

# FAMNet: Joint Learning of Feature, Affinity and Multi-dimensional Assignment for Online Multiple Object Tracking

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## Abstract

*Data association-based multiple object tracking (MOT) involves multiple separated modules processed or optimized differently, which results in complex method design and requires non-trivial tuning of parameters. In this paper, we present an end-to-end model, named FAMNet, where Feature extraction, Affinity estimation and Multi-dimensional assignment are refined in a single network. All layers in FAMNet are designed differentiable thus can be optimized jointly to learn the discriminative features and higher-order affinity model for robust MOT, which is supervised by the loss directly from the assignment ground truth. In addition, we integrate single object tracking technique and a dedicated target management scheme into the FAMNet-based tracking system to further recover false negatives and inhibit noisy target candidates generated by the external detector. The proposed method is evaluated on a diverse set of benchmarks including MOT2015, MOT2017, KITTI-Car and UA-DETRAC, and achieves promising performance on all of them in comparison with state-of-the-arts.*

## 1. Introduction

Tracking multiple objects in videos is critical for many applications, ranging from vision-based surveillance to autonomous driving. A current popular framework to solve multiple object tracking (MOT) uses the tracking-by-detection strategy where target candidates generated from an external detector are associated and connected to form the target trajectories across frames [1, 15, 22, 35, 38, 49, 52, 54]. At the core of tracking-by-detection strategy lies the data association problem, which is usually treated as three separate parts: *feature extraction* for candidate representation, *affinity metric* to evaluate the reliability of each association hypothesis and *association algorithm* to find the optimal association. These parts involve multiple individual data-processing steps and are optimized differently from

each other, which results in a complex method design and extensive tuning parameters to adapt different target categories and tracking scenarios.

Recently, deep neural network (DNN) has been investigated intensively to learn the association cost function in a unified architecture combining both feature extraction and affinity metric [11, 27, 46]. Through training, the task and scenario prior can be automatically adapted by the candidate representation and estimation metric without manually tuning the hyper-parameters. However, the association algorithm still stands outside the network, which requires dedicated affinity samples to be manually fabricated from ground truth association for the training process. It is not guaranteed that training and inference phases share the same data distribution; consequently it may lead to the degraded generalizability of the trained model. Moreover, crowded targets, similar appearance and fast motion impose great ambiguity for the association only considering pairs of neighboring frames. Successful association requires global optimization across multiple frames, where higher-order discriminative clues such as appearance changes over time and motion context could be included. Learning the robust representation and affinity criteria without the cooperation from the association procedure in this circumstance is even more complicated.

Our objective in this paper is to formulate an end-to-end model for MOT: the Feature representation, Affinity model and Multi-dimensional assignment (MDA) are refined in a single deep network named FAMNet, which is optimized jointly to learn the task prior. In particular, *feature sub-network* is used to extract features for candidates on each frame, after which an *affinity sub-network* estimates the higher-order affinity for all association hypothesis. With the affinity, the *MDA sub-network* is to optimize globally and obtain the optimal assignments. By all layers in FAMNet designed differentiable, the feature and affinity sub-network can be trained directly referring to the assignment ground truth. To realize it, we make the following novel contributions in the FAMNet-based tracking system:

- We design an affinity sub-network that fuses discrim-

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FAMNet-based tracking system (overview in Fig. 1).

### 3.1. Problem Formulation

Following the notation in [44], the input for MOT is denoted by  $\mathbb{O} = \{\mathbb{O}^{(k)}\}_{k=0}^K$ , which contains  $K + 1$  target candidate sets from  $K + 1$  frames. For frame  $k$ ,  $\mathbb{O}^{(k)} = \{\mathbf{o}_{i_k}^{(k)}\}_{i_k=1}^{I_k}$  is the set of  $I_k$  candidates to be matched or associated, where  $\mathbf{o}_{i_k}^{(k)}$  represents the status of the candidate such as its center coordinate on the image frame.

With the input candidate set  $\mathbb{O}$ , MOT is to find a multi-dimensional association that maximizes the overall affinity subject to the association constraints. In detail,  $c_{i_0:i_K} \doteq c_{i_0 i_1 \dots i_K} \geq 0$  denotes affinity for one possible association, or in term of MOT, one hypothesis trajectory  $\mathbf{t}_{i_0:i_K}$  composed by candidates  $\{\mathbf{o}_{i_0}^{(0)}, \mathbf{o}_{i_1}^{(1)}, \dots, \mathbf{o}_{i_K}^{(K)}\}$ . We use  $z_{i_0:i_K} \doteq z_{i_0 i_1 \dots i_K}$  to indicate whether a hypothesis trajectory is true ( $z_{i_0:i_K} = 1$ ) or not ( $z_{i_0:i_K} = 0$ ). If we further denote tensor  $\mathcal{C} = (c_{i_0:i_K})$  and  $\mathcal{Z} = (z_{i_0:i_K})$ , MOT can be formulated as following MDA problem to solve  $\mathcal{Z}$  given  $\mathcal{C}$ :

$$\arg \max_{\{z_{i_0:i_K}\}} \sum_{i_0:i_K} c_{i_0:i_K} z_{i_0:i_K} = \arg \max_{\mathcal{Z}} \|\mathcal{C} \circ \mathcal{Z}\|_1, \quad (1)$$

$$\text{s.t.} \begin{cases} \sum_{i_0:i_K / \{i_k\}} z_{i_0:i_K} = 1, & \forall k = 0, 1, \dots, K \\ z_{i_0:i_K} \in \{0, 1\}, & \forall i_k = 1, 2, \dots, I_k \end{cases} \quad (2)$$

where  $\circ$  denotes the element-wise product,  $\|\cdot\|_1$  is the matrix 1-norm, and  $\sum_{i_0:i_K / \{i_k\}}$  stands for summation over all subscripts  $i_0 : i_K$  except for  $i_k$ .

To solve Eq. 1, we follow the Rank-1 Tensor Approximation (R1TA) framework [44]. The multi-dimensional assignments  $\mathcal{Z}$  are first decomposed as the product of a series of local assignments  $\mathbf{X}^{(k)} = (x_{i_{k-1}i_k}^{(k)})$  which represent the assignments between candidates in adjacent frames, i.e.  $\mathbb{O}^{(k-1)}$  and  $\mathbb{O}^{(k)}$ . If we further rewrite the local assignment matrix into vector form  $\mathbf{x}^{(k)} = (x_{j_k}^{(k)})$  where  $j_k = (i_{k-1} - 1) \times I_k + i_k$ ,<sup>1</sup> optimization problem defined in Eq. 1 can be rewritten as follow:

$$\arg \max_{\mathbb{X}} \mathcal{A} \times_1 \mathbf{x}^{(1)} \times_2 \mathbf{x}^{(2)} \dots \times_K \mathbf{x}^{(K)}, \quad (3)$$

where  $\mathcal{A} = (a_{j_1:j_K})$  is the reshaped affinity tensor from the  $(K + 1)$ -th order tensor to a  $K$ -th order tensor following the rules defined in [44] and  $\times_k$  is the  $k$ -mode tensor product,  $\mathbb{X} = \{\mathbf{x}^{(1)}, \mathbf{x}^{(2)}, \dots, \mathbf{x}^{(K)}\}$  is the set of local assignment vectors which we are optimizing for.

### 3.2. Architecture Overview and Tracking Pipeline

For each association batch, the FAMNet based tracking system takes the  $K + 1$  image frames and corresponding detections provided by an external detector as input. Detection

<sup>1</sup>For notational convenience, the same symbol is used for elements in  $\mathbf{X}^{(k)}$  and  $\mathbf{x}^{(k)}$  with double subscripts and a single subscript respectively.

candidates are first used to generate the hypothesis trajectories. Image patches of target candidates together with the trajectory hypothesis are passed into FAMNet to compute the set of local assignments as shown in Fig. 1. Inside FAMNet, features of candidate patches are extracted through a feature sub-network. The affinity sub-network then calculates the affinity for all hypothesis trajectories on those features to form the affinity tensor as described in Sec. 4.1. With the affinity tensor, the optimal multi-dimension assignments are estimated by the MDA sub-network as explained in Sec. 4.2 and 4.3.

During training, the assignment ground truth is directly compared with the network output to compute the loss. The loss signal then back-propagates throughout the network to the feature and affinity sub-networks for learning, which is illustrated as the red paths in Fig. 1 and detailed in Sec. 4.4. In tracking phase, the output assignments together with single object tracking (SOT) predictions are used to update the trajectories of tracked targets through the target management scheme as described in Sec. 4.5 and 4.6.

We design our method in the online tracking framework intended for more casual applications. Under the constant velocity assumption, three frames are the minimum temporal span to calculate the motion affinity. Therefore, in the rest of paper,  $K = 2$  with two frames overlapping between association batches is used to balance the computation cost and the sufficient depth of association to include the higher-order discriminative clues.

## 4. FAMNet

### 4.1. Affinity Sub-Network

The affinity sub-network takes the features of candidates and hypothesis trajectories as input, and generates the affinity tensor as output.

For each association batch, the feature sub-network, which is a Siamese-style network, is first used to extract spatially aligned feature for the candidates from all frames in the batch. The candidates in the middle frame of the batch are treated as anchor candidates, and the middle frame is referred as anchor frame. E.g., for  $K = 2$ , the anchor frame refers to the frame  $k = 1$ . For each anchor candidate  $\mathbf{o}_{i_1}^{(1)}$ , three features are extracted respectively from the three frames, denoted as  $\mathbb{F}_{i_1} = \{\mathbf{f}_{i_1}^{(0)}, \mathbf{f}_{i_1}^{(1)}, \mathbf{f}_{i_1}^{(2)}\}$ . These features are all centered at the same location of  $\mathbf{o}_{i_1}^{(1)}$  on frame  $k = 1$ , as illustrated on the left of Fig. 2. This way, features in  $\mathbb{F}_{i_1}$  share the same coordinate origin thus can encode motion clue when concatenated along a channel. Spatial dimension of  $\mathbf{f}_{i_1}^{(1)}$  is determined by the bounding box of  $\mathbf{o}_{i_1}^{(1)}$ , while others are the multiples of  $\mathbf{f}_{i_1}^{(1)}$  in order to include enough candidates on adjacent frames into the same view. Note that, hypothesis trajectories sharing the same anchor candi-

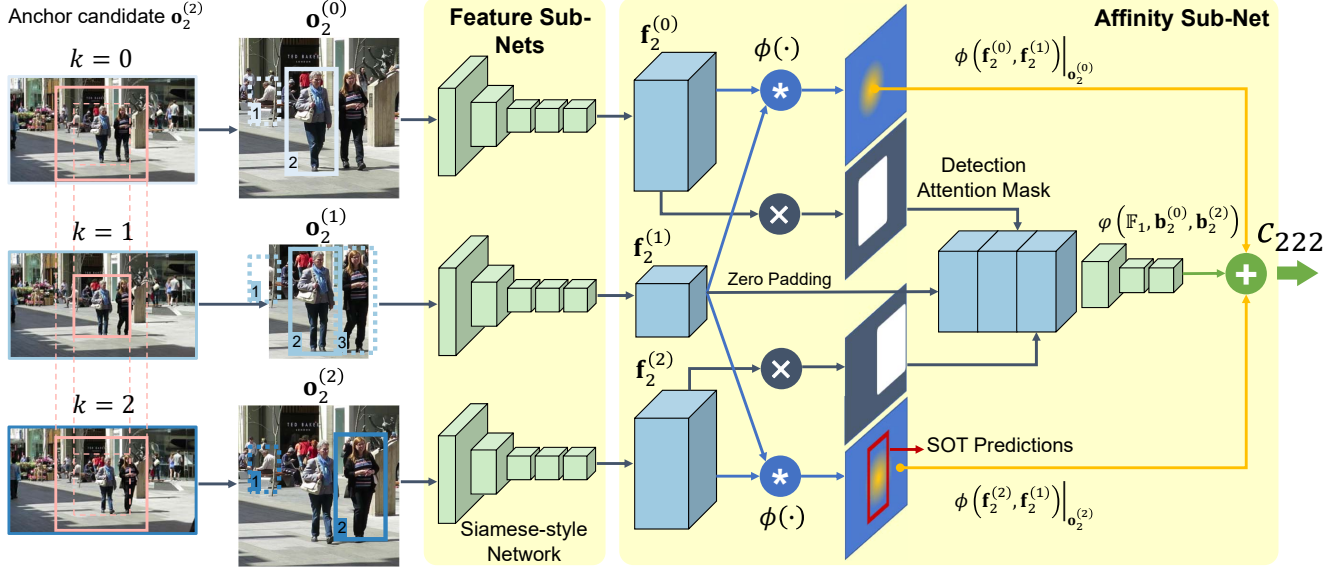


Figure 2. Illustration of the feature and affinity sub-networks for  $K = 2$ . It shows an example to calculate the affinity  $c_{222}$  for the hypothesis trajectory  $\mathbf{t}_{222}$ . The red bounding boxes in the first column of images indicate the locations on the image frame for the patch in the second column. The blue bounding boxes in the second column illustrate the detection candidates. Best viewed in color.

date have the same set of  $\mathbb{F}_{i_1}$ . Therefore,  $3I_1$  features are extracted for each association batch.

Two levels of affinities are calculated for each hypothesis trajectory using the extracted feature set, as shown in Fig. 2. In detail, the affinity tensor is calculated as following:

$$c_{i_0 i_1 i_2} = \begin{cases} \varphi(\mathbb{F}_{i_1}, \mathbf{b}_{i_0}^{(0)}, \mathbf{b}_{i_2}^{(2)}) \\ + \phi(\mathbf{f}_{i_1}^{(0)}|_{\mathbf{o}_{i_0}^{(0)}}, \mathbf{f}_{i_1}^{(1)}) & \mathbf{t}_{i_0 i_1 i_2} \in \mathbb{T} \\ + \phi(\mathbf{f}_{i_1}^{(2)}|_{\mathbf{o}_{i_2}^{(2)}}, \mathbf{f}_{i_1}^{(1)}), & \\ 0, & \mathbf{t}_{i_0 i_1 i_2} \notin \mathbb{T}, \end{cases} \quad (4)$$

where  $\mathbb{T}$  is the set of valid hypothesis trajectories,  $\mathbf{b}_{i_k}^{(k)}$  is the bounding box associated with  $\mathbf{o}_{i_k}^{(k)}$ ,  $\phi(\cdot)$  calculates the pair-wise affinity and  $\varphi(\cdot)$  evaluates the long-term affinity of a hypothesis trajectory,  $\mathbf{f}_{i_1}^{(0)}|_{\mathbf{o}_{i_0}^{(0)}}$  is a spatial subset of  $\mathbf{f}_{i_1}^{(0)}$  centered at  $\mathbf{o}_{i_0}^{(0)}$  with the same spatial dimension as  $\mathbf{f}_{i_1}^{(1)}$ . The actual center coordinates of  $\mathbf{o}_{i_0}^{(0)}$  in  $\mathbf{f}_{i_1}^{(0)}$  need to be converted accordingly. We use  $\mathbf{o}_{i_0}^{(0)}$  here for convenience.

For pair-wise affinity, the cross-correlation operation is used, such as

$$\phi(\mathbf{f}_{i_1}^{(0)}|_{\mathbf{o}_{i_0}^{(0)}}, \mathbf{f}_{i_1}^{(1)}) = \mathbf{f}_{i_1}^{(1)} * \mathbf{f}_{i_1}^{(0)}|_{\mathbf{o}_{i_0}^{(0)}} = \phi(\mathbf{f}_{i_1}^{(0)}, \mathbf{f}_{i_1}^{(1)})|_{\mathbf{o}_{i_0}^{(0)}}, \quad (5)$$

where  $*$  is the convolution operation. Due to the fact that hypothesis trajectories sharing the same anchor candidates have the same set of  $\mathbb{F}_{i_1}$ , we can calculate  $\mathbf{f}_{i_1}^{(1)} * \mathbf{f}_{i_1}^{(0)}$  first then take the value at  $\mathbf{o}_{i_0}^{(0)}$  from the cross-correlation result,

which is referred as  $\phi(\cdot)|_{\mathbf{o}_{i_0}^{(0)}}$ .

We use convolutional neural network (CNN) with spatial attention to evaluate the higher-order affinity of hypothesis trajectory. For this purpose, features  $\mathbf{f}_{i_1}^{(0)}$  and  $\mathbf{f}_{i_1}^{(2)}$  are multiplied with spatial masks generated from  $\mathbf{b}_{i_0}^{(0)}$  and  $\mathbf{b}_{i_2}^{(2)}$  as shown in Fig. 2. In particular, we create a binary mask of the same spatial size with  $\mathbf{f}_{i_1}^{(0)}$  or  $\mathbf{f}_{i_1}^{(2)}$  for each candidate. Inside each mask, the region within  $\mathbf{b}_{i_k}^{(k)}$  is set to 1 otherwise is 0. Each time, the actual position of  $\mathbf{b}_{i_k}^{(k)}$  in the mask is converted from the image frame to the coordinates centered at anchor candidates. After encoding the spatial-temporal information, features in  $\mathbb{F}_{i_1}$  are concatenated along channel to form the input of a CNN to estimate the long-term affinity. The final affinity for a hypothesis trajectory is the summation of two levels of affinity according to Eq. 4.

## 4.2. R1TA Power Iteration Layer

With the affinity tensor, we use R1TA power iteration to estimate the set of optimal assignments in Eq. 3. Solving the global optimum for MDA often requires NP-hard probing. A sub-optimal approximation is usually guaranteed by a power iteration algorithm which can be expressed in the pure mathematic format.

In order to fit this process into the deep network framework, we adapt a different iteration scheme than the one in [44] where the row/column  $\ell_1$  normalization is applied to  $\mathbb{X}$  after each iteration to enforce the constrain defined in Eq. 2. The tensor power iteration and row/column normalization are separated into two independent layers in our de-



sign. It avoids cumulating too deep operations in a single layer and alleviate the potential gradient vanishing. Downside of this scheme is that we **could not expect the same convergence property** as in [44]. However, benefited from the end-to-end training, it can be compensated by the learned more discriminative feature and affinity metric.

In detail, the optimal solution to Eq. 3 subject to Eq. 2 is approximated iteratively by:

**Forward pass.** At the  $(n + 1)$ -th iteration, the elements in  $\mathbf{x}^{(1)(n+1)}$  is calculated from<sup>2</sup>

$$x_{j_1}^{(1)(n+1)} = \frac{x_{j_1}^{(1)(n)}}{C^{(n)}} \sum_{j_2} a_{j_1 j_2} x_{j_2}^{(2)(n)}, \quad (6)$$

where  $C^{(n)} = \sum_{j_1, j_2} a_{j_1 j_2} x_{j_1}^{(1)(n)} x_{j_2}^{(2)(n)}$  is the  $\ell_1$  normalization factor. At initialization, elements in all local assignment vectors  $\mathbf{x}^{(k)(0)}$  are set to 1.

**Backward pass.** The RITA power iteration layer computes the loss gradient of affinity tensor  $\mathcal{A}$ , denoted by  $\partial L / \partial a_{j_1 j_2}$ , as backward output. The input of the backward pass is the loss gradient of all local assignment vectors at the last iteration, e.g.  $\partial L / \partial \mathbf{x}^{(k)(N)}$ , where  $N$  is the total number of iterations performed in the forward pass. The gradient output is calculated as follow:

$$\begin{aligned} \frac{\partial L}{\partial a_{j_1 j_2}} &= \sum_n \frac{x_{j_1}^{(1)(n)} x_{j_2}^{(2)(n)}}{C^{(n)}} \\ &\times \sum_k (\mathbf{i}_{j_k}^{(k)} - \mathbf{x}^{(k)(n+1)})^\top \frac{\partial L}{\partial \mathbf{x}^{(k)(n+1)}}, \end{aligned} \quad (7)$$

where  $\mathbf{i}_{j_k}^{(k)}$  is a unit vector of the same dimension as  $\mathbf{x}^{(k)}$  and has elements equal to 1 only at  $j_k$  and otherwise 0. In order to calculate Eq. 7 for all iterations, the loss gradients of assignment vectors at each iteration are also needed, which follows:

$$\begin{aligned} \frac{\partial L}{\partial x_{j_1}^{(1)(n)}} &= \frac{x_{j_1}^{(1)(n+1)}}{x_{j_1}^{(1)(n)}} \left[ (\mathbf{i}_{j_1}^{(1)} - \mathbf{x}^{(1)(n+1)})^\top \frac{\partial L}{\partial \mathbf{x}^{(2)(n+1)}} \right. \\ &\quad \left. - (\mathbf{x}^{(2)(n+1)})^\top \frac{\partial L}{\partial \mathbf{x}^{(2)(n+1)}} \right] + \frac{1}{C^{(n)}} \sum_{j_2} a_{j_1 j_2} \frac{\partial L}{\partial x_{j_2}^{(2)(n)}}, \end{aligned} \quad (8)$$

### 4.3. $\ell_1$ Normalization Layer

To satisfy the constraints defined in Eq. 2 required by MDA, row/column  $\ell_1$  normalization is applied to the result  $\mathbb{X}$ . The assignment vectors from the RITA power iteration layer are reshaped back to their matrix form such that  $\mathbf{X}^{(k)} = (x_{i_{k-1} i_k}^{(k)}) \in \mathbb{R}^{I_{k-1} \times I_k}$ . Then, the  $\ell_1$  normalization

<sup>2</sup>The second superscript indicates the round of iteration. Moreover, derivation in this subsection is on  $x_{j_1}^{(1)}$ , but is the same for  $x_{j_2}^{(2)}$ .

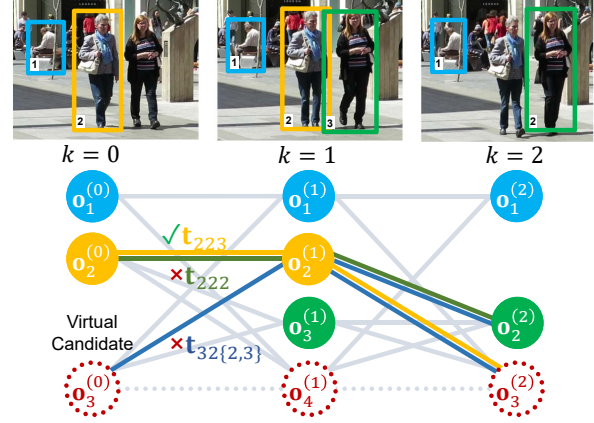


Figure 3. Hypothesis trajectory generation. It shows all hypothesis trajectories passing through candidate  $\mathbf{o}_2^{(1)}$ . The color of nodes indicates the ground truth associations.

is performed row and column alternatively through multiple iterations.

**Forward pass.** For each pair of iterations, we start from row normalization. In the  $(n + 1)$  and  $(n + 2)$ -th iteration:

$$\begin{aligned} \mathbf{X}^{(k)(n+1)} &= [\mathbf{X}^{(k)(n)} \mathbf{1}_{I_k}]^{-1} \mathbf{X}^{(k)(n)} \\ \mathbf{X}^{(k)(n+2)} &= \mathbf{X}^{(k)(n+1)} [\mathbf{1}_{I_{k-1}}^\top \mathbf{X}^{(k)(n+1)}]^{-1}, \end{aligned} \quad (9)$$

where  $\mathbf{1}_{I_k} \in \mathbb{R}^{I_k}$  is a vector with all elements being 1,  $[\mathbf{x}]$  here and below represents the diagonal matrix with  $\mathbf{x}$  as diagonal elements.

**Backward pass.** Given a starting gradient  $\partial L / \partial \mathbf{X}^{(k)(n+2)}$ , we iteratively compute the gradients as:

$$\begin{aligned} \frac{\partial L}{\partial \mathbf{X}^{(k)(n+1)}} &= \frac{\partial L}{\partial \mathbf{X}^{(k)(n+2)}} [\mathbf{1}_{I_{k-1}}^\top \mathbf{X}^{(k)(n+2)}]^{-1} - \mathbf{1}_{I_{k-1}} \\ &\quad \cdot \text{diag} \left( [\mathbf{1}_{I_{k-1}}^\top \mathbf{X}^{(k)(n+2)}]^{-2} (\mathbf{X}^{(k)(n+2)})^\top \frac{\partial L}{\partial \mathbf{X}^{(k)(n+2)}} \right)^\top \\ \frac{\partial L}{\partial \mathbf{X}^{(k)(n)}} &= [\mathbf{X}^{(k)(n+1)} \mathbf{1}_{I_k}]^{-1} \frac{\partial L}{\partial \mathbf{X}^{(k)(n+1)}} \\ &\quad - \text{diag} \left( [\mathbf{X}^{(k)(n+1)} \mathbf{1}_{I_k}]^{-2} \frac{\partial L}{\partial \mathbf{X}^{(k)(n+1)}} (\mathbf{X}^{(k)(n+1)})^\top \right) \mathbf{1}_{I_k}^\top. \end{aligned}$$

Our  $\ell_1$  normalization layer is similar to but differs from that in [59], in that our implementation allows partial row/column normalization to handle real and virtual candidates differently as detailed in Sec. 4.5.

### 4.4. Training

During the training, the total loss  $L$  is measured by the **binary cross entropy** between all predicted assignments  $(x_{i_{k-1} i_k}^{(k)} \in [0, 1])$  and assignment ground truth  $(\bar{x}_{i_{k-1} i_k}^{(k)} \in \{0, 1\})$ , which is written as

$$L = \sum_k \sum_{i_{k-1} i_k} \bar{x}_{i_{k-1} i_k}^{(k)} \log x_{i_{k-1} i_k}^{(k)} + (1 - \bar{x}_{i_{k-1} i_k}^{(k)}) \log (1 - x_{i_{k-1} i_k}^{(k)}).$$

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**Algorithm 1** Target Management

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1: Input: Assignment matrix  $\mathbf{X}^{(k)} = (x_{i_{k-1}i_k}^{(k)}) \in \mathbb{R}^{I_{k-1} \times I_k}$ .
2: Output: Tracked target trajectories.
3: Discretize  $\mathbf{X}^{(k)}$  using graph multicut [21].
4: for  $i_{k-1} = 1, \dots, I_{k-1}$  do
5:   if  $\mathbf{o}_{i_{k-1}}^{(k-1)}$  not tracked
     and  $\text{CNN}_{\text{BBE}}(\mathbf{b}_{i_{k-1}}^{(k-1)}) > 0.5$  then
6:     add new target trajectory starting with  $\mathbf{b}_{i_{k-1}}^{(k-1)}$ 
7:   end if
8:   if  $\mathbf{o}_{i_{k-1}}^{(k-1)}$  assigned to a real candidate, e.g.  $\mathbf{o}_{j_k}^{(k)}$  then
9:     if  $\text{IoU}(\mathbf{p}_{i_{k-1}}^{(k-1)}, \mathbf{b}_{j_k}^{(k)}) < t_{\text{dif}}$ 
       and  $\text{CNN}_{\text{BBE}}(\mathbf{b}_{j_k}^{(k)}) < 0.5$  then
10:      update target trajectory of  $\mathbf{o}_{i_{k-1}}^{(k-1)}$  using  $\mathbf{p}_{i_{k-1}}^{(k-1)}$ 
11:      continue
12:     end if
13:     update target trajectory of  $\mathbf{o}_{i_{k-1}}^{(k-1)}$  using  $\mathbf{b}_{j_k}^{(k)}$ 
14:   else
15:      $\triangleright \mathbf{b}_F$  is the bounding box of image frame.
16:     if  $\text{IoU}(\mathbf{p}_{i_{k-1}}^{(k-1)}, \mathbf{b}_F) < t_{\text{exit}}$  then
17:       exit target trajectory of  $\mathbf{o}_{i_{k-1}}^{(k-1)}$ 
18:     else
19:       update target trajectory of  $\mathbf{o}_{i_{k-1}}^{(k-1)}$  using  $\mathbf{p}_{i_{k-1}}^{(k-1)}$ 
20:     end if
21:   end if
22: end for
```

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With the total loss, gradients are calculated throughout the network back to the affinity and feature sub-networks.

We use each association batch containing three frames as one mini-batch during training and tracking. For each batch, three consecutive frames and target candidates on each frame provided by an external detector serve as the input. The candidate set is first used to generate the hypothesis trajectories  $\{\mathbf{t}_{i_0:i_2}\}$ . We set a **bound** for the hypothesis trajectory generation where two candidates from two consecutive frames **can be connected only when they are spatially close to each other** and have the similar bounding box size. We set **adaptive thresholds** for this strategy. In detail, if a candidate cannot connect with any candidate at a threshold, it re-searches using degraded thresholds for the possible connection. This strategy allows the connections for both fast and slow movement targets, and meanwhile rejects naive false positive connections. Hypothesis trajectories are generated **greedily** by iterating through all valid connections to form trajectories starting with candidates in  $\mathbb{O}^{(0)}$  and terminating in  $\mathbb{O}^{(2)}$ . Generated trajectories are sorted by their anchor candidates and together with image frames fed into our networks for training and tracking.

#### 4.5. Tracking by Integrating Detection and SOT

In the tracking phase, predictions using SOT techniques are included to **recover missing candidates** from the exter-

nal detector. We add a virtual candidate to each candidate set to represent missing candidates and allow it to connect with any candidate in consecutive frames as shown in Fig. 3. Both **real and virtual candidates** are used to generate trajectory hypothesis. When calculating affinity, we choose the location maximizing the affinity in Eq. 5 as the center of the virtual candidates for each anchor candidate such that

$$\arg \max_{\hat{\mathbf{o}}_{I_2+1}^{(2)}} \phi(\mathbf{f}_{i_1}^{(2)}, \mathbf{f}_{i_1}^{(1)}) = (\mathbf{f}_{i_1}^{(1)} * \mathbf{f}_{i_1}^{(2)})|_{\hat{\mathbf{o}}_{I_2+1}^{(2)}}. \quad (10)$$

Therefore, if an anchor candidate misses its detection in consecutive frame, it will connect with the virtual candidate which represents the location most similar to it in that consecutive frame, or, in terms of SOT, its tracking prediction. Each anchor candidate may have a different location predicted by SOT. We use  $\hat{\mathbf{o}}_{I_2+1}^{(2)}$  in Eq. 10 to refer to the virtual candidate, its center coordinates may vary on different anchor candidates.

To prevent MDA from always choosing the virtual candidates since their affinity are no smaller than any real candidate, a **coefficient  $\alpha \in (0, 1)$  is used to scale down their affinity**. The virtual candidates are handled specially in the  $\ell_1$  normalization layer: for the row (column) in  $\mathbf{X}^{(k)(n+1)}$  representing a virtual candidate, only column (row)  $\ell_1$  normalization is applied. This way, each real candidate can be assigned to only one candidate in consecutive frame including the virtual ones, while a **virtual candidate can be assigned to multiple candidates**. During optimization, if the affinities of real candidates are smaller than that of the virtual candidates, which represent tracking predictions, the anchor candidates will be automatically associated with the tracking prediction. This way, our tracking system integrates the detection and SOT **naturally**.

#### 4.6. Target Management

On receiving the assignment results, target management handles target entering, exiting and updating. In assignment results, if multiple anchor candidates choose to associate with a virtual candidate, new candidates will be added into candidate sets accordingly. For a virtual candidate not associated with any anchor candidate in assignment results, it will be dropped from the candidate set. Furthermore, if the virtual candidate associated with an anchor candidate in this batch appears as an anchor candidate in the next batch, the appearance feature of the anchor candidate is reused in the next batch in case that the missing detection is caused by occlusion. This SOT process will continue until a confident real candidate is associated.

For anchor candidates associated with real candidates, we train a CNN network to further refine their bounding boxes. During MDA, associations are made mainly based on the object center of each candidate. Most MOT tasks concern the actual bounding box enclosure of targets. When an anchor candidate is assigned to a real candidate, two

Table 1. Tracking Performance on the MOT2015 benchmark test set. Best in bold.

	Method	MOTA	IDF1	MT	ML↓	FP↓	FN↓	IDS↓
Offline	CEM [33]	19.3	0.0	8.5%	46.5%	14180	34591	813
	R1TA [44]	24.3	24.1	5.5%	46.6%	6664	38582	1271
	SCNN [28]	29.0	34.3	8.5%	48.4%	<b>5160</b>	37798	639
	DAM [24]	32.4	<b>45.3</b>	16.0%	43.8%	9064	32060	<b>435</b>
	JMC [22]	<b>35.6</b>	45.1	<b>23.2%</b>	<b>39.3%</b>	10580	<b>28508</b>	457
Online	RNN [32]	19.0	17.1	5.5%	45.6%	11578	36706	1490
	oICF [23]	27.1	40.5	6.4%	48.7%	7594	36757	<b>454</b>
	SCEA [56]	29.1	37.2	8.9%	47.3%	6060	36912	604
	AP [7]	38.5	<b>47.1</b>	8.7%	37.4%	<b>4005</b>	33203	586
	proposed	<b>40.6</b>	41.4	<b>12.5%</b>	<b>34.4%</b>	4678	<b>31018</b>	778

Table 2. Tracking Performance on the MOT2017 benchmark test set. Best in bold.

	Method	MOTA	IDF1	MT	ML↓	FP↓	FN↓	IDS↓
Offline	IOU17 [4]	45.5	39.4	15.7%	40.5%	19993	281643	5988
	bLSTM [25]	47.5	51.9	18.2%	41.7%	25981	268042	2069
	TLMHT [42]	50.6	<b>56.5</b>	17.6%	43.4%	<b>22213</b>	255030	<b>1407</b>
	jCC [47]	51.2	54.5	20.9%	<b>37.0%</b>	25937	247822	1802
	eHAF17 [43]	<b>51.8</b>	54.7	<b>23.4%</b>	37.9%	33212	<b>236772</b>	1843
Online	GMPhD [26]	39.6	36.6	8.8%	43.3%	50903	284228	5811
	DMAN [61]	48.2	<b>55.7</b>	<b>19.3%</b>	38.3%	26218	263608	<b>2194</b>
	MOTDT [8]	50.9	52.7	17.5%	35.7%	24069	<b>250768</b>	2474
	proposed	<b>52.0</b>	48.7	19.1%	<b>33.4%</b>	<b>14138</b>	253616	3072

bounding boxes will be associated with it: one from the real candidate itself denoted by  $\mathbf{b}_{i_k}^{(k)}$  and the other from the SOT predication of the anchor candidate  $\mathbf{p}_{i_{k-1}}^{(k-1)}$ . If the bounding box Intersection over Union (IoU) between  $\mathbf{b}_{i_k}^{(k)}$  and  $\mathbf{p}_{i_{k-1}}^{(k-1)}$  is smaller than a threshold  $t_{\text{dif}}$ , a CNN is used to evaluate the quality of  $\mathbf{b}_{i_k}^{(k)}$ . In detail, a CNN-based binary classifier  $\text{CNN}_{\text{BBE}}$  is trained to decide whether a bounding box has IoU larger than a threshold, *e.g.* 0.5, with the category target. The detailed procedure of the target management is listed in Alg. 1.

## 5. Experiment

We conduct experiments on four popular MOT datasets: MOT2015 [29] and MOT2017 [31] for pedestrian tracking, KITTI-Car [18] and UA-DETRAC [51] for vehicle tracking. All datasets are provided with referred detections from real detectors.

### 5.1. Experiment Setting

The proposed approach is implemented in PyTorch and runs on a desktop with CPU of 6 cores@3.60GHz and a Titan X GPU. We adapt the SiamFC proposed in [41] as our feature sub-network and use their weights as pre-trained model which is trained on the ILSVRC15 dataset for object detection in video. The CNN  $\varphi(\cdot)$  to estimate long-term affinity is constructed with three convolutional layers to map the concatenated spatial aligned fea-

ture into affinity score. A ResNet-101 with binary output is adapted for  $\text{CNN}_{\text{BBE}}$ , the pre-trained weights from MaskRCNN [19] on COCO dataset is used for initialization. Proposed method runs average 0.6 fps on MOT2017 dataset in tracking phase.

For each test sequence in MOT2015 and MOT2017, following their protocol, one or more similar sequences in the training set are used to **train a different set of FAMNet and  $\text{CNN}_{\text{BBE}}$  to best adapt the scenario prior.** Sequences in the **KITTI and UA-DETRAC** dataset are all recorded in a similar setting, therefore all training sequences in their datasets are used together to train one set of networks for all test sequences. To train the FAMNet, ground truth bounding boxes are used as input target candidates. Therefore, **no virtual candidate or SOT process is enabled during training.** When training the  $\text{CNN}_{\text{BBE}}$ , the training samples are collected from both the external detection and ground truth bounding box after random shift and scale. The IoU of bounding boxes with ground truth larger than 0.5 are selected as positive samples while smaller than 0.4 are for negative samples.

To evaluate the performance of the proposed method, the widely accepted CLEAR MOT metrics [2] are reported, which include multiple object tracking precision (MOTP) and multiple object tracking accuracy (MOTA) that combines false positives (FP), false negatives (FN) and the identity switches (IDS). Additionally, we also report the percentage of mostly tracked targets (MT), the percentage of mostly lost targets (ML). For MOT2015 and MOT2017, we also report the IDF1 scores [40].

### 5.2. Evaluation Results

**MOT2015.** MOT2015 [29] contains 11 different indoor and outdoor scenes of public places with pedestrians as the objects of interest, where camera motion, camera angle and imaging condition vary greatly. The dataset provides detections generated by the ACF-based detector [14]. The numerical results on its test set are reported in Tab. 1. Our approach achieves clearly the state-of-the-art performance. In particular, our method achieves better performance in most metrics than the RNN based end-to-end online methods due to our discriminative higher-order affinity and the optimization method adapted. Our method also surpasses the same R1TA-based method which is with hand-crafted features and affinity metrics.

**MOT2017.** Similar to MOT2015, MOT2017 [31] contains seven different sequences in both training and test datasets but with higher average target density (31.8 vs 10.6 on the test set), thus is more challenging. MOT2017 also focuses on evaluating the tracker performance on different detection quality. It provides three different detection inputs from DPM [17], Faster-RCNN [39] and SDP [55], ranked in ascending order by AP. We train seven different sets of net-

Table 3. Tracking Performance on the KITTI-Car benchmark test set. Best in bold.

	Method	MOTA	MOTP	MT	ML↓	FP↓	FN↓	IDS↓
Offline	DCO-X [34]	68.1	78.9	37.5%	14.1%	2588	8063	318
	RITA [44]	71.2	79.2	47.9 %	11.7%	1915	7579	418
	LP-SSVM [48]	77.6	77.8	56.3%	<b>8.5%</b>	1239	<b>6393</b>	62
	NOMT [9]	<b>78.1</b>	<b>79.5</b>	<b>57.2%</b>	13.2%	<b>1061</b>	6421	<b>31</b>
Online	RMOT [57]	65.8	75.4	40.2%	9.7 %	4148	7396	209
	mbodSSP [30]	72.7	78.8	48.8%	<b>8.7%</b>	1918	7360	<b>114</b>
	CIWT [37]	75.4	<b>79.4</b>	49.9%	10.3 %	954	7345	165
	proposed	<b>77.1</b>	78.8	<b>51.4%</b>	8.9%	<b>760</b>	<b>6998</b>	123

works according to different scenes, without further fitting on the different detections. The numerical results are reported in Tab. 2. The performance of our method is better than or on par with other published state-of-the-art methods.

**KITTI-Car.** The KITTI dataset [18] contains 21 video sequences in the training set and 29 in the test set for multiple vehicle tracking in street view, where videos are recorded through a camera mounting in front of a moving vehicle. Referred detections from the regionlet [50] detector are used in our experiment. The numerical results on the dataset of our method along with other methods using the same detections are summarized in Tab. 3. Our method again surpasses the hand-crafted feature-based RITA method, despite the fact that it uses a much larger association batch for off-line tracking. It is worth mentioning that motion affinity plays a more importance role in KITTI than in MOT2015 and MOT2017, since both targets and camera move faster and more regularly in KITTI.

**UA-DETRAC.** UA-DETRAC dataset [51] is another multiple vehicle tracking dataset with 60 sequences for training and 40 sequences for testing. All sequences are recorded with static camera at a lift-up position near different drive ways in various of weather conditions. We use referred detection from CompACT [5] detector in our experiment. UA-DETRAC reports the average of each MOT metric (PR-) from a serials of results using different detection confidence thresholds (from 0 to 1.0 with 0.1 step). Comparison with other methods using the same detections are reported in Tab. 4. Proposed method achieves state-of-the-art performance among the published works. Our method also surpasses the IOU tracker which is an offline method and using a private detector.

### 5.3. Ablation Study

We justify the effectiveness of different modules in proposed method through ablation study as shown in Tab. 5. We conduct the study using the sequences ETH-Pedcross2 and ETH-Sunnyday for testing and ETH-Bahnhof for training. All sequences are from the training set of MOT2015. We start from FAMNet with randomly initialized weights whose tracking performance is referred as “No training” in Tab. 5. Then the network is trained on sequence ETH-

Table 4. Tracking Performance on the UA-DETRAC benchmark test set. Best in bold.

Method	PR-MOTA	PR-MOTP	PR-MT	PR-ML↓	PR-FP↓	PR-FN↓	PR-IDS↓
CEM [33]	5.1	35.2	3.0%	35.3%	<b>12341</b>	260390	<b>267</b>
H <sup>2</sup> T [53]	12.4	35.7	14.8 %	19.4%	51765	173899	852
CMOT [1]	12.6	36.1	16.1%	18.6%	57886	167111	285
GOG [38]	14.2	<b>37.0</b>	13.9%	19.9%	32093	180184	3335
<sup>†</sup> IOU [4]	19.4	28.9	<b>17.7%</b>	18.4 %	14796	171806	2311
proposed	<b>19.8</b>	36.7	17.1%	<b>18.2%</b>	14989	<b>164433</b>	617

<sup>†</sup> Private detector used.

Table 5. Ablation study on sequences from MOT2015.

Method	MOTA	FP↓	FN↓	IDS↓
No training	35.5	240	4799	202
Training from scratch	44.1	281	4160	97
Without CNN <sub>BBE</sub>	40.5	518	4227	87
Without SOT	42.0	<b>200</b>	4412	99
Fine-tuning (proposed)	<b>45.2</b>	259	<b>4105</b>	<b>87</b>

Bahnhof. “Training from scratch” stands for the results in this scheme. Training with the limited MOT sequences may lead to overfitting of the feature and affinity sub-network. To increase the generalizability and further boost the performance, we use the weights trained on the ILSVRC15 dataset as initialization then perform fine-tuning on the MOT sequence, which is referred as “Fine-tuning” and is the scheme used in other experiments in this paper. “Without CNN<sub>BBE</sub>” shows the configuration where detection score is used for bounding box quality estimation instead of the dedicated CNN<sub>BBE</sub>. Target management without CNN<sub>BBE</sub> cannot efficiently prevent FPs merging into the tracking results. “Without SOT” in Tab. 5 stands for the case that only detections from external detector are used for association, no SOT prediction is included. By contrast, in the proposed solution, though SOT predictions introduce some FPs, it recovers much more missing candidates and reduces FN greatly.

## 6. Conclusion

In this paper we proposed a novel deep architecture for MOT, which learns jointly, in an end-to-end fashion, features and high-order affinity directly from the ground truth trajectories. During tracking, predictions from SOT and a dedicated target management are include to further boost tracking robustness. Experiments on the MOT2015, MOT2017, KITTI-Car and UA-DETRAC datasets clearly show the effectiveness of proposed approach.

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