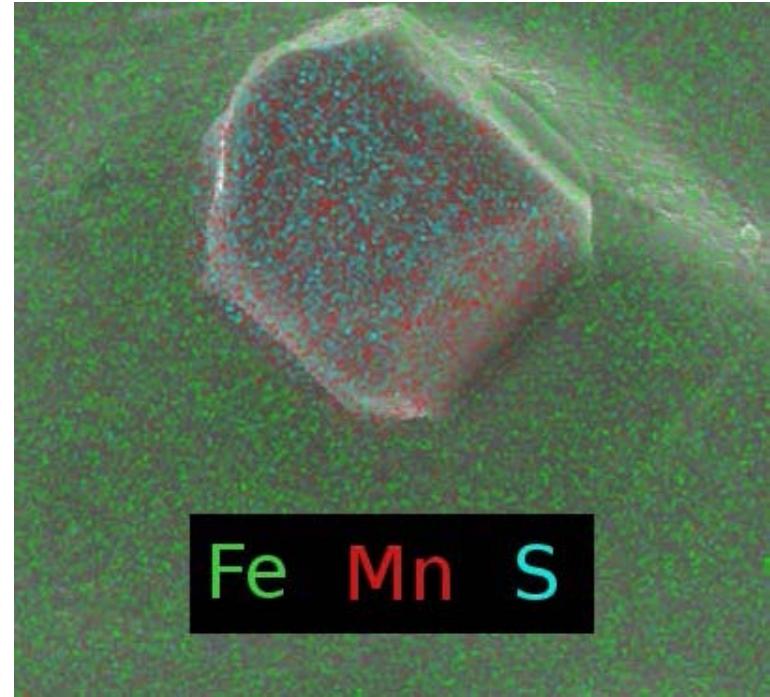

A Survey of Crystalline Defects

Outline – Defects

- 0D Defects
 - Vacancies & Interstitials
- 1D Defects (Dislocations)
- 2D Defects
 - Grain & twin boundaries
- 3D Defects
 - Coherent vs. incoherent inclusions, precipitates



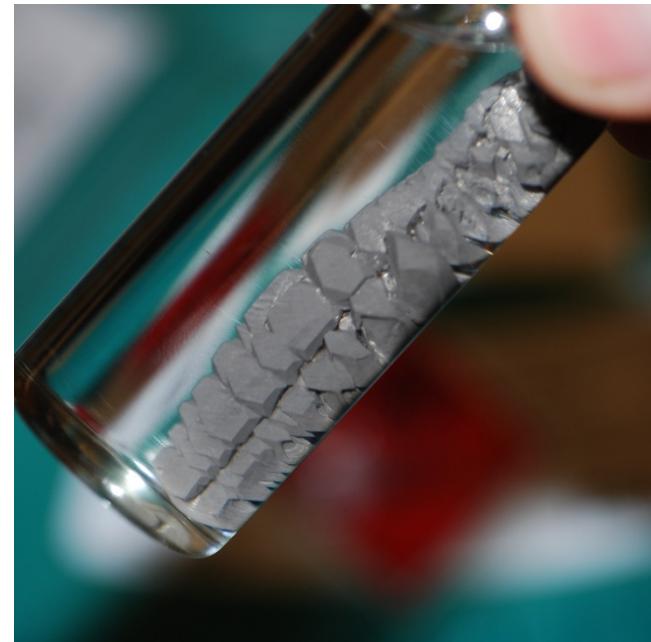
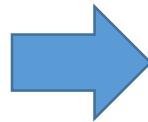
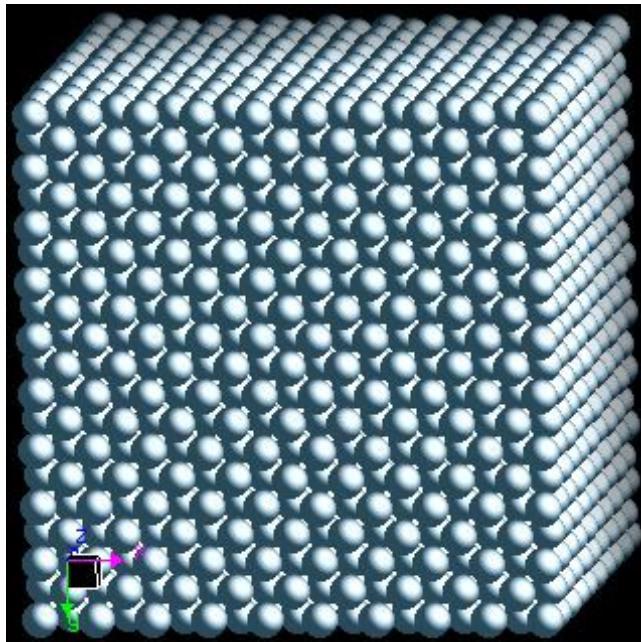
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Single crystal of MnS, space group Fm $\bar{3}$ m, FCC crystal structure

Crystalline Solids

http://www.webelements.com/calcium/crystal_structure.html

- Periodic, long-range ordered structures



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Face centered cubic calcium
crystal structure

Single crystals of calcium metal
under kerosene

Form Follows Structure

http://www.zkg.de/en/artikel/bildpopup_en_1698578.html?image=5

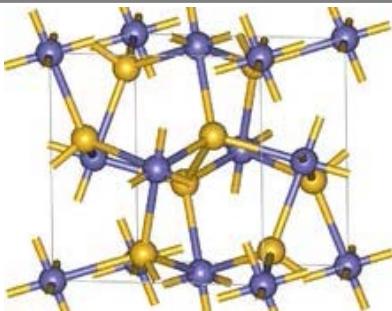
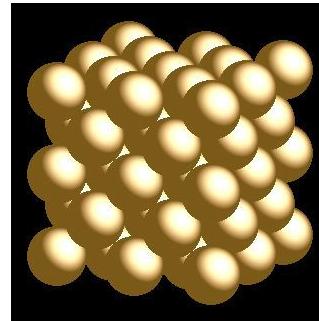


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**Pyrite (FeS_2), simple
cubic (SC)**
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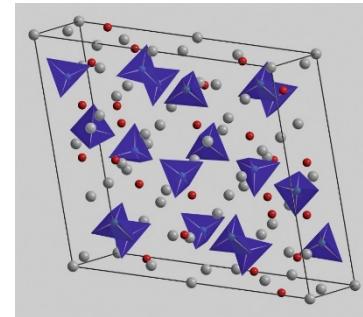


Courtesy of Mark Winter.
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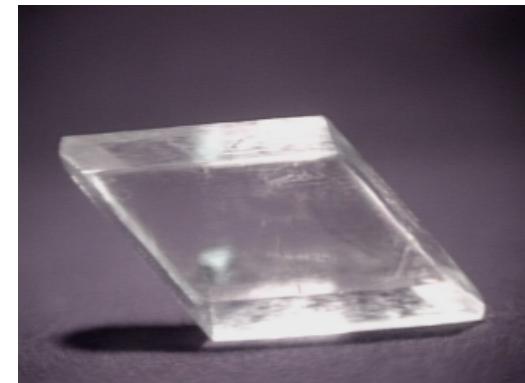


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**Gold (Au), face centered
cubic (FCC)**
[http://www.palaminerals.com/
news_2007_v2.php](http://www.palaminerals.com/news_2007_v2.php)



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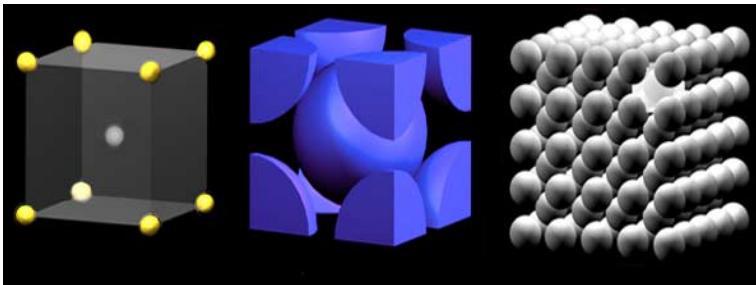


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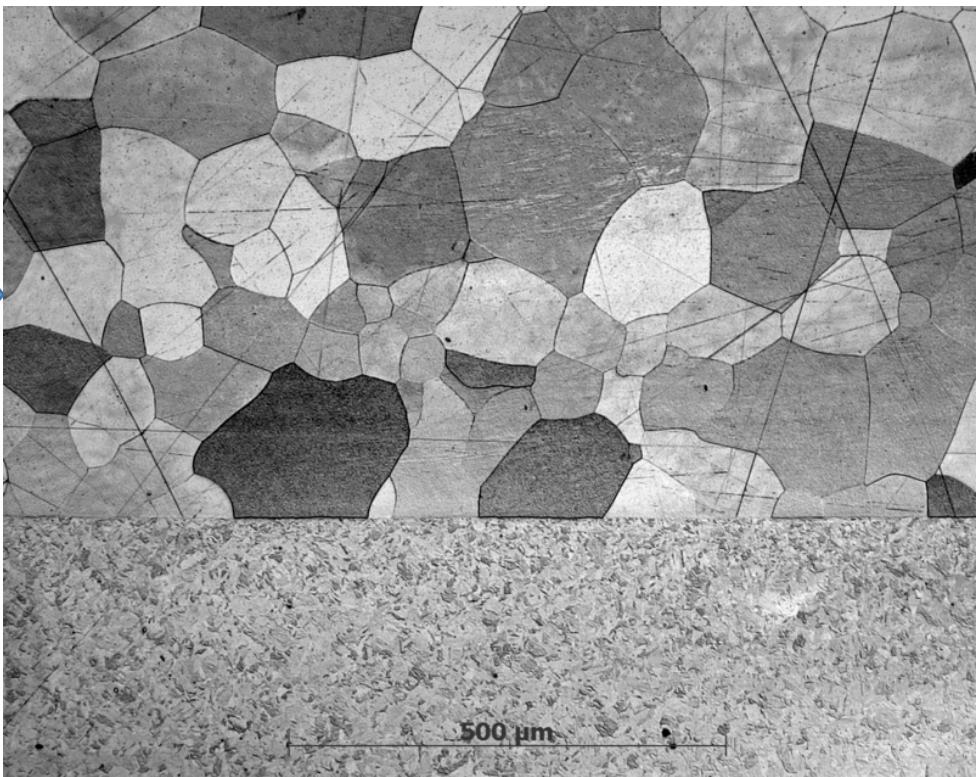
Gypsum, monoclinic
[http://www.galleries.com/minerals/
symmetry/monoclin.htm](http://www.galleries.com/minerals/symmetry/monoclin.htm)

Grain vs. Crystal Structure

- Why do grains look more spherical, when crystal structures are cubic?



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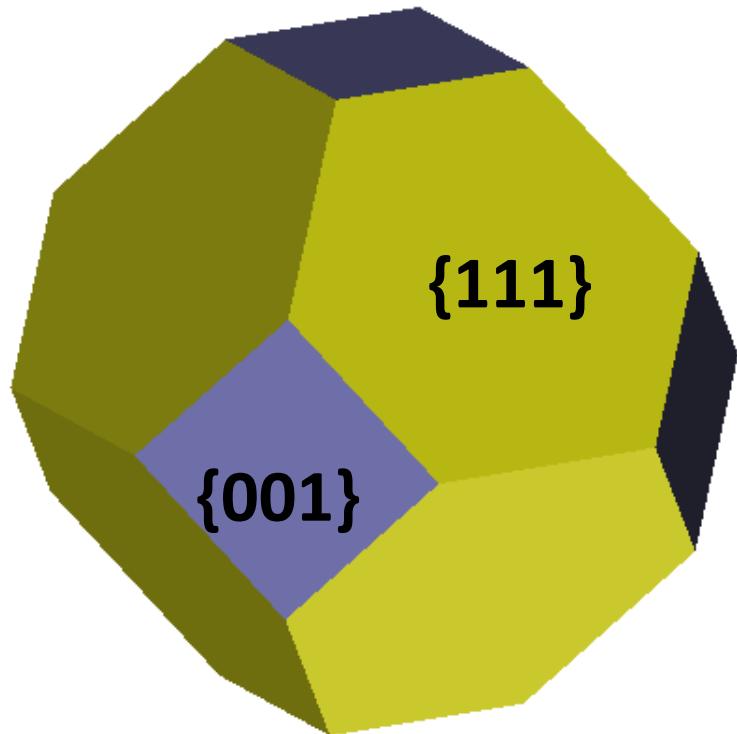


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Body centered cubic (BCC) iron crystal structure (left), micrograph of Fe-12Cr-2Si (right)

Grain vs. Crystal Structure

- Wulff crystals describe *lowest energy* surfaces
- Exposing *close packed planes* lowers surface energy

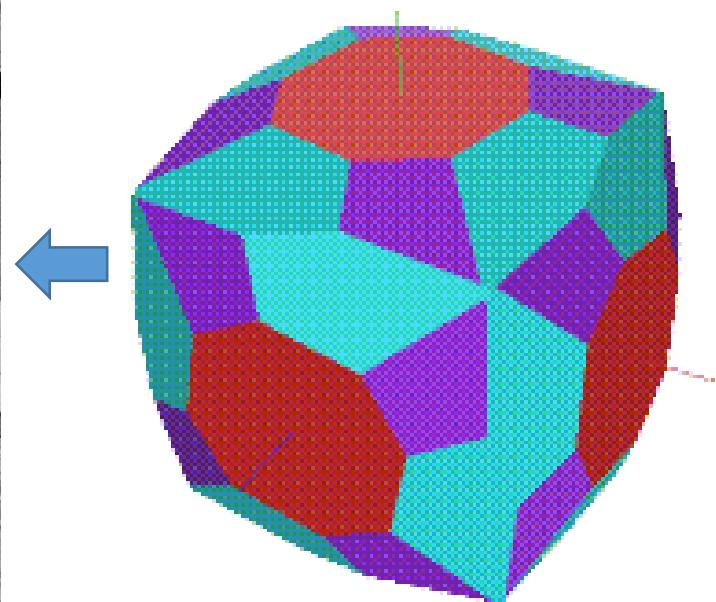
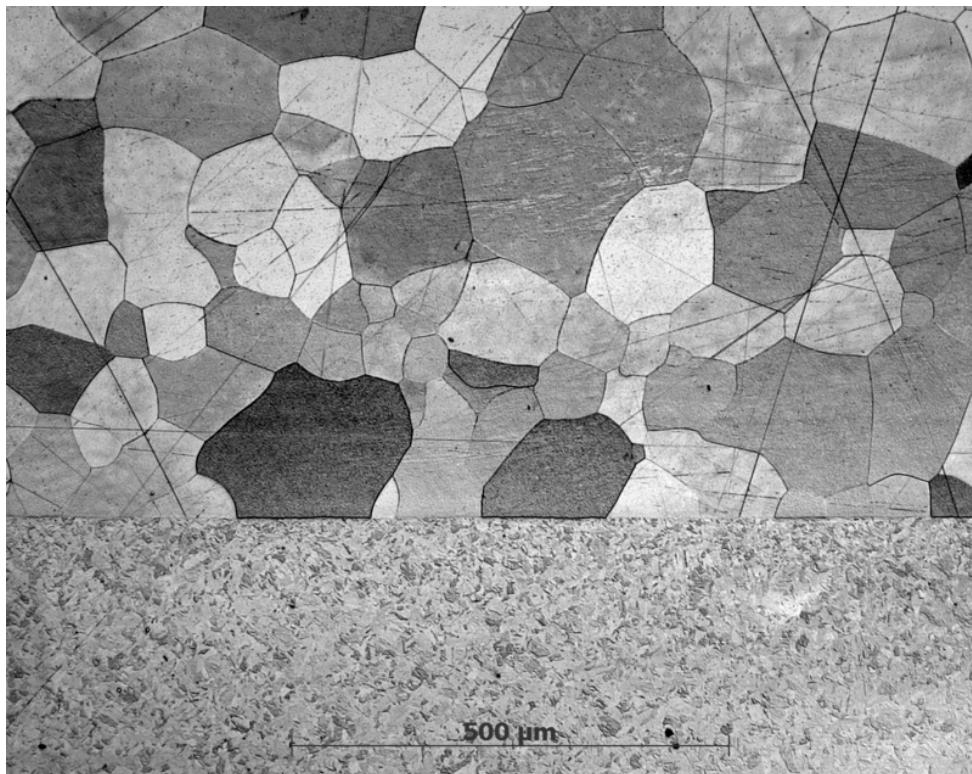


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<http://www.ctcms.nist.gov/wulffman/examples.html>

Grain vs. Crystal Structure

- We see 2D slices of Wulff crystals as grains!



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<http://www.ctcms.nist.gov/wulffman/examples.html>

Point Defects (0D) – Vacancies

Was, p. 163

[Was, Gary S. *Fundamentals of Radiation Materials Science*, p. 163.
ISBN: 9783540494713.] removed due to copyright restrictions.

Point Defects (0D) – Multiple Vacancies

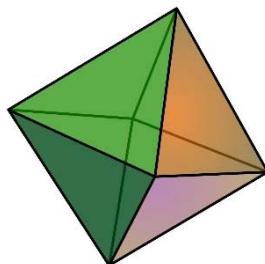
Was, p. 163

[Was, Gary S. *Fundamentals of Radiation Materials Science*, p. 163.
ISBN: 9783540494713.] removed due to copyright restrictions.

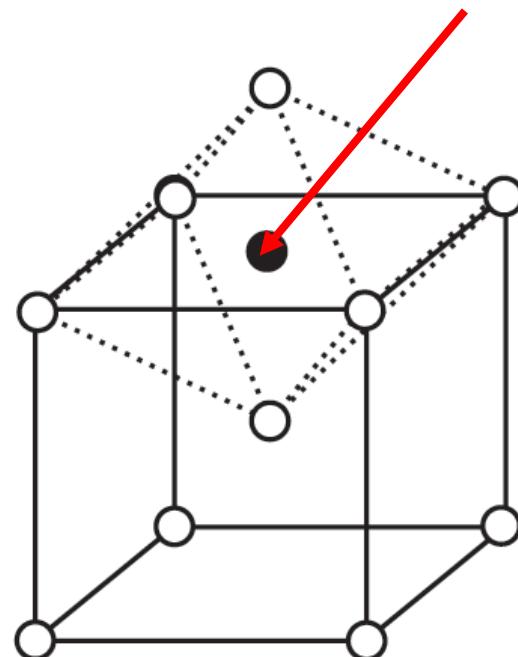
Point Defects (0D) – Interstitials

Was, p. 157

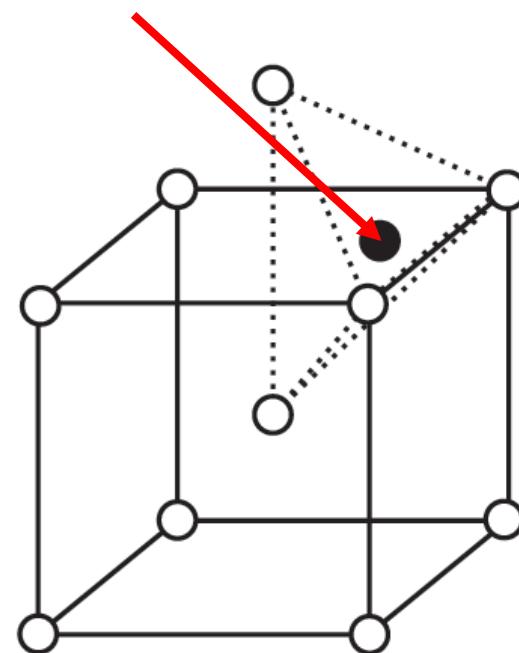
- Extra atoms shoved into the crystal lattice



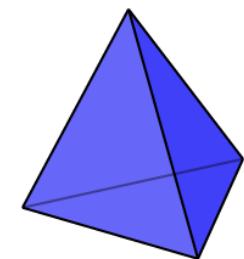
Octahedron



Octahedral interstitial in BCC
lattice



Tetrahedral interstitial in BCC
lattice



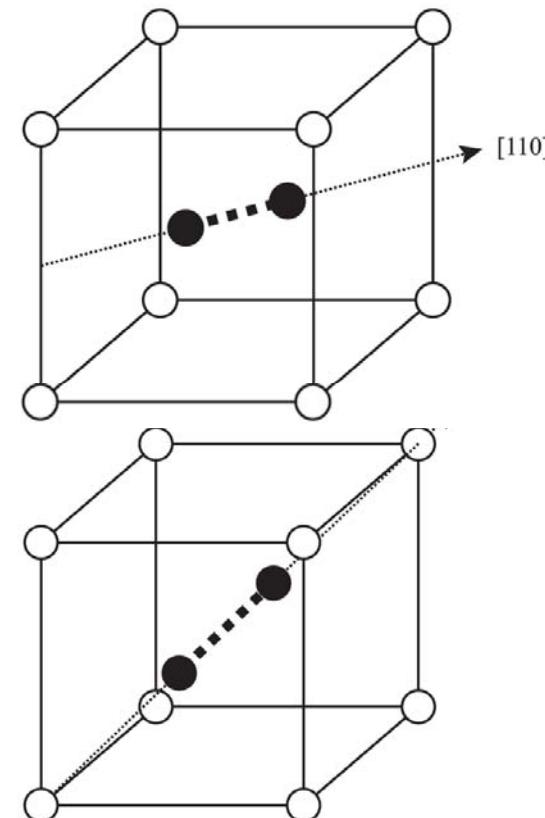
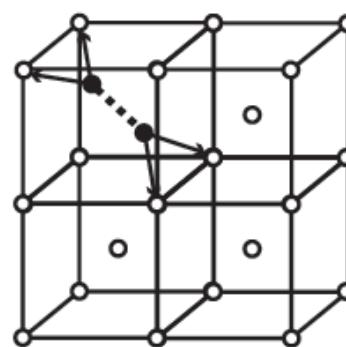
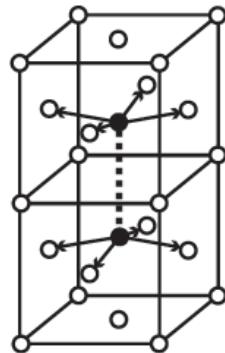
Tetrahedron

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Point Defects (0D) – Split Interstitials

Was, p. 159

- Dumbbells are often lower energy configurations
- Also much easier to diffuse
 - One interstitial can “knock” the other in their common direction
 - Lower distance to movement



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Point Defect Energies

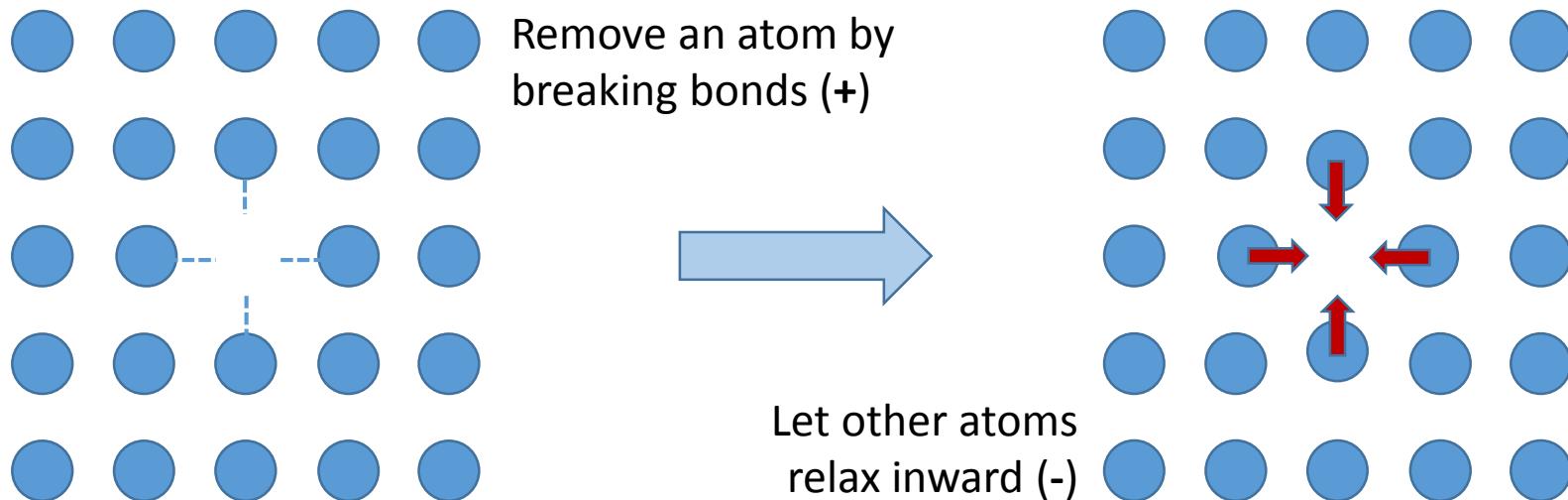
Was, p. 160

	Symbol	Unit	Al	Cu	Pt	Mo	W
Interstitials	Harder to make, easier to move						
Relaxation volume	V_{relax}^i	Atomic vol.	1.9	1.4	2.0	1.1	
Formation energy	E_f^i	eV	3.2	2.2	3.5		
Equilibrium concentration at T_m^*	$C_i(T_m)$	–	10^{-18}	10^{-7}	10^{-6}		
Migration energy	E_m^i	eV	0.12	0.12	0.06	0.054	
Vacancies	Easier to make, harder to move						
Relaxation volume	V_{relax}^v	Atomic vol.	0.05	-0.2	-0.4		
Formation energy	E_f^v	eV	0.66	1.27	1.51	3.2	3.8
Formation entropy	S_f^v	k	0.7	2.4		2	
Equilibrium concentration at T_m^*	$C_v(T_m)$	–	9×10^{-6}	2×10^{-6}		4×10^{-5}	
Migration energy	E_m^v	eV	0.62	0.8	1.43	1.3	1.8
Activation energy for self-diffusion	Q_{vSD}	eV	1.28	2.07	2.9	4.5	5.7
		Q_a					

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Point Defect Energetics

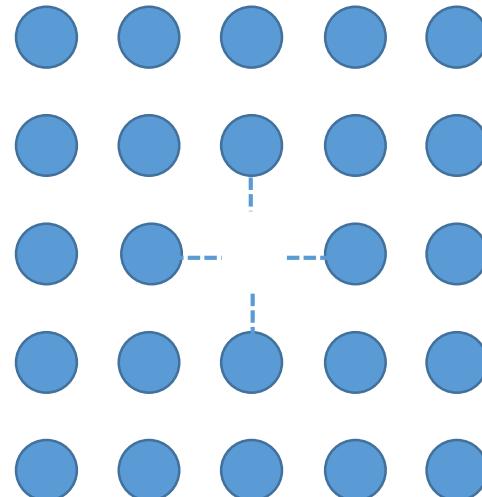
- How much energy to make a vacancy?



Point Defect Energetics

- How much energy to make a vacancy?
- Fe-Fe bond dissociation energy:
 $118 \frac{kJ}{mol} = 1.22eV$ [1]
 - Fe-Fe cluster calculations give 0.64eV [2]
- Z=8 in BCC Fe: 5.12 – 9.76eV

Remove an atom by breaking bonds (+)

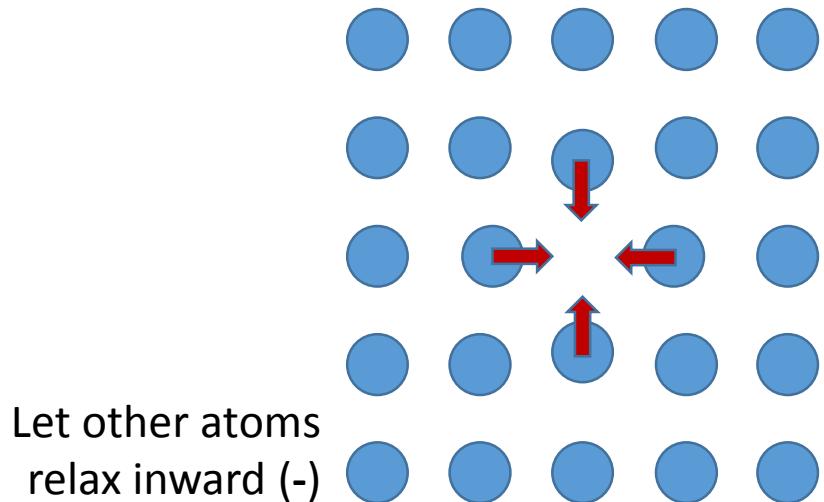


[1] Y-R Luo. "Bond Dissociation Energies." CRC Handbook (2009)

[2] T. Nakazawa, T. Igarashi, T. Tsuru, Y. Kaji, *Comp. Mater. Sci.*, 46(2):367-375 (2009)

Point Defect Energetics

- Z=8 in BCC Fe:
 5.12 [2] – 9.76 [1] eV
- Molecular dynamics (MD) calculations [3] show:
 $E_{Vacancy} = 1.83\text{eV}$
- Difference due to crystal relaxation



[1] Y-R Luo. "Bond Dissociation Energies." CRC Handbook (2009)

[2] T. Nakazawa, T. Igarashi, T. Tsuru, Y. Kaji, *Comp. Mater. Sci.*, 46(2):367-375 (2009)

[3] B. D. Wirth et al. *J. Nucl. Mater.*, 244:185:194 (1997)

Point Defect Energetics

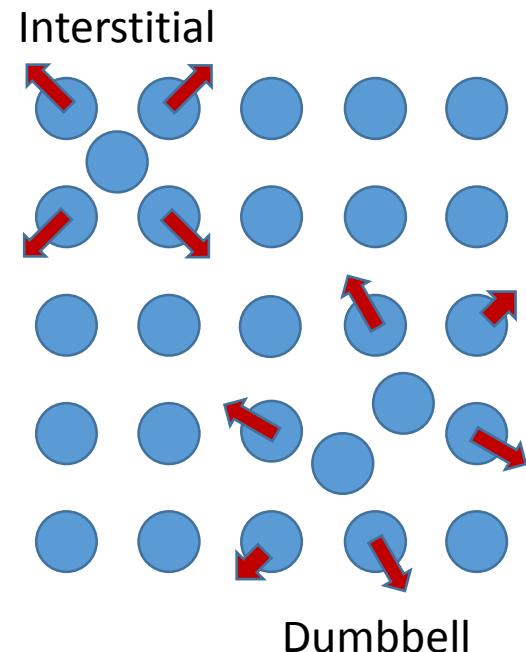
- Which interstitial is most stable?

Relaxed structure and formation properties of point-defects in α -iron ^a

Defect	Atomic positions (a)	Formation energy (eV)	Formation volume (Ω)
<110> dumbbell	(0.245, 0.245, 0.5) (0.755, 0.755, 0.5)	4.76	1.43
<111> dumbbell	(0.291, 0.291, 0.291) (0.709, 0.709, 0.709)	4.87	1.74
<111> crowdion	(0.331, 0.331, 0.331) (0.749, 0.749, 0.749) (1.167, 1.167, 1.167)	4.91	1.77
vacancy		1.83	0.93

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Source: Wirth, B. D., et al. "Energetics of Formation and Migration of Self-interstitials and Self-interstitial Clusters in α -iron." *Journal of Nuclear Materials* 244, no. 3 (1997): 185-94.



B. D. Wirth et al. *J. Nucl. Mater.*, 244:185:194 (1997)

Point Defect Energetics

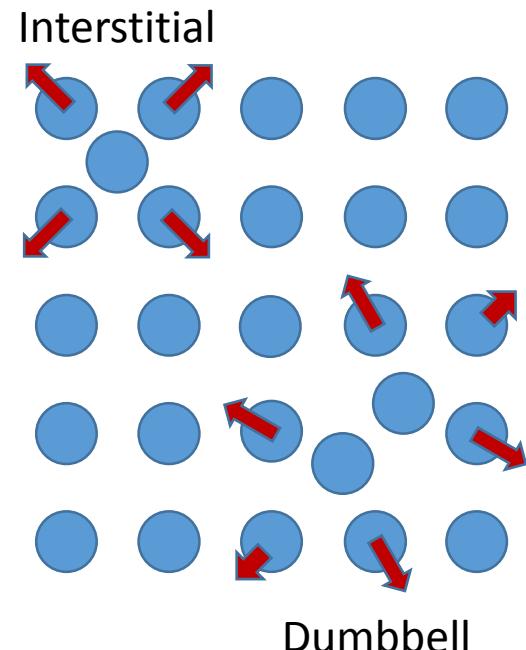
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Source: Wirth, B. D., et al. "Energetics of Formation and Migration of Self-interstitials and Self-interstitial Clusters in α -iron." *Journal of Nuclear Materials* 244, no. 3 (1997): 185-94.



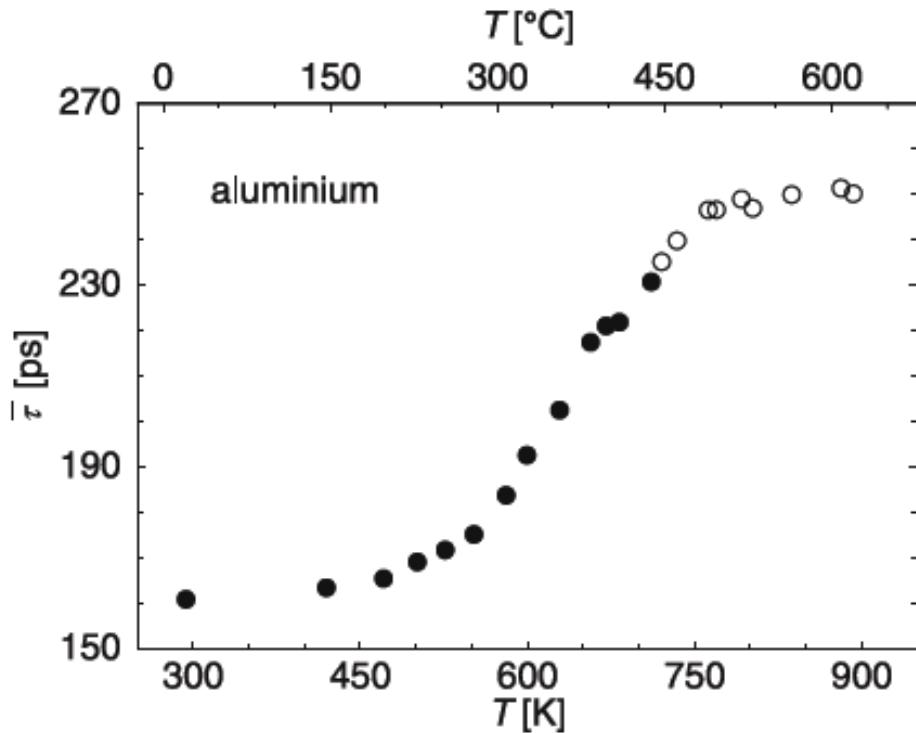
B. D. Wirth et al. *J. Nucl. Mater.*, 244:185:194 (1997)

- Does it matter?

Direct Measurement of C_{1V}^{eq}

Mehrer, p. 78

- Positron annihilation spectroscopy (PAS)
 - Shoot positrons into material, they annihilate very quickly with local electrons
 - Positrons can bind to vacancy, which has a reduced electron cloud
 - Lasts longer!



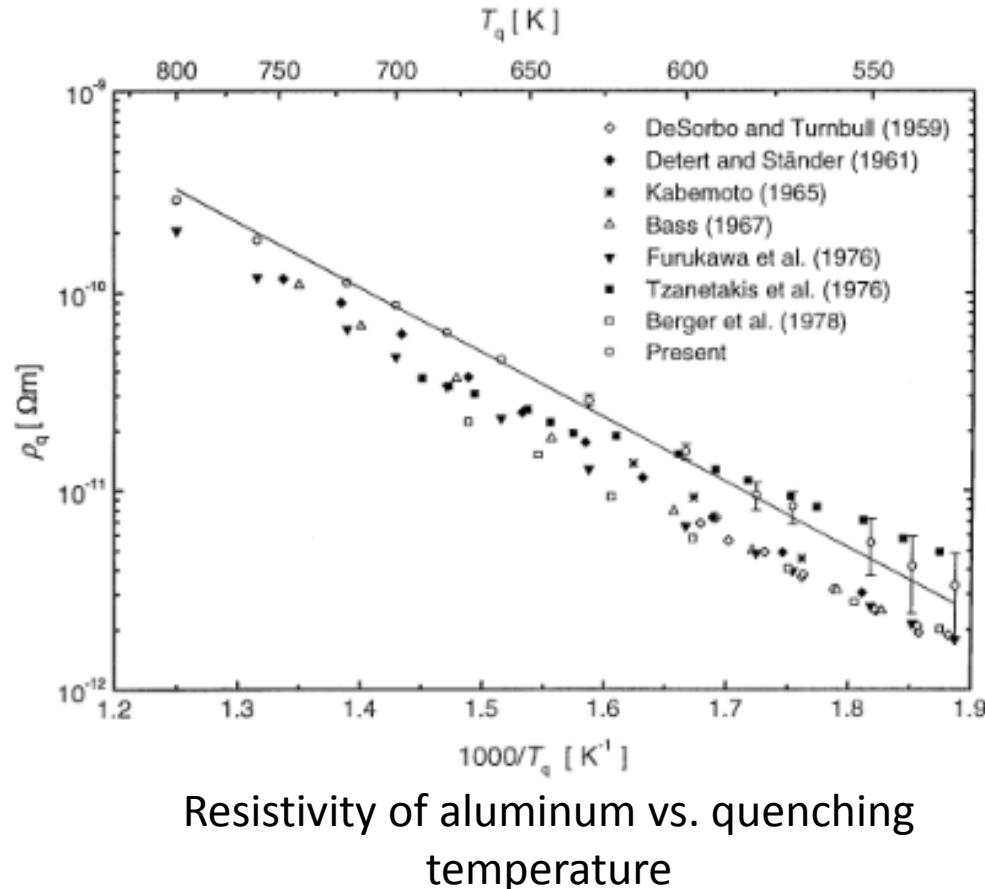
Mean positron lifetime in aluminum

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Direct Measurement of C_{1V}^{eq}

A. Khellaf et al., Mater. Trans. 43(2):186 (2002)

- Quenching resistance measurements
 - Heat material to high temperature, quench, measure resistivity
 - Resistivity directly proportional to vacancy concentration
 - Measured at liquid-He temperature



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Dislocations (1D)

Was, p. 268

- Extra half-plane of atoms shoved into the lattice
- Two types: **Edge & Screw**

[Fig. 7.2 in p. 268 from Was, Gary S. *Fundamentals of Radiation Materials Science*, ISBN: 9783540494713] removed due to copyright restrictions.

Dislocations (1D)

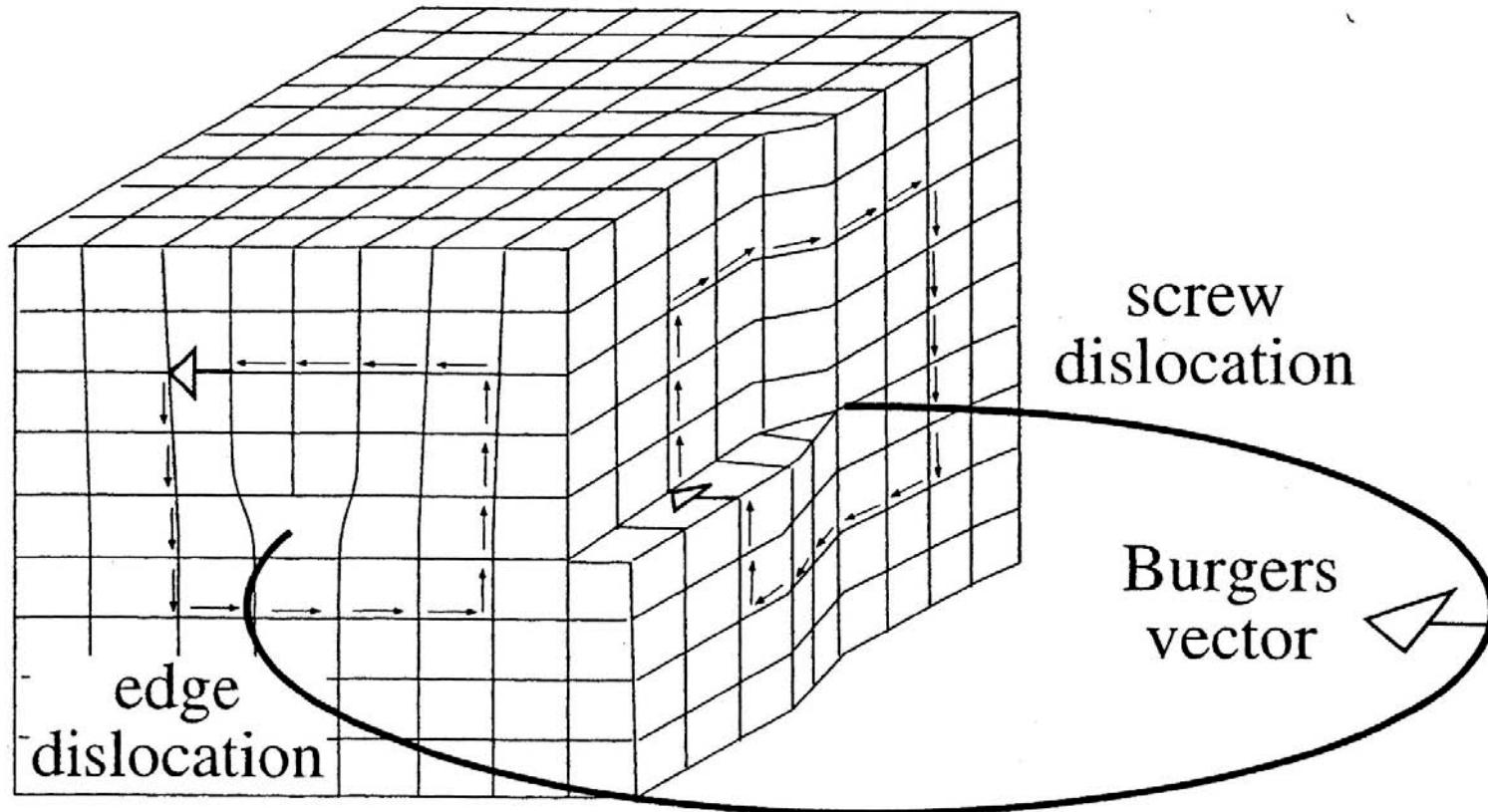
Was, p. 268

- Extra half-plane of atoms shoved into the lattice
- Two types: Edge & Screw

[Fig. 7.3 in p. 268 from Was, Gary S. *Fundamentals of Radiation Materials Science*, ISBN: 9783540494713] removed due to copyright restrictions.

Edge vs. Screw Dislocations

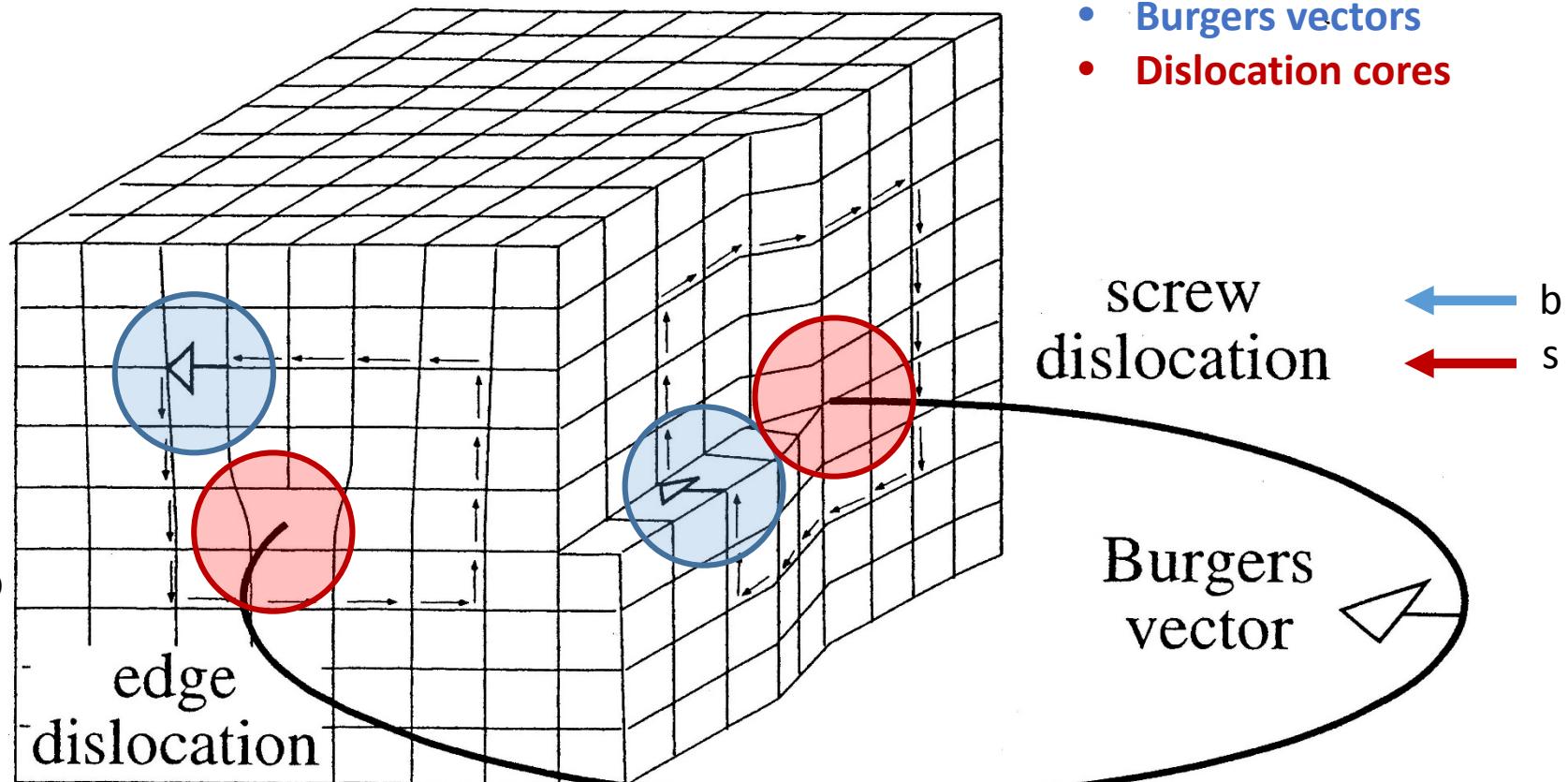
Passchier and Trouw, "Microtectonics," p. 33 (2005)



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Edge vs. Screw Dislocations

Passchier and Trouw, "Microtectonics," p. 33 (2005)

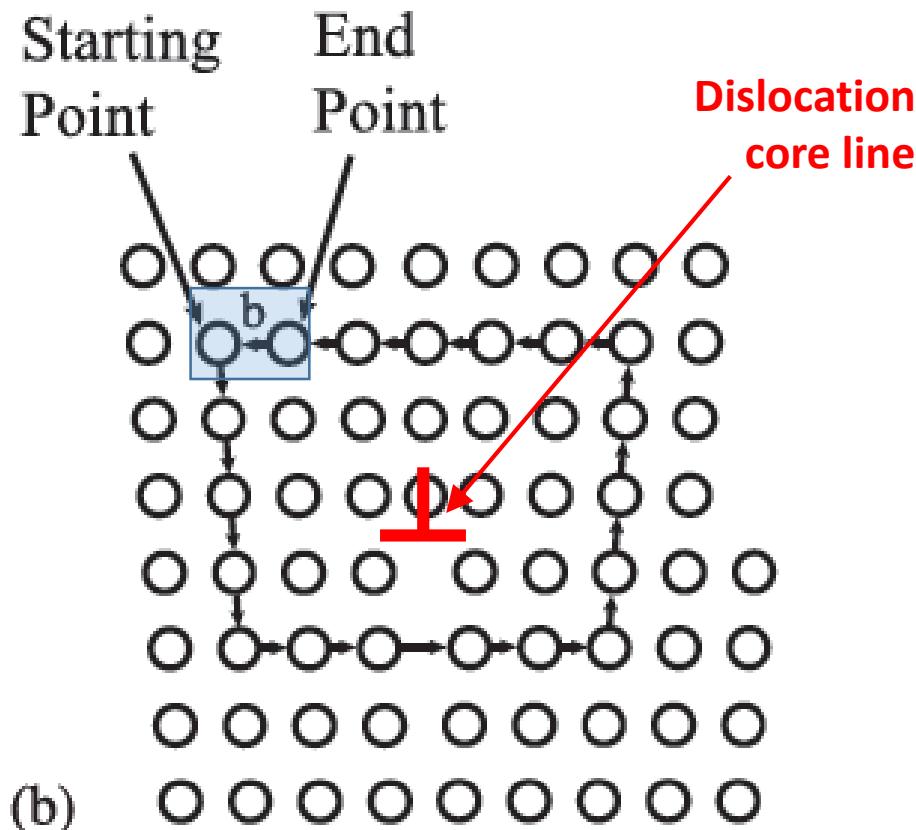


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The Burgers Vector

Was, p. 275

- Start at one atom, make a circle around the dislocation core
- The *Burgers Vector* is the direction you move to reach your starting point
- Example: Edge disloc.



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Dislocation Glide

Was, p. 272

- Movement one plane at a time along the slip direction

[Fig. 7.8 in p. 272 from Was, Gary S. *Fundamentals of Radiation Materials Science*, ISBN: 9783540494713] removed due to copyright restrictions.

Edge Dislocation Glide



A video is played in class to demonstrate the concept.

<http://youtu.be/kk2oOxSDQ7U>

Dislocation Glide

- Movement one plane at a time along the slip direction

[Fig. 7.9 from Was, Gary S. *Fundamentals of Radiation Materials Science*. ISBN: 9783540494713] removed due to copyright restrictions.

Dislocation Climb

Was, p. 273

- Vacancy diffusion to dislocation core
 - Vacancies are attracted to the compressive stress at core

[Fig. 7.12 in p. 273 from Was, Gary S. *Fundamentals of Radiation Materials Science*, ISBN: 9783540494713] removed due to copyright restrictions.

Dislocation Kinks, Joggs

Allen, "Kinetics of Materials," p. 116

- Dislocations preferentially move on slip systems
 - Certain directions of easier movement
 - Close packed planes slip in close packed directions

Crystal structure	Slip plane	Slip direction	Number of nonparallel planes	Slip directions per plane	Number of slip systems
Face-centered cubic	{111}	<1̄10>	4	3	12 = (4 × 3)
Body-centered cubic*	{110}	<1̄11>	6	2	12 = (6 × 2)
	{112}	<11̄1>	12	1	12 = (12 × 1)
	{123}	<11̄1>	24	1	24 = (24 × 1)
Hexagonal close-packed†	{0001}	<11̄20>	1	3	3 = (1 × 3)
	{10̄10}	<11̄20>	3	1	3 = (3 × 1)
	{10̄11}	<11̄20>	6	1	6 = (6 × 1)

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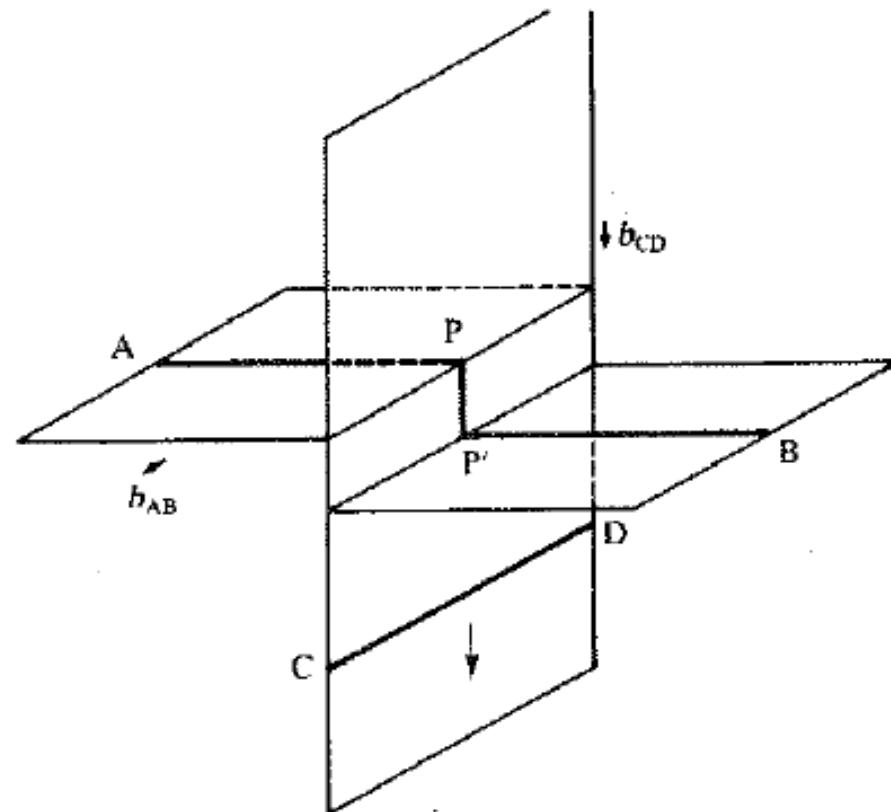
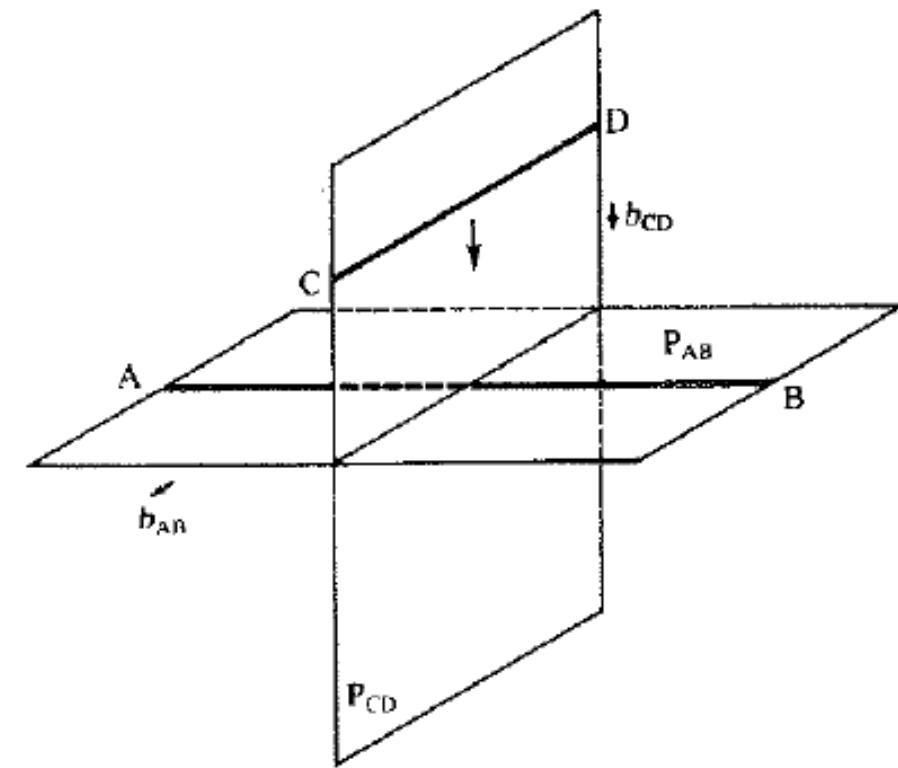
Dislocation Motion

Was, p. 277

[Fig. 7.18 in p. 277 from Was, Gary S. *Fundamentals of Radiation Materials Science*, ISBN: 9783540494713] removed due to copyright restrictions.

Glissile vs. Sessile Sections

Allen, "Kinetics of Materials," p. 124

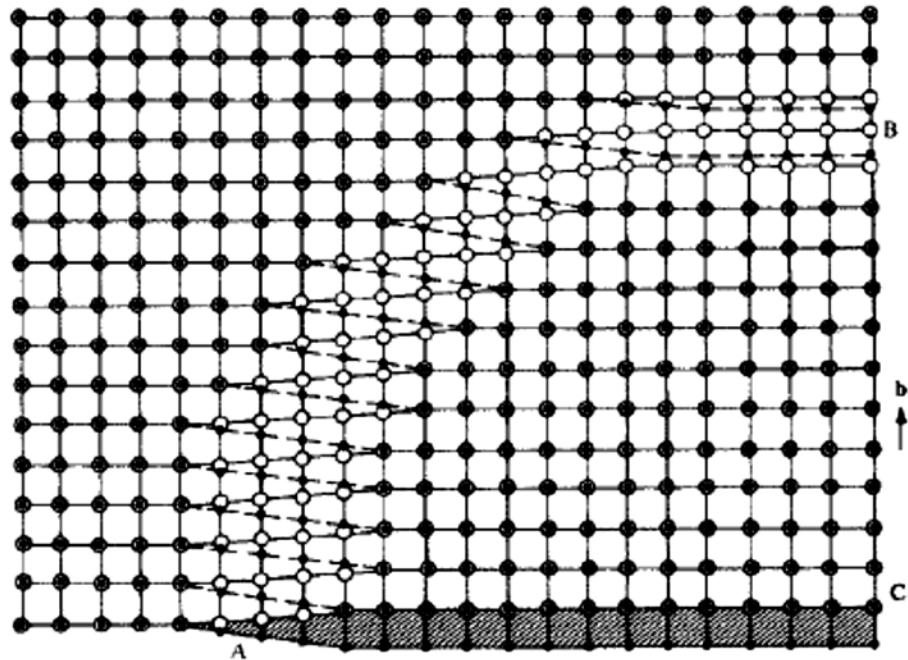
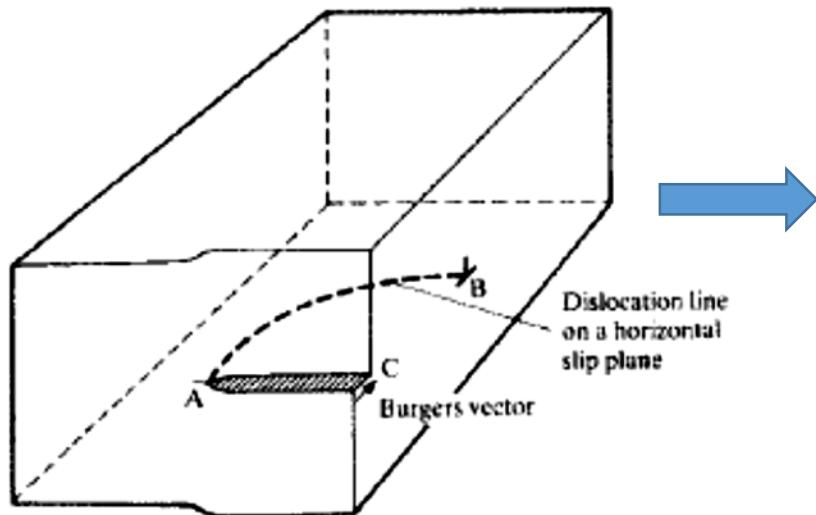


Two edge dislocations moving towards each other form a *sessile jog*

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Dislocation Loops

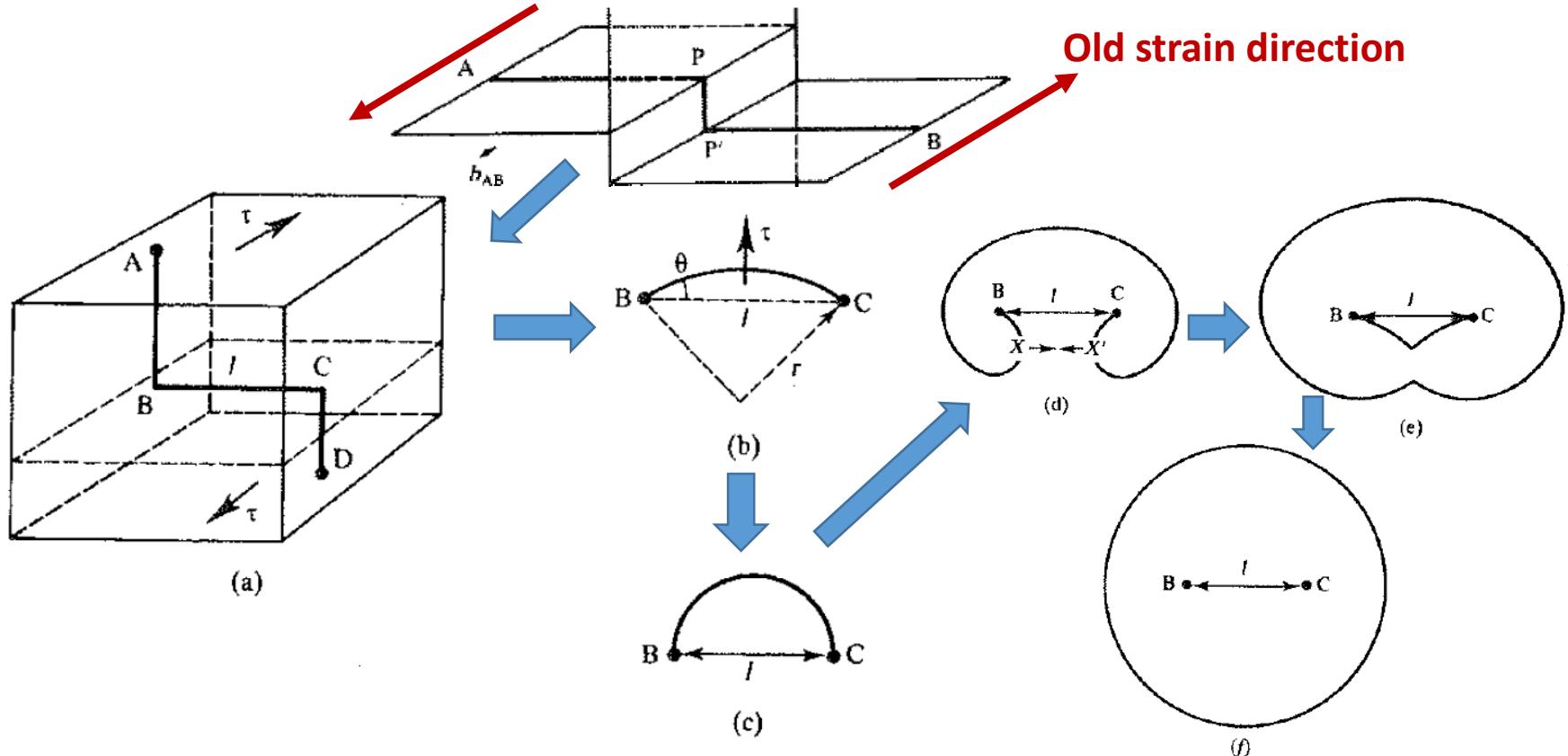
- Loops have mixed edge/screw character
 - May be circular planes of atoms between two planes



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Dislocation Loop Sources

- Come from sessile sections of dislocations



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Dislocation Videos!

<http://www.numodis.fr/tridis/TEM/mechanisms/multiplication.html>



Dislocation sources in Mo-5Nb

A video is played in class to demonstrate the concept.

Dislocation Videos!

<http://www.numodis.fr/tridis/TEM/mechanisms/multiplication.html>



A Frank-Read Source in Silicon

A video is played in class to demonstrate the concept.

Dislocation Videos!

<http://www.numodis.fr/tridis/TEM/mechanisms/multiplication.html>



Dislocation source in Ge at high temperature

A video is played in class to demonstrate the concept.

Dislocation Videos!

<http://www.numodis.fr/tridis/TEM/mechanisms/multiplication.html>

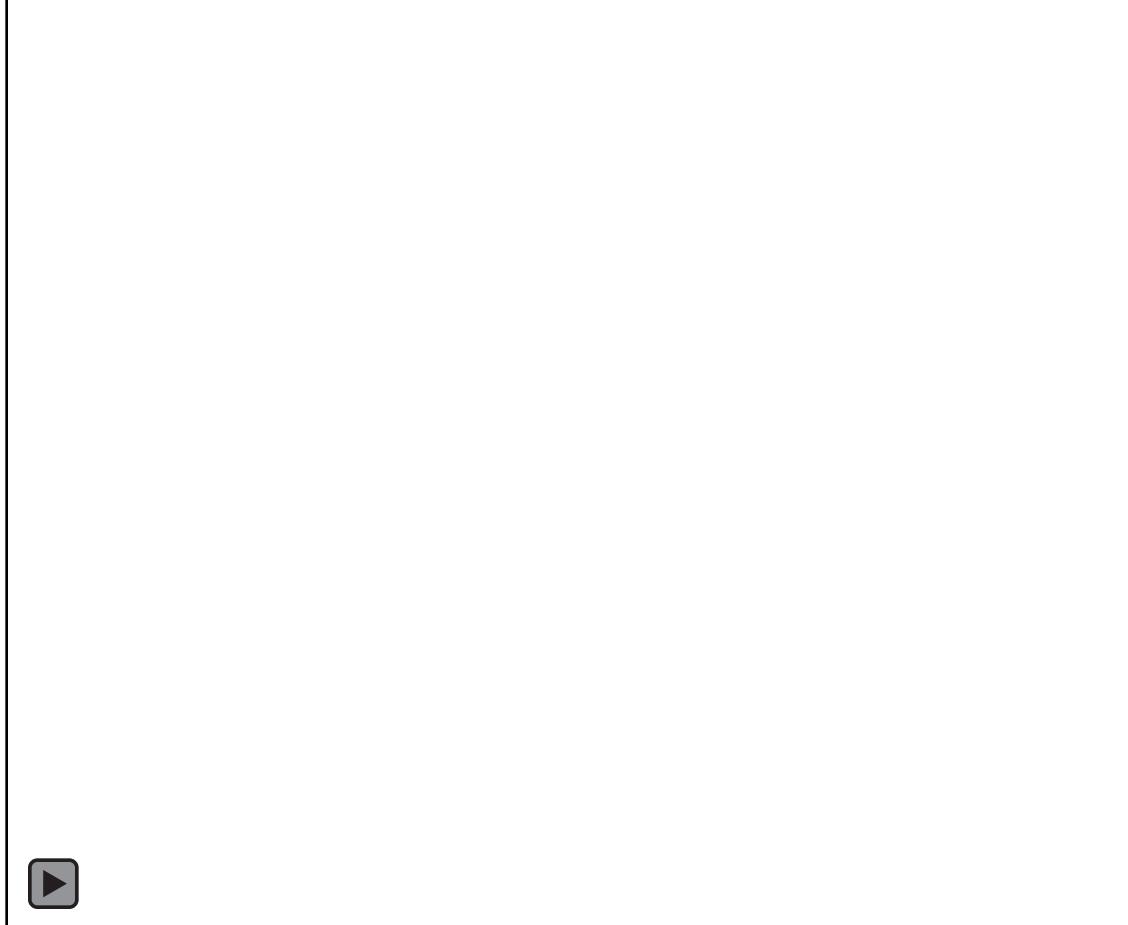


Dislocation sources and pileup in Ge

A video is played in class to demonstrate the concept.

Dislocation Videos!

<http://www.numodis.fr/tridis/TEM/mechanisms/multiplication.html>



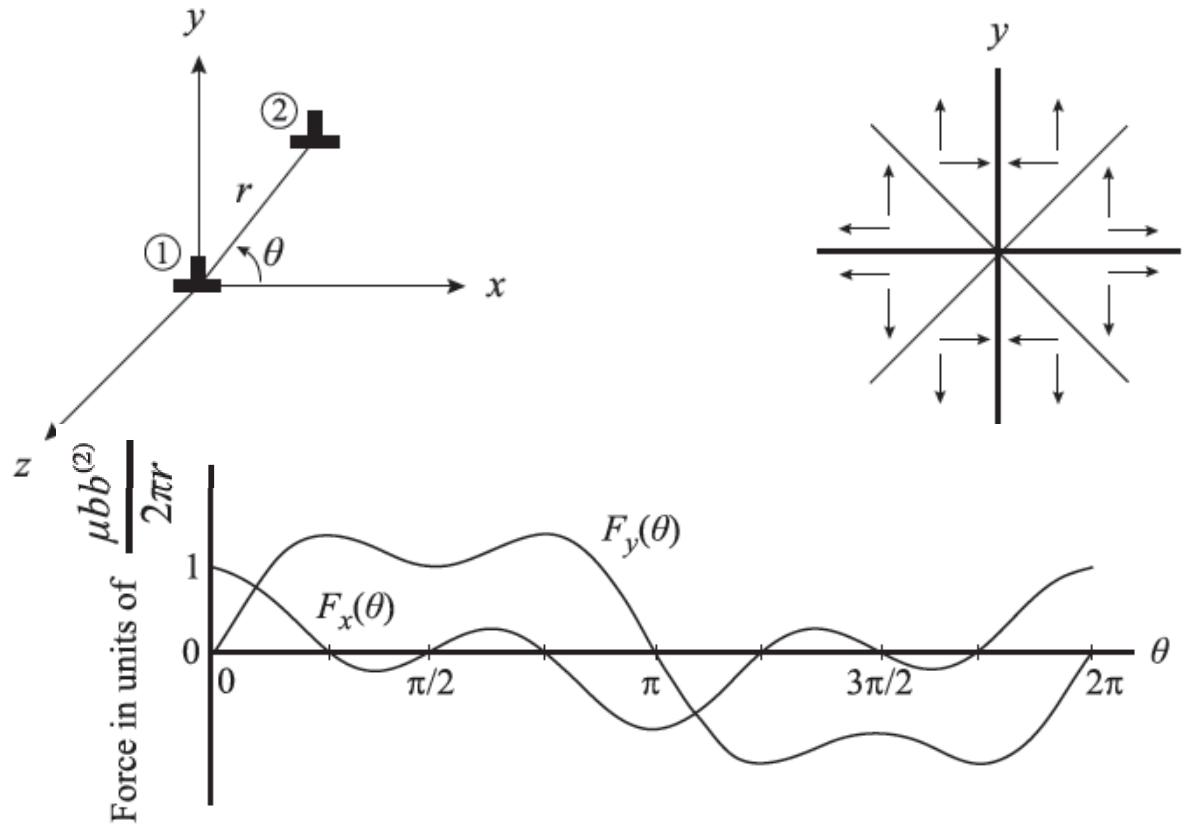
Dislocation sources in Si

A video is played in class to demonstrate the concept.

Forces Between Edge Dislocations

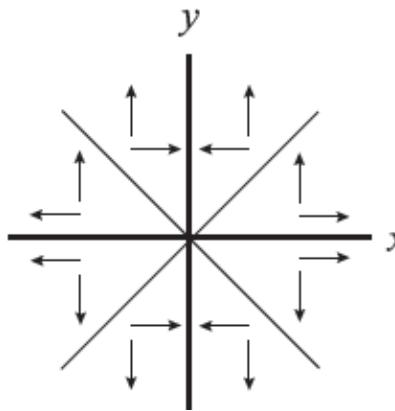
Was, p. 289-290

- X & Y forces, no Z-force



Peach-Kohler Equation

Burgers vector of
dislocation (2)
transposed



Line vector of
dislocation (2)
transposed

$$\mathbf{f} = \mathbf{b}_{(2)}^T \underline{\underline{\sigma}}_{(1)} \times \mathbf{s}_{(2)}$$

Force vector on
dislocation (2)

Stress tensor
induced by
dislocation (1)

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All Together: Loops, Movement, Pileup

Dislocations moving & piling up in Inconel 617 (Ni-based alloy) under *in-situ* straining in the TEM



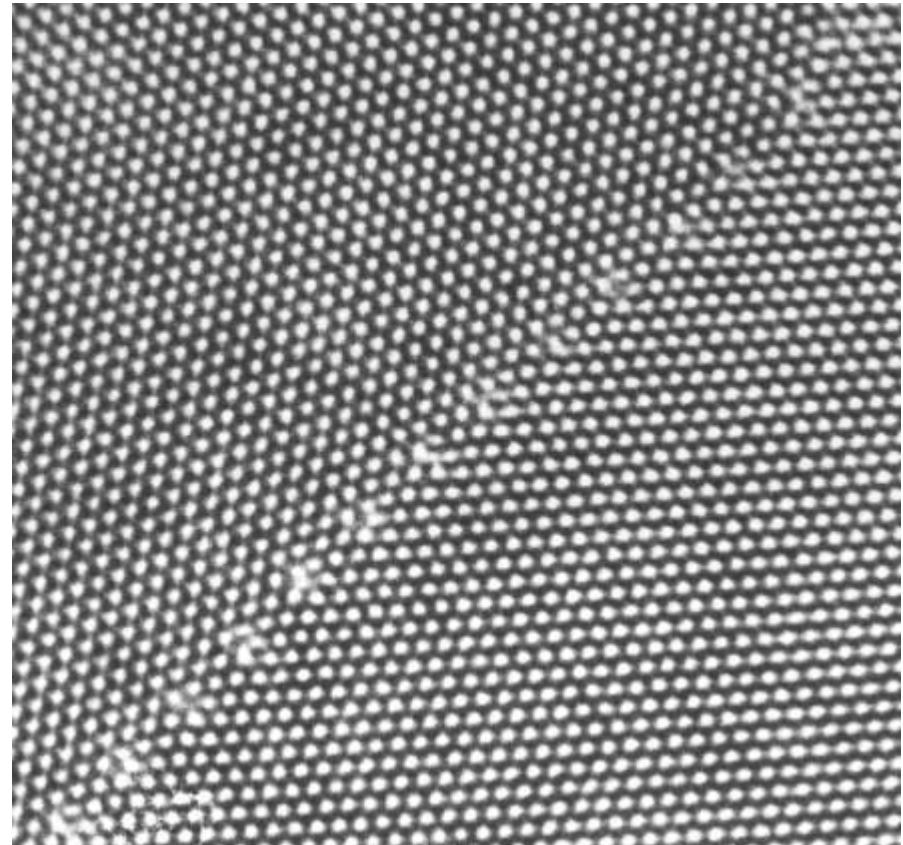
<http://youtu.be/r-geDwE8Z5Y>

A video is played in class to demonstrate the concept.

Grain Boundaries (2D)

<http://www-hrem.msm.cam.ac.uk/gallery/>

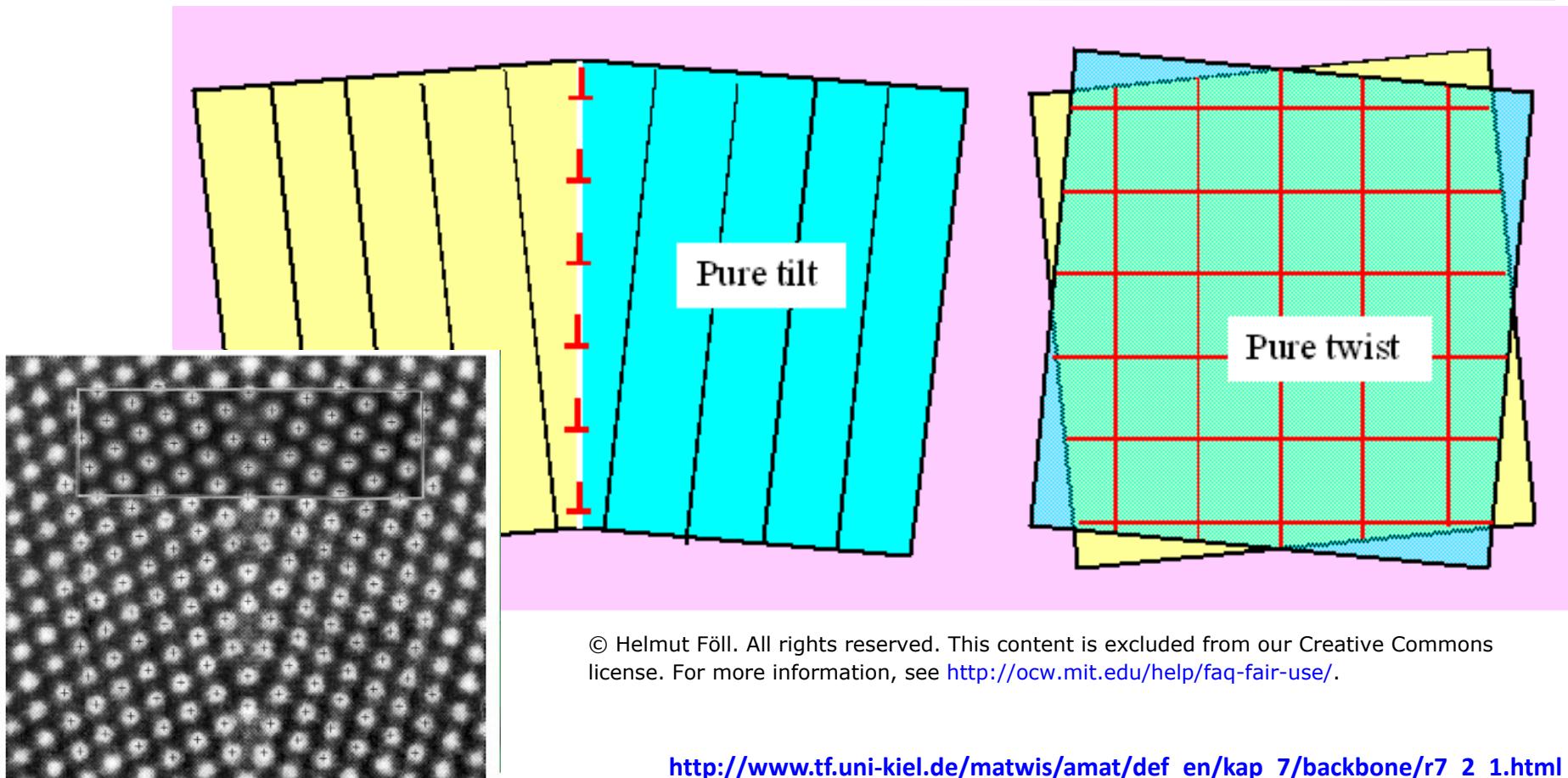
- Regions of different orientation
 - May also be different crystal structure



TEM image of a grain boundary in pure Al

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GBs can be Lines of Dislocations



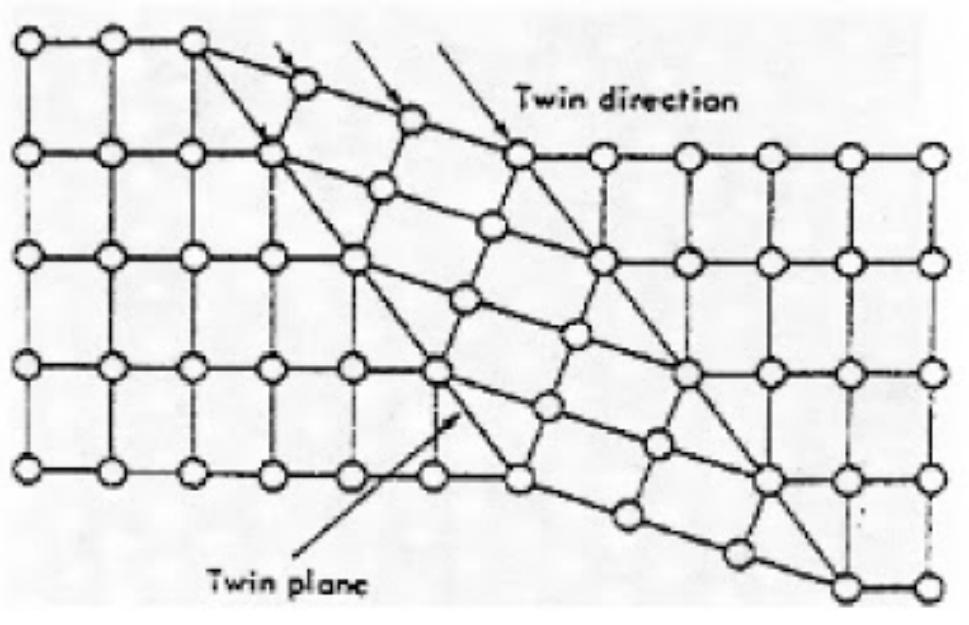
Tilt grain boundary in Al

This image is in the public domain.

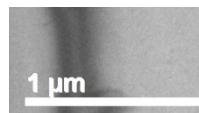
<http://moisespinedacaf.blogspot.com/>

Twinning

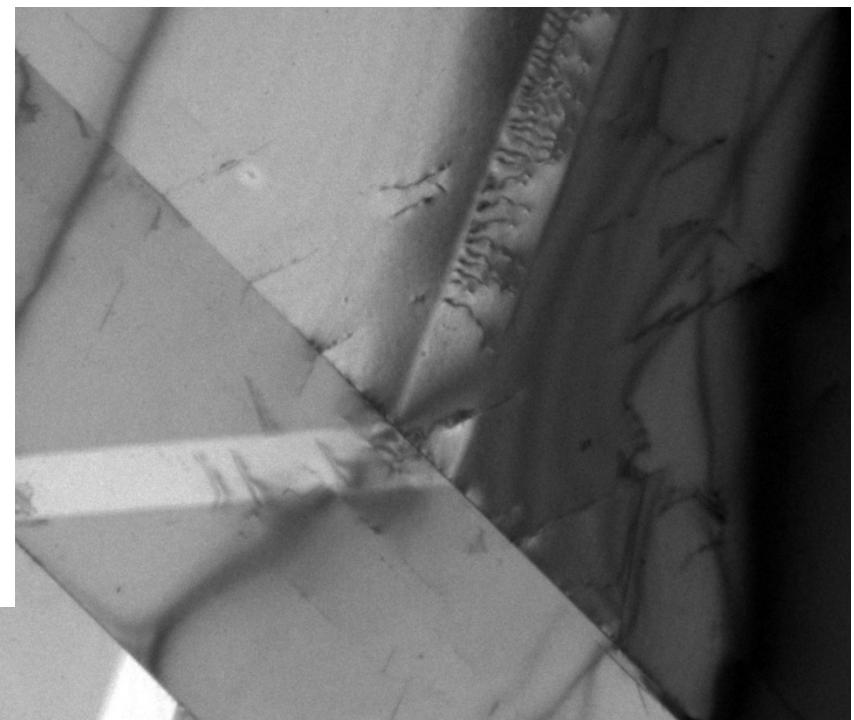
- Alternate plastic deformation mechanism



Twinning observed in irradiated reactor pressure vessel steel



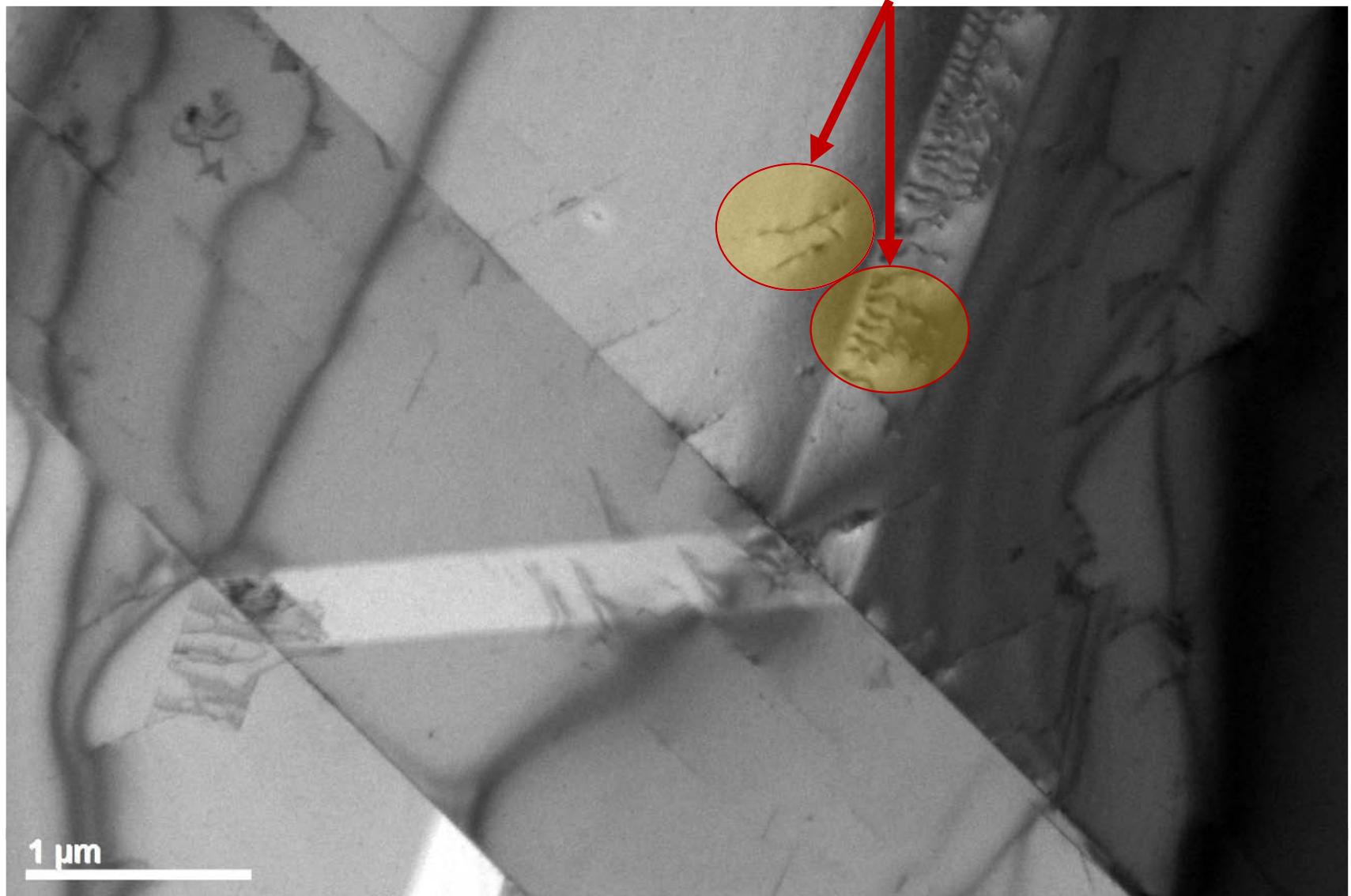
http://dcg.materials.drexel.edu/?page_id=14#nuclear



Courtesy of Dynamic Characterization Group, property of Drexel University. Used with permission.

Twinning

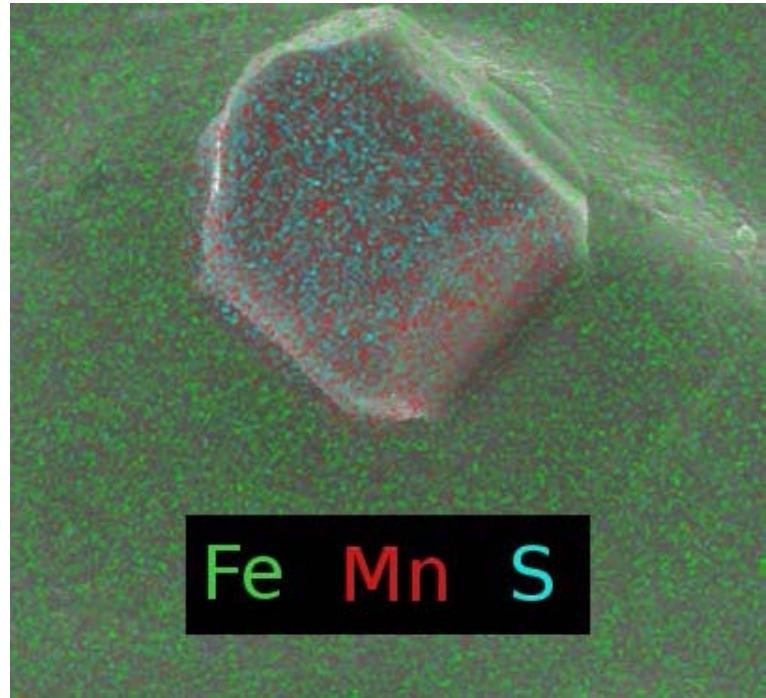
Differently oriented dislocations
inside/outside twin boundary!



Courtesy of Dynamic Characterization Group, property of Drexel University. Used with permission.

Inclusions (3D)

- Other phases trapped within base material
- Examples:
 - Secondary particle precipitates in Zircaloys
 - Carbides in steels
 - Y_2O_3 particles in Oxide Dispersion Strengthened (ODS) steels

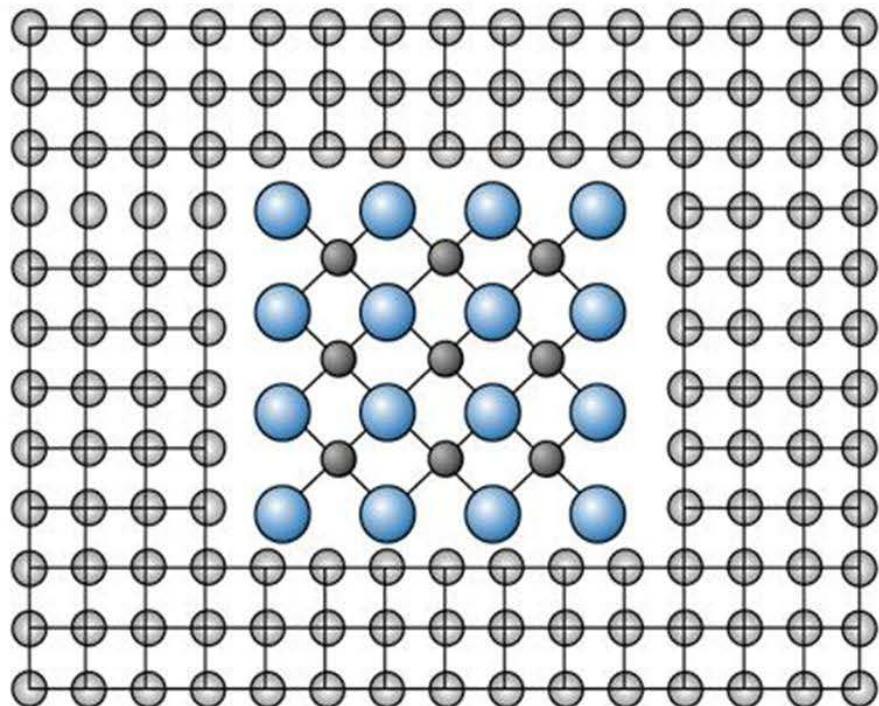


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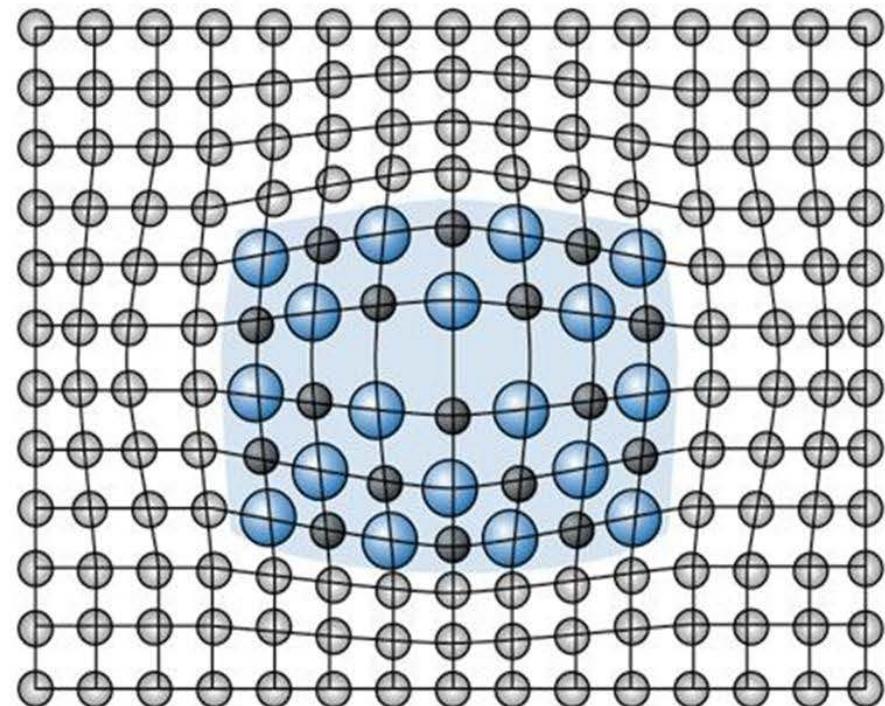
Single crystal of MnS, space group $\text{Fm}\bar{3}\text{m}$, FCC crystal structure embedded in Alcator rotor steel

Coherent vs. Incoherent

- Which do you think would be better at sinking defects? Stopping dislocations?



Incoherent inclusion



Coherent inclusion

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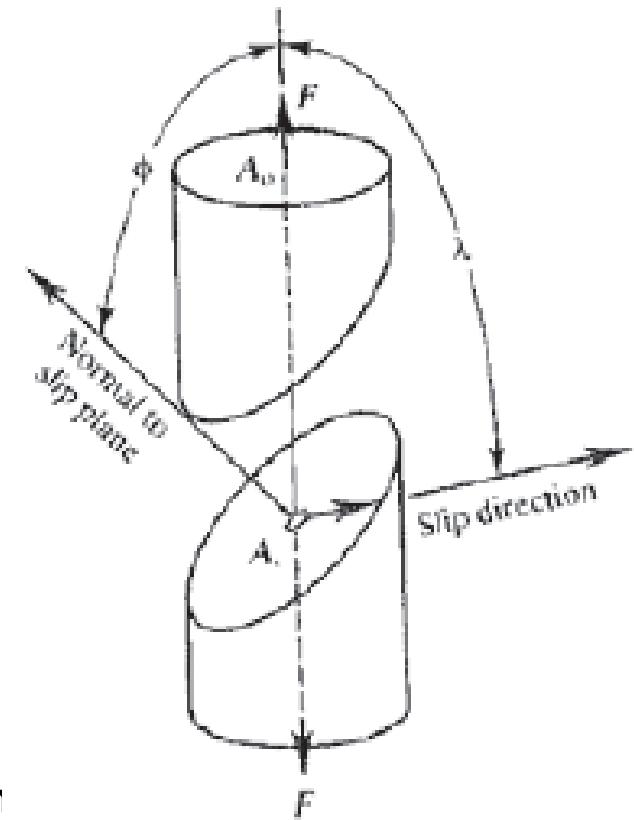
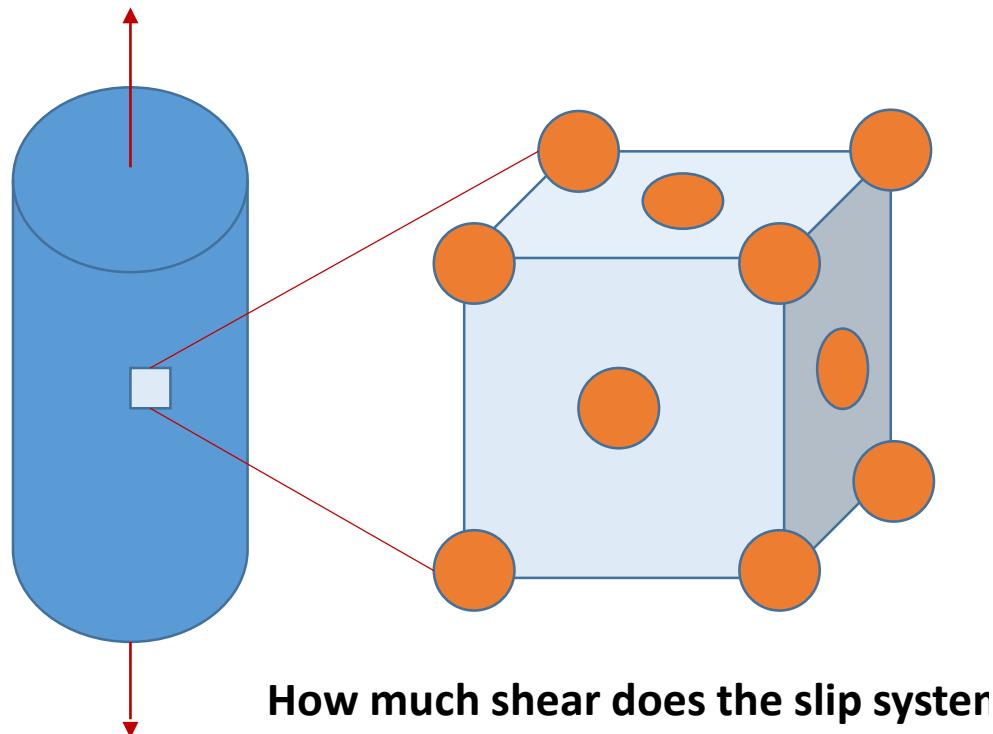
Switching Gears: Structural Material Properties

- Goals:
 - Understand true vs. engineering stress & strain
 - Quantify and differentiate between hardness, toughness, strength, ductility, stiffness
 - Know how to measure these properties
 - Resolve stresses onto slip systems
 - Predict the differences in mechanical response between single, dual, and polycrystalline materials

Images from now on are from T. H. Courtney, *Mechanical Behavior of Materials* unless otherwise noted

Resolved Shear Stress

- Consider a single crystal bar of FCC material, tensioned in the [001] direction:



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Resolved Shear Stress

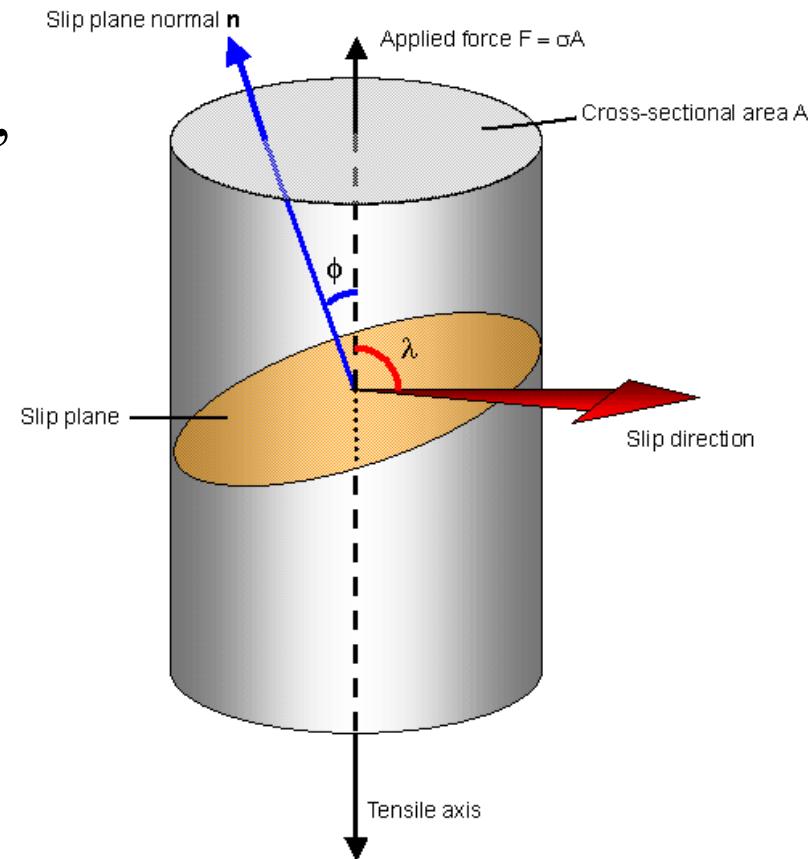
<http://www.doitpoms.ac.uk/tplib/slip/printall.php>

- Project force onto the tilted plane containing the slip system, to get the stress

$$\sigma_{slip} = \frac{F}{A_{slip}} = \frac{F}{\frac{A_0}{\cos \theta}} = \sigma \cos \theta$$

- Also project shear movement in direction of slip

$$\tau = \sigma \cos \lambda$$



Courtesy of University of Cambridge. Used with permission.

Resolved Shear Stress

- The total shear stress becomes:

$$\tau = \sigma \cos \lambda \cos \theta = \frac{\sigma}{m}$$

$$m = \frac{1}{\cos \lambda \cos \theta}$$

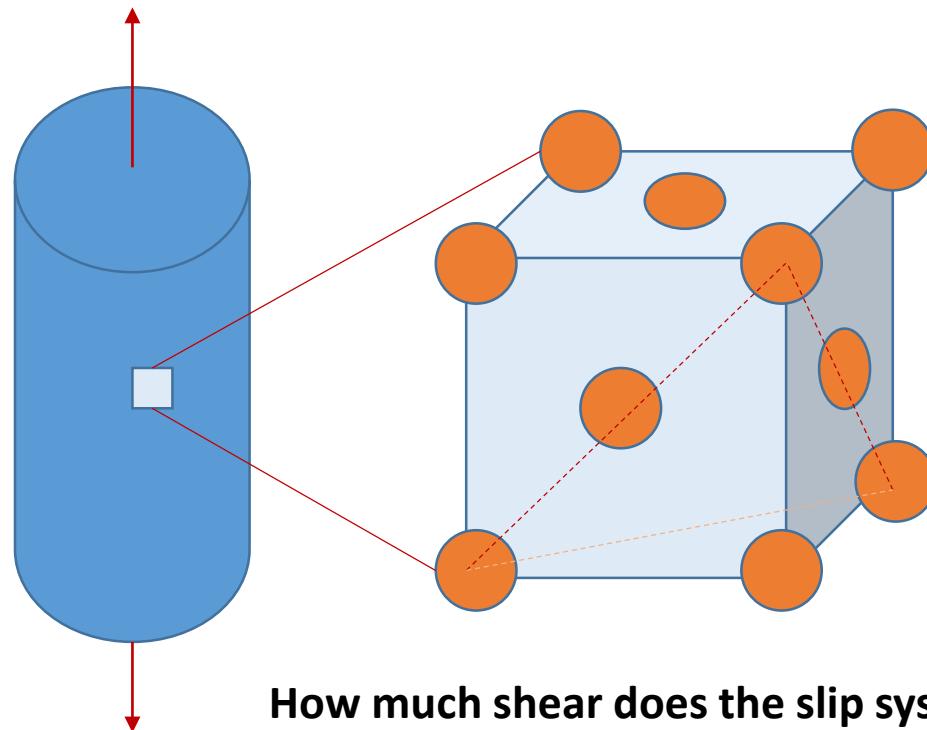


Schmid factor

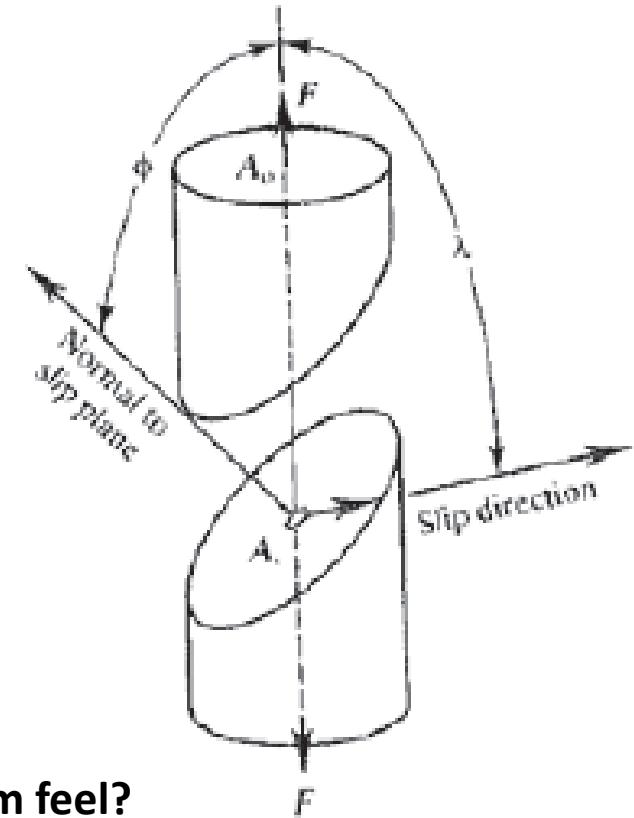
- Effectively reduces applied stress felt on a slip plane

Resolved Shear Stress

- Consider a single crystal bar of FCC material, tensioned in the [001] direction:



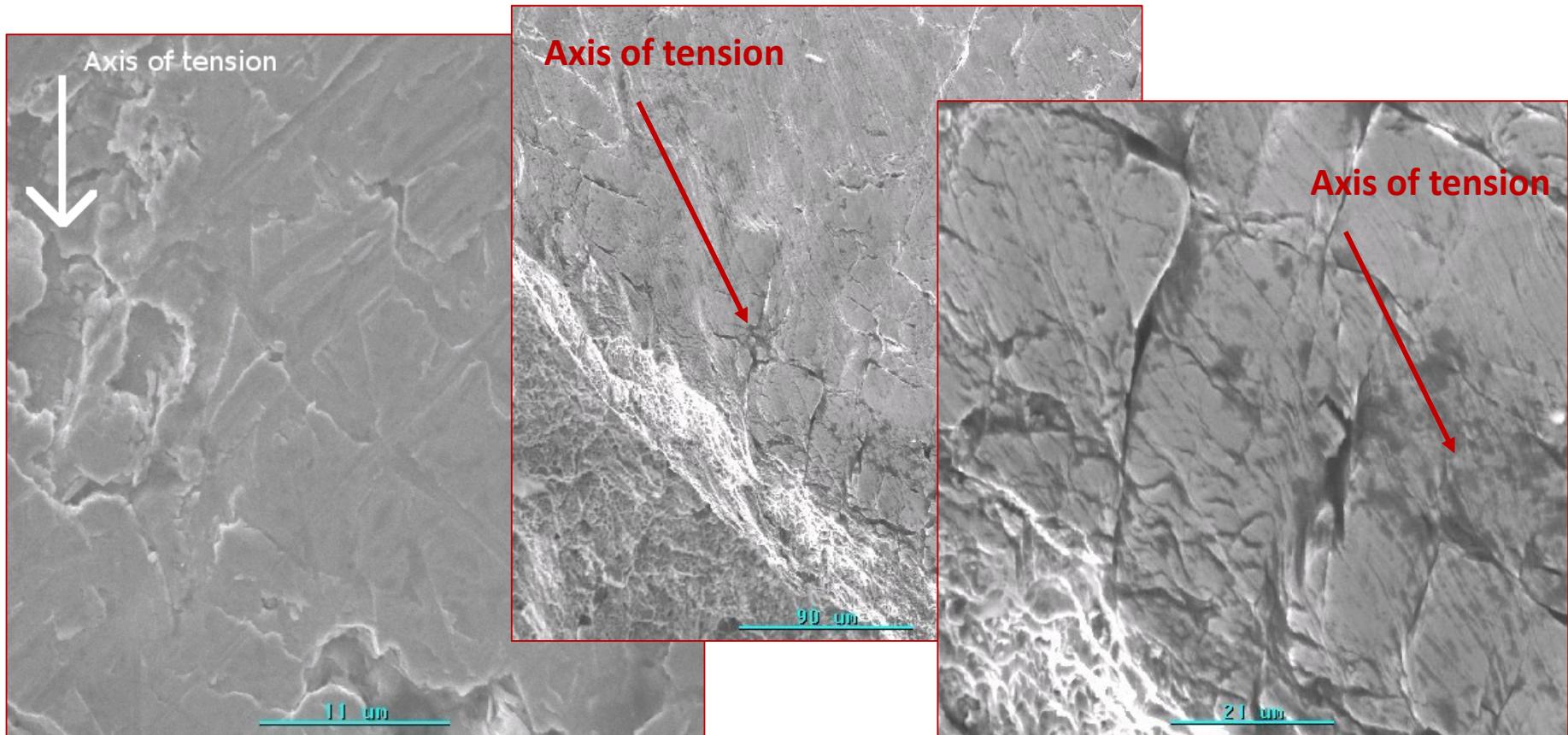
How much shear does the slip system feel?



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Examples of Shear & Slip

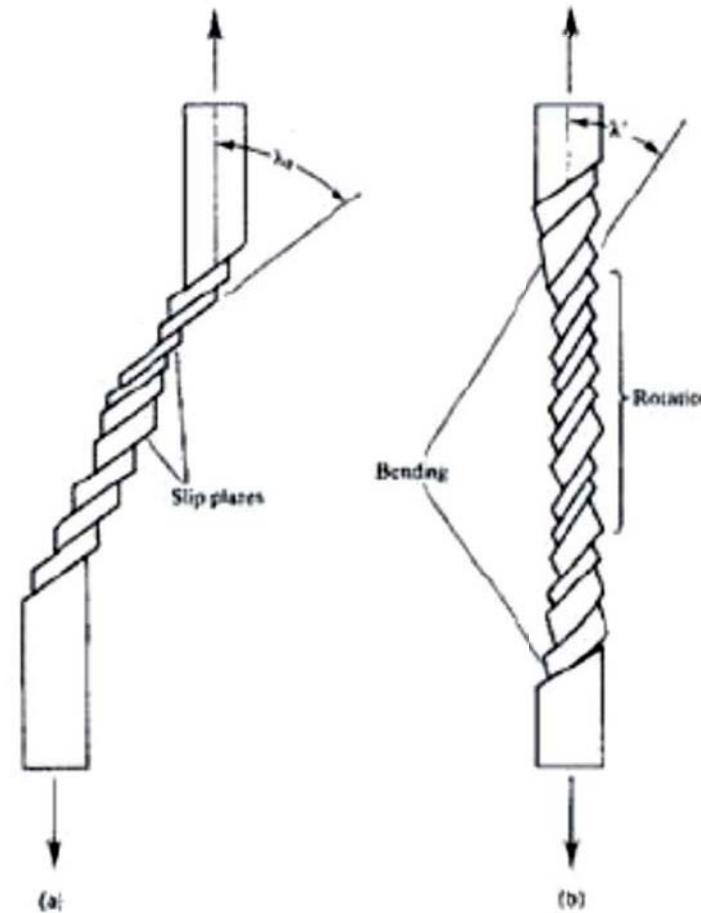
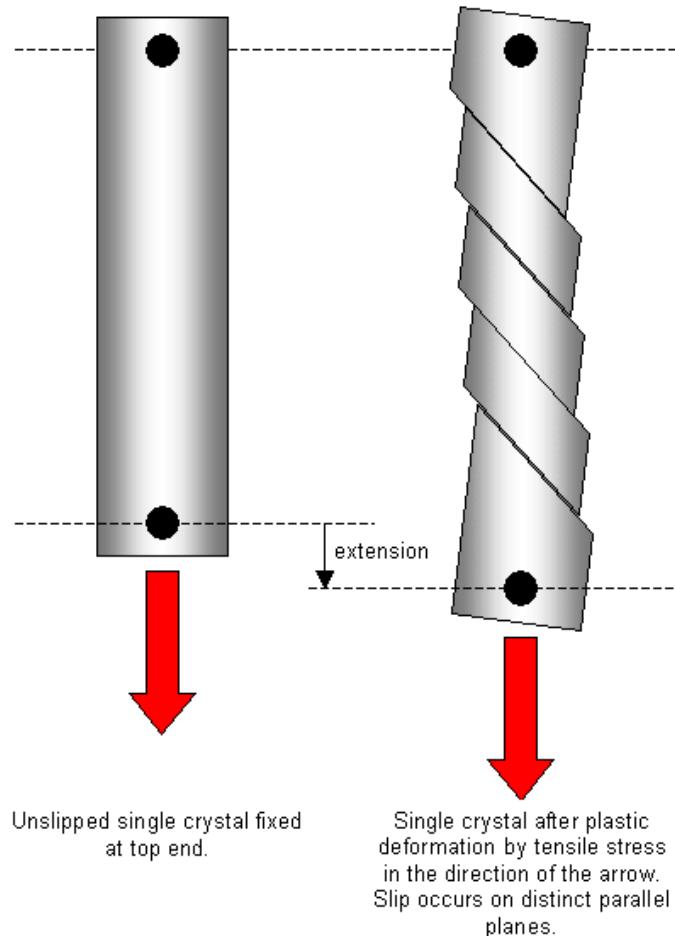
- Alcator C-Mod rotor steel in uniaxial tension:



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Evidence of Slip Systems

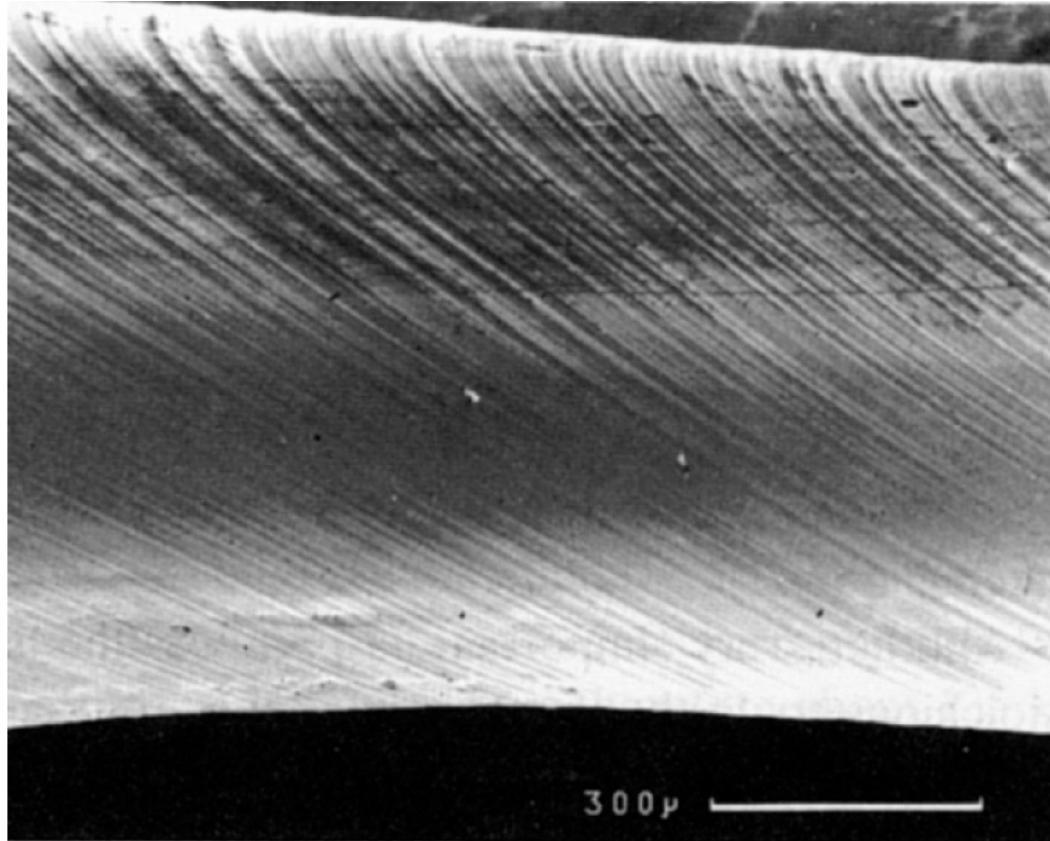
<http://www.doitpoms.ac.uk/tplib/slip/printall.php>



Courtesy of University of Cambridge. Used with permission.

Evidence of Slip Systems

http://www.doitpoms.ac.uk/tplib/miller_indices/printall.php

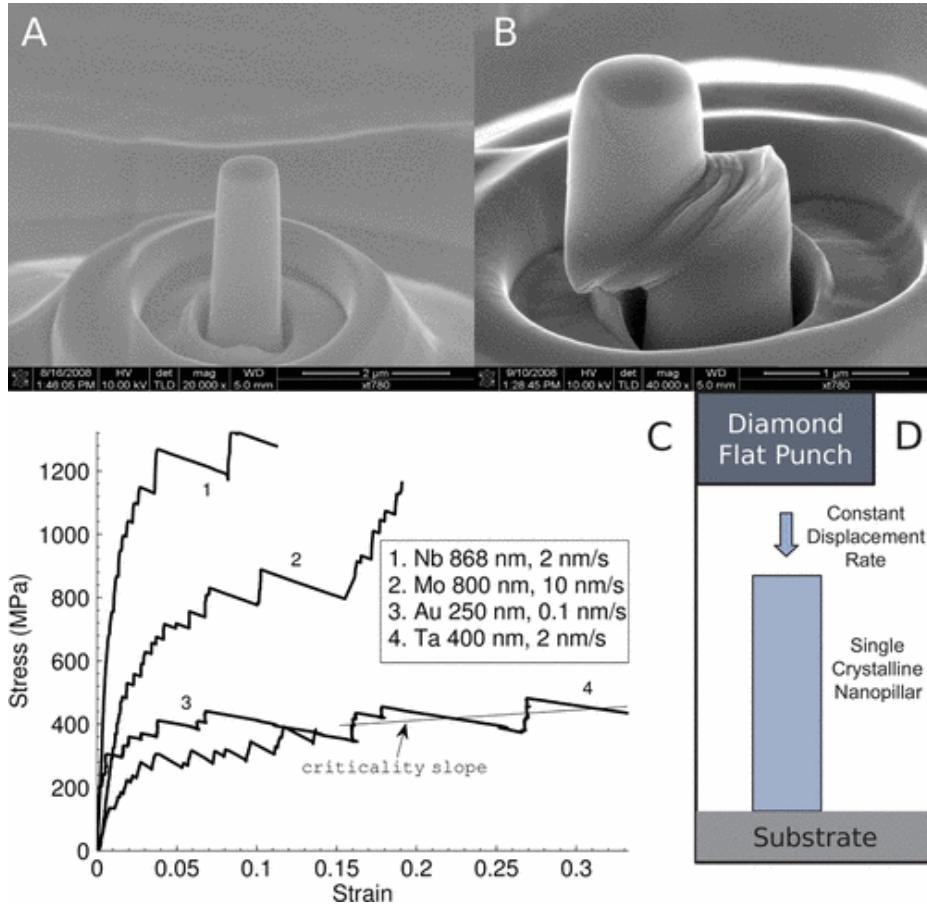


Courtesy of University of Cambridge. Used with permission.

A scanning electron micrograph of a single crystal of cadmium deforming by dislocation slip on 100 planes, forming steps on the surface

Evidence of Slip Systems

N. Friedman et al. Phys. Rev. Lett. 109, 095507 (2012)

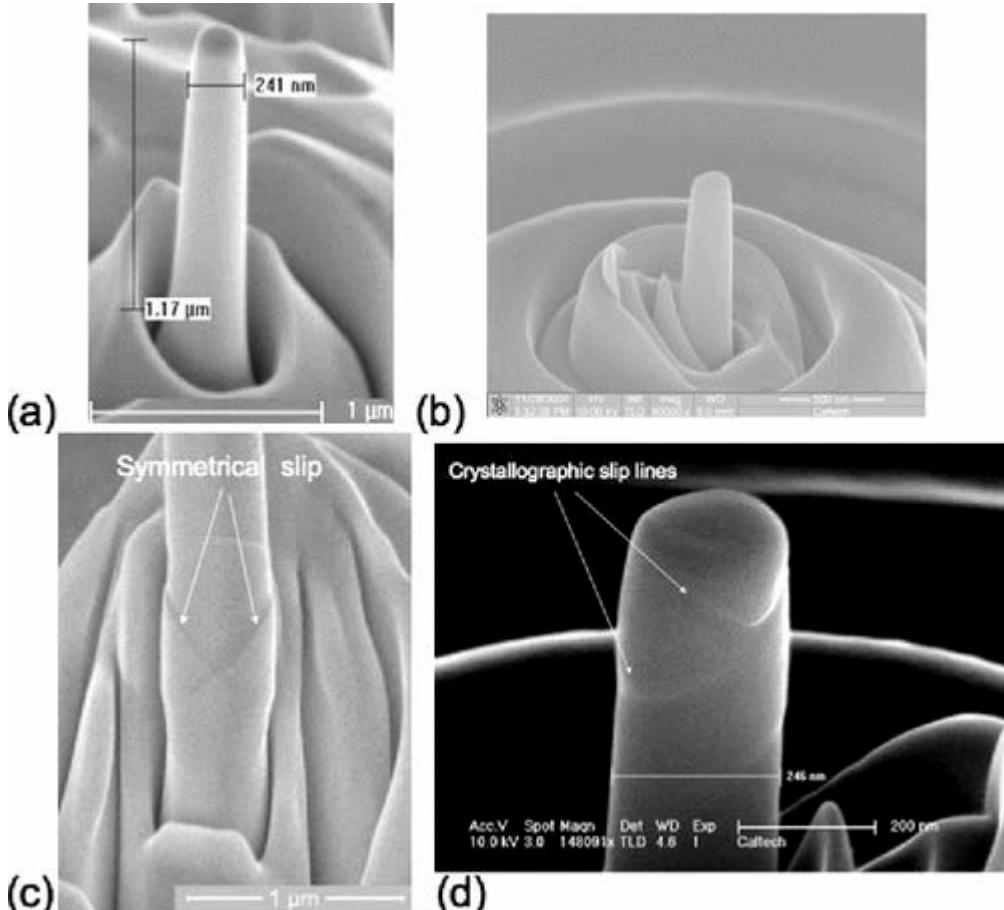


- Nanopillar compression tests using a diamond flat punch
- Clear 45 degree angles observed
- Slip systems activated by *shear*

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Evidence of Slip Systems

S. Brinckmann et al. Phys. Rev. Lett. 100, 155502 (2008)

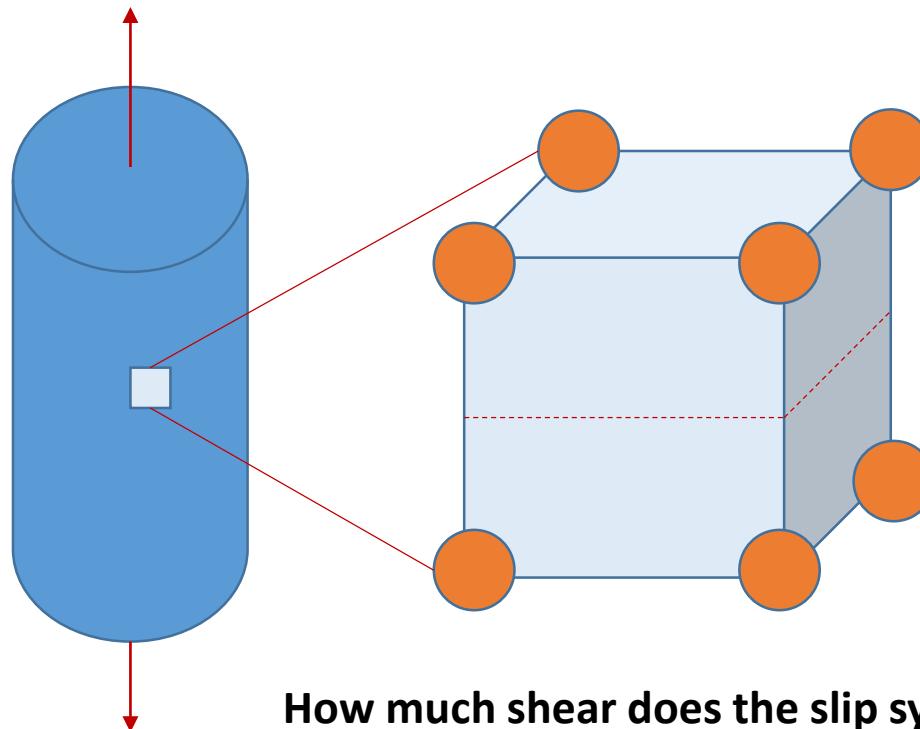


- Nanopillar compression tests using a diamond flat punch
- Clear 45 degree angles observed
- Slip systems activated by *shear*

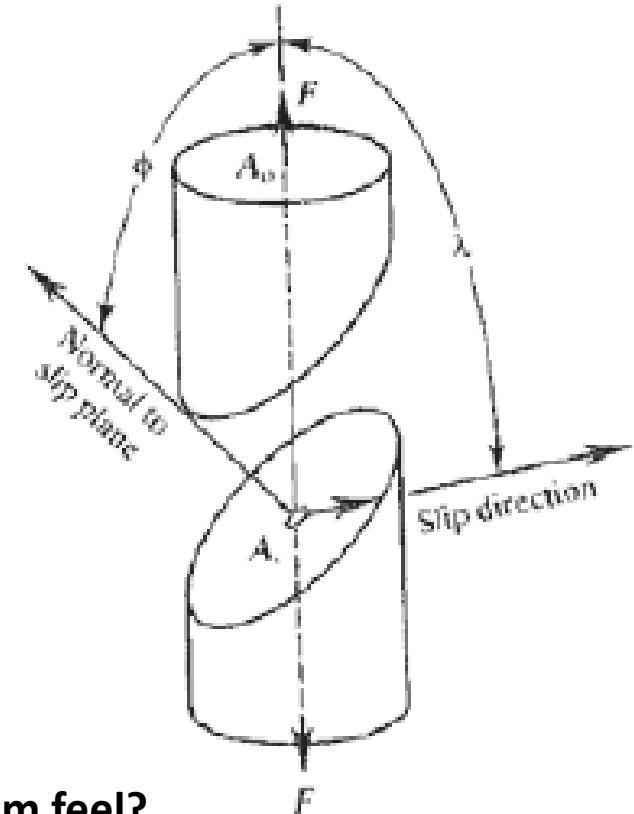
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Resolved Shear Stress

- Consider a single crystal bar of SC material, tensioned in the [001] direction:



How much shear does the slip system feel?



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Resolved Shear Stress

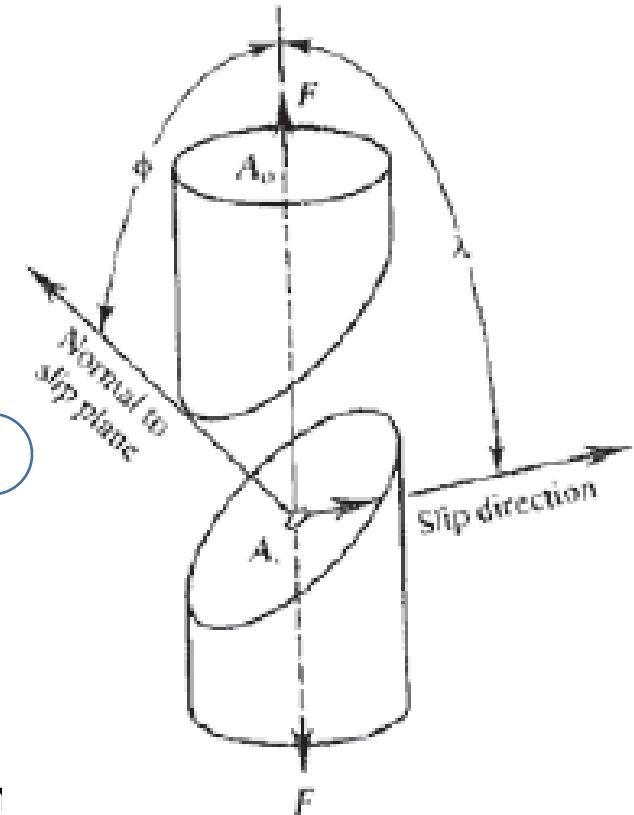
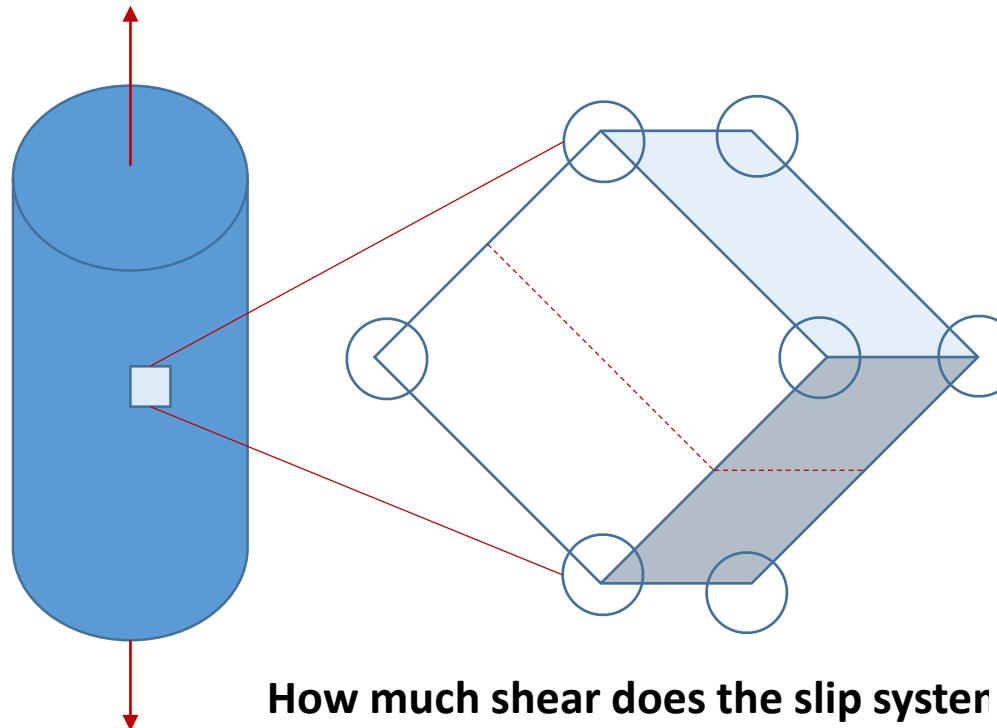
- Consider a single crystal bar of SC material, tensioned in the [001] direction:

Slip Plane	ϕ ($^{\circ}$) \rightarrow $\cos \phi$	Slip Direction	λ ($^{\circ}$) \rightarrow $\cos \lambda$	Schmid Factor
(100)	90 \rightarrow 0.00	[010]	0 \rightarrow 1.00	0
		[001]	90 \rightarrow 0.00	0
(010)	0 \rightarrow 1.00	[100]	90 \rightarrow 0.00	0
		[001]	90 \rightarrow 0.00	0
(001)	90 \rightarrow 0.00	[100]	90 \rightarrow 0.00	0
		[010]	0 \rightarrow 1.00	0

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Resolved Shear Stress

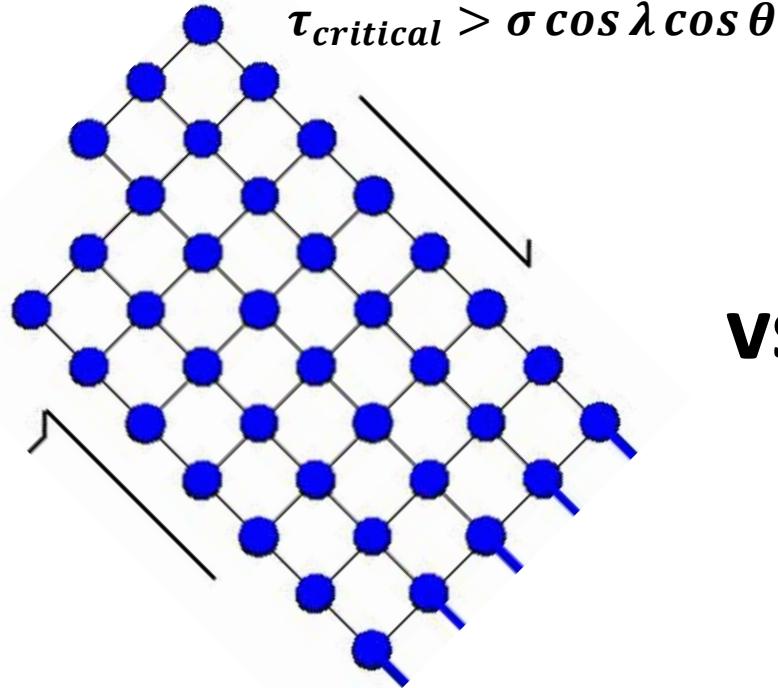
- Consider a single crystal bar of SC material, tensioned in the [011] direction:



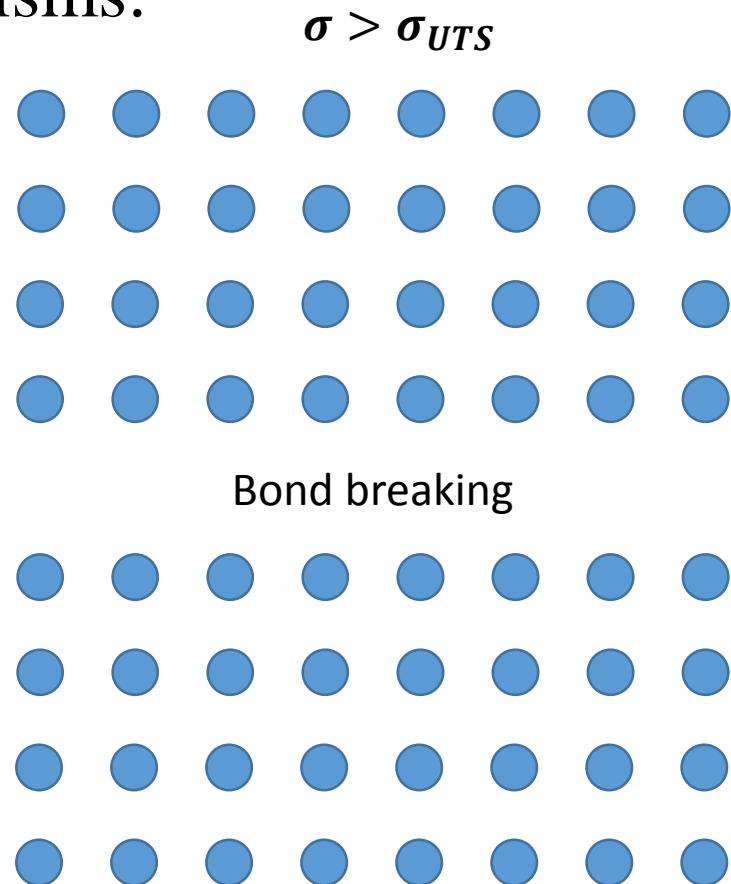
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Will It Slip or Break?

- Balance between two mechanisms:



VS.



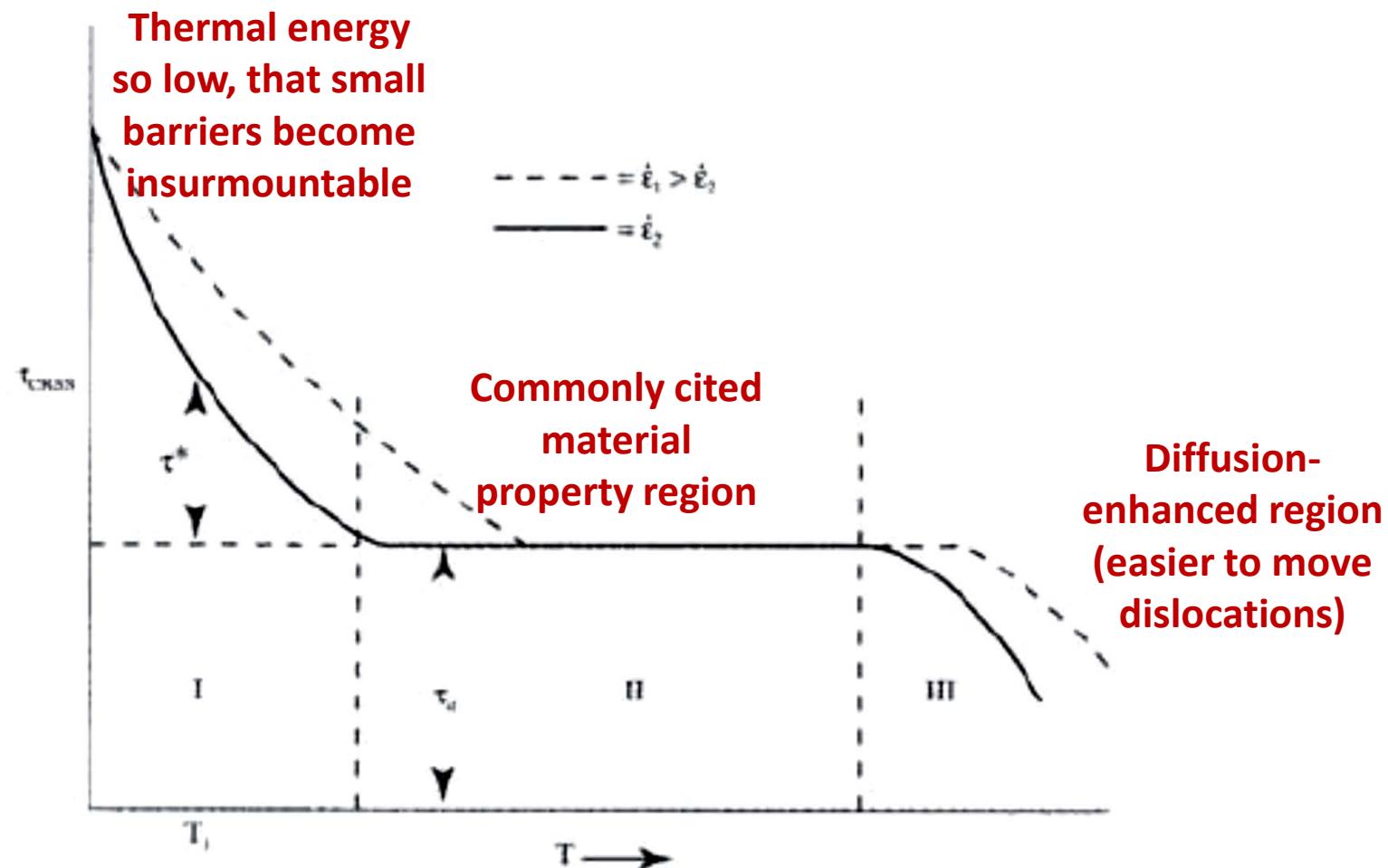
Critical Resolved Shear Stress (τ_{CRSS})

- Shear stress that is enough to get dislocations moving (plastic deformation)
- Related to the *yield stress* (σ_y), the stress where plastic deformation starts:

$$\sigma_y = m\tau_{CRSS}$$

- NOTE: σ_y has crystallographic dependence in single crystals! What about polycrystals?

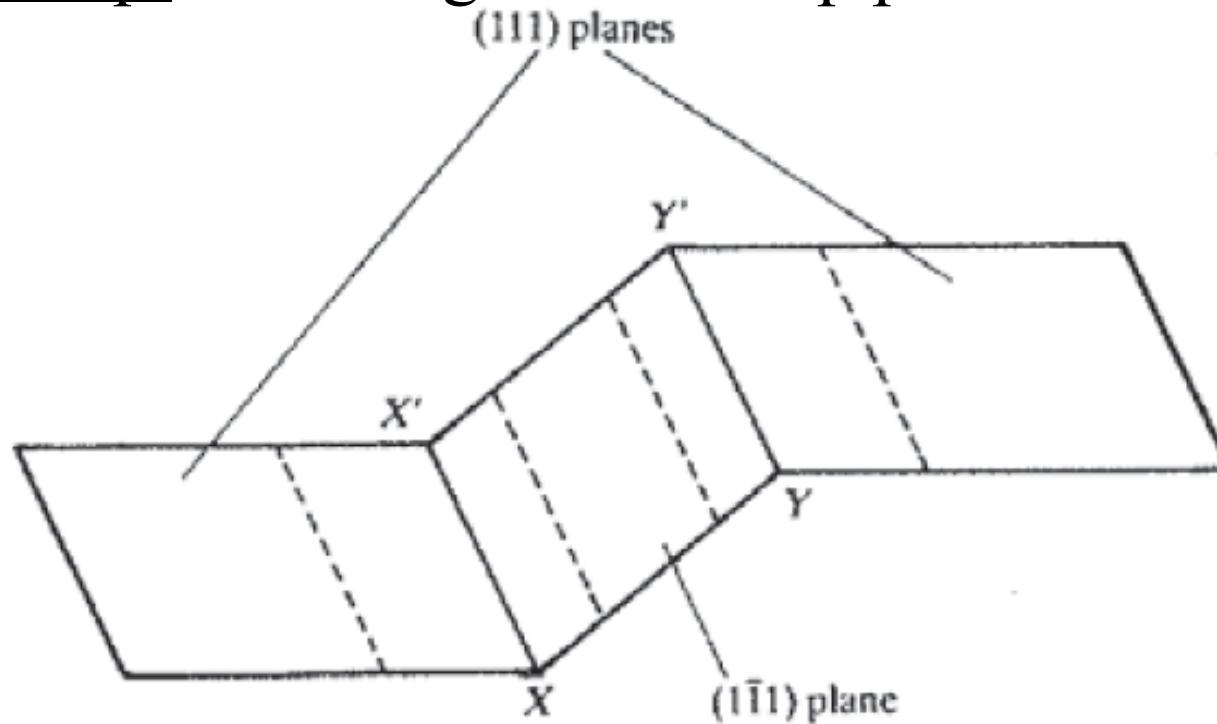
τ_{CRSS} vs. Temperature



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What Happens When Dislocations Get Stuck?

- Cross slip: switching to other slip planes



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- Resolved shear stress must be high enough!

Stress vs. Strain

- Stress: Force over area
- Engineering stress: Force divided by *original* area
- True stress: Force divided by *actual* area as it *changes*

$$\sigma = \frac{F}{A_0} \qquad \qquad \sigma_t = \frac{F}{A(t)} = \frac{F}{A_0} \frac{A_0}{A(t)} = \sigma \frac{A_0}{A(t)}$$

- Conserve volume during stretching: $V_0 = V(t)$

Stress vs. Strain

$$\sigma = \frac{F}{A_0}$$

$$\sigma_t = \frac{F}{A(t)} = \frac{F}{A_0} \frac{A_0}{A(t)} = \sigma \frac{A_0}{A(t)}$$

- Conserve volume during stretching: $V_0 = V(t)$

$$V_0 = A_0 L_0 = V(t) = A(t) L(t); \quad \frac{A(t)}{A_0} = \frac{L_0}{L(t)}$$

$$\sigma_t = \sigma \frac{A_0}{A(t)} = \sigma \frac{L(T)}{L_0} = \sigma \frac{L_0 + \delta L}{L_0} = \sigma \left(1 + \frac{\delta L}{L_0} \right)$$

Engineering strain (ϵ)



True vs. Engineering Strain

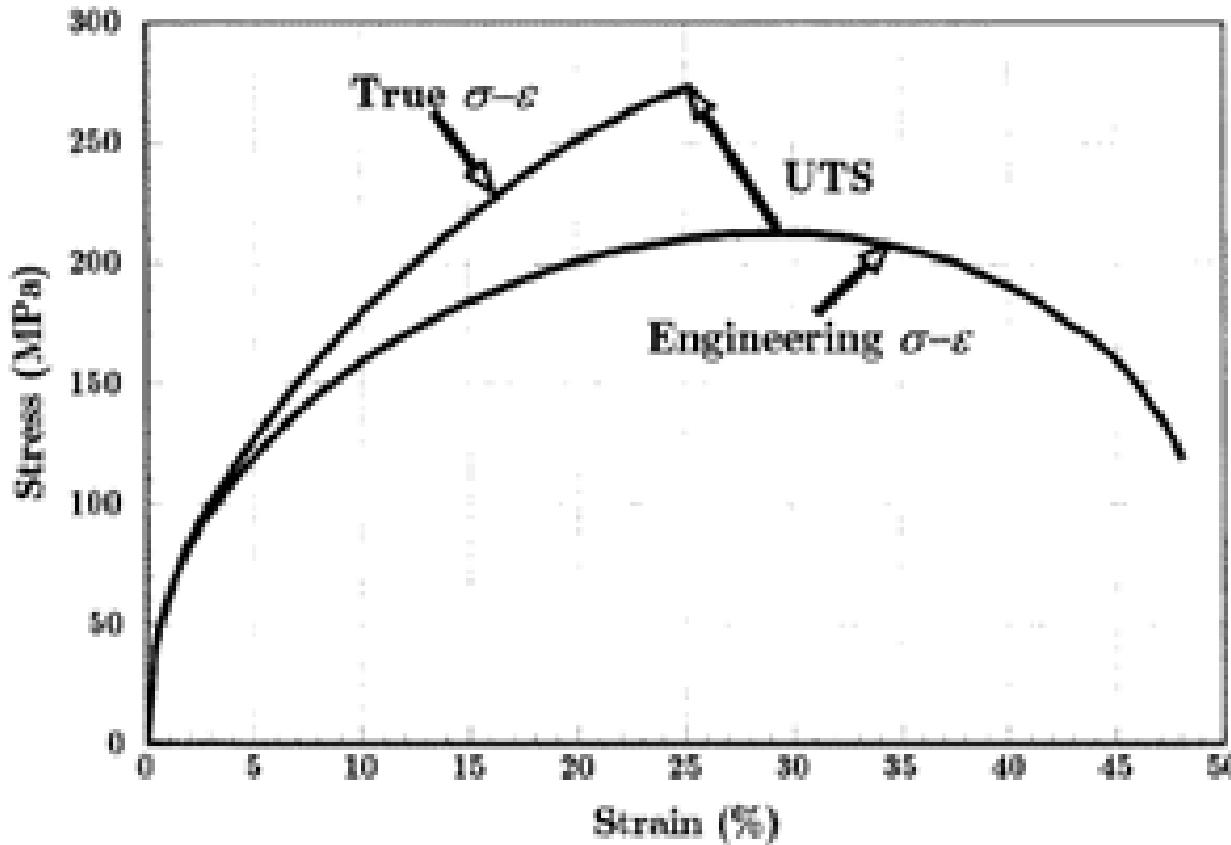
- Engineering strain (ε): $\frac{\delta L}{L_0}$ (from *original* length)
- True strain (ε_T): Instantaneous increase in length:

$$\varepsilon_T = \int_{L_0}^{L(t)} \frac{dL}{L} = \ln L(t) - \ln L_0 = \ln \left[\frac{L(t)}{L_0} \right]$$

$$\varepsilon_T = \ln \left[\frac{L_0 + \delta L}{L_0} \right] = \ln[1 + \varepsilon]$$

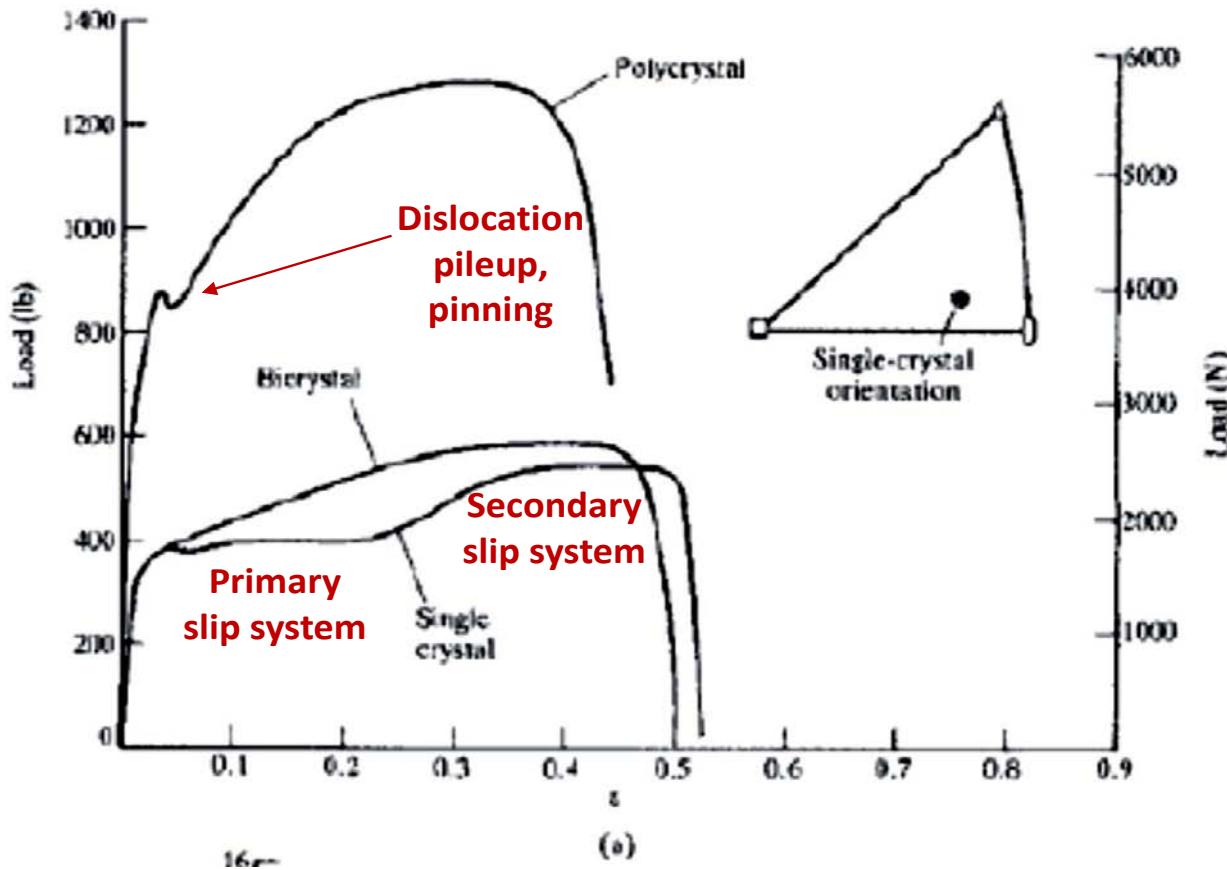
Stress-Strain Curves

<http://keytometals.com/page.aspx?ID=CheckArticle&site=kts&NM=42>



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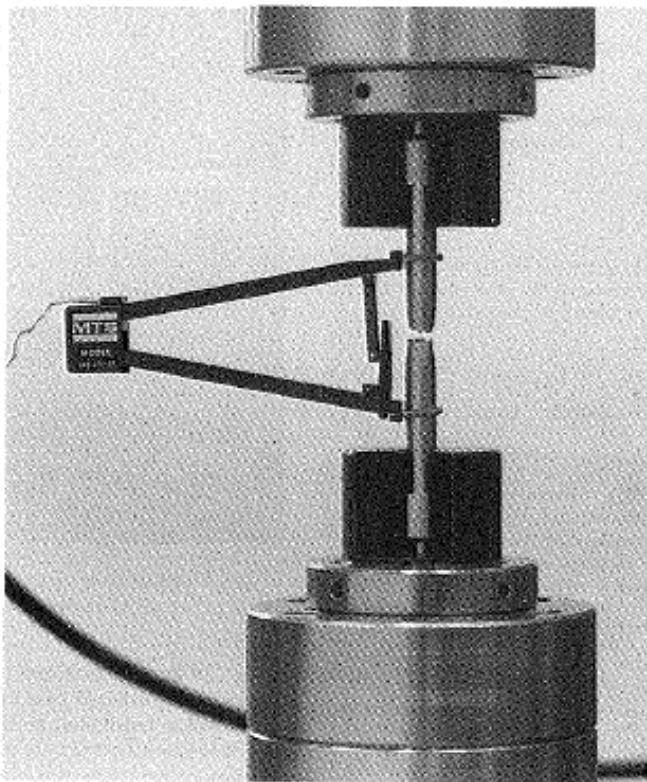
Single, Dual, and Polycrystals



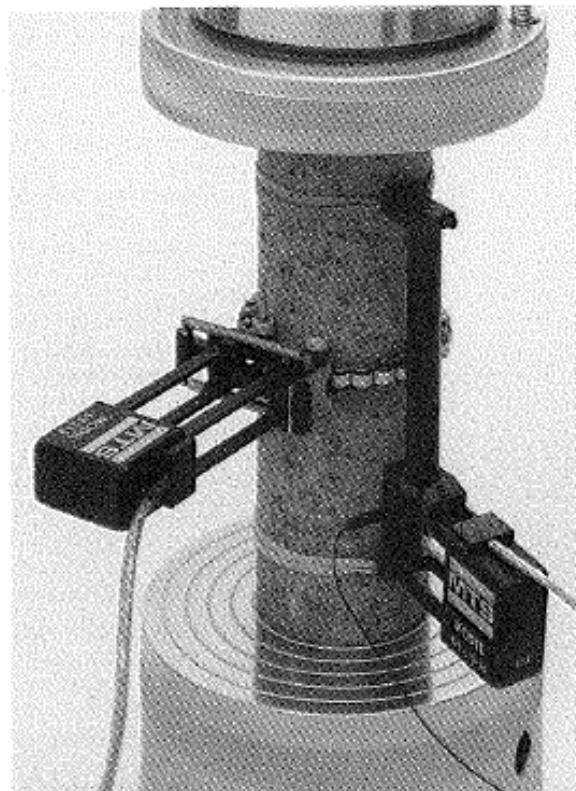
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Measuring Stress-Strain

J. M. Gere, "Mechanics of Materials," pp. 12, 14



Uniaxial tensile tester, with extensometer for measuring strain



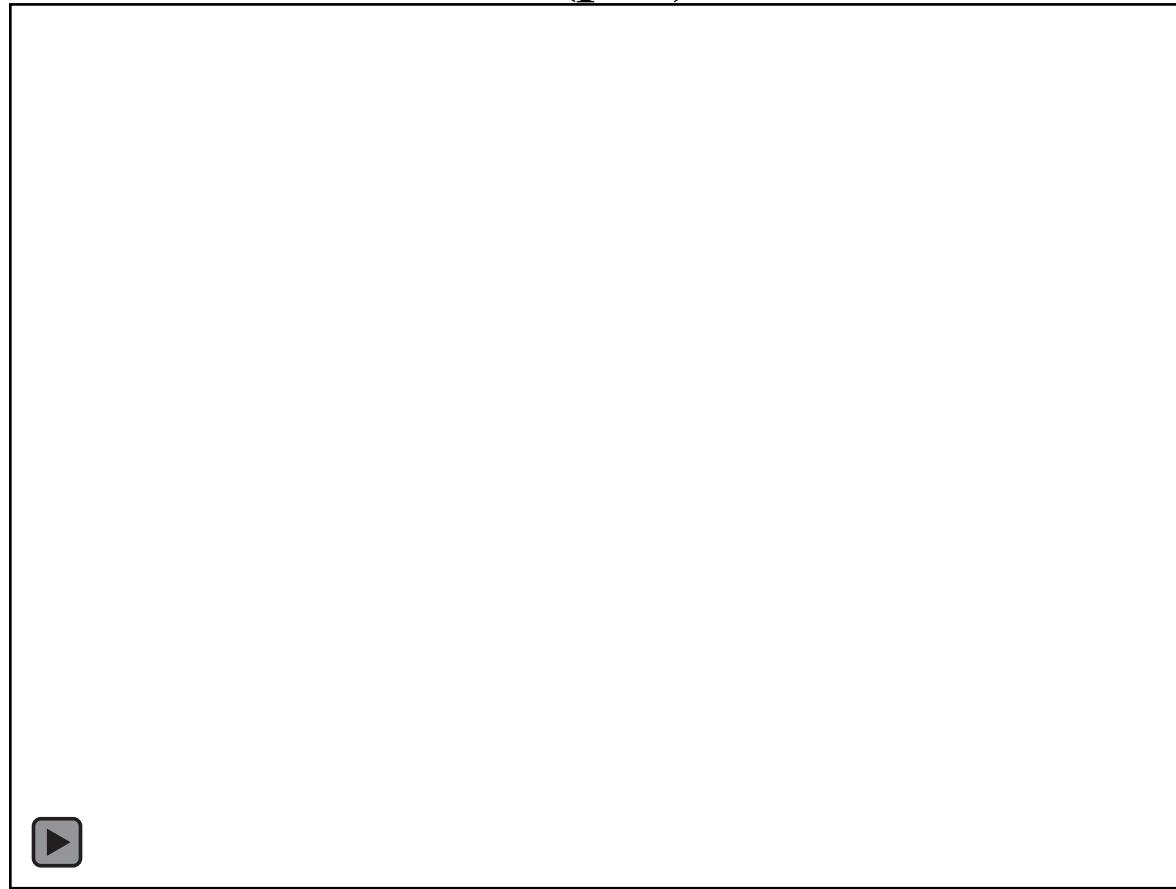
Uniaxial compression tester, with extensometer and diameter measurement

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Dislocations and Defects

E. Bitzek and P. Gumbsch, Dynamic aspects of dislocation motion: atomistic simulations, Materials Science and Engineering A, 400-401 (2005), pp. 40-44

- Defects can slow down (pin) dislocations



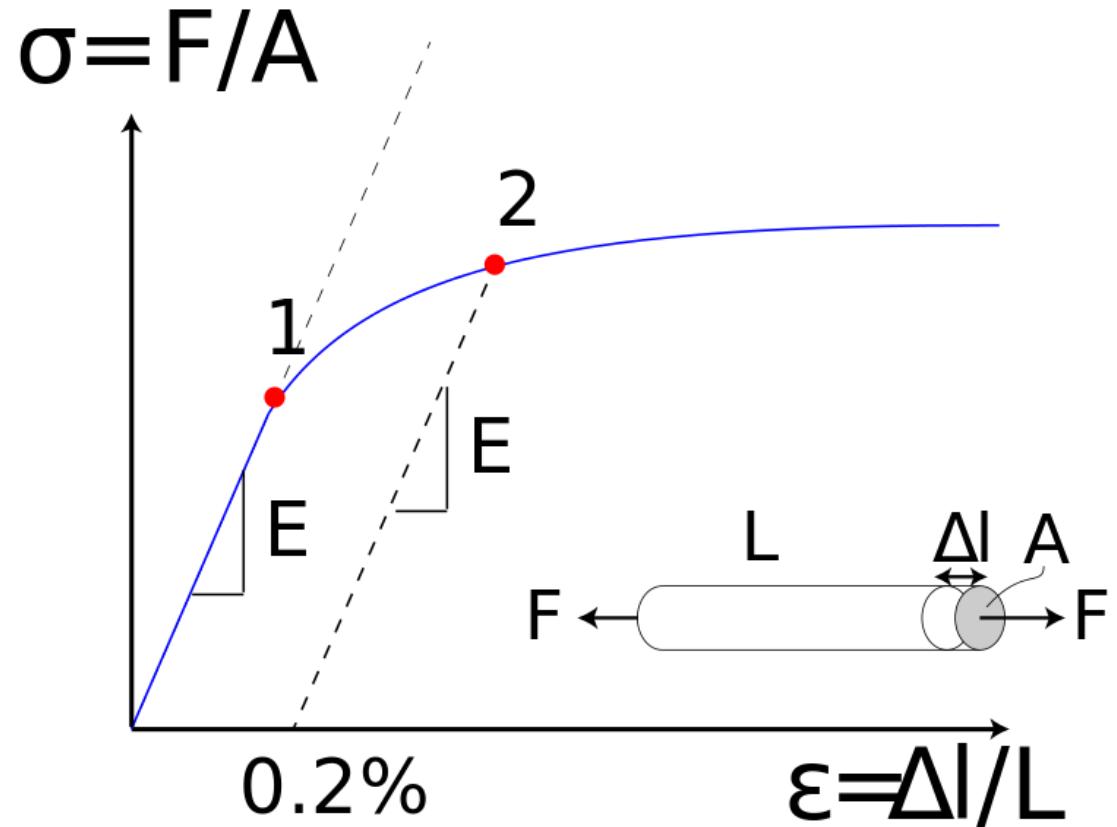
A video is played in class to demonstrate the concept.

Reviewing Material Properties

- Find the following on a stress-strain diagram:
- Toughness
- Strength
- Ductility
- Stiffness
- Perhaps define them first...

Young's Modulus (Stiffness, E)

Measures elastic deformation vs. stress



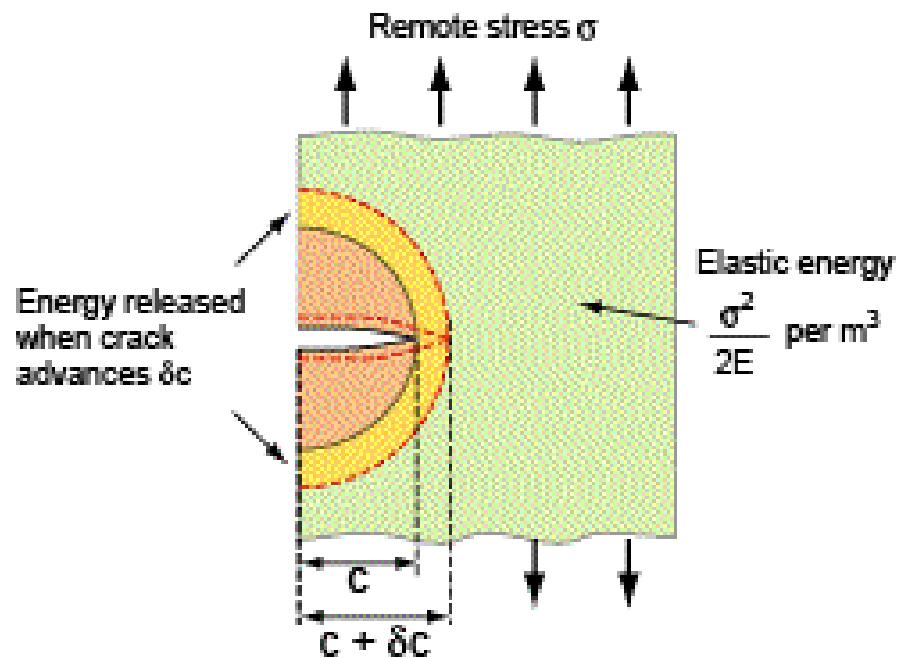
Source: Wikimedia Commons

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Toughness (G_c)

- Measures the energy it takes to separate a material

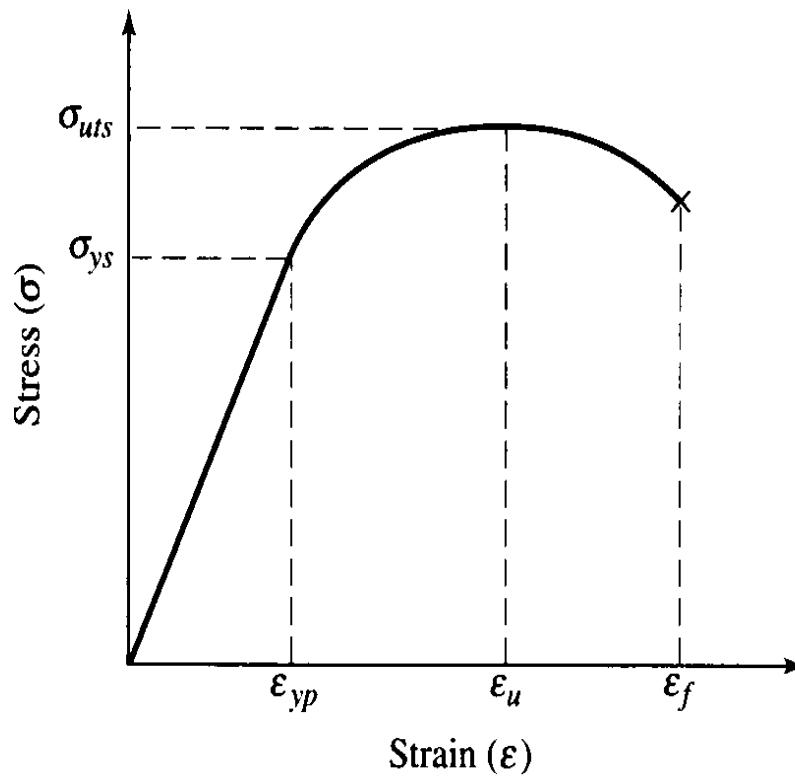
$$K_{Ic} = \sqrt{EG_c}$$



Source: inventor.grantadesign.com

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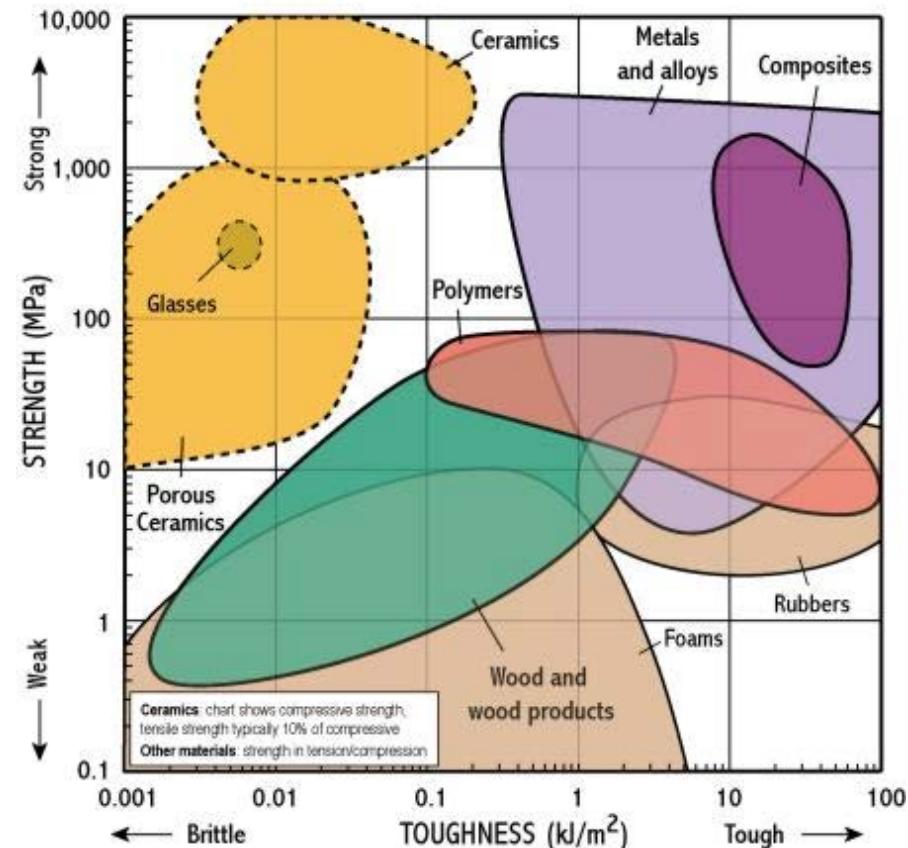
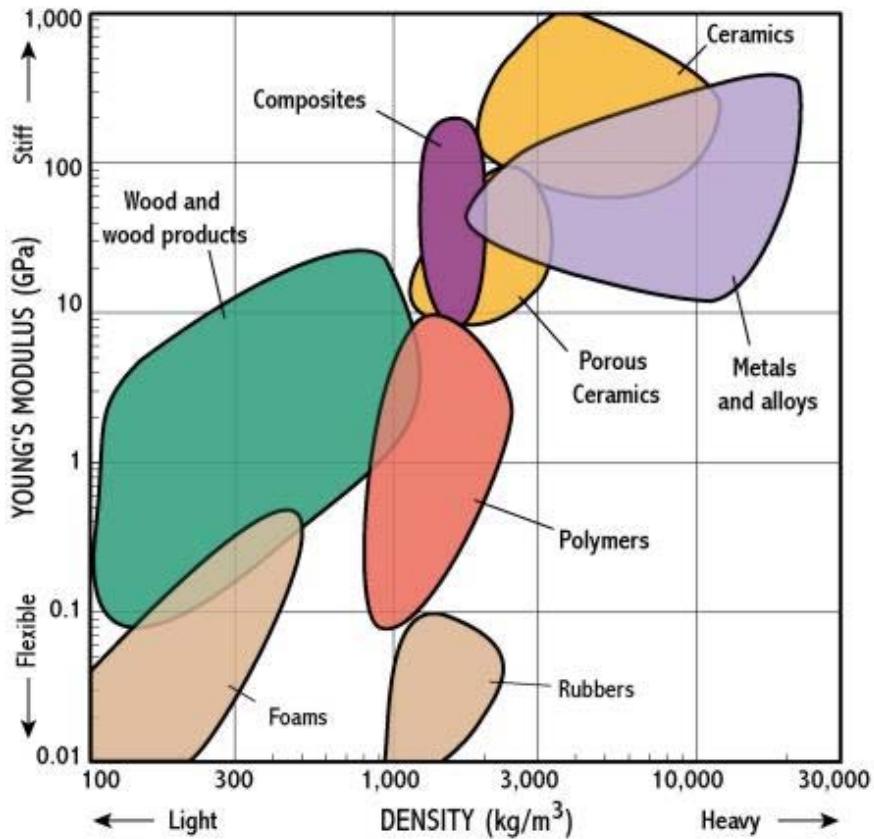
Material Properties on Stress-Strain Diagram



Courtesy of [Ben Best](#). Used with permission.

<http://www.benbest.com/cryonics/lessons.html>

Materials Selection Charts



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http://www-g.eng.cam.ac.uk/125/now/mfs/tutorial/non_IE/charts.html

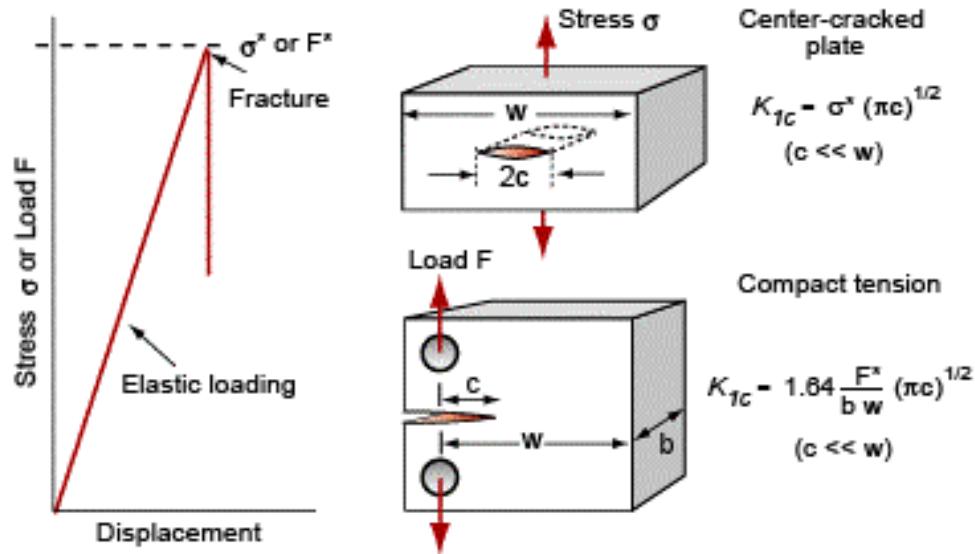
Failure Criteria – Crack Propagation

$$K_{Ic} = Y_1 \sigma^* \sqrt{\pi c} \text{ or } K_{Ic} = Y_2 \frac{F^*}{bw} \sqrt{\pi c}$$

Resistance to crack propagation

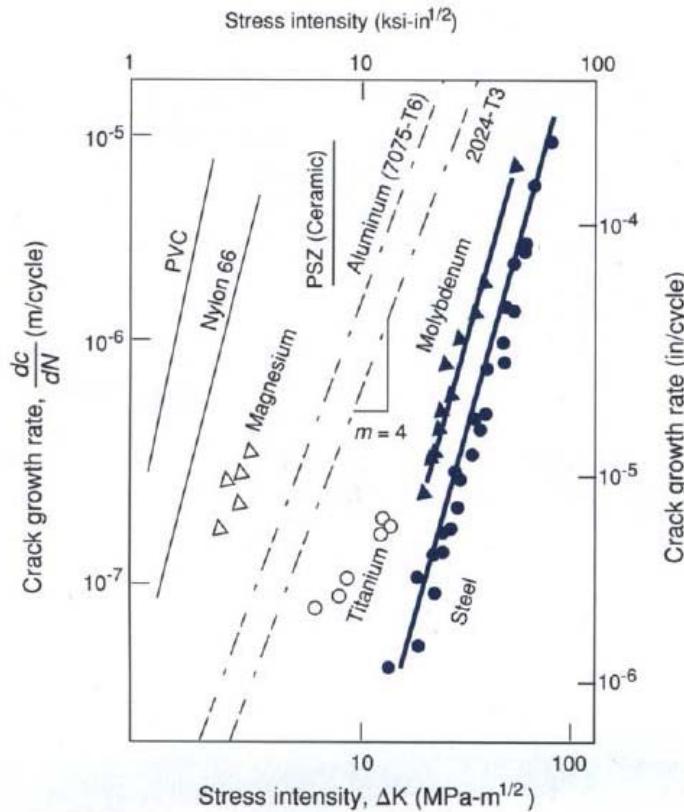
- Y_1, Y_2 are geometric factors near 1
- σ^*, F^* are critical stress and force, respectively

Source: inventor.grantadesign.com

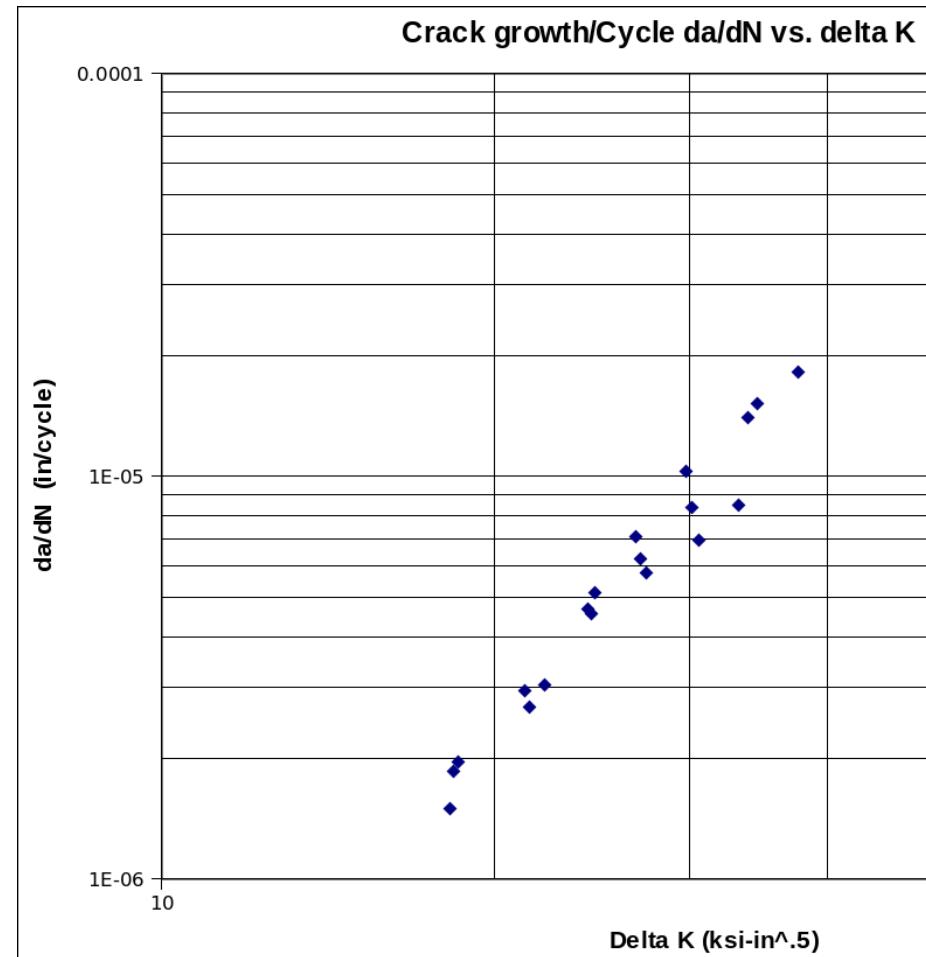


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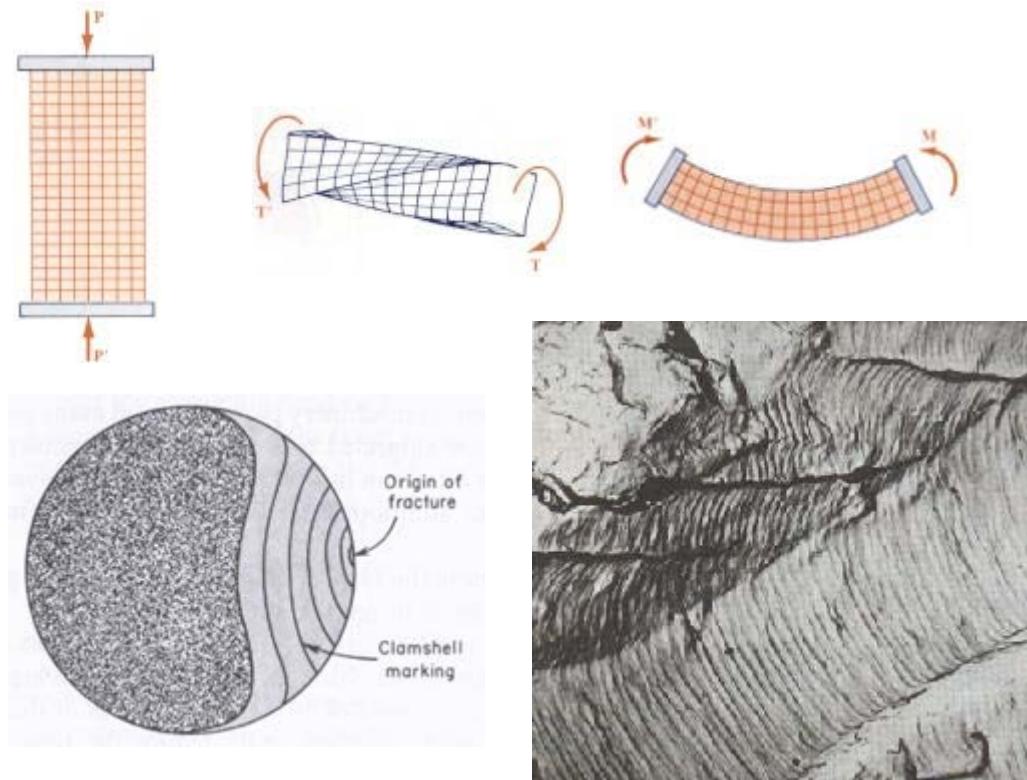
Fracture Toughness – Real Data from Alcator C-Mod



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Failure Criteria – Fatigue

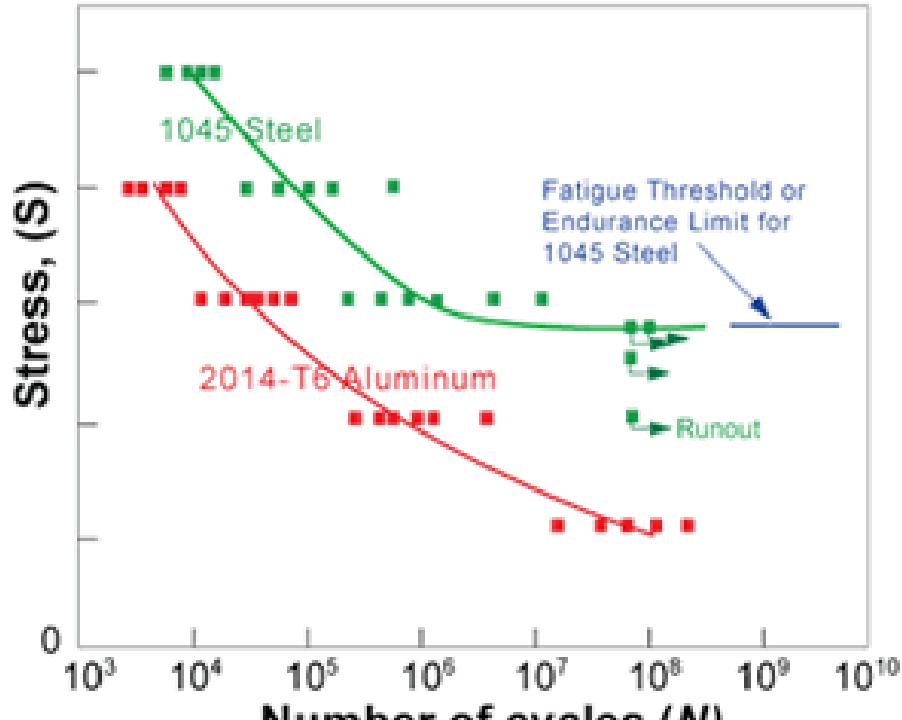


- Repeated application of stress can cause cracks to grow
- Induced by vibrations, mechanical loading
- Telltale “fatigue striations”
- **Where do these come from?**

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Source: www.sv.vt.edu/classes/MSE2094_NoteBook/97ClassProj/anal/kelly/fatigue.html

Failure Criteria – Fatigue

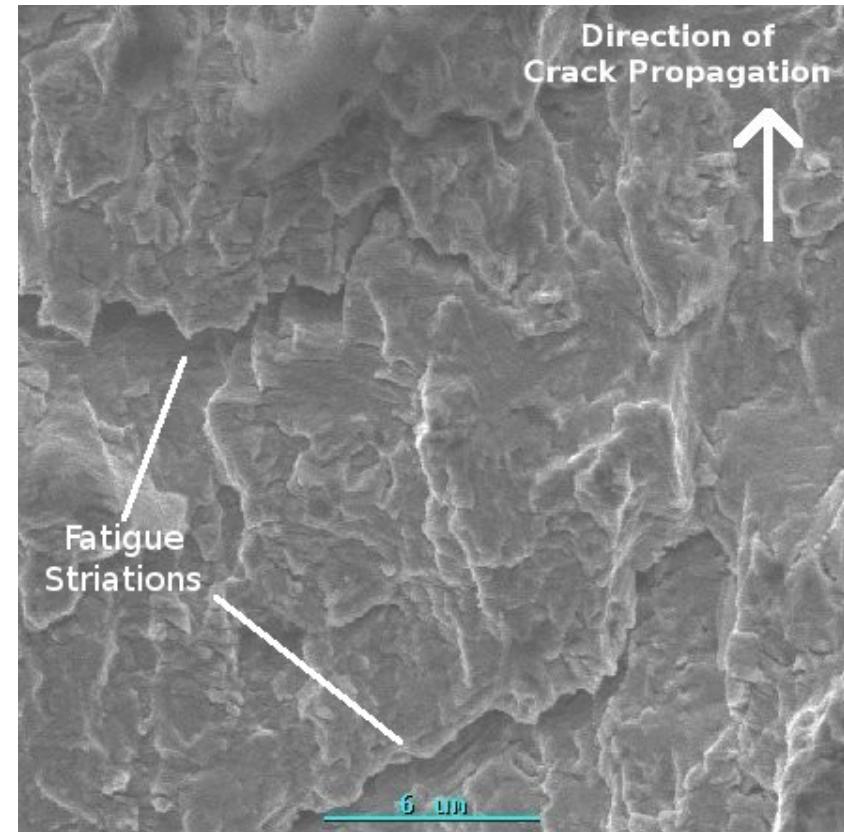
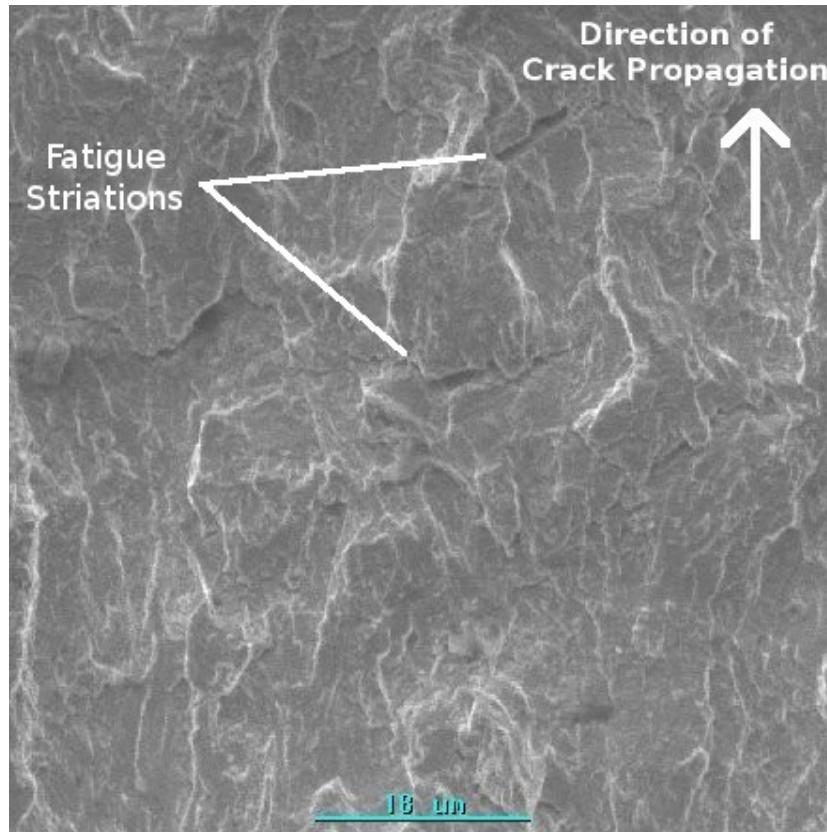


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- Stress (S) vs. number of cycles (N)
- Lower limit of stress (where N is infinite) is the “safe zone”
- **Why do these limits exist?**

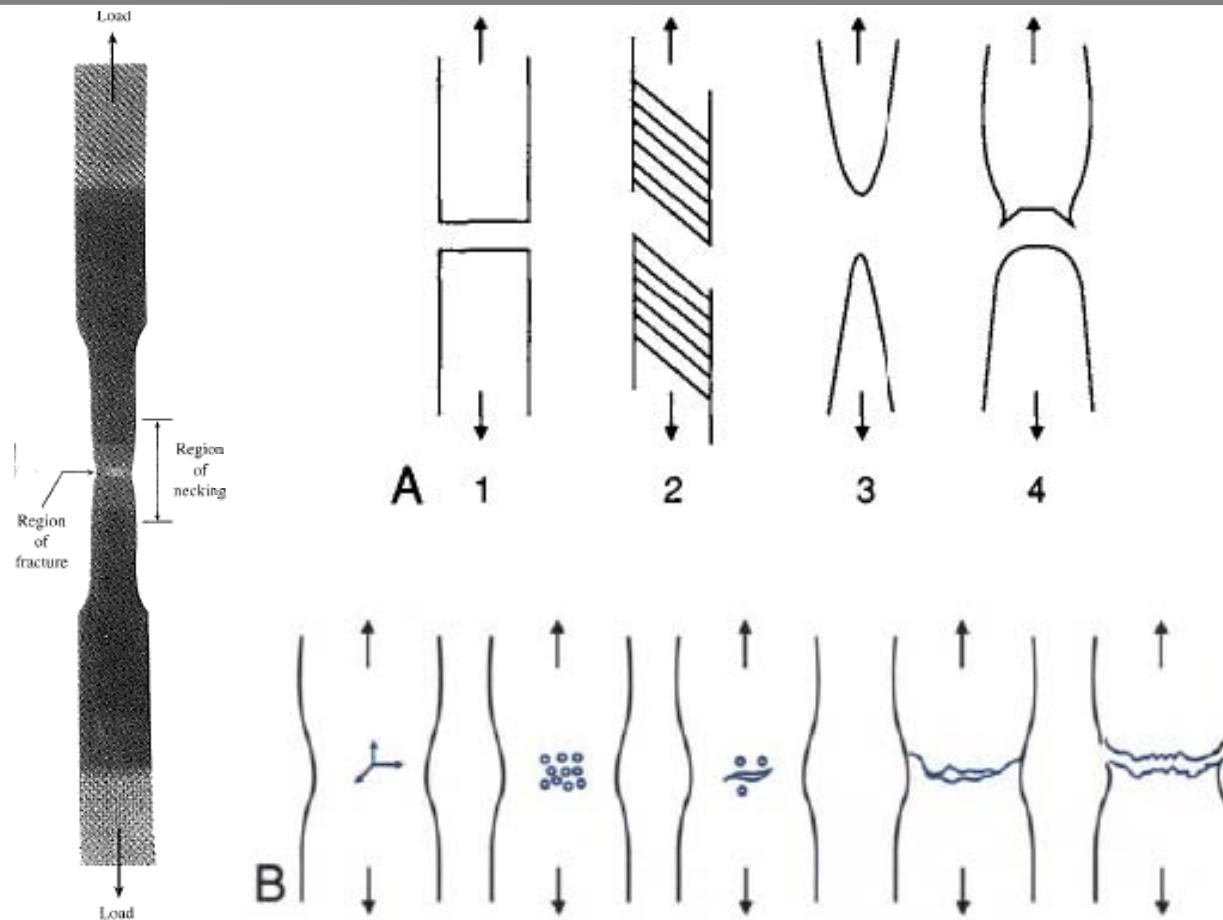
Source: www.nde-ed.org/EducationResources/CommunityCollege/Materials/Mechanical/S-NFatigue.htm

Fatigue Striations in Alcator C-Mod Rotor



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Failure Mechanisms in Tension

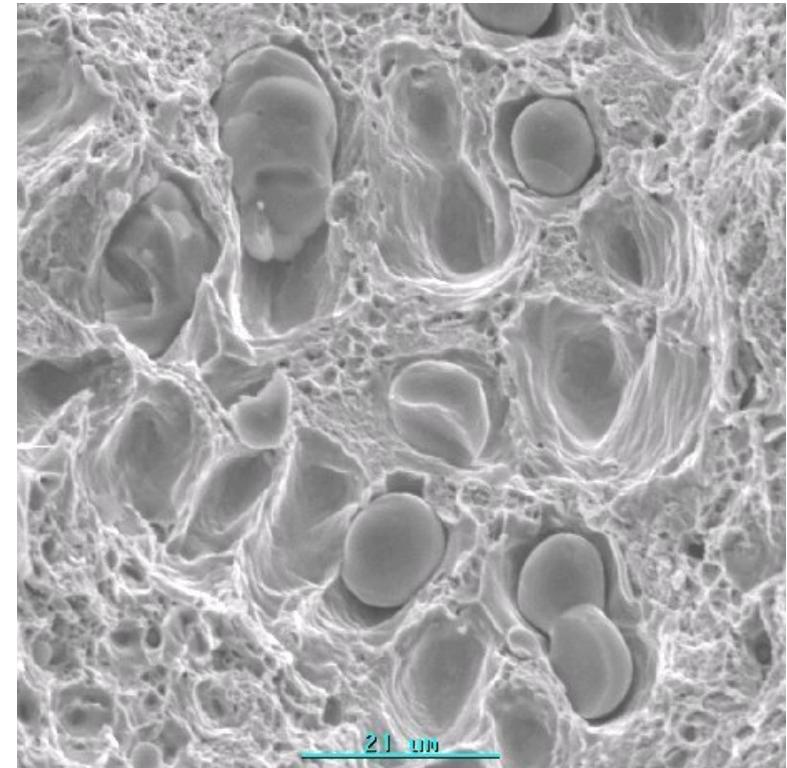
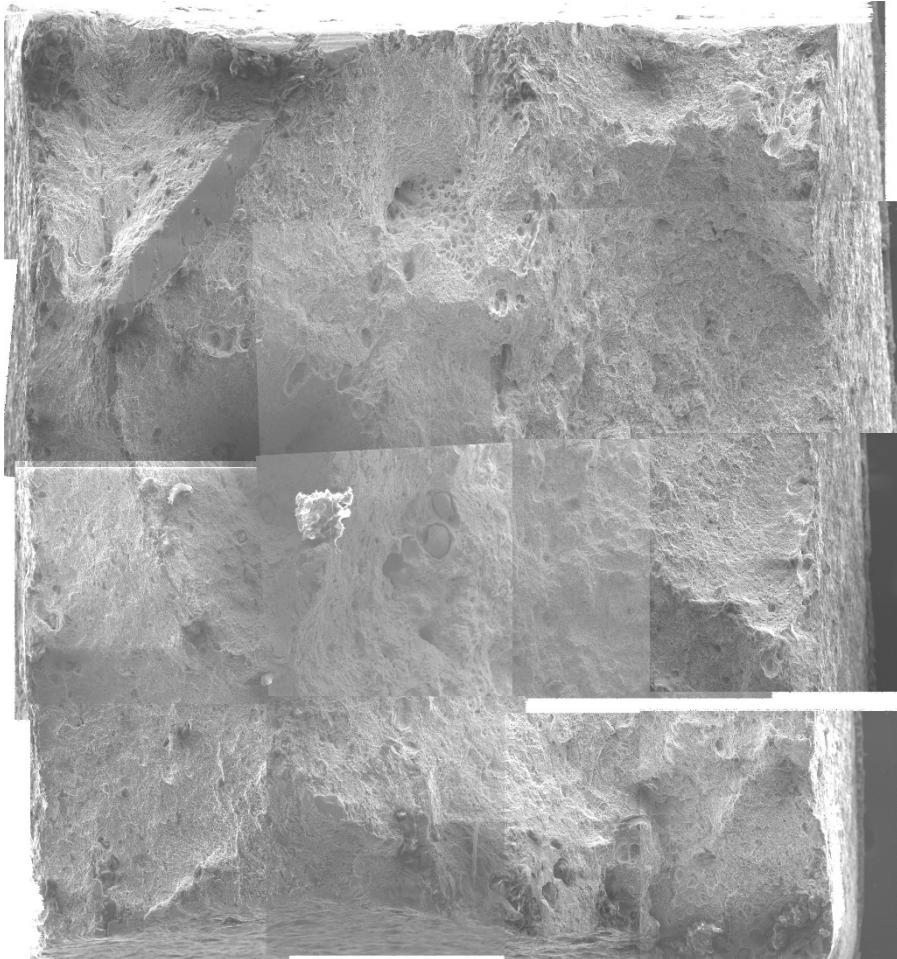


1. Brittle fracture
2. Single crystal slip bands
3. Ideal ductile fracture (full elongation)
4. Realistic cup-and-cone fracture

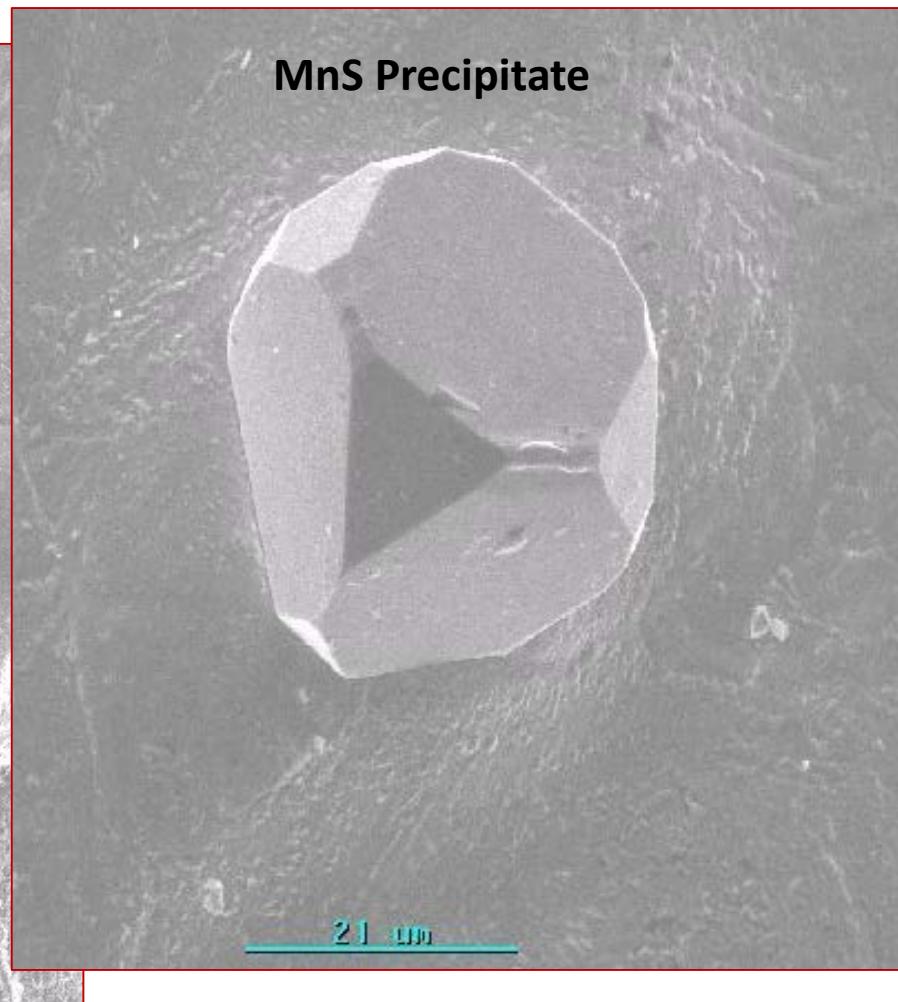
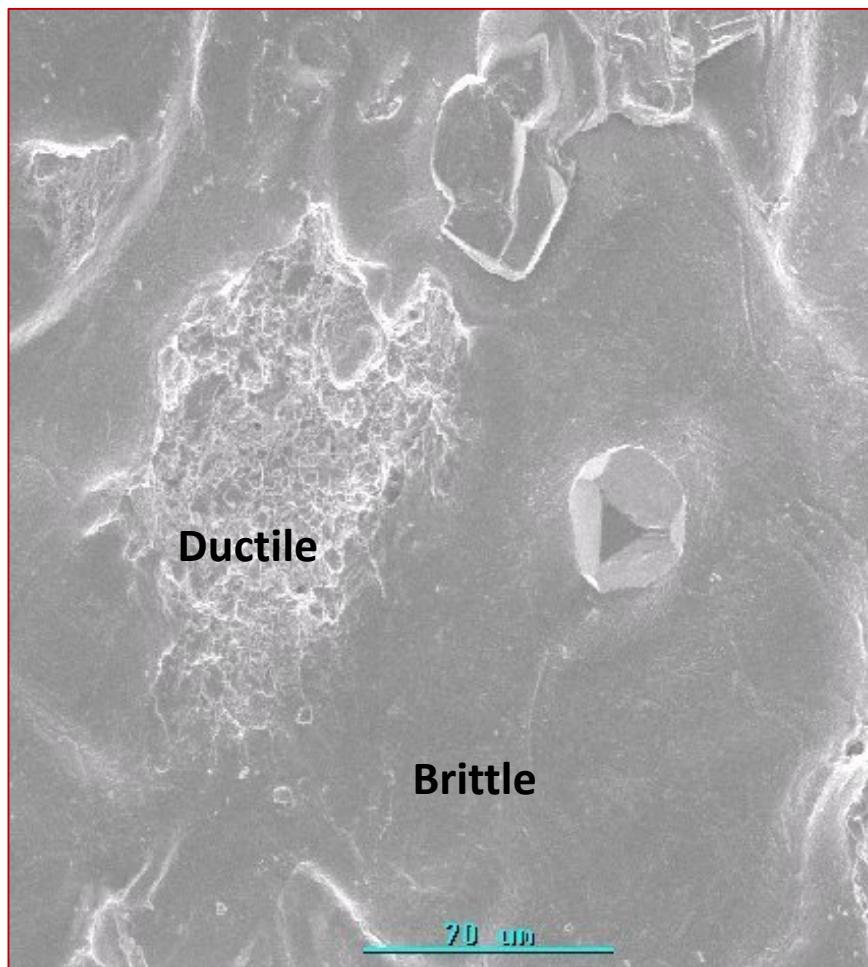
Stages of cup-and-cone fracture formation in ductile materials

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Examples of Cup-and-Cone Fracture in Alcator C-Mod

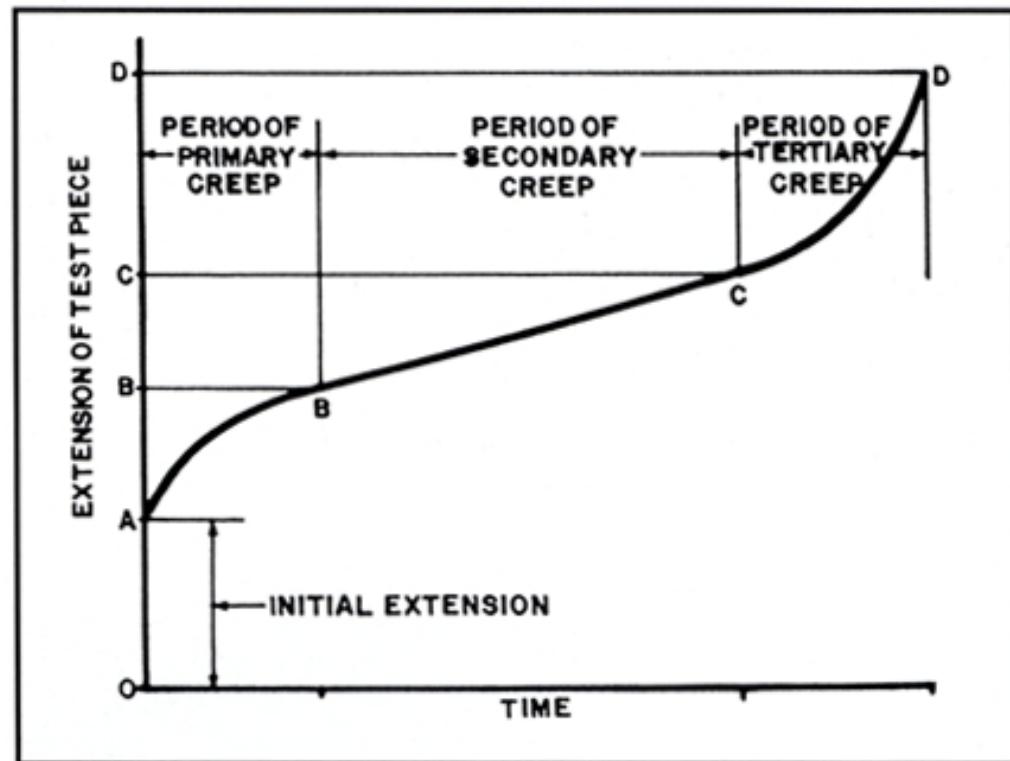
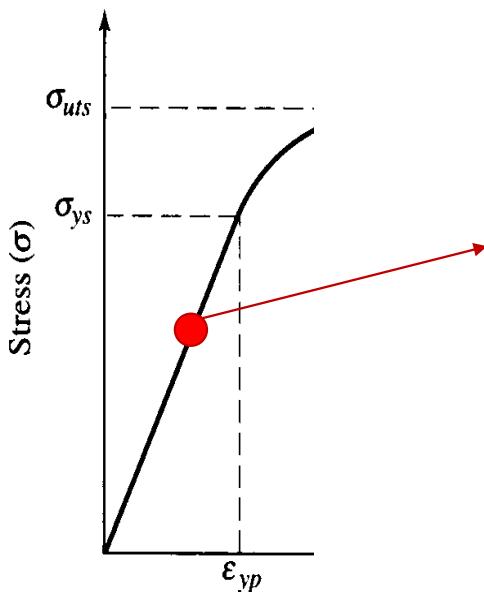


Brittle & Ductile Fracture, Side by Side



Creep – Plastic Deformation Below Yield Stress

- Imagine stretching a bar of metal within the elastic region



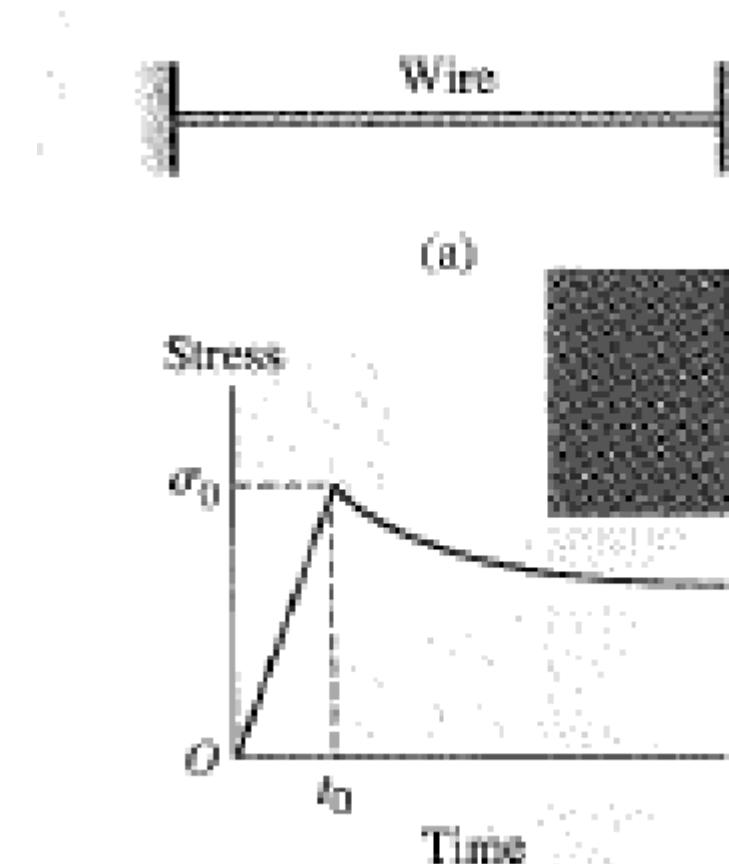
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<http://www.nationalboard.org/Index.aspx?pageID=181>

Creep – Stress vs. Time

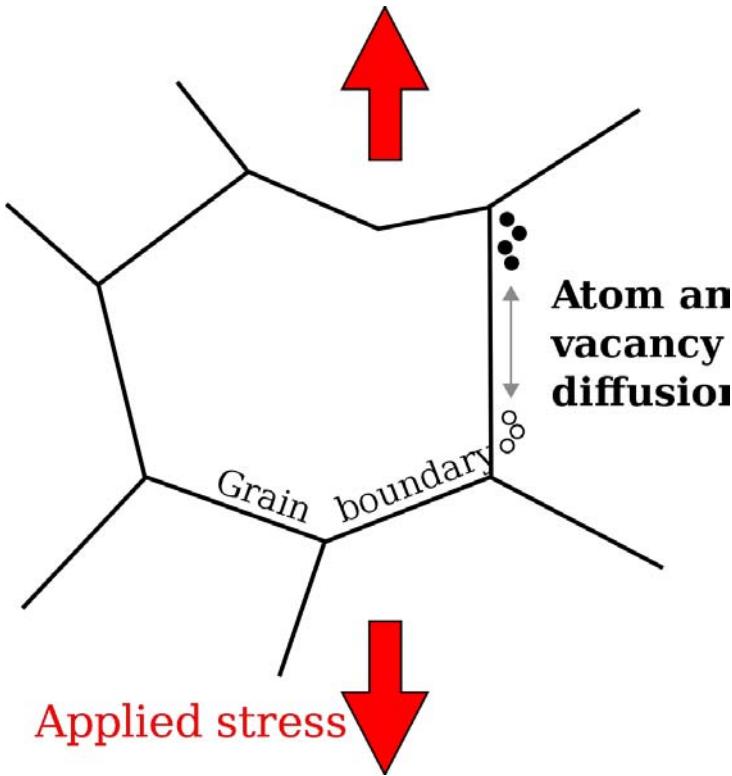
J. M. Gere, "Mechanics of Materials," pp. 22

- Stress increased elastically to σ_0
- Held for long time
- Stress at constant strain decreases due to *creep*



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Creep Mechanisms



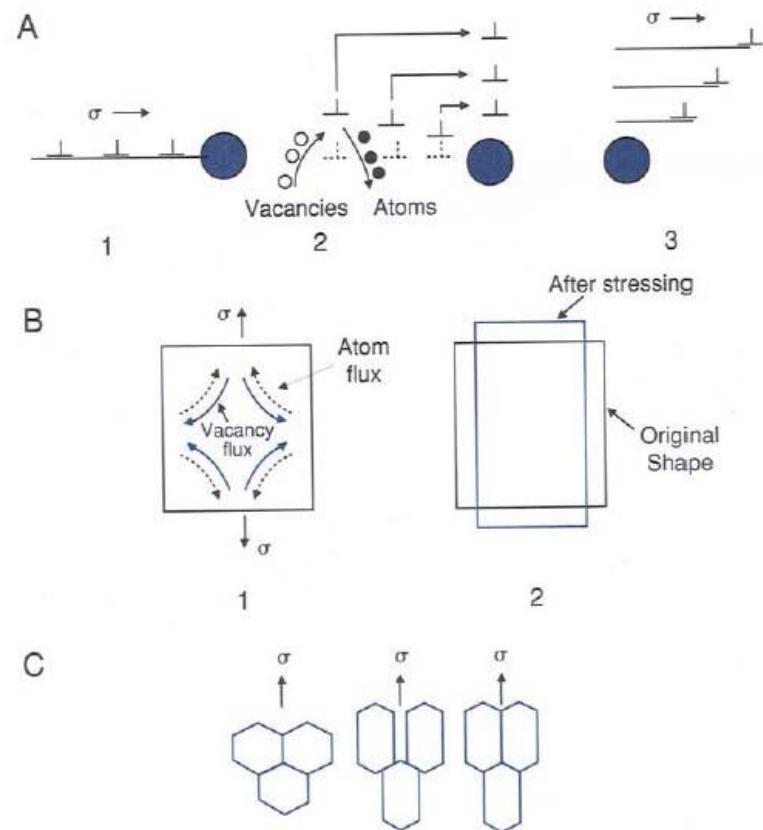
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Source: Wikimedia Commons

- Plastic flow under constant stress
- Tension, gravity...
- Happens well below yield stress
- Multiple modes (Coble, Nabarro-Herring...)

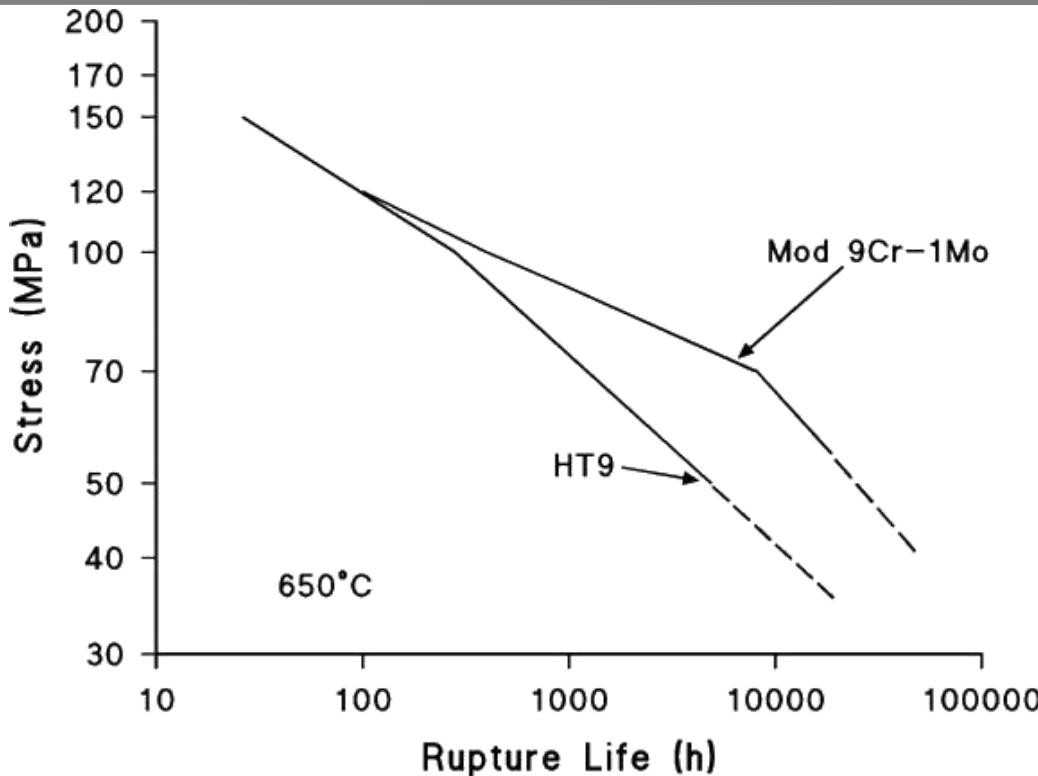
Creep Mechanisms

- Dislocation climb
 - Follows power law
- Nabarro-Herring (diffusional)
 - Vacancy movement
- Coble
 - Grain boundary movement



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Failure Criterion – Creep Lifetime



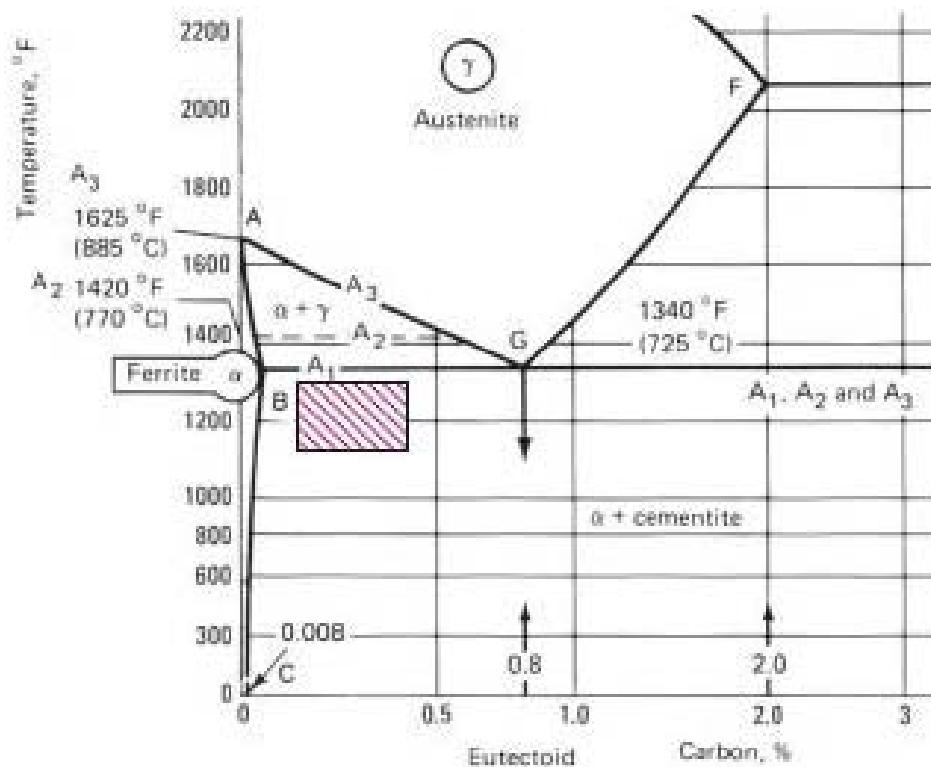
- Creep rupture lifetime can limit usefulness of part
- Example: Alloys HT9, T91 in high temperature service conditions

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Source: Klueh, R. L., and A. T. Nelson. "Ferritic / Martensitic Steels for Next-generation Reactors." *Journal of Nuclear Materials* 371, no. 1-3 (2007): 37-52.

Source: R.L. Klueh, A.T. Nelson. *J. Nucl. Mater.*, 371(1-3):37-52 (2007).

Creep Failure by Time at Temperature and Pressure



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Creep failure of alloy T91 due to improper heat treatment, heated above A_1 temperature. In T. Totenmeier, "Experience with Grade 91 Steel in the Fossil Power Industry." Presentation, ALSTOM, Feb. 2009.

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22.14 Materials in Nuclear Engineering

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