

Imágenes

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1 Imágenes

1.1 Introducción

En estas notas se crearon usando ipython 2.0 con la opción notebook, junto con las librerías scipy y numpy para realizar operaciones sobre las imágenes, la librería matplotlib para visualizar las imágenes. Es importante notar que para manipular imágenes en python una de las librerías más usadas es PIL, sin embargo, esta no se actualiza frecuentemente y solo funciona con python 2.7, por lo que se usará PILLOW que es un fork de PIL y sí funciona con python 3.

A continuación se da un ejemplo de cómo cargar una imagen en python.

```
In [2]: from scipy import misc
        l = misc.lena()
        #misc.imsave('lena.png', l) # Con esta instrucción se graba la imagen a disco, es usada por PIL
        l.shape, l.dtype
        import matplotlib.pyplot as plt
        import matplotlib.image as mpimg
        import matplotlib.cm as cm
        import numpy as np

        #Esta instrucción le dice a ipython que las imágenes las ponga dentro del mismo notebook
        # y no como una ventana independiente
        %matplotlib inline
        plt.figure(figsize=(14,10), dpi=300)
        plt.imshow(l, cmap=cm.Greys_r) #Es necesario avisar que se usará una imagen escala de grises en
        plt.show()
```



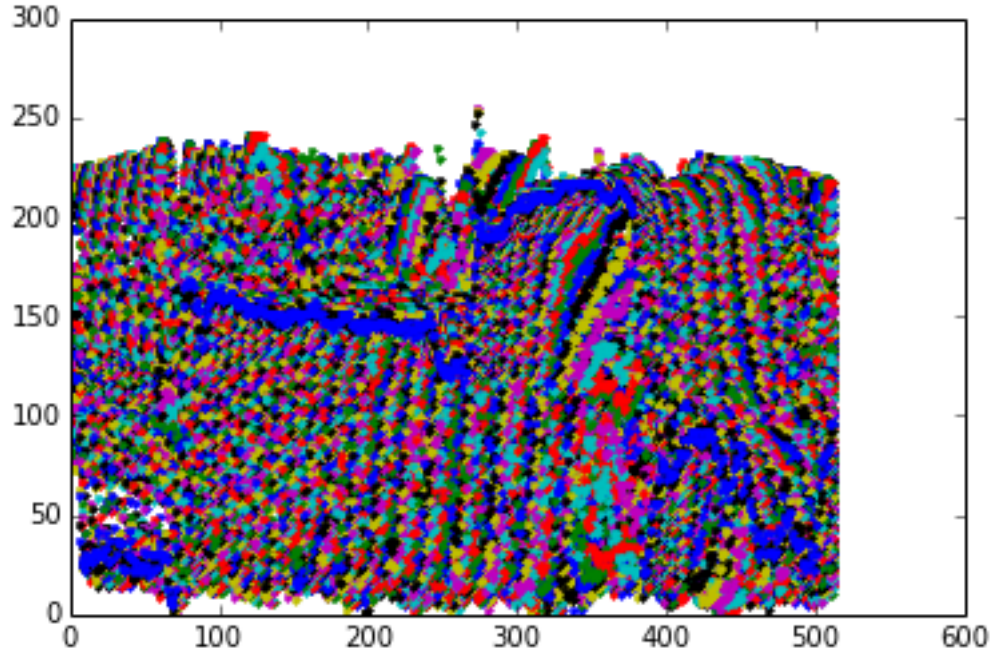
```
In [7]: from PIL import Image
        im = Image.open('lena.png')
        im2=im.convert('RGB') #Otro metodo es abrir la imagen es usando PIL convertir la imagen a RGB
        plt.figure(figsize=(14,10), dpi=300)
        plt.imshow(im2)
        plt.show()
```



```
In [8]: im2.size
```

```
Out[8]: (512, 512)
```

```
In [14]: im3=np.asarray(im2)
          im3.shape
          plt.plot(im3[:, :, 1], '.r')
          plt.show()
```



1.2 Interpolación

Interpolation is a basic tool used extensively in tasks such as zooming, shrinking, rotating, and geometric corrections. It introduces interpolation and applies it to image resizing (shrinking and zooming), which are basically image resampling methods.

Fundamentally, interpolation is the process of using known data to estimate values at unknown locations. We begin the discussion of this topic with a simple example. Suppose that an image of size 500 x 500 pixels has to be enlarged 1.5 times to 750 x 750 pixels. A simple way to visualize zooming is to create an imaginary 750 X 750 grid with the same pixel spacing as the original, and then shrink it so that it fits exactly over the original image. Obviously, the pixel spacing in the shrunken 750 X 750 grid will be less than the pixel spacing in the original image. To perform intensity-level assignment for any point in the overlay, we look for its closest pixel in the original image and assign the intensity of that pixel to the new pixel in the 750 X 750 grid. When we are finished assigning intensities to all the points in the overlay grid, we expand it to the original specified size to obtain the zoomed image.

The method just discussed is called **nearest neighbor interpolation** because it assigns to each new location the intensity of its nearest neighbor in the original image. This approach is simple but, it has the tendency to produce undesirable artifacts, such as severe distortion of straight edges. For this reason, it is used infrequently in practice. A more suitable approach is bilinear interpolation, in which we use the four nearest neighbors to estimate the intensity at a given location. Let (x, y) denote the coordinates of the location to which we want to assign an intensity value (think of it as a point of the grid described previously), and let $v(x, y)$ denote that intensity value. For bilinear interpolation, the assigned value is obtained using the equation

$$v(x, y) = ax + by + cxy + d \quad (1)$$

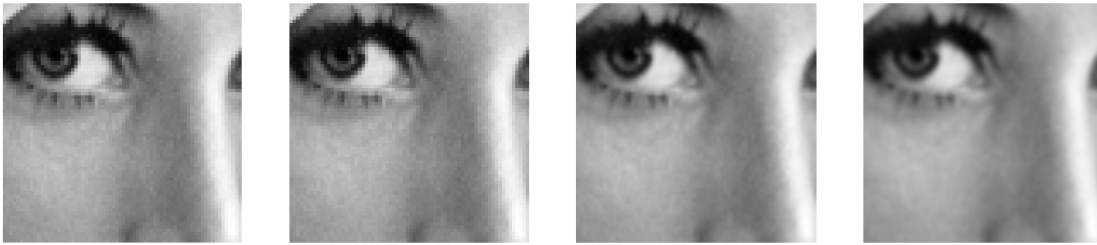
where the four coefficients are determined from the four equations in four unknowns that can be written using the four nearest neighbors of point (x, y) .

The next level of complexity is bicubic interpolation, which involves the sixteen nearest neighbors of a point. The intensity value assigned to point (x, y) is obtained using the equation

$$v(x, y) = \sum_{i=0}^3 \sum_{j=0}^3 a_{ij} x^i y^j \quad (2)$$

where the sixteen coefficients are determined from the sixteen equations in sixteen unknowns that can be written using the sixteen nearest neighbors of point (x, y) .

```
In [4]: plt.figure(figsize=(24,20), dpi=300)
plt.subplot(141)
plt.imshow(l[250:320, 250:320], cmap=plt.cm.gray, interpolation='none')
plt.axis('off')
plt.subplot(142)
plt.imshow(l[250:320, 250:320], cmap=plt.cm.gray, interpolation='nearest')
plt.axis('off')
plt.subplot(143)
plt.imshow(l[250:320, 250:320], cmap=plt.cm.gray, interpolation='bilinear')
plt.axis('off')
plt.subplot(144)
plt.imshow(l[250:320, 250:320], cmap=plt.cm.gray, interpolation='bicubic')
plt.axis('off')
plt.show()
```



It is possible to use more neighbors in interpolation, and there are more complex techniques, such as using splines and wavelets, that in some instances can yield better results than the methods just discussed.

1.3 Neighbors of a Pixel

A pixel p at coordinates (x, y) has four horizontal and vertical neighbors whose coordinates are given by

$$(x + 1, y), (x - 1, y), (x, y + 1), (x, y - 1)$$

1.3.1 Transformaciones

- Escalamiento

$$x = C_x V \quad (3)$$

$$y = C_y w \quad (4)$$

- Rotación

$$x = v \cos(\theta) + w \sin(\theta) \quad (5)$$

$$y = v \sin(\theta) + w \cos(\theta) \quad (6)$$

- Translación

$$x = v + t_x \tag{7}$$

$$y = w + t_x \tag{8}$$