M3

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 $\Sigma F_{\gamma} \Lambda = 0 \qquad V_{A} - 10 - 10 + S = 0$ $V_{A} = 15 \text{ km} \subseteq$

 $\sum_{A} = 0: M_{A} - 10 \times 1 - 10 \times 2 + 5 \times 3 = 0$

MA = 15 knm =

mococci 15km/ A X/S M 15km

 $\Sigma F_{y} = 0$ 1S - S = 0 S = 1S RW

 $\Sigma(M_X = 0: M - 1500 + 15 = 0$

M= 15x-15 (RNm)

$$\frac{1}{15} = \frac{1}{15} = \frac{1}{15}$$

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2.0

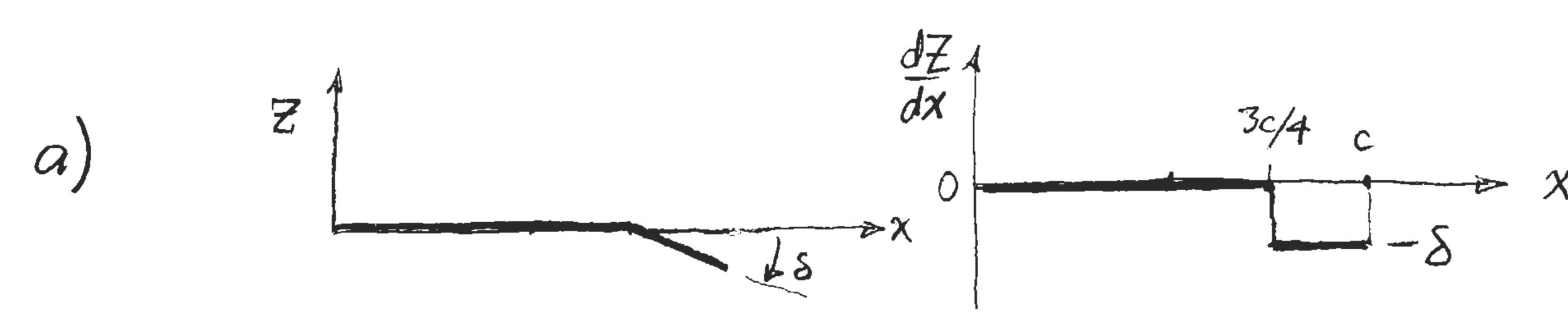
$$\sum_{i=1}^{n} \sum_{j=1}^{n} \sum_{j$$

$$\frac{1}{2} = \frac{1}{2} = \frac{1}$$

10 kw 10 km M * * * . . . A 4 W **.** 44. F F S . . . 4.1.5 1 4 4

.

4 - 4



$$\frac{\chi_h}{c} = 0.75, \quad \theta_h = \arccos\left(1 - 2\frac{\chi_h}{c}\right) = \frac{2\pi}{3} \quad \frac{d^2}{dx}$$

$$\frac{2\pi}{3} \quad \pi$$

b)
$$A_0 = x - \frac{1}{\pi} \int_0^{\pi} \frac{dz}{dx} d\theta = x - \frac{1}{\pi} \int_0^{\pi} - \delta d\theta = x - \frac{1}{\pi} (\pi - \frac{2\pi}{3})(-\delta) = x + \frac{1}{3}\delta$$

$$A_1 = \frac{2}{\pi} \int_0^{\pi} \frac{dz}{dx} \cos \theta d\theta = \frac{2}{\pi} \int_0^{\pi} - \delta \cos \theta d\theta = \frac{2}{\pi} (-\delta) (\sin \theta)^{\pi} = 0.551 \delta$$

$$A_2 = \frac{2}{\pi} \int_0^{\pi} \frac{dz}{dx} \cos 2\theta d\theta = \frac{2}{\pi} \int_0^{\pi} - \delta \cos 2\theta d\theta = \frac{2}{\pi} (-\delta) (\frac{\sin 2\theta}{2})^{\pi} = -0.276 \delta$$

$$C_{\ell} = \pi \left(2A_0 + A_1 \right) = 2\pi \left(x + 0.6098 \right)$$

$$C_{m,c/4} = \frac{\pi}{4} (A_2 - A_1) = -0.6498$$

C)
$$\frac{\partial c_{\ell}}{\partial s} = 2\pi \cdot 0.609 = 3.826$$

 $\frac{\partial c_{m}}{\partial s} = -0.649$

42-381 50 SHEETS 5 SQUARE 42-382 100 SHEETS 5 SQUARE 42-389 200 SHEETS 5 SQUARE

a) Assuming L'is uniform across the span,

$$D_i' = L \alpha_i = L \frac{W}{V_0}$$

$$D_{i} = D_{i}b = Lb\frac{w}{V} = L\frac{w}{V} = \frac{L^{2}}{2\rho V_{o}^{2}b^{2}} = \frac{L^{2}}{\frac{1}{2}\rho V^{2}} \frac{1}{4b^{2}}$$

$$C_{D_i} = \frac{D_i}{\frac{1}{2}\rho V_o^2 S} = \frac{L^2}{(\frac{1}{2}\rho V_o^2)^2 S^2} \cdot \frac{S}{4b^2} = \frac{C_L^2}{4R}$$

b)
$$C_L = 2\pi \alpha_{eff} = 2\pi (\alpha - \alpha_i)$$

ignore
$$\alpha_{L=0}$$
, no effect on $\frac{dC_L}{d\alpha}$

but we have
$$C_{D_i} = \alpha_i C_L$$
, or $\alpha_i' = \frac{C_{D_i}}{C_L} = \frac{C_L}{4R}$

$$\Rightarrow C_L = 2\pi(\alpha - \frac{C_L}{4R})$$

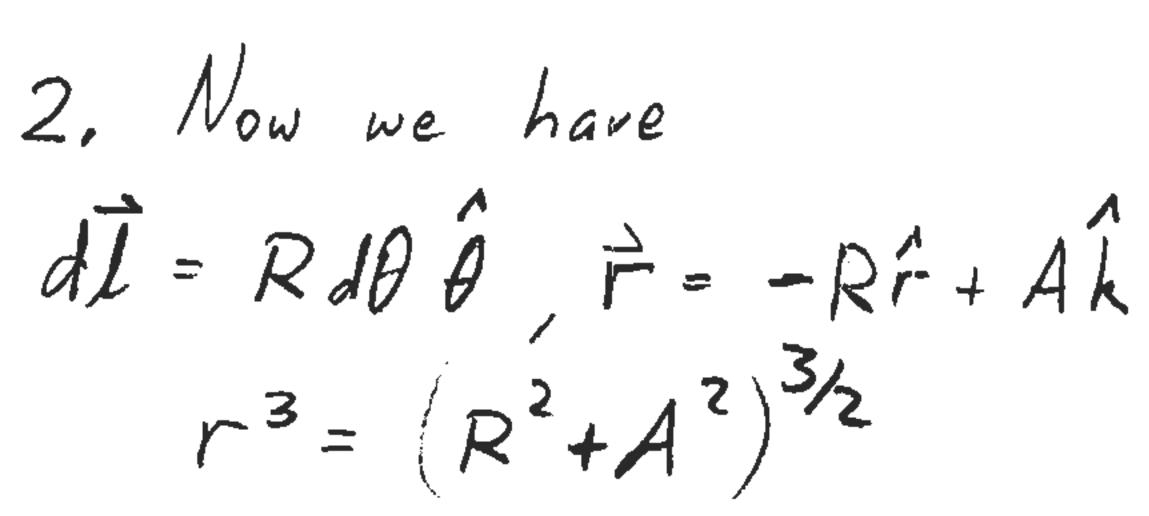
$$C_{L}\left(1+\frac{\pi}{2R}\right)=2\pi\alpha$$

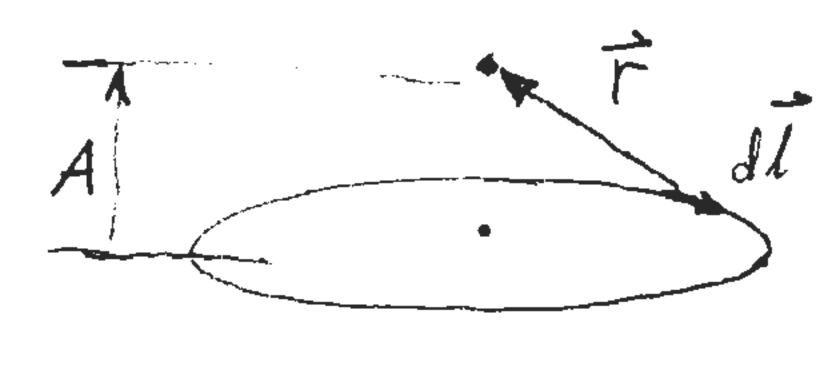
$$C_{2}(\alpha) = \frac{2\pi}{1+\frac{\pi}{2R}} \alpha$$

$$\frac{dC_L}{d\alpha} = \frac{2\pi}{1+\frac{\pi}{2R}}$$

small than 2-D value of ZIT
by factor of $\frac{1}{1+\frac{T}{2R}}$

UE Fluids F6 Solution Spring 04 (Anderson p 416) 1. $\vec{V} = \frac{\Gamma}{4\pi} \int \frac{d\vec{l} \times \vec{r}}{r^3}$ $d\vec{l} = R d\theta \ \theta \ \vec{r} = -R \vec{r} \ r = R$ $d\vec{l} \times \vec{r} = -R^2 d\theta \ \theta \times \vec{r} = -R^2 d\theta \ \hat{k}$ $\vec{V} = \frac{\Gamma}{4\pi} \int_{0}^{2\pi} \frac{2\pi}{R^3} d\theta \ \hat{k} = -\frac{\Gamma}{2R} \ \hat{k}$ 2. Now we have





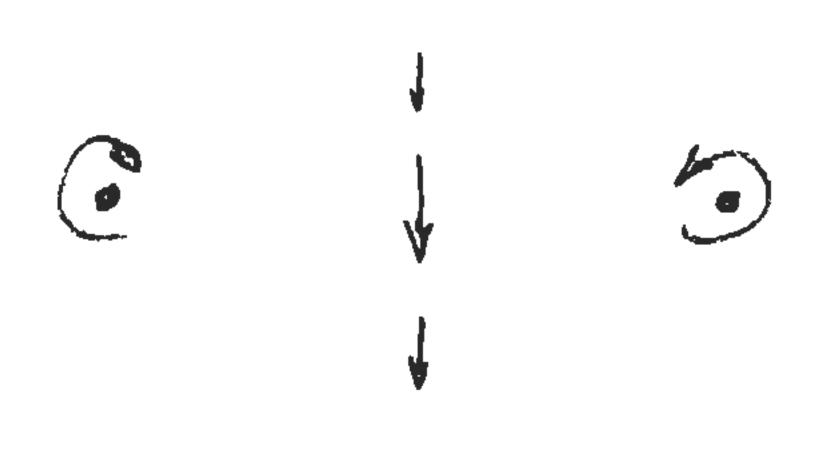
 $d\vec{l} \times \vec{r} = (-R^2(\hat{\theta} \times \hat{r}) + RA(\hat{\theta} \times \hat{k})) d\theta = (-R^2\hat{k} - RA\hat{r}) d\theta$ Note that \hat{k} is constant, but \hat{r} depends on θ (varies around circle)

$$\vec{V} = \frac{\Gamma}{4\pi} \int_{0}^{2\pi} \frac{-R^{2}\hat{k} - RA\hat{r}}{(R^{2} + A^{2})^{3}/2} d\theta$$

$$\vec{V} = -\frac{\Gamma}{2} \frac{R^{2}}{(R^{2} + A^{2})^{3}/2} \hat{k} + \frac{\Gamma}{4\pi} \frac{-RA}{(R^{2} + A^{2})^{3}/2} \int_{0}^{2\pi} d\theta \hat{r}$$

But we note that $\int_{0}^{2\pi} f d\theta = 0$, since \hat{r} cancels when integrated around perimeter.

$$\frac{1}{2} = -\frac{1}{2} \frac{R^2}{(R^2 + A^2)^{3/2}} k$$



M4

A

$$\frac{1}{2}$$
 $\frac{1}{2}$
 $\frac{1}{2}$

Mumant duahabatun

$$-25 - 5' + \int 5 - 2 doc = 0$$

$$5' = \left[5x - 2^2\right]^{\times} - 25 = 5x - x^2 - 25 = 0$$

$$\sum_{x=0}^{\infty} (M_{x}=0)M_{x}-83.3+\int_{2}^{\infty} (S-2C)x dsc-\int_{2}^{\infty} 2C=0$$

$$M_{x}-83.3+\frac{5x^{2}-2C^{2}-5x^{2}+2C^{2}+2C}{6}$$

$$M = -\frac{1}{12}x^3 + \frac{5}{2}x^2 - 25x + 83.3 = \frac{1}{2}$$

Max benduing stress at rost so 0 7: 1 1 when

Mmax = 83.3 RNM @ 5000

+ 1 =

$$= \frac{6 \times 83.3 \times (0^{3})^{2}}{50 \times 10^{-3} \times (100 \times 10^{-3})^{2}} = 1.60 \text{ (high)}$$

M4 tip deflection, fin moment constitue

Integrale mount wice ->

$$EIW = -\frac{1}{12} \frac{3c^{5}}{70} + \frac{5}{2} \frac{3c^{4}}{12} - \frac{253c^{2}}{6} + 83.33c^{2} + 8$$

$$EIW = \frac{3C}{240} + \frac{50c^4}{24} - \frac{25x^3}{6} + 83.3 x^3$$

d- hp 20=0

$$\delta = \frac{1}{EI} \left[\frac{-10^{S}}{240} + \frac{5.10^{4}}{24} - \frac{25\times10^{3}}{6} + \frac{83.10^{3}}{2} \right] = \frac{1650\times10^{3}}{EI}$$

$$E = 70 \times 10^9$$
, $T = \frac{1}{12} \times 50 \times 10^3 \times (100 \times 10^{-3})^3 = 4.17 \times 10^{-6}$

 $\mathcal{E} = \frac{1650 \times 10^3}{70 \times 10^9 \times 4.17 \times 10^{-6}} = 5.66 \text{ M}. \subseteq$

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deflection

CANAL PROCESS OF THE **建筑**和工作的企业,1975年,1976年,1986年, ,这分别是一种,我们都被我们的一种的人,我们就是一个是我们的人,我们不是一个人,我们就是一个人,我们也不是我们,我们也是我们的人,我们也是<mark>是我们的人,我们就是这个人</mark> : -- ٠. · · 2(M=0:34VB-PL=0:VB=P, (5Mx=0: M-2Poc=0 (SMx=0: M+P(2(-2)-2P2(=0 MERZHPL Part March

Apply boundary conditions

• . .

$$\frac{\partial x = L}{\partial w'} = \frac{dw^2}{dsc} \Rightarrow \frac{2PL^2 + A = -PL^2 + PL^2 + C}{6}$$

$$\omega^1 = \omega^2$$

$$\frac{2PL^{3}}{18} + AL = -\frac{PL^{3}}{18} + \frac{PL^{3}}{2} + CL + D$$

$$(A-C)L = \frac{PL^2}{3} + D$$

Subshbule in (1)
$$3PL^2+3CL+PL^2=0$$

 $S=\frac{1}{3}(-3PL^2-PL^2)=-\frac{19PL^2}{18}$

hv 220234

$$\omega = \frac{1}{61} \left(\frac{-Poc^{2}}{18} + \frac{PLoc^{2}}{2} - \frac{19PLx + PL^{3}}{6} \right)$$

Max deflection atom dar. O between 02266?

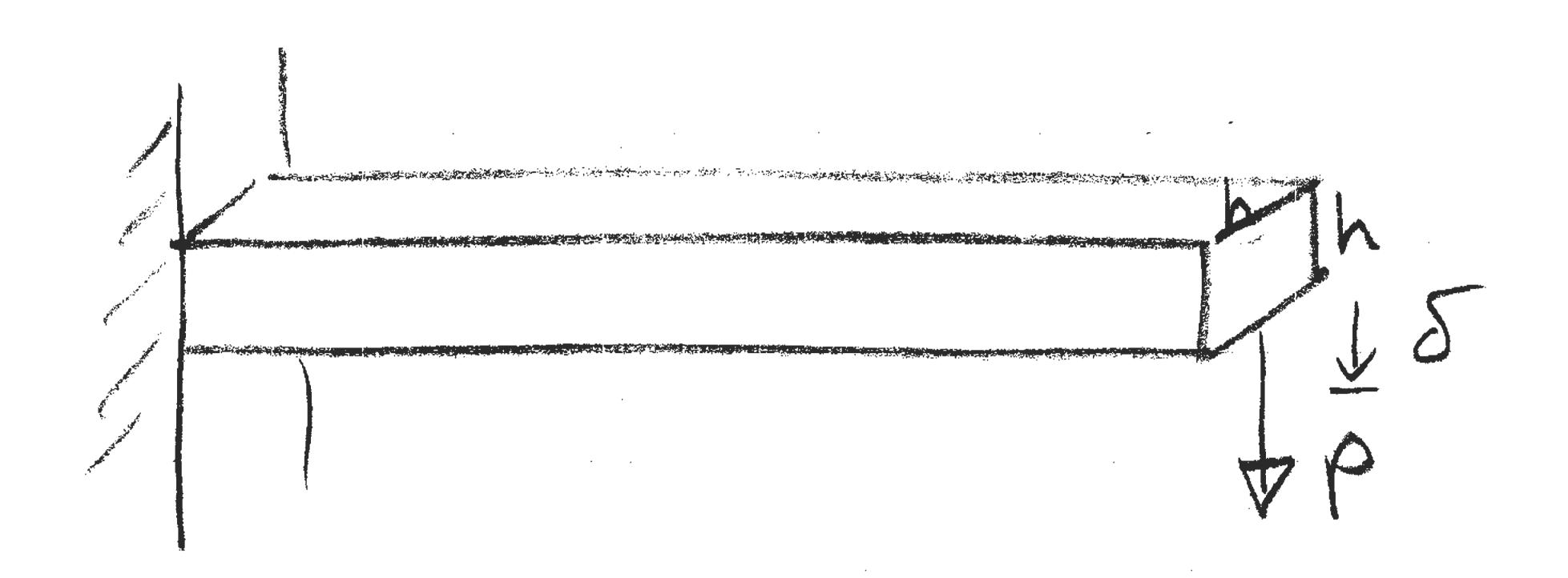
behveen 2 = 3 = 3 = 00 1 = 3 = 3

Rust between Land 32 = 20 = 1.37 L

$$= \delta = \frac{\rho L^2}{EI} \left(\frac{-1}{5} \right) = \frac{-\rho L^2}{5EI} = \frac{-\rho L^2}{5EI}$$

Note Mis dues not occur at DC= & where M= maximu.

M6



For Cantilever bean $S = \frac{PL^3}{3eI}$, $\sigma_{max} = \frac{PL}{2}$ $I = \frac{1}{12}h^4$

Mans of bean = PLA = PLh = m

density

Mar Shymens of bean: $P = \frac{3EI}{2} = \frac{3}{12}\frac{h^4 E}{L^3}$

elmate h² h² = e M eL

 $\frac{1}{8} \cdot \text{Sulphen} = \frac{1}{8} = \frac{1}{4} \left(\frac{M}{eL} \right)^2 = K$

max Shippers for given mans (or vice « versu)

requires max E2

 $\frac{1}{2} \frac{\partial}{\partial x} = \frac{1}{2} \frac{\partial}{\partial x} = \frac{1}{2} \frac{\partial}{\partial x}$

mans of beam, m = en2L

elmmale mh

$$P_{mx} = \frac{5}{6L} \left(\frac{m}{eL} \right)^{3/2}$$

So mu Pru Juin man required

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	E/GA	Of Marin		End 2	54 3/2
			7900	3092	2044
	_		7800	9056	2362
CERA	120		4500	5926	2815
Vood			1500	3 1111	120506
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			3000	JUVU C	1826

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7 0 L

e) a) Sic has the highest 6/e², but may be improvedical breams of its low boughness better dwices might be word a CFRP

6) CFRP has the highest 54/e3/2

omer factures - boughners, environmented dumbility, cost

d'I + 60x sectures are shuctually efficient becourse they more material away from the neutral axis of the beam.

The Key issue in selecting the obayce of a beam is the ability to manufacture the shape in question,

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