EECS16A: Homework 2

Problem 3: Finding Charges from Potential Measurements

[1. 2. 3.]

Problem 4: Kinematic Model for a Simple Car

This script helps to visualize the difference between a nonlinear model and a corresponding linear approximation for a simple car. What you should notice is that the linear model is similar to the nonlinear model when you are close to the point where the approximation is made.

First, run the following block to set up the helper functions needed to simulate the vehicle models and plot the trajectories taken.

```
In [1]: # DO NOT MODIFY THIS BLOCK!
    ''' Problem/Model Setup'''
    import numpy as np
    import matplotlib.pyplot as plt
    %matplotlib inline

# Vehicle Model Constants
L = 1.0 # length of the car, meters
dt = 0.1 # time difference between timestep (k+1) and timestep k, second
    ''' Nonlinear Vehicle Model Update Equation '''
def nonlinear_vehicle_model(initial_state, inputs, num_steps):
```

```
x = initial_state[0] # x position, meters
        = initial state[1] # y position, meters
   theta = initial_state[2] # heading (wrt x-axis), radians
        = initial state[3] # speed, meters per second
                          # acceleration, meters per second squared
   a = inputs[0]
   phi = inputs[1]
                          # steering angle, radians
   state history = [] # array to hold state values as the time st
   state history.append([x,y,theta,v]) # add the initial state (i.e. k
   for i in range(0, num steps):
       # Find the next state, at time k+1, by applying the nonlinear mo
                = x + v * np.cos(theta) * dt
       y \text{ next} = y + v * np.sin(theta) * dt
       theta_next = theta + v/L * np.tan(phi) * dt
                         + a * dt
                = V
       v next
       # Add the next state to the history.
       state history.append([x next,y next,theta next,v next])
       # Advance to the next state, at time k+1, to get ready for next
       x = x next
       y = y next
       theta = theta next
       v = v next
   return np.array(state history)
''' Linear Vehicle Model Update Equation '''
def linear vehicle model(A, B, initial state, inputs, num steps):
   # Note: A should be a 4x4 matrix, B should be a 4x2 matrix for this
         = initial state[0] # x position, meters
   y = initial state[1] # y position, meters
   theta = initial state[2] # heading (wrt x-axis), radians
        = initial state[3] # speed, meters per second
                           # acceleration, meters per second squared
   a = inputs[0]
   phi = inputs[1]  # steering angle, radians
                          # array to hold state values as the time st
   state history = []
   state history.append([x,y,theta,v]) # add the initial state (i.e. k
   for i in range(0, num steps):
       # Find the next state, at time k+1, by applying the nonlinear mo
       state next = np.dot(A, state history[-1]) + np.dot(B, inputs)
       # Add the next state to the history.
       state history.append(state next)
```

```
# Advance to the next state, at time k+1, to get ready for next
state = state_next

return np.array(state_history)

''' Plotting Setup'''

def make_model_comparison_plot(state_predictions_nonlinear, state_predictions_f = plt.figure()
    plt.plot(state_predictions_nonlinear[0,0], state_predictions_nonline
    plt.plot(state_predictions_nonlinear[:,0], state_predictions_nonline
    plt.plot(state_predictions_linear[:,0], state_predictions_linear[:,1
    plt.legend(loc='upper left')
    plt.xlim([4, 8])
    plt.ylim([9, 12])
    plt.show()
```

Part B

Task: Fill in the matrices A and B for the linear system approximating the nonlinear vehicle model under small heading and steering angle approximations.

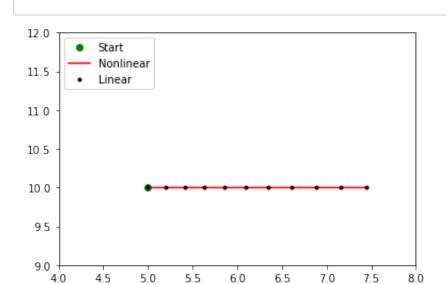
Part C

Task: Fill out the state and input values from Part C and look at the resulting plot. The plot should help you to visualize the difference between using a linear model and a nonlinear model for this specific starting state and input.

```
In [6]: # Your code here.
    x_init = 5
    y_init = 10
    theta_init = 0
    v_init = 2
    a_input = 1
    phi_input = 0.0001

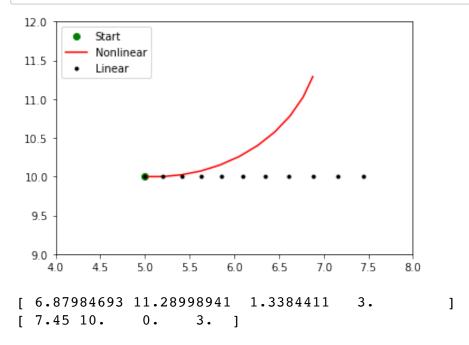
state_init = [x_init, y_init, theta_init, v_init]
    state_predictions_nonlinear = nonlinear_vehicle_model(state_init, [a_input_input])
    state_predictions_linear = linear_vehicle_model(A, B, state_init, [a_input_input])
```

make_model_comparison_plot(state_predictions_nonlinear, state_prediction



Part D

Task: Fill out the state and input values from Problem D and look at the resulting plot. The plot should help you to visualize the difference between using a linear model and a nonlinear model for this specific starting state and input.



In []: