3.012 Fund of Mat Sci: Bonding – Lecture 7 ALPHABET SOVP

Photograph of a bowl of alphabet soup removed for copyright reasons.

Homework for Wed Oct 5

- Study: 21.5, 21.6
- Read: 17.2 (Stern-Gerlach)
- Non-graded PS3 will be posted today

Last time:

1. Hamiltonian in a spherical potential:

$$\hat{H} = -\frac{\hbar^2}{2m_e} \frac{1}{r^2} \frac{d}{dr} \left(r^2 \frac{d}{dr} \right) + \frac{L^2}{2m_e r^2} + V(r)$$

- 2. \hat{H} , \hat{L}^2 , and \hat{L}_z all commute with each other
- 3. We can find common eigenfunctions

$$\psi_{nlm}(\vec{r}) = R_{nl}(r)Y_{lm}(\vartheta,\varphi)$$

labeled with the 3 quantum numbers *n*, *l*, *m*

Three Quantum Numbers

• $\hat{H} \leftrightarrow$ Principal quantum number **n** (energy, accidental degeneracy)

$$E_n = -\frac{e^2}{8\pi\varepsilon_0} \frac{Z^2}{a_0 n^2} = -(13.6058 \text{ eV}) \frac{Z^2}{n^2} = -(1 \text{ Ry}) \frac{Z^2}{n^2}$$

- $\hat{L}^2 \leftrightarrow$ Angular momentum quantum number l l = 0,1,...,n-1 (a.k.a. s, p, d... orbitals)
- $\hat{L}_z \leftrightarrow$ Magnetic quantum number mm = -l, -l+1, ..., l-1, l

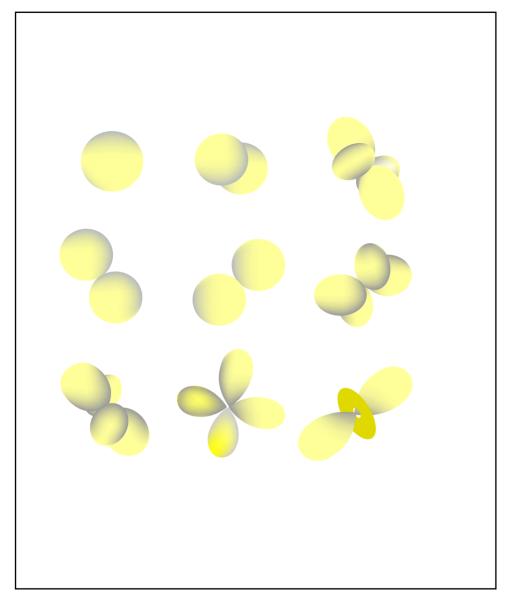


Figure by MIT OCW.

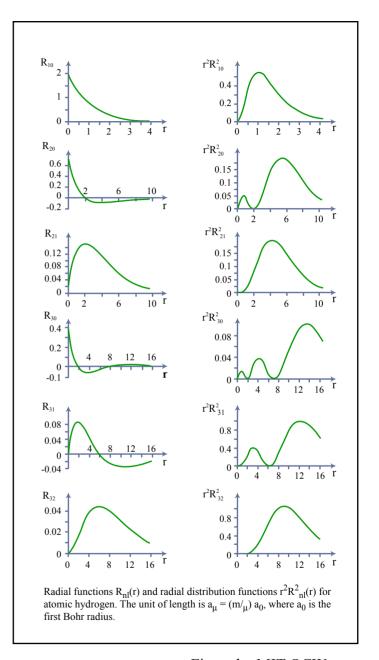
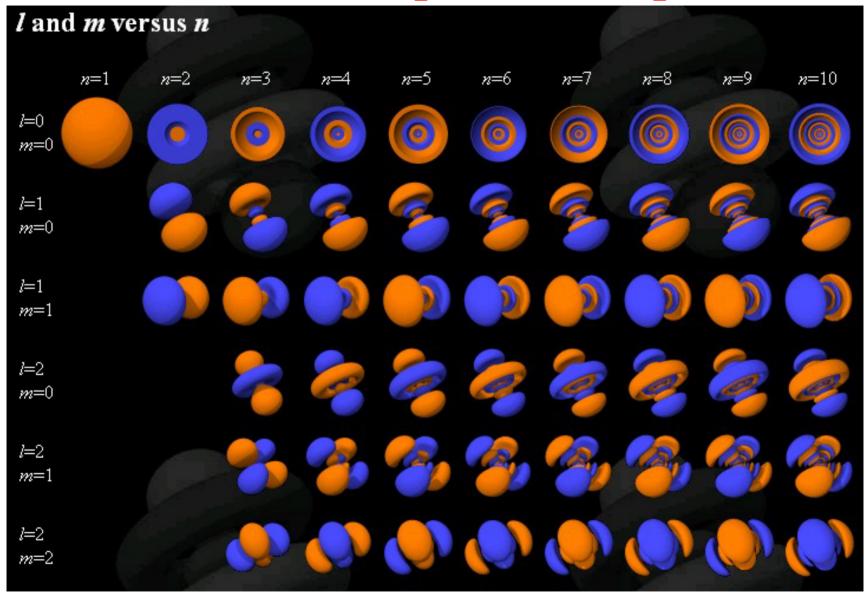


Figure by MIT OCW.

The Full Alphabet Soup



Courtesy of David Manthey. Used with permission. Source: http://www.orbitals.com/orb/orbtable.htm

Orbital levels in hydrogenoid atoms

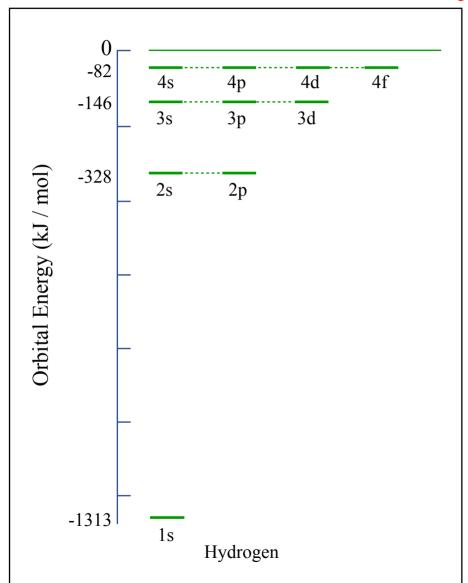
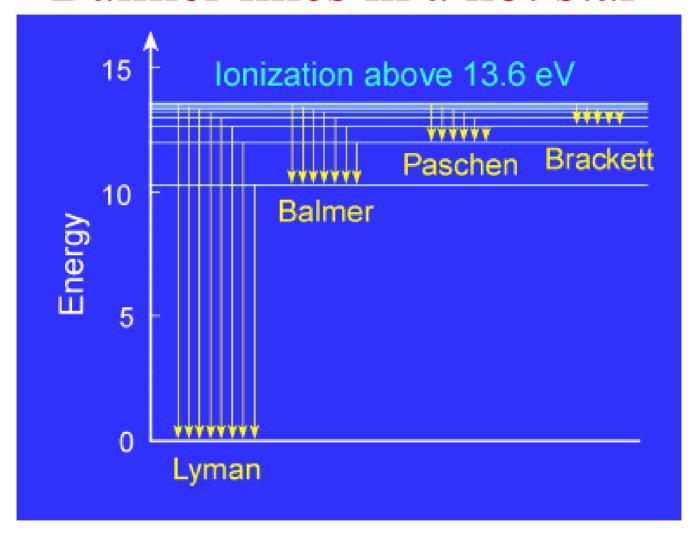


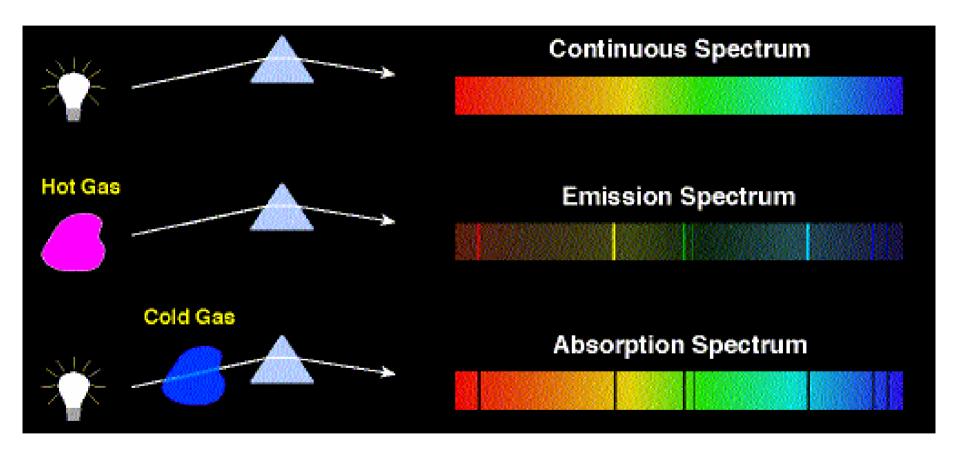
Figure by MIT OCW.

Balmer lines in a hot star



Courtesy of the Department of Physics and Astronomy at the University of Tennessee. Used with permission.

Emission and absorption lines



Courtesy of the Department of Physics and Astronomy at the University of Tennessee. Used with permission.

XPS in Condensed Matter

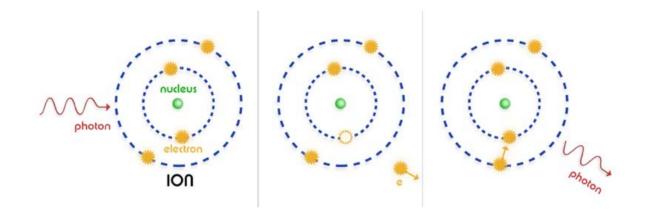
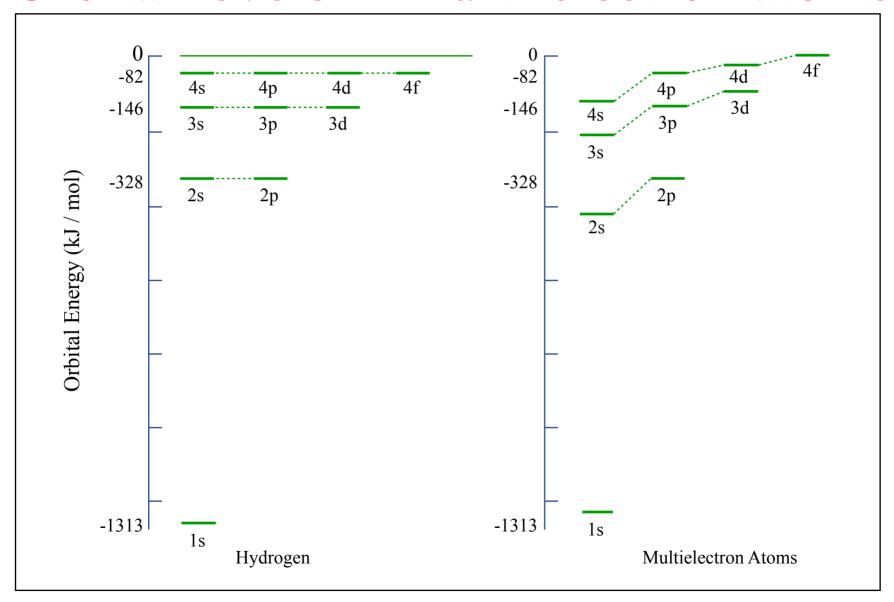


Diagram of Moon composition as seen in X-rays removed for copyright reasons.

Composition Analysis

Images of X-Ray element maps of mine waste soil particles removed for copyright reasons.

Orbital levels in multi-electron atoms



(I) "Centripetal" repulsion

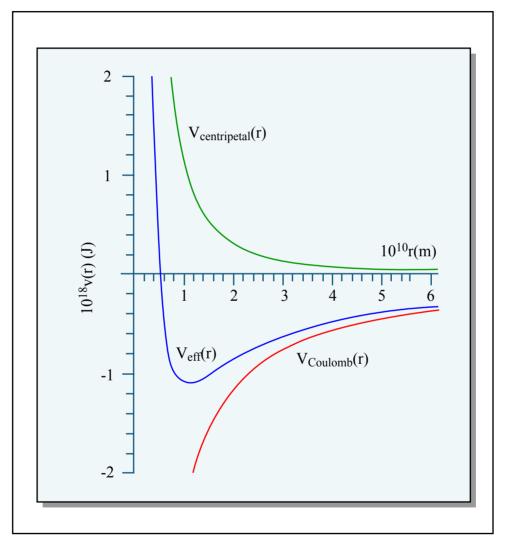


Figure by MIT OCW.

(II) Screening

(III) Screening

Stern-Gerlach Experiment

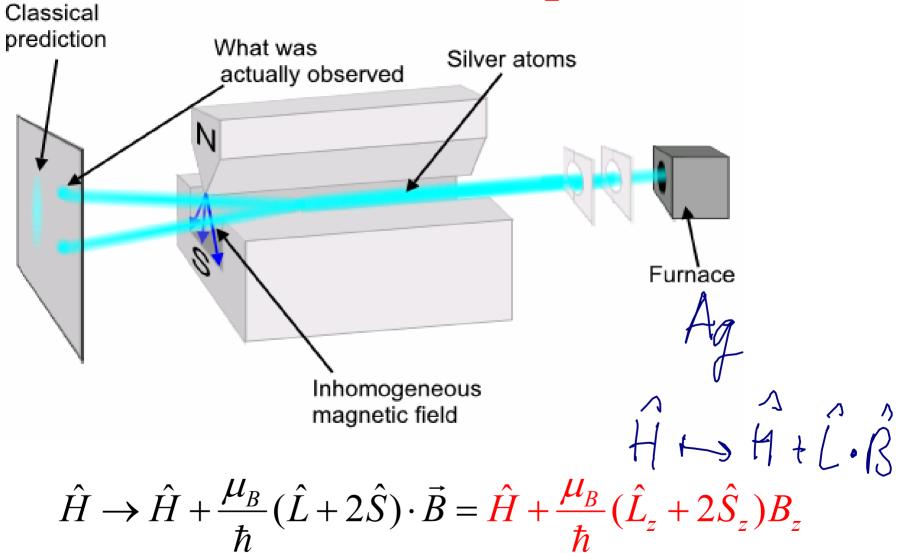


Image courtesy of Theresa Knott.

Goudsmit and Uhlenbeck

Spin

- Dirac derived the relativistic extension of Schrödinger's equation; for a free particle he found two independent solutions for a given energy
- There is an operator (spin S) that commutes with the Hamiltonian and that can only have two eigenvalues
- In a magnetic field, the spin combines with the angular momentum, and they couple via

$$\hat{H} \rightarrow \hat{H} + \frac{\mu_B}{\hbar} (\hat{L} + 2\hat{S}) \cdot \vec{B}$$

Spin Eigenvalues/Eigenfunctions

• Norm (s integer \rightarrow bosons, half-integer \rightarrow fermions)

$$\hat{S}^2 \Psi_{spin} = \hbar^2 s \left(s + 1 \right) \Psi_{spin}$$

• Z-axis projection (electron is a fermion with s=1/2)

$$\hat{S}_z \Psi_{spin} = \pm \frac{\hbar}{2} \Psi_{spin}$$

• Spin-orbital: product of the "space" wavefunction and the "spin" wavefunction