

Natural Language Processing CMSC 723 (spring, 2001)

April 11, 2001

- Review of Dynamic Programming
- Dotted Rule Notation
- Earley Algorithm
- Complexity of Earley
- Key to Efficiency

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Dynamic Programming and Parsing

Use a table of size $n + 1$. The table entries sit in the gaps between the words:

- Completed constituents
- In-progress constituents
- Predicted constituents

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Dynamic Programming

We want an algorithm that fills a table with solutions to subproblems that:

- Does not do repeated work
- Does top-down search with bottom-up filtering (sort of)
- Solves the left-recursion problem
- Solves an exponential problem in $O(n^3)$ time.

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States

$S \rightarrow \bullet VP$
 $NP \rightarrow Det \bullet Nominal$
 $VP \rightarrow V NP \bullet$

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States cont.

Keep track of:

- What word it is currently processing.
- Where it is in the processing of the current rule.
- Where it should return to when done w/ current rule.

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Graphical States

[Figure 10.15]

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States cont.

Parse: "Book that flight."

$S \rightarrow \bullet VP, [0,0]$
 $NP \rightarrow Det \bullet Nominal, [1,2]$
 $VP \rightarrow V NP \bullet, [0,3]$

Each State s_i : <dotted rule>, [<back pointer>,<current posn>]

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Success

$Start \rightarrow \alpha \bullet, [nil,n]$

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Parsing

- New predicted states are based on existing table entries that predict a certain constituent at that spot.
- New in-progress states are created by updating older states.
- New complete states are created when the dot moves to the end.

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Toward an Efficient Parsing Algorithm: Earley (1970)

Top-down parser with bottom-up filtering.

- Ambiguity
- Left recursion
- Repeated parsing of subtrees

What is the key to addressing these issues?

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Memoization and Dynamic Programming

- Use tables to keep track of previously solved sub-problems.
- Dynamic programming algorithms: oriented around systematically filling these tables.
- Memoization: achieves the same results but allows the algorithm to do so more efficiently.

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States and State Sets

Dotted Rule: **State** s_i is represented as <dotted rule>, [<back pointer>, <current posn>]

Define: **State Set** S_j to be a collection of states s_i with the same <current position>.

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Earley Algorithm

[Figure 10.16]

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Basic operations of the Earley Algorithm

- Predictor
- Completer
- Scanner

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Earley Algorithm (easier to read!)

- Add initial state in dotted form: S_o
Start $\rightarrow \bullet S, [nil, 0]$
- Apply predict/complete until no more states are added (closure under predict/complete).
- For each word W_i ($i = 1, \dots, n$), build state set S_i (Main Loop):
 - Apply scan to S_{i-1}
 - Close state set i under predict/complete
 - If state set i is empty, reject; else, continue
- If state set n includes state Start $\rightarrow S \bullet, [nil, n]$ then accept; else reject.

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SCAN Operation

$$S_j: A \rightarrow \alpha \bullet B \beta, [i, j]$$

$$S_{j+1}: A \rightarrow \alpha B \bullet \beta, [i, j + 1]$$

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PREDICT Operation

$S_j: A \rightarrow \alpha \bullet B \beta, [i, j]$

$S_j: B \rightarrow \bullet \gamma, [j, j]$

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Example

[Figure 10.17a]

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COMPLETE Operation

(Much more complicated! Relies heavily on return address.)

$S_k: B \rightarrow \delta \bullet, [j, k]$

$S_k: A \rightarrow \alpha B \bullet \beta, [i, k],$

where:

$S_j: A \rightarrow \alpha \bullet B \beta, [i, j]$

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Example (continued)

[Figure 10.17b]

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Example (continued)

[Figure 10.17c]

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Complexity Analysis of Earley

1. How many state sets will there be?
2. How big can the state sets get?

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Another Earley Algorithm Example

Grammar: $S \rightarrow NP VP$, $NP \rightarrow N$, $VP \rightarrow V NP$

Input: I saw Mary

S_0	Word: NIL
S_1	Word: I (N)
S_2	Word: saw (V,N)
S_3	Word: Mary (N)

Sentence Accepted.

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Analysis of SCAN, PREDICT, COMPLETE

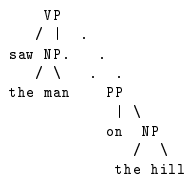
- Scan:
 $S_j: A \rightarrow \alpha \bullet B \beta, [i, j]$
 $S_{j+1}: A \rightarrow \alpha B \bullet \beta, [i, j + 1]$
- Predict:
 $S_j: A \rightarrow \alpha \bullet B \beta, [i, j]$
 $S_j: B \rightarrow \bullet \gamma, [j, j]$
- Complete:
 $S_k: B \rightarrow \delta \bullet, [j, k]$
 $S_k: A \rightarrow \alpha B \bullet \beta, [i, k]$,
 where:
 $S_j: A \rightarrow \alpha \bullet B \beta, [i, j]$

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Effect of Ambiguity on Earley Processing Time

How many ways can we complete a phrase of a given rule in a given state?

Example: I saw the man on the hill



$VP \rightarrow V NP \bullet, [j, i]$

$VP \rightarrow V NP PP \bullet, [k, i]$

$S \rightarrow NP VP \bullet, [l, i]$ (from state set j)

$S \rightarrow NP VP \bullet, [m, i]$ (from state set k)

Unambiguous grammar: $O(n^2)$.

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Key to Efficiency for Earley

- Why efficient?
- Other parsers?
- No grammar conversion.
- Additional efficiency measures
- Efficient for unambiguous grammars.

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Effect of Grammar Size on Earley Processing Time

Why is grammar size included?

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Local Ambiguity

Suppose we're parsing the VP "gave Mary a book" using the following rules:

$S \rightarrow VP$
 $VP \rightarrow V$
 $VP \rightarrow V NP$
 $VP \rightarrow V NP PP$
 $VP \rightarrow V NP NP$

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Global Ambiguity

Suppose we're parsing the VP "I shot an elephant in my pajamas" ...

[Figure 10.11]

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Left Recursion

What about parsing the NP "a flight from denver to boston" with the following rules:

NP \rightarrow NP PP
NP \rightarrow Det Nominal
NP \rightarrow ProperNoun

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Left Recursion

$A \rightarrow \bullet A B$

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