INDIAN INSTITUTE OF ENGINEERING SCIENCE AND TECHNOLOGY, SHIBPUR B.TECH IT 5TH SEMESTER FINAL SEMESTER EXAMINATION 2021 SUBJECT – INFORMATION AND CODING THEORY (IT 3105)

Full Marks = 50 Time: 90 mins

(Answer <u>Q1</u> and <u>any two</u> questions from the rest. Write your name and roll number on the front page. Scan your answer script, make a single .pdf file of your answer script and upload in the google classroom.)

- 1. Write short notes on:
 - (a) Channel capacity and Shannon limit for a Gaussian Channel
 - (b) Space time code

5 + 5 = 10

- 2. (a) Consider a source with number of levels/msg M = 3 with probabilities 0.5, 0.4, 0.1. Perform prefix free tree coding with block size n = 2. Find source entropy, decodability and optimality of the coding.
 - (b) For the Markov source given below, find individual source entropy, average source entropy. Draw the tree diagram. Find the probability of occurrence of the symbols AAA, ACB, ACC and BBB.

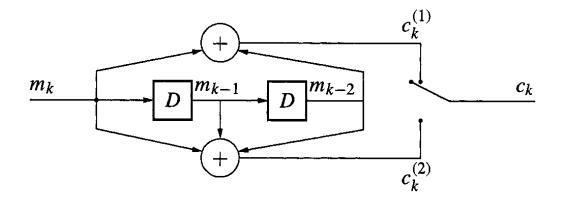
$$8 + 12 = 20$$

- 3. (a) Define a priory and a posteriory entropy of a noisy transmission channel with U input symbols and V output symbols. Design the channel matrix.
 - (b) For a Binary symmetric channel with α as the source probability and p as the channel error probability, calculate average mutual information (I). Then compute the maximum and minimum value of I. Explain your answer.

$$5 + 15 = 20$$

- 4. (a) What is Hamming Distance? Give example.
 - (b) Derive Hamming bound.
 - (c) For a (7, 3) systematic code with parity check matrix given below, compute the syndrome decoding table. For a received word $r = [0\ 0\ 1\ 1\ 0\ 1\ 1]$ detect and correct error if there is any.

$$5 + 5 + 15 = 20$$



- 5. (a) A convolutional encoder is given above. Find the code rate and constraint length of the encoder.
 - (b) For the input stream $m = [1 \ 1 \ 0 \ 0 \ 1 \ 0 \ 1]$ find the coded sequence.
 - (c) Draw the Trellis diagram for the encoder.

$$5 + 5 + 10 = 20$$