## 10.37 Chemical and Biological Reaction Engineering, Spring 2007 Prof. K. Dane Wittrup

## Lecture 14: Kinetics of Non-Covalent Biomolecular Interactions

This lecture covers: Significance, typical values and diffusion limit, approach to equilibriu, and multivalency

## Noncovalent Interactions

Figure 1. Protein-ligand binding.

Association rate = 
$$k_{on}C_pC_L$$
  
Dissociation rate =  $k_{off}C_c$   
@ equilibrium,  $k_{on}C_pC_L = k_{off}C_c$ 

$$\frac{C_p C_L}{C_c} = \frac{k_{off}}{k_{on}} = K_d$$

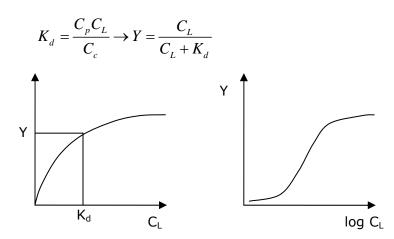
$$\frac{L}{\text{mol s}}$$

In general, for protein-protein interactions,  $k_{on} \approx 10^5 \, mol^{-1} s^{-1}$ 

half-time for complex dissociation  $au_{\mathrm{l/2}} = \frac{\ln 2}{k_{\mathrm{off}}}$ 

Fractional saturation 
$$Y = \frac{C_c}{C_{p,o}} = \frac{C_c}{C_c + C_p}$$

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**Figure 2**. Left: Graph of fractional saturation versus ligand concentration. Right: Graph of fractional saturation versus the logarithm of ligand concentration.

If 
$$C_{p,o} \approx C_{L,o}$$
, then at equilibrium,  $C_L \neq C_{L,o}$  
$$Y = \frac{C_{L,o} - yC_{p,o}}{C_{L,o} - yC_{p,o} + K_d}$$
 
$$Y = \frac{K_d + C_{L,o} + C_{p,o} - \sqrt{(K_d + C_{L,o} + C_{p,o})^2 - 4C_{p,o}C_{L,o}}}{2C_{p,o}}$$

If instead 
$$C_{L,o}\gg C_{p,o}$$
 ,  $C_L\approx C_{L,o}$  
$$Y=\frac{C_{L,o}}{C_{L,o}+K_d}$$

How quickly is equilibrium reached?

$$\frac{dC_c}{dt} = k_{on}C_LC_p - k_{off}C_c$$

If 
$$C_{L,o}\gg C_{p,o}$$
 "pseudo-1st order" 
$$k_{on}C_L=k_{on}C_{L,o}$$
 
$$C_{p,o}=C_p+C_c$$
 (complexed) 
$$C_p=C_{p,o}-C_c$$

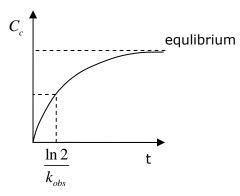
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$$\begin{split} \frac{dC_{c}}{dt} &= k_{on}C_{L,o}C_{p} - k_{off}C_{c} = k_{on}C_{L,o}(C_{p,o} - C_{c}) - k_{off}C_{c} \\ &= k_{on}C_{p,o}C_{L,o} - (k_{on}C_{L,o} + k_{off})C_{c} \end{split}$$

$$\begin{split} & \Rightarrow C_c(t) = C_{p,o} \, \frac{C_{L,o}}{C_{L,o} + K_d} (1 - e^{-k_{obs}t}) \\ & k_{obs} = k_{on} C_{L,o} + k_{off} \\ & \frac{\ln 2}{k_{obs}} = \text{half-time for reaching equilibrium} \end{split}$$



**Figure 3**. Concentration of complex versus time. Equilibrium is approached at long times.

## **Biosensor**

Surface plasmon resonance (label-free)

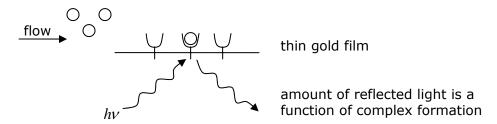


Figure 4. Schematic of how surface plasmon resonance works.

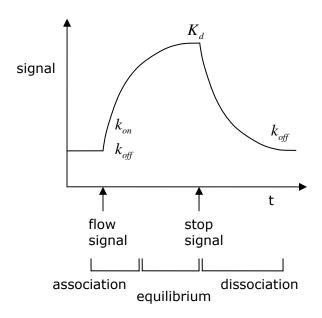


Figure 5. Signal of detector versus time.

redundant estimates:  $k_{o\!f\!f}$  in both association & dissociation,  $K_d=\frac{k_{o\!f\!f}}{k_{o\!n}}$  in equilibrium phase

best approach: fit one set of parameters to three phases of experiment. (global least squares)

Multivalency (Avidity)

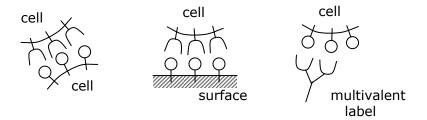


Figure 6. Three examples of multiple protein-ligand binding.

How does multivalency effect apparent interaction strength?

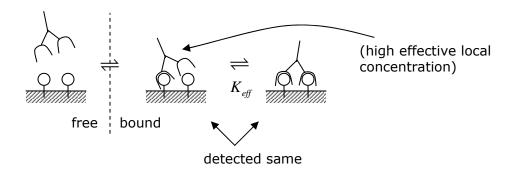


Figure 7. Multivalent binding equilibrium.