

Legendre functions

A collection of points from different sources

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Contents

I. Book: Higher transcendental functions, by Harry Bateman	5
1. introduction	7
2. Solution of Legendre Differential equations	9
2.1. Legendre functions and differential equations	9
II. Book: Asymptotic and special functions, by F.W.J Olver	11

Part I.

Book: Higher transcendental functions,
by Harry Bateman

1. introduction

1.1.

The expansion of $(a^2 - 2ar\cos(\gamma) + r^2)^{-\frac{1}{2}}$ in powers of r contains the coefficients in terms of $\cos(\gamma)$. These coefficients are polynomials of $\cos(\gamma)$. These were first introduced in 1784 by Legendre and are known as Legendre polynomials. The expression $(a^2 - 2ar\cos(\gamma) + r^2)^{-\frac{1}{2}}$ is dealing the potential at a point P of a source at the point A . Here r and a are the distances of P and A from O (Origin) respectively.

2. Solution of Legendre Differential equations

2.1. Legendre functions and differential equations

Definition 2.1.1 (Legendre's differential equation). *A differential equation of the form*

$$(1 - z^2) \frac{d^2\omega}{dz^2} - 2z \frac{d\omega}{dz} + [\nu(\nu + 1) - \frac{\mu^2}{(1 - z)^2}] \omega = 0,$$

where ν, μ and z are unrestricted (Complex numbers)

Definition 2.1.2 (Legendre functions). *The Legendre functions are solutions of Legendre's differential equation.*

Part II.

Book: Asymptotic and special
functions, by F.W.J Olver

Index

Legendre functions, 9