## **Practical Rankine cycle**

define some units  $kJ := 10^3 \cdot J$ 

this file calculates *irreversible* Rankine cycle with following parameters: condenser 40 deg C

steam pressure 30 bars (3 MPa)

superheat 460 deg C

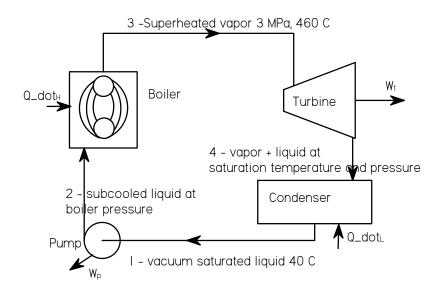
file derived from Rankine class example.mcd

 $kN := 10^3 \cdot N$   $kPa := 10^3 \cdot Pa$ 

 $MPa := 10^6 Pa$  bar := 0.1 MPa

#### differences/assumptions:

- 1-2 adiabatic irreversible compression
- 2-3 heat transfer small pressure loss ignore
- 3-4 adiabatic irreversible expansion
- 4-1 heat transfer to saturated liquid small subcooling ignored



#### states are the same

- 1 vacuum; saturated liquid
- 2 sub cooled liquid at boiler pressure
- 3 superheated vapor
- 4 vapor + liquid @ saturation temperature and pressure

xx<sub>s</sub> designates reversible (isentropic) process where different

refer to T-s and H-s diagrams at end of file

#### state 1: condenser outlet same as reversible

Table 1 or Table A.1.1

$$T_1 := 40$$

$$p_1 := 7.384 \text{kPa}$$

$$T_1 := 40$$
  $p_1 := 7.384 \text{kPa}$   $v_{f_1} := 0.0010078 \frac{\text{m}^3}{\text{kg}}$   $v_1 := v_{f_1}$ 

$$\mathbf{v}_1 \coloneqq \mathbf{v}_{\mathbf{f}_{-1}}$$

$$\mathbf{s_{f\_1}} \coloneqq 0.5725 \, \frac{\mathrm{kJ}}{\mathrm{kg} \cdot \mathrm{K}} \qquad \mathbf{s_{fg\_1}} \coloneqq 7.6845 \, \frac{\mathrm{kJ}}{\mathrm{kg} \cdot \mathrm{K}} \qquad \mathbf{h_{f\_1}} \coloneqq 167.57 \, \frac{\mathrm{kJ}}{\mathrm{kg}} \qquad \quad \mathbf{h_{fg\_1}} \coloneqq 2406.7 \, \frac{\mathrm{kJ}}{\mathrm{kg}}$$

$$s_{\text{fg\_1}} := 7.6845 \frac{\text{KJ}}{\text{kg·K}}$$

$$h_{f_1} := 167.57 \frac{KJ}{kg}$$

$$h_{fg\_1} := 2406.7 \frac{kJ}{kg}$$

$$s_1 := s_{f 1}$$

$$h_1 := h_{f,1}$$

properties p = 3 Mpa

### state 2: pump outlet - reversible

assume  $v_f = v_1$  constant, isentropic, ds = 0 => T\*ds= 0 => h2 = h1+v1\*dp from relationships Tds = dh + v\*dp integrated with constant v and Tds = 0

$$s_{2s} := s_1$$

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$$\begin{aligned} p_2 &:= 30 \text{bar} & h_{2s} &:= h_1 + v_1 \cdot \left( p_2 - p_1 \right) & h_{2s} &= 170.586 \, \frac{kJ}{kg} \\ w_{ps} &:= h_1 - h_{2s} & w_{ps} &= -3.016 \, \frac{kJ}{kg} \end{aligned}$$

calc of T in earlier version incorrect see VW&S 5.18 with C = 4.184 kJ/(kg\*K)Table A.7

using  $C_p = C_p := 4.184 \frac{kJ}{kg} = \frac{kJ}{kg \cdot K}$  actual units

and ... eqn 5.18  $h_2 - h_1 = Cp \cdot (T_2 - T_1)$ 

@ T = 40 C and ... eqn 5.18 
$$h_2 - h_1 = Cp \cdot (T_2 - T_1)$$
  $p = 3 \text{ MPa}$ 

$$h_{22s} := 170.21 \cdot \frac{kJ}{kg}$$
  $h_{2s} = 170.586 \frac{kJ}{kg}$   $T_{22} := 40$   $T_{2s} := T_{22} + \frac{h_{2s} - h_{22s}}{Cp}$   $T_{2s} = 40.09$ 

#### state 2: pump outlet - irreversible

pump efficiency ... 
$$\eta_p = \frac{\text{reversible\_}\Delta h}{\text{actual\_}\Delta h} = \frac{h_1 - h_{2s}}{h_1 - h_2} \qquad h_{2s} = h_1 + v_1 \cdot \left(p_2 - p_1\right) \qquad \eta_p := 0.9$$

$$\begin{split} h_2 &:= h_1 + \frac{v_1 \cdot \left(p_2 - p_1\right)}{\eta_p} & h_2 = 170.921 \, \frac{kJ}{kg} & w_p := h_1 - h_2 & w_p = -3.351 \, \frac{kJ}{kg} \\ T_2 &:= T_1 + \frac{h_2 - h_1}{Cp} & T_2 = 40.801 \end{split}$$

@ T = 40 C and ... eqn 5.18 
$$p = 3 \text{ MPa}$$
  $p_2 = 3 \text{ MPa}$   $p_2 = 3 \text{ MPa}$ 

$$h_{22} := 170.21 \cdot \frac{kJ}{kg}$$
  $h_2 = 170.921 \cdot \frac{kJ}{kg}$   $T_{22} := 40$   $T_{22} := T_{22} + \frac{h_2 - h_{22}}{Cp}$   $T_2 = 40.17$ 

find s from  $p = p_2$ ,  $h = h_2$ : interpolate from tbl\_2\_3MPa row 2 (index 1)

#### interpolation details

$$data = \begin{pmatrix} 40 & 0.571 & 170.21 \\ 80 & 1.073 & 337.26 \end{pmatrix}$$
 input = h<sub>2</sub> w/o units input = 170.921

interpolate for 
$$s_2$$
 and  $T_2$   $s_2 = 0.573 \, \frac{1}{K} \, \frac{kJ}{kg}$   $T_{int} = 40.17$  N.B. different from  $T_2$  above ?? granularity; investigating

summary ..

$$T_{2s} = 170.586 \frac{kJ}{kg}$$
  $T_{2s} = 40.0$ 

$$\begin{array}{lll} \text{reversible ...} & & \text{$h_{2s} = 170.586 \, \frac{kJ}{kg}$} & & \text{$T_{2s} = 40.09$} & & \text{$s_{2s} = 0.572 \, \frac{1}{K} \, \frac{kJ}{kg}$} & & \text{$w_{ps} = -3.016 \, \frac{kJ}{kg}$} \\ \end{array}$$

$$\text{irreversible ...} \qquad h_2 = 170.921 \, \frac{kJ}{kg} \qquad T_2 = 40.17 \qquad \qquad s_2 = 0.573 \, \frac{1}{K} \, \frac{kJ}{kg} \qquad \qquad w_p = -3.351 \, \frac{kJ}{kg}$$

state 3: boiler outlet same as reversible

$$p_3 := p_2$$
  $T_3 := 460$   $p_3 = 3 \text{ MPa}$   $h_3 := 3366.5 \frac{kJ}{kg}$   $s_3 := 7.113 \frac{kJ}{kg \cdot K}$ 

from interpolation Table A.1.3 P=3MPa page 622 interpolation\_class\_example.mcd

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#### state 4: turbine outlet -reversible

isentropic expansion to 40 deg C  $s_{4s} := s_3$ determine h₄ from x

$$s_{4s} := s_3$$

$$s_4 = s_{f_1} + x \cdot s_{fg_1}$$

$$s_4 = s_{f_1} + x \cdot s_{fg_1}$$
 =>  $x_s := \frac{s_{4s} - s_{f_1}}{s_{fg_1}}$   $x_s = 0.851$ 

$$\mathsf{h}_{4s} \coloneqq \mathsf{h}_{f\_1} + \mathsf{h}_{fg\_1} \cdot \mathsf{xs}$$

$$h_{4s} = 2216 \frac{kJ}{kg}$$
  $w_{ts} := h_3 - h_{4s}$ 

$$\mathbf{w}_{ts} \coloneqq \mathbf{h}_3 - \mathbf{h}_4$$

$$w_{ts} = 1151 \frac{kJ}{kg}$$
  $T_{4s} := 40$ 

$$T_{4s} := 40$$

#### state 4: turbine outlet - irreversible

same temperature

$$T_A := 40$$

$$\eta_t = \frac{\text{actual\_enthalpy\_change}}{\text{reversible\_enthalpy\_change}} = \frac{h_3 - h_4}{h_3 - h_{4s}}$$
 
$$h_4 = h_3 - \eta_t \cdot \left(h_3 - h_{4s}\right)$$
 
$$\eta_t \coloneqq 0.9$$

$$h_4 = h_3 - \eta_t \cdot (h_3 - h_{4s})$$

$$n_{+} := 0.9$$

$$h_4 := h_3 - \eta_t \cdot (h_3 - h_{4s})$$
  $h_4 = 2331.034 \frac{kJ}{kg}$ 

$$h_4 = 2331.034 \frac{kJ}{kg}$$

$$\mathbf{w}_{t} := \mathbf{w}_{ts} \cdot \mathbf{\eta}_{t}$$

$$\text{work of turbine} \qquad w_t \coloneqq w_{ts} \cdot \eta_p \qquad \qquad w_t = 1035.466 \\ \frac{kJ}{kg} \qquad \text{or } \dots \qquad \qquad w_{tv} \coloneqq h_3 - h_4 \qquad w_t = 1035.466 \\ \frac{kJ}{kg} \qquad \text{or } \dots \qquad \qquad w_{tv} \coloneqq h_3 - h_4 \qquad w_t = 1035.466 \\ \frac{kJ}{kg} \qquad \text{or } \dots = 1035.466 \\ \frac{kJ}{kg} \qquad \text{or } \dots$$

$$w_t = h_3 - h_3$$

$$w_t = 1035.466 \frac{kJ}{kg}$$

now calculate x should be > xs see plot below

$$h_4 = h_{f_1} + h_{fg_1} \cdot x$$

$$h_4 = h_{f_1} + h_{fg_1} \cdot x$$
  $x := \frac{h_4 - h_{f_1}}{h_{fg_1}}$   $x = 0.899$ 

$$x = 0.899$$

$$s_4 := s_{f_1} + x \cdot s_{fg_1}$$
  $s_4 = 7.48 \frac{1}{K} \frac{kJ}{kg}$ 

$$s_4 = 7.48 \frac{1}{K} \frac{kJ}{kg}$$

summary ..

$$h_{4s} = 2215.982 \frac{kJ}{kg}$$

y .. 
$$reversible ... \qquad h_{4s} = 2215.982 \, \frac{kJ}{kg} \qquad T_{4s} = 40 \qquad \qquad s_{4s} = 7.113 \, \frac{1}{K} \, \frac{kJ}{kg} \qquad \qquad w_{ts} = 1150.518 \, \frac{kJ}{kg}$$

$$w_{ts} = 1150.518 \frac{kJ}{kg}$$

irreversible ...

$$h_4 = 2331.034 \frac{kJ}{kg}$$
  $T_4 = 40$   $s_4 = 7.48 \frac{1}{K} \frac{kJ}{kg}$   $w_t = 1035.466 \frac{kJ}{kg}$ 

$$s_4 = 7.48 \frac{1}{K} \frac{kJ}{kg}$$

$$w_t = 1035.466 \frac{kJ}{kg}$$

# thermal efficiency - reversible

$$\eta_{th} = \frac{\text{work\_net}}{Q_H} = \frac{Q_H + Q_L}{Q_H} = \frac{w_t + w_p}{Q_H} = \frac{(h_3 - h_4) + (h_1 - h_2)}{h_3 - h_2}$$

$$\eta_{ths} := \frac{\left(h_3 - h_{4s}\right) + \left(h_1 - h_{2s}\right)}{h_3 - h_{2s}}$$
 $\eta_{ths} = 0.359$ 

$$\eta_{ths} = 0.359$$

$$\eta_{ths} = 0.359$$

$$\mathrm{Q}_{Hs} \coloneqq \, \mathrm{h}_3 \, - \, \mathrm{h}_{2s}$$

$$Q_{Ls} := h_1 - h_{4s}$$

$$\eta_{th_{-1}s} := \frac{Q_{Hs} + Q_{Ls}}{Q_{Hs}}$$
 $\eta_{th_{-1}s} = 0.359$ 

$$\eta_{th_{1s}} = 0.359$$

# thermal efficiency - irreversible

$$\eta_{th} \coloneqq \frac{\left(\mathtt{h}_3 - \mathtt{h}_4\right) + \left(\mathtt{h}_1 - \mathtt{h}_2\right)}{\mathtt{h}_3 - \mathtt{h}_2}$$

$$\eta_{th} = 0.323$$

$$\eta_{th} = 0.323 \qquad \qquad \eta_{th} = \frac{w_t + w_p}{h_3 - h_2}$$

$$\eta_{th} = 0.323$$

$$Q_H \coloneqq \mathbf{h}_3 - \mathbf{h}_2 \qquad \qquad Q_L \coloneqq \mathbf{h}_1 - \mathbf{h}_4$$

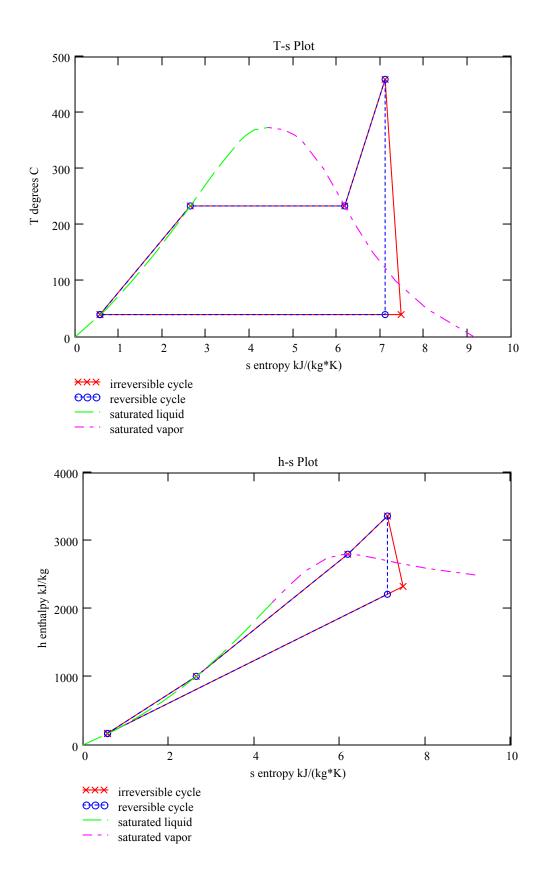
$$Q_L := h_1 - h_2$$

$$\eta_{th\_1} \coloneqq \frac{Q_H + Q_L}{Q_{tr}}$$

$$\eta_{th 1} = 0.323$$

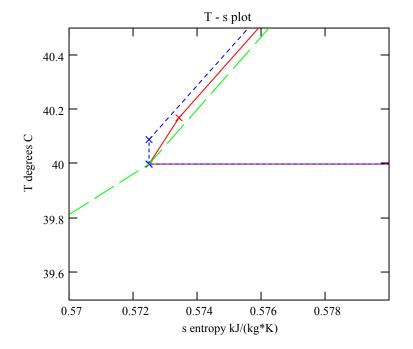
- data for saturation curve
- data for T s and H s plots

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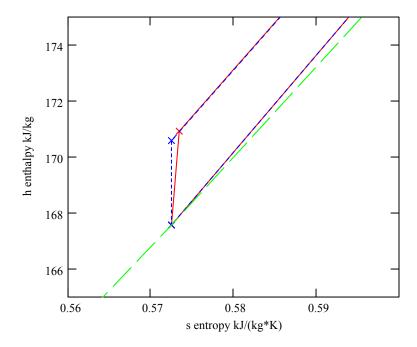


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#### close up of points 1 and 2



much expanded ref: class example scale 39.5 < T < 40.50.57 < s < 0.58



much expanded ref: class example scale 165 < h < 175 0.56 < s < 0.6

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