

APPLY EQUILIBRIUM TO FIND REACTIONS

$$+ \sum F_{x} = 0$$

$$+ \sum F_{y} = 0$$

$$+ \left(\sum M_{A} = 0\right)$$

$$V_{H}(4L) - P(2L) = 0$$

$$V_{H} = \frac{P}{2}$$

$$\Rightarrow V_{A} = \frac{P}{2}$$

TO DETERMINE THE DEFLECTION OF D, WE NEED TO EMPLOY COMPATIBILITY + CONSTITUTIVE LAWS.

OUR CONSTITUTIVE LAW FOR BAR DEFORMATION IS:

$$\int_{ij} = \frac{F_{ij} L_{ij}}{AE}$$

SO WE'LL MEED TO SOLVE FOR THE BAR FORCES
IN ORDER TO DETERMINE THEIR EXTENSIONS,
AND HENCE THE TRUSS DEFLECTION.

BECAUSE OF SYMMETRY, I ONLY NEED TO FIND YALF OF THE BAR FORCES. ALL OF THE PAIRS MIRRORED IN THE D-E AXIS WILL HAVE THE SAME BAR FORCE:

$$F_{AC}$$
 =  $F_{CH}$   $F_{BD}$  =  $F_{DC}$   
 $F_{AB}$  =  $F_{FH}$   $F_{CD}$  =  $F_{DC}$   
 $F_{BC}$  =  $F_{FC}$   $F_{CE}$  =  $F_{CC}$ 

SOLVE FOR INDEPENDENT BAR FORCES:

MOJ @ A:

Fac 
$$\Sigma F_{y} = \frac{\rho}{2} - F_{AB} \cos 46 = 0$$

$$F_{AB} = P/\sqrt{2}$$

$$\Sigma F_{x} = F_{Ac} + F_{AB} \sin 45 = 0$$

$$F_{AC} = -\frac{\rho}{2}$$

MOJ @ B:

$$F_{BC}$$
  $\Sigma F_{y=0} = F_{BC} + (P/\sqrt{2})_{\cos 45} = F_{BC} = -P/2$ 

$$\Sigma F_{x=0} = F_{BD} - (P/\sqrt{2})_{\sin 45}$$

$$F_{BD} = P/2$$

$$\sum_{F_{co}} F_{ce} = \frac{P}{2} - F_{co} \cos 45$$

$$F_{co} = \frac{P}{\sqrt{2}}$$

$$M_{D} = 0 = -F_{ce} k - \frac{P}{2} (2k) = 0$$

$$F_{ce} = -P$$

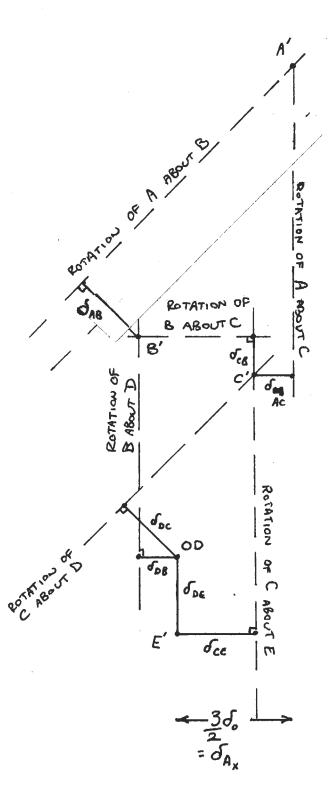
$$\Sigma F_{y} = 0$$

$$-P - F_{0E} = 0$$

$$F_{0E} = -P$$

| BAR   | FORCE $\left(\frac{F_{ij}}{P}\right)$ | LENGTH (Lij) | DEFORMATION SIJ/PL |
|-------|---------------------------------------|--------------|--------------------|
| - BAR | PORCE (P)                             |              |                    |
| AB    | + 1/12                                | √a           | + /                |
| Ac    | -1/2                                  | 1            | -1/2               |
| СВ    | - 1/2                                 | 1            | - 1/2              |
| CE    | -1                                    | I            | - 1                |
| CD    | 功                                     | 12           | +1                 |
| BD    | + ½                                   | 1            | + 1                |
| ED    | -1                                    | . 1          | - 1                |
| EG    | -1                                    | 1            | -1                 |
| DG    | + 1/2                                 | V2           | +1                 |
| DF    | + 1/2 + 2                             | . 1          | + 1/2              |
| GF    | - '2                                  | 1            | - ½                |
| CH    | - 1/2                                 | 1            | - <del>-</del> ā   |
| FH    | + 1/1/2                               | √2           | +1                 |

NOW WE CAN GO AHEAD AND PET OUR TRUSS DEFLECTION DIAGRAM. So AE



IF MY HINGE POINT A'
ENDS UP DISPLACED FROM
MY ORIGIN BY OA, AND OA,
THEN BY ORIGIN OD IS
DISPLACED FROM A' BY
- OA, AND - OA,

1300 = OAY FIXED FRAME OA, WHERE
A AND A ARE THE SAME,
I CAN FIND THE DEFLECTION
OF D'IN THE FIXED
FRAME, WHICH IS JUST
ITS DISPLACEMENT FROM
A, NAMELY
-OA I - OAYI.

THE JOINT D WILL TRANSLATE

DOWN BY 13 PL
AND

LEFT BY 3 PL
2 AE

## ESTIMATE OF TRUSS DEFLECTIONS

BARS IN EXPERIMENTAL TRUSS MADE OF STEEL
-HOLLOW WITH 22 MM OUTER DIAMETER AND
1.5 MM WALL THICKNESS (IENORE END FITTINGS)

 $A \approx 2\pi r + \approx 10.5 \times 10^{-3} \times 2 \times \pi \times 1.5 \times 10^{-3}$ 

L = 0.5 m

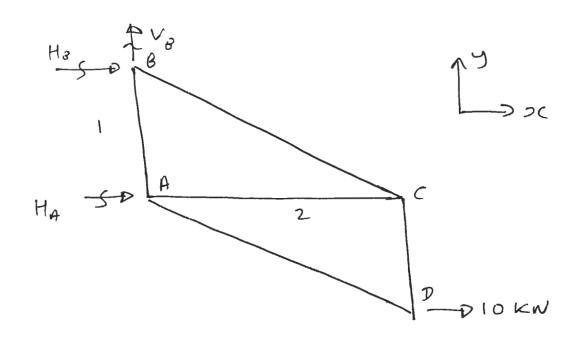
E = 210 GPa

CENTER POINT DEFLECTION

$$\frac{d_{D}}{P} = \left(\frac{0.5}{100 \times 10^{6}} \times 210 \times 10^{9}\right) \left(\frac{-13}{2}\hat{j} - \frac{3}{2}t\right)$$

$$\frac{\delta_{0}}{P} = -\frac{3}{2} \frac{1 \times 10^{-7}}{\hat{2}} \hat{j} - \frac{7.1 \times 10^{-8}}{2} \hat{i} \frac{m}{N}$$

M9



$$\{\vec{F}_{A} = 0: 10 + H_{8} + H_{A} = 0$$
 (1)

Box Truces

FAD 
$$A^{FcD}$$
 ( $\omega s O = \frac{2}{\sqrt{5}}$ 

$$Sin O = \frac{1}{\sqrt{5}}$$

$$\Sigma \vec{F}_{x} = 0$$
 -  $F_{AD} \cos \theta + 10 = 0 \Rightarrow F_{AD} = \frac{10.55}{2} = +11.2 \text{ kW}$ 

$$\Sigma F_{\gamma} 1 = 0$$
  $F_{AD} \sin \Theta + F_{CD} = 0$   
 $F_{CD} = -F_{AD} \sin \Theta = -10.45 \cdot 1 = -5 \text{ kN} = -5 \text{ kN}$ 

FAC 
$$OCO = \frac{1}{\sqrt{5}}$$
 $Cos O = \frac{2}{\sqrt{5}}$ 

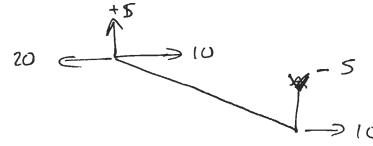
$$SiO = \frac{1}{\sqrt{5}}$$

$$\cos O = \frac{2}{\sqrt{5}}$$

$$F_{cg} = + - \frac{5}{5} F_{cp} = - \frac{5}{5} \text{ KN} \in$$

$$Sin O = \frac{1}{\sqrt{S}}$$

## check MUS



OK!

Baw Twee (KN) F/P Length Length 
$$\frac{\delta}{AE} = \frac{\delta}{AE} \times 10^3$$
AB +5 +\frac{1}{2} | 1 | 1 + \frac{1}{3}\frac{1}{2} | +5

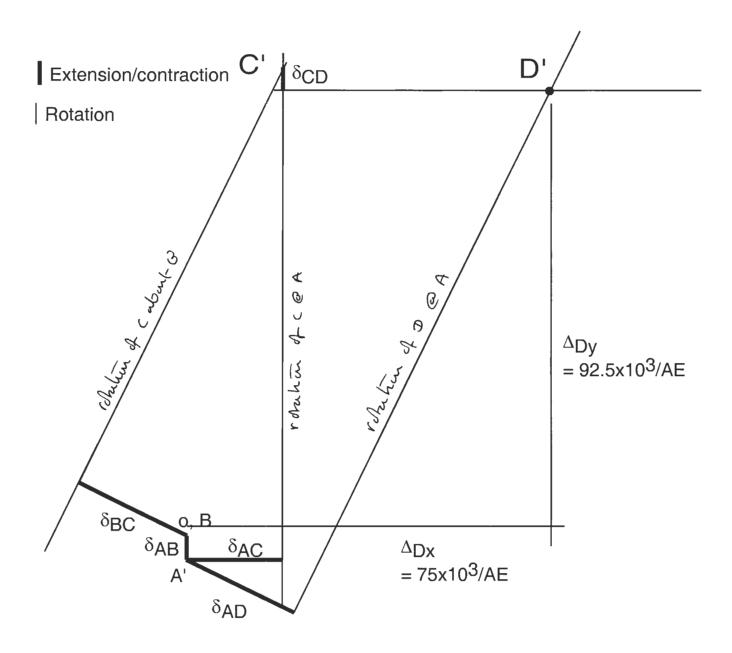
AC +10 +1 | 2 | 2 | +2 | +20

BC -5\sqrt{5} | -\frac{15}{2} | \sqrt{5} | \sqrt{5} | -\frac{5}{2} | -25

AD +5\sqrt{5} | +\sqrt{5}/2 | \sqrt{5} | \sqrt{5} | \sqrt{5} | +\frac{5}{2} | +25

CD -5 -\frac{1}{2} | 1 | -\frac{1}{2} | -5

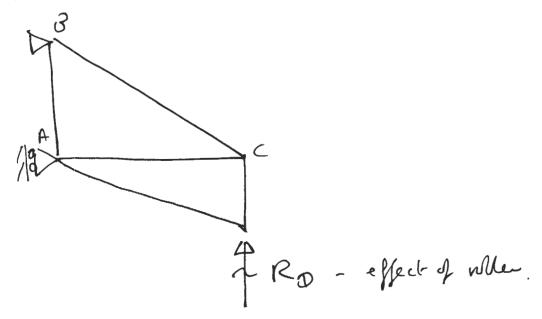
Draw dis placement diagram (see attached)



10<sup>3</sup>/AE

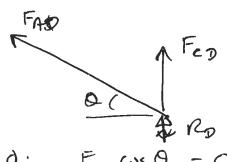
## M10

Use superposition (or set up as a set of unknowns)

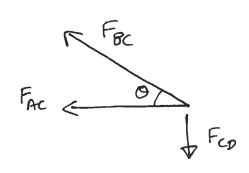


$$H_A = -2R_D$$

Bor fires: Melhod of jonts



$$\{F_{\lambda}=0: F_{AD}\cos\theta=0\} = F_{AD}=0$$

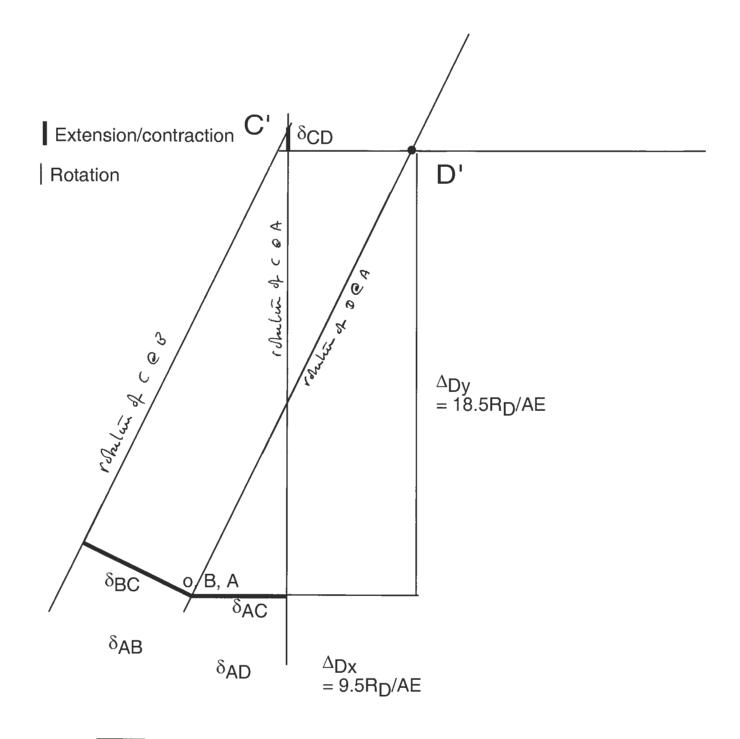


Cos 0 = NS

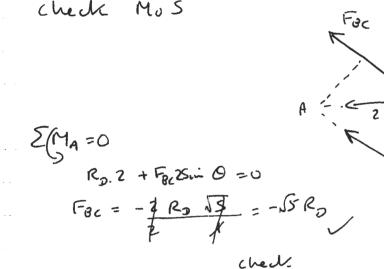
5,i0 = 1

$$\Sigma \overrightarrow{F_{x}} = 0 : -F_{AC} - F_{BC} \cos \Theta = 0$$

$$F_{AC} = R_{DA} \overrightarrow{F_{BC}} = 2R_{D} = 2R_{D}$$



2R<sub>D</sub>/AE



Don displacement diagram

D displaces upward 
$$\triangle Dy = 18.5 R_D$$
 $AE$ 

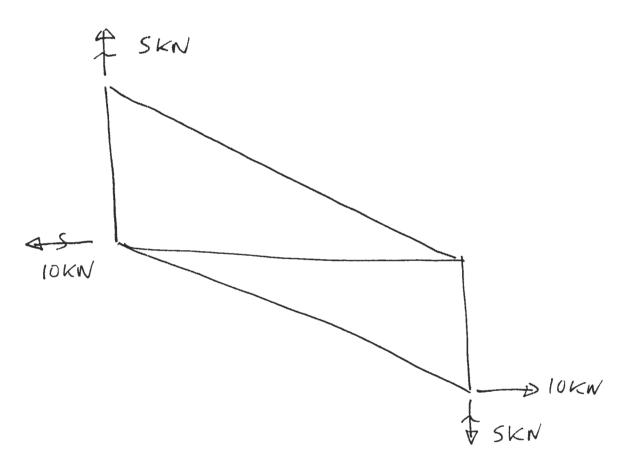
$$\frac{92.5 \times 10^{3}}{DE} + \frac{18.5 R_{D}}{DE} = 0 \qquad R_{D} = -\frac{92.5 \times 10^{3}}{18.5} = -5 \text{ RN} \in$$

Harisahl deflection:

$$\Delta D_{x}^{Mq} + \Delta D_{x}^{M10} = \frac{75 \times 10^{3}}{AE^{-}} + (9.5 \times -5) \times 10^{3} = 786 \times 10^{-6}$$

Reactions

$$R_{H_8} = H_8^{M_9} + H_8^{M_{10}} = +10 + 2(-5) = 0$$
 $H_A = H_A^{M_9} + H_A^{M_{10}} = -20 + 2(-2(-5)) = -10 \text{ kW} = 10 + 2(-5) = -10 + 2(-5) = -10 \text{ kW} = 10 + 2(-5) = -10 + 2(-5) = -10 + 2(-5)$ 

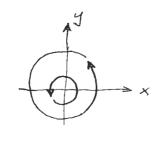


$$\frac{dy}{dx} = \frac{v}{u} = \frac{x}{y}$$

$$y dy = -x dx$$

$$\frac{1}{2}y^{2} = -\frac{1}{2}x^{2} + C$$

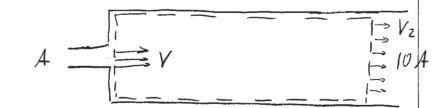
$$x^2 + y^2 = 2C$$



 $x^2 + y^2 = 2C$  circles of radius  $\sqrt{2C}$ 

For steady flow, with p= const, must have V. V = du + dy = 0  $2i = \frac{-y}{x^2 + y^2} \qquad \frac{\partial y}{\partial x} = \frac{y \cdot 2x}{(x^2 + y^2)^2}$   $V = \frac{x}{x^2 + y^2} \qquad \frac{\partial y}{\partial y} = \frac{-x \cdot 2y}{(x^2 + y^2)^2}$ 

Control Volume:



a) mass conservation

$$\oint e^{\vec{V} \cdot \hat{n}} dA = -e^{VA} + e^{V_2} (10A) = 0 - V_2 = \frac{1}{10}V$$

6) momentum conservation

$$0 = \oint [p\hat{n} + \rho(\vec{V} \cdot \hat{n}) \vec{V}] dA = -p, 10A - \rho V.A + p_2 \cdot 10A + \rho V_2^2 \cdot 10A$$

$$0 = (p_2 - p_1) \cdot 10A + \rho (-V^2 + \frac{1}{10}V^2) A$$

$$p_2 - p_1 = \frac{9}{100} \rho V^2 A$$

Control Volume:

By mass conservation, V2 = V



Because flow is periodic, V3 = V4, P3 = P4 And since  $\hat{n}_4 = -\hat{n}_3$ , then sides 3 and 4 will cancel in momentum integral.

 $\mathcal{G}(p\hat{n} + \varrho\vec{V} \cdot \hat{n} \vec{V}) dA + \mathcal{G}(p\hat{n} + \varrho\vec{V} \cdot \hat{n} \vec{V}) dA = -\vec{F}$ 

By symmetry, & ph dA + \$ ph dA = 0

\$(pv.nv)d1 + \$ppv.nvd4 = - F

$$-\rho V_{\frac{\sqrt{2}}{2}} \cdot V_{\frac{\sqrt{2}/2}{\sqrt{2}/2}} h + \rho V_{\frac{\sqrt{2}}{2}} \cdot V_{-\frac{\sqrt{2}/2}{2}} = -\vec{F}$$

F = OV2H Vertical Force