

## 1. Figuring Out the Tips

a)

In the case of 6 guests, the answer is no.

For example, 1) If all guests give 3 as their tip, then each plate will have a tip of 3  
2) If  $G_1, G_3, G_5$  give tips of 4 and  $G_2, G_4, G_6$  give tips of 2, then each plate will have a tip of 3. So, that's why the answer is no.

b)

Yes, in the case of 5 guests you can

figure out each guest tips.

$$\left\{ \begin{array}{l} \frac{1}{2}G_1 + \frac{1}{2}G_5 = P_1 \\ \frac{1}{2}G_1 + \frac{1}{2}G_2 = P_2 \\ \frac{1}{2}G_2 + \frac{1}{2}G_3 = P_3 \\ \frac{1}{2}G_3 + \frac{1}{2}G_4 = P_4 \\ \frac{1}{2}G_4 + \frac{1}{2}G_5 = P_5 \end{array} \right. \quad \left| \begin{array}{ccccc|c} & \frac{1}{2} & 0 & 0 & 0 & \frac{1}{2} \\ & \frac{1}{2} & \frac{1}{2} & 0 & 0 & 0 \\ 0 & \frac{1}{2} & \frac{1}{2} & 0 & 0 & 0 \\ 0 & 0 & \frac{1}{2} & \frac{1}{2} & 0 & 0 \\ 0 & 0 & 0 & \frac{1}{2} & \frac{1}{2} & 0 \end{array} \right| \begin{array}{c} P_1 \\ P_2 \\ P_3 \\ P_4 \\ P_5 \end{array}$$

By looking at the columns of this matrix, we can see that they're linearly independent. So, this matrix is invertible and only a unique solution exists.

c)

When  $n$  is an even number, there's multiple ways to set guest tips, such that they cancel out or add up to a common plate tip. But, that is not the case when  $n$  is an odd number. In other words, we can figure out everyone's tip when there are odd number of guests and can't when there are even.



## 2. Show It!

a) Let  $\vec{x}_1$  and  $\vec{x}_2$  be unique solutions to  $A\vec{x} = \vec{b}$

That means,

$$A\vec{x}_1 = \vec{b} \quad A\vec{x}_2 = \vec{b}$$

$$A\vec{x}_1 = A\vec{x}_2$$

$$A(\vec{x}_1 - \vec{x}_2) = \vec{0}$$

$$[\vec{c}_1, \vec{c}_2, \dots, \vec{c}_n](\vec{x}_1 - \vec{x}_2) = \vec{0}$$

Since  $\vec{x}_1 \neq \vec{x}_2$ ,  $\vec{x}_1 - \vec{x}_2 \neq \vec{0}$

$$\text{Let } \vec{u} = \vec{x}_1 - \vec{x}_2$$

$$[\vec{c}_1, \vec{c}_2, \dots, \vec{c}_n] \begin{bmatrix} u_1 \\ u_2 \\ \vdots \\ u_n \end{bmatrix} = \vec{0}$$

$$u_1\vec{c}_1 + u_2\vec{c}_2 + \dots + u_n\vec{c}_n = \vec{0}$$

let  $u_1 \neq 0$ , then

$$\vec{c}_1 = -\frac{u_2}{u_1}\vec{c}_2 + \dots + \frac{u_n}{u_1}\vec{c}_n$$

Thus,  $A$  is linearly dependent.

c) Given that set  $\{\vec{v}_1, \vec{v}_2, \dots, \vec{v}_k\}$  is a linearly dependent set in  $\mathbb{R}^n$ , we know that

For some  $a_1, a_2, \dots, a_k \in \mathbb{R}$

$$a_1\vec{v}_1 + a_2\vec{v}_2 + \dots + a_k\vec{v}_k = \vec{0}$$

Let  $A$  be any  $n \times n$  matrix

$$A(a_1\vec{v}_1 + a_2\vec{v}_2 + \dots + a_k\vec{v}_k) = A(\vec{0})$$

$$A(a_1\vec{v}_1) + A(a_2\vec{v}_2) + \dots + A(a_k\vec{v}_k) = \vec{0}$$

$$a_1A\vec{v}_1 + a_2A\vec{v}_2 + \dots + a_kA\vec{v}_k = \vec{0}$$

The equation still holds true, meaning that some vector is  $\{A\vec{v}_1, A\vec{v}_2, \dots, A\vec{v}_k\}$  can be represented by a linear combination of some other vector in the set.

Thus, the set  $\{A\vec{v}_1, A\vec{v}_2, \dots, A\vec{v}_k\}$  is linearly dependent.



Scanned with  
CamScanner

### 3. Quadcopter Transformations

a)

$$R_x(30^\circ) = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos(30^\circ) & -\sin(30^\circ) \\ 0 & \sin(30^\circ) & \cos(30^\circ) \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \frac{\sqrt{3}}{2} & -\frac{1}{2} \\ 0 & \frac{1}{2} & \frac{\sqrt{3}}{2} \end{bmatrix}$$

$$R_z(60^\circ) = \begin{bmatrix} \cos(60^\circ) & -\sin(60^\circ) & 0 \\ \sin(60^\circ) & \cos(60^\circ) & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} & 0 \\ \frac{\sqrt{3}}{2} & \frac{1}{2} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} & 0 \\ \frac{\sqrt{3}}{2} & \frac{1}{2} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & \frac{\sqrt{3}}{2} & -\frac{1}{2} \\ 0 & \frac{1}{2} & \frac{\sqrt{3}}{2} \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} \frac{1}{2} + 0 + 0 & 0 - \frac{3}{4} + 0 & 0 + \frac{\sqrt{3}}{4} + 0 \\ \frac{\sqrt{3}}{2} + 0 + 0 & 0 + \frac{\sqrt{3}}{4} + 0 & 0 - \frac{1}{4} + 0 \\ 0 & \frac{1}{2} + 0 + 0 & 0 + 0 + \frac{\sqrt{3}}{2} \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

$$\begin{bmatrix} \frac{1}{2} & -\frac{3}{4} & \frac{\sqrt{3}}{4} \\ \frac{\sqrt{3}}{2} & \frac{\sqrt{3}}{4} & -\frac{1}{4} \\ 0 & \frac{1}{2} & \frac{\sqrt{3}}{2} \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

2 resulting matrix

b) We'll multiply the 2 matrices now in reverse

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & \frac{\sqrt{3}}{2} & -\frac{1}{2} \\ 0 & \frac{1}{2} & \frac{\sqrt{3}}{2} \end{bmatrix} \begin{bmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} & 0 \\ \frac{\sqrt{3}}{2} & \frac{1}{2} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} \frac{1}{2} + 0 + 0 & -\frac{\sqrt{3}}{2} + 0 + 0 & 0 \\ 0 + \frac{3}{4} + 0 & 0 + \frac{\sqrt{3}}{4} + 0 & -\frac{1}{2} \\ 0 + \frac{\sqrt{3}}{4} + 0 & 0 + \frac{1}{4} + 0 & \frac{\sqrt{3}}{2} \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

$$\begin{bmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} & 0 \\ \frac{3}{4} & \frac{\sqrt{3}}{4} & -\frac{1}{2} \\ \frac{\sqrt{3}}{4} & \frac{1}{4} & \frac{\sqrt{3}}{2} \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

computed matrix



c) Intended : 
$$\left[ \begin{array}{ccc|c} \frac{1}{2} & -\frac{\sqrt{3}}{4} & \frac{\sqrt{3}}{4} & 1 \\ \frac{\sqrt{3}}{2} & \frac{\sqrt{3}}{4} & -\frac{1}{4} & 1 \\ 0 & \frac{1}{2} & \frac{\sqrt{3}}{2} & 1 \end{array} \right] \xrightarrow{\text{Row operations}} \left[ \begin{array}{c|c} \frac{\sqrt{3}-1}{4} & \\ \frac{3+\sqrt{3}}{4} & \\ \frac{\sqrt{3}+1}{2} & \end{array} \right]$$

Actual : 
$$\left[ \begin{array}{ccc|c} \frac{1}{2} & -\frac{\sqrt{3}}{2} & 0 & 1 \\ \frac{\sqrt{3}}{4} & \frac{\sqrt{3}}{4} & -\frac{1}{2} & 1 \\ \frac{\sqrt{3}}{4} & \frac{1}{4} & \frac{\sqrt{3}}{2} & 1 \end{array} \right] \xrightarrow{\text{Row operations}} \left[ \begin{array}{c|c} \frac{1-\sqrt{3}}{2} & \\ \frac{1+\sqrt{3}}{4} & \\ \frac{1+\sqrt{3}+\sqrt{3}}{4} & \end{array} \right]$$

The expected and actual positions are different.

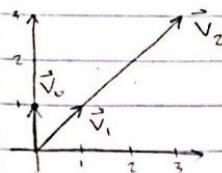
d)  $\|\vec{z}\| = 1$ . The distance is still the same.

This is because rotation matrices don't change the magnitude of the position vector.



#### 4. Image Stitching

a)  $\vec{v}_2 = \begin{bmatrix} 2 & 2 \\ -2 & 2 \end{bmatrix} \vec{v}_0 + \vec{v}_1 = \begin{bmatrix} 2 & 2 \\ -2 & 2 \end{bmatrix} \begin{bmatrix} 0 \\ 1 \end{bmatrix} + \begin{bmatrix} 1 \\ 0 \end{bmatrix} = \begin{bmatrix} 2 \\ 2 \end{bmatrix} + \begin{bmatrix} 1 \\ 0 \end{bmatrix} = \begin{bmatrix} 3 \\ 2 \end{bmatrix}$



$\vec{v}_2$  was scaled and rotated from  $\vec{v}_0$ .

b)  $\begin{bmatrix} q_x \\ q_y \end{bmatrix} = \begin{bmatrix} R_{xx} & R_{xy} \\ R_{yx} & R_{yy} \end{bmatrix} \begin{bmatrix} p_x \\ p_y \end{bmatrix} + \begin{bmatrix} T_x \\ T_y \end{bmatrix} \rightarrow \begin{cases} q_x = R_{xx}p_x + R_{xy}p_y + T_x \\ q_y = R_{yx}p_x + R_{yy}p_y + T_y \end{cases}$

There are 6 unknowns. You need at least 6 independent equations to solve for all unknowns. You need 3 pairs of common points  $\vec{p}$  and  $\vec{q}$ .

c) 
$$\begin{cases} q_{bx} = R_{xx}p_{1x} + R_{xy}p_{1y} + T_x \\ q_{by} = R_{yx}p_{1x} + R_{yy}p_{1y} + T_y \\ q_{bx} = R_{xx}p_{2x} + R_{xy}p_{2y} + T_x \\ q_{by} = R_{yx}p_{2x} + R_{yy}p_{2y} + T_y \\ q_{bx} = R_{xx}p_{3x} + R_{xy}p_{3y} + T_x \\ q_{by} = R_{yx}p_{3x} + R_{yy}p_{3y} + T_y \end{cases}$$

$$\begin{array}{cccccc|c|c} p_{1x} & p_{1y} & 0 & 0 & 1 & 0 & R_{xx} & q_{bx} \\ 0 & 0 & p_{1x} & p_{1y} & 0 & 1 & R_{xy} & q_{by} \\ p_{2x} & p_{2y} & 0 & 0 & 1 & 0 & R_{yx} & - \\ 0 & 0 & p_{2x} & p_{2y} & 0 & 1 & R_{yy} & q_{bx} \\ p_{3x} & p_{3y} & 0 & 0 & 1 & 0 & T_x & q_{by} \\ 0 & 0 & p_{3x} & p_{3y} & 0 & 1 & T_y & q_{bx} \\ \hline & & & & & & & q_{by} \end{array}$$

↓  
vector of unknowns



e) I expected the matrix to linearly dependent and that's what I got as the output.

This is because since  $\vec{P}_1$ ,  $\vec{P}_2$ , and  $\vec{P}_3$  form a straight line, you can represent  $\vec{P}_2$  and  $\vec{P}_3$  using  $\vec{P}_1$ . Thus, the matrix is linearly dependent



## 5. Properties of Pump Systems

a) 
$$\begin{cases} x_b[n+1] = 0 \\ x_a[n+1] = x_b[n] + x_a[n] \end{cases}$$

b)  $\vec{x}[n+1] = A \vec{x}[n]$   

$$\begin{bmatrix} x_a[n+1] \\ x_b[n+1] \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} x_a[n] \\ x_b[n] \end{bmatrix}$$
  

$$A$$

c) 1)  $x_a[0] = 0.5, x_b[0] = 0.5$   

$$\begin{bmatrix} x_a[1] \\ x_b[1] \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} 0.5 \\ 0.5 \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

2)  $x_a[0] = 0.3, x_b[0] = 0.7$

$$\begin{bmatrix} x_a[1] \\ x_b[1] \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} 0.3 \\ 0.7 \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

d) No, this is because there's infinite number of solutions to the matrix  $\begin{bmatrix} 1 & 1 \\ 0 & 0 \end{bmatrix}$

e) No, you can't decide which initial state you started with by just observing  $\vec{x}[1]$ .

What we can tell about matrix A is that:

1) A is not invertible

2) A has infinite number of solutions

Proof by contradiction:

Let  $\vec{x}_1[0], \vec{x}_2[0]$  be 2 distinct initial states

that lead to same  $\vec{x}[1]$ , then

$$A\vec{x}_1[0] = A\vec{x}_2[0]$$

$$A'(A\vec{x}_1[0]) = A'(A\vec{x}_2[0])$$

$$\vec{x}_1[0] = \vec{x}_2[0] \leftarrow \text{we got a contradiction}$$

So, A is not invertible and thus, has  $\infty$  # of solutions



f) 
$$\begin{cases} x_1[n+1] = 0 \\ x_2[n+1] = 0.4x_1[n] + 0.5x_2[n] + 0.2x_3[n] \\ x_3[n+1] = 0.6x_2[n] + 0.35x_3[n] \end{cases}$$

$$\vec{x}[n+1] = A\vec{x}[n]$$

$$\vec{x}[n+1] = \begin{bmatrix} 0 & 0 & 0 \\ 0.4 & 0.5 & 0.2 \\ 0 & 0.6 & 0.35 \end{bmatrix} \vec{x}[n]$$

A

Sum of entries of the columns:

$$c_1 = 0.4 < 1$$

$$c_2 = 1.1 > 1$$

$$c_3 = 0.55 < 1$$

This means that the total water in the system is decreasing over time.

## 6. Homework Process

I worked on this homework alone.  
 I read all the notes, then did the homework little by little each night.



# EECS16A: Homework 3

## Problem 4: Image Stitching

This section of the notebook continues the image stitching problem. Be sure to have a `figures` folder in the same directory as the notebook. The `figures` folder should contain the files:

```
Berkeley_banner_1.jpg  
Berkeley_banner_2.jpg  
stacked_pieces.jpg  
lefthalfpic.jpg  
righthalfpic.jpg
```

Note: This structure is present in the provided HW3 zip file.

Run the next block of code before proceeding

```
In [1]: import numpy as np  
import numpy.matlib  
import matplotlib.pyplot as plt  
from mpl_toolkits.mplot3d import Axes3D  
from numpy import pi, cos, exp, sin  
import matplotlib.image as mpimg  
import matplotlib.transforms as mtransforms  
  
%matplotlib inline  
  
#loading images  
image1=mpimg.imread('figures/Berkeley_banner_1.jpg')  
image1=image1/255.0  
image2=mpimg.imread('figures/Berkeley_banner_2.jpg')  
image2=image2/255.0  
image_stack=mpimg.imread('figures/stacked_pieces.jpg')  
image_stack=image_stack/255.0  
  
image1_marked=mpimg.imread('figures/lefthalfpic.jpg')  
image1_marked=image1_marked/255.0  
image2_marked=mpimg.imread('figures/righthalfpic.jpg')  
image2_marked=image2_marked/255.0
```

```
def euclidean_transform_2to1(transform_mat,translation,image,position,LL
new_position=np.round(transform_mat.dot(position)+translation)
new_position=new_position.astype(int)

if (new_position>=LL).all() and (new_position<UL).all():
    values=image[new_position[0][0],new_position[1][0],:]
else:
    values=np.array([2.0,2.0,2.0])

return values

def euclidean_transform_1to2(transform_mat,translation,image,position,LL
transform_mat_inv=np.linalg.inv(transform_mat)
new_position=np.round(transform_mat_inv.dot(position-translation))
new_position=new_position.astype(int)

if (new_position>=LL).all() and (new_position<UL).all():
    values=image[new_position[0][0],new_position[1][0],:]
else:
    values=np.array([2.0,2.0,2.0])

return values

def solve(A,b):
    try:
        z = np.linalg.solve(A,b)
    except:
        raise ValueError('Rows are not linearly independent. Cannot solve')
    return z
```

We will stick to a simple example and just consider stitching two images (if you can stitch two pictures, then you could conceivably stitch more by applying the same technique over and over again).

Daniel decided to take an amazing picture of the Campanile overlooking the bay. Unfortunately, the field of view of his camera was not large enough to capture the entire scene, so he decided to take two pictures and stitch them together.

The next block will display the two images.

```
In [2]: plt.figure(figsize=(20,40))

plt.subplot(311)
plt.imshow(image1)

plt.subplot(312)
plt.imshow(image2)

plt.subplot(313)
plt.imshow(image_stack)

plt.show()
```



Once you apply Marcela's algorithm on the two images you get the following result (run the next block):

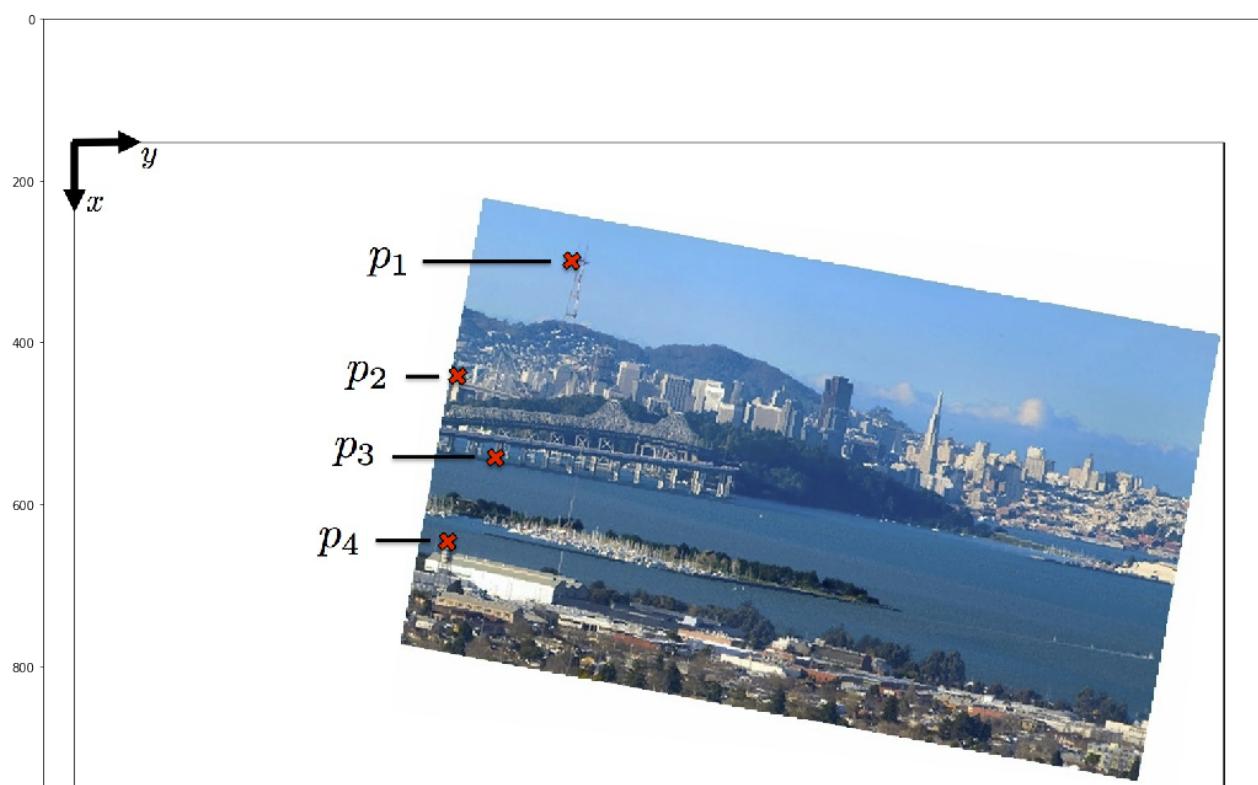
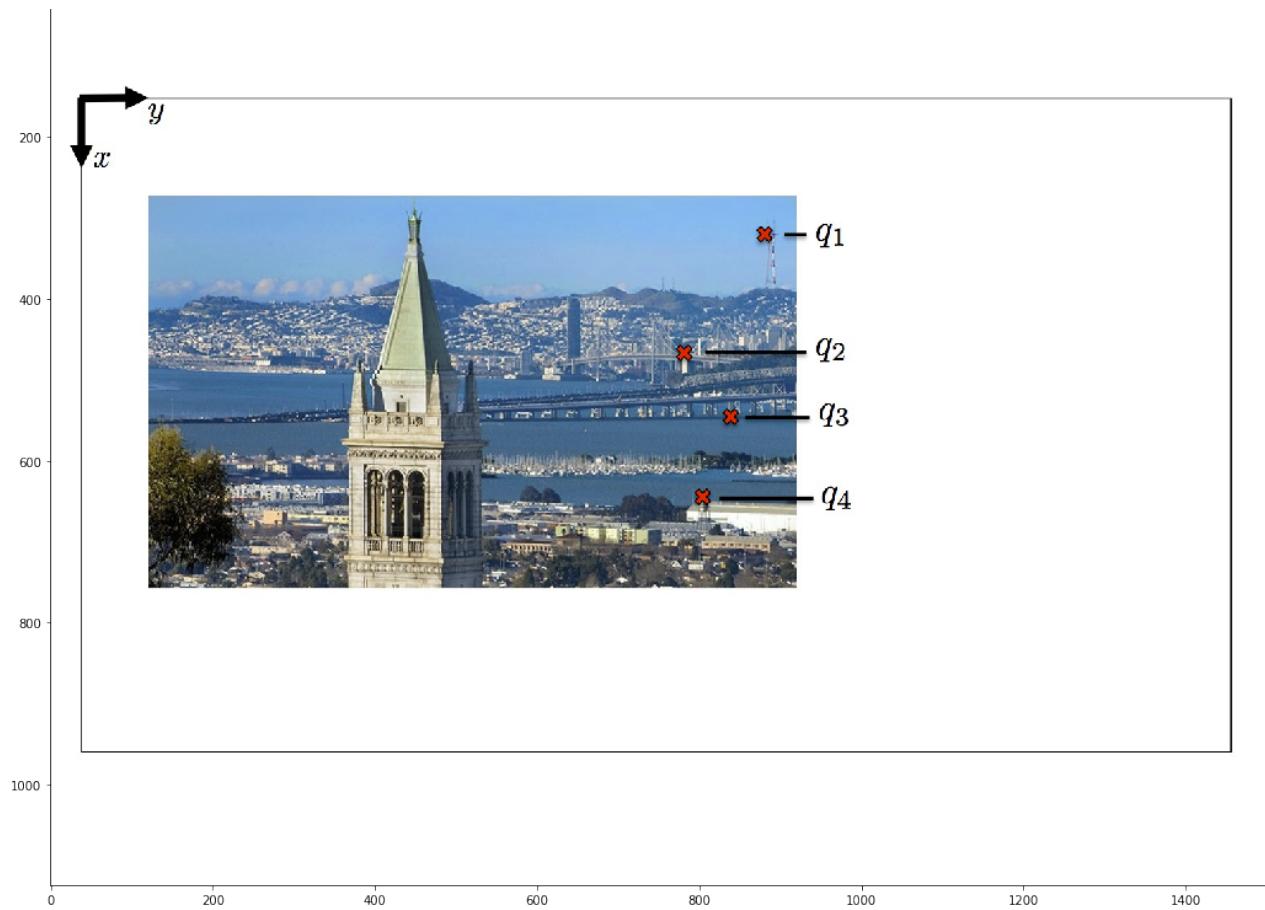
```
In [3]: plt.figure(figsize=(20,30))

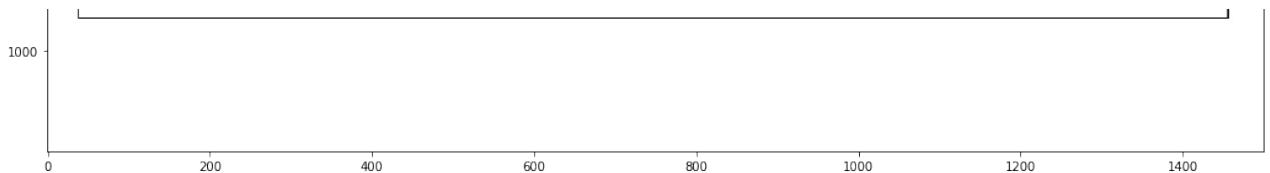
plt.subplot(211)
plt.imshow(image1_marked)

plt.subplot(212)
plt.imshow(image2_marked)
```

Out[3]: <matplotlib.image.AxesImage at 0x120bd48d0>







As you can see Marcela's algorithm was able to find four common points between the two images. These points expressed in the coordinates of the first image and second image are

$$\begin{aligned}\vec{p}_1 &= \begin{bmatrix} 200 \\ 700 \end{bmatrix} & \vec{p}_2 &= \begin{bmatrix} 310 \\ 620 \end{bmatrix} & \vec{p}_3 &= \begin{bmatrix} 390 \\ 660 \end{bmatrix} & \vec{p}_4 &= \begin{bmatrix} \cdot \\ \cdot \end{bmatrix} \\ \vec{q}_1 &= \begin{bmatrix} 162.2976 \\ 565.8862 \end{bmatrix} & \vec{q}_2 &= \begin{bmatrix} 285.4283 \\ 458.7469 \end{bmatrix} & \vec{q}_3 &= \begin{bmatrix} 385.2465 \\ 498.1973 \end{bmatrix} & \vec{q}_4 &= \begin{bmatrix} 465.7 \\ 455.0 \end{bmatrix}\end{aligned}$$

It should be noted that in relation to the image the positive x-axis is down and the positive y-axis is right. This will have no bearing as to how you solve the problem, however it helps in interpreting what the numbers mean relative to the image you are seeing.

Using the points determine the parameters  $R_{11}, R_{12}, R_{21}, R_{22}, T_x, T_y$  that map the points from the first image to the points in the second image by solving an appropriate system of equations. Hint: you do not need all the points to recover the parameters.

```
In [4]: # Note that the following is a general template for solving for 6 unknowns
# You do not have to use the following code exactly.
# All you need to do is to find parameters R_11, R_12, R_21, R_22, T_x,
# If you prefer finding them another way it is fine.

# fill in the entries
A = np.array([[200, 700, 0, 0, 1, 0],
              [0, 0, 200, 700, 0, 1],
              [310, 620, 0, 0, 1, 0],
              [0, 0, 310, 620, 0, 1],
              [390, 660, 0, 0, 1, 0],
              [0, 0, 390, 660, 0, 1]])

# fill in the entries
b = np.array([[162.2976],[565.8862],[285.4283],[458.7469],[385.2465],[49.0]])

A = A.astype(float)
b = b.astype(float)

# solve the linear system for the coefficients
z = solve(A,b)

#Parameters for our transformation
R_11 = z[0,0]
R_12 = z[1,0]
R_21 = z[2,0]
R_22 = z[3,0]
T_x = z[4,0]
T_y = z[5,0]
```

Stitch the images using the transformation you found by running the code below.

**Note that it takes about 40 seconds for the block to finish running on a modern laptop.**

```
In [5]: matrix_transform=np.array([[R_11,R_12],[R_21,R_22]])
translation=np.array([T_x,T_y])

#Creating image canvas (the image will be constructed on this)
num_row,num_col,blah=image1.shape
image_rec=1.0*np.ones((int(num_row),int(num_col),3))

#Reconstructing the original image

LL=np.array([[0],[0]]) #lower limit on image domain
UL=np.array([[num_row],[num_col]]) #upper limit on image domain
```

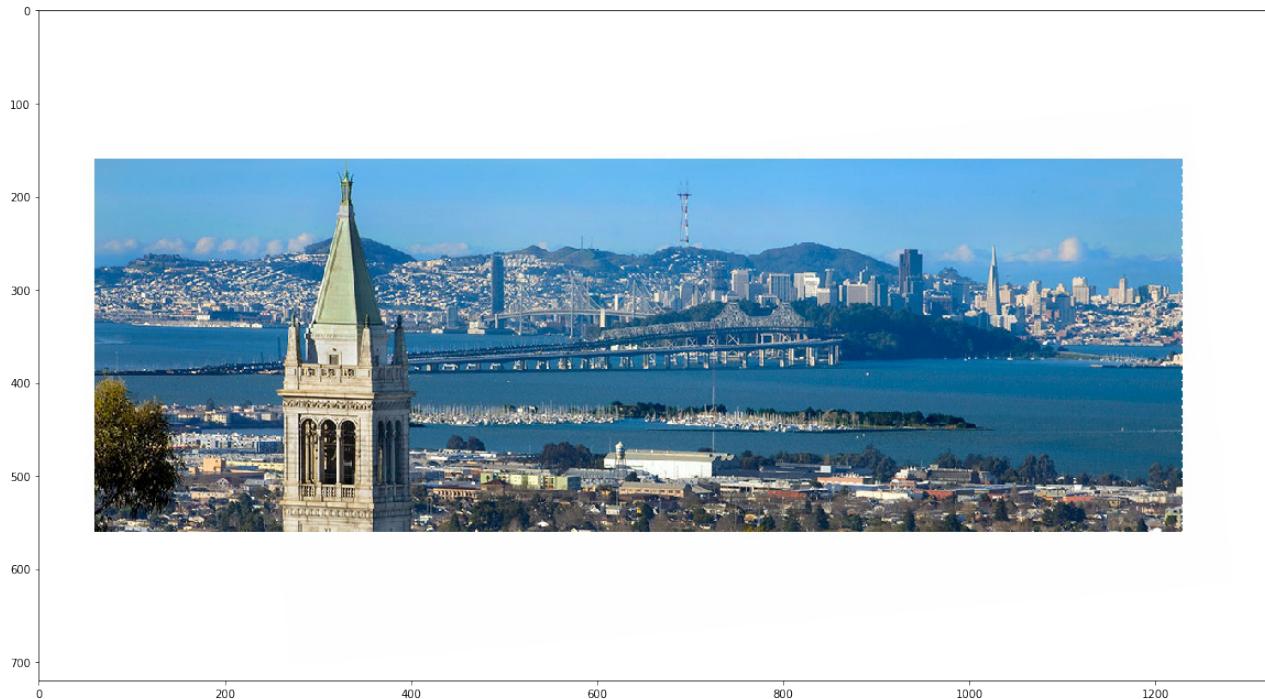
```

for row in range(0,int(num_row)):
    for col in range(0,int(num_col)):
        #notice that the position is in terms of x and y, so the c
        position=np.array([[row],[col]])
        if image1[row,col,0] > 0.995 and image1[row,col,1] > 0.995 and image1[row,col,2] > 0.995:
            temp = euclidean_transform_2tol(matrix_transform,translation)
            image_rec[row,col,:] = temp
        else:
            image_rec[row,col,:] = image1[row,col,:]

plt.figure(figsize=(20,20))
plt.imshow(image_rec)
plt.axis('on')
plt.show()

```

Clipping input data to the valid range for imshow with RGB data ([0..1] for floats or [0..255] for integers).



## Part E: Failure Mode Points

$$\begin{aligned}\vec{p}_1 &= \begin{bmatrix} 390 \\ 660 \end{bmatrix} & \vec{p}_2 &= \begin{bmatrix} 425 \\ 645 \end{bmatrix} & \vec{p}_3 &= \begin{bmatrix} 460 \\ 630 \end{bmatrix} \\ \vec{q}_1 &= \begin{bmatrix} 385 \\ 450 \end{bmatrix} & \vec{q}_2 &= \begin{bmatrix} 425 \\ 480 \end{bmatrix} & \vec{q}_3 &= \begin{bmatrix} 465 \\ 510 \end{bmatrix}\end{aligned}$$

To solve: # Note that the following is a general template for solving for 6 unknowns

```
In [10]: # Note that the following is a general template for solving for a unknown  
# You do not have to use the following code exactly.  
# All you need to do is to find parameters R_11, R_12, R_21, R_22, T_x,  
# If you prefer finding them another way it is fine.  
  
# fill in the entries  
A = np.array([[390, 660, 0, 0, 1, 0],  
              [0, 0, 390, 660, 0, 1],  
              [425, 645, 0, 0, 1, 0],  
              [0, 0, 425, 645, 0, 1],  
              [460, 630, 0, 0, 1, 0],  
              [0, 0, 460, 630, 0, 1]])  
  
# fill in the entries  
b = np.array([[385],[450],[425],[480],[465],[510]])  
  
A = A.astype(float)  
b = b.astype(float)  
  
# solve the linear system for the coefficiens  
z = solve(A,b)  
  
#Parameters for our transformation  
R_11 = z[0,0]  
R_12 = z[1,0]  
R_21 = z[2,0]  
R_22 = z[3,0]  
T_x = z[4,0]  
T_y = z[5,0]
```

```
-----  
-----  
LinAlgError                                     Traceback (most recent call  
last)  
<ipython-input-1-4ee2c81e8dee> in solve(A, b)  
    51     try:  
---> 52         z = np.linalg.solve(A,b)  
    53     except:  
  
~/miniconda3/lib/python3.7/site-packages/numpy/linalg/linalg.py in sol  
ve(a, b)  
    402         extobj = get_linalg_error_extobj(_raise_linalgerror_singul  
ar)  
--> 403         r = gufunc(a, b, signature=signature, extobj=extobj)  
    404  
  
~/miniconda3/lib/python3.7/site-packages/numpy/linalg/linalg.py in _ra  
ise_linalgerror_singular(err, flag)  
    96 def _raise_linalgerror_singular(err, flag):  
---> 97     raise LinAlgError("Singular matrix")  
    98
```

```
LinAlgError: Singular matrix
```

During handling of the above exception, another exception occurred:

```
ValueError                                Traceback (most recent call
last)
<ipython-input-6-85bd29877f64> in <module>
    19
    20 # solve the linear system for the coefficiens
--> 21 z = solve(A,b)
    22
    23 #Parameters for our transformation

<ipython-input-1-4ee2c81e8dee> in solve(A, b)
    52         z = np.linalg.solve(A,b)
    53     except:
--> 54         raise ValueError('Rows are not linearly independent. C
annot solve system of linear equations uniquely. :)')
    55     return z

ValueError: Rows are not linearly independent. Cannot solve system of
linear equations uniquely. :)
```

In [ ]: