completion of the work.
- if B leaves two days before the scheduled completion of the work.
- if B does negative work with his same work rate.

SOLUTION (a) A's efficiency = 8.33%

B's efficiency = 6.66%

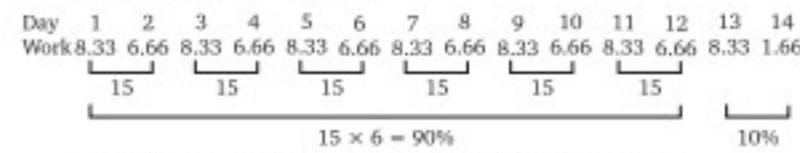
Combined efficiency = 15%

$$\text{So, the required time} = \frac{100}{15} = 6 \frac{2}{3} \text{ days.}$$

(b) In every two days A and B work 15%. So in 12 days they will complete 90% work. Now on the 13th day, A will finish 8.33% of the remaining (i.e., 10% work) and the rest 1.66% will be finished by B on 14th day by taking time $\frac{1.66}{6.66} = \frac{1}{4}$ day.

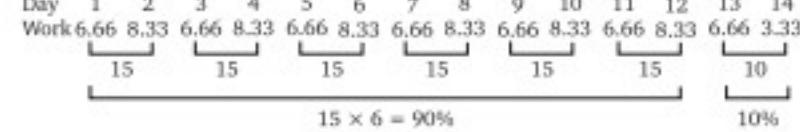
$$\text{Thus, total required time} = 12 + 1 + \frac{1}{4} = 13 \frac{1}{4} \text{ days.}$$

See the chart below :



(c) Here the difference is in the last day/days only.

See the chart below :



So, after the completion of 90% work in 12 days, on the 13th day 6.66% work will be finished by B and then 3.33% (the last part of the work) will be finished by A by taking time $\frac{3.33}{8.33} = \frac{2}{5}$ day.

$$\text{Thus, the required time} = 12 + 1 + \frac{2}{5} = 13 \frac{2}{5} \text{ days.}$$

(d) It means B worked for 2 days more than A has worked for.

Now, since B completes $2 \times 6.66 = 13.33\%$ work in two days.

So the remaining work will be done by A and B together.

Therefore the time taken by A and B , working together

$$= \frac{86.66}{15} \frac{(\text{remaining work})}{(\text{combined efficiency})} = 5 \frac{7}{9} \text{ days}$$

Thus the total required time to finish the whole work

$$= 2 + 5 \frac{7}{9} = 7 \frac{7}{9} \text{ days.}$$

(e) It means A alone worked for 2 days which is equal to

$$8.33 \times 2 = 16.66\%$$

So, the remaining (83.33%) work will be done by A and B together.

$$\therefore \text{Time taken together} = \frac{83.33}{15} = 5 \frac{5}{9} \text{ days}$$

$$\text{Thus, the total required time} = 2 + 5 \frac{5}{9} = 7 \frac{5}{9} \text{ days.}$$

(f) 'A leaves two days before the actual completion of the work' means in the last two days B has worked alone which is $6.66 \times 2 = 13.33\%$

Therefore the remaining work i.e., 86.66% work was only done by A and B together in $\frac{86.66}{15} = 5 \frac{7}{9}$ days

$$\text{Thus, the required time} = 2 + 5 \frac{7}{9} = 7 \frac{7}{9} \text{ days.}$$

NOTE This case is exactly same as part (d) of the same example. The difference is only in order of days. In part (d) B worked alone initially for 2 days and in part (f) B worked alone in the last 2 days.

(g) Applying the same concept as above we can calculate the required number of days which is same as in case (e)

Work	$A + B$	A
	$15 \times 5 \frac{2}{5}$	8.33×2
	83.33%	16.66%

(h) 'A leaves two days before the scheduled completion of the work' means A works with B only for $4 \frac{2}{3}$ days since the scheduled time is $6 \frac{2}{3}$ [see the case (a)]

Scheduled time is the time in which work could be finished by working together without any change in efficiency or work force.

Now since both A and B have worked together for $4 \frac{2}{3}$ days it

means the last 2 days work (scheduled) which is equal to 30% (since if A and B working together can finish 30% work in 2 days) will be done by B only.

\therefore required time to complete 30% work by B alone

$$= \frac{30}{6.66} = 4.5 \text{ days}$$

Thus the total required time to finish the whole work

$$= 4 \frac{2}{3} + 4 \frac{1}{2} = 9 \frac{1}{6} \text{ days.}$$

(i) Very similar to the case (h) A and B worked only for $4 \frac{2}{3}$ days (2 days less than the scheduled time $6 \frac{2}{3}$ days)

(It is obvious that in $4 \frac{2}{3}$ days A and B , working together completes 70% work, but we can directly calculate that they can complete 30% if they work together, in 2 days)

Thus 30% work is done by A alone

$$\therefore \text{time taken} = \frac{30}{8.33} = 3 \frac{3}{5} \text{ days}$$

$$\text{Thus, the total time} = 4 \frac{2}{3} + 3 \frac{3}{5} = 8 \frac{4}{15} \text{ days.}$$

$$\begin{aligned} \text{(j) Combined efficiency of } A \text{ and } B &= (8.33) + (-6.66) \\ &= 1.66\% \end{aligned}$$

\therefore Time required by A and B working together

$$= \frac{100}{1.66} = 60 \text{ days}$$

(Negative work means, B works against A)

EXAMPLE 5 *A* can complete a work in 10 days, *B* in 12 days and *C* in 15 days. All of them began the work together, but *A* had to leave the work after 2 days of the start and *B* 3 days before the completion of the work. How long did the work last?

SOLUTION See the diagram and then interpret the language of the question.

Initial 2 days	Last 3 days
$A + B + C$	$B + C$
$25 \times 2 = 50\%$	$15\% \times 2 = 30\%$

$100 - (50 + 30) = 20\%$	$6.66 \times 3 = 20\%$
--------------------------	------------------------

Since initially for 2 days all of them A , B and C work together so they complete the 50% work

and for the last 3 days only C works which is equal to 20% work.

Thus, the remaining work = 30% $[100 - (50 + 20)]$

This 30% work was done by B and C in 2 days = $\left(\frac{30}{15}\right)$.

NOTE

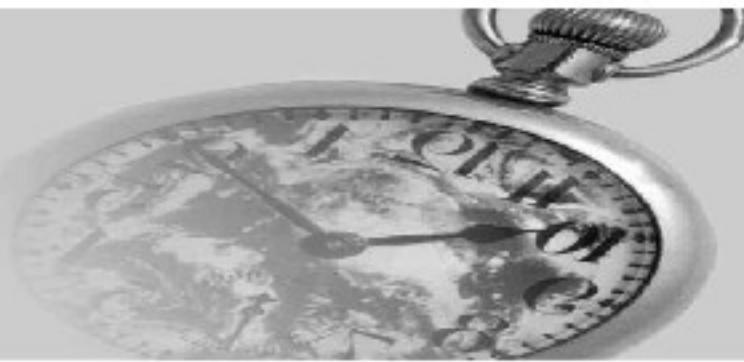
Efficiency of A = 10%

Efficiency of B = 8.33%

Efficiency of C = 6.66%

So, the total number of required days = $2 + 2 + 3 = 7$ days.

EXERCISE



LEVEL 1

19. A and B can do a piece of work in 8 days, B and C can do the same work in 12 days and A and C complete it in 8 days. In how many days A, B and C can complete the whole work, working together?
 (a) 4 (b) 6
 (c) 12 (d) 9

20. A and B can do a piece of work in 12 days, B and C in 15 days C and A in 20 days. In how many days can C alone do it?
 (a) 60 (b) 50
 (c) 25 (d) 24

21. Ganga, Jamuna and Saraswati can do a piece of work, working together, in 1 day. Ganga is thrice efficient as Jamuna and Jamuna takes the twice the number of days as Saraswati takes to do it alone. What is the difference between the number of days taken by Ganga and Saraswati?
 (a) 1 (b) 2
 (c) 3 (d) 4

22. A can finish a work in 12 days and B can do it in 15 days. After A had worked for 3 days, B also joined A to finish the remaining work. In how many days, the remaining work will be finished?
 (a) 3 (b) 4
 (c) 5 (d) 6

23. Raja can do a piece of work in 14 days, while Rani can do the same work in 21 days. They started the work together but 3 days before the completion of the work, Raja left the work. The total number of days to complete the work is :
 (a) 7 (b) 8.5
 (c) 5 (d) $10\frac{1}{5}$

24. A and B can complete a task in 30 days when working together after A and B have been working together for 11 days, B is called away and A, all by himself completes the task in the next 28 days. Had A been working alone, the number of days taken by him to complete the task would have been :
 (a) $33\frac{3}{19}$ (b) $19\frac{6}{25}$
 (c) $44\frac{4}{19}$ (d) none of these

25. Sonu can do a piece of work in 20 days. He started the work and left after some days, when 25% work was done. After it Abhijeet joined and completed it working for 10 days. In how many days Sonu and Abhijeet can do the complete work, working together?
 (a) 6 (b) 8
 (c) 10 (d) 12

26. Efficiency of Asha is 25% more than Usha and Usha takes 25 days to complete a piece of work. Asha started a work alone and then usha joined her 5 days before actual completion of the work. For how many days Asha worked alone?
 (a) 9 (b) 11
 (c) 10 (d) 15

27. Krishna can do a work in 10 days while Mohan can do the same work in 20 days. They started work together. After 3 days Krishna left the work and Mohan completed it. For how many days Mohan worked alone more than the number of days required when both worked together?
 (a) $4\frac{1}{3}$ (b) $3\frac{1}{4}$
 (c) $2\frac{3}{5}$ (d) $3\frac{2}{3}$

28. Kareena can do a piece of work in 9 days and Karishma can do the same work in 18 days. They started the work. After 3 days Shahid joined them, who can complete alone the same whole work in 3 days. What is the total number of days in which they had completed the work?
 (a) 12 (b) 8
 (c) 4 (d) 6

29. Kavita, Babita and Samita started a work. 5 days later Samita left the work and Babita left the work after working 8 days. In how many more days Kavita would have completed the rest of work if they take 20, 60 and 30 days individually to finish a work?
 (a) 4 (b) 5
 (c) 6 (d) 8

30. The ratio of efficiency of A is to C is 5 : 3. The ratio of number of days taken by B is to C is 2 : 3. A takes 6 days less than C, when A and C completes the work individually. B and C started the work and left after 2 days. The number of days taken by A to finish the remaining work is :
 (a) 4.5 (b) 5
 (c) 6 (d) $9\frac{1}{3}$

31. Anand can do a piece of work in 45 days, but Bahuguna can do the same work in 5 days less, than Anand, when working alone. Anand and Bahuguna both started the work together but Bahuguna left after some days and Anand finished the remaining work in 56 days with half of his efficiency but he did the work with Bahuguna with his complete efficiency. For how many days they had worked together?
 (a) 6 (b) 8
 (c) 9 (d) 12

32. Chandni and Divakar can do a piece of work in 9 days and 12 days respectively. If they work for a day alternatively, Chandni beginning, in how many days, the work will be completed?
 (a) $10\frac{1}{4}$ (b) $9\frac{1}{5}$
 (c) 11.11 (d) 10

33. Fatima and Zahira can do a piece of work in 12 days and 15 days respectively. If they work for alternate day and Fatima starts the work first, then in how many days the work will be completed?
 (a) $12\frac{1}{5}$ (b) $13\frac{1}{4}$
 (c) $13\frac{1}{5}$ (d) 15

34. In the previous question (number 33) if Zahira starts first, then in how many days, the work will be completed?
 (a) $14\frac{1}{5}$ (b) 14
 (c) $13\frac{1}{5}$ (d) $13\frac{2}{5}$

35. The number of days required by A, B and C to work individually is 6, 12 and 8 respectively. They started a work doing it alternatively. If A has started then followed by B and so on, how many days are needed to complete the whole work?
 (a) 8 (b) 7.5
 (c) 8.5 (d) $9\frac{1}{2}$

75. C is twice efficient as A. B takes thrice as many days as C. A takes 12 days to finish the work alone. If they work in pairs (i.e., AB, BC, CA) starting with AB on the first day then BC on the second day and AC on the third day and so on, then how many days are required to finish the work?
- (a) $6\frac{1}{5}$ days (b) 4.5 days
 (c) $5\frac{1}{9}$ days (d) 8 days
76. Ahluwalia and Bimal together take 6 days to finish the work. Bimal and Jalan together take 10 days to finish the work. What is the difference between number of days taken by Ahluwalia and Jalan when they worked alone to complete the whole work?
- (a) 12 days (b) 16 days
 (c) 15 days (d) can't be determined
77. B is twice efficient as A and A can do a piece of work in 15 days. A started the work and after a few days B joined him. They completed the work in 11 days, from the starting. For how many days they worked together?
- (a) 1 day (b) 2 days
 (c) 6 days (d) 5 days
78. A, B and C can complete a piece of work in 15, 30 and 40 days respectively. They started the work together and A left 2 days before the completion of the work and B left 4 days before the completion of the work. In how many days was the work completed?
- (a) $7\frac{3}{10}$ (b) $10\frac{2}{15}$
 (c) $10\frac{7}{30}$ (d) none of these
79. There was a leakage in the container of the refined oil. If 11 kg oil is leaked out per day then it would have lasted for 50 days, if the leakage was 15 kg per day, then it would have lasted for only 45 days. For how many days would the oil have lasted, if there was no leakage and it was completely used for eating purpose?
- (a) 80 days (b) 72 days
 (c) 100 days (d) 120 days
80. A contractor undertook to complete the work in 40 days and he deployed 20 men for his work. 8 days before the scheduled time he realised that $\frac{1}{3}$ rd of the work was still to be done. How many more men were required to complete the work in stipulated time?
- (a) 16 (b) 15
 (c) 20 (d) 25
81. 7 Indian and 4 Chinese finish a job in 5 days. 7 Japanese and 3 Chinese finish the same job in 7 days. Given that the efficiency of each person of a particular nationality is same but different from others. One Indian, one Chinese and one Japanese will complete the work in :
- (a) $18\frac{3}{13}$ days (b) $20\frac{5}{12}$ days
 (c) $21\frac{6}{14}$ days (d) $20\frac{7}{12}$ days
82. A, B and C are three book binders. A takes 8 minutes, B takes 12 minutes and C takes 16 minutes to bind a book. If they work each day for 12 hours, then on an average, how many books each one bind per day?
- (a) 65 (b) 52
 (c) 48 (d) 70
83. A piece of work can be completed by 10 men and 6 women in 18 days. Men works 9 hours per day while women works 7.5 hours per day. Per hour efficiency of a woman is $\frac{2}{3}$ rd of a man's efficiency. In how many days 10 men and 9 women complete the work?
- (a) 16 days (b) 20 days
 (c) 30 days (d) 25 days
84. B and C are equally efficient, but the efficiency of A is half of each B and C. A and B started a work and 3 days later C joined them. If A alone can do the work in 14 days, then in how many more days the work will be completed?
- (a) 1 (b) 2
 (c) 3 (d) 4.5
85. A can do a piece of work in 10 days, B in 15 days. They work together for 5 days, the rest of the work is finished by C in two more days. If they get Rs. 3000 as wages for the whole work, what are the daily wages of A, B and C respectively (in Rs.) :
- (a) 200, 250, 300 (b) 300, 200, 250
 (c) 200, 300, 400 (d) none of these
86. A can do a piece of work in 2 hours, B can do thrice the work in 8 hours and 'C' can do the same work as A in 8 hours. If all of them work together, how long it would take them to complete the work :
- (a) 1 hour (b) 2 hours
 (c) 3 hours (d) 4 hours
87. A is twice efficient as B and together they do the same work in as much time as C and D together. If C and D can complete the work in 20 and 30 days respectively, working alone, then in how many days A can complete the work individually :
- (a) 12 days (b) 18 days
 (c) 24 days (d) 30 days
88. 4 men and 2 boys can finish a piece of work in 5 days. 3 women and 4 boys can finish the same work in 5 days. Also 2 men and 3 women can finish the same work in 5 days. In how many days 1 man, 1 woman and one boy can finish the work, at their double efficiency?
- (a) $4\frac{8}{13}$ (b) $4\frac{7}{13}$
 (c) $3\frac{7}{13}$ (d) none of these
89. If m men can do a work in r days, then the number of days taken by $(m+n)$ men to do it is :
- (a) $\frac{m+n}{mn}$ (b) $\frac{m+n}{mr}$
 (c) $\frac{mr}{(m+n)}$ (d) $\frac{(m+n)r}{mn}$
90. Pipe A can fill a tank in 36 minutes and pipe B can fill it in 45 minutes. If both the pipes are opened to fill an empty tank, in how many minutes will it be full?

LEVEL (2)

- (a) 26th day (b) 27th day
(c) 28th day (d) 30th day
5. In the previous question what per cent of the time of the morning shift was utilised?
(a) 33.33% (b) 60%
(c) 100% (d) none of these
6. Working together *B* and *C* take 50% more number of days than *A*, *B* and *C* together take and *A* and *B* working together, take $\frac{8}{3}$ more number of days than *A*, *B* and *C* take together. If *A*, *B* and *C* all have worked together till the completion of the work and *B* has received Rs. 120 out of the total earning of Rs. 450, then in how many days did *A*, *B* and *C* together complete the whole work?
(a) 10 (b) 6
(c) 4 (d) 2
7. At Technosys Pvt Ltd. there are some engineering students employed as trainee engineers, belong to two eminent institutions of India. One group belong to MIT and another to NIT. Each student of MIT works for 10 hours a day till 60 days and each student of NIT works for 8 hours till 80 days on the two same projects. The ratio of number of students of MIT and that of NIT is 4 : 5 respectively. Students of which institution is slower in work and by how much?
(a) Each student of MIT is 20% less efficient than that of NIT
(b) Each student of NIT is 33.33% less efficient than that of MIT
(c) Each student of NIT is 25% less efficient than that of MIT
(d) Each student of MIT is 33.33% less efficient than that of NIT.

Directions for questions 8, 9 and 10 : At Arihant Prakashan every book goes through 3 phases (or stages) typing, composing and binding. There are 16 typists, 10 composers and 15 binders. A typist can type 8 books in each hour, a composer can compose 12 books in each hour and a binder can bind 12 books in each hour. All of the people at Arihant Prakashan works for 10 hours a day and each person is trained to do only the job of 1 category.

8. How many books can be prepared in each day?
(a) 1500 (b) 1200
(c) 1440 (d) 1380
9. If company has hired 12 more people, who can do any of the three jobs, then maximum how many books can be prepared in each day?
(a) 1500
(b) 1680
(c) 1800
(d) more than 2000
10. If company wanted to reduce the number of employees by 3, then from which category it reduces the number of employees without reducing the amount of production of books?
(a) It should reduce two binders and 1 typist
(b) It should reduce three binders only
(c) It should reduce 1 typist, 1 composer and 1 binder
(d) both (a) and (b) are possible

11. Bunty and Babli working together completed a job in 8 days. If Bunty worked twice efficiently as he actually did and Babli worked $\frac{1}{3}$ as efficiently as she actually did, the work would have been completed in 6 days. Find the time taken by Bunty to complete the job alone :
(a) 8 days (b) $\frac{38}{35}$ days
(c) $\frac{15}{2}$ days (d) $13\frac{1}{3}$ days
12. A single reservoir supplies the petrol to the whole city, while the reservoir is fed by a single pipeline filling the reservoir with the stream of uniform volume. When the reservoir is full and if 40,000 litres of petrol is used daily, the supply fails in 90 days. If 32,000 litres of petrol is used daily, it fails in 60 days. How much petrol can be used daily without the supply ever failing?
(a) 64000 litres (b) 56000 litres
(c) 78000 litres (d) 60000 litres
13. Railneer is packaged in a water bottling plant, with the help of two machines M_1 and M_2 . M_1 and M_2 produces 400 and 600 bottles per minute. One day's production can be processed by M_1 operating alone for 9 hours, by M_2 operating alone for 6 hours or by both M_1 and M_2 operating simultaneously for 3 hours and 36 minutes. If one day's production is processed by M_1 operating alone for $\frac{1}{3}$ of the time and M_1 and M_2 simultaneously operating for $\frac{2}{3}$ of the time, then in how many hours total production of one day will be completed?
(a) 2 (b) 3
(c) 4.5 (d) 4.8
- Directions for questions 14 and 15 :** A contractor employed a certain number of workers to finish constructing a road in a certain scheduled time. Sometime later, when a part of work had been completed, he realised that the work would get delayed by three-fourth of the scheduled time, so he at once doubled the number of workers and thus he managed to finish the road on the scheduled time.
14. How much work he had been completed, before increasing the number of workers?
(a) 10%
(b) $14\frac{2}{7}\%$
(c) 20%
(d) can't be determined
15. Some-time after the new workers were introduced, all of the newly introduced workers left the work due to heavy rain and the efficiency of the remaining workers reduced by 20% due to which the work finally got completed by delay of 60% of the scheduled time then how much work still remained incomplete by the end of the scheduled time?
(a) $17\frac{3}{5}\%$ (b) 21%
(c) $27\frac{5}{7}\%$ (d) 28%

Directions for questions 16 to 20 : Mr. Stenley employed a certain number of typists for his project. 8 days later 20% of the typist left the job and it was found that it took as much time to complete the rest work from then as the entire work needed with all the employed typists. The average speed of a typist is 20 pages/hour.

16. How many typists left the work?
 - (a) 10
 - (b) 5
 - (c) 16
 - (d) can't be determined
 17. Minimum how many typist could be employed?
 - (a) 10
 - (b) 5
 - (c) 15
 - (d) 4
 18. What could be the number of typists remained at work when 20% of the employed typists left the job?
 - (a) 15
 - (b) 18
 - (c) 68
 - (d) 78
 19. What is the actual number of days required, when it is done with actual work force, through out the completion :
 - (a) 32 days
 - (b) 48 days
 - (c) 40 days
 - (d) can't be determined
 20. 16 days after the 20% typist left the job it was decided to complete the work on time by increasing the work-force again. By how much percentage increase in work-force is required?
 - (a) 100%
 - (b) 50%
 - (c) 200%
 - (d) none of these
 21. Five tailors A, B, C, D and E stich 1800 shirts in 90 days working alternatively. Find the minimum possible number of shirts that can be stiched in a single day by working together :
 - (a) 100
 - (b) 20
 - (c) 50
 - (d) 4
- Directions for question number 22, 23 :** 8 men and 5 women working 6 hours a day can complete a work in 4 days. Also 4 men and 5 women working for 8 hours a day can complete the same job in 5 days. Similarly 5 boys working 8 hours a day can complete the same job in 30 days.
22. If 4 men, 3 women and 4 boys worked together everyday for 5 hours, then in how many days they have completed the work?
 - (a) 3
 - (b) 4
 - (c) 8
 - (d) 6
 23. If women and children (boys) can't be employed, then minimum how many men are required to complete the job in 6 days if the working hours per day cannot exceed 9?
 - (a) 4
 - (b) 5
 - (c) 6
 - (d) 7
 24. Eklavya can do the 6 times the actual work in 36 days while Faizal can do the one-fourth of the original work in 3 days. In how many days will both working together complete the 3 times of the original work?
 - (a) 6
 - (b) 10
 - (c) 12
 - (d) 15
 25. Progressive Company Pvt. Ltd. hired some employees in a fix pattern. On the first day it hired one person, on the second day one more joined him. On the third, fourth etc (i.e., every

next day) one more person increased in this group. The capacity of each person was same. The whole work was completed on the 24th day then out of total Rs. 5000, maximum how much a person had earned?

- (a) Rs. 500
 - (b) Rs. 400
 - (c) Rs. 200
 - (d) Rs. 250
26. Two persons having different productivity of labour, working together can reap a field in 2 days. If one-third of the field was reaped by the first man and rest by the other one working alternatively took 4 days. How long did it take for the faster person to reap the whole field working alone?
 - (a) 12
 - (b) 8
 - (c) 6
 - (d) 3
 27. The total number of men, women and children working in a factory is 18. They earn Rs. 4000 in a day. If the sum of the wages of all men, all women and all children is in the ratio of 18 : 10 : 12 and if the wages of an individual man, woman and child is in the ratio 6 : 5 : 3, then how much a woman earn in a day?
 - (a) Rs. 400
 - (b) Rs. 250
 - (c) Rs. 150
 - (d) Rs. 120
 28. A group of workers was put on a job. From the second day onwards, one worker was withdrawn each day. The job was finished when the last worker was withdrawn. Had no worker been withdrawn at any stage, the group would have finished the job in 55% of the time. How many workers were there in the group?
 - (a) 50
 - (b) 40
 - (c) 45
 - (d) 10
 29. Two workers undertake to do a job. The second worker started working 2 hours after the first. Five hours after the second worker has begun working there is still $\frac{9}{20}$ of the work to be done. When the assignment is completed, it turns out that first worker has done 60% of the work, while second worker has done rest of the work. How many hours would it take each one to do the whole job individually?
 - (a) 10 hours and 12 hours
 - (b) 15 hours and 10 hours
 - (c) 20 hours and 25 hours
 - (d) 18 hours and 20 hours
 30. A group of men decided to do a job in 4 days. But since 20 men dropped out every day, the job completed at the end of the 7th day. How many men were there at the beginning?
 - (a) 240
 - (b) 140
 - (c) 280
 - (d) 150
 31. Brahma, Vishnu and Mahesh are three friends with different productivity. Brahma working alone needs as much time as Vishnu and Mahesh working together, while Vishnu himself needs 8 hours more working alone than when he works with Mahesh. Brahma working alone needs 8 hours less than Vishnu needs working alone. In how much time Brahma, Vishnu and Mahesh working together can complete the job?
 - (a) 4 hours
 - (b) 5 hours
 - (c) 6 hours
 - (d) 8 hours

32. Milinda takes $8\frac{1}{3}$ hours more when she works alone in comparison of when she works with Bill. While Bill takes $5\frac{1}{3}$ hours more when he work alone in comparison to the time, when he works with Milinda. How long it will take Bill to complete the work alone?
 (a) 10 hours (b) 15 hours
 (c) 18 hours (d) 12 hours
33. Pascal and Rascal are two workers. Working together they can complete the whole work in 10 hours. If the Pascal worked for 2.5 hours and Rascal worked for 8.5 hours, still there was half of the work to be done. In how many hours Pascal working alone, can complete the whole work?
 (a) 24 hours (b) $17\frac{1}{7}$ hours
 (c) 40 hours (d) can't be determined
34. Boston, Churchill and David are three workers, employed by a contractor. They completed the whole work in 10 days. Initially all of them worked together, but the last 60% of the work was completed by only Churchill and David together. Boston worked with Churchill and David only for initial two days then he left the work due to his poor health. Also Churchill takes 20% less time to finish the work alone than that of David working alone. If they were paid Rs. 3000 for the entire work, then what is the share of least efficient person?
 (a) Rs. 900 (b) Rs. 1200
 (c) Rs. 1000 (d) none of these
35. There are three boats B_1 , B_2 and B_3 working together they carry 60 people in each trip. One day an early morning B_1 carried 50 people in few trips alone. When it stopped carrying the passengers B_2 and B_3 started carrying the people together. It took a total of 10 trips to carry 300 people by B_1 , B_2 and B_3 . It is known that each day on an average 300 people cross the river using only one of the 3 boats B_1 , B_2 and B_3 . How many trips it would take to B_1 to carry 150 passengers alone?
 (a) 15 (b) 30
 (c) 25 (d) 10
36. Three men and 5 women together can finish a job in 3 days. Working on the same job 3 women take 5 days more than the time required by 2 men. What is the ratio of efficiency of a man to a woman?
 (a) 2 : 1 (b) 3 : 2
 (c) 5 : 2 (d) 4 : 1
37. Henry and Ford are two different persons, but when they worked together, they complete it in 10 days. Had Henry worked at half of his efficiency and Ford at five times of his efficiency it would have taken them to finish the job in 50% of the scheduled time. In how many days Ford can complete the job working alone?
 (a) 12 (b) 24
 (c) 15 (d) 30
38. Anne, Benne and Cenne are three friends. Anne and Benne are twins. Benne takes 2 days more than Cenne to complete the work. If Anne started a work and 3 days later Benne joins

him, then the work gets completed in 3 more days. Working together Anne, Benne and Cenne can complete thrice the original work in 6 days. In how many days Benne can complete twice the original work with double the efficiency working alone?

- (a) 2 (b) 3
 (c) 4 (d) 6

39. Three typists A , B and C working together 8 hours per day can type 900 pages in 20 days. In a day B types as many pages more than A as C types as many pages more than B . The number of pages typed by A in 4 hours equal to the number of pages typed by C in 1 hour. How many pages C types in each hour?

- (a) 1 (b) 2
 (c) 3 (d) 4

40. *Directions for question number 40 and 41: Four pipes A , B , C and D can fill a cistern in 20, 25, 40 and 50 hours respectively.*

40. The first pipe A was opened at 6:00 am, B at 8:00 am, C at 9:00 am and D at 10:00 am. When will the cistern be full?

- (a) 4:18 pm (b) 3:09 pm
 (c) 12:15 pm (d) 11:09 am

41. If A and B are opened as inlet pipe into the cistern and C and D are opened as outlet pipes from the cistern and all the four pipes are opened simultaneously, how many hours will it take to fill the cistern completely?

- (a) 20 hours (b) $11\frac{1}{9}$ hours
 (c) $22\frac{2}{9}$ hours (d) 45 hours

42. A tank is connected with four pipes A , B , C and D of which two are filling the tank and other two are emptying it. The time taken by A , B , C and D to finish their jobs are 10 hours, 15 hours, 20 hours and 30 hours respectively. All four pipes are opened. When the tank was empty, it took 12 hours to fill it completely. Which two are the outlet pipes?

- (a) A and B (b) C and D
 (c) A and C (d) B and D

43. Two pipes A and B can fill a tank in 24 hours and $\frac{120}{7}$ hours respectively. Harihar opened the pipes A and B to fill an empty tank and some times later he closed the taps A and B , when the tank was supposed to be full. After that it was found that the tank was emptied in 2.5 hours because an outlet pipe C connected to the tank was open from the beginning. If Harihar closed the pipe C instead of closing pipes A and B the remaining tank would have been filled in :

- (a) 2 hours (b) 8 hours
 (c) 6 hours (d) 4 hours

44. Pipe A can fill a tank in 12 hours and pipe B can fill it in 15 hours, separately. A third pipe C can empty it in 20 hours. Initially pipe A was opened, after one hour pipe B was opened and then after 1 hour when pipe B was opened pipe C was also opened. In how many hours the tank will be full?

- (a) $9\frac{2}{3}$ hours (b) $6\frac{2}{3}$ hours
 (c) 10 hours (d) none of these

Directions for question number 45 and 46: A tank has an inlet and outlet pipe. The inlet pipe fills the tank completely in 2 hours when the outlet pipe is plugged. The outlet pipe empties the tank completely in 6 hours when the inlet pipe is plugged.

45. If both pipes are opened simultaneously at a time when the tank was one-third filled, when will the tank fill thereafter?
 (a) $\frac{3}{2}$ hours (b) $\frac{2}{3}$ hour
 (c) 2 hours (d) $1\frac{2}{3}$ hours
46. If there is a leakage also which is capable of draining out the liquid from the tank at half of the rate of outlet pipe, then what is the time taken to fill the empty tank when both the pipes are opened?
 (a) 3 hours (b) $3\frac{2}{3}$ hours
 (c) 4 hours (d) none of these
47. An inlet pipe can fill a tank in 5 hours and an outlet pipe can empty the same tank in 36 hours, working individually. How many additional number of outlet pipes of the same capacity are required to be opened, so that the tank never overflows?
 (a) 3 (b) 6
 (c) 8 (d) 7

Directions for question number 48 and 49: In a public bathroom there are n taps 1, 2, 3... n . Tap 1 and tap 2 take equal time to fill the tank while tap 3 takes half the time taken by tap 2 and tap 4 takes half the time taken by tap 3. Similarly each next number of tap takes half the time taken by previous number of tap i.e., K^{th} tap takes half the time taken by $(K-1)^{\text{th}}$ tap.

48. If the 10th tap takes 2 hours to fill the tank alone then what is the ratio of efficiency of 8th tap and 12th tap, respectively?
 (a) 4 : 1 (b) 5 : 3
 (c) 16 : 1 (d) 1 : 16
49. If the 8th tap takes 80 hours to fill the tank then the 10th and 12th taps working together take how many hours to fill the tank?
 (a) 2 hours (b) 4 hours
 (c) 6 hours (d) none of these
50. Pipe A takes $3/4$ of the times required by pipe B to fill the empty tank individually. When an outlet pipe C is also opened simultaneously with pipe A and pipe B, it takes $3/4$ more time

to fill the empty tank than it takes, when only pipe A and pipe B are opened together. If it takes to fill 33 hours when all the three pipes are opened simultaneously, then in what time pipe C can empty the full tank operating alone?

- (a) 66 hours (b) 50 hours
 (c) 44 hours (d) can't be determined

Directions for question number 51, 52 and 53: A contractor undertook a project to complete it, in 20 days which needed 5 workers to work continuously for all the days estimated. But before the start of the work the client wanted to complete it earlier than the scheduled time, so the contractor calculated that he needed to increase 5 additional men every 2 days to complete the work in the time the client wanted it :

51. How many men were working on the day the project was completed as per the date of client wanted to complete it?
 (a) 5 (b) 10
 (c) 20 (d) none of these
52. Find the number of days in which client wanted to complete his work.
 (a) 15 (b) 10
 (c) 8 (d) can't be determined
53. If the work was further increased by 50% but the contractor continues to increase the 5 workers on every 2 days then how many more days are required over the initial time specified by the client?
 (a) 1 day (b) 2 days
 (c) 5 days (d) none of these
54. A tank is connected with 8 pipes. Some of them are inlet pipes and rest work as outlet pipes. Each of the inlet pipe can fill the tank in 8 hours, individually, while each of those that empty the tank i.e., outlet pipe, can empty it in 6 hours individually. If all the pipes are kept open when the tank is full, it will take exactly 6 hours for the tank to empty. How many of these are inlet pipes?
 (a) 2 (b) 4
 (c) 5 (d) 6
55. A tank has two inlet pipes which can fill the empty tank in 12 hours and 15 hours working alone and one outlet pipe which can empty the full tank in 8 hours working alone. The inlet pipes are kept open for all the time but the outlet pipe was opened after 2 hours for one hour and then again closed for 2 hours then once again opened for one hour. This pattern of outlet pipe continued till the tank got completely filled. In how many hours the tank has been filled, working on the given pattern?
 (a) 8 hours 24 minutes (b) 10 hours 15 minutes
 (c) 9 hours 10 minutes (d) 9 hours 6 minutes



Final Round

Directions for question number 1 to 5: In a nut-bolt factory 180 workers are working for 6 hours a day. Out of 180 workers there are some men, some women and rest are boys. All the workers can produce either nut or bolt or both of them. A man can produce 60 nuts and 80 bolts in each hour and a woman

can produce 30 nuts and 60 bolts per hour. A man is thrice as efficient as a boy and 3/2 times as efficient as a woman. Given that all men, all women and all boys produce equal number of articles of one kind (i.e., either nut or bolt) per hour.

Directions for question number 7 to 11 : A company produces three products. The products are processed on 3 different machines. The time required to manufacture one unit of each the three products and the daily capacity of three machines are given in the table below :

Machine	Time per unit (in min.)			Machine capacity (min./day)
	Product 1	Product 2	Product 3	
M_1	2	2	3	450
M_2	2	5	—	410
M_3	3	—	4	480

Q. Directions for questions 9, 10 and 11 : Read the following additional data for question number 9, 10 and 11. The profit per unit for product 1, 2 and 3 is Rs. 3, Rs. 4 and Rs. 5.

9. What combination of P_1 , P_2 and P_3 will yield maximum profit under the manufacturing constraints?

 1. $P_1 = 25$, $P_2 = 50$, $P_3 = 100$
 2. $P_1 = 20$, $P_2 = 60$, $P_3 = 80$
 3. $P_1 = 100$, $P_2 = 0$, $P_3 = 50$
 4. $P_1 = 0$, $P_2 = 80$, $P_3 = 100$

(a) 4 (c) 3	(b) 2 (d) 1
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10. Which of the machine if it breaks down will affect profitability the least?

(a) Machine 1 (c) Machine 3	(b) Machine 2 (d) Machine 1 or 3
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11. If no production of product 2 is scheduled today and it is decided to only produce one type of product today, then what is the maximum profits that can be had today?

(a) Rs. 480 (c) Rs. 600	(b) Rs. 750 (d) none of these
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Directions for question number 12-15 : Ready Tailoring Services is very well known in its quality and time bound services. The company (Ready Tailoring Services) received a large order for stitching military uniforms. It has two different orders to prepare the shirts one for Officers and second for Jawans (non-officers). It has three cutters who will cut the fabric. Six tailors who will do the stitching and 3 assistant to stitch the buttons and iron the shirts. Each of these 12 persons will work for exactly 8 hours a day. Each of the Officers uniform requires 20 minutes for cutting the fabric, 1 hour for stitching and 20 minutes for stitching buttons and ironing the shirts. Whereas the Jawan's uniform requires 15 minutes for cutting the fabric and 60 minutes for stitching and 10 minutes for buttons and ironing.

12. If the company has to supply 40 officers uniforms only and no other on a particular day, how many man-hours are utilised on that day?

(a) $33\frac{1}{3}$ hours (b) $66\frac{2}{3}$ hours
 (c) 40 hours (d) 60 hours

13. If the number of tailors will be increased by 50% then maximum how many uniforms for officers can be completed in one day?

(a) 48 (b) 50
 (c) 60 (d) 72

14. If the company can increase maximum 3 employees of any category then for which category should it hire to get maximum increase in production capacity, assuming that it needs to stitch only officer's uniform :

(a) cutter (b) tailor
 (c) assistant (d) can't be determined

15. If the company has to produce the shirts for only one category then of which category it can produce maximum number of uniforms?

(a) Officers (b) Jawans
 (c) either (a) or (b) (d) none of these



Answers

LEVEL-1

1. (c)	2. (b)	3. (c)	4. (a)	5. (d)	6. (b)	7. (b)	8. (c)	9. (b)	10. (c)
11. (b)	12. (c)	13. (a)	14. (a)	15. (b)	16. (b)	17. (a)	18. (a)	19. (b)	20. (a)
21. (a)	22. (c)	23. (d)	24. (c)	25. (b)	26. (b)	27. (a)	28. (c)	29. (c)	30. (c)
31. (b)	32. (a)	33. (b)	34. (d)	35. (a)	36. (c)	37. (c)	38. (b)	39. (b)	40. (d)
41. (a)	42. (b)	43. (b)	44. (c)	45. (b)	46. (a)	47. (a)	48. (c)	49. (a)	50. (a)
51. (c)	52. (a)	53. (d)	54. (b)	55. (a)	56. (c)	57. (b)	58. (a)	59. (d)	60. (a)
61. (a)	62. (c)	63. (b)	64. (d)	65. (c)	66. (b)	67. (b)	68. (a)	69. (b)	70. (b)
71. (b)	72. (c)	73. (d)	74. (a)	75. (c)	76. (d)	77. (b)	78. (b)	79. (b)	80. (c)
81. (b)	82. (a)	83. (a)	84. (a)	85. (b)	86. (a)	87. (b)	88. (d)	89. (c)	90. (c)
91. (d)	92. (c)	93. (a)	94. (b)	95. (a)	96. (c)	97. (a)	98. (b)	99. (c)	100. (a)

LEVEL-2

1. (a)	2. (c)	3. (c)	4. (b)	5. (c)	6. (c)	7. (c)	8. (b)	9. (c)	10. (d)
11. (d)	12. (b)	13. (c)	14. (b)	15. (c)	16. (d)	17. (b)	18. (c)	19. (c)	20. (d)
21. (a)	22. (c)	23. (b)	24. (c)	25. (b)	26. (d)	27. (b)	28. (d)	29. (c)	30. (b)
31. (c)	32. (d)	33. (b)	34. (c)	35. (a)	36. (c)	37. (d)	38. (d)	39. (c)	40. (b)
41. (c)	42. (b)	43. (b)	44. (a)	45. (c)	46. (c)	47. (d)	48. (d)	49. (b)	50. (c)
51. (c)	52. (c)	53. (b)	54. (b)	55. (c)					

FINAL ROUND

1. (c)	2. (b)	3. (a)	4. (c)	5. (c)	6. (c)	7. (a)	8. (b)	9. (d)	10. (b)
11. (c)	12. (b)	13. (d)	14. (b)	15. (c)					



Hints & Solutions

LEVEL (1)

1. Efficiency of $A = \frac{100}{12} = 8.33\%$

Efficiency of $B = \frac{100}{15} = 6.66\%$

Combined efficiency of A and $B = 8.33 + 6.66 = 15\%$

Number of days taken by A and B , when worked together

$$= \frac{100}{15} = 6 \frac{10}{15} = 6 \frac{2}{3} \text{ days}$$

NOTE Efficiency \times Time period = Fixed amount of work

Also, in terms of percentage total work to be done is considered as 100% (in fraction it is 1), unless otherwise stated.

Alternatively : It can be done through unitary method, also.

2. Efficiency of $A = \frac{100}{10} = 10\%$

Efficiency of $B = \frac{100}{12} = 8.33\%$

Efficiency of $C = \frac{100}{15} = 6.66\%$

Combined efficiency of A , B and $C = 10 + 8.33 + 6.66 = 25\%$
 \therefore Required number of days, when A , B and C worked together

$$= \frac{100}{25} = 4 \text{ days}$$

3. Efficiency of $A = 20\% \left(= \frac{100}{5}\right)$

Efficiency of $B = 10\% \left(= \frac{100}{10}\right)$

Efficiency of A , B and $C = 50\% \left(= \frac{100}{2}\right)$

\therefore Efficiency of $C = (\text{Efficiency of } A, B \text{ and } C) - (\text{Efficiency of } A \text{ and } B)$
 $= (50) - (20 + 10) = 20\%$

\therefore Number of days required by C to work alone $= \frac{100}{20} = 5 \text{ days}$

Alternatively : Go through options and satisfy the values.

	A	B	C	$(A + B + C)$
Days	5	10	5	2
Efficiency	20%	10%	20%	50%

Consider option (c)

4. Efficiency of $A = 12.5\%$

Efficiency of $B = 6.25\%$

Efficiency of $C = 1.25\%$

Efficiency of $(A + B + C) = 20\% (= 12.5 + 6.25 + 1.25)$

Required number of days $= \frac{100}{20} = 5 \text{ days}$

5. Efficiency of $A = 10\%$

Efficiency of $B = 6.66\%$

\therefore Required number of days $= \frac{100}{16.66} = 6 \text{ days}$

6. Efficiency of $A = \frac{100}{24} = 4.16\%$

Efficiency of $B = \frac{100}{30} = 3.33\%$

Efficiency of $(A + B + C) = \frac{100}{12} = 8.33\%$

\therefore Efficiency of $C = (8.33) - (4.16 + 3.33) = 0.83\%$

\therefore Number of days required by C to complete the work alone

$$= \frac{100}{0.83} = \frac{100}{5/6} = 120 \text{ days}$$

NOTE $\frac{5}{6} = 0.833$

7. Efficiency of $A = 10\%$

Efficiency of $B = 4.16\%$

Efficiency of $(A + B + C) = 16.66\%$

$$\left. \begin{array}{l} \frac{100}{10} = 10 \\ \frac{100}{24} = 4.16 \\ \frac{100}{6} = 16.66 \end{array} \right\}$$

Efficiency of $C = (16.66) - (10 + 4.16) = 2.5\%$

Number of days required by C alone to finish the work

$$= \frac{100}{2.5} = 40 \text{ days}$$

8. Efficiency of $A = 7.14\%$

Efficiency of $B = 4.76\%$

Efficiency of $A + B = 11.9\%$

\therefore Number of days required by A and B , working together

$$= \frac{100}{11.9} = 8.4 \text{ days}$$

HINT You can see that there is only one option between 8 and 9 which is 8.4 hence (c) is the correct choice.

Explanation : For 8 days denominator should be 12.5 and for 9 days denominator should be almost 11.

Alternatively : One day's work of A and B

$$= \frac{1}{14} + \frac{1}{21} = \frac{5}{42}$$

\therefore Required number of days $= \frac{42}{5} = 8.4 \text{ days}$

9. Efficiency of $A = 4.16\%$

Efficiency of $B = 1.6 \times 4.16 = 6.66\%$

$$\therefore \text{Number of days required by } B = \frac{100}{6.66} = 15 \text{ days}$$

Alternatively :

	A	B
Efficiency	\rightarrow	x
Days	\rightarrow	$1.6k$

(Since number of days are inversely proportional to efficiency)

$$\text{Now } 1.6k = 24 \Rightarrow k = 15 \text{ day}$$

Alternatively : A 's one day's work = $\frac{1}{24}$

$$\therefore B$$
's one day's work = $160\% \text{ of } \frac{1}{24} = \frac{1}{15}$

$$\therefore \text{Required number of days} = 15$$

10. Efficiency of $A + B = \frac{100}{14} = 7.14\%$

Again the ratio of efficiency of A and $B = 2:1$

$$\therefore \text{Efficiency of } A = \frac{2}{3} \times 7.14 = 4.76\%$$

$$\therefore \text{Required number of days by } A = \frac{100}{4.76} = 21 \text{ days}$$

NOTE Only choice (c) lies between 20 and 24.

Explanation : For 20 days denominator should be 5 and for 24 days, denominator should be 4.16 also the only choice (c) gives a value which is multiple of 7 and very close to the answer (as appears).

Alternatively : One day's work of

$$A \text{ and } B = \frac{1}{x} + \frac{1}{2x} = \frac{1}{14}$$

$$\Rightarrow x = 21$$

Since A is twice efficient as B so A will take half of the days taken by B .

11. Efficiency of $A + B = 14.28\% \left(= \frac{100}{7} \right)$

Now, since the ratio of efficiency of A and B is $2:1$

$$\text{So, the efficiency of } A = \frac{2}{3} \times 14.28 = 9.52\%$$

$$\therefore \text{Number of days required by } A = 10.5 \text{ days}$$

HINT Only choice (b) is correct since there is no other value (in option) lies between 10 and 11.

Explanation : For 10 days, denominator should be 10 and for 11 days, denominator should be 9.09.

Alternatively : Let A takes x days and then B takes $2x$ days

$$\text{then } 1 \text{ day's work of } A \text{ and } B = \frac{1}{x} + \frac{1}{2x} = \frac{1}{7}$$

$$\Rightarrow x = 10.5$$

Thus A takes 10.5 days.

12.

Efficiency	\rightarrow	A	B
Days	\rightarrow	3	1
	:	:	3

(Since number of days are inversely proportional to the efficiency)

Now if A requires x days, so B requires $3x$ days

$$\therefore \text{Difference of required days} (= 3x - x) = 2x = 10$$

$$\Rightarrow x = 5$$

Hence the number of days required by $B = 3x = 3 \times 5 = 15$ days

13.

Efficiency	\rightarrow	A	B
Days	\rightarrow	2	1
	:	:	2

$$\left(\text{Days} \propto \frac{1}{\text{Efficiency}} \right)$$

Now, let A requires x days, then B requires $2x$ days

$$\therefore \text{Difference in number of days} (= 2x - x) = x = 6$$

$$\Rightarrow x = 6$$

$\therefore B$ requires $2x = 2 \times 6 = 12$ days

Alternatively : If A takes x days, then B takes $x + 6$ days

Now, A 's 1 day's work = $\frac{1}{x}$

B 's 1 day's work = $\frac{1}{x+6}$

$$\therefore \frac{1/x}{1/(x+6)} = \frac{2}{1}$$

$$\frac{1}{x} = \frac{2}{x+6}$$

(Since A does twice the work as B does)

$$\Rightarrow x = 6$$

$\therefore B$ takes $2x = 12$ days.

Alternatively : $\frac{1}{x} + \frac{1}{(x+6)} = \frac{1}{4}$

$\Rightarrow x = 6$ and $2x = 12$ days (required by B)

Alternatively : Go through option and satisfy all the conditions.

14.

Ratio of efficiency	\rightarrow	A	B	C
	:	3	1	2

Ratio of number of days	\rightarrow	$\frac{1}{3}$	$\frac{1}{1}$	$\frac{1}{2}$
	:	1	1	2

or	\rightarrow	2	6	3
----	---------------	---	---	---

Hence, (a) is correct $\left[\because \text{Time} \propto \frac{1}{\text{Efficiency}} \right]$

15.

Efficiency	\rightarrow	$Ajit$	$Bablu$
	:	3	1

No. of days	\rightarrow	1	3
	:	1	3

16.

Efficiency	\rightarrow	X	Y
	:	5	1

No. of days	\rightarrow	1	5
	:	1	5

17. Efficiency of $A + B = \frac{100}{20} = 15\%$

No. of days	\rightarrow	A	B
	:	4	5

Efficiency	\rightarrow	5	4
	:	1	1

$$\therefore \text{Efficiency of } B = \frac{4}{9} \times 15 = \frac{20}{3} = 6\frac{2}{3}\%$$

18. Efficiency of $A + B = 33.33\% \left(= \frac{100}{3} \right)$

Ratio of efficiency of A and $B = 3:1$

$$\therefore \text{Efficiency of } A = \frac{3}{4} \times 33.33 = 25\%$$

$$\therefore \text{Number of days taken by } A = 4 \left(= \frac{100}{25} \right)$$

Alternatively :

	A	B
Efficiency	3	1
No. of days	$1(x)$	$3(x)$

$$\therefore \text{Difference in days} = 2x = 8$$

$$\Rightarrow x = 4 \text{ and } 3x = 12$$

Therefore number of days taken by A , working alone = 4 days

Alternatively : $\frac{1}{x} + \frac{1}{(x+8)} = \frac{1}{3}$

Now, you can use the options, or solve the equations to get the value of x which is equal to 4.

19. Efficiency of $(A + B) = 12.5\%$

Efficiency of $(B + C) = 8.33\%$

Efficiency of $(C + A) = 12.5\%$

$$\therefore \text{Efficiency of } [(A + B) + (B + C) + (C + A)] = 33.33\%$$

$$\therefore \text{Efficiency of } (A + B + C) = 16.66\%$$

\therefore Number of days required by A, B and C together = 6 days

$$\left(= \frac{100}{16.66} \right)$$

20. Efficiency of $(A + B) = 8.33\%$

Efficiency of $(B + C) = 6.66\%$

Efficiency of $(C + A) = 5.00\%$

$$\therefore \text{Efficiency of } A + B + C = \frac{1}{2} (8.33 + 6.66 + 5) = 10\%$$

$$\therefore \text{Efficiency of } C = \text{Efficiency of } [(A + B + C) - (A + B)] \\ = (10 - 8.33) = 1.66\%$$

$$\therefore \text{Number of days required by } C \text{ alone} = \frac{100}{1.66} = 60 \text{ days}$$

21. Remember

$$\text{Time} \propto \frac{1}{\text{Efficiency}}$$

Now,

	Ganga	:	Jamuna	:	Saraswati
Efficiency	→ 3	:	1	:	2
No. of days	→ 2	:	6	:	3

Again, efficiency of Ganga, Jamuna and Saraswati

$$= \frac{100}{1} = 100\%$$

$$\therefore \text{Efficiency of Ganga} = \frac{3}{6} \times 100 = 50\%$$

$$\text{Efficiency of Saraswati} = \frac{2}{6} \times 100 = 33.33\%$$

$$\text{Now, number of days taken by Ganga} = \frac{100}{50} = 2$$

$$\text{Number of days taken by Saraswati} = \frac{100}{33.33} = 3$$

\therefore Difference in number of days taken by Ganga and Saraswati
 $= 3 - 2 = 1$ day

22. Day 1 2 3 4 5 6 7 8
 $\frac{A}{A} \frac{A}{A} \frac{A}{A} (A + B) (A + B) (A + B) (A + B) (A + B)$

$$3 \times \frac{1}{12} = \frac{3}{12} = 25\% \quad \left. \begin{array}{l} \text{Remaining work} \\ \text{work completed} \end{array} \right\} = 75\% = (100 - 25)$$

Now, efficiency of $A + B = 15\% = (8.33 + 6.66)$

$$\therefore \text{Number of days required by } A + B = \frac{75}{15} = 5$$

to complete rest work ($= 75\%$)

23. '3 days before the completion of the work Raja left the work' means in last 3 days only Rani has worked alone.

$$\text{So, in last 3 days worked done by Rani} = 3 \times \frac{1}{21} = \frac{1}{7}$$

So, the rest $\left(1 - \frac{1}{7} \right) = \frac{6}{7}$ work was done by Raja and Rani both.

Number of days in which Raja and Rani worked together

$$= \frac{6/7}{5/42} = \frac{36}{5} = 7 \frac{1}{5} \text{ days}$$

NOTE Work done by Raja and Rani in one day = $\frac{1}{14} + \frac{1}{21} = \frac{5}{42}$

$\left(\text{Also, number of days} = \frac{\text{Total work to be done}}{\text{Work to be done in one day}} \right)$

24. Work done in 11 days = $\frac{11}{30}$

$$\text{Rest work} = \frac{19}{30}$$

$$1 \text{ day's work of } A = \frac{19/30}{28} = \frac{19}{30 \times 28} = \frac{19}{840}$$

Total number of days required to complete the whole work alone

$$= \frac{1}{19/840} = \frac{840}{19} = 44 \frac{4}{19} \text{ days}$$

25. Efficiency of Sonu = $5\% = \left(\frac{100}{20} \right)$

Rest work = 75%

$$\therefore \text{Efficiency of Abhijeet} = \frac{75}{10} = 7.5\%$$

\therefore Combined efficiency of Sonu and Abhijeet
 $= 12.5\% = (7.5 + 5)$

\therefore Number of days required by Sonu and Abhijeet, to work together

$$= \frac{100}{12.5} = 8 \text{ days}$$

26. Asha Usha

Efficiency	5	4
No. of days	$4x$	$5x = 25$

\therefore Number of days required by Asha to finish the work alone
 $= 20 \quad \because (4x = 4 \times 5)$

(Alternatively, from percentage change graphic, number of days taken by Asha will be 20% less than Usha, if efficiency of Asha is 25% more than Usha)

Now, since Asha and Usha did work together for last 5 days
 $= 5 \times 9 = 45\%$

(Since efficiency of Asha = 5% and Usha's efficiency = 4%)

It means Asha completed 55% work alone

∴ Number of days taken by Asha to complete 55% work
 $= \frac{55}{5} = 11 \text{ days}$

27. Krishna's efficiency = 10%

Mohan's efficiency = 5%

Work done by Krishna and Mohan together in 3 days
 $= 15 \times 3 = 45\%$

Now, number of days in which B completed rest (55%) work alone
 $= \frac{55}{5} = 11$

Total number of days in which B worked = $3 + 11 = 14$

Now number of days required by B, when A and B both worked together = $\frac{100}{15} = 6 \frac{2}{3}$

∴ Required difference in number of days = $(11) - \left(6 \frac{2}{3}\right)$
 $= \frac{13}{3} = 4 \frac{1}{3} \text{ days}$

28. Efficiency of Kareena and Karishma

$$= 11.11 + 5.55 = 16.66\%$$

Work done in 3 days = $3 \times 16.66 = 50\%$

Rest work done by Kareena, Karishma and Shahid = $\frac{50}{50} = 1 \text{ day}$

(Since efficiency of Shahid = 33.33%)

Thus in 4 ($= 3 + 1$) days they have completed the work.

29. Efficiency of Kavita = 5%

Efficiency of Babita = 1.66%

Efficiency of Samita = 3.33%

Work done in 5 days by $K + B + S = 5 \times (10) = 50\%$

Work done in 3 days by $K + B = 3 \times (6.66) = 20\%$

Remaining work (30%) done by Kavita alone = $\frac{30}{5} = 6 \text{ days}$

30. $A : B : C$
 Efficiency $\rightarrow 10 : 9 : 6$
 No. of days $\rightarrow 9x : 10x : 15x$

Now, $15x - 9x = 6$

$$\Rightarrow x = 1$$

∴ Number of days taken by A = 9

Number of days taken by B = 10

Number of days taken by C = 15

Work done by B and C in initial 2 days = $\frac{2 \times 1}{6} = \frac{1}{3}$

$$\text{rest work} = \frac{2}{3}$$

Number of days required by A to finish $\frac{2}{3}$ work = $\frac{2/3}{1/9} = 6 \text{ days}$

31.

	Anand	Bahuguna
No. of days	45	40
Efficiency	$2.22\% \left(= \frac{1}{45}\right)$	$2.5\% \left(= \frac{1}{40}\right)$

Anand did the work in 56 days = $56 \times \frac{1}{45 \times 2} = \frac{28}{45}$

∴ Rest work $\left(\frac{17}{45}\right)$ was done by Anand and Bahuguna
 $= \frac{17/45}{17/360} = 8 \text{ days}$

(Since Anand and Bahuguna do the work in one day
 $= \frac{1}{45} + \frac{1}{40} = \frac{17}{360}$)

32. Efficiency of Chandni = 11.11%

Efficiency of Divakar = 8.33%

They do 19.44% work in 2 days

∴ They need 10 days to do 97.22% work,

Now the rest work (2.78) was done by Chandni in $\frac{2.78}{11.11} = \frac{1}{4}$ day

Therefore total number of days required = $10 + \frac{1}{4} = 10 \frac{1}{4} \text{ days}$

Alternatively : Chandni's one day's work = $\frac{1}{9}$

Divakar's one day's work = $\frac{1}{12}$

Chandni's and Divakar's ($1 + 1$) = 2 day's work = $\frac{1}{9} + \frac{1}{12} = \frac{7}{36}$

So, in 10 days they do = $\frac{7 \times 5}{36} = \frac{35}{36}$ work

So, the remaining $\frac{1}{36} \left(= 1 - \frac{35}{36}\right)$ work will be done by

Chandni = $\frac{1/36}{1/9} = \frac{1}{4} \text{ day}$

Thus total number of required days = $10 + \frac{1}{4} = 10 \frac{1}{4} \text{ days}$

HINT

Day	1	2	3	4	5	6	7	8	9	10	11								
Turn	C	D	C	D	C	D	C	D	C	D	C								
Work	$\frac{1}{9}$	$\frac{1}{12}$	$\frac{1}{36}$																
	$\underline{7/36}$		$\underline{7/36}$		$\underline{7/36}$		$\underline{7/36}$		$\underline{7/36}$		$\underline{35/36}$								

Day	1	2	3	4	5	6	7	8	9	10	11	12	13	14
F	Z	F	Z	F	Z	F	Z	F	Z	F	Z	F	Z	
$\frac{1}{12}$	$\frac{1}{15}$	$\frac{1}{12}$	$\frac{1}{60}$											
$\underline{9/60}$	$\underline{6/60}$													

In two days Fatima and Zahira do = $\frac{1}{12} + \frac{1}{15} = \frac{9}{60}$ work. In 12 days they do = $\frac{6 \times 9}{60} = \frac{54}{60}$ work

So, the remaining work = $\frac{6}{60} = \frac{1}{10}$

Now, $\frac{1}{12}$ work will be done by Fatima in 13th day

So, the remaining work = $\frac{1}{10} - \frac{1}{12} = \frac{1}{60}$

This $\frac{1}{60}$ work will be done by Zahira = $\frac{1/60}{1/15} = \frac{1}{4}$ day

Thus the total number of days required

$$= 12 + 1 + \frac{1}{4} = 13\frac{1}{4} \text{ days}$$

Alternatively : A's efficiency = 8.33%
B's efficiency = 6.66% 15%

Thus in 12 days 90% work will be done and in 13th day 8.33% more work will be done so the rest work 1.66% will be done by Zahira

$$= \frac{1.66}{6.66} = \frac{1}{4} \text{ day}$$

Thus, total number of required days = $12 + 1 + \frac{1}{4} = 13\frac{1}{4}$

34. The difference will arise only on the last two days only. The work done on 13th day = $\frac{1}{15}$

$$\text{rest work} = \frac{1}{10} - \frac{1}{15} = \frac{1}{30}$$

This rest work $\left(\frac{1}{30}\right)$ will be done by Fatima = $\frac{1/30}{1/12} = \frac{2}{5}$ day

Thus total number of required days = $12 + 1 + \frac{2}{5} = 13\frac{2}{5}$ days.

1	2	3	4	5	6	7	8
A	B	C	A	B	C	A	B
$1/6$	$1/12$	$1/8$	$1/6$	$1/12$	$1/8$	$1/6$	$1/12$
$3/8$		$3/8$				$1/4$	

$$\frac{6}{8} = \frac{3}{4}$$

In 3 days A, B, C do $\frac{3}{8}$ work

In 6 days A, B, C do $\frac{3}{4}$ work

Rest work = $\frac{1}{4}$, which is less than $\frac{3}{8}$

On the 7th day, $\frac{1}{6}$ more work will be done by A

Now rest work = $\frac{1}{4} - \frac{1}{6} = \frac{1}{12}$

Now, this rest work $\left(\frac{1}{12}\right)$ will be done by B in 1 complete day.

Thus, total number of days = $6 + 1 + 1 = 8$ days

Alternatively : Efficiency of A = 16.66%

Efficiency of B = 8.33%

Efficiency of C = 12.5%

Efficiency of A + B = 25%

Efficiency of A + B + C = 37.5%

In 3 days A, B, C completes 37.5% work

In 6 days A, B, C completes 75% work

Rest work = 25%

This 25% work will be completed by A and B in next 2 days
Thus total 6 + 2 = 8 days are needed.

36. From the previous solution 75% work will be completed in 6 days. In the next two days (i.e., on 7th and 8th day) B and C will complete 20.83% (12.5 + 8.33) more work.

So the remaining work = 4.16%

This 4.16% work will be completed by A = $\frac{4.16}{16.66} = \frac{1}{4}$ day

So, the total number of required days = $6 + 2 + \frac{1}{4} = 8\frac{1}{4}$ days.

37. Let B takes x days to complete the work individually.

Then, the B's 1 day's work = $\frac{1}{x}$

A's 1 day's work = $\frac{1}{x-6}$

C's 1 day's work = $\frac{1}{x-8}$

$$\therefore \frac{1}{x-6} + \frac{1}{x} = \frac{1}{x-8}$$

Now either solve the equation or satisfy the equation from the choices given in the question.

Thus option (c) is correct.

Alternatively : Select an appropriate option and then solve through % efficiency.

38. A's share = Rs. 250
B's share = Rs. 100

It means the ratio of efficiency of A : B = 250 : 100 = 5 : 2

\therefore Ratio of days taken by A and B = $2x : 5x$

Now, $5x - 2x = 9 \Rightarrow x = 3$

\therefore Number of days taken by A = 6 (efficiency = 16.66%)

Number of days taken by B = 15 (efficiency = 6.66%)

Therefore number of days taken by A and B, working together

$$= \frac{100}{23.33} = \frac{300}{70} = 4\frac{2}{7} \text{ days}$$

39. Alen's one day's work = $\frac{1}{21}$

Border's one day's work = $\frac{1}{42}$

(working alternatively) Alen and Border's two days work

$$= \frac{1}{21} + \frac{1}{42} = \frac{1}{14}$$

So, Alen and Border do $\frac{1}{14}$ work in 2 days

So, they complete the work in $14 \times 2 = 28$ days.

40. Efficiency of A and B = 16.66%

Efficiency of B and C = 10%

But efficiency of A is twice that of C

\therefore Therefore, $A = 2C$

Now $A + B = 16.66$ and $B + C = 10$

$$\Rightarrow 2C + B = 16.66 \quad \dots(1)$$

$$\text{and} \quad C + B = 10 \quad \dots(2)$$

∴ from eq. (1) and (2) $C = 6.66\%$

∴ $A = 13.33\%$

∴ Number of days taken by A to complete the work alone

$$= \frac{100}{13.33} = 7 \frac{1}{2} \text{ days}$$

41. $A + B = 70\%$

$$B + C = 50\% \quad \left[\because A + B + C - (A + B + C) = B \right]$$

$$70 + 50 - 100 = 20\%$$

$$\Rightarrow B = 20\%$$

$$A = 50\%$$

and

$$C = 30\%$$

Hence, A is most efficient.

42. $C + M = \frac{8}{17}$

$$M + G = \frac{12}{17}$$

$$\Rightarrow M = \frac{3}{17}$$

$$[\because (C + M + M + G) - (C + M + G) = M]$$

$$\left[\left(\frac{8}{17} + \frac{12}{17} \right) - 1 = \frac{3}{17} \right]$$

$$\therefore C = \frac{5}{17}$$

$$G = \frac{9}{17}$$

So the whole amount will be distributed in the ratio of 5 : 3 : 9 among C , M and G respectively.

Now since M is least efficient so he get his own share

$$= \frac{3}{17} \times 816 = \text{Rs. } 144$$

43. $\begin{array}{lll} & \text{Sharma} & \text{Kelkar} \\ \text{Efficiency} & 0.8x & x \\ \text{Number of day} & k & 0.8k = 24 \\ \therefore 0.8k = 24 & \Rightarrow k = 30 \end{array}$

Thus Sharma requires 30 days, to complete the work, alone.

44. $\begin{array}{lll} \text{Man} & \text{Days} \\ \frac{1}{5} \uparrow \left(\begin{array}{ll} 30 & 24 \\ 36 & 20 \end{array} \right) & \frac{1}{6} \downarrow \end{array}$

Applying product constancy method.

For a constant work when days are reduced by $\frac{1}{6}$, then

number of men is increased by $\frac{1}{5}$. Hence 6 men will increase.

Alternatively : $24 \times 30 = 20 \times x$

$$\Rightarrow x = 36$$

Therefore 6 more men are required.

45. $\begin{array}{lll} \text{Women} & \text{Days} \\ \downarrow \frac{1}{3} \left(\begin{array}{ll} 12 & 20 \\ 8 & 30 \end{array} \right) & \frac{1}{2} \uparrow \end{array}$

Thus 10 more days are required.

Alternatively : $12 \times 20 = 8 \times x$

$$\Rightarrow x = 30$$

∴ 10 more days are required.

46. $\begin{array}{lll} \text{Boys} & \text{Days} \\ \frac{2}{5} \downarrow \left(\begin{array}{ll} 35 & 15 \\ 21 & 25 \end{array} \right) & \frac{2}{3} \uparrow \end{array}$

Thus 14 boys did not turn up for the job.

Alternatively : $35 \times 15 = 25 \times x$

$$\Rightarrow x = 21$$

∴ $35 - 21 = 14$ boys did not turn up for the job.

47. $x \times 32 = 24 \times 40 \quad (M_1 D_1 = M_2 D_2)$

48. $M \times D = W$

$$16 \times 6 = \frac{1}{3} W$$

$$\text{Rest work} = \frac{2}{3} W$$

For double work in same time we need double men. So 16 more men are required.

Alternatively : $2 \times (16 \times 6) = 6 \times M$

$$\Rightarrow M = 32$$

∴ 16 more men are required.

49. $M \times D = 10 \times 20 = 200 \text{ Man-days}$

$$\text{New Man-days} = (20 \times 2) \times x$$

$$200 = 20 \times 2 \times x$$

$$x = 5 \text{ days}$$

or $M_1 D_1 = M_2 D_2$

$$10 \times 20 = (20 \times 2) \times x$$

$$\Rightarrow x = 5$$

50. $M_1 D_1 = M_2 D_2$

$$M_1 \times 20 = (M_1 - 12) \times 32$$

$$\Rightarrow M_1 = 32$$

Also, using the above concept you can go through options.

51. Go through options. Consider option (c)

$$30 \times 20 = 30 \times 6 + 21 \times 20$$

600 = 600, hence presumed option is correct.

Alternatively : $30 \times 20 = 30 \times x + 21 \times (26 - x)$

$$\Rightarrow x = 6$$

52. Go through options. Consider choice (a)

$$25 \times 30 = 25 \times 15 + 75 \times 5$$

750 = 750, hence choice (a) is correct.

Alternatively : $25 \times 30 = 25 \times x + 75 \times (20 - x)$

$$\therefore \left[30 \times \frac{2}{3} = 20 \right]$$

53. Go through options. Consider choice (d)

$$36 \times 120 = 40 \times 108$$

$$4320 = 4320$$

Hence, choice (d) is correct.

Alternatively :

$$\begin{array}{ccccc}
 & \text{Men} & & \text{Days} & \\
 \frac{1}{9} \uparrow & x & 120 & \left(\frac{1}{10}\right) \downarrow & \\
 & \downarrow & \downarrow & & \\
 \left(x \times \frac{10}{9}\right) & & (12) & &
 \end{array}$$

From percentage change (product constancy) graphic when number of days are decreased by $\frac{1}{10}$ then the number of men are increased by $\frac{1}{9}$ and $\frac{1}{9}$ is equivalent to 4 men so the actual number of men are $9 \times 4 = 36$.

Alternatively : $M_1 D_1 = M_2 D_2$

$$x \times 120 = (x + 4) \times 108$$

$$\Rightarrow x = 36$$

54. Efficiency (per minute) of Modi = 4 copies/min

Efficiency of Modi and Xerox together = 10 pages/min

∴ Efficiency of Xerox alone = $10 - 4 = 6$ pages/min

∴ Mr. Xerox needs 6 minutes to copy 36 pages.

55. Work done = $\frac{1}{3}$

$$\text{Remaining work} = \frac{2}{3}$$

$$2 \times (20 \times 12) = 12 \times x$$

$$\Rightarrow x = 40$$

So, 20 men will be increased.

56. Work done = $\frac{1}{5}$

$$\text{remaining work} = \frac{4}{5}$$

$$4 (20 \times 75) = 40 \times x$$

$$x = 150$$

Therefore 75 men should be increased.

57. Work done by 6 men = Work done by 10 women.

$$\Rightarrow \text{Work done by 1 man} = \text{work done by } \frac{10}{6} = \frac{5}{3} \text{ women}$$

$$\therefore 12 \text{ men} + 5 \text{ women} = 12 \times \frac{5}{3} + 5 = 25 \text{ women}$$

$$\therefore W_1 \times D_1 = W_2 \times D_2, \quad W = \text{women}, D = \text{days}$$

$$10 \times 15 = 25 \times D_2$$

$$D_2 = 6$$

58. Work done by 2 men = 3 women = 4 boys

$$\therefore 1 \text{ man} = 2 \text{ boys}$$

$$1 \text{ woman} = \frac{4}{3} \text{ boys}$$

$$\therefore \text{boys} \times \text{days} = 4 \times 52 \text{ (boys-days)}$$

$$\text{Again } 1 \text{ man} + 1 \text{ woman} + 1 \text{ boy} = 2 + \frac{4}{3} + 1 = \frac{13}{3} \text{ boys}$$

$$B_1 \times D_1 = B_2 \times D_2, \quad B = \text{boys}, D = \text{days}$$

$$4 \times 52 = \frac{13}{3} \times D_2$$

$$D_2 = 48 \text{ days}$$

59. 2 men = 7 boys $\Rightarrow 1 \text{ man} = \frac{7}{2} \text{ days}$

$$5 \text{ women} = 7 \text{ boys} \Rightarrow 1 \text{ woman} = \frac{7}{5} \text{ boys}$$

$$7 \text{ men} + 5 \text{ women} + 2 \text{ boys} = 7 \times \frac{7}{2} + 5 \times \frac{7}{5} + 2 = \frac{67}{2} \text{ boys}$$

$$\text{Now, } B_1 \times D_1 = B_2 \times D_2$$

$$7 \times 469 = \frac{67}{2} \times D_2$$

$$\Rightarrow D_2 = 98 \text{ days}$$

60. $6C + 2M = 6 \text{ days}$

$$\Rightarrow 36C + 12M = 1 \text{ days}$$

$$\text{Again } 1M = 2C$$

$$\therefore 36 + 12 \times 2 = 1 \text{ day}$$

60 children can do the work in 1 day

$$\text{Now, } 5 \text{ men} = 10 \text{ children}$$

∴ 10 children can do the work in 6 days.

61. $8M + 12W = 4 \text{ days (whole work)}$

$$\Rightarrow 32M + 48W = 1 \text{ day} \quad \dots(1)$$

$$\text{Again } 6M + 14W = 5 \text{ days}$$

$$\Rightarrow 30M + 70W = 1 \text{ day} \quad \dots(2)$$

From eq. (1) and (2)

$$32M + 48W = 30M + 70W$$

$$\Rightarrow 2M = 22W$$

$$\Rightarrow 1M = 11W$$

$$\text{Now, } 30M + 70W = 1 \text{ day}$$

$$(30 \times 11 + 70)W = 1 \text{ day}$$

Therefore 400W requires 1 day to complete the whole work.

Thus 20W needs 20 days to complete the whole work.

62. Efficiency of A = 6.66%

Efficiency of B = 5.55%

Efficiency of A + B + C = 16.66%

∴ Efficiency of C = 4.44%

Now, number of days required by

$$C = \frac{100}{4.44} = \frac{100}{(10 \times 4)/9} = \frac{45}{2} \text{ days}$$

63. Ratio of efficiencies of A, B and C = 6 : 5 : 4

$$\therefore \text{Share of } C = \frac{4}{15} \times 27000 = 7200$$

64. In 1 hour 314 weavers weave = 6594×6 shawls

$$\text{In 1 hour 1 weaver weaves} = \frac{6594 \times 6}{314} \text{ shawls} = 126 \text{ shawls}$$

65. $3M + 2W = 4 \text{ days}$

$$\Rightarrow 12M + 8W = 1 \text{ day} \quad \dots(1)$$

$$\text{Again, } 2M + 3W = 5D$$

$$\Rightarrow 10M + 15W = 1D \quad \dots(2)$$

From eq. (1) and (2)

$$12M + 8W = 10M + 15W$$

$$\Rightarrow 2M = 7W$$

$$\Rightarrow \frac{M}{W} = \frac{7}{2}$$

Since the ratio of efficiency of women : men = 2 : 7
So, the amount of a man per day = Rs. 154

$$\left[\left(\frac{7}{2} \times 44 \right) = 154 \right]$$

66. Go through options.

Alternatively :

$$30 \times 40 = 30 \times x + 20 \times (46 - x)$$

$$\Rightarrow x = 28 \text{ days}$$

67. Women \times hours = 8 \times 10 = 80 women hours

Now, women \times hours = 12 \times 8 = 96 women hours

Since new work force is 20% greater than previous work force.

So, the new quantity of tea leaves will be increased by 20% which is equal to $200 \times \frac{20}{100} = 40 \text{ kg}$, hence (b)

68. New work = 3 \times 450 man-day

$$\therefore 3 \times 450 = 27 \times x \\ x = 50 \text{ days}$$

69. $4B + 5G = 10$

$$\Rightarrow 40B + 50G = 1 \quad \dots(1)$$

$$\text{Again, } 6B + 6G = 7$$

$$\Rightarrow 42B + 42G = 1 \quad \dots(2)$$

Comparing eq. (1) and (2)

$$40B + 50G = 42B + 42G$$

$$\Rightarrow 2B = 8G \Rightarrow 1B = 4G$$

$$\text{Now, } (42 \times 4 + 42) \text{ girls} = 1 \text{ day}$$

210 girls can do a work in 1 day

$$\text{Again } 2B + 7G = 15 \text{ girls}$$

$$\text{So, } 15 \text{ girls require } \frac{210}{15} = 14 \text{ days}$$

70. Equate the man-days

For 20 km road, $20 \times 20 = 400$ man-days are required

\therefore For 40 km road 800 man-days are required

$$\text{So, } 800 = 40 \times x$$

$$\Rightarrow x = 20 \text{ days}$$

$$71. \frac{3}{4} \times (x - 2)x = (x + 7)(x - 10)$$

$$\Rightarrow x^2 - 6x - 280 = 0$$

$$\Rightarrow x = 20 \text{ and } x = -14$$

So, the acceptable values is $x = 20$

$$\therefore \text{Total work} = (x - 2) \times x = 18 \times 20 = 360 \text{ unit}$$

$$\text{Now } 360 = 30 \times k \quad \therefore (30 = 20 + 10)$$

$$\Rightarrow k = 12 \text{ days}$$

72. Efficiency of a man : woman : girl = 6 : 3 : 1

$$\therefore \text{Share of a woman and girl} = \frac{(3+1)}{(6+3+1)} \times 10,000 \\ = \frac{4}{10} \times 10000 = \text{Rs. 4000}$$

73. Total work = $33 \times 30 = 990$ man-days

$$\text{First day's work} = \frac{1}{990} \times 44$$

$$\text{Second day's work} = \frac{1}{990} \times 43$$

$$\text{Third day's work} = \frac{1}{990} \times 42 \text{ and so on}$$

$$\text{So, the total work in 44 days} = \frac{1}{990} (44 + 43 + 42 + \dots) \\ = \frac{1}{990} \times \frac{44 \times 45}{2} = 1$$

Hence in 44 days total work will be completed.

$$74. \text{Efficiency of Abhishek} = 2.5\% = \left(\frac{100}{40} \right)$$

Work done in 8 days = 20%

Rest work = 80%

$$\text{Efficiency of Bacchhan} = \frac{80}{24} = 3.33\%$$

$$\therefore \text{Required number of days} = \frac{100}{(2.5 + 3.33)} \\ = \frac{100}{5.83} = \frac{100 \times 6}{35} = 17 \frac{1}{7}$$

HINT $0.83 = \frac{5}{6}$, so, $5.83 = 5 + \frac{5}{6} = \frac{35}{6}$

$$75. \begin{array}{cccccc} & A & & B & & C \\ \text{Efficiency} & 3 & : & 2 & : & 6 \\ \text{Number of days} & 2 & : & 3 & : & 1 \end{array}$$

\therefore Number of days taken by A = 12

Number of days taken by B = 18

Number of days taken by C = 6

$$1 \text{ day's work of } (A + B) = \frac{5}{36}$$

$$1 \text{ day's work of } (B + C) = \frac{8}{36}$$

$$1 \text{ day's work of } (C + A) = \frac{9}{36}$$

Day	\rightarrow	1	2	3	4	5	6
Work	\rightarrow	$\frac{5}{36}$	$\frac{8}{36}$	$\frac{9}{36}$	$\frac{5}{36}$	$\frac{8}{36}$	$\frac{1}{36}$
35/36						1/36	

In 5 days total work done = $\frac{35}{36}$

Now, the rest work (1/36), which is done by AC.

\therefore Number of days taken by AC for the rest work

$$= \frac{1/36}{9/36} = \frac{1}{9}$$

Therefore, total time = $5 + \frac{1}{9} = 5 \frac{1}{9}$ days

76. Efficiency of A + B = 16.66

Efficiency of B + J = 10

We have no further relevant informations, so we cannot determine.

	A	B	
Efficiency	x	$2x$	
Number of days	15	$15/2$	

$$A's \text{ one day's work} = \frac{1}{15}$$

$$B's \text{ one day's work} = \frac{2}{15}$$

$$(A+B)'s \text{ one day's work} = \frac{3}{15}$$

Now, let us assume B joined A after $(11 - x)$ days, then

$$\frac{(11-x)}{15} + \frac{x \times 3}{15} = 1$$

$$\Rightarrow (11-x) + 3x = 15$$

$$\Rightarrow x = 2$$

It means they worked together for 2 days.

Alternatively: Go through options and check easily with the percentage efficiency.

$$9 \times 6.66 + 2 \times 20 = 100\%$$

78. Efficiency of A = 6.66%

$$\text{Efficiency of B} = 3.33\%$$

$$\text{Efficiency of C} = 2.5\%$$

Work done in last two days (only C do it) = $2 \times 2.5 = 5\%$

Work done in the 3rd and 4th day from the last day (only A and C do it)

$$= 2 \times 9.16 = 18.33\%$$

$$\text{Remaining work} = 100 - (5 + 18.33) = 76.66\%$$

This 76.66% work was done by all of A, B and C.

$$\therefore \text{Number of days taken by them} = \frac{76.66}{12.5} = \frac{460}{75} = 6 \frac{2}{15}$$

$$\therefore \text{Total time required} = 6 \frac{2}{15} + 2 + 2 = 10 \frac{2}{15} \text{ days}$$

79. Let x kg of oil is used for eating purpose, daily, then

$$(x + 11) \times 50 = (x + 15) \times 45$$

$$x = 25$$

$$\therefore \text{Total quantity of oil} = (25 + 11) \times 50 = 1800$$

$$\therefore \text{Required number of days} = \frac{1800}{25} = 72 \text{ days}$$

80. Work done = $\frac{2}{3}$

$$\text{Remaining work} = \frac{1}{3}, \text{ which is half of } \frac{2}{3}$$

$$\therefore \frac{1}{2} \times (20 \times 32) = 8 \times x$$

$$\Rightarrow x = 40 \text{ men}$$

Therefore, 20 more men were required.

81. One day's work of 7 Indian with 4 Chinese = $\frac{1}{5}$

$$\text{and one day's work of 7 Japanese and 3 Chinese} = \frac{1}{7}$$

Therefore, one day's work of 7 Indian, 7 Chinese and 7 Japanese

$$= \frac{1}{5} + \frac{1}{7} = \frac{12}{35}$$

Therefore, one day's work of 1 Indian, 1 Chinese and 1 Japanese

$$= \frac{12}{35} \times \frac{1}{7} = \frac{12}{35 \times 7}$$

Therefore, number of days required by 1 Indian, 1 Chinese and 1 Japanese

$$= \frac{1}{12/(35 \times 7)} = \frac{35 \times 7}{12} = 20 \frac{5}{12} \text{ days}$$

82. In 1 minute A, B and C bind = $\frac{1}{8} + \frac{1}{12} + \frac{1}{16} = \frac{13}{48}$ book

$$\text{In 12 hours A, B and C bind} = 12 \times 60 \times \frac{13}{48} = 195 \text{ books}$$

$$\therefore \text{Average number of books bind by each} = \frac{195}{3} = 65 \text{ books}$$

83. Work of a man for 1 hour = $\frac{3}{2}$ women's work for 1 hour

Again, work of a man for 1 day

$$= \left(\frac{3}{2} \times \frac{9}{7.5} \right) \text{ women's work for 1 hour}$$

$$\Rightarrow \text{Work of a man for 1 day} = \frac{9}{5} \text{ women's work for 1 day}$$

$$\Rightarrow 1 \text{ man} = \frac{9}{5} \text{ women}$$

$$\therefore 10 \text{ men} + 6 \text{ women} = 10 \times \frac{9}{5} + 6 = 24 \text{ women}$$

$$\therefore 10 \text{ men} + 9 \text{ women} = 10 \times \frac{9}{5} + 9 = 27 \text{ women}$$

Now, $D_1 \times W_1 = D_2 \times W_2$

$$18 \times 24 = D_2 \times 27$$

$$\Rightarrow D_2 = 16 \text{ days}$$

84. Number of days taken by A to complete work alone = 14 days

$$\text{Number of days taken by B to complete work alone} = 7 \text{ days}$$

$$\text{Number of days taken by C to complete work alone} = 7 \text{ days}$$

$$\text{One day's work of A and B} = \frac{1}{14} + \frac{1}{7} = \frac{3}{14}$$

$$\text{and one day's work of A, B and C} = \frac{1}{14} + \frac{1}{7} + \frac{1}{7} = \frac{5}{14}$$

$$3 \text{ day's work of A and B} = 3 \times \frac{3}{14} = \frac{9}{14}$$

$$\text{remaining work} = \frac{5}{14} \quad \left(1 - \frac{9}{14}\right)$$

This remaining work will be done by A, B and C

$$= \frac{5/14}{5/14} = 1 \text{ day}$$

85. A's 5 days work = 50%

$$B's 5 \text{ days work} = 33.33\%$$

$$C's 2 \text{ days work} = 16.66\% \quad [100 - (50 + 33.33)]$$

$$\text{Ratio of contribution of work of A, B and C} = 50 : 33 \frac{1}{3} : 16 \frac{2}{3}$$

$$= 3 : 2 : 1$$

$$A's \text{ total share} = \text{Rs. } 1500$$

$$B's \text{ total share} = \text{Rs. } 1000$$

$$C's \text{ total share} = \text{Rs. } 500$$

$$A's \text{ one day's earning} = \text{Rs. } 300$$

$$B's \text{ one day's earning} = \text{Rs. } 200$$

$$\text{and } C's \text{ one day's earning} = \text{Rs. } 250$$

$$86. \text{ Efficiency of } A = 50\% \quad \left(\frac{100}{2} \right)$$

$$\text{Efficiency of } B = 37.5\% \quad \left(\frac{100}{8/3} \right)$$

$$\text{Efficiency of } C = 12.5\% \quad \left(\frac{100}{8} \right)$$

$$\text{Combined efficiency of } A, B \text{ and } C = 100\%$$

So, they complete the work in 1 hour.

$$87. \quad \begin{array}{rcl} A & + & B \\ \downarrow & & \downarrow \\ 10x & + & 5x \\ \hline 15x & & \end{array} = \begin{array}{rcl} C & + & D \\ \downarrow & & \downarrow \\ 9x & + & 6x \\ \hline 15x & & \end{array}$$

Ratio of efficiency

$$\text{Therefore, ratio of efficiency of } A : C = 10 : 9$$

$$\text{Therefore, ratio of days taken by } A : C = 9 : 10$$

$$\text{Therefore, number of days taken by } A = 18 \text{ days}$$

$$88. \text{ Efficiency of 4 men and 2 boys} = 20\%$$

$$\text{Efficiency of 3 women and 4 boys} = 20\%$$

$$\text{Efficiency of 2 men and 3 women} = 20\%$$

$$\therefore \text{Efficiency of 6 men, 6 women and 6 boys} = 60\%$$

$$\therefore \text{Efficiency of 1 man, 1 woman and 1 boy} = 10\%$$

Now, since they will work at double their efficiency

$$\therefore \text{Efficiency of 1 man, 1 woman and 1 boy} = 20\%$$

$$\therefore \text{Required number of days} = 5$$

$$89. \quad \begin{array}{l} M_1 \times D_1 = M_2 \times D_2 \\ m \times r = (m+n) \times D_2 \\ D_2 = \frac{mr}{(m+n)} \end{array}$$

$$90. \text{ Efficiency of } A = 2.77\%$$

$$\text{Efficiency of } B = 2.22\%$$

$$\therefore \text{Combined efficiency of } A \text{ and } B = 5\%$$

$$= (2.77 + 2.22)$$

$$\text{Thus, it will take total of 20 minutes} \quad \left(\because 20 = \frac{100}{5} \right)$$

$$91. \text{ Efficiency of } A = 8.33\%$$

$$\text{Effective efficiency} = 6.66\%, \text{ when there is leakage}$$

$$\therefore \text{Efficiency of leakage} = 1.66\% = (8.33 - 6.66)$$

It means due to leakage a full tank will be empty in 60 hours.

$$92. \text{ Efficiency of } A + B = 10 + 6.66 = 16.66\%$$

$$\text{Efficiency of } A + B + C = 5.55\%$$

$$\therefore \text{Efficiency of } C \text{ (outlet pipe)} = 16.66 - 5.55$$

$$= 11.11\%$$

It means outlet pipe C can empty in 9 hours.

$$93. \text{ Efficiency of only leakage} = 16.66\%$$

$$\text{Effective efficiency of leakage} = 6.66\%$$

It means the capacity of filling pipe = 10%

Therefore, the inlet pipe can fill the tank in 10 hours hence the capacity of tank = 100 l.

$$94. \text{ Efficiency of tap } A \text{ and } B = 16.66\% = (10 + 6.66)$$

$$\therefore 16.66x + 10 \times (8 - x) = 100\%$$

$$\Rightarrow x = 3$$

$$95. \quad \begin{array}{l} \text{Efficiency of } A = 5\% \\ \text{Efficiency of } B = 4\% \\ \text{Efficiency of } C = -3.33\% \end{array}$$

It means in every 3 consecutive hours tops A, B and C can fill 5.66% ($= 5 + 4 - 3.33$).

Therefore in 51 hours ($= 3 \times 17$) tops A, B and C can fill 96.33% ($= 5.66 \times 17$).

\therefore the remaining part i.e., 3.66% ($= 100 - 96.33$) can be filled up by A in $\frac{11}{15}$ hours ($= \frac{3.66}{5}$), since it is now A 's turn.

$$\text{Hence, the total time required} = 51 + \frac{11}{15} = 51 \frac{11}{15}$$

$$97. \text{ Efficiency when both pipes used to fill} = A + B \\ \text{and efficiency when pipe } A \text{ is used to fill and pipe } B \text{ is used to empty the tank} = A - B$$

$$\therefore \frac{A + B}{A - B} = \frac{2}{1}$$

$$\Rightarrow \frac{A}{B} = \frac{3}{1} \quad (\text{By componendo and dividendo})$$

Thus, the ratio of efficiency of pipe A and B = 3 : 1.

98. In ideal case:

$$\text{Time taken to fill the half tank by } A \text{ and } B = \frac{50}{41.66} = \frac{6}{5} \text{ hours}$$

Time taken by A, B and C to fill rest half of the tank

$$= \frac{50}{16.66} = 3 \text{ hours}$$

$$\text{Total time} = \frac{6}{5} + 3 = 4 \text{ hours } 12 \text{ minutes}$$

In second case:

$$\text{Time taken to fill } \frac{3}{4} \text{ tank by } A \text{ and } B = \frac{75}{41.66} = \frac{9}{5} \text{ hours}$$

$$\text{Time taken by } A, B \text{ and } C \text{ to fill rest } \frac{1}{4} \text{ tank} = \frac{25}{16.66} = \frac{3}{2} \text{ hours}$$

$$\text{Total time} = \frac{9}{5} + \frac{3}{2} = 3 \text{ hours } 18 \text{ minutes}$$

Therefore, difference in time = 54 minutes

$$99. \text{ Time taken by pipes } A \text{ and } B \text{ to fill the whole tank} = \frac{100}{16.66} = 6 \text{ hours}$$

Capacity filled in 2 hours by pipes A, B and C = 2×13.33

$$= 26.66\%$$

Remaining capacity = 73.33%

This remaining capacity can be filled by A and B

$$= \frac{73.33}{16.66} = 4 \frac{2}{5} \text{ hours}$$

So, the total time required = $2 + 4 \frac{2}{5} = 6 \text{ hours } 24 \text{ minutes}$

Thus, in this case 24 minutes extra are required.

100. In one hour pipe A can fill = $\frac{1}{30}$ part of the tank

In one hour pipe B can fill = $\frac{1}{45}$ part of the tank

In two hour pipes A and B can fill = $\frac{1}{18}$ part of the tank

Therefore in 36 hours the tank will be completely filled.

Alternatively: Efficiency of pipe A = 3.33%

Efficiency of pipe B = 2.22%

and Combined efficiency = 5.55%

Therefore in 2 hours pipe A and B fill 5.55%.

Thus to fill 100% tank, these pipe will take 36 hours.

LEVEL (2)

1. LCM of 2, 3 and 4 = 12

In 12 hours A will make 6 shawls

" " " B will make 4 shawls

" " " C will make 3 shawls

i.e., in 12 hours they will weave 13 shawls

so, in 84 hours they will weave 91 shawls

Now, in 9 hours A will make 4 shawls

in 9 hours B will make 3 shawls

in 9 hours C will make 2 shawls

So, they will complete 100 shawls in 93 hours.

It is clear that in two days finally they work very similar to the alternate days i.e., finally A work for 10 hours and B also works for 10 hours.

Thus in every two days they will complete 7.5% work. So, in 26 days they will complete 97.5% of the total work.

Now, the remaining work = 2.5%

Now, this is the turn of A,

Since A does 4.16% work in 10 hours.

So, he will do 2.5% work in 6 hours.

4. Thus, the work will be finished on 27th day.

5. Since, A does 2.5% work in 6 hours, which is the actual duration of morning shift. So 100% time of the morning shift was utilised.

6. **From the first statement :**

	$(B + C)$	$(A + B + C)$
Efficiency	$2x$	$3x$
Days	$3y$	$2y$

Thus, we can say that efficiency of A is $\frac{1}{3}$ the efficiency of $(A + B + C)$.

- From the last statement:**

$$\text{Share of } B \text{ out of total amount} = \frac{120}{450} = \frac{4}{15}$$

From these two results we can conclude that:

$$\text{Ratio of efficiency} \quad \frac{A}{15} : \frac{B}{15} : \frac{C}{15} \quad (A : B : C = 2 : 3 : 1)$$

$$\Rightarrow 5 : 4 : 6$$

$$\text{Ratio of number of days} \Rightarrow \frac{1}{5} : \frac{1}{4} : \frac{1}{6}$$

$$\Rightarrow 12x : 15x : 10x$$

$$\text{One day's work of } A \text{ and } B = \frac{1}{12x} + \frac{1}{15x} = \frac{9}{60x}$$

$\therefore A \text{ and } B \text{ will take } \frac{60x}{9} \text{ days to complete the whole work,}$

Again one day's work of A, B and C

$$= \frac{1}{12x} + \frac{1}{15x} + \frac{1}{10x} = \frac{15}{60x}$$

$\therefore A, B \text{ and } C \text{ working together complete the work in } \frac{60x}{15} \text{ days}$

$$\therefore \frac{60x}{9} - \frac{60x}{15} = \frac{8}{3}$$

- NOTE Since, they cannot share each-others work so B will take completely 9 hours to make 3 shawls, even when A and C stay idle for the last 1 hour till B completes his own work.

2.	M	T	W	Th	F	S
	A	S	A	S	A	S
Work \rightarrow	<u>15%</u>	<u>15%</u>	<u>7.5%</u>			
	37.5%					

{This pattern continued for total 2 weeks only till 75% work got completed.}

Thus in 2 weeks they will complete 75% work.

Now 15% of the remaining (25% of the work) will be done in the third week in Monday and Tuesday. Again 10% work remained undone. Out of this 8.33% work will be done by Arun on Wednesday and remaining 1.66% work will be completed on Thursday by Satyam.

Final week

M	T	W	Th
A	S	A	S
<u>15%</u>	8.33%	1.66%	
	25%		

3. Efficiency of Kaushalya = 5%

Efficiency of Kaikeyi = 4%

Thus, in 10 days working together they will complete only 90% of the work.

$$[(5 + 4) \times 10] = 90$$

Hence, the remaining work will surely done by Sumitra, which is 10%.

Thus, Sumitra will get 10% of Rs. 700, which is Rs. 70.

4. **Solutions for question number 4 and 5:**

	1st day	2nd day
Morning shift	A	B
Evening shift	B	A

(Since, A and B take $\frac{8}{3}$ days more than A, B and C)

$$\Rightarrow x = 1$$

∴ Number of days required to complete the whole work by A, B and C = $4x = 4 \times 1 = 4$ days

Alternatively: You can solve through option.

Alternatively: Ratio of efficiencies of A, B and C = $5x : 4x : 6x$

$$\therefore \text{Number of days required by A and B} = \frac{100}{9x} \quad \dots(1)$$

$$\text{and number of days required by A, B and C} = \frac{100}{15x} \quad \dots(2)$$

$$\therefore \frac{100}{9x} - \frac{100}{15x} = \frac{8}{3} \Rightarrow x = \frac{5}{3}$$

From eq. (2) number of days required by A, B and C working together

$$= \frac{100}{15x} = \frac{100}{15 \times \frac{5}{3}} = \frac{100}{25} = 4 \text{ days}$$

7.

MIT

$$4 \times 10 \times 60 \times E_1 = 5 \times 8 \times 80 \times E_2$$

$$\Rightarrow \frac{E_1}{E_2} = \frac{4}{3}$$

where E_1 and E_2 are the respective working efficiencies per hour.

∴ Each engineer from NIT is 25% less efficient than each engineer from MIT.

8.

T	C	B
16	10	15
8	12	12
128	120	180
1280	1200	1800

← in one hour

Since, restriction is imposed by composers i.e., since only 1200 books can be composed in 10 hours so not more than 1200 books can be finally prepared.

9. To maximise the production we locate 5 persons for composing and 7 persons for typing. Only then we can maximise our production which is 1800 books per day.

T	C	B
(16 + 7)	(10 + 5)	15
8	12	12
184	180	180
1840	1800	1800

10. 1st case

T	C	B
15	10	13
8	12	12
120	120	156
1200	1200	1560

No change in critical value

2nd case

T	C	B
16	10	12
8	12	12
128	120	144

No change in critical value*

NOTE In third case it will reduce the production below 1200 books per day (or 120 books per hour)

So, option (d) is correct.

11. Efficiency of Bunty and Babli (jointly) = 12.5%

Now, go through options and satisfy the conditions.

Consider option (d).

Efficiency	Bunty	Babli
Days	→ 7.5% → 5% ← 40/3	20 ←

Now, the new efficiency of Bunty = 15%

and the new efficiency of Babli = $\frac{5}{3}$ %

∴ Combined efficiency = $\frac{50}{3}$ %

∴ Number of days taken by them = $\frac{100}{50/3} = 6$ days

Hence, the presumed option (d) is correct.

NOTE Without solving the complete problem we can say that only option (d) is true since other 3 options gives the efficiency of Bunty equal to or more than 12.5% which is inadmissible i.e., cannot be equal to or greater than the combined efficiency of both persons together.

12. Let x litre be the per day filling and v litre be the capacity of the reservoir, then

$$90x + v = 40000 \times 90 \quad \dots(1)$$

$$\text{and} \quad 60x + v = 32000 \times 60 \quad \dots(2)$$

Solving eq. (1) and (2), we get

$$x = 56000$$

Hence, 56000 litres per day can be used without the failure of supply.

13. One day's production = $400 \times 9 \times 60 = 2160000$ bottles per day

Ratio of time utilised by M_1 and $(M_1 + M_2) = 1 : 2$

Now, the production of bottles by M_1 in 1 minute = 400 and the production of bottles by M_1 and M_2 together in

2 minutes = 2000

Thus total 2400 bottles can be processed in 3 minutes

∴ 216000 bottles can be processed in

$$216000 \times \frac{3}{2400} = 4.5 \text{ hours}$$

14. Let he initially employed x workers which works for D days and he estimated 100 days for the whole work and then he doubled the worker for $(100 - D)$ days.

$$D \times x + (100 - D) \times 2x = 175x$$

$$\Rightarrow D = 25 \text{ days}$$

NOTE $175 = 100 + \frac{3}{4} \times 100$, since required number of days are 75%

$\left(\text{i.e., } \frac{3}{4}\right)$ more than the estimated number of days.

Now, the work done in 25 days = $25x$

$$\text{Total work} = 175x$$

∴ Work done before increasing the number of workers

$$= \frac{25x}{175x} \times 100 = 14 \frac{2}{7} \%$$

*Critical value means the minimum amount of job which creates the restriction.

15. **Note:** For easier calculation consider some convenient value of x (i.e., number of workers). Let initially there were 20 workers employed.

It means work done till 25 days

$$= 25 \times 20 = 500 \text{ man-days}$$

Now, since delay in works is 60%.

It means the work was completed in 160 days. Let the increased workers worked for k days then

$$40 \times k + 16 \times (135 - k) = 75 \times 40$$

$$\Rightarrow k = 35 \text{ days}$$

\therefore 40 workers work for only 35 days

Here 40 means twice the work force of 20 and 16 means 80% efficiency of the original work-force and 135 means $(160 - 25)$ days and 75 means $(100 - 25)$ days

Since, number of days are increased by 60 in which only 16 workers work.

\therefore Remaining work after 100 days = $60 \times 16 = 960$

$$= \frac{960}{3500} \times 100 = 27 \frac{5}{7} \%$$

Solutions for 16–20: Let the actual number of typists be n required to work for D days, then

$$nD = (n \times 8) + \left(\frac{4n}{5} \times D \right)$$

$$\Rightarrow D = 40$$

16. Since, the above equation is independent of n (i.e., number of typists) so cannot be calculated. It means there are many possible values.

17. Since 20% (i.e., $\frac{1}{5}$) typists left the job. So, there can be any value which is multiple of 5 i.e., whose 20% is always an integer. Hence, 5 is the least possible value.

18. The remaining value must be divisible by 4.

Since, $\frac{4x}{5} = k$ $x \rightarrow$ actual number of typists

$\Rightarrow x = \frac{k \times 5}{4}$ $k \rightarrow$ remaining number of typists

So, k must be divisible by 4, since a person cannot be a fraction. Hence, option (c) could be the possible answer.

19. Since, $D = 40$

20. Work done in 8 days = $8x$

Work done in further 16 days = $16 \times \frac{4}{5}x = \frac{64x}{5}$

Remaining work = $40x - \left(8x + \frac{64x}{5} \right) = \frac{96x}{5}$

Remaining number of days = $40 - (8 + 16) = 16$

\therefore New work-force = $\frac{96x/5}{16} = \frac{6x}{5}$

\therefore Change (or increase) in work-force

$$= \frac{\left(\frac{6x}{5} \right) - x}{x} \times 100 = 20\%$$

21. Let A, B, C, D and E stiches a, b, c, d and e shirts per day then

$$\frac{1}{a} + \frac{1}{b} + \frac{1}{c} + \frac{1}{d} + \frac{1}{e} = \frac{90}{1800} = \frac{1}{20}$$

when $a = b = c = d = e$, we get the minimum value

$$\therefore 5 \times \frac{1}{a} = \frac{1}{20}$$

$$\Rightarrow a = 100 = b = c = d = e$$

22. $(8M + 5W) \times 6 \times 4 = (4M + 5W) \times 8 \times 5$

$$\Rightarrow 4M = 10W$$

$$\Rightarrow 1M = 2.5W$$

Now, substituting the value M by W , we get total work-done

$$\text{Work} = (8 \times 2.5 + 5) \times 6 \times 4 = 600 \text{ women-days-hours} \\ = 240 \text{ man-days-hours}$$

Again work = $5 \times 8 \times 30 = 1200$ boy-days-hours

$$\therefore 1M = 2.5W = 5B$$

$$4M + 3W + 4B = 30 \text{ boys}$$

$$\therefore \text{Required number of days} = \frac{1200}{30 \times 5} = 8 \text{ days}$$

23. $9 \times 6 \times M = 240$

$$M = \frac{240}{6 \times 9} = 4.4 \text{ men}$$

Therefore, minimum 5 men are required.

24. Efficiency of Eklaya = 16.66%

Efficiency of Faizal = 8.33%

Total efficiency of Eklaya and Faizal = 25%

So, they can do actual work in 4 days

\therefore 3 times work requires 12 days.

25. $1 + 2 + 3 + 4 + 5 + \dots + 24 = \frac{24 \times 25}{2} = 300$

Total work = 300 man-days

But, the person who started the work on the first day works for 24 days. Hence, his share will be maximum which is equal to $\frac{24}{300} = \frac{2}{25}$.

Thus, he will receive $5000 \times \frac{2}{25} = \text{Rs. } 400$.

26. Total efficiency of two persons = 50%

Ratio of efficiencies of first person to the second person = 1 : 2

Therefore, efficiency of second person = 33.33%

Hence, he will take 3 days to complete the work alone.

27. Ratio of number of men, women and children

$$= \frac{18}{6} : \frac{10}{5} : \frac{12}{3} = 3x : 2x : 4x$$

$$\therefore (3x + 2x + 4x) = 18$$

$$\therefore x = 2$$

Therefore, number of women = 4

$$\text{Share of all women} = \frac{10}{40} \times 4000 = \text{Rs. } 1000$$

($\because 18 + 10 + 12 = 40$)

$$\therefore \text{Share of each woman} = \frac{1000}{4} = \text{Rs. } 250$$

28. It can be solved easily through option.

$$(10 + 9 + 8 + \dots + 1) = 10 \times \left(10 \times \frac{55}{100}\right)$$

$$55 = 55 \quad \text{Hence correct.}$$

Alternatively: $\frac{n(n+1)}{2} = n \times \frac{55n}{100}$

$$\Rightarrow n = 10$$

In both cases total work is 55 man-days.

29. Go through option. Consider choice (c).

Efficiency of first worker = 5%

Efficiency of second worker = 4%

∴ In 7 hours first worker completed 35% work

In 5 hours second worker completed 20% work

Thus, work completed = 55%

Remaining work = 45%

Hence, one condition is satisfied.

Again, they will take 5 more hours to complete 45% work

$$\left[\frac{45}{4+5} = 5 \right]$$

Thus, first person completes $7 \times 5 + 5 \times 5 = 60\%$ work

and second person completes $5 \times 4 + 5 \times 4 = 40\%$ work

Hence, second condition is also satisfied. Hence, correct option is (c).

30. Go through option

$$140 \times 4 = (140 + 120 + 100 + \dots + 20)$$

$$560 = 560$$

Alternatively: Let n be the initial number of workers then

$$n \times 4 = n + (n - 20) + (n - 40) + \dots + (n - 120)$$

$$4n = 7n - 420$$

$$\Rightarrow 3n = 420$$

$$\Rightarrow n = 140 \text{ workers}$$

31. From the first statement

$$B \quad (V + M)$$

$$\text{Number of days} \quad x \quad = \quad x$$

$$\text{Efficiency} \quad 1 \quad : \quad 1$$

From the second statement

$$V \quad (V + M)$$

$$\text{Number of days} \rightarrow (K + 8) \quad K$$

From the third statement

$$B \quad V$$

$$\text{Number of days} \rightarrow (n - 8) \quad n$$

Now, go through option and consider option (c).

Efficiency of $(B + V + M) = 16.66\%$ (number of days = 6)

∴ Efficiency of $B = 8.33\%$ (number of days = 12)

and Efficiency of $(V + M) = 8.33\%$ (number of days = 12)

Therefore, B will take 12 days.

Now, from third statement V will take 20 days.

Hence, the efficiency of V is 5%.

Therefore, V will take 20 days. Hence, second statement is also true. Thus, the presumed option (c) is correct.

32. Consider option (d)

Time taken by Bill = 12 hours

Efficiency of Bill = 8.33%

Therefore, time taken by Bill and Milinda working together

$$= 6 \frac{2}{3} \text{ hours}$$

Hence, the efficiency of Milinda and Bill = 15%

Therefore efficiency of Milinda = $15 - 8.33 = 6.66\%$

Thus, the number of days taken by Milinda = 15, which is $8 \frac{1}{3}$ days more than when both work together.

Hence, all the conditions satisfied.

	M	$B + M$	B
Efficiency	→	6.66%	15%
Number of days	→	15	$6 \frac{2}{3}$

33. Efficiency of Pascal and Rascal = 10%

Pascal worked for 2.5 hours and Rascal worked separately 8.5 hours. Which means it can be considered that Pascal and Rascal worked together for 2.5 hours and Rascal worked alone for 6 hours.

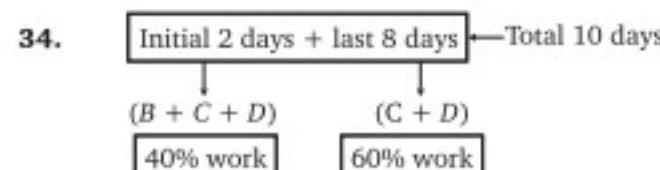
Thus, Pascal and Rascal in 2.5 hours can complete 25% work. It means the remaining $(50 - 25) = 25\%$ of the work was done by Rascal in 6 hours.

Therefore, Rascal can do 100% work in 24 hours. It means the efficiency of Rascal = 4.16%.

Therefore, efficiency of Pascal = $(10 - 4.16) = 5.83\%$

Thus, Pascal require $\frac{100}{5.83} = 17 \frac{1}{7}$ hours to complete the work alone.

Alternatively: Go through option.



From the above diagram it is clear that efficiency of C and D is 7.5%, since C and D complete 60% work in 8 days and efficiency of B , C and D is 20%. It means efficiency of B alone is $12.5\% = (20 - 7.5)$.

Now

$$C : D$$

$$\text{Number of days} \quad 4x : 5x$$

$$\text{Efficiency} \quad 5y : 4y$$

$$\therefore \text{Efficiency of } C = \frac{5}{9} \times 7.5 = 4.16\%$$

$$\text{and} \quad \text{Efficiency of } D = \frac{4}{9} \times 7.5 = 3.33\%$$

Thus, D is the least efficient person.

Now share of work done by David

$$(D) = 3.33\% \times 10 = 33.33\%$$

Hence, his share of amount = 33.33% of Rs. 3000 = Rs. 1000

35. Combined efficiency of all the three boats = 60 passenger/trip
Now, consider option (a).

15 trips and 150 passengers means efficiency of $B_1 = 10 \frac{p}{t}$

which means in carrying 50 passengers B_1 must have taken 5 trips. So the rest trips equal to $5 (10 - 5 = 5)$ in which B_2 and B_3 together carried remaining 250 (300 - 50) passengers.

Therefore the efficiency of B_2 and B_3 = $\frac{250}{5} = 50 \frac{P}{t}$

Since, the combined efficiency of B_1 , B_2 and B_3 is 60. Which is same as given in the first statement hence option (a) is correct.

Alternatively: It can be solved by framing quadratic equation.

36. Efficiency of 3 men + 5 women = 33.33%

Required number of days by 2 men = x

\therefore Required number of days by 3 women = $x + 5$

Now, consider option (c).

Therefore, $3M + 5W = 3M + 2M = 5$ men

Therefore, efficiency of a man = 6.66%

Hence, a man needs 15 days to finish the job, working alone.

Again $3M + 5W = 7.5W + 5W = 12.5W$

Therefore, efficiency of a woman = 2.66%

Therefore, a woman needs 37.5 days.

Thus, 2 men needs 7.5 days to work alone $\therefore \left(7.5 = \frac{15}{2}\right)$

and 3 women needs 12.5 days to work alone $\therefore \left(12.5 = \frac{37.5}{3}\right)$

Hence, the difference in number of days = 5 which is same as given in the problem. Hence correct option is (c).

37. Efficiency of Henry and Ford (combined) = 10%

Consider option (d).

Efficiency of Ford = 3.33% (30 days)

Therefore, Efficiency of Henry = 6.66%

Now, the new efficiency of Ford = 16.66%

and the new efficiency of Henry = 3.33%

Therefore, newly combined efficiency of H and F = 20%

Therefore, required number of days by Henry and Ford working together = 5

Since 5 is half of 10, hence the option (d) is correct.

38. **From the last statement:**

Efficiency of Anne (A), Benne (B) and Cenne (C) = 50%

From the first statement: Number of days taken by B is 2 more than C.

From the second statement: Anne had worked for 6 days and Benne had worked for 3 days only. Now, consider option (d).

Number of days taken by B = 6,

Efficiency = 16.66%

It means Benne had completed $16.66 \times 3 = 50\%$ work in 3 days.

Therefore Anne had completed 50% work in 6 days.

Thus, the efficiency of Anne = $8.33\% \left(\frac{50}{6} \right)$

Hence, the efficiency of Cenne = $50 - (16.66 + 8.33) = 25\%$

Thus B takes 6 days (\because efficiency = 16.66%)

and C takes 4 days (\because efficiency = 25%)

which is true according to the first statement, hence option (d) is correct.

39. Number of pages typed by A, B and C together per day = 45
Now let the number of pages typed by B is x
then the number of pages typed by A = $x - d$
and the number of pages typed by C = $x + d$
 $\Rightarrow (x - d) + (x) + (x + d) = 45$
 $\Rightarrow x = 15$ pages per day.

Again let C types k pages per day then A types $\frac{k}{4}$ pages per day.

Therefore, the ratio of typing of pages per day of A and C = 1 : 4

\therefore Number of pages typed by C in one day

$$= \frac{4}{5} \times 30 = 24 \text{ pages} \quad (30 = 45 - 15)$$

\therefore Number of pages typed by C per hour = $\frac{24}{8} = 3$ pages/hour

40. Efficiency of P = 5%

Efficiency of Q = 4%

Efficiency of R = 2.5%

Efficiency of S = 2%

Till 10 am pipe P filled 20%
Till 10 am pipe Q filled 8%
Till 10 am pipe R filled 2.5% $\left. \right\} 30.5\%$

Thus, at 10 am pipe P, Q and R filled 30.5% of the cistern.
Now, the time taken by P, Q, R and S together to fill the remaining capacity of the cistern

$$= \frac{69.5}{13.5} = \frac{139}{27} = 5 \text{ hours and 9 minutes (approx)}$$

Therefore, total time = 4 hours + 5 hours 9 minutes
= 9 hours and 9 minutes

It means cistern will be filled up at 3 : 09 pm

41. Efficiency of P + Q = 9% (inlet pipes)

Efficiency of R + S = 4.5% (outlet pipes)

Net efficiency = 4.5%

So, the time taken = $\frac{100}{4.5} = 22 \frac{2}{9}$ hours

42. Efficiency of A = 10%

Efficiency of B = 6.66%

Efficiency of C = 5%

Efficiency of D = 3.33%

Efficiency of A + B + C + D = 8.33 (time = 12 hours)

Now, go through options and consider A and B as inlet pipes and C and D as outlet pipes, then

$$(10 + 6.66) - (5 + 3.33) = 8.33$$

which is required hence it is certain that C and D are outlet pipes.

NOTE There is no any other such combination.

43. Efficiency of inlet pipe A = 4.16%

$$\left(\frac{100}{24} \right)$$

Efficiency of inlet pipe B = 5.83%

$$\left(\frac{100}{120/7} \right)$$

∴ Efficiency of A and B together = 10% ∴ (time = 10 hours)

Now, if the efficiency of outlet pipe be $x\%$ then in 10 hours the capacity of tank which will be filled = $10 \times (10 - x)$

Now, since this amount of water is being emptied by C at $x\%$ per hour, then

$$\frac{10 \times (10 - x)}{x} = 2.5 \text{ hours} \Rightarrow x = 8\%$$

Therefore in 10 hours 20% tank is filled only. Hence, the remaining 80% of the capacity will be filled by pipes A and B in $\frac{80}{10} = 8$ hours.

44. Efficiency of pipe A = 8.33%

Efficiency of pipe B = 6.67%

Efficiency of pipe C = 5%

When tap C was opened pipe A filled 16.66% capacity

When tap C was opened pipe B filled 6.67% capacity

Therefore rest capacity of the tank to be filled

$$= 100 - 23.34 = 76.66\%$$

Now, the net efficiency of A , B and C = 10%

Hence, pipes A , B and C will take = $\frac{76.66}{10} = 7.66 = 7 \frac{2}{3}$ hours

$$\therefore \text{Total time} = 2 \text{ hours} + 7 \frac{2}{3} \text{ hours} = 9 \frac{2}{3} \text{ hours}$$

45. Efficiency of inlet pipe = 50%

Efficiency of outlet pipe = 16.66%

Net efficiency of pipes A and B = 33.33%

Capacity of tank to be filled up = 66.66%

$$\text{Hence, required time} = \frac{66.66}{33.33} = 2 \text{ hours}$$

46. Rate of leakage = 8.33% per hour

$$\text{Net efficiency} = 50 - (16.66 + 8.33) = 25\%$$

$$\text{Time required} = \frac{100}{25} = 4 \text{ hours}$$

47. Since, an inlet pipe is 7.2 times efficient than an outlet pipe. Therefore, in order to tank never overflow we will need total 8 outlet pipes.

Thus we need only 7 more ($8 - 1 = 7$) outlet pipes.

48. Time taken by 8th tap = $2 \times 2 \times 2 = 8$ hours

$$\text{and time taken by 12th tap} = 2 \times \frac{1}{2} \times \frac{1}{2} = \frac{1}{2} \text{ hour}$$

$$\text{Ratio of time taken by 8th tap and 12th tap} = 8 : \frac{1}{2} = 16 : 1$$

∴ Ratio of efficiencies of 8th tap and 12th tap = 1 : 16

49. Time taken by 10th tap = $80 \times \frac{1}{2} \times \frac{1}{2} = 20$ hours

$$\text{Time taken by 12th tap} = 80 \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} = 5 \text{ hours}$$

Thus 10th tap and 12th tap together will take 4 hours.

50. Let pipe A fill the tank in $3x$ hours then pipe B fill it in $4x$ hours.

$$\text{Therefore, in 1 hour they will fill} = \frac{1}{3x} + \frac{1}{4x} = \frac{7}{12x}$$

i.e., they will take $\frac{12x}{7}$ hours

When an inlet pipe C is also opened then it takes

$$\begin{aligned} &= \frac{12x}{7} + \frac{12x}{7} \times \frac{3}{4} \\ &= \frac{12x}{7} \left(\frac{7}{4} \right) = 3x \text{ hours} \end{aligned}$$

Now, in one hour pipe A , B and C working together fill

$$\begin{aligned} &= \frac{1}{3x} + \frac{1}{4x} - \frac{1}{C} = \frac{1}{3x} \\ \Rightarrow & \frac{7}{12x} - \frac{1}{C} = \frac{1}{3x} \\ \Rightarrow & \frac{1}{C} = \left(\frac{1}{12x} - \frac{1}{3x} \right) \\ \Rightarrow & C = 4x \end{aligned}$$

Hence in $4x$ hours pipe C can empty the whole tank.

Now, since $3x = 33 \Rightarrow x = 11$

$$\therefore 4x = 4 \times 11 = 44 \text{ hours}$$

51. Total work = $5 \times 20 = 100$ man-days.

Let the client needed to complete it in n days then

$$(5 \times 2) + (10 \times 2) + (15 \times 2) + (20 \times 2) = 100$$

Hence, in 8 days all the work will be completed as per the requirement of client.

And on the 8th day 20 men were working.

52. It requires total 8 days by adding the work force successively.

53. Total work = $100 + 50 = 150$ man-days

In 8 days 100 man-days work has been completed. Now on 9th and 10th day there will be 25 workers. So in 2 days they will complete additional 50 man-days work. Thus the work requires 2 more days.

54. Let there be ' n ' inlet pipes then there must be $(8 - n)$ outlet pipes.

$$\text{Therefore } (8 - n) \frac{1}{6} - n \times \frac{1}{8} = \frac{1}{6} \Rightarrow n = 4$$

$$\text{Alternatively: } (8 - n) 16.66 - n \times 12.5 = 16.66$$

$$\Rightarrow n = \frac{116.66}{29.16} = \frac{700}{175} = 4$$

Alternatively: It can be solved through options very easily.

55. Efficiency of two inlet pipes A and B = $8.33 + 6.66 = 15\%$

Efficiency of two inlet pipes A and B along with an outlet pipe

$$C = 8.33 + 6.66 - 12.5 = 2.5\%$$

Hours	1	2	3	4	5	6	7	8	9	10
Efficiency →	15	15	2.5	15	15	2.5	15	15	2.5	
				32.5		32.5		32.5		2.5%

In 9 hours 97.5% tank will be completely filled. On the 10th hour 2.5% (remaining capacity) will be filled by pipe A , B with its 15% efficiency.

$$\text{Thus, } A \text{ will take} = \frac{2.5}{15} = \frac{1}{6} \text{ hour} = 10 \text{ minutes}$$

Therefore, total time = 9 hours and 10 minutes.



7

CI/SI/INSTALMENTS

The concept of simple interest and compound interest is one of those concepts which are widely used in Business and Banking etc. Questions are rarely asked in CAT from this chapter, but it is important for the purpose of Data interpretation. Since the questions based on the concept of 'interest' are rather easy so it is common that MAT, FMS, CET etc. asked enough questions from this chapter. The questions of this chapter are so easy that 95% questions can be solved orally or using unitary methods *i.e.*, sometimes you don't need to apply the given formula and I think that is essential.

Simple interest is nothing but the fix percentage of the principal (invested/borrowed amount of money)

Some key words used in the concept of interest.

Principal :(P) It is the sum of money deposited/loaned etc. also known as **capital**.

Interest : It is the money paid by borrower, calculated on the basis of **Principal**.

Time (T/n) : This is the duration for which money is lent/borrowed.

Rate of Interest (r/R) : It is the rate at which the interest is charged on principal.

Amount (A) = Principal + Interest

Simple Interest : When the interest is calculated uniformly only on the principal for the given time period.

Compound Interest : In this case for every next period of time the interest is charged on the total previous amount (which is the sum of principal and interest charged on it so far.) *i.e.*, every time we calculate successive increase in the previous amount.

IMPORTANT FORMULAE

Simple Interest (SI)

$$SI = \frac{P \times r \times t}{100}$$

P = Principal

r = rate of interest (in %)

t = time period (yearly, half yearly etc.)

$$\text{Amount } (A) = P + \frac{Prt}{100} = P \left(1 + \frac{rt}{100}\right)$$

NOTE Out of the five variables A , SI , P , r , t we can find any one of these, if we have the requisite information.

CONVERSION OF TIME PERIOD-RATE OF INTEREST

Given ($r\%$)	Given (t)	Required ($r\%$)	Required (t)
$r\%$ annual	t years	$\frac{r}{2}\%$ half-yearly	$2t$
$r\%$ annual	t years	$\frac{r}{4}\%$ quarterly	$4t$
$r\%$ annual	t years	$\frac{r}{12}\%$ monthly	$12t$

Compound Interest (CI)

1. $CI = A - P$ [A is the amount including interest and principal (P) both]

$$\text{2. Amount } (A) = P \left(1 + \frac{r}{100}\right)^t$$

3. When rate of interest is half-yearly

$$A = P \left(1 + \frac{(r/2)}{100}\right)^{2t}$$

4. When the rate of interest is quarterly

$$A = P \left(1 + \frac{r/4}{100}\right)^{4t}$$

Difference between CI and SI for two years

$$(\text{also in second year}) = P \left(\frac{r}{100}\right)^2$$

Difference between CI and SI for three years

$$= P \left(\frac{r}{100}\right)^2 \left(\frac{r}{100} + 3\right)$$

Depreciation : It is known that the prices of some articles depreciates in their values over a time period. When the value in terms of currency decreases, we say that the value of the article is depreciating.

$$V_f = V_i \left(1 - \frac{r}{100}\right)^t$$

V_i = initial value of the article

V_f = final (depreciated) value of article

r , is the rate of interest by which the price of article decreases over the time period 't'.

Population : It has been observed that the population of a particular locality/nation etc. increases or decreases successively over its previous value i.e., it increases or decreases as compound interest for the money. Thus we use similar formulae for the calculation of population.

$$(\text{Total population}) P = P_0 \left(1 + \frac{r}{100}\right)^n,$$

when population increases

$$(\text{Total population}) P = P_0 \left(1 - \frac{r}{100}\right)^n,$$

when population decreases.

Instalments : When a borrower paid the sum in parts (i.e., not in a single amount) then we say that he/she is paying in instalments. For example A borrowed Rs. 100 from B and he pays back it to B in several parts i.e., Rs. 20 in 5 times or Rs. 50 in 2 times etc. But the important point is that borrower has to also pay the interest for using the borrowed sum/or purchased article. In general the value of each instalment is kept constant even when the interest charged on each instalment vary for each instalment.

For Simple Interest

$$A = \left[x + \left(x + \frac{x \times r \times 1}{100} \right) + \left(x + \frac{x \times r \times 2}{100} \right) + \left(x + \frac{x \times r \times 3}{100} \right) + \dots \right]$$

A = Total amount paid

x = Value of each instalment

EXAMPLE 1. Find the simple interest on Rs. 1000 at 12% per annum for 5 years.

SOLUTION $SI = \frac{Prt}{100} = \frac{1000 \times 12 \times 5}{100} = \text{Rs. 600}$

{Total amount = $P + SI = 1000 + 600 = \text{Rs. 1600}$ }

EXAMPLE 2. Find the simple interest on Rs. 800 at 7% per annum and on Rs. 700 at 16% p.a. and on Rs. 500 at 4% p.a. for 2 years.

SOLUTION $SI = \frac{P_1 r_1 t_1}{100} + \frac{P_2 r_2 t_2}{100} + \frac{P_3 r_3 t_3}{100}$

$$= \frac{800 \times 7 \times 2}{100} + \frac{700 \times 16 \times 2}{100} + \frac{500 \times 4 \times 2}{100}$$

$$= 112 + 224 + 40$$

$$= \text{Rs. 376}$$

EXAMPLE 3. A sum of money (P) doubles in 10 years. In how many years it will be treble at the same rate of simple interest?

Also,

$$A = P + \frac{P \times n \times r}{100}$$

P is the principal

n is the number of instalments

r is the rate of interest

For Compound Interest

(loan amount)

$$P = \left[\frac{x}{\left(1 + \frac{r}{100}\right)} + \frac{x}{\left(1 + \frac{r}{100}\right)^2} + \frac{x}{\left(1 + \frac{r}{100}\right)^3} + \dots + \frac{x}{\left(1 + \frac{r}{100}\right)^n} \right]$$

$x \rightarrow x$ is the value of each instalment.

$$\text{Total amount paid in instalments } (A) = P \left(1 + \frac{r}{100}\right)^n$$

n is the number of instalments.

Difference between CI and SI for n^{th} year

$$= \frac{Pr}{100} \left[\left(1 + \frac{r}{100}\right)^{n-1} - 1 \right]$$

For Compound Interest

$$\frac{\text{increase in amount in } n^{\text{th}} \text{ year}}{\text{increase in amount in } (n+1)^{\text{th}} \text{ year}} = \frac{100}{(100+r)}$$

Similarly,

$$\frac{\text{decrease in amount in } n^{\text{th}} \text{ year}}{\text{decrease in amount in } (n+1)^{\text{th}} \text{ year}} = \frac{100}{(100-r)}$$

where r is rate of interest.

SOLUTION

$$A = 2P$$

$$SI = P$$

$$(SI = 2P - P)$$

$$P = \frac{P \times r \times 10}{100}$$

$$\Rightarrow r = 10\%$$

So, the new amount = $3P$

But the new $SI = 2P = (3P - P)$

$$2P = \frac{P \times 10 \times t}{100}$$

$$t = 20 \text{ years}$$

$$(r = 10\%)$$

EXAMPLE 4. A sum of money in 3 years becomes 1344 and in 7 years it becomes Rs. 1536. What is the principal sum where simple rate of interest is to be charged?

- (a) 4000 (b) 1500 (c) 1200 (d) 2800

SOLUTION It would be very time saving if we do it by unitary method.

$$1536 - 1344 = \text{Rs. 192}$$

EXAMPLE 14. Jadeja purchased a maruti car 3 years ago for Rs. 2 lakh. Its value depreciated each year @ 25% p.a. What is the present value of the car ?

SOLUTION $200000 \left(1 - \frac{25}{100}\right)^3 = 200000 \times \left(\frac{3}{4}\right)^3$

EXAMPLE 15. The difference between CI and SI for 3 years @ 20% p.a. is Rs. 152. What is the principal lent in each case ?

SOLUTION Difference between CI and SI for 3 years = Rs. 152

$$P \left(\frac{r}{100} \right)^2 \left(\frac{r}{100} + 3 \right) = 152$$

$$P \left(\frac{1}{25} \right) \left(\frac{16}{5} \right) = 152$$

$$P = \frac{152 \times 25 \times 5}{16}$$

$$P = 9.5 \times 25 \times 5 = 1187.5$$

EXAMPLE 16. A sum is being lent at 20% p.a. compound interest. What is the ratio of increase in amount of 4th year to 5th year?

SOLUTION
$$\frac{P \left(1 + \frac{r}{100}\right)^4}{P \left(1 + \frac{r}{100}\right)^5} = \frac{1}{\left(1 + \frac{r}{100}\right)}$$

EXAMPLE 17. Rs. 12000 amounts to Rs. 20736 in 3 years at $r\%$ p.a. of compound interest. What is the value of r ?

- (a) 10% (b) 25% (c) 12% (d) 20%

$$\begin{aligned}
 \text{SOLUTION} \quad A &= P \left(1 + \frac{r}{100}\right)^3 \\
 20736 &= 12000 \left(1 + \frac{r}{100}\right)^3 \\
 \Rightarrow \quad \frac{20736}{12000} &= \left(1 + \frac{r}{100}\right)^3 \\
 \Rightarrow \quad \frac{1728}{1000} &= \left(1 + \frac{r}{100}\right)^3 \\
 \Rightarrow \quad \left(\frac{12}{10}\right)^3 &= \left(1 + \frac{r}{100}\right)^3 \\
 \Rightarrow \quad \left(1 + \frac{2}{10}\right)^3 &= \left(1 + \frac{r}{100}\right)^3 \\
 \Rightarrow \quad r &= 20\%
 \end{aligned}$$

Alternatively : The best way for this problem is to go through options.

$$12000 \times 1.2 \Rightarrow 14400 \times 1.2 \Rightarrow 17280 \times 1.2 \Rightarrow 20736$$

EXAMPLE 18. A certain sum amounts to Rs. 14641 in 4 years @ 10% p.a. compounded annually. What is the value of principal?

$$\begin{aligned}
 \text{SOLUTION} \quad 14641 &= P \left(1 + \frac{10}{100}\right) \\
 14641 &= P \left(\frac{11}{10}\right)^4 \\
 P &= 14641 \times \left(\frac{10}{11}\right)^4 \\
 &= 10000
 \end{aligned}$$

EXAMPLE 19. A sum of Rs. 10000 is borrowed at 8% p.a. compounded annually which is paid back in 3 equal annual instalments. What is the amount of each instalments?

$$\begin{aligned}
 \text{SOLUTION} \quad 10000 &= x \left[\frac{25}{27} + \left(\frac{25}{27} \right)^2 + \left(\frac{25}{27} \right)^3 \right] \\
 &= x \times \frac{25}{27} \left[1 + \frac{25}{27} + \frac{625}{729} \right] \\
 &= \frac{25x}{27} \left[\frac{2029}{729} \right] \\
 \Rightarrow x &= \text{Rs. } 3880.335
 \end{aligned}$$

Alternatively:

$$10000 (1.08)^3 = x [1 + (1.08) + (1.08)^2]$$

EXAMPLE 20. A scooty is sold by an automobile agency for Rs. 19200 cash or for Rs. 4800 cash down payment together with five equal monthly instalments. If the rate of interest charged by the company is 12% per annum find each instalment.

SOLUTION Balance of the price to be paid through instalments

= Rs. 14400

Rate of interest (r) = 12% p.a.

$$\therefore \left(14400 + \frac{14400 \times 12 \times 5}{100 \times 12} \right) = \left[x + \left(x + \frac{12x}{1200} \right) \right. \\ \left. + \left(x + \frac{12x \times 2}{12 \times 100} \right) + \dots + \left(x + \frac{12x \times 4}{12 \times 100} \right) \right]$$

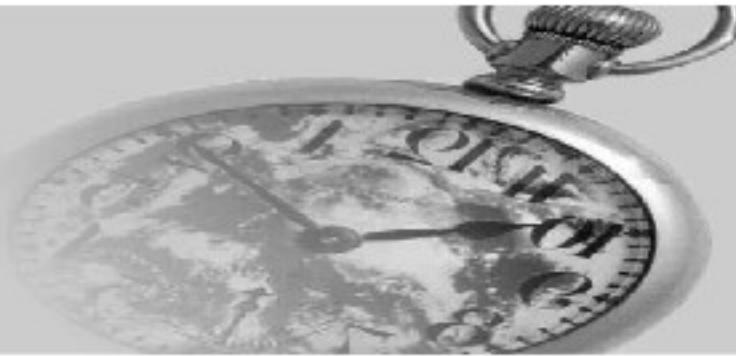
$\Rightarrow x = \text{Rs. } 2964.70$, where x is the value of each instalment.

NOTE In the left hand side and right hand side given amounts are equal. Each amount is equal to the total amount payable after 5 months.

Important : For quick and smooth calculation to the problems of this chapter you can remember the following values :

Rate of Interest	For Rs. 100, amount				
	after one year	after 2 years	after 3 years	after 4 years	after 5 years
5%	105	110.25	115.7625	121.550625	127.62815625
6%	106	112.36	119.1016	126.247696	133.82255776
8%	108	116.64	125.9712	136.048896	146.93280768
10%	110	121.00	133.1000	146.4100	161.051
12%	112	125.44	140.4928	157.351936	176.23416832
15%	115	132.25	152.0875	174.900625	201.13571875
20%	120	144.00	172.80	207.36	248.832
25%	125	156.25	195.3125	244.140625	305.17578125
30%	130	169.00	219.70	285.61	371.293
50%	150	225.00	337.50	506.25	759.375

EXERCISE



LEVEL (1)

19. Find the amount of Rs. 2500 invested at 12% during the period from 4th February, 2005 to 18 April 2005 :
 (a) Rs. 3000 (b) Rs. 3800
 (c) Rs. 2560 (d) Rs. 2600

20. Find the amount of Rs. 1700 invested at 16% half yearly at simple interest for one year :
 (a) 2100 (b) 2244
 (c) 2200 (d) 2500

21. The compound interest on Rs. 1000 at 10% p.a. in 3 years is :
 (a) 331 (b) 1331
 (c) 133 (d) 300

22. The compound interest on Rs. 10000 at 20% p.a. in 4 years :
 (a) 10736 (b) 736
 (c) 20736 (d) 7280

23. The compound interest on Rs. 4000 at 25% p.a. in 3 years :
 (a) 1235 (b) 5625
 (c) 3812.5 (d) 3750.5

24. The compound interest on Rs. 5000 at 30% per annum for 4 years :
 (a) 4280.5 (b) 6700
 (c) 9280.5 (d) 3857.5

25. A sum of Rs. 400 would become Rs. 441 after 2 years at $r\%$ compound interest, find the value of ' r ' :
 (a) 10% (b) 5%
 (c) 15% (d) 20%

26. At compound interest, if a certain sum of money doubles in n years, then the amount will be four fold in :
 (a) n^2 years (b) $2n^2$ years
 (c) $2n$ years (d) $4n$ years

27. Rs. 6000 amounts to Rs. 7986 in 3 years at CI. The rate of interest is :
 (a) 20% (b) 10%
 (c) 6% (d) 7.5%

28. The least number of complete years in which a sum of money put at 20% CI will be more than doubled is :
 (a) 4 (b) 5
 (c) 6 (d) 8

29. The CI on Rs. 5000 for 3 years at 8% for first year, 10% for second year and 12% for third year will be :
 (a) Rs. 1750 (b) Rs. 1652.80
 (c) Rs. 1575 (d) Rs. 1685.20

30. A sum of Rs. 2400 deposited at CI, doubled after 5 years. After 20 years it will become :
 (a) Rs. 24000 (b) Rs. 38400
 (c) Rs. 19200 (d) can't be determine

31. A sum of Rs. 550 was taken as a loan. This is to be paid back in two equal annual instalments. If the rate of interest be 20% compounded annually, then the value of each instalments is :
 (a) 300 (b) 360
 (c) 250 (d) none of these

32. The difference between CI and SI on a sum of money lent for 2 years at 10% is Rs. 40. The sum is :
 (a) 1600 (b)
 (c) 4000 (d) none of these

33. The difference between simple and compound interest on Rs. 6000 for 1 year at 20% per annum reckoned half yearly is :
 (a) 120 (b) 60
 (c) 180 (d) 72

34. A certain sum amounts to Rs. 8988.8 in two years and to Rs. 9528.128 in three years, at compound interest per annum. What is the principal and rate of interest?
 (a) Rs. 12,000, 5% (b) Rs. 6,000, 8%
 (c) Rs. 8,000, 6% (d) Rs. 10,000, 8.5%

35. The compound interest and the simple interest for two years on a certain sum of money at a certain rate of interest are Rs. 2257.58, Rs. 2100 respectively. Find the principal and rate percent :
 (a) 6000, 7% (b) 7500, 8%
 (c) 14000, 10% (d) 7000, 15%

36. The compound interest on a certain sum at a certain rate of interest for the second year and third year is Rs. 21780 and Rs. 23958 respectively. What is the rate of interest?
 (a) 6% (b) 12%
 (c) 10% (d) 15%

37. Amit borrowed Rs. 800 at 10% rate of interest. He repaid Rs. 400 at the end of first year. What is the amount required to pay at the end of second year to discharge his loan which was calculated at compound interest?
 (a) 420 (b) 440
 (c) 450 (d) 528

38. A sonata watch is sold for Rs. 440 cash or for Rs. 200 cash down payment together with Rs. 244 to be paid after one month. Find the rate of interest charged in the instalment scheme :
 (a) 10% (b) 15%
 (c) 20% (d) 25%

39. A cellphone is available for Rs. 600 or for 300 cash down payment together with Rs. 360 to be paid after two months. Find the rate of interest charged under this scheme :
 (a) 20% (b) 50%
 (c) 120% (d) none of these

40. Abhinav purchases a track suit for Rs. 2400 cash or for Rs. 1000 cash down payments and two monthly instalments of Rs. 800 each. Find the rate of interest :
 (a) 75% (b) 120%
 (c) 50% (d) none of these

41. Indicom cell-phone is available for Rs. 2500 cash or Rs. 520 cash down payments followed by 4 equal monthly instalments. If the rate of interest charged is 25% per annum, calculate the monthly instalment :
 (a) 520 (b) 480
 (c) 550 (d) none of these

42. An article is sold for Rs. 500 cash or for Rs. 150 cash down payments followed by 5 equal monthly instalments. If the rate of interest charged is 18% p.a., compute the monthly instalment :
 (a) 63.07% (b) 37.06%
 (c) 75.0% (d) 73.06%

43. A sum of Rs. 390200 is to be paid back in three equal annual instalments. How much is each instalment, if the rate of interest charged is 4% per annum compounded annually?
 (a) Rs. 140608 (b) Rs. 120560
 (c) Rs. 10000 (d) Rs. 18000

44. Purnima borrowed a sum of money and returned it in three equal quarterly instalments of Rs. 17576 each. Find the sum borrowed, if the rate of interest charged was 16% per annum compounded quarterly. Find also the total interest charged :
 (a) 46900 and 4700 (b) 48775 and 3953
 (c) 68320 and 1200 (d) none of these

LEVEL (2)

- (a) 12.5% (b) 18%
(c) 20% (d) 16.66%
8. A bicycle can be purchased on cash payment of Rs. 1500. The same bicycle can also be purchased at the down payment (initial payment, at the time of purchasing) of Rs. 350 and rest can be paid in 3 equal installments of Rs. 400 for next 3 months. The rate of SI per annum charged by the dealer is :
(a) $23\frac{9}{17}\%$ (b) $17\frac{9}{23}\%$
(c) $13\frac{9}{17}\%$ (d) none of these
9. Data Ram lends equal sum of money at the same rate of interest to A and B. The money lends to A becomes twice of the original amount in just four years at simple interest. While Data Ram lends to B for the first two years at compound interest and for the rest two years at simple interest. If the difference between the amount of A and B after 4 years is Rs. 2750. What is the amount of money that Data Ram lends to each one?
(a) Rs. 40000 (b) Rs. 6000
(c) Rs. 8000 (d) Rs. 80000
10. Akram Ali left an amount of Rs. 340000 to be divided between his two sons aged 10 years and 12 years such that both of them would get an equal amount when each attain 18 years age. What is the share of elder brother if the whole amount was invested at 10% simple interest :
(a) 12000 (b) 16000
(c) 160000 (d) 180000
11. Satyam took loan from IDIDI Bank for his 2 years course of MBA at IMD. He took the loan of Rs. 6 lakh such that he would be charged at 8% per annum at CI during his course and at 10% CI after the completion of course. He returned half of the amount which he had to be paid on the completion of his studies and remaining after 2 years. What is the total amount returned by Satyam ?
(a) Rs. 7.73323 lakh (b) Rs. 7.58 lakh
(c) Rs. 7.336 lakh (d) none of these
12. We had 1000 goats at the beginning of year 2001 and the no. of goats each year increases by 10% by giving birth (compounded annually). At the end of each year we double the no. of goats by purchasing the same no. of goats as there is the no. of goats with us at the time. What is the no. of goats at the beginning of 2004?
(a) 10600 (b) 10648
(c) 8848 (d) 8226
13. Rs. 100000 was invested by Mohan in a fixed deposit @ 10% per annum at CI. However every year he has to pay 20% tax on the compound interest. How much money does Mohan has after 3 year?
(a) 128414 (b) 108000
(c) 126079.2 (d) none of these
14. A property dealer bought a rectangular plot (of land) in Noida 5 years ago at the rate of Rs. 1000 per m^2 . The cost of plot is increases by 5% in every 6 years and the worth of a rupee falls down at a rate of 2% in every 5 years. What is the approximate value of the land per meter 2 25 years hence?
(a) Rs. 995 (b) Rs. 1134
(c) Rs. 1500 (d) Rs. 1495
15. A and B run a joint venture in which the profit earned by A and B are in the ratio 28 : 15. A invest his share at the start of the year and B joins in after 9 months of the same year. What is the ratio of their initial investment respectively?
(a) 7 : 15 (b) 8 : 13
(c) 5 : 17 (d) 15 : 7
16. In the previous problem if A gets a profit of Rs. 4200 the amount invested by B is :
(a) 2250 (b) 2600
(c) 1350 (d) can't be determined
17. Arvind and Govind each invested Rs. 15000 for 3 years at the same rate of interest but Arvind's investment is compounded annually while Govind's investment is charged on simple interest. What amount did Arvind receive more than Govind?
(a) Rs. 680 (b) Rs. 3450
(c) data insufficient (d) none of these
18. Shyam Lal takes a loan of Rs. 10500 at 10% p.a. compounded annually which is to be repaid in two equal annual instalments. One at the end of one year and the other at the end of the second year. The value of each instalments is :
(a) 5987 (b) 6050
(c) 6352.5 (d) 5678.5
19. Hari Lal and Hari Prasad have equal amounts. Hari Lal invested all his amount at 10% compounded annually for 2 years and Hari Prasad invested $1/4$ at 10% compound interest (annually) and rest at $r\%$ per annum at simple interest for the same 2 years period. The amount received by both at the end of 2 year is same. What is the value of r ?
(a) 14% (b) 12.5%
(c) 10.5% (d) 11%
20. The annual sales of a company in the year 2000 was Rs. 1000 and in the year 2005 was Rs. 2490. Find the compounded annual growth rate (CAGR) of sales in the given period of the same company :
(a) 14.289% (b) 10%
(c) 15% (d) 20%
21. HDFC lends 1 million to HUDCO at 10% simple interest p.a. for 2 years and HUDCO lends the same amount to SAHARA STATES HOUSING corporation at 10% p.a. of compound interest for 2 years. What is the earning of HUDCO in this way?
(a) Rs. 133100 (b) Rs. 33100
(c) Rs. 131000 (d) no profit no loss
22. ICICI lent Rs. 1 lakh to captain Ram Singh @ 6% per annum of simple interest for 10 years period. Meanwhile ICICI offered a discount in rate of interest for armed forces. Thus the rate of interest ICICI decreased to 4%. In this way Ram Singh had to pay total amount 1.48 lakh.
After how many year Ram Singh got the discount in rate of interest?
(a) 3 years (b) 4 years
(c) 6 years (d) 5 years
23. Sanjay purchased a hotel worth Rs. 10 lakh and barkha purchased a car worth Rs. 16 lakh. The value of hotel every year increases by 20% of the previous value and the value of car every year depreciates by 25%. What is the difference between the price of hotel and car after 3 years?
(a) Rs. 925000 (b) Rs. 10,53,000
(c) remains constant (d) can't be determined



Answers

LEVEL-1

1. (d)	2. (b)	3. (c)	4. (d)	5. (c)	6. (b)	7. (b)	8. (b)	9. (b)	10. (c)
11. (c)	12. (d)	13. (d)	14. (c)	15. (c)	16. (c)	17. (b)	18. (b)	19. (c)	20. (b)
21. (a)	22. (a)	23. (c)	24. (c)	25. (b)	26. (c)	27. (b)	28. (a)	29. (b)	30. (b)
31. (b)	32. (c)	33. (b)	34. (c)	35. (d)	36. (c)	37. (d)	38. (c)	39. (c)	40. (b)
41. (a)	42. (d)	43. (a)	44. (b)	45. (c)	46. (b)	47. (d)	48. (b)	49. (b)	50. (b)
51. (b)	52. (b)	53. (b)	54. (c)	55. (c)	56. (d)				

LEVEL-2

1. (b)	2. (a)	3. (d)	4. (b)	5. (d)	6. (c)	7. (c)	8. (d)	9. (c)	10. (d)
11. (a)	12. (b)	13. (d)	14. (b)	15. (a)	16. (d)	17. (c)	18. (b)	19. (c)	20. (a)
21. (c)	22. (b)	23. (b)							



Hints & Solutions

LEVEL 1

1. $4000 + (4000 \times 5 \times 0.15) = \text{Rs. } 7000$

2. $(12000 - 8000) = \frac{8000 \times t \times 20}{100}$

$$\Rightarrow t = \frac{5}{2} \text{ years}$$

3. $1960 = \frac{14000 \times r \times 2}{100} \Rightarrow r = 7\%$

4. $6300 = \frac{P \times 7 \times 15}{100 \times 2}$

$\Rightarrow P = \text{Rs. } 12000$

5. $6000 = \frac{P \times 12 \times 1}{100}$

$\Rightarrow P = 50000$

6. In my opinion this question should be solved by unitary method instead of making complex solution

Years	Rate of Interest	Interest
2	4%	112
2	1%	28
1	1%	14

It means the principal sum is Rs. 1400

Alternatively: $\frac{P}{100} \times 2[(r + 4) - r] = 112$

$\Rightarrow P = 1400$

7. $SI = 2P - P = P$ (Interest = Amount - Principal)

$$P = \frac{P \times 20 \times t}{100} \Rightarrow t = 5 \text{ years}$$

8. $P = \frac{P \times r \times 20}{100}$ (Interest = Amount - Principal)

$\Rightarrow r = 5\% \text{ p.a.}$

9. $2P = \frac{P \times 15 \times r}{100}$ $(2P = 3P - P)$

$$r = \frac{40}{3}\% \text{ p.a.}$$

10. $P = \frac{P \times r \times 12}{100} \Rightarrow r = \frac{100}{12}\% \text{ p.a.}$

Now, $2P = \frac{P \times 100 \times t}{12 \times 100} = 24 \text{ years}$

Shortcut (for SI) Since SI in second case is double the SI in first case, so the time period will also be double since SI is directly proportional to the time period, provided that rate of interest be same and principal as well.

11. $\frac{P_1 \times 5 \times 2}{100} = \frac{P_2 \times 10 \times 4}{100}$

$\Rightarrow P_1 : P_2 = 4 : 1$

Therefore second principal is Rs. $125 \left(= 625 \times \frac{1}{5} \right)$

Alternative: Go through options.

12. Best way is to go through option

So, $1300 \times 0.12 + 1200 \times 0.125 = 306$

Hence, (d) is the correct option.

Alternatively: Solve through alligation

Therefore the ratio of first principal to the second principal is $13 : 12$.

$$\begin{array}{ccc} 12 & & 12.5 \\ & 12.24 & \\ 0.26 & & 0.24 \\ 13 & : & 12 \end{array} \quad \left| \begin{array}{l} 306 = \frac{2500 \times r \times 1}{100} \\ r = \frac{306}{25} = 12.24 \end{array} \right.$$

13. $\left(\frac{6000 \times 2 + 1500 \times 4}{100} \right) r = 900$

$\Rightarrow r = 5\%$

14. Amount to be paid in first year $= \frac{200 \times 5 \times 1}{100} + 200 = 210$

Amount left as a principal for the second year

$$= 210 - 100 = 110$$

\therefore Amount paid in second year $= 110 + \frac{110 \times 5 \times 1}{100} = 115.5$

$$\begin{array}{ll} 15. & \begin{array}{ll} A & B \\ P_A = P & P_B = 2P \\ r_A = 5\% & r_B = 5\% \\ t = 10 \text{ years} & t = 5 \text{ years} \\ \text{Interest of } A = \frac{P \times 5 \times 10}{100} & \text{Interest of } B = \frac{2P \times 5 \times 5}{100} \\ & = \frac{P}{2} \\ & = \frac{P}{2} \end{array} \end{array}$$

Hence (c) is correct

16. **Statement (I)** $\frac{P \times 5 \times 50}{100 \times 3} \neq P$, hence wrong

Statement (II) $SI = \frac{P \times 5 \times 20}{100} = P$, hence correct

Statement (III) $P = \frac{P \times 5 \times r}{100} \Rightarrow r = 20\%$

Again $SI = \frac{P \times 10 \times 20}{100} = 2P$ hence wrong

17. $\frac{P_1 \times 2 \times 5}{100} = \frac{P_2 \times 3 \times 5}{100} = \frac{P_3 \times 4 \times 5}{100}$

$\Rightarrow 10P_1 = 15P_2 = 20P_3$

$\Rightarrow P_1 : P_2 : P_3 = 30 : 20 : 15 = \frac{1}{10} : \frac{1}{15} : \frac{1}{20}$

18. $580 = \left[(x) + \left(x + \frac{x \times 1 \times 8}{100} \right) + \left(x + \frac{x \times 2 \times 8}{100} \right) + \left(x + \frac{x \times 3 \times 8}{100} \right) + \left(x + \frac{x \times 4 \times 8}{100} \right) \right]$

$$580 = 5x + \frac{8x}{10} = \frac{58x}{10}$$

$$\Rightarrow x = 100$$

19. Time period = Feb 24 + March 31 + April 18

$$= 73 \text{ days} = \frac{1}{5} \text{ year}$$

$$\therefore 2500 + \frac{2500 \times 12 \times 1}{100 \times 5} = \text{Rs. 2560}$$

20. $1700 + \frac{1700 \times 16 \times 2}{100} = \text{Rs. 2244}$

21. $A = P \left(1 + \frac{r}{100} \right)^n$

$$A = 1000 \left(1 + \frac{10}{100} \right)^3$$

$$A = 1000 \times (1.1)^3$$

$$A = 1331$$

$$\therefore \text{CI} = A - P = 1331 - 1000 = 331$$

22. $A = 10000 \times (1.2)^4$

$$A = 10000 \times 2.0736$$

$$A = 20736$$

$$\text{CI} = A - P$$

$$\text{CI} = 20736 - 10000 = 10736$$

23. $\text{CI} = [4000 \times (1.25)^3] - (4000)$

$$= 4000 \times 1.953125 - 4000$$

$$= 4000 \times 0.953125$$

$$= 3812.5$$

24. $\text{CI} = 5000 \times (1.3)^4 - 5000$

$$= 5000 \times 2.8561 - 5000$$

$$= 5000 (1.8561)$$

$$= 9280.5$$

25. $441 = 400 \left(1 + \frac{r}{100} \right)^2$

$$\Rightarrow \frac{21}{20} = 1 + \frac{r}{100}$$

$$\Rightarrow r = 5\%$$

26. Since, $A = 2P$, then

$$2P = P \left(1 + \frac{r}{100} \right)^n$$

$$\Rightarrow 2 = \left(1 + \frac{r}{100} \right)^n$$

$$\Rightarrow 4 = (2)^2 = \left[\left(1 + \frac{r}{100} \right)^n \right]^2 = \left[\left(1 + \frac{r}{100} \right)^{2n} \right]$$

$$\Rightarrow \text{time period} = 2n \quad (\because (a^m)^n = a^{mn})$$

(This question can be easily done by considering some appropriate values)

27. $7986 = 6000 \left(1 + \frac{r}{100} \right)^3$

$$\frac{7986}{6000} = \left(1 + \frac{r}{100} \right)^3$$

$$\frac{1331}{1000} = \left(1 + \frac{r}{100} \right)^3$$

$$\frac{11}{10} = \left(1 + \frac{r}{100} \right)$$

$$\Rightarrow r = 10\%$$

Alternatively: Go through options.

$$6000 \xrightarrow{+10\%} 6600 \xrightarrow{+10\%} 7260 \xrightarrow{+10\%} 7986$$

Hence, assumed option is correct.

28. Go through option

$$1 \times (1.2) = 1.2$$

$$1 \times (1.2)^2 = 1.44$$

$$1 \times (1.2)^3 = 1.728$$

$$1 \times (1.2)^4 = 2.0736$$

Hence minimum 4 years are required to double the sum.

29. $A = P \left(1 + \frac{R_1}{100} \right) \left(1 + \frac{R_2}{100} \right) \left(1 + \frac{R_3}{100} \right) \dots$

$$A = 5000 (1.08) (1.1) (1.12)$$

$$A = 6652.8$$

$$\text{CI} = 1652.8 = (6652.8 - 5000)$$

30. $2P = P \left(1 + \frac{r}{100} \right)^5$

$$\Rightarrow 2 = \left(1 + \frac{r}{100} \right)^5$$

$$\text{Now, } (2)^4 = \left(\left(1 + \frac{r}{100} \right)^5 \right)^4 = \left(1 + \frac{r}{100} \right)^{20}$$

\Rightarrow The amount becomes 16 ($= 2^4$) times

\therefore Hence (b) is correct, $\because (2400 \times 16 = 38400)$

31. $550 = x \left[\left(\frac{1}{1.2} \right) + \left(\frac{1}{1.2} \right)^2 \right]$

$$\Rightarrow 550 = x \left[\frac{2.2}{1.44} \right]$$

$$\Rightarrow x = \text{Rs. 360}$$

32. Difference between CI and SI for 2 years = $P \left(\frac{r}{100} \right)^2$

$$40 = P \left(\frac{10}{100} \right)^2 \Rightarrow P = 4000$$

Alternatively: Go through options

	First year	Second year
SI	400	400
CI	400	440

Alternatively: Go back in the reverse process. Rs. 40 at 10% implies that the principal for this interest was Rs. 400. Again by the same logic Rs. 400 as interest obtained at the principal of Rs. 4000 at 10%.

33. $6000 \left(\frac{10}{100} \right)^2 = 60$

34.
$$\frac{P \left(1 + \frac{r}{100} \right)^3}{P \left(1 + \frac{r}{100} \right)^2} = \left(1 + \frac{r}{100} \right)$$

$$\therefore \frac{9528.128}{8988.8} = \left(1 + \frac{r}{100} \right)$$

$$\Rightarrow \left(1 + \frac{84270}{1404500} \right) = \left(1 + \frac{r}{100} \right)$$

$$\Rightarrow \left(1 + \frac{6}{100} \right) = \left(1 + \frac{r}{100} \right)$$

$$\Rightarrow r = 6\%$$

So, $8988.8 = P \left(1 + \frac{6}{100} \right)^3$

$$\Rightarrow P = 8000$$

Alternatively: Best way is to go through options.

35. Difference between CI and SI for 2 years will be equal to the interest on SI for first year.

Hence, $6000 \times 0.07 \Rightarrow 420 \times 0.07 = 29.4 \neq 157.5$

and $7500 \times 0.08 \Rightarrow 600 \times 0.08 = 48 \neq 157.5$

and $14000 \times 0.1 \Rightarrow 1400 \times 0.1 = 140 \neq 157.5$

and $7000 \times 0.15 \Rightarrow 1050 \times 0.15 = 157.5 = 157.5$

Thus option (d) is correct.

36.
$$\frac{P \left(1 + \frac{r}{100} \right)^3}{P \left(1 + \frac{r}{100} \right)^2} = \left(1 + \frac{r}{100} \right)$$

$$\frac{23958}{21780} = \left(1 + \frac{r}{100} \right)$$

$$1 + \frac{2178}{21780} = 1 + \frac{r}{100}$$

$$r = 10\%$$

Alternatively: Remember the difference between compound interest of any two consecutive years will be same as the interest on the amount of total previous years.

So, $23958 - 21780 = 2178$

Now $r = \frac{2178}{21780} \times 100$

$$r = 10\%$$

37. Amount to be paid at the end of 2 year

$$= \frac{800 \times 10 \times 2}{100} + 800 = 880$$

Amount left as principal for the second year

$$= 480 = (880 - 400)$$

$$\begin{aligned} \text{Amount to be paid after 2nd year} &= 480 + \frac{480 \times 10}{100} \\ &= \text{Rs. 528} \end{aligned}$$

38. Principal for next month = $440 - 200 = 240$

Amount paid after next month = 244

Therefore interest charged at Rs. 240 = 4

$$\therefore 4 = \frac{240 \times r \times 1}{12 \times 100}$$

$$r = 20\% \text{ per annum}$$

39. Amount as a principal for first and

second month = $600 - 300 = \text{Rs. 300}$

Now, interest = $360 - 300 = \text{Rs. 60}$

$$\therefore 60 = \frac{300}{100} \times \frac{2}{12} \times r$$

$$r = 120\%$$

40. Amount as a principal for 2 month = $2400 - 1000 = 1400$
At the rate of $r\%$ per annum after 2 months, Rs. 1400 will amount to

$$\text{Rs.} \left(1400 + \frac{1400 \times r \times 2}{100 \times 12} \right) \quad \dots(i)$$

Again total amount for the 2 instalments at the end of second month will be

$$\text{Rs.} \left[800 + \left(800 + \frac{800 \times r \times 1}{100 \times 12} \right) \right] \quad \dots(ii)$$

from (i) and (ii), we get

$$\begin{aligned} 1400 + \frac{2800r}{1200} &= 1600 + \frac{800r}{1200} \\ \frac{2000r}{1200} &= 200 \end{aligned}$$

$$\Rightarrow r = 120\%$$

41. Balance price to be paid in instalments = 1980

At the rate of $r\%$ per annum after 4 months, Rs. 1980 will amount to $\text{Rs.} \left(1980 + \frac{1980 \times 4 \times 25}{12 \times 100} \right) = \text{Rs. 2145} \quad \dots(i)$

Now, the total amount for the 4 instalments at the end of fourth month will be

$$\begin{aligned} & \left[x + \left(x + \frac{25x \times 1}{12 \times 100} \right) + \left(x + \frac{25x \times 2}{12 \times 100} \right) + \left(x + \frac{25x \times 3}{12 \times 100} \right) \right] \\ &= 4x + \frac{25x}{1200} (1 + 2 + 3) \\ &= \frac{33x}{8} \quad \dots(ii) \end{aligned}$$

from (i) and (ii) $\frac{33x}{8} = 2145$

$$x = 520$$

42. Balance price to be paid in instalments = 350

At the rate of $r\%$ per annum after 5 months, Rs. 350 will amount to

$$\text{Rs.} \left(350 + \frac{350 \times 18 \times 5}{12 \times 100} \right) = \left(350 + \frac{1750 \times 18}{1200} \right) \quad \dots(i)$$

Again, total amount for the 5 instalments at the end of 5th month will be

$$\begin{aligned}
 & \text{Rs.} \left[x + \left(x + \frac{18x \times 1}{1200} \right) + \left(x + \frac{18x \times 2}{12 \times 100} \right) \right. \\
 & \quad \left. + \left(x + \frac{18x \times 3}{12 \times 100} \right) + \left(x + \frac{18x \times 4}{12 \times 100} \right) \right] \\
 & = \left[5x + \frac{18x}{1200} (1 + 2 + 3 + 4) \right] \\
 & = 5x + \frac{180x}{1200} = \left(\frac{6180x}{1200} \right)
 \end{aligned}$$

from (i) and (ii), we get

$$\begin{aligned}
 & \left(350 + \frac{1750 \times 18}{1200} \right) = \frac{6180x}{1200} \\
 \Rightarrow & \quad x = 73.058
 \end{aligned}$$

43. Let each instalments be Rs. x

The amount to be paid instalments = 390200
The total value of all the three instalments is

$$\text{Rs.} \left[x \left(\frac{25}{26} \right) + x \left(\frac{25}{26} \right)^2 + x \left(\frac{25}{26} \right)^3 \right]$$

and this must be equal to Rs. 390200

$$\begin{aligned}
 \text{Hence, } & x \times \frac{25}{26} \left[1 + \frac{25}{26} + \frac{625}{676} \right] = 390200 \\
 & x = \text{Rs. 140608}
 \end{aligned}$$

44. Rate of interest = 16% annum

Actual rate of interest = 4% per quarter
Principal of all three instalments

$$\begin{aligned}
 & = \left[17576 \left(\left(\frac{25}{26} \right) + \left(\frac{25}{26} \right)^2 + \left(\frac{25}{26} \right)^3 \right) \right] \\
 & = \frac{17576 \times 25 \times 1951}{26 \times 676} \\
 & = 48775
 \end{aligned}$$

Total amount paid = Rs. $17576 \times 3 = 52728$

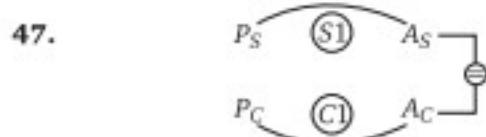
Interest charged = $52728 - 48775 = 3953$

45. Rate of interest = $\frac{40/3}{2} \% = \frac{20}{3} \% \text{ half yearly}$

$$\begin{aligned}
 \therefore & 10815 = x \left[\frac{15}{16} + \left(\frac{15}{16} \right)^2 + \left(\frac{15}{16} \right)^3 \right] \\
 \Rightarrow & x = 4096
 \end{aligned}$$

46. $P = 486680 \left[\frac{20}{23} + \left(\frac{20}{23} \right)^2 + \left(\frac{20}{23} \right)^3 \right]$

$$\begin{aligned}
 \Rightarrow & P = \left[486680 \times \frac{20}{23} \left(1 + \frac{20}{23} + \frac{400}{529} \right) \right] \\
 & P = 1111200
 \end{aligned}$$

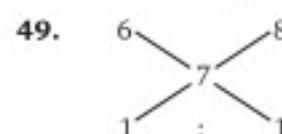


Obviously $P_S > P_C$, therefore percentage gain of P_C is greater than P_S .

48. $A_S = P + \frac{P \times 6 \times 6}{100} = P \left(\frac{136}{100} \right)$

$$A_C = P \left(1 + \frac{6}{100} \right)^6 = P \left(\frac{106}{100} \right)^6$$

$$\therefore \frac{A_S}{A_C} = \frac{136}{100} \times \left(\frac{100}{106} \right)^6$$



50. Difference between CI and SI for n^{th} year

$$= \frac{Pr}{100} \left[\left(1 + \frac{r}{100} \right)^{n-1} - 1 \right]$$

$$7280 = \frac{P \times 20}{100} [(1.2)^3 - 1]$$

$$\Rightarrow P = 50000$$

Alternatively:

	Initially	I st year	II nd year	III rd year	IV th year
SI	10000	12000	14000	16000	18000
CI	10000	12000	14400	17280	20736

CI for 4th year = $20736 - 17280 = 3456$

SI for 4th year = 2000

Difference between CI and SI = 1456 for Rs. 10000

So, the difference of Rs. 7280 is for Rs. 50000

51. $\frac{P \times 5 \times 9}{100 \times 12} - \frac{P \times 14 \times 3}{100 \times 12} = 10$

$$\Rightarrow P = \text{Rs. 4000}$$

$$\text{Now, } \frac{4000}{100 \times 12} [5 \times 9 + 14 \times 3] = \text{Rs. 290}$$

52. Let the principal be x , then

$$\frac{\left(\frac{x}{7} \times 4 + \frac{x}{2} \times 5 + \frac{5x}{14} \times 6 \right)}{100} = 730$$

$$\Rightarrow x = 14000$$

Alternatively: Go through suitable options.

Choose any middlemost option so that if the chosen option is not correct, then you can determine that whether you have to increase or decrease the value of the choices given.

53. $\frac{P_1 \times 2 \times 7x}{100} = \frac{P_2 \times 2 \times 8x}{100}$

$$\Rightarrow \frac{P_1}{P_2} = \frac{8}{7}$$

54. $\frac{P \left[\left(1 + \frac{r}{100} \right)^3 - 1 \right]}{\frac{pr}{100}} = \frac{\left(1 + \frac{r}{100} \right)^3 - 1}{\frac{r}{100}} = 3.64$

Now go through options and verify

$$\frac{\left(1 + \frac{20}{100}\right)^3 - 1}{\frac{20}{100}} = \frac{(1.2)^3 - 1}{0.2} = \frac{0.728}{0.2} = 3.64$$

Hence (c) is correct.

55. $\frac{13p}{5} - p = \frac{8p}{5}$
 Now, $\frac{8}{5}p = \frac{p \times r \times 32}{100}$
 $\Rightarrow r = 5\%$

56. $\frac{1500 \times 3}{100} (r_1 - r_2) = 18$
 $\Rightarrow r_1 - r_2 = 0.4$

LEVEL (2)

1. CI for 2 years = Rs. 756

SI for 2 years = Rs. 720

It means the interest on the interest of the first year = Rs. 36 ($= 756 - 720$)

This implies that the rate of interest is 10%

as $\frac{36}{360} \times 100 = 10\%$

It means the principal for first year was Rs. 3600

$\therefore \frac{P \times 10 \times 1}{100} = 360$

$\Rightarrow P = 3600$

Now, $\frac{P \times k \times k}{100} = \text{SI}$, where $r = t = k$

$$\frac{3600 \times k^2}{100} = 900$$

$\Rightarrow k = 5$

2. $30000(1 + 1.1 + (1.1)^2) - 30000(1 + 1.1 + 1.2)$

\Rightarrow Rs. 300

$$30000 \left(1 + \frac{10}{100}\right)^2 - \frac{30000 \times 10 \times 2}{100}$$

\Rightarrow Rs. 300

3. Interest received from Birbal = $\frac{Pr}{100}$

Interest received from Chanakya = $\frac{\left(2 \frac{Pr}{100}\right) \times \frac{r}{2}}{100}$

$$= P \left(\frac{r}{100}\right)^2$$

4. $100(1.3)^3 = 219.7$

$\Rightarrow \text{CI} = 119.7$

and $\text{SI} = \frac{100 \times 3 \times 30}{100} = 90$

\therefore CI is greater than SI by Rs. 29.7 $(119.7 - 90)$

$\therefore \text{% increase} = \frac{29.7}{90} \times 100 = 33.0\%$

5. The best way is to go through options

$$\frac{2200 \times 4 \times 3}{100} + \frac{1300 \times 6 \times 3}{100} = \text{Rs. 498}$$

Hence the presumed option is correct.

Alternatively: Average % rate = $\frac{166}{35}\%$

$$\left[\because 498 = \frac{3500 \times r \times 3}{100} \right] \Rightarrow r = \frac{166}{35}\% \\ \therefore \frac{35}{35} \times 4 \quad \frac{6 \times 35}{35} \\ \frac{166}{35} \\ \frac{44}{35} \quad \frac{26}{35} \\ 22 \quad : \quad 13$$

Thus the ratio of principal at 4% and 6% will be in the ratio of 22 : 13 respectively.

6. $\frac{\text{Decreases in second year}}{\text{Decreases in third year}} = \frac{100}{100 - r} = \frac{10}{9}$

$\Rightarrow r = 10\%$

Let the population of vultures 3 years ago be P , then

$$P \left(1 - \frac{10}{100}\right)^3 = 29160$$

$\Rightarrow P = 40000$

7. On the second year (in terms of CI) is

$$\frac{P \left(1 + \frac{r}{100}\right)^2}{\left(P + \frac{Pr}{100}\right)} = \frac{6}{5} \Rightarrow \left(1 + \frac{r}{100}\right) = \frac{6}{5}$$

$\Rightarrow r = 20\%$

8. Balance price to be paid in instalments = Rs. 1150 ... (i)
 $\because (1500 - 350) = 1150$

Now, the total amount for the next 3 instalments at the end of 3rd month will be

$$\left(1150 + \frac{1150 \times r \times 3}{12 \times 100}\right) = \\ \left[400 + \left(400 + \frac{400 \times r \times 1}{100 \times 12}\right) + \left(400 + \frac{400 \times r \times 2}{100 \times 12}\right)\right] \\ \left(\frac{46000 + 115r}{40}\right) = \left(1200 + \frac{400 \times 3r}{1200}\right) \\ \Rightarrow r = \frac{80}{3} = 26.66\% \quad \dots \text{(ii)}$$

9. A : $P = \frac{P \times 4 \times r}{100}$

$\Rightarrow r = 25\%$

B : $P \left(1 + \frac{25}{100}\right)^2 = \frac{25P}{16}$

NOTE When we consider Rs. 2200 for 4%, then the rest amount i.e., $Rs. 1300 - (3500 - 2200)$ will be considered automatically for 6%.

$$\text{Again } \frac{25P}{16} \times \frac{2 \times 25}{100} = \frac{25P}{32}$$

Therefore total amount of A after 4 years = $2P$

$$\text{and total amount of B after 4 years} = \frac{25P}{16} + \frac{25P}{32} = \frac{75P}{32}$$

$$\text{Therefore difference in amount} = \frac{75P}{32} - 2P = \frac{11P}{32} = 2750$$

$$\Rightarrow P = 8000$$

10. Go through options

$$1.8 + \frac{1.8 \times 6 \times 10}{100} = 1.6 + \frac{1.6 \times 8 \times 10}{100},$$

Hence (d) is correct.

$$\text{Alternatively: } P_1 + \frac{P_1 \times 6 \times 10}{100} = P_2 + \frac{P_2 \times 8 \times 10}{100}$$

$$\Rightarrow \frac{P_1}{P_2} = \frac{9}{8}$$

11. Amount which is to be returned on completion of studies

$$= 600000 \times (1.08)^2$$

$$= 699840$$

But only half of 699840 is returned which is equal to Rs. 349920

∴ Amount which is returned after two years of completion of studies

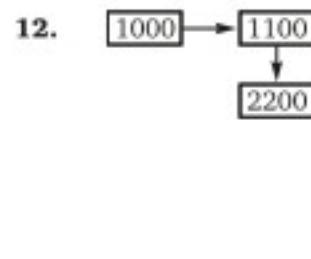
$$= 349920 \left(1 + \frac{10}{100}\right)^2$$

$$= 423403.2$$

Total amount returned

$$= 349920 + 423403.2 = 773323.2$$

$$= \text{Rs. 7.73323 lakh}$$



13. Note that, ultimately 8% interest is charged.

So the net value after 3 years = 125971.2

14. Total time = $25 + 5 = 30$ years

$$\text{Again no. of time periods for cost increment} = \frac{30}{6} = 5$$

and no. of time periods for rupee depreciation = $\frac{30}{5} = 6$

Now, the net value of the plot = $1000 \times (1.05)^5 \times (0.98)^6$
≈ Rs. 1130

15.

$$\frac{A}{B} = \frac{12 \times x}{3 \times y} = \frac{28}{15}$$

⇒

$$\frac{A}{B} = \frac{7}{15}$$

16. We can find the profit of B but not investment.

17. We don't know the rate of interest.

18. $10500 = x \left[\frac{10}{11} + \left(\frac{10}{11} \right)^2 \right]$

$$\Rightarrow x = 6050$$

19. Let the amount of investment with each one be Rs. 400, then
Hari Lal Hari Prasad

$$[400 (1.1)^2] = [100 (1.1)^2] + \left[300 + \frac{300 \times r \times 2}{100} \right]$$

$$\Rightarrow r = 10.5\%$$

20. Best way is to go through options

$$1000 \times (1.2)^2 = 2488.32 \approx 2490$$

21. Amount earned by HDFC = $1000000 + \frac{1000000 \times 10 \times 2}{100}$
= 1200000

$$\text{Amount earned by HUDCO} = 1000000 (1.1)^3 = 1331000$$

$$\text{Net earning of HUDCO} = 1331000 - 1200000 = 131000$$

22. Interest paid by Ram Singh = Rs. 48000

Now go through option

$$48000 = \frac{100000}{100} [6 \times 4 + 4 \times 6]$$

$$48000 = 48000$$

Hence proved that option (b) is correct. It means Ram Singh availed the discount after 4 years of loaning.

23. Worth of hotel after 3 years = $1000000 (1.2)^3$

$$= 1728000$$

$$\text{Worth of car after 3 years} = 1600000 \left(\frac{3}{4}\right)^3$$

$$= \text{Rs. 6,75,000}$$

So, the difference in their worth (pertaining to hotel and car) is

$$= 1728000 - 675000 = 10,53,000$$

