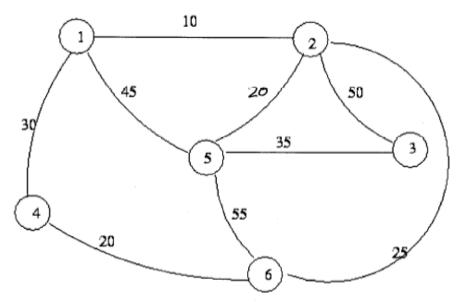
Home Work 9

The problems in this problem set cover lectures C7, C8, C9 and C10

1. What is the Minimum Spanning Tree of the graph shown below using both Prim's and Kruskal's algorithm. Show all the steps in the computation of the MST (not just the final MST).

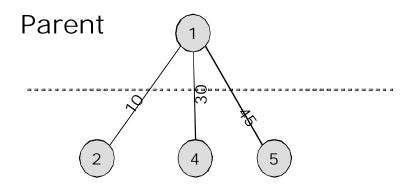


Prim's Algorithm

Step 1.

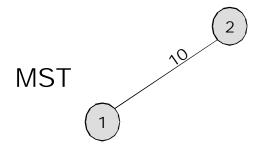
MST

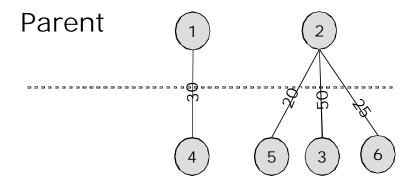




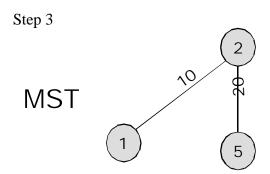
Fringe Set

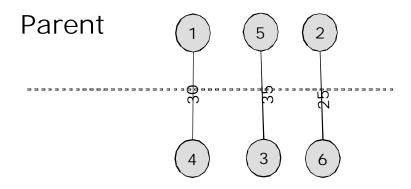
Step 2



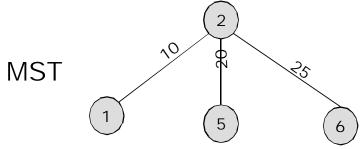


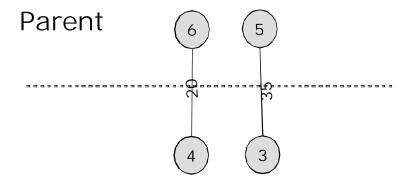
Fringe Set



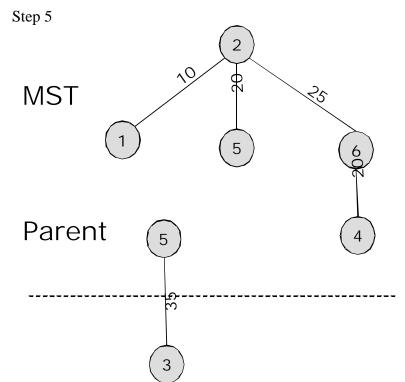


Fringe Set



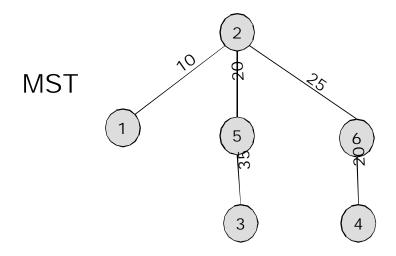


Fringe Set



Fringe Set

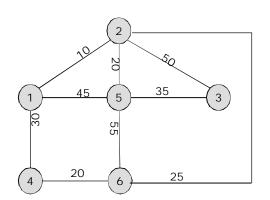
Minimum Spanning Tree



Weight of the MST = 10 + 20 + 25 + 20 + 35 = 110

Kruskals Algorithm

Initialization



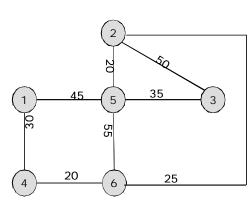


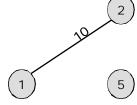






Step 1



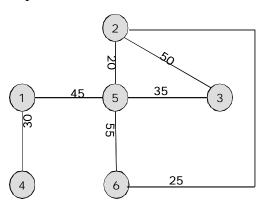


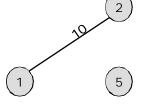




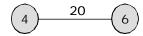


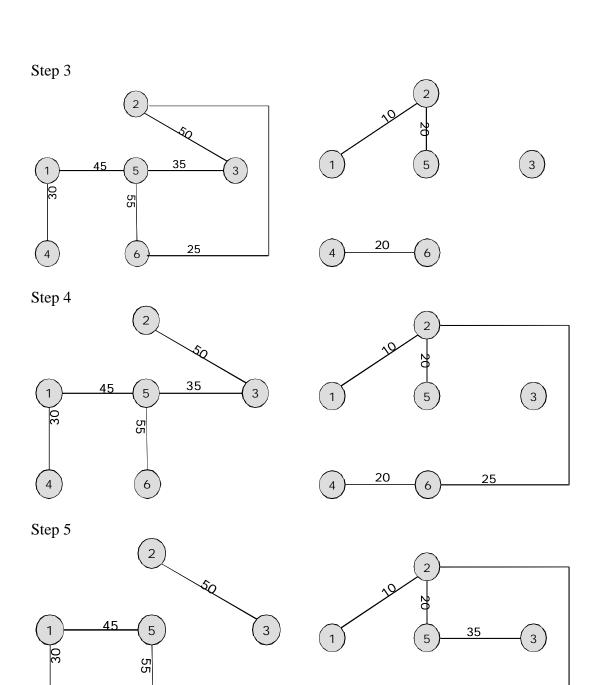
Step 2











Weight of the MST = 10 + 20 + 20 + 25 + 35 = 110

2. Compute the computation complexity of the bubble sort algorithm. Show all the steps in the computation based on the algorithm.

Algorithm

Procedure Bubble_Sort(Input_Output_Array)

end Bubble_Sort;

$$O(N(N-1)) = O(N^2)$$

- 3. What are the best case and worst case computation complexity of:
- a. Inserting a node into an unsorted singly linked list

Inserting into an unsorted singly linked list is carried out using the add_to_front operation.

Both the best and worst case execution time is O(1).

b. Inserting a node into a sorted singly linked list

In the case of a sorted linked list, the list has to be traversed to find the right position. The list traversal takes O(n) in the worst case.

Best case execution time is O(1) if the element being inserted is the smallest element in the list (list in ascending order)

Worst case execution time is O(n) if the element being inserted is the largest element in the list (list in ascending order)

4.

- a. Design an Ada95 Package to:
 - i. Read in N integers from an input file into an array. (N is user defined <=50)
 - ii. Sort the array in ascending order

type my_array is array (1 .. 50) of integer;

iii. Perform binary search on the array.

The package is designed as follows: Data Structures:

```
Subprograms:
```

```
-- procedure to create an array with <=50 elements
-- assumes that input can be found in input_file.txt
-- accepts the array
-- returns array with elements read from file and the number of elements read
procedure Create (
   Num_Array : in out My_Array;
   Size : out Integer );
procedure Merge (
   Input_Array : in out My_Array;
   Lb_1
            : in Integer;
   Ub_1
            : in Integer;
   Lb 2
             : in Integer;
   Ub 2
             : in Integer );
-- procedure to sort the array in ascending order
-- accepts the array and the lowerbound(lb) and upperbound(ub)
-- returns the sorted array
procedure Merge_Sort (
   Num_Array: in out My_Array;
   Lb
          : in Integer;
   Ub
          : in Integer );
--function to perform binary search on the array
-- accepts the array, lb, ub and the element being searched for
-- returns the index of the element if it is found
-- returns -1 if the element is not found
function Binary_Search (
   Num_Array : My_Array;
   Lb
           : Integer;
   Ub
            : Integer;
   Looking_For : Integer )
 return Integer;
```

Algorithms:

Create

Pre-conditions: An array of 50 elements (num_array)

Post-Condition: Array with a maximum of 50 elements loaded from the file, size of the

array.

Algorithm

- 1. Open the file input_file.txt
- 2. Initialize the counter to 0
- 3. While not End_Of_File (input_file)
 - a. Increment the counter
 - b. Read an element from the file into num_array(Counter)
- 4. Return num_array and Counter

Merge_Sort

Merge Sort is a *sort* algorithm that splits the items to be sorted into two groups, *recursively* sorts each group, and *merges* them into a final, sorted sequence.

Pre-Conditions: An array of 1 or more elements

Post-Condition : A sorted array

Algorithm

- 1. Check if LB < UB
 - a. Call merge sort with
 - 1. Input Array
 - LB = LB
 - 3. UB = (UB + LB)/2
 - b. Call merge sort with
 - 1. Input Array
 - 2. LB = (UB + LB)/2 + 1
 - 3. UB = UB
 - c. Call merge with
 - 1. Merge with parameters
 - Array to be sorted
 - Lower bound
 - (Lower bound + Upper bound) / 2
 - (Lower bound + Upper bound) / 2 +1
 - Upper bound

The merge sort procedure will recursively call itself until it has only single element arrays. These are inherently sorted. It will then merge the successively larger elements until the whole sorted array is produced.

Merge

```
Pre-Conditions: An array of 1 or more elements, Legal values of Lower_Bound_1, Upper_Bound_1, Lower_Bound_2 and Upper_Bound_2,
```

Post-Condition: A merged array that is sorted

Algorithm

- 1. Check if
 - a. Lower_Bound_1 < Upper_Bound_1
 - b. Lower_Bound_2 < Upper_Bound_2
 - c. Lower_Bound_1 < Lower_Bound_2
 - d. Upper_Bound_1 < Upper_Bound_2
- 2. If any of the above conditions are violated,
 - a. Display Error
 - b. Stop Executing the program
- 3. Set
 - a. Index 1 := Lower Bound 1;
 - b. Index_2 := Lower_Bound_2;
 - c. Index := Lower Bound 1;
 - d. Temp_Array := Input_Array
- 4. While (Index_1 <= Upper_Bound_1) and (Index_2 < = Upper_Bound_2)
 - a. If (Input Array(Index 1) < Input Array (Index 2)
 - i. Temp_Array(Index) := Input_Array(Index_1)
 - ii. $Index_1 := Index_1 + 1$;
 - iii. Index := Index + 1;
 - b. Else
 - i. Temp_Array(Index) := Input_Array(Index_2)
 - ii. Index 2 := Index 2 + 1:
 - iii. Index := Index + 1;
- 5. While (Index_1 <= Upper_Bound_1)
 - a. Temp_Array(Index) := Input_Array(Index_1)
 - b. $Index_1 := Index_1 + 1$;
 - c. Index := Index + 1;
- 6. While (Index_2 <= Upper_Bound_2)
 - a. Temp_Array(Index) := Input_Array(Index_2)
 - b. Index 2 := Index 2 + 1;

```
c. Index := Index + 1;
```

7. Input_Array := Temp_Array

Binary Search

Pre-Conditions: Array to be searched

Item that you are searching for

Post-condition: Index location of the item you are searching for

Return -1 if the number is not found.

Algorithm

1. Set Return_Index to -1;

- 2. Set Current_Index to (Upper_Bound Lower_Bound + 1) /2.
- 3. Loop
- i. if the lower_bound > upper_boundExit:
- ii. if (Input_Array(Current_Index) = Number_to_Search) then
 Return_Index = Current_Index)
 Exit;
- iii. if (Input_Array(Current_Index) > Number_to_Search) then
 Lower_Bound = Current_Index +1
 else
 Upper_Bound = Current_Index 1
- 4. Return Return Index
- b. Write a program to test your package that will
 - Prompt the user for a number to search for.
 - If the number is found using the binary search algorithm
 - Display the location (index)
 - Display the number
 - If the number is not found using the binary search algorithm
 - Display "Number not in array to the user"

```
--- program to test Home_Work_9 Package
-- Programmer: Jayakanth Srinivasan
-- Date Last Modified: April 06,2004
--------
with Ada.Text_Io;
with Ada.Integer_Text_IO;
with Home_Work_9;
use Home_Work_9;
procedure Test_Hw_9 is
```

```
My_Test_Array: My_Array;
 Size
           : Integer;
 Location : Integer;
 Find: Integer;
begin
  -- create the array
 Create(My_Test_Array,Size);
  -- get number to search for from user
 Ada.Text_Io.Put("Please Enter the Number to Search For");
 Ada.Integer_Text_Io.Get(Find);
 -- display unsorted array to the user
 for I in 1.. Size loop
   Ada.Text_Io.Put_Line(Integer'Image(My_Test_Array(I)));
 end loop;
 Ada.Text_Io.New_Line;
 -- sort the array using the merge sort algorithm
 Merge_Sort(My_Test_Array,1,Size);
 -- display the sorted algorithm
 for I in 1..Size loop
   Ada.Text_Io.Put_Line(Integer'Image(My_Test_Array(I)));
 end loop;
 -- perform a binary search on the array
 Location:= Binary_Search(My_Test_Array, 1, Size, Find);
 if Location /= -1 then
   Ada.Text_Io.Put("Found number at");
   Ada.Text_Io.Put_Line(Integer'Image(Location));
   Ada.Text_Io.Put_Line(Integer'Image(My_Test_Array(Location)));
   Ada.Text_Io.Put_Line("Number Not Found in Array");
 end if;
end Test_Hw_9;
```

- 5. Implement the merge sort algorithm as an Ada95 program. Your program should
 - Read in N integers from an input file. (N is user defined <=50)
 - Sort using your merge sort implementation.
 - Display the sorted and unsorted inputs to the user

Solved in problem 4.