

**The University of Hong Kong
School of Public Health**

**CMED6100/MMPH6002/CMED7100
Introduction to Biostatistics (Semester I)
Practical 3 Suggested solution**

Part 1: Hypothesis tests

Describe and evaluate the association between breastfeeding status and SGA/AGA status, by using the Pearson's chi-square test.

We want to test whether there is an association between the breastfeeding status and SGA/AGA status using the Pearson's chi-square test.

a) State the null hypothesis.

H₀: **There is no association between the breastfeeding status and SGA/AGA status**

b) Construct a frequency table between breastfeeding status and SGA/AGA status. What is the expected frequency if breastfeeding status and SGA/AGA status are independent? Complete the tables.

Data -> Manage variables in active dataset -> Convert numeric variables to factors [Variables: feeddur; Factor Levels: Use numbers]

Statistics -> Contingency table -> Two-way table [Row variable: feeddur; Column variable: sga; Statistics: Compute Percentages: Column Percentages; Chi-square test of independence; Print expected frequencies]

Percentages of expected frequencies can be directly computed on R [e.g. type '314.1/572']

Observed breastfeeding status of the birth cohort, stratified by SGA/AGA status

Breastfeeding status*	AGA (n=572)	SGA (n=282)
Never breastfed	293 (51.2%)	176 (62.4%)
Partially breastfed	169 (29.5%)	64 (22.7%)
Exclusively breastfed $\leq 2m$	66 (11.5%)	18 (6.4%)
Exclusively breastfed $> 2m$	44 (7.7%)	24 (8.5%)

*Children with missing breastfeeding status were excluded

Expected breastfeeding status of the birth cohort, stratified by SGA/AGA status

Breastfeeding status*	AGA (n=572)	SGA (n=282)
Never breastfed	314.1 (54.9%)	154.9 (54.9%)
Partially breastfed	156.1 (27.3%)	76.9 (27.3%)
Exclusively breastfed $\leq 2m$	56.3 (9.8%)	27.7 (9.8%)
Exclusively breastfed $> 2m$	45.5 (8.0%)	22.5 (8.0%)

*Children with missing breastfeeding status were excluded

- c) By using R Commander, what is the value of the Pearson's chi-square test statistic? How many degrees of freedom? What is the p-value?

From the output in b)

Chi-square value	Degree of freedom	p-value
12.8	3	0.005

- d) How do the children classified as AGA differ from those classified as SGA in terms of breastfeeding status? By using a 0.05 level of significance, state your conclusion based on your above findings.

There was a higher proportion of children with SGA status who were never breastfed. At a 0.05 level of significance, we reject the null hypothesis and conclude that there are association between breastfeeding status and AGA/SGA status.

Part 2: Designing studies

- (a) If two groups of equal size are compared at the 5% significance level, how large should each group be if there is to be 90% power to detect a change in mean skin fold of 0.5 mm? (Hints: you can apply "two sample t-test")

[Two-sample t-test; $\sigma_1, \sigma_2 = 2.3$, true difference = 0.5, $\alpha = 0.05$, power = 0.9]

$n_1 = n_2 = 446$, a sample of 892 subjects is needed.

- (b) How many would I need if the desired power were 80%?

[power = 0.8]

$n_1 = n_2 = 334$, a sample of 668 subjects is needed.

- (c) Suppose I can recruit 300 patients only, what difference can I detect with 80% power?

[$n_1 = n_2 = 150$, change the difference until power = 0.8]

Difference = 0.747mm

- (d) Suppose I decide that a change of 1 mm in mean skin-fold is of interest after all. How many patients do I need for a power of 80%?

[$\sigma_1, \sigma_2 = 2.3$, true difference = 1, $\alpha = 0.05$, change n_1/n_2 until power = 0.8]

$n_1 = n_2 = 85$, a sample of 170 subjects is needed.

- (e) There is some uncertainty about the standard deviation, and it may be as low as 2 mm or as high as 3 mm. Complete the following table for the sample size required for 80% power.

$[\sigma_1, \sigma_2 = 2.3, 2 \text{ or } 3, \alpha = 0.05, \text{ change } n_1/n_2 \text{ until power} = 0.8]$

Standard deviation	Sample size required
2 mm	128
2.3 mm	170
3 mm	286

Scenario 2: Dichotomous outcome, 2 groups

Two methods of the management of malignant low bile duct obstruction are surgical biliary bypass and endoscopic insertion of a stent. A randomized controlled trial was performed to compare these approaches.

The primary outcome of the trial will be the binary variable which shows the dichotomous responses (yes/no) to the question “Did the patient die within 30 days of the procedure?” The trial will be designed to test the null hypothesis at the 5% level of significance with 95% power. The trial should be able to detect a change in mortality rate from 20% to 5%. How large is the sample needed for the study? (Hints: you can use “test for comparing two proportions”.)

$[\text{Test comparing two proportions; } p_2 = 0.2, p_1 = 0.05, \alpha = 0.05, \text{ change } n_1/n_2 \text{ until power} = 0.95]$

Assumptions

Level of significance:	<u>0.05</u>
Statistical power of hypothesis test:	<u>0.95</u>

Sample size calculations

Sample size in each group:	<u>137</u>
Total sample size:	<u>274</u>

Scenario 3: Unbalanced design and resource constraints

Suppose you test $H_0: OR = 1$ at $\alpha = 0.05$ (two-sided) with 100 cases in a case-controlled study. The prevalence of exposure in the control population is assumed to be 25%. You aim to know the statistical power to detect odds ratios of 2.0.

- (a) What is the statistical power of the test if you decide to use different case-to-control ratios?

$$p_2 = 0.25, \text{ odds ratio} = 2.0 \Rightarrow p_1 = 0.4$$

Case-to-control ratio = 1: 2, 100 cases → 200 controls

$n_1=100$, $n_2=200$ controls

$n_1=100$, $n_2=400$ controls

$n_1=100$, $n_2=600$ controls

$n_1=100$, $n_2=800$ controls

[Test comparing two proportions; $p_2 = 0.25$, $p_1 = 0.4$, $\alpha = 0.05$, $n_2 = 200, 400, 600$ and 800 , $n_1 = 100$]

Case-to-control ratio	Statistical power
1: 2	0.7131
1: 4	0.8015
1: 6	0.8316
1: 8	0.8466

You can request funding from a local agency, but the budget must be no higher than \$120,000. The cost of recruiting a case is \$400, while controls are easier to find and recruit and will only cost \$200 each.

- (b) If you recruit cases and control in the ratio 1:1, what sample size could you achieve with \$120,000?

For 1:1, let X be the number of subjects in the control group, then the number of subjects in the case group is also X and we have:

$$\$200X + \$400X = \$120,000$$

$$\rightarrow \$600X = \$120,000$$

$$\rightarrow X = 200$$

200 cases and 200 controls.

- (c) Complete the following table for possible sample sizes with alternative ratios of cases to controls:

For 2:1, let X be the number of subjects in the control group, then the number of subjects in the case group is also $2X$ and we have:

$$\$400(2X) + \$200(X) = \$120000$$

$$\rightarrow \$1000 X = \$120000$$

$$\rightarrow X=120$$

120 controls and 240 cases

Table. Total costs					
Case-to-control ratio	2:1	1:1	1:2	1:4	1:8
Number of cases	240	200	150	100	60
Number of controls	120	200	300	400	480
Total costs	\$120,000	\$120,000	\$120,000	\$120,000	\$120,000

- (d) Complete the following table to describe the power of each possible study to detect odds ratios of 1.5, 1.8 and 2.0.

$p_2 = 0.25$, odds ratio = 2, 1.8 and 1.5 $\Rightarrow p_1 = 0.4, 0.375$ and 0.333 , respectively

[Test comparing two proportions; $p_2 = 0.25$, $p_1 = 0.4, 0.375$ and 0.333 , $\alpha = 0.05$,
 $(n_2, n_1) = (120, 240)$
 $(n_2, n_1) = (200, 200)$
 $(n_2, n_1) = (300, 150)$
 $(n_2, n_1) = (400, 100)$
 $(n_2, n_1) = (480, 60)$]

Table. Statistical power					
Case-to-control ratio	2:1	1:1	1:2	1:4	1:8
OR = 2	0.781	0.875	0.879	0.802	0.630
OR = 1.8	0.620	0.737	0.746	0.653	0.484
OR = 1.5	0.314	0.404	0.416	0.349	0.247

- (e) What is the optimal study design given the constraints listed above?

Design with case-to-control ratio 1:2. Its power is largest under the same budget constraint.