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Revised Effective Ionic Radii and Systematic Studies of Interatomic Distances in Halides and Chalcogenides

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The effective ionic radii of Shannon & Prewitt [*Acta Cryst.* (1969), B25, 925–945] are revised to include more unusual oxidation states and coordinations. Revisions are based on new structural data, empirical bond strength–bond length relationships, and plots of (1) radii *vs* volume, (2) radii *vs* coordination number, and (3) radii *vs* oxidation state. Factors which affect radii additivity are polyhedral distortion, partial occupancy of cation sites, covalence, and metallic character. Mean $\text{Nb}^{5+}\text{--O}$ and $\text{Mo}^{6+}\text{--O}$ octahedral distances are linearly dependent on distortion. A decrease in cation occupancy increases mean $\text{Li}^+\text{--O}$, $\text{Na}^+\text{--O}$, and $\text{Ag}^+\text{--O}$ distances in a predictable manner. Covalence strongly shortens $\text{Fe}^{2+}\text{--X}$, $\text{Co}^{2+}\text{--X}$, $\text{Ni}^{2+}\text{--X}$, $\text{Mn}^{2+}\text{--X}$, $\text{Cu}^+\text{--X}$, $\text{Ag}^+\text{--X}$, and M--H^- bonds as the electronegativity of X or M decreases. Smaller effects are seen for $\text{Zn}^{2+}\text{--X}$, $\text{Cd}^{2+}\text{--X}$, $\text{In}^{3+}\text{--X}$, $\text{Pb}^{2+}\text{--X}$, and $\text{Tl}^+\text{--X}$. Bonds with delocalized electrons and therefore metallic character, *e.g.* Sm--S , V--S , and Re--O , are significantly shorter than similar bonds with localized electrons.

Introduction

A thorough and systematic knowledge of the relative sizes of ions in halides and chalcogenides is rapidly being developed by crystal chemists as a result of (1) extensive synthesis within certain structure types, *e.g.* rocksalt, spinel, perovskite and pyrochlore; (2) preparation of new compounds with unusual oxidation states and coordination numbers; and (3) the abundance of accurate crystal structure refinements of halides, chalcogenides, and molecular inorganic compounds. A set of effective ionic radii which showed a number of systematic trends with valence, electronic spin state, and coordination was recently developed (Shannon & Prewitt, 1969, hereafter referred to as SP 69). This work has since been supplemented and improved by studies of certain groups of ions: rare earth and actinide ions (Peterson & Cunningham, 1967, 1968); tetrahedral oxyanions (Kálmán, 1971); tetravalent ions in perovskites (Fukunaga & Fujita, 1973); rare earth ions (Greis & Petzel, 1974); and tetravalent cations (Knop & Carlow, 1974).

Further, the relative sizes of certain ions or ion pairs were studied by Khan & Baur (1972): NH_4^+ ; Ribbe & Gibbs (1971): OH^- ; Wolfe & Newnham (1969): $\text{Bi}^{3+}\text{--La}^{3+}$; McCarthy (1971): $\text{Eu}^{2+}\text{--Sr}^{2+}$; Silva, McDowell, Keller & Tarrant (1974): No^{2+} . These authors' results have been incorporated here into a comprehensive modification of the Shannon–Prewitt radii.

In this paper the revised list of effective ionic radii, along with the relations between radii, coordination number, and valence is presented. The factors responsible for the deviation of radii sums from additivity such as polyhedral distortion, partial occupancy of cation sites, covalence, and metallic behavior (electron delocalization) will be discussed.

Procedure

The same basic methods used in SP 69 were employed in preparing the revised list of effective ionic radii (Table 1). Some of the same assumptions were made:

(1) Additivity of both cation and anion radii to reproduce interatomic distances is valid if one considers coordination number (CN), electronic spin, covalency, repulsive forces, and polyhedral distortion.*

(2) With these limitations, radii are independent of structure type.

(3) Both cation and anion radii vary with coordination number.

(4) With a constant anion, unit-cell volumes of isostructural series are proportional (but not necessarily linearly) to the cation volumes.

Other assumptions made in SP 69 have been modified:

(1) The effects of covalency on the shortening of M--F and M--O bonds are *not* comparable.

(2) Average interatomic distances in similar polyhedra in one structure are *not* constant but vary in a predictable way with the degree of polyhedral distortion (and anion CN). Both of these modified assumptions will be discussed in detail later.

The anion radii used in SP 69 were subtracted from available average distances. Approximately 900 distances from oxide and fluoride structures were used, and Table 2 lists their references according to CN and spin. These references generally cover from 1969 to 1975. The cation radii were derived to a first approximation from these distances, and then adjusted to be consistent with both the experimental interatomic distances and radii–unit cell volume (r^3 *vs* V) plots, as in

* Polyhedral distortion was not considered in SP 69.

SP 69. Although such r^3 vs V plots are not always linear (Shannon, 1975), their regular curvilinear nature still allows prediction of radii. This system is particularly accurate for radii in the middle of a series, and least reliable for large polarizable cations like Cs^+ , Ba^{2+} , and Ti^{3+} . Radii-volume plots were used by Knop & Carlow (1974) and Fukunaga & Fujita (1973) to derive radii of tetravalent cations. These radii were used along with experimental interatomic distances in deriving the final radii. Greis & Petzel (1974) derived rare earth radii in eight- and nine-coordination using accurate cell dimensions for rare earth trifluorides and distances calculated using the structural parameters of YF_3 and LaF_3 . These radii were used in Table 1 after applying small corrections ($+0.030 \text{ \AA}$ to IXLa^{3+} , IXCe^{3+} , IXPr^{3+} , and IXNd^{3+} ; $+0.025 \text{ \AA}$ to all other Greis & Petzel IXRE^{3+} radii, and 0.015 \AA to all

VIIIRe^{3+} radii) for consistency with experimental interatomic distances and radii-CN plots.

Where structural data were not available or not accurate, plots of (1) radii vs unit cell volumes, (2) radii vs CN and (3) radii vs oxidation state, or combinations of these were used to obtain estimated values. Fig. 1 shows examples of radii-valence plots used to provide consistency between experimental radii and those anticipated from the regular nature of these plots. Cations whose final radii values were derived from both estimated values and experimental interatomic distances are: VIOS^{3+} , VIOS^{6+} , VIOS^{7+} , VIRe^{4+} , VIRe^{5+} , VIRe^{6+} , VIRe^{7+} , VIIRh^{4+} , VIIU^{4+} , VIIU^{5+} , and VIIU^{6+} .

Fig. 2(a)-(e) shows plots of radii vs CN. Generally, it was assumed that radii-CN plots for two different ions do not cross. Radii for IVCu^+ , VICu^+ , IXRb^+ , VNI^{2+} , VIIEr^{3+} , VIIYb^{3+} , VIITb^{3+} , XIINd^{3+} , IVCr^{4+} ,

Table 1. *Effective ionic radii*

CR crystal radius, IR effective ionic radius, R from r^3 vs V plots, C calculated, E estimated, ? doubtful, * most reliable, M from metallic oxides.

ION	EC	CN	SP	CR	*IR*	ION	EC	CN	SP	CR	*IR*	ION	EC	CN	SP	CR	*IR*
AC+3 6P 6 VI			1.26	1.12	R	CL-1 3P 6 VI			1.67	1.81	P	GD+3 4F 7 VII			1.14	1.00	
AG+1 4D10 II			.81	.67		CL+5 3S 2 IIIPY			.26	.12		GE+2 4S 2 VI			1.193	1.053	R
IV			1.14	1.00	C	CL+7 2P 6 IV			.22	.08	*	GE+4 3D10 IV			1.247	1.107	RC
IVSQ			1.16	1.02		VI			.41	.27	A	VI			.87	.73	A
V			1.23	1.09	C	CM+3 5F 7 VI			1.11	.97	R	VI			.930	.390	*
VI			1.29	1.15	C	CM+4 5F 6 VI			.99	.85	R	VI			.670	.530	R*
VII			1.36	1.22		VIII			1.09	.95	R	H +1 1S 0 I			-.24	-.38	
VIII			1.42	1.28		CO+2 3D 7 IV	HS		.72	.58		II			-.04	-.18	
AG+2 4D 9 IVSQ			.93	.79		V			.81	.67	C	HF+4 4F14 IV			.72	.58	R
VI			1.08	.94		VI	LS		.79	.65	R	VI			.85	.71	R
AG+3 4D 8 IVSQ			.81	.67		HS			.885	.745	R*	VII			.90	.76	
VI			.89	.75	R	CO+3 3D 6 VI	LS		1.04	.90		VIII			.97	.83	
AL+3 2P 6 IV			.53	.39	*	VI			.685	.565	R*	HG+1 6S 1 III			1.11	.97	
VI			.62	.48		HS			.75	.61		VI			1.33	1.19	
V			.675	.535	R*	CO+4 3D 5 IV	HS		.54	.40		HG+2 5D10 II			.83	.69	
AM+2 5F 7 VII			1.35	1.21		VI			.67	.53	R	IV			1.10	.96	
VIII			1.40	1.26		LS			.87	.73	E	VI			1.16	1.02	
IX			1.45	1.31		HS			.94	.80	R	VIII			1.28	1.14	R
AM+3 5F 6 VI			1.115	.975	R	CR+3 3D 3 VI			.755	.615	R*	HO+3 4F10 VI			1.041	.901	R
VIII			1.23	1.09		CR+4 3D 2 IV			.55	.41		VIII			1.155	1.015	R
AM+4 5F 5 VI			.99	.85	R	VI			.69	.55	R	IX			1.212	1.072	R
VIII			1.09	.95		CR+5 3D 1 IV			.485	.345	R	X			1.26	1.12	
AS+3 4S 2 VI			.72	.58	A	VI			.63	.49	EA	I -1 5P 6 VI			2.06	2.20	A
AS+5 3D10 IV			.675	.535	R*	VIII			.71	.57		I +5 5S 2 IIIPY			.58	.44	*
VI			.60	.46	C*	CR+6 3P 6 IV			.40	.26		VI			1.09	.95	
AT+7 5D10 VI			.76	.62	A	VI			.58	.44	C	I +7 4D10 IV			.56	.42	
AU+1 5D10 VI			1.51	1.37	A	CS+1 5P 6 VIII			1.81	1.67		VI			.67	.53	
AU+3 5D 8 IVSQ			.82	.68		IX			1.88	1.74		IN+3 4D10 IV			.76	.62	
VI			.99	.85	A	IX			1.92	1.78		VI			.940	.800	R*
AU+5 5D 6 VI			.71	.57		X			1.95	1.81		VIII			1.06	.92	RC
8 +3 1S 2 III			.55	.41	*	XI			1.99	1.85		IR+3 5D 6 VI			.82	.68	E
IV			.55	.41	*	XII			2.02	1.88		IR+4 5D 5 VI			.765	.625	R
VI			.41	.27	C	CU+1 3D10 II			.60	.46		IR+5 5D 4 VI			.71	.57	EM
BA+2 5P 6 VI			1.49	1.35		IV			.74	.60	E	K +1 3P 6 IV			1.51	1.37	
VII			1.52	1.38		VI			.91	.77	E	VI			1.52	1.38	
VIII			1.56	1.42	C	CU+2 3D 9 IV			.71	.57		VII			1.60	1.46	
IX			1.61	1.47		IVSQ			.71	.57	*	VIII			1.65	1.51	
X			1.66	1.52		V			.79	.65	*	IX			1.69	1.55	
XI			1.71	1.57		VI			.87	.73		X			1.73	1.59	
XII			1.75	1.61	C	CU+3 3D 8 VI	LS		.68	.54		XI			1.78	1.64	
BE+2 1S 2 III			.30	.16		D +1 1S 0 II			.04	-.10		LA+3 4D10 VI			1.172	1.032	R
IV			.41	.27	*	DY+2 4F10 VI			1.21	1.07		VII			1.24	1.10	
VI			.59	.45	C	VIII			1.27	1.13		VIII			1.300	1.160	R
BI+3 6S 2 V			1.10	.96	C	VI			1.33	1.19		IX			1.356	1.216	R
VI			1.17	1.03	R*	UY+3 4F 9 VI			1.052	.912	R	X			1.41	1.27	
VII			1.31	1.17	R	VII			.11	.97		XI			1.50	1.36	C
BI+5 5D10 VII			.90	.76	E	VIII			1.167	1.027	R	LI+1 1S 2 IV			.730	.590	*
BK+3 5F 8 VI			1.10	.96	R	IX			1.223	1.083	R	VI			.90	.76	*
BK+4 5F 7 VI			.97	.83	R	ER+3 4F11 VI			1.030	.890	R	VIII			1.06	.92	C
VIII			1.07	.93	R	VII			1.085	.945		LU+3 4F14 VI			1.001	.861	R
BR-1 4P 6 VI			1.82	1.66	P	VIII			1.144	1.004	R	VII			1.117	.977	R
BR+3 4P 2 IVSQ			.73	.59		IX			1.202	1.062	R	IX			1.172	1.032	R
BR+5 4S 2 IIIPY			.45	.31		EU+2 4F 7 VI			1.31	1.17		VI			.71	.57	
BR+7 3D10 IV			.39	.25		V			1.34	1.20	V	VI			.80	.66	
VI			.53	.39	A	VIII			1.39	1.25		VII			.860	.720	*
C +4 1S 2 III			.06	-.08		IX			1.44	1.30		VIII			1.03	.89	C
IV			.29	.15	P	X			1.49	1.35		HS			.80	.66	
VI			.16	.02		EU+3 4F 6 VI			1.087	.947	R	VI	HS		.89	.75	C
CA+2 3P 6 VI			1.14	1.00		VII			1.15	1.01		LS			.81	.67	E
VII			1.20	1.06	*	VIII			1.206	1.066	R	HS			.970	.830	R*
VIII			1.26	1.12	*	IX			1.260	1.120	R	VI			1.04	.90	C
IX			1.32	1.18		F -1 2P 6 VI			1.145	1.005		VIII			1.10	.96	R
X			1.37	1.23	C	III			1.16	1.30		VI			.72	.58	
XI			1.48	1.34	C	IV			1.17	1.31		LS			.72	.58	R
CD+2 4D10 IV			.92	.78		VI			1.19	1.33		HS			.785	.645	R*
V			1.01	.87		F +7 1S 2 VI			.22	.08	A	VI			.53	.39	R
VI			1.09	.95		FE+2 3D 6 IV	HS		.77	.63		VI			.670	.530	R*
VII			1.17	1.03	C	IVSQ			.78	.64		HS			.67	.53	R
VIII			1.24	1.10	C	VI			.75	.61	E	MN+6 3D 1 IV			.75	.61	R
IX			1.45	1.31		VI	HS		.920	.780	R*	MN+7 3P 6 IV			.39	.25	
CE+3 6S 1 VI			1.15	1.01	R	VIII			1.06	.92	C	VI			.60	.46	A
VII			1.21	1.07	E	FE+3 3D 5 IV	HS		.63	.49	*	VI			.83	.69	E
VIII			1.283	1.143	R	V			.72	.58		MO+4 4D 2 VI			.790	.650	RM
IX			1.336	1.196	R	VI	LS		.69	.55	R	MO+5 4D 1 IV			.60	.46	R
X			1.39	1.25	C	HS			.785	.645	R*	VI			.75	.61	R
XI			1.48	1.34	C	FE+4 3D 4 VI	HS		.92	.78	C	VI			.55	.41	R*
CE+4 5P 6 VI			1.01	.87	R	FE+6 3D 2 IV			.725	.585	R	VI			.64	.50	
VIII			1.11	.97	R	FR+1 6P 6 VI			.94	1.80	A	VI			.73	.59	R*
X			1.21	1.07		GA+3 3D10 IV			.61	.47	*	VII			.87	.73	
XI			1.14	.99		VI			.69	.55		N -3 2P 6 VI			1.32	1.18	
CF+3 6D 1 VI			1.09	.95	R	VI			.69	.55		N +3 2S 2 VI			.30	.16	A
CF+4 5F 8 VI			.961	.821	R	VI			.760	.620	R*	N +5 1S 2 III			.044	-.104	A
VIII			1.06	.92		GD+3 4F 7 VI			1.078	.938	R	VI			.27	-.13	A

Table 1 (cont.)

ION	EC	CN	SP	CR	'IR'	ION	EC	CN	SP	CR	'IR'	ION	EC	CN	SP	CR	'IR'
Na+1 2P 6 IV				1.13	.99	PR+3 4F 2 VI				1.13	.99 R	TC+4 4D 3 VI				.785	.645 RM
V				1.14	1.00	VIII				1.266	1.126 R	TC+5 4D 2 VI				.74	.60 ER
VI				1.16	1.02	IX				1.317	1.179 R	TC+7 4P 6 VI				.51	.37
VII				1.26	1.12	PR+4 4F 1 VI				.99	.85 R	TE-2 5P 6 VI				2.07	2.21 P
VIII				1.32	1.18	VIII				1.10	.96 R	TE+4 5S 2 III				.66	.52
IX				1.38	1.24 C	PT+2 5D 8 IVSQ				.74	.60	VI				.80	.66
X				1.53	1.39	IX				.94	.80 A	VI				1.11	.97
NB+3 4D 2 VI				.86	.72	PT+4 5D 6 VI				.765	.625 R	TE+6 4D10 IV				.57	.43 C
NB+4 4D 1 VI				.82	.68 RE	PT+5 5D 5 VI				.71	.57 ER	VI				.70	.56 *
VIII				.93	.79	PU+3 5F 5 VI				1.14	1.00 R	TH+4 6P 6 VI				1.08	.94 C
NB+5 4P 6 VI				.78	.64 C	PU+4 5F 4 VI				1.00	.86 R	VIII				1.19	1.05 RC
VII				.83	.69 C	PU+5 5F 3 VI				.88	.74 E	IX				1.23	1.09 *
VIII				.88	.74	PU+6 5F 2 VI				.85	.71 R	X				1.27	1.13 E
ND+2 4F 4 VIII				1.43	1.29	RA+2 6P 6 VIII				1.62	1.48 R	XI				1.32	1.18 C
IX				1.49	1.35	XII				1.84	1.70 R	XII				1.35	1.21 C
ND+3 4F 3 VI				1.123	.983 R	RB+1 4P 6 VI				1.66	1.52	TI+2 3D 2 VI				1.00	.86 E
VIII				1.249	1.109 R*	VII				1.70	1.56	TI+3 3D 1 VI				.810	.670 RM
IX				1.303	1.163 R	VIII				1.75	1.61	TI+4 3P 6 IV				.56	.42 C
XII				1.41	1.27 E	IX				1.77	1.63 E	V				.65	.51 C
NI+2 3D 8 IV				.69	.55	X				1.80	1.66	VI				.745	.605 R*
IVSQ				.63	.49	XI				1.83	1.69	VIII				.88	.74 C
V				.77	.63 E	XII				1.86	1.72	TL+1 6S 2 VI				1.64	1.50 R
VI				.830	.690 R*	XIV				1.97	1.83	VIII				1.73	1.59 R
NI+3 3U 7 VI	LS			.70	.56 R*	RE+4 5D 3 VI				.77	.63 RM	XII				1.84	1.70 RE
HS				.74	.60 E	RE+5 5D 2 VI				.72	.58 E	TL+3 5D10 IV				.89	.75
LS				.62	.48 R	RE+6 5D 1 VI				.69	.55 E	VI				1.025	.885 R
NI+4 3D 6 VI				1.24	1.1 E	RE+7 5P 6 IV				.52	.38	VIII				1.12	.98 C
ND+2 5F14 VI				1.24	1.10	VI				.67	.53	TM+2 4F13 VII				1.17	1.03
NP+2 5F 5 VI				1.01	.87 R	RH+3 4D 6 VI				.805	.665 R	VII				1.23	1.09
NP+3 5F 4 VI				1.24	1.01	RH+4 4D 5 VI				.74	.60 RM	VIII				1.020	.880 R
NP+4 5F 3 VI				1.12	.98 R	RH+5 4D 4 VI				.69	.55	VIII				1.134	.994 R
NP+5 5F 2 VI				.89	.75	RU+3 4D 5 VI				.82	.68	IX				1.192	1.05 R
NP+6 5F 1 VI				.86	.72 R	RU+4 4D 4 VI				.760	.620 RM	U +3 5F 3 VI				1.165	1.025 R
NP+7 6P 6 VI				.85	.71 A	RU+5 4D 3 VI				.705	.565 ER	U +4 5F 2 VI				1.03	.89
O -2 2P 6 II				1.21	1.35	RU+7 4D 1 IV				.52	.38	VII				1.09	.95 E
III				1.22	1.36	RU+8 4P 6 IV				.50	.36	IV				1.14	1.00 R*
IV				1.24	1.38	S -2 3P 6 VI				1.70	1.84 P	IX				1.19	1.05
V				1.26	1.40	S +4 3S 2 VI				.51	.37 A	XII				1.31	1.17 E
VII				1.28	1.42	S +6 2P 6 IV				.26	.12 *	U +5 5F 1 VI				.90	.76
VIII				1.18	1.32	VI				.63	.29 C	VI				.98	.84 E
DM-1				1.20	1.34	SB+3 5S 2 IVPV				.90	.76	U +6 6P 6 II				.59	.45
IV				1.21	1.35 E	V				.94	.80	IV				.66	.52
VI				1.23	1.37 E	VI				.90	.76 A	VI				.87	.73 *
OS+4 5D 4 VI				.770	.630 RM	SB+5 4D10 VI				.74	.60 *	VII				.95	.81 E
OS+5 5D 3 VI				.715	.575 E	SC+3 3P 6 VI				.885	.745 R*	VIII				1.00	.86
OS+6 5D 2 V				.63	.49	VIII				1.010	.870 R*	V +2 3D 3 VI				.93	.79
OS+7 5D 1 VI				.685	.545 E	SE-2 4P 6 VI				1.84	1.98 P	V +3 3D 2 VI				.70	.56 RM
OS+8 5P 6 IV				.53	.39	SE+4 4S 2 VI				.64	.50 A	V +4 3D 1 V				.67	.53
P +3 3S 2 VI				.58	.44 A	SE+6 3D10 IV				.42	.28 *	VI				.72	.58 R*
P +5 2P 6 IV				.31	.17 *	SI+4 2P 6 VI				.56	.42 C	VIII				.86	.72 E
V				.52	.38 C	VI				.60	.46 *	V +5 3P 6 IV				.60	.46 *
VI				.52	.38 C	SM+2 4F 6 VII				1.36	1.22	VI				.68	.54
PA+3 5F 2 VI				1.18	1.04 E	VIII				1.41	1.27	W +4 5D 2 VI				.80	.66 RM
PA+4 6D 1 VI				1.04	.90 R	IX				1.32	1.17	W +5 5D 1 VI				.76	.62 R
VIII				1.15	1.01	SM+3 4F 5 VI				1.098	.958 R	W +6 5P 6 IV				.56	.42 *
PA+5 6P 6 VI				.92	.78	VII				1.16	1.02 E	V				.65	.51
VIII				1.05	.91	VIII				1.219	1.079 R	VI				.74	.60 A
IX				1.09	.95	IX				1.272	1.132 R	XE+8 4D10 IV				.56	.40
PB+2 6S 2 IVPV				1.12	.98 C	XII				1.38	1.24 C	VI				.62	.48
VI				1.33	1.19	SN+4 4D10 IV				.69	.55 R	Y +3 4P 6 VI				1.040	.900 R*
VII				1.37	1.23 C	V				.76	.62 C	IX				.96	.82
VIII				1.43	1.29 C	VI				.830	.690 R*	VIII				1.159	1.019 R*
IX				1.49	1.35 C	VII				.89	.75	IX				1.215	1.075 R
X				1.54	1.40 C	VIII				.95	.81 C	YB+2 4F14 VI				1.16	1.02
XI				1.59	1.45 C	SR+2 4P 6 VII				1.32	1.18	VII				1.22	1.08 E
XII				1.63	1.49	VIII				1.35	1.21	VIII				1.28	1.14
PB+4 5D10 IV				.79	.65 E	IX				1.40	1.26	YB+3 4F13 VI				1.008	.868 R*
V				.87	.73 E	IX				1.45	1.31	VII				1.065	.925 E
VI				.915	.775 R	X				1.50	1.36 C	VIII				1.125	.985 R
VIII				1.08	.94 R	XII				1.58	1.44 C	IX				1.182	1.042 R
PD+1 4D 9 II				.73	.59	TA+3 5D 2 VI				.86	.72 E	ZN+2 3D10 IV				.74	.60 *
PD+2 4D 8 IVSQ				.78	.64	TA+4 5D 1 VI				.82	.68 E	V				.82	.68 *
IX				1.00	.86	TA+5 5P 6 VI				.78	.64	VI				.880	.740 R*
PD+3 4D 7 VI				.90	.76	VII				.83	.69	VIII				1.04	.90 C
PD+4 4D 6 VI				.755	.615 R	VIII				.88	.74	ZR+4 4P 6 IV				.73	.59 R
PN+3 4F 4 VI				1.11	.97 R	IX				1.063	.923 R	V				.80	.66 C
VIII				1.233	1.093 R	TI+3 4F 8 VI				1.12	.98 E	VI				.86	.72 R*
IX				1.284	1.144 R	VII				1.180	1.040 R	VII				.92	.78 *
PD+4 6S 2 VI				1.08	.94 R	VIII				1.235	1.095 R	VIII				.98	.84 *
VIII				1.22	1.08 R	IX				.90	.76 R	IX				1.03	.89
PD+6 5D10 VI				.81	.67 A	TI+4 4F 7 VIII				1.02	.88						

VIII V^{4+} , IV Pb^{4+} , and X Th^{4+} obtained from these plots were used to help determine the values in Table 1. The first estimate of VIII V^{4+} was made from distances in $\text{C}_{32}\text{H}_{28}\text{S}_8\text{V}$ (Bonamico, Dessy, Fares & Scaramuzza, 1974).

Another method used to estimate radii was based on the empirical relationship between interatomic distances and bond strengths. Brown & Shannon (1973) derived these relationships for the cations in the first three rows of the periodic table from a large number of experimental interatomic distances. These curves can be used to calculate hypothetical distances for cations in any coordination (Brown & Shannon, 1973; Shannon, 1975; Brown, 1975). Examples of cations whose radii were calculated in this way are: IV Mn^{2+} , VI Be^{2+} , VI B^{3+} , VI P^{5+} , VI S^{6+} , VIII Mg^{2+} , and VIII Fe^{2+} . These are marked with a C in Table 1. In certain cases, these values were combined with known structural data (see Table 2) to obtain the radii in Table 1. Although the

majority of radii were derived from oxides and fluorides,* some were taken from chlorides, bromides, iodides, and sulfides. For large electropositive cations with highly ionic bonds, very little covalent shortening is believed to occur and radii derived from these other compounds should differ only slightly from those derived from fluorides and oxides. Examples are divalent rare earths such as Yb^{2+} , Tm^{2+} , Dy^{2+} , Sm^{2+} , Nd^{2+} and the ions Am^{2+} , Ac^{3+} , Np^{3+} , and U^{4+} .

Another useful scheme for estimation of radii is the comparison of unit-cell volumes of compounds containing cations of similar size. McCarthy (1971) prepared a number of isotopic Sr^{2+} and Eu^{2+} ternary oxides and generally found the unit cells of the Sr^{2+}

* Because of covalency differences in M-O and M-F bonds, oxide distances were emphasized. Therefore the radii in Table 1 are more applicable to oxides than fluorides. This subject is treated further in the discussion *Effects of covalence*.

Table 2. References for Table 1

The references here and in Tables 4, 5, 6 and 8 are abbreviated according to *Codens for Periodic Titles* (1966).

AG+3 VI	68 JINCA	30	823 AC CL3
AG+1 II	71 INDOCA	10	719 AG FE 02
72 ZAACA	393	246	58 AG 04
73 ZENBA	280	263	BA AG 04
AG+1 IV	71 JSSCB	3	364 AG 02 CR 04
AG+1 IVS0	42 JACSA	64	354 AG 03 AS 04
69 ACSAA	23	2261	AG 2 S 03
AG+1 V	70 JSSCB	1	484 AG 06 MO10 033
AG+1 V	32 ZKKA	82	161 AG 02 S04
47 JACSA	69	222	AG 03 P04
71 JSSCB	3	364	AG 02 CR 04
69 ACACB	25	5116	AG 02 CR 07
70 JSSCB	1	484	AG 02 MO 04
AG+1 VII	70 JSSCB	1	484 AG 06 MO10 033
69 ACACB	25	5116	AG 02 CR 07
AG+1 VIII	65 ACCRA	19	180 AG 7 N 011
AG+2 IVS0	71 JPCSA	32	543 AG F2
AG+2 VI	71 JPCSA	32	543 AG F2
AG+3 IVS0	65 ACCRA	19	180 AG 7 N 011
AL+3 V	67 ACCRA	23	754 NA T12 AL5 012
68 NJMMA	1968	80	CA AL B 04
70 AGACA	26	1230	CA AL B 04
70 NJMMA	1970	547	CA12 AL10 033
71 SPMDA	15	905	CA AL 010 (OH)6
71 SPMDA	15	905	CA AL 010 (OH)6
71 SPMDA	15	905	CA AL 010 (OH)6
72 JACSA	27	1826	BE14 AL2 03
72 JSSCB	4	60	AG AL11 017
AL+3 V	68 ACACA	24	1518 (MG,FE) AL3 S1 B 09
68 AMNIA	53	1096	AL2 P04 (OH)3
AL+3 VI	71 AMNIA	56	18 NA3 AL2 L13 F12
72 JSSCB	4	11	ND AL 03
72 JSSCB	4	11	ND AL 03
58 ACACA	5	684	MG AL2 04
72 ACACA	28	1899	AL2 BE3 S10 D18
68 JACSA	80	22	AL1AC1A
73 ACACA	29	2291	AL P 0412 H2 0
67 ZKKA	125	1423	CS BE4 B12-X1 AL4 O28 H2
74 ACACA	30	1311	NA AL 1P 0412 IO H14
74 ACACA	139	125	AL IO H13
AM+2 VII	72 JINCA	34	3427 AM 12
AM+2 VIII	73 JINCA	35	483 AM BR2
AM+2 IX	73 JINCA	35	483 AM CL2
AM+3 VIII	72 JINCA	11	2233 AM2 (S 04)3.0H2 0
AM+4 VI	67 ACACA	71	228 NA AM 03
67 INUCA	3	327	R (BK+)
AS+5 IV	69 ZKKA	130	231 ZH2 CU AS2 08
68 CJCHA	46	917	CU3 AS2 08
63 BAPCA	11	361	MG AS2 07
69 ACACA	25	1544	CA H AS 04.2 H2 0
69 ACACA	25	2658	R H AS 04.2 H2 0
68 AMNIA	53	1841	MN2 0 H AS 04
63 CARIA	7	561	CA CU AS 04 0 H
70 ACACA	24	1584	NA2 H AS 04.7 H2 0
69 ACACA	26	1574	NA2 H AS 04.7 H2 0
69 CHDCA	268	1694	BA H12 AS2 08
70 AMNIA	55	2023	MN2 IO H19 (H2 012
70 ACACA	26	1809	IN H12 H AS 04
70 ACACA	24	1711	LI H2 02 AS 04
70 INUCA	9	2259	CAZ AS 04 CL
69 ACACA	18	777	CU3 AS 04 IO H13
70 CJCHA	48	801	CU3 AS2 08
71 CJCHA	49	1036	CA AS 04
70 AMNIA	55	1409	MN2 H AS 012
71 ACACA	27	2124	NA3 AS 04.12 H2 0
73 ACACA	29	2611	MG AS2 08
61 AMNIA	46	1077	CAZ B AS 04 (OH)4
73 CJCHA	51	2082	NA4 AS2 07
68 ZAACA	347	133	CR H AS 04 H2 0
66 ZAACA	347	140	SR H AS 04 H2 0
71 AMNIA	56	1167	ZNA AS2 08 (OH)2.2H2 0
70 ACACA	26	403	CA H AS 04
70 ZKKA	132	332	CU3 AS2 08
73 ACACA	29	141	LU AS 04
73 ACACA	29	2121	MN4 H AS 04
AS+5 VI	71 CJCHA	49	2539 CL F2 AS F6
73 JSSCB	6	80	MGAS AS3 016
70 CJCHA	48	3124	CU8 AS3 016
73 ACACA	29	266	CALCULATED
74 INDOCA	13	780	XL AS F11.4E2 AS F9
74 ACACA	30	250	K AS F6
AU+3 IVS0	69 JPCSA	1969	1936 R AU F4
70 ZAACA	375	43	L13 AU O3.4 AU O2.8B AU O2
70 JCSIA	1970	3092	R AU INDO314
AU+5 VI	74 INUCA	13	775 RE2 AU F17
D+3 III	68 NJMMA	1968	80 CA AL B 04
71 SPMDA	15	902	R BE2 B 03 F2
71 ACACA	27	672	ZN B4 07
70 ACACA	26	1189	B 02
71 ACACA	27	904	L13 B 03
70 ZKKA	132	241	CA B3 05 (OH)1
71 JACSA	4	284	LU B 04
74 JPCSA	60	1899	MN B4 07
74 MRBUA	9	1661	ND AL3 (B 03)4
B+3 IV	68 ACACA	24	869 B2 J3 I1
68 ACACA	24	1703	NA B F4
68 CJCHA	47	2579	R B F4
71 ACACA	27	677	CU B2 04
71 ACACA	27	1102	R H4 F4
70 ZKKA	132	241	CA B3 05 0 H
63 ACACA	16	1233	NA B IO H14.2 H2 0
74 JPCSA	60	1899	MN B4 07
71 AMNIA	56	1553	MG (NO 07 IO H16) .2 H2 0
73 ACACA	27	672	ZN B4 07
B+3 VI	73 ACACA	29	266 CALCULATED
BA+2 VI	70 ZKKA	131	161 BA3 V2 08
73 ZENBA	280	263	BA AG 04
BA+2 VII	71 ACACA	27	1263 BA FE2 04
73 ACACA	29	2009	BA2 TI 04
BA+2 VIII	58 ZKKA	110	231 CU BAZ IC 0 H16.4 H2 0
69 JPCSA	51	428	BA MN F4
70 JPCSA	53	3279	BA CU F4
71 JPCSA	55	1093	BA W 04
71 AMNIA	56	758	BA C 03
71 ZAACA	386	1	BA2 C 04
73 ACACA	29	2009	BA2 TI 04
BA+2 IX	71 ZAACA	386	1 BA2 C 04
73 ACACA	27	1653	BA TE (S2 03)2.2 H2 0
73 ACACA	27	1653	BA TE (S2 03)2.2 H2 0
BA+2 X	70 ZKKA	131	161 BA3 IV 0412
70 ACACA	26	105	BA3 S14 NB6 026
67 BUFGA	90	24	BA P2 06
BA+2 XI	71 ACACA	27	1263 BA FE2 04
BA+2 XII	70 ACACA	26	102 BA5 TA 015
72 CSCMC	1	1	BA T16 013
71 MRBUA	6	725	BA CA FE4 08
69 CHDCA	280	1694	BA H12 AS2 08
75 ACACA	31	596	K2 BA CU (IN 02)6
BE+2 III	69 ACACA	25	1647 SR BE3 04
66 ACACA	20	295	CA12 BE17 029
BE+2 IV	68 SPMDA	6	733 NA BE P 04
68 ACACA	24	672	L42 BE2 05
68 ACACA	24	607	CS BE F3
69 ACACA	25	1847	SR BE3 04
71 SPMDA	15	909	FE3 BE S13 09 (F,OH)2
72 SPMDA	16	1021	BE2 S14 0 P
73 ACACA	28	1899	AL2 BE3 S16 018
73 ACACA	229	2976	NA3 BE TH10 F45
69 ACACA	12	634	BE AR F4T1
67 ZKKA	125	423	CU BE4 B12-X1 AL4 O28 H2
74 ACACA	30	396	NA6 (S116 AL2)BE10H12 0391
74 ACACA	30	2434	L12 BE S1 04
74 AMNIA	59	1267	CA BE2 P2 08
BI+3 V	69 JSCDA	7	1797 B12 M 06
70 ACACA	24	384	B12 03 ALPHA
BI+3 VI	70 ACACA	24	384 B12 03 ALPHA
71 JPCSA	32	1315	BI FE 03
BI+3 VIII	72 MRBUA	7	1025 BI TITANATES
BI+5 VI	R3 VS V (BA2 LA BI 06)		
BR+4 VI	67 INUCA	3	327 R (BK+)
BR+4 IV S0	71 JPCSA	1969	1936 K AR F4
BR+5 III	69 ACACA	25	421 SR (BR 03)3.9H2 0
67 ACACA	21	2834	MG BR 03
BR+7 IV	71 JCSIA	1971	1857 BR(+7)0
C+4 III	65 ACCRA	18	689 CA C 03
71 JINCA	35	27	CA C 03
73 AMNIA	58	1029	MG C 03
67 PLRCA	92	125	MN C 03
75 ACACA	31	890	NA2 C 03.2H2 0
CA+2 VI	68 NJMMA	1968	80 CA AL B 04
69 ACACA	25	1933	CA IN2 BE P 0213
57 JPCSA	26	563	CA IO H12
55 ACACA	18	689	CA C 03
CA+2 VII	71 CJCHA	49	1036 CA3 AS2 08
71 ACACA	27	2311	CA2 AL FE 05
73 MRBUA	8	593	CA CR F5
69 ACACA	25	1534	CA10 (P 04)6 IO H12
CA+2 VIII	71 INDOCA	7	1345 CA2 P2 07
74 CJCHA	52	1155	CA18 MG2 H2 (P 04)14
CA+2 IX	71 JINCA	35	27 CA C 03
69 ACACA	25	1534	CA10 (P 04)6 IO H12
CA+2 X	69 ACACA	25	955 CA B2 04 I11
CA+2 XII	69 ACACA	25	965 CA B2 04 IV
74 AMNIA	59	41	CA AL3 IO H16
74 JACSA	98	6606	K2 CA CU (IN 02)6
CD+2 IV	59 ACACA	12	1049 CO IN2 04
71 ZAACA	382	27	K2 CO2 04
CD+2 V	69 CJCHA	47	3409 CO2 P2 07
70 ZKKA	132	332	CU3 AS2 08
69 CJCHA	47	3409	CO2 P2 07
70 ZKKA	132	332	CU3 AS2 08
66 SPMDA	11	11	CO W 04
67 HCACA	50	2023	CO2 MN3 08
74 JCSIA	1974	674	CO CA H6 06
74 ACACA	30	1880	CO2 C4 H12 012
CD+2 VII	74 ACACA	28A	119 CO D1C H2 C 0 D12.3 1/2 H2 0
74 JCSIA	1974	1922	CO D1C H2 C 0 U12.3 H2 0
CD+2 VIII	55 PRVBA	98	903 CO2 NB2 07
69 ACACA	25	1804	CO IN 03)2.4 D2 0
74 JCSIA	1974	674	CO CA H6 06
CE+3 VIII	74 ZAACA	403	1 R3 VS V (CE F3)
74 JCSIA	1974	1165	C41 H24 CE F12 N DB 54
CE+3 IX	67 SPMDA	12	214 CE B S1 05
74 ZAACA	403	1	R3 VS V (CE F3)
CE+3 X	60 AMNIA	45	1 CE4 ME NE2 T12 S14 022
CE+4 VI	72 ACACA	28	956 BA CE 03
73 JSSCB	8	331	R (CE+4)
CE+4 VII	69 INUCA	8	33 IN H612 CE F6
74 JCSIA	1974	2021	NA6 CE D10 D36.2.30H2 0
74 JCSIA	15	397	CE15 OH12
74 ACACA	28	1079	AC CE (ACACA)
CE+4 XII	68 JACSA	90	3589 (HMH)2 H6 ICE MD12 042)1.2 H2 0
CF+3 VI	71 JINCA	36	2023 R3 VS V (CF2 S 04)3
CL+5 III	73 MRBUA	8	791 RB CL 03
CL+7 IV	72 ACACA	28	839 TMPO CL 04
62 ZKKA	84	65	K CL 04
60 ACACA	13	855	N U2 CL 04.8 H CL 04
59 JPCSA	63	270	H CL 04.2 H2 0
59 JACSA	80	5075	CA H6 H6 CL 04
57 PISAA	50	134	N H CL 04
57 PISAA	50	143	R CL 04
62 ACACA	15	1201	N H CL 04
71 JCSIA	1971	1371	CU (CL IO H312 ICL 04)2
70 ACACA	26	1928	N2 H5 CL 04
71 ACACA	27	898	H CL 04 IO 1/2 H2 0
73 INCAH	7	477	IC N12-TRILEN-CU CL 04
71 ACACA	27	898	H CL 04.2 1/2 H2 0
72 MRBUA	7	1281	CL1(+7) -0
71 JCSIA	1971	1857	CL1(+7) -0
62 ACACA	15	18	H3 0 CL 04 (1-80 C1
59 ACACA	25	1875	H3 0 H CL 04
73 ACASA	27	2309	(P84 IO H14)3 C 03 ICL 0410
73 ACASA	27	3523	CU (C3 H4 N214 ICL 04)2
LM+4 VI	67 INUCA	3	327 R (CH+4)
CO+2 IV	69 ZAACA	369	306 CO V2 04
CO+2 V	72 SCBCA	28	2803 CO2 P2 07 ALPHA
CO+2 VI	68 ZAACA	358	125 CO SE 04
68 ZKKA	126	298	CO GE 03
70 CJCHA	48	881	CO3 AS2 08
70 JPCSA	53	3279	BA CO F4
70 PERIA	3	181	CO2 S1 04
73 ACACA	29	2304	CO3 V2 08
71 HCACA	54	1621	CO3 IO H12 (S 04)2.2 H2 0
REF 1	CO2 S1 04		
72 ACACA	28	2883	CO2 P2 07
70 INDOCA	9	151	CO (OHMA)3 ICL 0412
73 ACACA	29	2741	CO S1 F4.6 H2 0
74 AMNIA	59	475	CO2 S1 04
74 JCLMB	4	55	C16 H18 CO 06
CO+2 VIII	66 INDOCA	5	1208 (AS1C6 H514)2(COIN 03)3
CO+3 VI	68 CJCHA	1968	871 CO (IN 03)3
68 CJCHA	46	3472	CO3 04
68 JACSA	88	2951	CO (C5 H7 02)3
74 ACACA	30	822	CO (H2 02)3
69 JACSA	91	6881	IN H416 (H4 CO2 MO10 0381
74 ZAACA	408	97	K CO2 04
CO+4 IV	71 ZAACA	386	1 BA2 CO 04
73 ZAACA	398	54	L18 CO 06
74 ZAACA	408	75	CS2 CO 03
74 ZAACA	409	152	K6 CO2 07
CO+4 VI	67 STGBA	3	1 R3 VS V (FLUORIDES)
74 ACACA	408	97	K CO2 04
CR+2 VI	71 ANCPA	6	41 TA2 CR 06
69 ACACA	25	925	R VS 0 ELECTRONS
CR+3 VI	69 MRBUA	4	621 NA3 CR F6
70 INDOCA	9	2289	NA3 ICR MO 06 024 H61.8 H2 0
70 SPMDA	15	902	NA2 CR3 08 0 H
73 MRBUA	8	593	CA CR F5
65 ACACA	19	131	CR (C5 H7 02)3
CR+4 IV	74 ZAACA	407	129 BA2 CR 04
CR+4 VI	72 MRBUA	7	157 CR 02
CR+5 VI	67 STGBA	3	1 R3 VS V (FLUORIDES)
CR+6 IV	68 CJCHA	46	935 K2 CR2 07
70 ACACA	26	222	CR 03
69 JCSIA	1969	1857	(HMH)2 CR 04
69 ACACA	25	1516	AG2 CR2 07
70 SPMDA	15	930	K2 CR 013
70 AMNIA	55	784	P82 CR2 05
70 ACASA	24	3627	NA2 CR3 08 0 H
71 SPMDA	15	820	NA2 CR2 07.2 H2 0

Table 2 (cont.)

74 ZAACA 403 1 R3 VS V (DY F3)	73 ACBCA 29 869 HG MO D4	74 ACBCA 30 2491 MG2 V2 D7
ER+3 VI 74 ACBCA 26 484 ER2 S12 D7	HO+3 VIII 74 ACBCA 30 2049 K MO BE F6	71 AMNIA 56 1593 MG 186 D7 (O M)61.2M2 U
ER+3 VII 74 ACBCA 26 484 ER2 S12 D7	70 SSCOA 8 1745 MO3 FES D12	73 AMNIA 56 1029 MG C D3
70 SPHCA 15 36 ER2 GE2 D7	72 BUCCA 95 437 MO P5 D14	74 CJCHA 52 1185 CA18 MG2 H2 (P D4)14
72 JCMLB 2 197 ER8 U (THD)10 (O M)12	74 ZAACA 403 1 R3 VS V (HO F3)	70 INOCA 9 151 MG (OMPA)3 (CL D4)2
ER+3 VIII 68 CHPLB 2 47 ER P D4; ER V D4	HO+3 IX 74 ZAACA 403 1 R3 VS V (HO F3)	72 CJCHA 50 3619 MG V2 U6
70 INOCA 9 1100 ER (C2 D4) (M C2 D4).JH2 D	74 ACBCA 30 2613 MOIC2 H5 S D4)3.9M2 D	73 ACBCA 29 2613 MG3 AS2 D8
70 SSCOA 6 1745 ER3 FES D12	74 INOCA 13 2535 HO1H2 D14 (M C 03)13.2M2 D	MG+2 VIII 73 ACBCA 29 266 CALCULATED
71 ACSAA 25 372 ER (M U C H2 C D D)13.2M2 D	73 CJCHA 53 831 (N D12)HO1N D15)1	MG+2 VI 70 AMNIA 55 1489 MN7 S8 AS D12
74 ZAACA 403 1 R3 VS V (ER F3)	74 INOCA 13 2535 HO1H2 D14 (M C 03)13.2M2 D	71 ACBCA 27 1044 MN CO CR D4
72 JCMLB 2 197 ER8 U (THD)10 (O M)12	71 JCPSA 54 2556 N H4 I D3	69 PHSSA 32 K91 MN CR2 D4
ER+3 IX 59 ZKKKA 112 362 ER (C2 M5 S D4)3.9M2 D	68 ACBCA 20 758 L1 I D3	73 ACBCA 29 266 CALCULATED
74 ZAACA 403 1 R3 VS V (ER F3)	66 ACBCA 20 801 L1 I D3	MG+2 VI 68 AMNIA 53 1841 MN2 O M AS D4
EU+2 VI 70 ZAACA 374 201 L1 EU3 D4	58 ACBCA 9 1015 CE (I 03)14	74 MPMTA 21 246 MN2 AS D4 OM
EU+2 VII 70 ZAACA 374 201 L1 EU3 D4	58 ACBCA 11 794 CE (I 03)14.M2 D	69 ACBCA 25 925 R VS O ELECTRONS
70 ZAACA 374 201 L1 EU3 D4	43 RTCPB 62 759 N H4 I D3	MG+2 VI 69 SCIEA 165 586 MN2 GE U4
69 ACBCA 25 1104 EU2 U (FE F3)	1+5 VI 71 JCPSA 54 2556 N H4 I D3	69 JCPSA 51 4928 BA MN F4
73 REF 3 112 EU5 D8	70 ACBCA 26 1782 NA I D4	70 ZKKKA 132 1 NM5 (O M)12 S12 D8
EU+2 VIII 73 RVCMA 10 77 EU CL2 EU F2	71 JCPSA 1971 1857 (I+7)U	69 AMNIA 54 1312 MN FE2 (P D4)12 (OH)2.8M2 D
UNPUL 73 RVCMA 10 77 EU CL2 EU F2	1+7 VI 71 ACBCA 20 765 H5 I U4	70 NJMIA 113 1 MN7 NA12 (S D4)13.15M2 D
EU+2 X 71 NATMA 58 218 EU2 S1 U4	65 ACBCA 19 629 K4 H2 I2 D10.8M2 D	65 ACBCA 19 854 MN S D4
EU+3 VI 68 REF 4 EU4 AL2 D9	37 JACSA 59 2036 (N H4)12 H3 I U6	72 AMNIA 57 621 MN2 GE D4
70 ZAACA 374 201 L1 EU3 D4	74 ZAACA 409 97 RB2 IN4 D7	67 PRALAA 92 125 MN C D3
73 REF 3 112 EU5 D8	73 ZAACA 395 280 SR2 IN2 D5	67 HCACA 50 2023 MN5 D8
EU+3 VII 68 REF 4 EU4 AL2 D9	IN+3 VI 74 ZAACA 409 97 RB2 IN4 D7	MG+2 VI 72 AMNIA 57 621 MN2 GE D4
73 REF 3 112 EU5 D8	IN+3 VII 74 ZAACA 409 97 RB2 IN4 D7	MG+2 VIII 69 ZKKKA 129 427 MN3 FE2 GE3 D12
EU+3 VIII 68 JCPSA 48 1094 EU3 FE2 GA3 D12	61 ACSAA 15 1437 (M O M S O4).1M2 D12	71 AMNIA 56 791 GARNETS
74 ZAACA 403 1 R3 VS V (EU F3)	68 ACBCA 24 388 L12 IN2 D5	73 SSCOA 12 109 MN3 AL2 GE3 D12
73 ACSAA 27 2827 EU2 (C3 H2 D4)3.8M2 D	70 ACSAA 24 1662 (M O D H)	74 JCPSA 49 1809 MN H4 D7
EU+3 IX 74 ZAACA 403 1 R3 VS V (EU F3)	69 INOCA 8 1985 IN2 D3	MG+3 VI 71 21 2871 MN2 D3
73 ACSAA 27 2827 EU2 (C3 H2 D4)3.8M2 D	74 ACBCA 30 2613 MOIC2 H5 S D4)3.9M2 D	67 ZKKKA 124 428 MN2 D3
71 ACSAA 25 3347 EU TRISOLYCOLATE	74 SPHDA 18 761 IN2 GE2 D7	68 ACBCA 24 1233 MN O D H
FE+2 IV SO HS 74 AMNIA 59 1166 BA FE S14 D10	IR+4 VI 71 JSSCB 3 174 SR IR D3	69 JCPSA 50 1068 (N H4)12 MN F5
FE+2 V HS 69 SCIEA 166 1399 (NA)M12 FE4 S112 D30.H2 D	IR+5 VI 74 MRBUA 9 1177 R3 VS V (CU2 IR2 D7)	65 PHSSA 3 K444 MN2 D3
69 ZAACA 369 306 FE V2 D4	K+1 IV 68 ZAACA 358 241 K AG D K2 D	68 BUCCA 91 339 TB MN D3; PR MN D3; NU MN D3
71 JUPSA 31 452 FE2 T1 D4	K+1 VI 51 ZAACA 264 144 K S8 F6	71 JSSCB 3 238 LA MN D3; MNS D4
72 JUPSA 33 1296 FE2 MO D4	68 SPHDA 12 1095 K F M2 D8	LA-55 CA-05 MN D3
FE+2 VI LS 69 ACBCA 25 925 R VS A (FE S2)	69 CCJDA 11 406 K2 F2 D5	73 JSSCB 6 16 NA MN7 D12
FE+2 VII HS 69 NMMA 1069 430 FE AL2 (P D4)12 (O M)12 (O M)12	K+1 VII 68 JCCHA 46 935 K2 CR2 D7	74 AMNIA 59 985 MG2 MN B D5
70 BUCCA 93 190 FE S D4	69 JCCHA 1969 849 K2 MO D4	68 ACBCA 24 1114 NA4 MN4 T15 D18
71 SPHCA 15 999 FE3 BE S13 D9 (F4)12 H2	71 SSCOA 9 335 K FE F4	74 INOCA 13 1854 MN (C7 M5 D2)13/4 C6 H5 CH3
67 ACBCA 22 775 FE (NH4)1215 D4)2.8M2 D	K+1 VIII 70 ZKKKA 74 306 K H2 P D4	74 INOCA 13 1864 MN (ACAC)3
68 CMYTA 68 290 L1 FE D3	62 ZKKKA 117 411 K2 T16 D13	MG+4 IV 73 JSSCB 13 275 R3 VS V (NA MN D4)
74 AMNIA 59 486 FE2 S1 D4	72 ZKKKA 98 286 K H2 (M5 D1) 85 D10	73 JSSCB 8 234 BA MN D3
FE+2 VIII 71 AMNIA 56 791 GARNETS	71 INUCA 7 873 K H2 C D4	69 INOCA 8 335 NA12 MN NB12 D38.50M2 D
71 ZKKKA 134 333 FE3 AL2 S13 D12	68 JCCHA 66 935 K2 CR2 D7	65 CZIPA 13 998 NA4 MN H1 D4)13.15M2 D
73 ACBCA 29 266 CALCULATED	70 JCCHA 1970 3092 K H2 (O M)12	67 HCACA 50 2023 MN5 D8; C2D MN3 D8
FE+3 IV HS 70 ACBCA 26 1469 CA2 FE2 D5	70 ZKKKA 132 27 K1.4 NA5.5 CA0.3 AL7.5	MG+5 IV 72 ACBCA 28 2845 K2 MN D4
70 SSCOA 8 1745 ER3 FES D12	69 ACBCA 25 400 L16 S D32	MG+7 IV 68 ACBCA 24 1053 AG MN U4
71 ACBCA 27 1263 BA FE2 D4	69 ACBCA 25 1919 K UZ F9	MG+8 IV 69 ACBCA 25 400 K3 MO CL6
71 MRBUA 6 725 BA CA FE4 D8	K+1 X 73 CJCHA 51 2613 K AL P2 D7	69 INOCA 8 2694 K3 MO F6
71 ACSAA 25 3616 CA2 FE2 D5	K+1 XII 68 SPHCA 13 420 K Y W2 D8	71 MRBUA 6 555 L12 MO F6
73 ACBCA 29 832 BA FE2 D4	71 INOCA 10 1264 K2 PB CU (N D2)16	MG+5 VI 71 INOCA 13 2715 R3 VS V (RE MO D4)
FE+3 V 71 JSSCB 4 1 FE V D4	67 INOCA 5 514 K2 BA CU (N D2)16	MG+6 VI 71 INOCA 10 922 BA2 ND MO D6
FE+3 VI HS 70 ACBCA 26 1469 CA2 FE2 D5	74 JACSA 96 6606 K2 CA CU (N D2)16	MG+7 IV 68 JCPSA 48 2619 CU MO D4
70 SSCOA 8 1745 ER3 FES D12	75 ACBCA 31 594 K2 BA CU (N D2)16	68 SPHDA 12 1095 K Y M2 D8
71 SSCOA 9 335 K FE F4	57 PISAA 50 143 K CL D4	69 JCCHA 1969 849 K2 MO D4
71 JSSCB 4 1 FE V D4	LA+3 VI 69 ZKKKA 129 259 CU LA D2	72 ACBCA 28 60 GU2 MO3 D12
71 JCPSA 32 1315 L1 FE D3	73 MRBUA 8 1269 R3 VS V (REZ M3 D12)	68 JCPSA 50 86 GU2 MO3 D12
71 ACSAA 25 3616 CA2 FE2 D5	LA+3 VIII 59 1277 LA5 MG2 T13 S14 D22	71 SPHCA 15 829 K AL M2 D8; K FE M2 D8
67 ACBCA 23 239 FE (C5 M7 D2)13	73 ACBCA 29 2074 LA2 MO3 D12	71 JCPSA 55 1093 CA MO D4; MO MO D4
69 CCJDA 1969 440 FE (C7 M5 D2)13	68 INOCA 7 2295 LA (C5 M7 D2)13	73 ACBCA 29 2074 LA2 MO3 D12
FE+3 VIII 73 JSSCB 8 331 ESTIMATED	74 ZAACA 403 1 R3 VS V (LA F3)	71 JCCHA 1971 1857 MO(+6) - D
FE+3 VI 73 JSSCB 8 331 R3 VS V (ISA FE D3)	74 SPHCA 18 675 LA2 SR3 (B D3)14	67 CCJDA 1967 374 K2 MO3 D10
FE+3 VII 73 JSSCB 8 43 K2 FE D4	LA+3 IX 71 MRBUA 6 23 LA FE D3	68 JCCHA 1968 1398 K2 MO3 D10
73 JSSCB 8 43 K2 FE D4	74 ZAACA 403 1 R3 VS V (LA F3)	69 JCCHA 1968 1398 K2 MO3 D10
GA+3 IV 71 ACBCA 27 616 L15 GA D4	74 AMNIA 59 1277 LA5 MG2 T13 S14 D22	68 JCCHA 1968 1398 K2 MO3 D10
75 ACBCA 31 500 SR GA2 S12 D8	L1+1 VI 39 ZKKKA 102 119 L1 O M H2 D	70 JSSCB 1 486 AG6 MO3 D33
74 ACBCA 30 1364 C15 H21 D6 GA	70 ZAACA 39 1977 L1 C D2	70 INOCA 9 2228 NA3 (CR MO D6)24 H61.8M2 D
GD+3 VII 70 ACBCA 26 484 GD2 S12 D7	71 AMNIA 56 18 NA3 AL2 L13 F12	70 ACSAA 24 3711 L1 MO D2 AS D4
72 ACBCA 28 60 GD2 MO3 D12	71 ACBCA 27 616 L15 GA D4	66 ACBCA 20 2698 MO F6 (GA)5
72 SPHCA 16 790 GD2 GE2 D7	73 JSSCB 6 530 L13 V D4	70 CCJDA 1970 50 MO D3 H2 D12
69 IVNMA 5 1823 GD9.33 S16 D26	73 ACBCA 29 2625 L1 (N2 M5) BE F4	72 ACBCA 28 2222 MO D3.2M2 D
72 JSSCB 5 266 GD9.33 S16 D26	64 ACBCA 17 703 L12 C2 D4	64 INOCA 3 1803 K2 (MO D2 (C2 D4) H2 D12 D
GD+3 VIII 71 SPHCA 15 926 NA GD S1 D4	74 ACBCA 30 2434 L12 BE S1 D4	73 ACBCA 29 869 MG MO D4
72 SPHCA 16 790 GD2 GE2 D7	L1+1 VI 68 ACBCA 24 225 L13 AL F6	74 ACBCA 30 1795 MO D3M2 D
74 ZAACA 403 1 R3 VS V (GD F3)	69 ZAACA 371 306 L12 ZR O D4	N+3 IV REF 6 MG3 N2.513 N4.8 N.TI N
GD+3 IX 72 SPHCA 16 790 GD2 GE2 D7	70 ZKKKA 132 118 L12 AL2 S13 D10	N+5 III REF 6 NM4 N O3.NA N O3.K N O3; BAIN D3)2.TIIN D3)14
69 IVNMA 5 1823 GD9.33 S16 D26	71 MRBUA 6 555 L12 MO F6	NA+1 IV 74 ZAACA 409 69 NA6 IN D4
74 ZAACA 403 1 R3 VS V (GD F3)	59 ACBCA 19 561 L1 C6 U7 H7	REF 2 NA2 O
GE+4 IV 68 ZKKKA 126 299 CU GE D3	74 ACTEA 86 819 L1 NB D2	68 ACBCA 24 1077 NA2 S12 D5
69 SCIEA 165 586 MN2 GE D4	68 CMYTA 68 250 L1 FE P D4	68 SPHDA 12 987 NA2 ZN2 S12 D7
69 ZKKKA 129 427 MN3 FE2 GE3 D12	71 ACSAA 25 3337 L1 MO3 D8	64 JACSA 329 110 NA2 MG D2
70 JSSCB 2 612 MG28 GE10 D48	73 CJCHA 51 265 L1 V D3	NA+1 VI 74 1287 NA4 SN2 GE4 D12 (O M)14
71 SPHCA 15 926 NA SN2 GE4 D12 (O M)14	73 ACBCA 29 2294 L12 ZR F6	65 ACBCA 19 561 NA CA D7 H7
70 ACSAA 24 1287 NA4 SN2 GE4 D12 (O M)14	70 ZAACA 377 70 CA LUG D4	63 ACCRA 15 1233 NA B (OH)4.2M2 D
67 ACBCA 21 1281 NA8 SN4 GE10 D30 (O M)14	71 JACCA 4 284 LU B D3	60 EKKRA 113 430 NA2 AL2 S13 D10.2M2 D
70 MOCBM 102 906 NA2 GE D3	LU+3 VI 74 ZAACA 403 1 R3 VS V (LU F3)	58 EKKRA 111 241 NA CL D3
71 MOCBM 102 1245 K2 GE4 D9	MG+2 IV 72 ACBCA 28 267 K2 MG5 S112 D30	56 ACBCA 9 811 (NA AS D3)1X
72 SPHCA 17 244 CU GE D3	22 ACBCA 5 684 MG AL2 O4	53 ARKEA 8 77 NA 38 F4
72 MOCBM 103 1560 GE5 D (P D4)16	72 ACBCA 28 3583 K2 MG5 S116 D15	59 ACBCA 12 526 NA U ACETATE
GE+4 VI 70 SSCOA 1 557 CA2 GE D4	68 ACSAA 22 1966 MG3 P2 D8	74 ACBCA 30 1872 NA2 N D4
70 JSSCB 2 612 MG28 GE10 D48	66 NMMA 1966 142 MG B4 D7	75 ACBCA 31 890 K2 C O3.H2 D
71 MOCBM 102 1245 K2 GE4 D9	UNPUL MG2 P2 D8	NA+1 VII 71 926 NA GD S1 D4
71 ACBCA 27 2133 GE D2	MG+2 VI 65 CJCHA 43 1139 MG2 P2 D7	70 NJMIA 113 1 MN7 NA12 (S D4)13.15M2 D
72 AMNIA 57 62 MN2 GE D4 DELTA	63 BAPCA 11 361 MG2 AS2 D7	73 SPHCA 29 890 NA2 CR2 OT ALPHA
72 ZKKKA 136 387 GE (O M)1 P D4	70 ACBCA 26 1429 MO N H4 P D4	68 ACBCA 24 1703 NA B F4
72 MOCBM 103 1560 GE5 D (P D4)16	69 INOCA 8 1065 C54 MG3 F10	68 SPHDA 12 987 NA2 ZN2 S12 D7
MG+2 I 57 JUMSA 1 43 T F	69 ZKKKA 129 427 MN3 FE2 GE3 D12	71 AMNIA 56 18 NA3 AL2 L13 F12
66 JCPSA 45 275 M F	65 MMLD 1965 195 MG AL B U4	NA+1 XII 71 JSSCB 3 89 NA13 NB35 D94
MG+2 IV 73 JSSCB 13 275 R3 VS V (NA MN D4)	69 SPHCA 13 933 M H4 S D2	72 ZKKKA 81 135 NA AL S1 D4
70 JACCA 53 126 MF D2	70 JSSCB 2 612 MG28 GE10 D48	MG+2 VI 74 ACBCA 30 1795 MO D3M2 D
69 ACSAA 27 3347 MF4 (OH)18 (CR D4)14.2M2 D	65 MMLD 1965 195 MG AL B U4	NA+1 VIII 68 JCPSA 48 2619 CU MO D4
73 ACSAA 27 2455 MF (O M)12 S O4	70 BSCCA 1970 4243 MG S D4.H2 D	70 JSSCB 1 439 M-NB2 D5
MG+2 VI 71 CCJDA 1971 468 MG2 F2	71 ACBCA 27 815 M4 TE D6	45 NA2 MN D11
MG+2 II 71 JCCHA 1971 1857 MO(+6) - D	68 ACSAA 22 1466 MG3 P2 D8	70 AMNIA 55 90 CA NB2 D6
	70 RIF 1 CA MG S1 D4	55 PRVAA 98 903 CU2 NB2 D7
		71 JSSCB 3 89 NA13 NB35 D94
		74 JINCA 380 119 MN NB2 D6
		71 JCCHA 1971 1280 D13 NB17 Q47

Table 2 (cont.)

70 ACBCA	26	105	BA3	S14	NB6	D26		
71 ACSAA	25	3347	L1	NB3	O8			
59 SPHCA	4	796	LY	YB1	NB	O4		
73 JSSCA	4	150	B1	NB	O4			
66 ACSAA	20	72	NB	P	O5			
74 BUCFA	97	3	NA3	NB	O4			
NB+5 VI								
70 JSSCB	1	454	NA2	NB	O11			
71 JSSCB	1	89	NA12	NB	O9			
71 ACBCA	27	1610	(NH4)3	NB	O	IC2 O413.H2 O		
75 ACBCA	31	673	NB2	O5				
ND+2 VII								
UNPUL						ND 12		
ND+2 IX						ND CL2, ND BR2		
ND+3 VI								
71 INDOCA	10	922	BA2	ND	ND	O6		
74 MRBUA	9	1661	ND	BA3	BA	O12		
ND+3 VII								
69 JCPFA	50	86	ND2	MO3	O12			
71 JSSCB	3	458	ND	V	O4			
70 SPHCA	14	518	R	ND	M2	O8		
70 ACBCA	26	1484	ND2	T12	O7			
70 ACSAA	26	3408	ND4	RE2	O11			
71 SPHDA	15	636	ND2	M	O6			
71 SPHCA	15	991	ND4	M5	O15			
74 MRBUA	9	129	ND	P5	O14			
74 ZAACA	403	1	R3	VS	V	(ND F3)		
74 ACBCA	30	468	ND	P3	O9			
ND+3 IX								
70 ACSAA	24	2969	ND2	IC2	O413.10.H2 O			
71 SPHCA	15	2791	ND2	IC3	O413.10.H2 O			
73 ACSAA	27	2441	ND2	IC3	H2	O413.8H2 O		
74 ZAACA	403	1	R3	VS	V	(ND F3)		
73 ACSAA	27	2815	ND2	IC3	H2	O413.6H2 O		
73 ACSAA	27	2973	ND	OH	C	O3		
74 AMHIA	59	1277	ND4	MG2	T13	S14	O22	
ND+3 XII								
72 JSSCB	4	11	ND	AL	O3			
NI+2 IV								
61 JAPFA	32	685	NI	CR2	O4			
65 BSCFA	1965	1085	SPINELS					
NI+2 IV SO								
66 INDOCA	5	1200	NI	(DPH)2				
NI+2 V								
67 BAPCA	15	47	NI2	P2	OT			
NI+2 VI								
74 AMHIA	59	486	NI2	S1	O4			
74 ACBCA	30	1686	NI	(PY N	D16	1B F412		
68 ZAACA	358	125	NI	SE	O4			
67 BAPCA	15	47	NI2	P2	OT			
70 ACBCA	26	1464	R8	NI	F3			
70 ZAACA	378	129	SR2	NI	TE	O6		
70 JSSCB	2	416	R8	NI	F3			
71 PHSSA	438	125	NI	(O	H12			
70 REF	1							
64 ACBCA	17	1481	NI	(C5	MT	O212.2H2 O		
73 ACBCA	29	2741	NI	(F6	OH2	O		
63 ZKKA	118	291	NI	(H	O	O12.2H2 O		
74 JCPFA	61	852	NI	(C4	OH4	2H2 O		
73 JCHLS	3							
73 ACBCA	29	2304	NI3	V2	O8			
NI+3 VI								
74 ZAACA	405	167	M4	NI	F6			
71 CHDOCA	272	2163	HO	NI	O3			
NI+3 VI HS								
54 JACSA	76	1499	NA	NI	O2			
NI+4 VI LS								
67 STGBA	3	1	R3	VS	V	(FLUORIDES)		
74 JINCA	36	1561	K2	NI	TE	O4		
ND+2 VI								
74 INDOCA	13	2233	ESTIMATED					
NP+3 VI								
68 JINCA	30	823	NP	CL3				
NP+4 VI								
67 INUCA	3	327	ESTIMATED					
74 CJCHA	52	2175	R3	VS	V			
NP+6 VI								
						R3 VS V (BA2 SR NP O6)		
OH-1 III								
71 AMHIA	56	1155	MG6.6	FE4	S13	O12 F O H, R10H-11(RF-11)+O4		
OH-1 III								
71 AMHIA	56	1155	MG6.6	FE4	S13	O12 F O H, R10H-11(RF-11)+O4		
OH-1 IV								
						R10H-11(RF-11)+O4		
OH-1 VI								
						R10H-11(RF-11)+O4		
OS+4 VI								
69 JCDOA	17	459	OS	O2				
70 ACSAA	24	123	OS	O2				
OS+5 VI								
71 JCSIA	1971	2789	OS	F5				
74 SSCOA	14	357	R3	VS	V	(CO2 OS2 OT)		
OS+6 VI								
65 JINCA	2	79	K	OS	F6			
OS+7 VI								
						R3 VS V (PEROVSKITES)		
OS+8 IV								
						R3 VS V (PEROVSKITES)		
OS+8 IV								
66 ACSAA	20	395	OS	O4				
73 ACBCA	29	1983	OS	O4				
65 ACBCA	19	157	OS	O4				
71 JCSIA	1971	1857	OS(8+)	-O				
PA+5 IV								
72 ACBCA	28	2883	CO2	P2	OT			
68 CJCHA	46	605	CO2	P2	OT			
65 CJCHA	43	1159	MO2	P2	OT			
68 INDOCA	7	1345	CA2	P2	OT			
71 BSCFA	1971	426	2R	P2	OT			
70 ACBCA	26	1826	M3	P	O4.1/2	H2 O		
71 NJMMA	1971	241	SR	AL3	(P	O412 IO H15.H2 O		
69 ZKKA	130	148	R	ZR2	(P	O413		
71 ACBCA	27	2124	NA3	P	O4.12H2 O			
68 ACSAA	22	1822	NA	R2	P1	O12		
68 ZKKA	127	21	AL3	P2	O8.5H2 O			
68 CJCHA	18	290	LI	FE	O4			
70 ACBCA	26	1826	M3	P	O4			
72 AMHIA	57	45	NA45	FE	35	P	D4	
72 ACBCA	28	2005	(H	NH4)2	M	P	O4	
73 ACBCA	29	141	LU	P	O4			
71 ACBCA	27	2247	CA	1H2	P	O412.H2 U		
73 ACBCA	29	2242	AL	P	O4.2H2 O			
71 ACSAA	25	512	K	H5	(P	O412		
70 JSSCB	1	120	ZH2	P2	OT			
PA+5 V								
67 JACSA	89	2268	C23	H29	OS	P		
67 JACSA	89	2270	C23	H29	OS	P		
PA+5 VI								
71 ZAACA	380	51	P	CL5				
72 CCJDA	1972	676	ET3	M	(C6	HA	O213	P
74 ACBCA	29	246	CALCULATED					
PA+4 VI								
67 INUCA	3	327	R	(PU+4)				
74 CJCHA	52	2175	R3	VS	V			
PA+5 VI								
71 ACBCA	27	731	R	PA	O3			
PA+5 IX								
67 JCSIA	1967	1429	K2	PA	F7			
PB+2 IV PY								
68 ZKKA	126	98	P8	S1	O3			
PB+2 VI								
70 ACACB	26	501	P82	O3				
PB+2 VII								
69 ZKKA	128	213	P8	CA2	S13	O9		
64 ACBCA	17	1539	P8	P2	O6			
PB+2 VIII								
71 SPHCA	15	928	P8	M	O4			
64 ACBCA	17	1539	P8	P2	O6			
73 CJCHA	51	70	P82	V2	OT			
72 MRBUA	7	1025	B1	TITANATES				
PB+2 IX								
67 ACBCA	22	744	P8	F2				
73 CJCHA	51	70	P82	V2	OT			
74 ZKKA	139	215	P8	C	O3			
74 CJCHA	52	2701	P8	V2	O6			
PB+2 X								
70 ZKKA	132	228	P83	P2	O8			
PB+2 XII								
57 ACBCA	10	103	P8	(N	O312			
							R3 VS V (BA S O4)	
70 ZKKA	132	228	P83	P2	O8			
71 INDOCA	10	1264	K2	P8	CU	1N	O216	
PB+4 IV								
72 JCSIA	1972	2448	R3	VS	V	(NA4	PB	O4)
PB+4 V								
70 ZAACA	375	255	R82	P8	O3			
PB+4 VI								
60 ACACB	26	501	P82	O3				
65 JINCA	27	1509	P83	O4				
74 CJCHA	52	2175	R3	VS	V			
PD+4 VII								
68 MRBUA	3	153	P8	O2				
PD+2 IV SO								
67 INDOCA	6	730	PD	(C6	H5	CH3	CH1C	O212)
68 JSTCA	9	166	PD	(IC6	HS12	CH	CH2	O212)
PD+4 VI								
68 MRBUA	3	699	R3	VS	V	(M2	PD2	OT)
73 INDOCA	12	1726	KE	PD	F11			
61 JCSIA	1961	3728	K2	PD	F6			
PM+3 VI								
PM+3 VIII								
74 ZAACA	403	1	R3	VS	V	(PH	F3)	
PM+3 IX								
74 ZAACA	403	1	R3	VS	V	(PH	F3)	
PD+4 VI								
74 CJCHA	52	2175	R3	VS	V			
PD+4 VIII								
							R3 VS V (FLUORITE)	
PR+3 VI								
71 MRBUA	6	545	R3	VS	V	(PR2	MO3	O12)
PR+3 VIII								
70 SPHCA	15	28	PR2	M2	O9			
74 ZAACA	403	1	R3	VS	V	(PR	F3)	
PR+3 IX								
70 SPHCA	15	28	PR2	M2	O9			
59 ZKKA	112	362	PR	(C2	H5	S	O413.2H2 O	
74 ZAACA	403	1	R3	VS	V	(PR	F3)	
PR+4 VI								
72 ACBCA	26	956	BA	PR	O3			
75 ACBCA	31	971	PR2	O12				
73 JSSCB	8	331	R	(PR+4)				
74 CJCHA	52	2175	R3	VS	V			
PT+2 IV SO								
72 REF	5							
PT+2 VI								
69 JINCA	31	3803	PT	O2				
74 CJCHA	52	2175	R3	VS	V			
PT+5 VI								
67 STGBA	3	1	R3	VS	V	(FLUORIDES)		
67 JCSIA	1967	478	KE	PT	F11			
PUR+3 VI								
67 INUCA	3	327	R	(PU+3)				
75 JINCA	37	743	R	(PU+3)				
PUR+4 VI								
67 INUCA	3	327	R	(PU+4)				
73 JSSCB	8	331	R	(PU+4)				
74 CJCHA	52	2175	R3	VS	V			
PUR+6 VI								
							R3 VS V (BA2 SR PU O4)	
RB+1 VI								
70 ZAACA	375	255	R82	P8	O3			
RB+1 IX								
74 ACBCA	30	1640	R82	S	O4			
RB+1 XI								
74 ACBCA	30	1640	R82	S	O4			
RB+1 XII								
70 ACBCA	26	1464	R8	NI	F3			
70 JSSCB	2	416	R8	NI	F3			
70 JSSCB	2	582	R8	NI	F3			
RB+1 XIV								
65 ACBCA	19	205	RB	U	O2	IN	O312	
RE+4 VI								
68 INDOCA	7	108	LA4	RE6	O19			
74 CJCHA	52	2175	R3	VS	V			
RE+5 VI								
70 ACSAA	24	3406	ND4	RE2</				

Table 2 (cont.)

72 ACBCA 28 956 BA T8 03	71 JINCA 33 2867 CR2 U 06	69 PHSSA 32 K91 ZN FE2 04
TC+5 VI 67 STBGA 3 1 R3 VS V (FLUORIDES)	72 ACBCA 28 3609 U 02 0 H12	73 ACBSA 27 1541 ZN S 03.2 1/2H2 U
TC+7 IV 69 ACIEA 8 381 TG2 07	73 ACBCA 29 7 U F6	64 INDOCA 3 245 ZN 0PMH2
71 ZAACA 380 146 TG2 07	U6+ VII 72 ACBCA 28 3609 U 03	ZN+2 V 70 JSSCB 1 120 ZN2 P2 07
TE+4 IV 69 ACBCA 25 1551 H3 FE2 TE4 012 CL	U6+ VIII 69 ACBCA 25 787 CA U 04	73 CJCHA 51 1004 ZN2 V2 07
71 ACBCA 27 602 T1 TE3 08, 3N TE3 08, TE 02, HF TE3 08, ZR TE3 08	69 ACCRA 19 205 RB U 02 (IN 0313)	71 AMHIA 56 1147 ZN4 AS2 08 0 H12.2H2 0
71 ACBCA 27 608 U TE3 09	V+2 VI UNPUS V F2	ZN+2 VI 65 CJCHA 43 1147 ZN2 P2 07
TE+4 VI 61 ZKKA 116 345 TE 02	V+3 VI 70 PRBBA 2 3771 V2 03	68 SPHCA 13 127 ZN 04
71 ACBCA 27 602 M TE3 08	69 ACBCA 25 1354 V IC5 H7 0213	70 JSSCB 1 120 ZN2 P2 07
71 ACBCA 27 608 U TE3 09	69 ZAACA 369 306 M V2 04	71 CJCHA 49 3056 ZN3 V2 08
TE+6 IV 71 JCISA 1971 1857 TE(+6)+0	74 MRBBA 9 1091 UVO-99 CR0.0112 03	73 ACBCA 29 2741 ZN S1 F6.4H2 0
TE+6 VI 70 ZENBA 24 647 L16 TE 06	70 JCPCA 31 2569 V2 03	73 ACBSA 27 1541 ZN S 03.2 1/2H2 0
70 MRBBA 5 109 M03 TE 06	V4+ V 65 ACBSA 19 432 L1 V2 05	75 JSSCB 13 275 R3 VS V (M4 ZR 04)
69 ACBSA 23 3062 NA2 KA TE2 08 0 H12 1H2 0114	61 JCPSA 35 55 V 0 IC5 H7 0212	ZR+4 V 69 CCJDA 1969 727 K2 ZR 03
64 INDOCA 3 634 K TE 0 10 H15.2H2 0	73 ACBCA 29 269 CA V3 07	70 JSSCB 2 410 K2 ZR 03
64 NATMA 51 552 K TE 0 H	73 ACBCA 29 1335 CA V4 09	ZR+4 VI 69 ACBSA 25 2658 ZR 1H AS 0412.H2 0
66 ACBSA 20 2138 K4 TE2 06 0 H14.H2 0	V4+ VI 72 JSSCB 5 446 CU V 03	69 ZAACA 371 306 L12 ZR 03
70 NATMA 57 393 M03 TE 06	61 JSSCB 6 419 V4 07	70 JSSCB 1 478 K2 ZR2 05
70 ZAACA 378 129 SR2 NI TE 06	72 PRBBA 5 2541 V 02 CR	68 ACBSA 22 1822 NA ZR2 P3 012
70 ACBSA 24 3178 TE 10 H16	74 ACBSA 30 2644 V3 07	73 ACBCA 29 2294 L12 ZR F6
68 ACBSA 20 1535 TE F6	71 ACBSA 25 2675 V6 013	71 ACBCA 27 1944 RB5 ZR F21
71 ACBCA 27 615 M03 TE 06	70 ACBSA 24 420 V02	74 CJCHA 52 2175 R3 VS V
65 ZAACA 334 225 K TE 02 0 H13	74 PRBBA 10 490 V02	ZR+4 VII 69 ACBCA 25 2164 NA2 ZR F6
68 CHODA 267 1435 02 TE 06	V5+ IV 68 ACBCA 24 292 Y V 04	70 ACBCA 26 417 (H M13) ZR F7
69 MOCBM 100 1809 AG2 TE 02 0 H14	68 CHPLB 2 47 ER V 04	70 JACTA 53 126 ZR 02
71 BUFGA 94 172 TE 10 H16	67 ACBSA 25 250 H7 H2 07	73 ACBSA 27 177 ZR4 0 H16 (CR 0415.H2 0
73 ACBCA 29 643 TE 06	70 ZKKA 131 161 BA3 (Y 0412	73 ACBSA 27 2614 ZR 10 H12 S 04.H2 0
73 ACBCA 29 956 H2 TE2 06	71 JSSCB 3 458 ND V 04	71 ACBCA 27 1944 RB5 ZR F21
73 ACBSA 27 85 TE 10 H16	27 71 ACBSA 29 2259 CAZ V 04 CL	ZR+4 VIII 69 ACBSA 25 1558 ZR2 S 0414 1H2 018.6H2 0
74 ACBSA 29 2976 NA3 BE TH10 P45	71 CJCHA 49 1629 M03 V2 08	69 ACBSA 25 1566 ZR2 S 0414 1H2 018.2H2 0
74 ACBCA 30 2095 (IN H416 1T6 M06 024) TE (H016 7H2 0	71 ACBSA 29 2361 001 V2 08, N13 V2 08	69 ACBSA 25 1572 ZR2 S 0414.5H2 0
	72 JSSCB 4 29 FE V 04	71 AMHIA 56 782 ZR S1 04
TH+4 VI 74 CJCHA 52 2175 R3 VS V	73 CJCHA 51 1004 ZN2 V2 07	63 INDOCA 2 243 ZR 1ACAC14
TH+4 VIII 71 ACBCA 27 629 K5 TH F9	71 CJCHA 49 3056 ZN3 V2 08	63 INDOCA 27 1944 RB5 ZR F21
71 ACBCA 27 2290 K7 TH F31	73 JSSCB 6 518 L13 V 04	63 INDOCA 2 250 NA4 ZR 1C2 0414.3H2 0
74 ICHAA 8 273 K TH P3 010	72 CJCHA 50 3944 C03 V2 07	
TH+4 IX 68 CCJDA 1968 990 (IN H414 TH F8	71 CJCHA 51 1004 ZN2 V2 07	HEF 1 G. E. BROWN, PH.D. THESIS, VIRGINIA
69 ACBSA 25 1958 (IN H414 TH F8	73 ACBCA 29 141 Y V 04	POLYTECH. INST., UNIV. MICROFILMS, 78-498
68 CCACA 40 147 K TH2 P3 012	73 ACBSA 29 1338 CUS V2 010	REF 2 R.W.C. WYCKOFF, CRYSTAL STRUCTURES, WILEY, N.Y., 1965
70 ICHAA 4 571 NA TM2 (P 0413	74 ACBSA 30 1678 NA V 03	REF 3 H.BARNIGHAUSEN ET AL., PROD. 10TH R.E. RES. CONF. CAREER, ARIZ. 1973, 490
71 ACBCA 27 1823 RB TH F13	74 NJMMA 5 2110 CS (V 0413 0 H	REF 4 C.BRANDLE, STEINFINK, PROD. 7TH R.E. RES. CONF., CORONADO, CAL. OCT. 28, 1968
71 ACBSA 29 2976 NA3 BE TH10 P45	V4+ V 50 ACBSA 4 1119 V2 05	REF 5 R.D. SHANNON, U.S. PAT. 3,663,181, MAY 16, 1972
70 ACBSA 26 1185 K NA TH F6	71 RVCAZ 4 509 M03 V2 05	REF 6 W.H. BAUR, NITROGEN, HANDBOOK OF GEUECHEM, SPRINGER-VERLAG, N.Y., 1974
71 ACBCA 27 2279 (IN H413 TH F7	74 ACBSA 30 2644 V3 07	REF 7 A.W. SLEIGHT, U.S. PAT. 3,869,954, NOV. 19, 1974
TH+4 X 73 ACBCA 29 2687 TH (IN 0314 (1G H513 P 012	74 ACBSA 30 2644 V3 07	UNPUB. H.BARNIGHAUSEN, PERSONAL COMMUNICATION
TH+4 XI 68 ACBSA 20 842 TH (IN 0314.5H2 0	73 ACBSA 29 587 RB V2 07	UNPUB. A.W. SLEIGHT, PERSONAL COMMUNICATION
66 ACBSA 20 836 TH (IN 0314.5H2 0	70 CHODA 270 952 CA V2 06	UNPUB. C. CALVO, PERSONAL COMMUNICATION
TH+4 XII 65 ACBSA 18 698 MG TH (IN 0316.8H2 0	V4+ VI 50 ACBSA 4 1119 V2 05	UNPUB. C.T. PREWITT, PERSONAL COMMUNICATION
TI+3 VI 73 JSSCB 6 213 TH 07	71 ACBSA 25 2675 V6 013	UNPUB. W.H. BAUR, PERSONAL COMMUNICATION
63 PHRVA 130 2230 T12 03	72 CJCHA 50 3619 MG V2 06	ACACB ACTA CRYST. SECT. A
74 JSSCB 9 255 T12 03	73 CJCHA 51 2184 K3 V 02 C2 04.3H2 0	ACBCA ACTA CRYST. SECT. B
74 ACBSA 30 662 CS T1 15 0412.1H2 0	73 ACBSA 29 1743 CU V2 06	ACBSA ACTA CRYST. SECT. C
TI+4 IV 67 STBGA 3 1 R3 VS V (FLUORIDES)	V5+ VI 67 STBGA 3 1 R3 VS V (FLUORIDES)	ACBSA ACTA CRYST. SECT. D
73 ACBCA 29 2009 BA2 T1 04	M6+ IV 25 1704 K2 M 04	ACBSA ACTA CRYST. SECT. E
61 ACBSA 14 875 BA2 T1 04	69 ACBSA 15 636 ND2 M 06	ACBSA ACTA CRYST. SECT. F
71 JCISA 1971 1857 T1(+4)+0	71 SPHCA 15 928 RB M 04	ACBSA ACTA CRYST. SECT. G
74 ZAACA 408 60 RB2 T1 03	72 ACBSA 28 3174 SN 04	ACBSA ACTA CRYST. SECT. H
TI+4 V 68 ACBCA 24 1327 V2 T1 05	71 JCPSA 55 1093 SR M 04, BA M 04	ACBSA ACTA CRYST. SECT. I
TI+4 VI 70 ZKKA 131 278 V2 T12 07	71 JCISA 1971 1857	ACBSA ACTA CRYST. SECT. J
71 ACBCA 27 635 NE M6 T1 F6	74 ACBSA 30 1872 NA2 M 04	ACBSA ACTA CRYST. SECT. K
71 JSSCB 3 340 T14 07	74 ACBSA 30 1878 AL2 (IN 0413	ACBSA ACTA CRYST. SECT. L
70 ACBCA 28 336 BA T1 03	M6+ V 74 ACBSA 30 2587 CA3 M 05 CL2	ACBSA ACTA CRYST. SECT. M
64 ACBSA 17 240 CO T1 03	M6+ VI 69 ACBSA 13 933 MG M 04	ACBSA ACTA CRYST. SECT. N
71 JCPSA 55 3266 T1 02	69 SSCDA 7 1797 B12 M 06	ACBSA ACTA CRYST. SECT. O
72 CSCMC 1 1 BA T16 013	70 SPHCA 14 518 K ND (IN 0412	ACBSA ACTA CRYST. SECT. P
72 ZKKA 136 273 T1 02	74 SPHCA 14 515 L12 FE (M 0412	ACBSA ACTA CRYST. SECT. Q
74 ZKKA 139 103 K T1 P 05	70 SPHCA 15 28 PR2 M2 09	ACBSA ACTA CRYST. SECT. R
72 INDOCA 11 2989 (T1 01C5 H7 021212	70 ACBSA 26 1020 CU M 04	ACBSA ACTA CRYST. SECT. S
74 ICHAA 11 243 (NH412 T1 01C2 0412.H2 0	70 JSSCB 2 278 L1 FE (M 0412	ACBSA ACTA CRYST. SECT. T
74 ACBSA 30 2894 BA T12 05	66 ACBSA 20 2698 M F6 1GAS1	ACBSA ACTA CRYST. SECT. U
74 CJCHA 52 2175 R3 VS V	72 ZENBA 27 203 SN M 04	ACBSA ACTA CRYST. SECT. V
TI+4 VIII 68 JCISA 1966 1496 T1 (IN 0314	71 SPHCA 15 991 ND4 M3 015	ACBSA ACTA CRYST. SECT. W
TL+1 VI R3 VS V (MF)	74 JSSCB 10 5 FE2 M 06	ACBSA ACTA CRYST. SECT. X
TL+1 VIII 75 ACBSA 31 365 TL N 03	X ACBSA 30 2069 BA M 04	ACBSA ACTA CRYST. SECT. Y
TL+3 IV 71 JCISA 1971 1857 XE(+8)+0	71 JCPSA 52 812 XE 04	ACBSA ACTA CRYST. SECT. Z
71 ZAACA 381 129 L15 TL 04	71 JCISA 1971 1857 XE(+8)+0	
73 ACBSA 396 113 SR4 TL2 07	XE+8 VI 64 INDOCA 3 1412 NA4 XE 06.0H2 0	
74 ACBSA 405 197 BA2 TL2 05	64 INDOCA 3 1417 NA4 XE 06.0H2 0	
TL+3 VI 68 ZKKA 126 143 TL2 03	Y+3 VI 67 ACBSA 22 354 V2 BE 04	
74 ZAACA 405 197 BA2 TL2 05	68 ZAACA 358 138 SR Y2 04	
75 ZAACA 412 37 RB TL F4	67 SPHCA 11 583 NA Y S1 04	
TL+3 VIII 72 ZAACA 393 223 TL F3	69 ACBSA 25 2140 Y2 03	
TM+2 VI UNPUB. TM 12	71 SPHCA 15 806 Y2 S1 05	
TM+2 VII UNPUB. TM CL2, TM BRZ	71 JCISA 1974 229 C66 H72 13 N12 06 Y	
TM+3 VI 63 PHSSA 3 K446 TM2 03	Y+3 VII 68 INDOCA 7 1777 YIC65C0CCH313.H20	
TM+3 VIII 70 SSCDA 8 1749 TM3 FE5 012	Y+3 VIII 68 ACBSA 24 292 Y V 04	
74 ZAACA 403 1 K3 VS V (TM F3)	57 ACBSA 10 239 Y3 FE5 012	
TM+3 IX 74 ZAACA 403 1 K3 VS V (TM F3)	68 SPHCA 12 1095 K Y ND2 08	
UN+3 VI 74 ZAACA 403 1 K3 VS V (TM F3)	69 SPHCA 13 420 K Y W2 08	
UN+3 VII 68 JINCA 30 823 R (U+3)	70 ZKKA 131 278 V2 T12 07	
UN+3 VIII 73 JSSCB 8 331 R3 VS V	67 ACBSA 23 939 Y T4 04	
67 CJCHA 52 2175 R3 VS V	74 ZAACA 403 1 R3 VS V (Y F3)	
UN+3 IX 70 ACBSA 26 38 (IN H414 U F6	Y+3 IX 69 ZKKA 112 362 Y (CZ H5 S 0413.9H2 0	
73 ACBSA 29 1442 U CL4	74 ZAACA 403 1 R3 VS V (Y F3)	
UN+3 X 69 ACBSA 25 1919 K U2 F9	YB+2 VI 74 ZAACA 386 221 YB BR2, YB 12	
69 ACBSA 27 245 CS U6 F25	YB+2 VII 74 ZAACA 386 221 YB CL2	
70 ACBSA 27 245 CS U6 F25	74 ACBSA 386 221 YB BR2	
70 ACBSA 27 245 CS U6 F25	YB+2 VIII 74 ACBSA 386 221 YB F2	
70 ACBSA 27 245 CS U6 F25	YB+2 IX 70 SPHCA 14 854 YB2 S1 05	
UN+3 XI 67 ACBSA 23 805 CS U6 F5	70 ACBSA 26 1020 CU M 04	
70 JINCA 32 3701 NA U 03	70 ZAACA 377 70 CA YB2 04, SR YB2 04	
65 BUFGA 80 214 U CR 04	74 ACBSA 30 1857 YB P3 09	
67 BUFGA 80 257 U FE 04	YB+3 VII 70 SPHCA 14 854 YB2 S1 05	
UN+3 XII 73 SPHCA 18 323 U2 RD 08	69 INDOCA 8 22 YB2 S12 07	
UN+3 VI 68 ACBSA 24 967 CU U 04	69 INDOCA 8 29 YB2 S12 07 (H2 01) 1/2 C6 H6	
69 ACBSA 25 787 SR U 04, BA U 04, CAZ U 05	YB+3 VIII 9 1094 YB L1 F4	
UN+3 VII 68 ACBSA 24 967 CU U 04	69 INDOCA 8 1745 YB3 FE5 012	
UN+3 VIII 68 ACBSA 24 967 CU U 04	74 MRBBA 9 179 YB P5 014	
UN+3 IX 68 ACBSA 24 967 CU U 04	74 ZAACA 403 1 R3 VS V (YB F3)	
UN+3 X 68 ACBSA 24 967 CU U 04	YB+3 IX 74 ZAACA 403 1 R3 VS V (YB F3)	
UN+3 XI 68 ACBSA 24 967 CU U 04	ZN+4 VI 68 SPHDA 12 987 NA2 ZN2 S12 07	
UN+3 XII 68 ACBSA 24 967 CU U 04	69 ACBSA 25 1233 ZN 03	

compounds to be slightly larger than those of the Eu^{2+} compounds. This difference was assumed to exist for all Sr^{2+} and Eu^{2+} coordinations. Because compounds of Am^{2+} and Sr^{2+} have similar cell volumes, the radius of Am^{2+} was made equal to that of Sr^{2+} .

Wolfe & Newnham (1969) studied $\text{Bi}_{4-x}\text{RE}_x\text{Ti}_3\text{O}_{12}$ and concluded that Bi^{3+} and La^{3+} have nearly equal radii. From a study of BiTaO_4 Sleight & Jones (1975) have concluded that although Bi^{3+} and La^{3+} have essentially equal radii, the size of Bi^{3+} depends on the degree of the $6s^2$ lone-pair character. When BiTaO_4 transforms from a structure where the lone-pair character is dominant to the LaTaO_4 structure, it undergoes a volume reduction. Table 3 shows a comparison of isotypic Bi^{3+} and La^{3+} compounds where the lone-pair character of Bi^{3+} is (1) constrained and (2) dominant. Bi pyrochlores such as $\text{Bi}_2\text{Ru}_2\text{O}_7$, $\text{Bi}_2\text{Ir}_2\text{O}_7$ and $\text{Bi}_2\text{Pt}_2\text{O}_7$ were omitted from the table because no corresponding La pyrochlore exists, but they have unit-cell volumes close to those of the Sm or Nd pyrochlores and thus have smaller volumes than those of La. When Bi^{3+} is forced into high symmetry, a Bi^{3+} compound has a smaller volume than that of La^{3+} , but when the lone-pair character is dominant, the Bi^{3+} compound is distorted and Bi^{3+} and La^{3+} compounds have approximately equal volumes. This behavior was also noted in the highly symmetric garnet structure where the hypothetical $\text{Bi}_3\text{Fe}_3\text{O}_{12}$ was estimated to have cell dimensions between those of the hypothetical $\text{Nd}_3\text{Fe}_3\text{O}_{12}$ and $\text{Pr}_3\text{Fe}_3\text{O}_{12}$ (Geller, Williams, Espinosa, Sherwood & Gilleo, 1963). For practical purposes, Bi^{3+} is listed as slightly smaller than La^{3+} but this dependence on lone-pair character must be kept in mind when comparing the volumes of Bi^{3+} and La^{3+} compounds. Similar behavior may also exist for Pb^{2+} and Sr^{2+} , but this relationship was not investigated.

Table 3. Cell volumes of isotypic Bi^{3+} and La^{3+} compounds

(a) Lone pair character of Bi^{3+} constrained

Compound	Cell volume	Ratio
$\text{BiLi}(\text{MoO}_4)_2$	314.7	0.96
$\text{LaLi}(\text{MoO}_4)_2$	328.7	
$\text{BiNa}(\text{MoO}_4)_2$	320.5	
$\text{LaNa}(\text{MoO}_4)_2$	332.1	0.97
BiOF	87.6	
LaOF	97.7	
BiOCl	110.7	0.95
LaOCl	116.8	
BiOBr	123.8	
LaOBr	126.4	0.98
BiPO_4	293.0	
LaPO_4	304.7	

(b) Lone pair character of Bi^{3+} dominant

Bi_2MoO_6	268.5 ($\times 8$)	1.00
La_2MoO_6	267.3	
BiFeO_3	62.49 ($\times 6$)	1.03
LaFeO_3	60.77 ($\times 4$)	
$\text{Bi}_2\text{Sn}_2\text{O}_7$	1219.9 ($\times 8$)	1.00
$\text{La}_2\text{Sn}_2\text{O}_7$	1225.3	

A similar study of relative cell volumes of isotypic compounds involving the pairs Cu^+-Li^+ , Ag^+-Na^+ , Tl^+-Rb^+ , and $\text{Pb}^{2+}-\text{Sr}^{2+}$ was used to obtain more reliable estimates of the radii of Cu^+ , Ag^+ , Tl^+ , and Pb^{2+} (Shannon & Gummerman, 1975).

The nature of Sn^{2+} , NH_4^+ , and H^- made it impossible to define their ionic radii. The coordination of Sn^{2+} by oxygen or fluorine is always extremely irregular,* leading to average distances which depend on the degree of distortion. Since this distortion varies widely from one compound to another, it is not meaningful to define an ionic radius.

Khan & Baur (1972) derived an apparent radius of the NH_4^+ ion by analyzing the N-O distances in a large number of ammonium salts. They concluded that NH_4^+ has an octahedral radius of 1.61 Å, between that of Rb^+ (1.52 Å) and Cs^+ (1.67 Å). Alternatively, cell volumes of NH_4^+ and Rb^+ fluorides, chlorides, bromides, iodides and oxides may be compared. This leads to the conclusion that NH_4^+ is not significantly different in size from Rb^+ . No explanation is offered for this inconsistency and therefore the radius of NH_4^+ is not included.

The radius of the hydride ion, H^- , has been the subject of some controversy. A number of different radii have been proposed: 2.08 (Pauling, 1960); 1.40 (Gibb, 1962); and 1.53 Å (Morris & Reed, 1965). Gibb studied interatomic distances in many hydrides and concluded that good agreement between observed and calculated distances could be obtained using $r(\text{VIH}^-) = 1.40$ Å if corrected for cation and anion coordination. The value of $r(\text{IVH}^-)$ was taken to be 1.22 Å.

Morris & Reed (1965) concluded that differences in observed distances in hydrides were caused by the large H^- polarizability. Because of such wide variations in the apparent H^- radius, it was omitted. However, an explanation for the variations based on covalence differences will be discussed later.

* Although cell dimensions of $\text{Sn}_2\text{M}_2\text{O}_7$ pyrochlores were used in SP 69 to derive $r(\text{VIIISn}^{2+})$, Stewart, Knop, Meads & Parker (1973) and Birchall & Sleight (1975) recently found that the pyrochlore A site in $\text{Sn}_2\text{Ta}_2\text{O}_7$ is not fully occupied. Thus, even this example of apparently regular Sn^{2+} polyhedra is not valid.

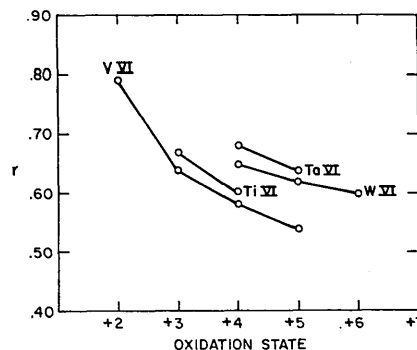
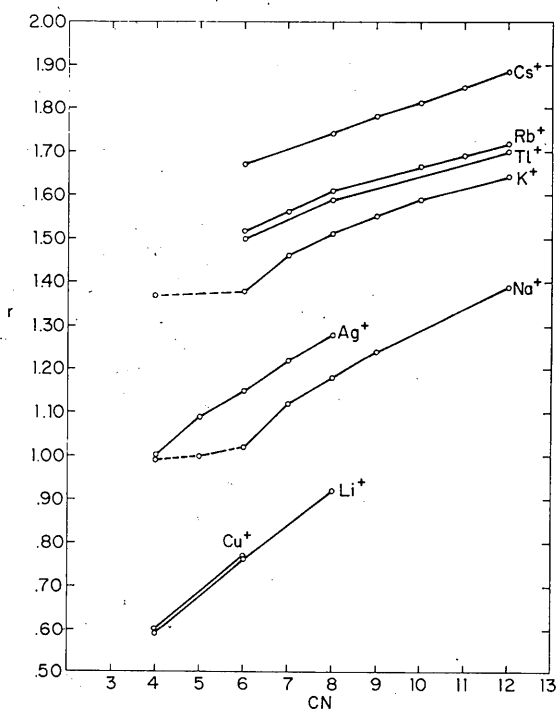


Fig. 1. Effective ionic radius (Å) vs oxidation state.

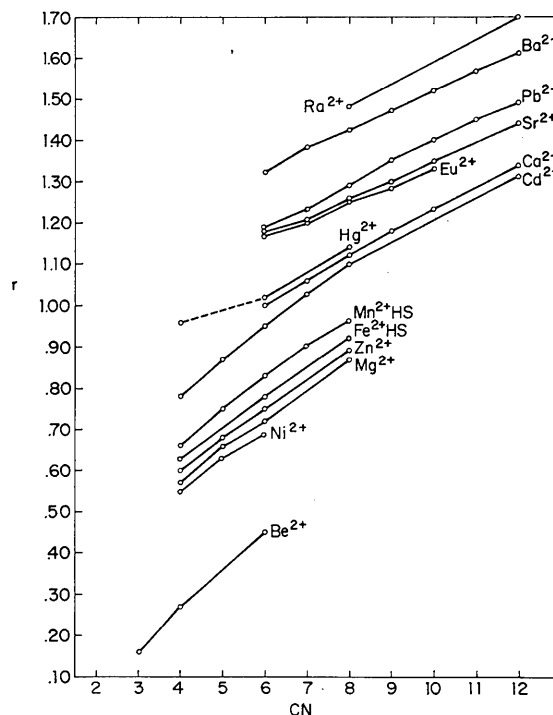
Results and discussion

In Table 1 two sets of radii are included. The first is a set of traditional radii based on $r(\text{VI}\text{O}^{2-}) = 1.40 \text{ \AA}$. The

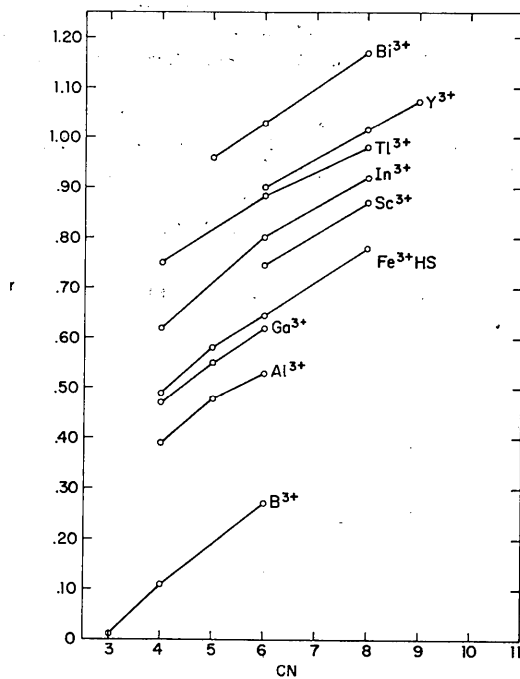
other set is based on $r(\text{VI}\text{O}^{2-}) = 1.26$ and $r(\text{VI}\text{F}^-) = 1.19 \text{ \AA}$, and corresponds to crystal radii as defined by Fumi & Tosi (1964). As pointed out in SP 69, crystal radii differ from traditional radii only by a constant factor



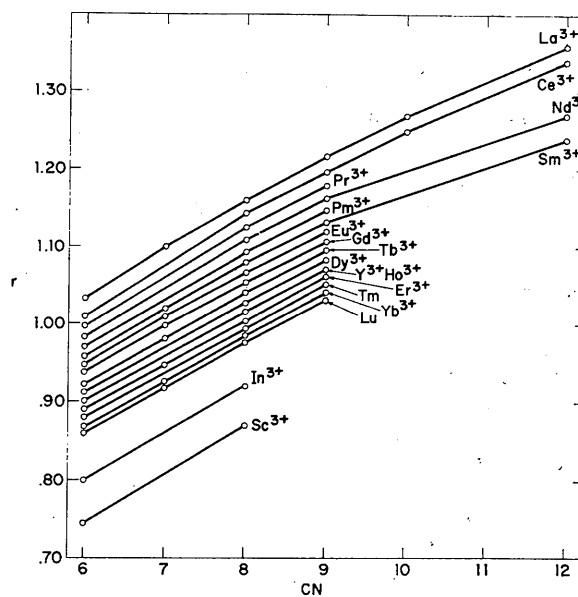
(a)



(b)

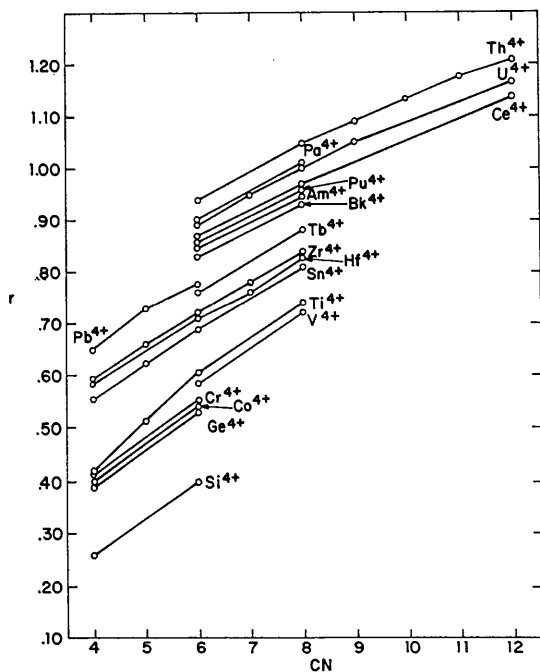


(c)



(d)

Fig. 2. (a)–(e) Effective ionic radius (\AA) vs CN for some common cations.



(e)

Fig. 2. (cont.)

of 0.14 Å. Although their inclusion in Table 1 may seem superfluous, it is felt that crystal radii correspond more closely to the physical size of ions in a solid. They should be used, for example, in discussions of closest packing of spheres, structure field maps (Muller & Roy, 1974), and diffusion in solids (Flygare & Huggins, 1973). Traditional radii have been retained because of their familiarity to crystal chemists and physicists. They will probably continue to be used for comparison of unit-cell volumes and interatomic distances. In the table, the ion is followed by electron configuration (EC), coordination number (CN), spin state (SP), crystal radius (CR), and effective ionic radius (IR), and in the last column, a symbol indicating the derivation of the radii and their reliability. Those with a question mark are doubtful because of: uncertainty in CN, or deviation from radii *vs* CN, or radii *vs* valence plots. Where at least five structural determinations resulted in radii differing by no more than ± 0.01 Å, the values are marked with an asterisk.

When the choice of a radius was influenced by any of the various correlations described earlier, it is indicated by the following: *R* – from r^3 *vs* unit cell volume plots; *C* – calculated from bond length–bond strength equations; *E* – estimated from one or more plots of r *vs* valence, r *vs* CN, and r *vs* cell volume. *E* implies poor or nonexistent structural data. Radii in this category include $^{VI}\text{Fe}^{2+}\text{LS}$, $^{VI}\text{Mn}^{2+}\text{LS}$, $^{VI}\text{Cr}^{2+}\text{LS}$, $^{VI}\text{V}^{2+}$, $^{VI}\text{Ni}^{3+}\text{HS}$, $^{VI}\text{Ir}^{3+}$, $^{VI}\text{Mo}^{3+}$, $^{VI}\text{Ta}^{3+}$, $^{VI}\text{Pa}^{3+}$, $^{VI}\text{Ta}^{4+}$, $^{IV}\text{Pb}^{4+}$, $^{VI}\text{Ir}^{5+}$, $^{VI}\text{Os}^{5+}$, $^{VI}\text{Re}^{5+}$, $^{VI}\text{Pu}^{5+}$, $^{VI}\text{Bi}^{5+}$,

$^{VI}\text{Os}^{6+}$, $^{VI}\text{Re}^{6+}$, and $^{VI}\text{Os}^{7+}$. The symbol *A* means that Ahrens (1952) ionic radius was used whereas *P* means Pauling's (1960) crystal radius was used. The symbol *M* means that the radius was derived from a compound having metallic conductivity. Distances calculated from these radii may be too small for use in compounds having localized electrons. (See discussion *Effects of electron delocalization*.)

In addition, the sources of the radii are indicated in Table 2.

Fig. 2(a)–(e) shows that r –CN plots are reasonably regular. Notable exceptions are $^{IV}\text{Na}^+$, $^{V}\text{Na}^+$, and $^{IV}\text{K}^+$. It is apparent that Na–O and K–O distances do not decrease as much as anticipated from the r –CN curve* when the CN falls below six. Typical distances and corresponding radii in Table 4 show that Na–O distances in four-coordination are only slightly less than in six-coordination. The reduction in interatomic distances is caused primarily by the decreased repulsive forces due to fewer ligands according to the expression of Pauling (1960):

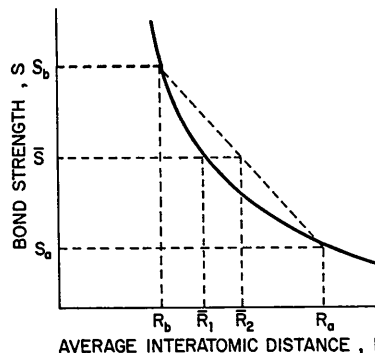
$$\frac{R_{\text{CsCl}}}{R_{\text{NaCl}}} = \left[\frac{A_{\text{NaCl}}}{A_{\text{CsCl}}} \frac{B_{\text{CsCl}}}{B_{\text{NaCl}}} \right]^{1/(n-1)}$$

where R = interatomic distance, A = Madelung constant, B = the cation CN and n = Born repulsion coefficient. It appears that this equation is not valid for four-coordinated Na^+ or K^+ .

There are a few small irregularities in r –CN plots probably caused by poor or insufficient data, *e.g.* curves for Ti^{3+} *vs* Y^{3+} . The differences in slopes of Ti^{4+} *vs* Cr^{4+} and V^{5+} *vs* As^{5+} are probably caused by Ti^{4+} –O and V^{5+} –O octahedra being generally more distorted, which leads to greater average interatomic distances.

It is also interesting to compare distances in square planar coordination *versus* tetrahedral coordination. Radii of square planar Cu^{2+} and Ag^+ are equal to or slightly greater than corresponding tetrahedral radii, consistent with the trend anticipated from anion

* Extrapolation of the Na curve gives $r(^{IV}\text{Na}^+) = 0.90$ Å.

Fig. 3. Typical bond length *vs* bond strength plot.

repulsion effects. A similar comparison with Fe^{2+} and Ni^{2+} cannot be made because of electron distribution changes from tetrahedral to square planar coordination.

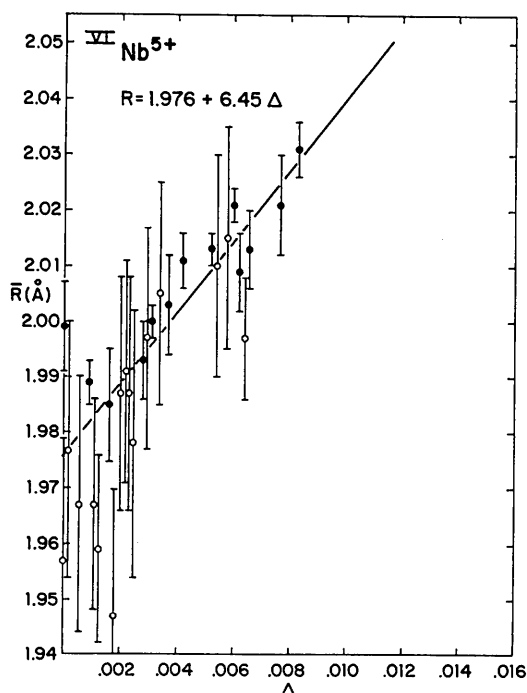


Fig. 4. Mean Nb^{5+} -O bond length *vs* distortion. Vertical bars represent average e.s.d.'s quoted by the authors. Solid circles represent more accurate data.

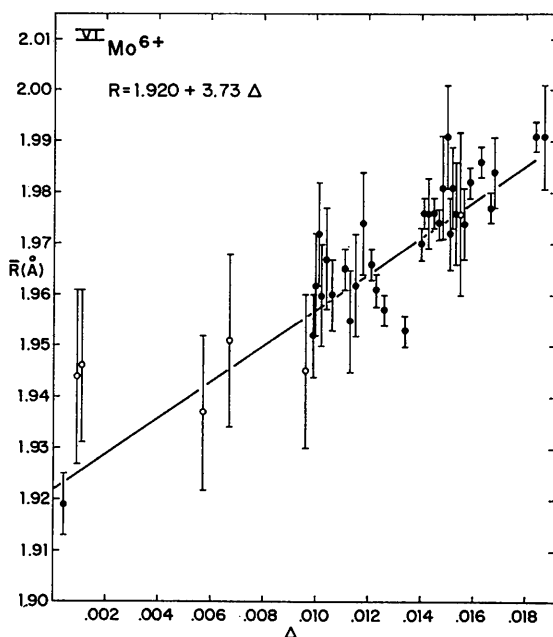


Fig. 5. Mean Mo^{6+} -O bond length *vs* distortion.

Table 4. *Interatomic distances in some compounds containing tetrahedral and octahedral Na^+*

Compound	\bar{R} (Å)	r (Å)	Reference
(a) IVNa^+			
Na_2O	2.40	1.02	
$\text{Na}_3\text{P}_3\text{O}_{10}$	2.37	0.99	60 ACCRA 13 263
$\text{NaOH} \cdot \text{H}_2\text{O}$	2.36	1.00	57 ACCRA 10 462
Na_6ZnO_4	2.39	0.99	69 ZAACA409 69
Mean	2.38	1.00	
(b) VI Na^+			
Na_2WO_4	2.38	1.00	74 ACBCA 30 1872
$\text{NaC}_6\text{O}_7\text{H}_7$	2.37	1.01	65 ACCRA 19 561
$\text{Na}_4\text{Sn}_2\text{Ge}_4\text{O}_{12}(\text{OH})_4$	2.39	1.02	70 ACSAA 24 1287
$\text{Na}_2\text{P}_2\text{O}_7 \cdot 10\text{H}_2\text{O}$	2.48	1.10	64 ACCRA 17 672
NaHCO_3	2.44	1.06	65 ACCRA 18 818
$\text{Na}_2\text{B}_4\text{O}_6(\text{OH})_2 \cdot 3\text{H}_2\text{O}$	2.41	1.04	67 SCIEA 154 1453
$\text{Na}_4\text{P}_4\text{O}_{12} \cdot 4\text{H}_2\text{O}$	2.415	1.05	61 ACCRA 14 555
$\text{NaAl}(\text{SO}_4)_2 \cdot 12\text{H}_2\text{O}$	2.45	1.10	67 ACCRA 22 182
$\text{NaB}(\text{OH})_4 \cdot 2\text{H}_2\text{O}$	2.460	1.09	63 ACCRA 16 1233
NaU acetate	2.375	1.025	59 ACCRA 12 526
$\text{C}_{10}\text{H}_{13}\text{N}_5\text{NaO}_6\text{P} \cdot 6\text{H}_2\text{O}$	2.406	1.046	75 ACBCA 31 19
Mean	2.42	1.05	

Factors affecting mean interatomic distances

Additivity of radii to give mean interatomic distances is not so important to the synthetic chemist who is primarily interested in ionic radii for predicting substitution in crystal structures. Crystallographers and physicists, however, are concerned with comparing calculated and experimental interatomic distances and predicting distances, *e.g.* for distance least-squares (DLS) structure refinements (Baur, 1972; Tillmanns, Gebert & Baur, 1973; Dempsey & Strens, 1975). The effective ionic radii in Table 1 can be used to reproduce moderately well most average interatomic distances in oxides and fluorides. However, certain deviations do occur. Some of these are unexplained but others can be attributed to (1) polyhedral distortion, (2) covalence, (3) partial occupancy of cation sites, or (4) electron delocalization.

1. Polyhedral distortion

To see the effects of polyhedral distortion consider the relationship between bond length (R) and Pauling bond strength (s) (Brown & Shannon, 1973). The analytical expression $s = s_0(R/R_0)^{-N}$, where s_0 is an ideal bond strength associated with R_0 , and R_0 and N are fitted parameters, was evaluated for cation-oxygen pairs for the first three rows of the periodic table. Using these relationships, the sums of bond strengths about cations and anions were found to equal the valences with a mean deviation of about 5%. Accepting the approximate validity of Pauling's second rule, $p = \sum s$ where p = valence, it is possible to derive the effects of distortion of various polyhedra on their mean bond distances. Fig. 3 shows a typical R - s curve. An undistorted octahedron results in an average bond strength \bar{s} and a mean distance \bar{R}_1 . A distorted octahedron with three bonds of length R_a and three of length R_b results in the same average bond strength, \bar{s} , but a mean distance $\bar{R}_2 > \bar{R}_1$.

The effects of distortion on mean bond lengths in numerous polyhedra have been determined. Although distortions in tetrahedra are not as important as in octahedra, they can contribute to variations in mean tetrahedral distances (Baur, 1974; Hawthorne, 1973). Strongly distorted octahedra like those containing V^{5+} , Cu^{2+} , and Mn^{3+} show a significant variation in mean distance with distortion, Δ^* (Brown & Shannon, 1973; Shannon & Calvo, 1973a; Shannon, Gurnerman & Chenavas, 1975). Octahedra containing Mg^{2+} , Zn^{2+} , Co^{2+} , and Li^+ are generally less distorted than those of V^{5+} , Cu^{2+} , and Mn^{3+} and show a less pronounced dependence on mean bond length (Brown & Shannon, 1973).

The effects of distortion on mean bond lengths in Nb^{5+} -O and Mo^{6+} -O octahedra are illustrated in Figs. 4 and 5. Tables 5 and 6 list the data used to derive the figures.

Table 7 lists the results of linear regression analyses of mean bond length on distortion for all octahedra studied. It is clear from Fig. 4 that undistorted Nb^{5+} octahedra in pyrochlores have a distinctly smaller mean value than in compounds like $NbOPO_4$, $CaNb_2O_6$, and Na_3NbO_4 . Most of the accurately refined molybdates have relatively distorted octahedra. However, certain ordered perovskites with no octahedral distortion such as Ba_2CaMoO_6 would be expected to have much smaller mean Mo^{6+} -O distances than a typical molyb-

date. In fact, the Mo^{6+} -O octahedra in $Mo_2(O_2C_6Cl_4)_6$ with a very small distortion have the short mean distance of 1.919 Å.

Table 7 also lists the results of regression analyses for Ta^{5+} -O and W^{6+} -O octahedra but they are only approximate because of the scarcity of accurate structural data. Analysis of Ti^{4+} -O octahedra was unsuccessful because of scatter in the data. Distances in $Ba_6Ti_{17}O_{40}$ (Tillmanns & Baur, 1970) and $BaTiO_3$ (Evans, 1951) deviated significantly from a linear relation.

Relations between mean distance and distortion should be particularly useful to help determine oxidation states in mixed valence compounds with such combinations as Mo^{5+} - Mo^{6+} , W^{5+} - W^{6+} , V^{4+} - V^{5+} , Nb^{4+} - Nb^{5+} and Mn^{3+} - Mn^{4+} . Such considerations helped rationalize Mn-O distances in $NaMn_7O_{12}$ and the mineral pinakolite (Shannon, Gurnerman & Chenavas, 1975).

The radii in Table 1 are generally derived for an average degree of distortion. Thus, interatomic distances calculated from these radii may be inaccurate if the distortion in a particular compound is much less or greater than usual. This applies particularly to cations whose polyhedra frequently show a large distortion, e.g. Mo^{6+} , Nb^{5+} , V^{5+} , Ba^{2+} , and the alkali ions.

2. Effects of partial occupancy of cation sites on mean cation-anion distances

In compounds with partially occupied sites, abnormally large cation-anion distances are usually found, as expected if the anions surrounding unoc-

* Octahedral distortion is defined by $\Delta = \frac{1}{6} \sum (R_i - \bar{R})^2$ where \bar{R} = average bond length and R_i = an individual bond length.

Table 5. Comparison of mean octahedral Nb^{5+} -O distances with distortion

Only structures with e.s.d.'s for Nb-O distances of <0.025 Å were used.

Compound	\bar{R} (Å)	Distortion $\Delta = \langle (\Delta R/R)^2 \rangle \times 10^4$	Reference	
$Hg_2Nb_2O_7$	1.999	0	68 INOCA	7 1704
$Cd_2Nb_2O_7$	1.957	0	72 CJCHA	50 3648
$Na_2Nb_4O_{11}$	1.977	1	70 JSSCB	1 454
$Ba_{0.27}Sr_{0.73}Nb_2O_{5.78}$	1.967	6	61 JCPSA	48 5048
$Na_{13}Nb_{35}O_{94}$	1.965	7	71 JSSCB	3 89
$Ba_3Si_4Nb_6O_{26}$	1.989	9	70 ACBCA	26 102
$Na_{13}Nb_{35}O_{94}$	1.967	11	71 JSSCB	3 89
$Na_{13}Nb_{35}O_{94}$	1.959	12	71 JSSCB	3 89
$Na_{13}Nb_{35}O_{94}$	1.964	12	71 JSSCB	3 89
$NaNbO_3$	1.985	16	69 ACBCA	25 851
$Na_{13}Nb_{35}O_{94}$	1.947	18	71 JSSCB	3 89
$Na_{13}Nb_{35}O_{94}$	1.991	22	71 JSSCB	3 89
$Na_{13}Nb_{35}O_{94}$	1.987	22	71 JSSCB	3 89
$Na_{13}Nb_{35}O_{94}$	1.978	24	71 JSSCB	3 89
$LiNb_2O_8$	1.993	28	71 ACSAA	25 3337
$LiNbO_3$	2.000	31	66 JPCSA	27 997
$Ca_2Nb_2O_7$	1.997	31	74 JINCA	36 1965
$Ca_2Nb_2O_7$	2.005	34	74 JINCA	36 1965
$SbNbO_4$	2.003	37	65 CCJDA	1965 611
$KNbO_3$	2.011	42	67 ACACA	22 639
Na_3NbO_4	2.013	52	74 BUFCA	97 3
$Ca_2Nb_2O_7$	2.010	53	74 JINCA	36 1965
$Ca_2Nb_2O_7$	2.015	58	74 JINCA	36 1965
Na_3NbO_4	2.021	60	74 BUFCA	97 3
$CaNb_2O_6$	2.021	76	70 AMMIA	55 90
$GaNbO_4$	2.031	83	65 ACACA	18 874

Table 6. Comparison of mean octahedral Mo⁶⁺-O distances with distortion

Only structures with e.s.d.'s for Mo-O distances of <0.025 Å were used.

Compound	\bar{R} (Å)	Distortion		Reference	
		$\Delta = \langle (\Delta R/R)^2 \rangle \times 10^4$			
Mo ₂ (O ₂ C ₆ Cl ₄) ₆	1.919	5	75 JACSA	97	2123
Mo ₄ O ₁₁ orthorhombic	1.944	9	63 ARKEA	21	365
Mo ₄ O ₁₁ monoclinic	1.946	10	63 ARKEA	21	365
Mo ₄ O ₁₁ monoclinic	1.937	56	63 ARKEA	21	365
Mo ₄ O ₁₁ orthorhombic	1.951	67	63 ARKEA	21	365
Mo ₄ O ₁₁ orthorhombic	1.911	96	63 ARKEA	21	365
Mo ₄ O ₁₁ monoclinic	1.945	96	63 ARKEA	21	365
(C ₁₅ H ₁₁ O ₂) ₂ MoO ₂	1.952	99	74 ACBCA	30	300
(NH ₄) ₆ [Mo ₇ O ₂₄]·4H ₂ O	1.962	99	75 JCSIA	1975	505
(NH ₄) ₆ [Mo ₇ O ₂₄]·4H ₂ O	1.972	101	75 JCSIA	1975	505
(NH ₄) ₆ [Mo ₇ O ₂₄]·4H ₂ O	1.960	104	75 JCSIA	1975	505
LiMoO ₂ AsO ₄	1.967	104	70 ACSAA	24	3711
(NH ₄) ₆ Mo ₈ O ₂₇ ·4H ₂ O	1.960	106	74 ACBCA	30	48
HgMoO ₄	1.965	111	73 ACBCA	29	869
(NH ₄) ₆ [Mo ₇ O ₂₄]·4H ₂ O	1.955	113	75 JCSIA	1975	505
(NH ₄) ₆ [Mo ₇ O ₂₄]·4H ₂ O	1.962	115	75 JCSIA	1975	505
(NH ₄) ₆ [Mo ₇ O ₂₄]·4H ₂ O	1.974	118	68 JACSA	90	3275
MoO ₃ ·2H ₂ O	1.966	121	72 ACBCA	28	2222
MoO ₃ ·2H ₂ O	1.961	123	72 ACBCA	28	2222
MoO ₃ ·2H ₂ O	1.957	126	72 ACBCA	28	2222
MoO ₃ ·2H ₂ O	1.953	134	72 ACBCA	28	2222
(NH ₄) ₅ [MoO ₃] ₅ (PO ₄)(HPO ₄)]·3H ₂ O	1.970	140	74 JCSIA	1974	941
Na ₃ (CrMo ₆ O ₂₄ H ₆)·8H ₂ O	1.976	141	70 INOCA	9	2228
(NH ₄) ₆ Mo ₈ O ₂₇ ·4H ₂ O	1.976	141	74 ACBCA	30	48
Na ₃ CrMo ₆ O ₂₄ H ₆ ·8H ₂ O	1.976	143	70 INOCA	9	2228
(NH ₄) ₅ [(MoO ₃] ₅ (PO ₄)(HPO ₄)]·3H ₂ O	1.974	145	74 JCSIA	1974	941
(NH ₄) ₆ [TeMo ₆ O ₂₄]·Te(OH) ₆ ·7H ₂ O	1.981	147	74 ACBCA	30	2095
CoMoO ₄	1.991	150	65 ACACA	19	269
(NH ₄) ₆ Mo ₈ O ₂₇ ·4H ₂ O	1.972	151	74 ACBCA	30	48
MoO ₃	1.981	151	63 ARKEA	21	357
(NH ₄) ₆ [Mo ₇ O ₂₄]·4H ₂ O	1.976	152	68 JACSA	90	3275
K ₂ {[MoO ₂ (C ₂ O ₄)(H ₂ O)] ₂ O}	1.976	152	64 INOCA	3	1603
(NH ₄) ₆ Mo ₈ O ₂₇ ·4H ₂ O	1.974	152	74 ACBCA	30	48
(NH ₄) ₅ [(MoO ₃] ₅ (PO ₄)(HPO ₄)]·3H ₂ O	1.982	159	74 JCSIA	1974	941
Na ₃ CrMo ₆ O ₂₄ H ₆ ·8H ₂ O	1.986	163	70 INOCA	9	2228
(NH ₄) ₅ [(MoO ₃] ₅ (PO ₄)(HPO ₄)]·3H ₂ O	1.977	167	74 JCSIA	1974	941
MoO ₃ ·H ₂ O	1.984	167	74 ACBCA	30	1795
(NH ₄) ₅ [(MoO ₃] ₅ (PO ₄)(HPO ₄)]·3H ₂ O	1.991	186	74 JCSIA	1974	941
(NH ₄) ₆ [Mo ₇ O ₂₄]·4H ₂ O	1.991	189	75 JCSIA	1975	505
(NH ₄) ₆ [Mo ₇ O ₂₄]·4H ₂ O	2.008	197	75 JCSIA	1975	505

Table 7. Variation of mean M-O distance and effective ionic radius in octahedral environments as a function of distortion

Ion	Maximum $\Delta \times 10^4$	N^*	R_0^\dagger	r_0^\ddagger	m	Correlation coefficient	Goodness of fit ($\times 10^3$)
Mo ⁶⁺	212	38	1.920		3.73	0.74	67
				0.572	3.01	0.63	70
W ⁶⁺	122	7	1.925		3.30	0.75	19
				0.565	3.28	0.66	24
V ⁵⁺	576	16	1.887		2.62	0.98	8
Nb ⁵⁺	83	29	1.976		6.45	0.69	71
				0.599	6.83	0.44	99
Ta ⁵⁺	79	6	1.984		6.70	0.81	18
				0.617	3.79	0.15	46
Mn ³⁺	71	15	1.994		7.08	0.82	30
				0.624	6.15	0.54	50
Cu ²⁺	316	26	2.085		3.99	0.82	77
Mg ²⁺	156	28	2.094		8.31	0.72	21
				0.728	8.86	0.77	18
Co ²⁺	46	15	2.106		7.38	0.42	19
				0.734	11.70	0.70	16
Zn ²⁺	71	16	2.099		7.70	0.64	21
				0.736	8.20	0.74	16
Li ⁺	148	11	2.159		8.42	0.81	30
				0.784	9.02	0.79	35

* N = number of independent octahedra $^\dagger R = R_0 + m\Delta$. $^\ddagger r = r_0 + m\Delta$.

cupied sites relax toward their bonded cation neighbors. Therefore average distances should increase as the occupancy factor decreases. In general, partial occupancy seems to be more prevalent for cations which are weakly bonded to oxygen like Cu^+ , Ag^+ , alkali ions, and large alkaline earths. The most prominent examples are Li and Na compounds. Table 8 summarizes the existent data on some structures with partial cation occupancy. Fig. 6 shows the dependence of mean Li–O bond length on the degree of occupancy. Although the data are not extensive, it is apparent that mean distance increases as occupancy factor decreases. Extrapolation of the Li curve in Fig. 6 to zero occupancy, *i.e.* a tetrahedral Li vacancy, gives 2.10–2.15 Å, which is close to the 2.11 Å found for $\alpha\text{-Li}_5\text{GaO}_4$ by Stewner & Hoppe (1971) and for β eucryptite by Tscherry, Schulz & Laves (1972).

Another example of the effects of partial occupancy can be found in the non-stoichiometric feldspar $\text{Sr}_{0.84}\text{Na}_{0.03}\text{Al}_{1.69}\text{Si}_{2.29}\text{O}_8$ reported by Grundy & Ito (1974). The mean Sr–O distance in this compound is 0.03 Å greater than in the stoichiometric $\text{SrAl}_2\text{Si}_2\text{O}_8$ (Chiari, Calleri, Bruno & Ribbe, 1975).

The relation between mean distance and occupancy probably cannot be quantified precisely because the relaxation of oxygen ions will depend on the nature and number of other cation neighbors.

3. Effects of covalence

Changes in interatomic distances due to covalence effects are anticipated in compounds with (1) anions less electronegative than fluorine or oxygen, *i.e.* chlor-

ides, bromides, sulfides, selenides, *etc.* and (2) tetrahedral oxyanions such as the VO_4^{3-} and AsO_4^{3-} groups. The effects of covalence show up as a lack of additivity of the radii and are generally referred to as 'covalent shortening'.

(a) *Halides and chalcogenides.* Covalence effects can be observed by comparing the relative contraction of cation–anion distances in two different isotypic compounds as the anion becomes less electronegative, *e.g.* Fe^{2+} in Fe_2GeO_4 and Fe_2GeS_4 vs Mg^{2+} in Mg_2GeO_4 and Mg_2GeS_4 . Covalence shortens both Fe–S and Mg–S bonds relative to Fe–O and Mg–O bonds, but because of the greater electronegativity of Fe^{2+} (1.8) compared to Mg^{2+} (1.2), the Fe–S bonds are shortened to a greater extent. Thus a 'covalency contraction' parameter (Shannon & Vincent, 1974) can be defined:

$$R_d = \frac{d(\text{Fe-X})^3}{d(\text{Mg-X})^3}$$

where $d(\text{Fe-X})$ = mean Fe–X distance.

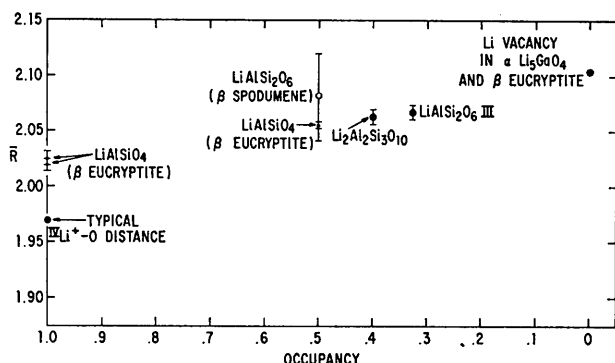
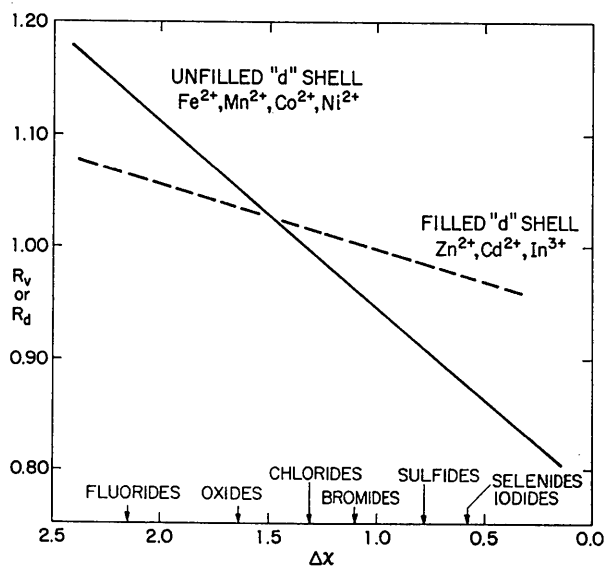
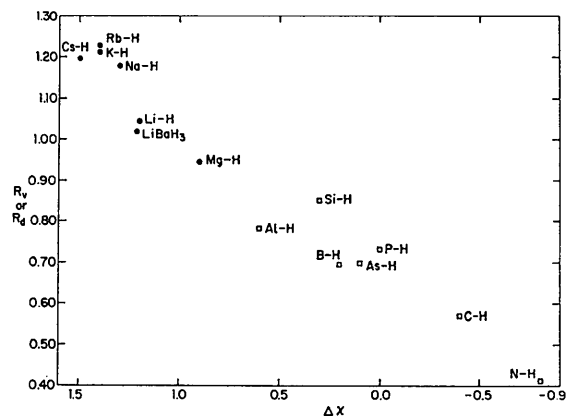
A similar parameter

$$R_v = \frac{V(\text{Fe}_m\text{X}_n)}{V(\text{Mg}_m\text{X}_n)}$$

compares the volume of an Fe^{2+} compound with that of an isotypic Mg^{2+} compound. To see the effects of covalence on the Fe–X distance relative to the Mg–X distance, the ratio R_v or R_d may be plotted against the difference in electronegativity of the Fe–X bond, $\Delta\chi_{\text{Fe-X}}$. Such schematic R_v – $\Delta\chi$ plots are shown in Fig. 7. The reference ions for Cd^{2+} and In^{3+} are Ca^{2+} and Sc^{3+} respectively. Such plots usually show a strong

Table 8. Mean distances in structures with partially occupied cation sites

Compound	Occupancy factor	\bar{R}	Reference		
(a) $^{\text{IV}}\text{Li}^+$					
Typical	1.00	1.97	Table 1		
LiAlSiO_4 (β eucryptite)	1.00	2.020 (4)	73 AMMIA	58	681
		2.025 (7)	72 ZKKKA	135	175
$\text{LiAlSi}_2\text{O}_6$ II (β spodumene)	0.50	2.08 (4)	68 ZKKKA	126	46
		2.085 (9)	69 ZKKKA	130	420
LiAlSiO_4 (β eucryptite)	0.50	2.056 (2)	72 ZKKKA	135	161
$\text{Li}_2\text{Al}_2\text{Si}_3\text{O}_{10}$	0.40	2.064 (4)	70 ZKKKA	132	118
$\text{LiAlSi}_2\text{O}_6$ III	0.33	2.068 (5)	68 ZKKKA	127	327
$\alpha\text{-Li}_5\text{GaO}_4$	0.00	2.11	71 ACBCA	27	616
LiAlSiO_4	0.00	2.11	72 ZKKKA	135	175
(b) $^{\text{VI}}\text{Na}^+$					
Typical	1.00	2.42	Table 1		
$\text{Na}_2\text{Fe}_2\text{Al}(\text{PO}_4)_3$ (wyllieite)	0.91	2.533 (6)	74 AMMIA	59	280
NaSbO_3	0.82	2.74	74 JSSCB	9	345
$\text{Na}_2\text{Fe}_2\text{Al}(\text{PO}_4)_3$ (wyllieite)	0.70	2.723 (6)	74 AMMIA	59	280
$\text{NaAlSi}_3\text{O}_8$ (high albite)	0.50	2.600 (9)	69 ACBCA	25	1503
$\text{NaAl}_{11}\text{O}_{17}$ ($\beta\text{-Al}_2\text{O}_3$)	0.35	2.839 (1)	68 ZKKKA	127	94
NaSbO_3	0.29	2.65	74 JSSCB	9	345
$\text{Na}_{2.58}\text{Al}_{21.81}\text{O}_{34}$ ($\beta\text{-Al}_2\text{O}_3$)	0.25	2.88	71 ACBCA	27	1826
(c) $^{\text{VI}}\text{Ag}^+$					
Typical	1.00	2.50	Table 1		
AgSbO_3	0.44	2.64	74 JSSCB	9	345
AgSbO_3	0.33	2.75	74 JSSCB	9	345
$\text{Ag}_{2.4}\text{Al}_{22}\text{O}_{34.2}$	0.22	2.83	72 JSSCB	4	60

Fig. 6. Mean $\text{Li}^+\text{-O}$ bond length vs partial occupancy.Fig. 7. Covalency contraction parameter, R_v or R_d , vs $\Delta\chi$ for filled and unfilled d shell cations.Fig. 8. Covalency contraction parameter, R_v or R_d , vs $\Delta\chi$ for hydrides. Solid circles represent ratios of cell volumes of isotopic compounds. Squares represent ratios of the cubed M-H distances to the cubed M-F distances.

dependence of R_v on $\Delta\chi$. For $\text{Fe}^{2+}\text{-Mg}^{2+}$ the Fe^{2+} fluoride volumes are $\sim 110\%$ of the corresponding Mg^{2+} fluoride volumes whereas the Fe^{2+} sulfide volumes are $\sim 96\%$ of the corresponding Mg^{2+} sulfide volumes. Plots for the cations with filled 'd' shells show a markedly smaller dependence on $\Delta\chi$. This appears to be due to the difference in covalence of hybrid orbitals formed from metal 'd' orbitals vs metal 's-p' orbitals.

These relations show that effective ionic radii derived primarily from oxides are not strictly applicable to fluorides – note the change in R_v for Fe^{2+} , Co^{2+} , Ni^{2+} , and Mn^{2+} from fluorides to oxides. This effect is particularly noticeable in $R_v\text{-}\Delta\chi$ plots for the pairs $\text{Cu}^+\text{-Li}^+$ and $\text{Ag}^+\text{-Na}^+$ (Shannon & Gurneman, 1975). The $\text{Cu}^+\text{-Li}^+$ and $\text{Ag}^+\text{-Na}^+$ plots are very steep, e.g. the volume of AgF is 120% of the volume of NaF , whereas the volume of Ag_2Se is only 72% of the volume of Na_2Se . Although most of this change arises from covalency, double repulsion effects present in the Li and Na halides described by Pauling (1960) may also play a role.

Covalence effects are useful in explaining certain differences between the effective ionic radii of Table 1 and the ionic radii of Pauling (1927) and Ahrens (1952). Pauling's radii for Cu^+ (0.96 Å) and Ag^+ (1.26 Å) are considerably larger than those in Table 1 (0.77 and 1.15 Å respectively). Since these radii were derived from comparison of alkali halide distances, using an equation relating effective nuclear charge and screening constants (Pauling, 1927), they are valid in primarily ionic crystals. The smaller radii in Table 1 are applicable in the more covalent oxides. Extrapolation of R vs $\Delta\chi$ curves such as in Fig. 7 leads to values of 0.91 Å and 1.23 Å for fluorides, which are close to Pauling's ionic values.

A final example of covalence effects concerns $\text{M}^+\text{-H}^-$ distances. According to Gibb (1962), the radius of the hydride ion is slightly larger than the radius of the fluoride ion. To rationalize the behavior of the hydride ion, the M-H bond has been treated as covalent. Therefore, it is useful to make R_v vs $\Delta\chi$ plots similar to those just discussed for Fe^{2+} , Cu^+ , etc. In this case, the reference ion is F^- and volumes of certain hydrides are compared to those of isotopic fluorides. The results of this analysis are shown in Fig. 8. The solid circles represent volume ratios, $R_v = V(\text{M}_m\text{H}_n)/V(\text{M}_m\text{F}_n)$; open squares represent ratios of typical distances $R_d = d(\text{M-H})^3/d(\text{M-F})^3$. In the more ionic hydrides of Cs, Rb, K, and Na, hydride volumes are considerably larger than those of the fluorides. For the Li and Mg compounds, hydride and fluoride volumes are approximately equal, whereas the more covalent hydrides have increasingly smaller relative volumes than the corresponding fluorides. Fig. 8 partly explains the differences in reported radii. The Morris & Reed (1965) value of 1.53 Å was derived essentially from the large alkali halides, while Gibb's value of 1.40 Å was derived primarily from hydrides of the more electronegative

metals such as: Sc, Ti, Y, Zr, Hf, Nb, Ta, and Th. Because of this strong dependence of M–H distances on cation electronegativity, it does not seem very useful to quote a unique radius for H^- .

(b) *Tetrahedral oxyanions.* Lack of additivity also appears in most small tetrahedral groups and is particularly noticeable for the ions $^{IV}B^{3+}$, $^{IV}Fe^{3+}$, $^{IV}Ge^{4+}$, $^{IV}As^{5+}$, $^{IV}V^{5+}$, $^{IV}S^{6+}$, $^{IV}Se^{6+}$, and $^{IV}Cl^{7+}$. The deviations in vanadates have been studied in detail (Shannon & Calvo, 1973b). Assuming that the V–O bond is strongly covalent, and that relatively electronegative cations such as Cu^{2+} , Ni^{2+} , and Co^{2+} tend to remove electron density from the V–O bond, a V–O bond length increase in Cu, Ni, and Co vanadates is anticipated. Plots of mean radii (\bar{r}) *vs* mean cation electronegativity ($\bar{\chi}$) show a marked slope with a gradual increase in $\bar{r}(^{IV}V^{5+})$ from vanadates of the alkali and alkaline earth ions to those of Cu, Ni, and Co. Similar plots for other ions, P^{5+} , As^{5+} (Shannon & Calvo, 1973b), B^{3+} , Si^{4+} , Se^{6+} (Shannon, 1975), showed the same behavior. The statistical data on the tetrahedra of B^{3+} , Si^{4+} , Ge^{4+} , P^{5+} , As^{5+} , S^{6+} , Se^{6+} , Cr^{6+} , Mo^{6+} , W^{6+} , and Cl^{7+} have been summarized by Shannon (1975). The slopes of the \bar{r} *vs* $\bar{\chi}$ plots were greatest for V^{5+} , Se^{6+} , and Cl^{7+} , and least for Si^{4+} . Although the evidence for covalence as the origin of these effects in the above systems is only indirect, this behavior is consistent with accepted ideas of ‘covalent shortening’ of bonds.

The evidence for covalent shortening of $^{IV}Fe^{3+}$ –O bonds is more direct. Jeitschko, Sleight, McClellan & Weiher (1976) have found a good correlation between (1) the Fe Mössbauer isomer shift and mean Fe–O distance and (2) $\bar{\chi}$ and mean Fe–O distance (\bar{R}). Thus, in β - $NaFeO_2$ $\bar{R}=1.86$ Å and $\delta=0.18$ mm s $^{-1}$ relative to α Fe whereas in $Bi_3(FeO_4)(MoO_4)_2$ $\bar{R}=1.909$ Å and $\delta=0.282$ mm s $^{-1}$.

4. Effects of electron delocalization

At a pressure of 6.5 kbar SmS (NaCl structure) undergoes a semiconductor to metal transition and a reduction in cell edge from 5.97 to 5.70 Å (Jayaraman, Narayanamurti, Bucher & Maines, 1970). The reduction in cell volume was attributed to a partial conversion of Sm^{2+} to Sm^{3+} ; some of the electrons presumably go into a conduction band.

Electron delocalization effects can also be seen by comparing the volumes of the conducting V sulfides VS, V_7S_8 , V_3S_4 and V_5S_8 with the corresponding Cr sulfides which have localized ‘*d*’ electrons (de Vries & Jellinek, 1974). The V compounds have volumes ~5% smaller than the corresponding chromium compounds. This does not agree with the relative sizes of V and Cr in oxides and fluorides, *e.g.* $r(^{IV}V^{3+})=0.64$ and $r(^{VI}Cr^{3+})=0.615$ Å. For the sulfides, this unit-cell volume anomaly is not simply attributable to metallic *vs* semiconducting behavior. While Cr_3S_4 , Cr_5S_6 , and Cr_7S_8 show a positive temperature dependence of resistivity typical of a metal, magnetic susceptibility

measurements indicate Curie–Weiss behavior and therefore nearly localized electrons (van Bruggen, 1969). This is in contrast to the Pauli paramagnetic behavior of the corresponding V sulfides (de Vries & Haas, 1973) characteristic of delocalized electrons. Thus, in SmS and the sulfides of V metallic character accompanied by electron delocalization appears to be associated with reduced bond distances.

A further example of delocalization effects occurs in the compound $NaVS_2$ (Weigers, van der Meer, van Heinigen, Kloosterboer & Alberink, 1974). The molecular volume of Pauli paramagnetic $NaVS_2$ I (67.9 Å 3) is significantly less than that of $NaVS_2$ II (72.7 Å 3). $NaVS_2$ II is characterized by localized electrons (Jellinek, 1975) and its molecular volume is consistent with that of isotopic $NaCrS_2$ (71.1 Å 3).

If electron delocalization in oxides results in reduced metal–oxygen distances and thereby an effective increase in valence, radii derived for the ions Mo^{4+} , Tc^{4+} , Ru^{4+} , Rh^{4+} , W^{4+} , Re^{4+} , Os^{4+} , and Ir^{5+} from metallic oxides may not be reliable when applied to insulating oxides. Thus, radii obtained from distances in the metallic phases, *e.g.* RhO_2 , ReO_2 , and $Cd_2Ir_2O_7$, will be smaller than radii obtained from semiconducting or insulating compounds.* When both types of compounds have been studied, a significant difference in distances is generally found. The mean octahedral Re^{4+} –O distance in insulating $K_4[Re_2O_2(C_2O_4)_4] \cdot 3H_2O$ (Lis, 1975) of 2.021 (10) Å ($r=0.671$ Å) is greater than the estimated mean distance in metallic ReO_2 of 1.99 Å ($r=0.63$ Å). Knop & Carlow’s (1974) value of $r=0.662$ Å derived from cell volumes of the insulating Cs_2ReF_6 phases is consistent with the radius of Re^{4+} from $K_4[Re_2O_2(C_2O_4)_4] \cdot 3H_2O$. The Re^{5+} –O distance in $Nd_4Re_2O_{11}$ (Wilhelmi, Lagervall & Muller, 1970) of 1.987 (12) Å ($r=0.607$ Å) is significantly greater than the distance in metallic $Cd_2Re_2O_7$ (Sleight, 1975) of 1.93 (2) Å ($r=0.55$ Å). The radii of 0.58 Å derived from XeF_2RuF_6 and 0.60 Å from $XeFRuF_6$ (Bartlett, Gennis, Gibler, Morrell & Zalkin, 1973) are greater than the radius of 0.565 Å derived from the r^3 – V plot for metallic $Cd_2Ru_2O_7$. In contrast, however, the Mo^{4+} radius of 0.64 Å derived from insulating Li_2MoF_6 (Brunton, 1971) is not greatly different from the radius of 0.65 Å derived from metallic MoO_2 (Brandt & Skapski, 1967).

Although there appears to be ample evidence to show that M–O bond distances in compounds with localized electrons are greater than M–O distances in compounds with delocalized electrons, the data are not yet sufficient to derive a reliable set of radii for semiconducting compounds containing Mo^{4+} , Tc^{4+} , Ru^{4+} , Rh^{4+} , W^{4+} , Re^{4+} , Os^{4+} , and Ir^{5+} . This will become possible as additional accurate structure refinements of fluorides, molecular inorganic compounds, and semiconducting oxides containing these ions become available.

* This assumes that metallic character can be equated with delocalized electron behavior in these compounds.

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