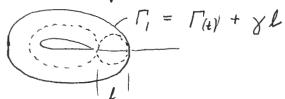
$C_{\ell} = 2\pi \left(\alpha(\ell) - \alpha_{\ell=0} \right)$

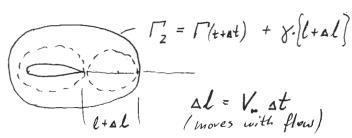
instantaneous lift corresponds to instantaneous X, as given

b) Let I be the length of wake inside larger circuit at time t.

At time t:



At time t+at: (circuit moves) with flow)



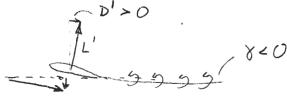
Since circuit is defined to move with flow, Kelvins Thim applies:

1/2 Voc 2π (wt - α/0) + xt = 2 Vac 2π (w.(K+at) - α/0) + x(L+ Vat) after cancelling left & right terms:

$$O = \frac{1}{2} Ve^{2\pi} \omega \Delta t + \gamma V \Delta t$$

$$\gamma = -\pi c \omega$$

C) Vortex sheet causes downwash at airfoil. Lift vector will tilt aft, giving D>0



2. a) T.A.T. Result:
$$C_{\ell} = 2\pi(\alpha + 2\epsilon)$$
, $\epsilon = \frac{L}{c}$

Here, $h = \frac{L}{K}$ or $\epsilon = \frac{L'}{cK}$
 $C_{\ell} = 2\pi(\alpha + 2\epsilon)$

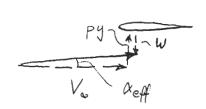
But
$$L' = \frac{1}{2} \rho V_{\infty}^{2} C C_{\ell}$$

so $L' = \frac{1}{2} \rho V_{\infty}^{2} C 2\pi \left(\alpha + 2\frac{L}{cK}\right)$
 $L' \left(1 - 4\pi \frac{g_{\infty}}{K}\right) = g_{\infty} C 2\pi \alpha$

$$L' = g_{\infty} C \frac{2\pi}{1 - 4\pi \frac{g_{\infty}}{K}} \alpha$$
 $C_{\ell} = \frac{L'}{g_{\infty} C} = \frac{2\pi}{1 - 4\pi \frac{g_{\infty}}{K}} \alpha$

$$\frac{dc_{\ell}}{dx} = \frac{2\pi}{1 - 4\pi \frac{3\infty}{K}}$$

b) $\frac{dC_{e}}{dx}$ tends to ∞ as $4\pi \frac{g_{m}}{k} \rightarrow 1$ or $g_{\infty} \rightarrow \frac{K}{4\pi}$ Airfoil billows out without limit if g_{∞} exceeds $\frac{K}{4\pi}$ 3. a) Velocities seen by airfoil at locationy:



y Vortex wake

 $\alpha_{\text{eff}} = \frac{p_{\text{y}}}{V_{\text{m}}} - \alpha_{i}, \quad \alpha_{i} = \sum_{n=1}^{\infty} n A_{n} \frac{\sin n\theta}{\sin \theta}$

For this case, only A_2 is nonzero: $X_i = 2A_2 \frac{\sin 2\theta}{\sin \theta}$ or $X_i = 2A_2 \frac{2\cos \theta \sin \theta}{\sin \theta} = 4A_2 \cos \theta$

 $C_{\ell} = 2\pi \alpha_{eff} = 2\pi \left[\frac{p_{y}}{V_{\infty}} - 4A_{z} \cos \theta \right] = 2\pi \left[\frac{p_{\theta}}{2V_{\infty}} - 4A_{z} \right] \cos \theta$

b) r = Az sin 20 = 2 Vc Ce

since $y = \frac{b}{2} \cos \theta$

26 Va Az 2 sind cort = & VCo sind. 2r [Pb 2Va - 4Az] sort

46 Va Az = TVaco [\$6 - 4Az]

 $(4bV_{o} + \pi V_{o}c_{o}.4)A_{2} = \pi V_{o}c_{o}\frac{bb}{2V_{o}}$ $A_{2} = \frac{\pi c_{o}pb/2}{(4b + 4\pi c_{o})V_{o}}$

c) Moment is opposite to roll rate