

11-1 MESSAGE INTEGRITY

The cryptography systems that we have studied so far provide secrecy, or confidentiality, but not integrity. However, there are occasions where we may not even need secrecy but instead must have integrity.

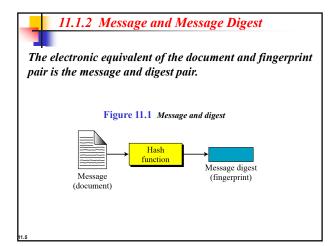
Topics discussed in this section:

- 11.1 Document and Fingerprint
- 11.2 Message and Message Digest
- 11.3 Difference
- 11.4 Checking Integrity
- 11.5 Cryptographic Hash Function Criteria

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11.1.1 Document and Fingerprint

One way to preserve the integrity of a document is through the use of a fingerprint. If Alice needs to be sure that the contents of her document will not be changed, she can put her fingerprint at the bottom of the document.



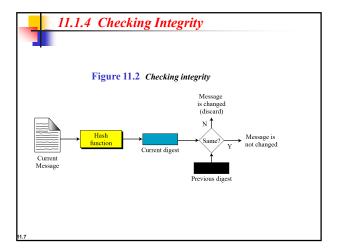
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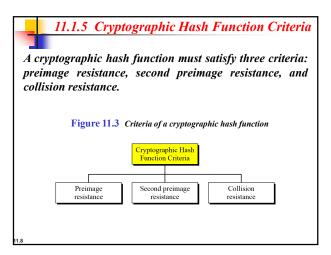
11.1.3 Difference

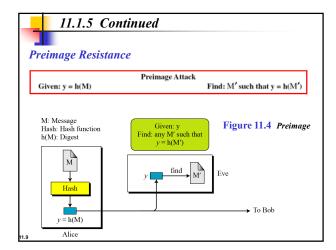
The two pairs (document / fingerprint) and (message / message digest) are similar, with some differences. The document and fingerprint are physically linked together. The message and message digest can be unlinked separately, and, most importantly, the message digest needs to be safe from change.

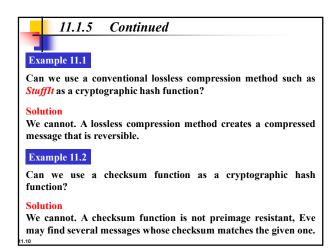


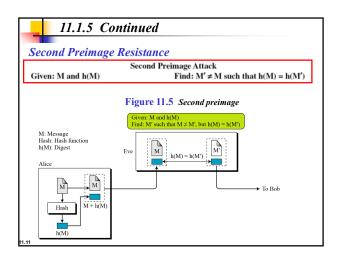
The message digest needs to be safe from change.

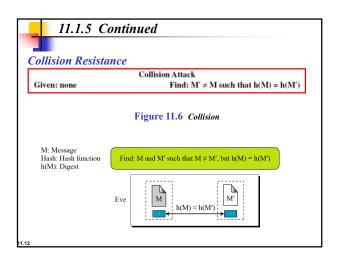












11-2 RANDOM ORACLE MODEL

The Random Oracle Model, which was introduced in 1993 by Bellare and Rogaway, is an ideal mathematical model for a hash function.

Topics discussed in this section:

11.2.1 Pigeonhole Principle

11.2.2 Birthday Problems

11.2.3 Attacks on Random Oracle Model

11.2.4 Attacks on the Structure

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11-2 Continued

Example 11.3

Assume an oracle with a table and a fair coin. The table has two columns.

Table 11.1 Oracle table after issuing the first three digests

Message	Message Digest
4523AB1352CDEF45126	13AB
723BAE38F2AB3457AC	02CA
AB45CD1048765412AAAB6662BE	A38B

a. The message AB1234CD8765BDAD is given for digest calculation. The oracle checks its table.

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11-2 Continued

Example 11.3 Continued

Table 11.2 Oracle table after issuing the fourth digest

Message	Message Digest
4523AB1352CDEF45126	13AB
723BAE38F2AB3457AC	02CA
AB1234CD8765BDAD	DCB1
AB45CD1048765412AAAB6662BE	A38B

b. The message 4523AB1352CDEF45126 is given for digest calculation. The oracle checks its table and finds that there is a digest for this message in the table (first row). The oracle simply gives the corresponding digest (13AB).

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11-2 Continued

Example 11.4

The oracle in Example 11.3 cannot use a formula or algorithm to create the digest for a message. For example, imagine the oracle uses the formula $h(M) = M \mod n$. Now suppose that the oracle has already given h(M1) and h(M2). If a new message is presented as M3 = M1 + M2, the oracle does not have to calculate the h(M3). The new digest is just $[h(M1) + h(M2)] \mod n$ since

 $h(M_3) = (M_1 + M_2) \mod n = M_1 \mod n + M_2 \mod n = [h(M_1) + h(M_2)] \mod n$

This violates the third requirement that each digest must be randomly chosen based on the message given to the oracle.

11.1



11.2.1 Pigeonhole Principle

If n pigeonholes are occupied by n+1 pigeons, then at least one pigeonhole is occupied by two pigeons. The generalized version of the pigeonhole principle is that if n pigeonholes are occupied by k+1 pigeons, then at least one pigeonhole is occupied by k+1 pigeons.

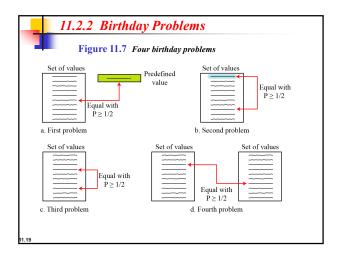


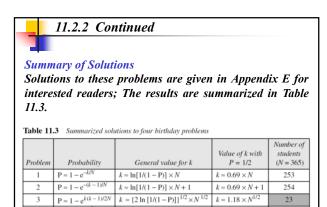
11.2.1 Continued

Assume that the messages in a hash function are 6 bits long and the digests are only 4 bits long. Then the possible number of digests (pigeonholes) is $2^4 = 16$, and the possible number of messages (pigeons) is $2^6 = 64$. This means n = 16 and kn + 1 = 64, so k is larger than 3. The conclusion is that at least one digest corresponds to four (k+1) messages.

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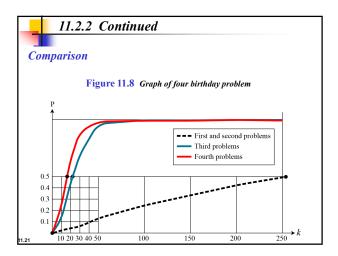


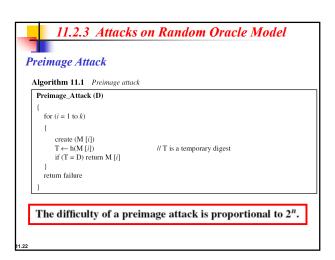
 $k \approx \{\ln [1/(1-P)]\}^{1/2} \times N^{1/2}$

 $P \approx 1 - e^{-k^2/2N}$

 $k \approx 1.18 \times N^{1/2}$

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11.2.3 Continued

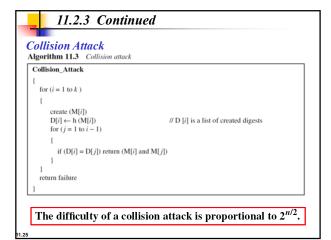
Example 11.6

A cryptographic hash function uses a digest of 64 bits. How many digests does Eve need to create to find the original message with the probability more than 0.5?

Solution

The number of digests to be created is $k \approx 0.69 \times 2^n \approx 0.69 \times 2^{64}$. This is a large number. Even if Eve can create 230 (almost one billion) messages per second, it takes 0.69 \times 2³⁴ seconds or more than 500 years. This means that a message digest of size 64 bits is secure with respect to preimage attack, but, as we will see shortly, is not secured to collision attack.

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11.2.3 Continued
Second Preimage Attack.
Algorithm 11.2 Second preimage attack
 Second Preimage Attack (D, M)
   for (i = 1 \text{ to } k - I)
      create (M [i])
       T \leftarrow h (M [i])
                                     // T is a temporary digest
      if (T = D) return M[i]
    The difficulty of a second preimage attack is proportional to 2^n.
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11.2.3 Continued

Example 11.7

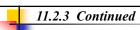
A cryptographic hash function uses a digest of 64 bits. How many digests does Eve need to create to find two messages with the same digest with the probability more than 0.5?

Solution

The number of digests to be created is $k \approx 1.18 \times 2^{n/2} \approx 1.18 \times 2^{32}$. If Eve can test 2^{20} (almost one million) messages per second, it takes 1.18×2^{12} seconds, or less than two hours. This means that a message digest of size 64 bits is not secure against the collision attack

11.2

Alternate Collision Attack Algorithm 11.4 Alternate collision attack Alternate_Collision_Attack (M [k], M'[k]) { for (i = 1 to k) { D[i] \leftarrow h (M[i]) D[i] \leftarrow h (M'[i]) if (D [i] = D'[j]) return (M[i], M'[j]) } return failure } The difficulty of an alternative collision attack is proportional to $2^{n/2}$.



Summary of Attacks

Table 11.4 shows the level of difficulty for each attack if the digest is n bits.

Table 11.4 Levels of difficulties for each type of attack

Attack	Value of k with P=1/2	Order
Preimage	$k \approx 0.69 \times 2^n$	2^n
Second preimage	$k \approx 0.69 \times 2^n + 1$	2^n
Collision	$k \approx 1.18 \times 2^{n/2}$	$2^{n/2}$
Alternate collision	$k \approx 0.83 \times 2^{n/2}$	$2^{n/2}$

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11.2.3 Continued

Example 11.8

Originally hash functions with a 64-bit digest were believed to be immune to collision attacks. But with the increase in the processing speed, today everyone agrees that these hash functions are no longer secure. Eve needs only $2^{64/2}=2^{32}$ tests to launch an attack with probability 1/2 or more. Assume she can perform 2^{20} (one million) tests per second. She can launch an attack in $2^{32}/2^{20}=2^{12}$ seconds (almost an hour).

11.2.3 Continued

Example 11.9

MD5 (see Chapter 12), which was one of the standard hash functions for a long time, creates digests of 128 bits. To launch a collision attack, the adversary needs to test 2⁶⁴ (2¹²⁸/2) tests in the collision algorithm. Even if the adversary can perform 2³⁰ (more than one billion) tests in a second, it takes 2³⁴ seconds (more than 500 years) to launch an attack. This type of attack is based on the Random Oracle Model. It has been proved that MD5 can be attacked on less than 2⁶⁴ tests because of the structure of the algorithm.

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11.2.3 Continued

Example 11.10

SHA-1 (see Chapter 12), a standard hash function developed by NIST, creates digests of 160 bits. The function is attacks. To launch a collision attack, the adversary needs to test $2^{160/2} = 2^{80}$ tests in the collision algorithm. Even if the adversary can perform 2^{30} (more than one billion) tests in a second, it takes 2^{50} seconds (more than ten thousand years) to launch an attack. However, researchers have discovered some features of the function that allow it to be attacked in less time than calculated above.

11.2.3 Continued

Example 11.11

The new hash function, that is likely to become NIST standard, is SHA-512 (see Chapter 12), which has a 512-bit digest. This function is definitely resistant to collision attacks based on the Random Oracle Model. It needs $2^{512/2} = 2^{256}$ tests to find a collision with the probability of 1/2.

11.32



11.2.4 Attacks on the Structure

The adversary may have other tools to attack hash function. One of these tools, for example, is the meet-in-the-middle attack that we discussed in Chapter 6 for double DES.

11-3 MESSAGE AUTHENTICATION

A message digest does not authenticate the sender of the message. To provide message authentication, Alice needs to provide proof that it is Alice sending the message and not an impostor. The digest created by a cryptographic hash function is normally called a modification detection code (MDC). What we need for message authentication is a message authentication code (MAC).

Topics discussed in this section:

11.3.1 Modification Detection Code (MDC)

11.3.2 Message Authentication Code (MAC)

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11.3.1 Modification Detection Code (MDC)

A modification detection code (MDC) is a message digest that can prove the integrity of the message: that message has not been changed. If Alice needs to send a message to Bob and be sure that the message will not change during transmission, Alice can create a message digest, MDC, and send both the message and the MDC to Bob. Bob can create a new MDC from the message and compare the received MDC and the new MDC. If they are the same, the message has not been changed.

Figure 11.9 Modification detection code (MDC)

Alice

Insecure channel

M: Message
Hash: Cryptographic hash function
MDC: Modification detection code

M: Message
Hash: Cryptographic hash function
MDC: Modification detection code

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