

AUTHENTICATION FUNCTIONS

Authentication → verifying the user's identity

Raman → John

An authenticator must be there to authenticate the message.

Types of Authentication | Types of fn to produce authentication

- (i) Message Encryption (ciphertext act as authenticator)
- (ii) MAC (message authentication code)
→ we will have some authentication fn and
we apply them on the plaintext along
with the key which produces a fixed

~~ator~~
be used to
sg

(ii) Message Authentication Code (MAC) (ciphertext act as authentication code)
→ we will have some authentication fn and
we apply them on the plaintext along
with the key which produces a fixed length code called MAC

message
 $c(M, K) \neq$ fixed length code (MAC)
authentication fn key

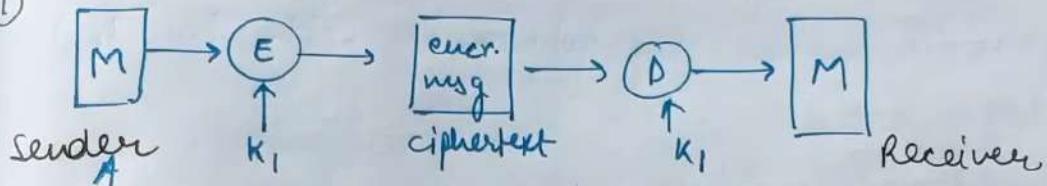
This will act as
an authenticator
here.

(iii) Hash functions (H)

$H(M)$ = fixed length code (Hash code 'h')
independent of Key
act as an
authenticator

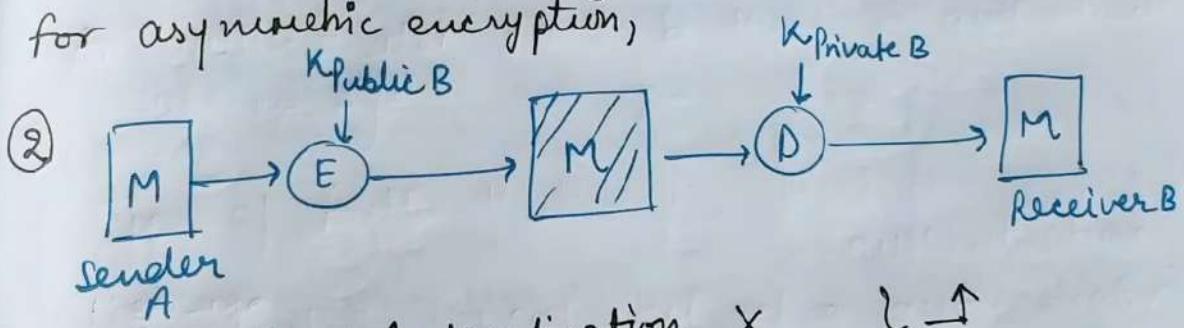
1. Message encryption \rightarrow ciphertext is an authenticator

①

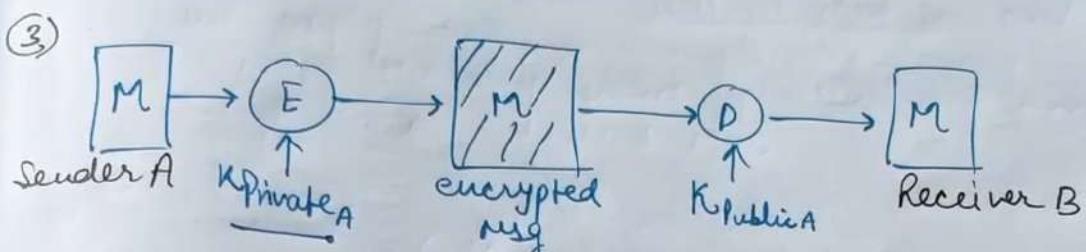


\rightarrow key K_1 shared only b/w sender & receiver only.

for asymmetric encryption,

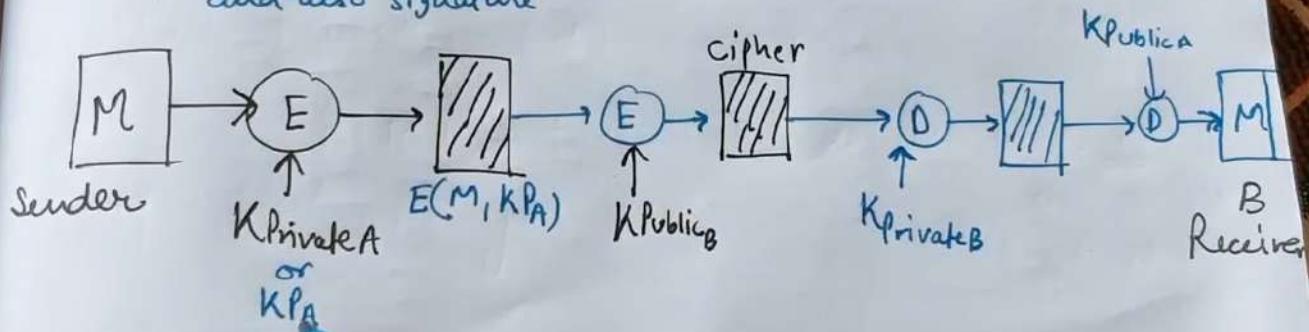


Authentication X
Confidentiality ✓ } \uparrow



authentication ✓
confidentiality X

(4) To get both and also signature



Block cipher modes of operation

for different types of messages, we need different modes of operations.

5 modes of operation are:

- (i) ECB electronic codebook mode
- (ii) CBC cipher block chaining mode
- (iii) CFB cipher feedback mode
- (iv) OFB output feedback mode
- (v) CTR counter mode

ECB (Electronic codebook Mode)

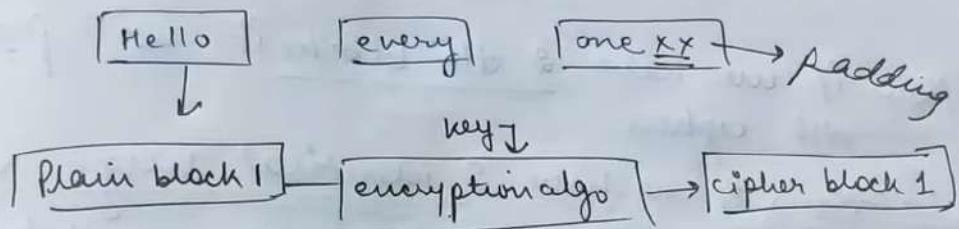
- * simplest mode of operation
- * plain text is divided into a no. of fixed size block.
- * if message is not a multiple of block size, then padding is done

"padding" is done ~~multiple~~ of block size, then

- * Take one block at a time and encrypt it.
- * Same key used for encryption and decryption.

eg] Let block size = 5

Plain Text → Hello everyone

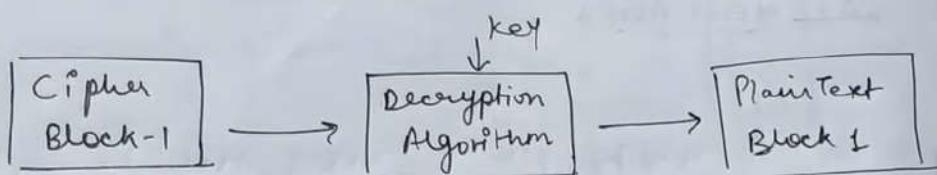


This will happen for all the ~~blocks~~ blocks.

Note → best for short amount of data, such as a key
→ not secure for lengthy data

④ If identical blocks appear, then this mode produces same cipher.

→ for decryption process



This will happen for every box.

Payphone
one direction

- * If message is over padding is done
- * Take one block
- * Same key used
- * Let block size

Plain Tex

Hello

Plain block

This

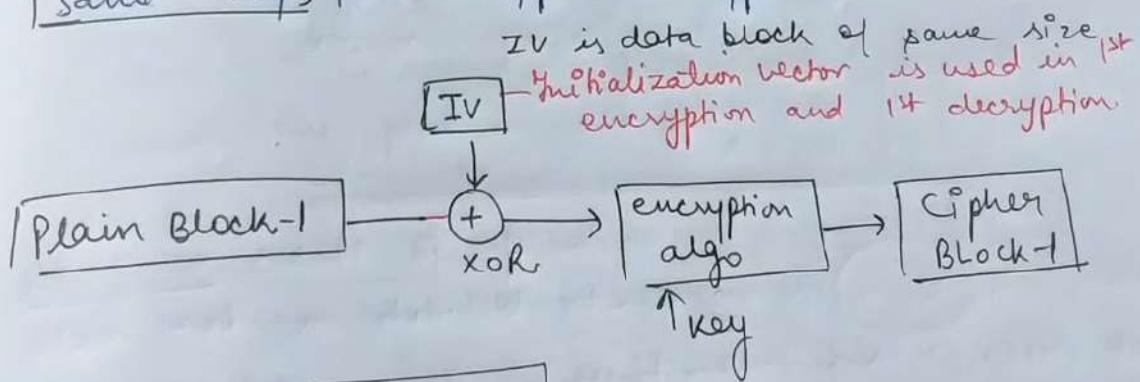
Note →

(ii) CBC cipher block chaining mode

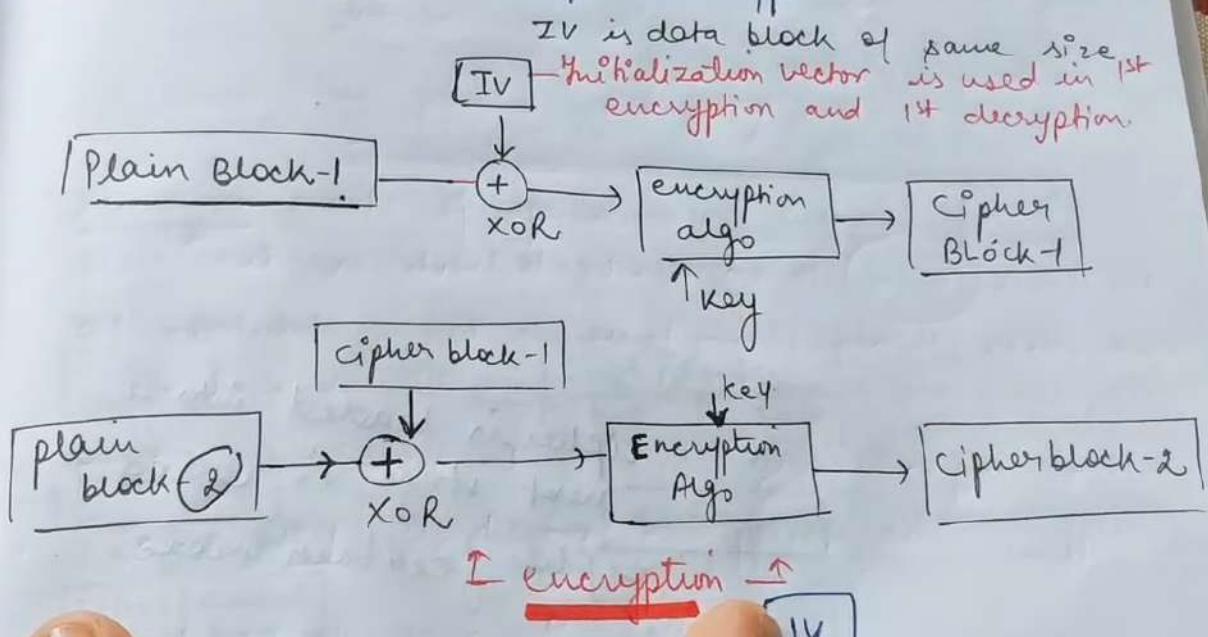
To overcome security issues of ECB mode
(b/c if same blocks appear then cipher text produced will be same).

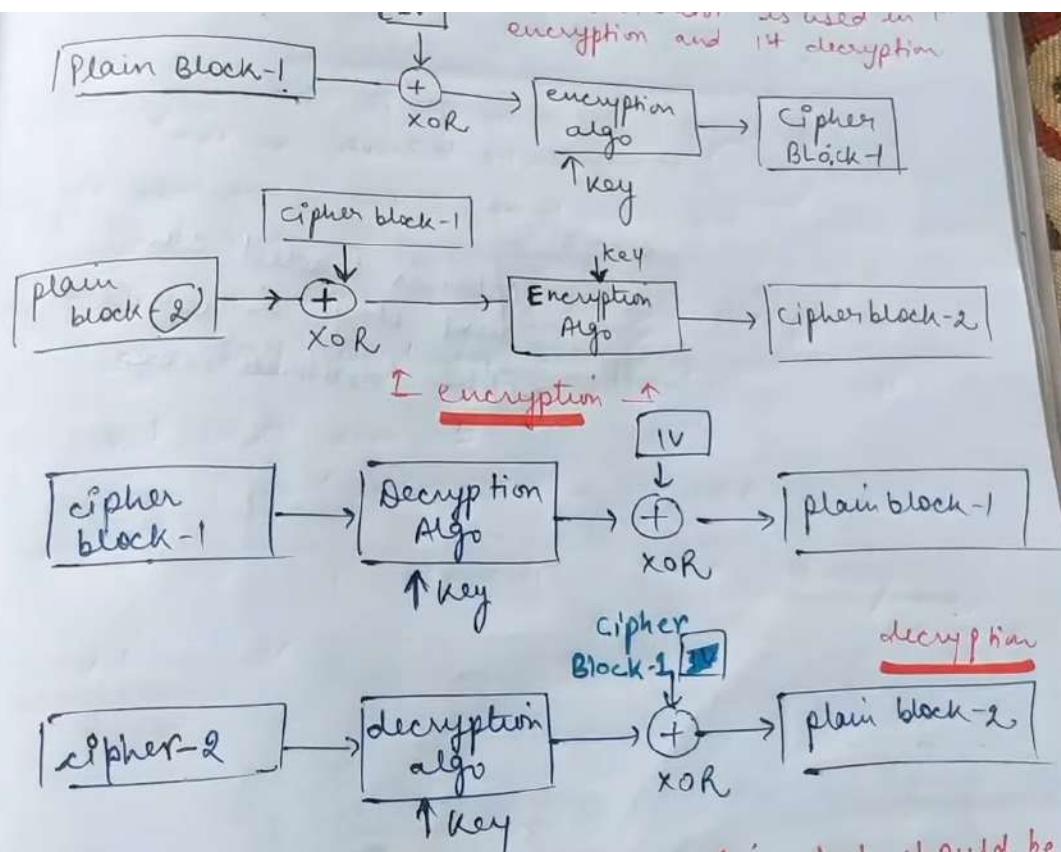
Input to the encryption algo is XOR of the current plaintext block and the preceding ciphertext block. So, repeating patterns not exposed.

same key for encrypt + decrypt.



- (ciphertext produced will be same).
- (i) G/P to the encryption algo is XOR of the current plaintext block and the preceding ciphertext block. So, repeating patterns not exposed.
 - (ii) Same key for encrypt + decrypt.





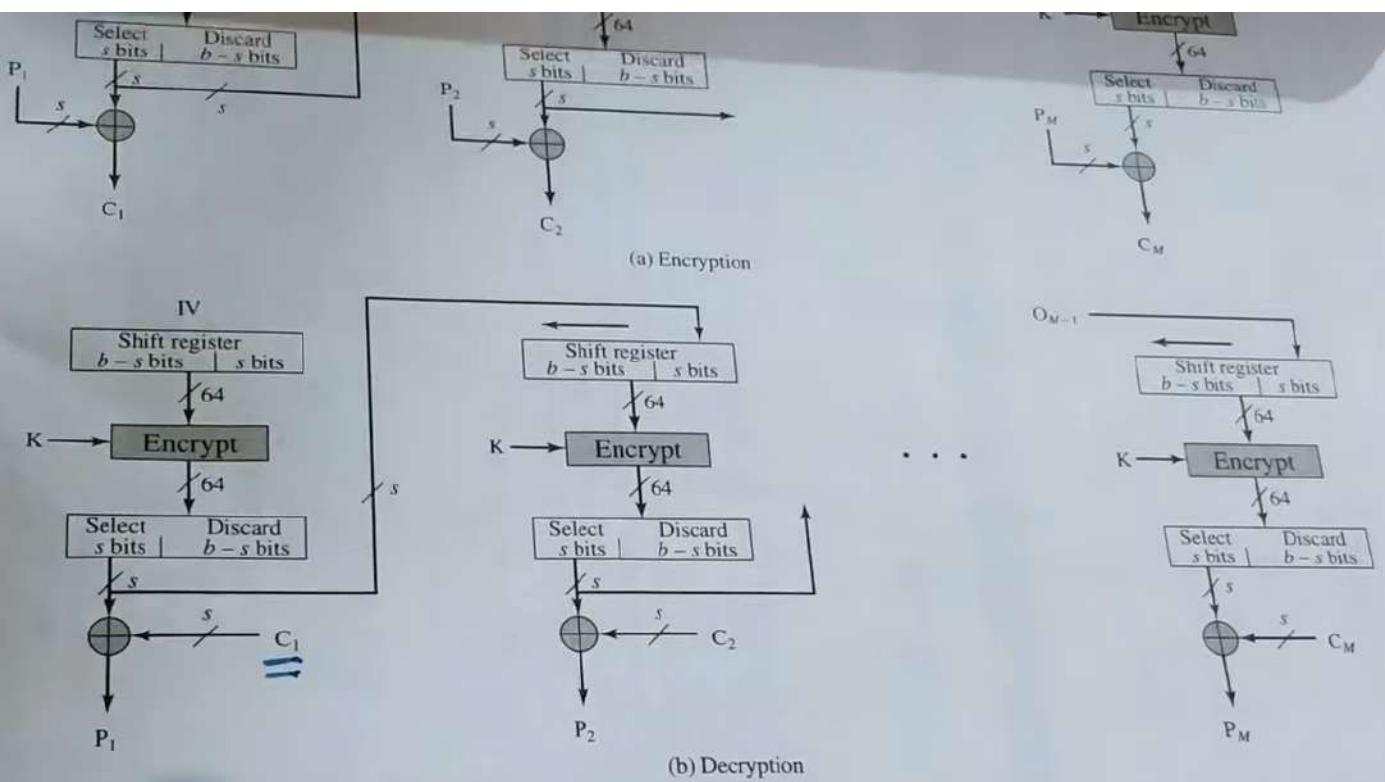


Figure 6.6 *s*-bit Output Feedback (OFB) Mode

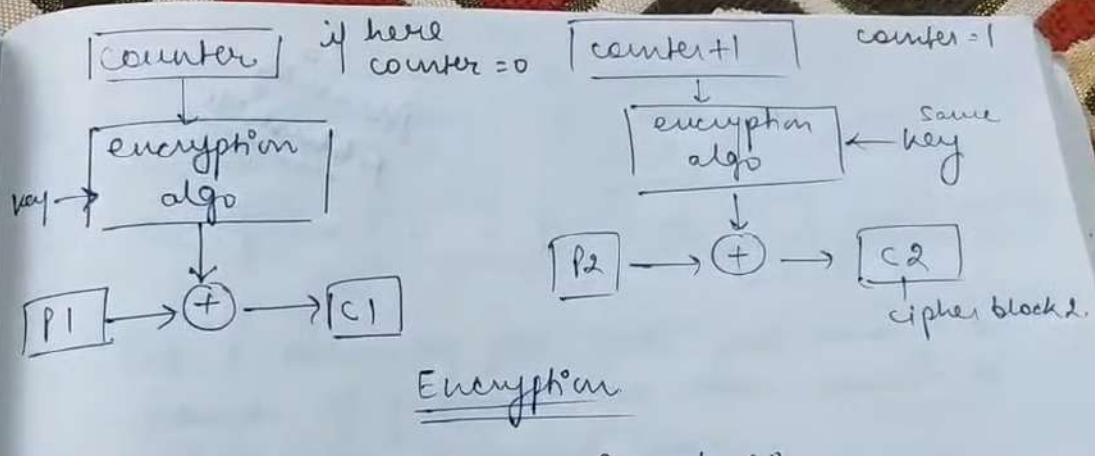


For decryption, c_j and p_j will be exchanged.

5) COUNTER mode [CTR]

- simple and fast
- a counter, equal to the plaintext block size is used.

- ④ counter is initialised to some value and then incremented by 1 for each subsequent block.



for decryption, change P_i and C_i

BLOWFISH ALGORITHM

in CRYPTOGRAPH &
Network Security

- * symmetric key algo.
- * block cipher (64 bit) algo.
- * It is an alternative to DES encryption Technique & IDEA algo.

encryption technique

designed by Bruce Schneier(1993)

Block size / Plain Text in 1 block \rightarrow 64 bit
key size \rightarrow variable (32 to 448) bits
No. of subkeys \rightarrow 18 (P-array) P_0, P_1, \dots, P_{17} \rightarrow 32 bit each
No. of rounds \rightarrow 16
No. of substitution boxes \rightarrow 4 S-boxes
having 256 entries
 \downarrow
each is of 32 bit

Note \rightarrow It follows Feistel structure
Fast, Simple, Secure

1) Generation of subkeys
 \rightarrow 18 subkeys ($P[0] \dots P[17]$) are used for encryption as well as decryption
 \rightarrow 18 subkeys are stored in a P-array with each array element being 32-bit entry.

eg $P[0] = "243f6a68"$ } hexadecimal representation of each
 $P[1] = "8979abf3"$ } subkey.
 \vdots
 $\rightarrow "a7" \text{ as 5 odd}$

* block cipher (64 bit) algo. || designed by Bruce Schneier
* It is an alternative to DES encryption Technique & IDEA algo.

or
as per your convenience

Block size / Plain Text in 1 block \rightarrow 64 bit
Key size \rightarrow variable (32 to 448) bits
No. of subkeys \rightarrow 18 (P-array) P_0, P_1, \dots, P_{17} \rightarrow 32 bit each
No. of rounds \rightarrow 16
No. of substitution boxes \rightarrow 4 S-boxes
having 256 entries
 \downarrow
each is of 32 bit

1) Generation of subkeys
 \rightarrow 18 subkeys ($P[0] \dots P[17]$) are used for encryption as well as decryption
 \rightarrow 18 subkeys are stored in a P-array with each array element being 32-bit entry.

eg
 $P[0] = "243f6a68"$ } hexadecimal representation of each subkey.
 $P[1] = "8979abf3"$
 $P[17] = "c97c5odd"$

Note \rightarrow It follows feistel structure

✓ fast, compact, simple, secure
executes in less memory
 \downarrow
XOR & add operation
 \downarrow
variable length key

Confidentiality → refers to, protecting the information from being accessed by ~~a~~ unauthorized parties.

In other words, only the people who are authorized to do so can gain access to the sensitive data.

Data Integrity → It is the overall completeness, accuracy and consistency of data over its entire life-cycle.

i.e., data must not change during transit, steps must be taken and steps must be

ie, ~~data must be complete, accurate and consistent~~
over its entire life-cycle.

data must not change during transit,
and steps must be taken ~~and steps must be taken~~
~~to ensure that data cannot be altered~~
by unauthorized people.

Authentication → verifying the user's identity.

Authenticity is used to make sure you
really communicate with the actual
person.

DES ANALYSIS

Properties

(i) Avalanche effect → It means a small change in plaintext (or key) should create a significant change in the ciphertext.

DES has been proved to be strong with regard to this property.

e.g. Plain → 0000000000000000
cipher → 4789FD476E82A5F1

Plain → 0000000000000000 1
cipher → 0A4ED5C1SA63FEA3

→ Key used is same
say
key = 22234512987ABB
23

plain → 00000000000000000000000000000000
cipher → 0A4ED5C15A62FEA3

Key used is same
say
key = 22234512987ABB
23

Although, the two plaintexts differ only in 1 bit, ciphertext block differs a lot/significantly.

2. Completeness effect → It means that each bit of the ciphertext needs to depend on many bits on the plaintext.

The confusion and diffusion produced by D-boxes and S-boxes in DES, show a very strong completeness effect.

D.E.S

Data Encryption Standard

- (i) block cipher
- (ii) symmetric cipher (same key for encryption + decryption)
- (iii) 64 bit plain text block
It encrypts the data in blocks of size 64 bits each
- (iv) 16 rounds . each round is a feistel round.

Steps

- (i) Initial permutation
- (ii) 16 feistel rounds
- (iii) swapping / left right swap
- (iv) Final permutation / Inverse initial permutation

Round - 1

Basic structure

64 bit plain text

↓
Initial permutation

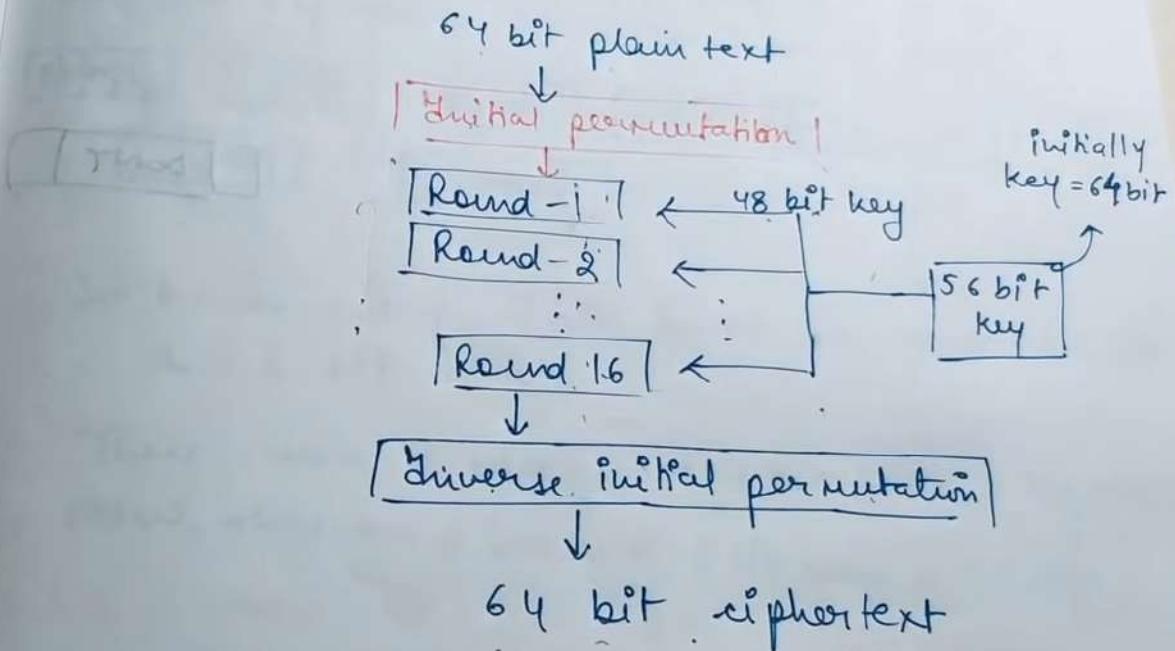
Initially
key = 64 bit

Round - 1

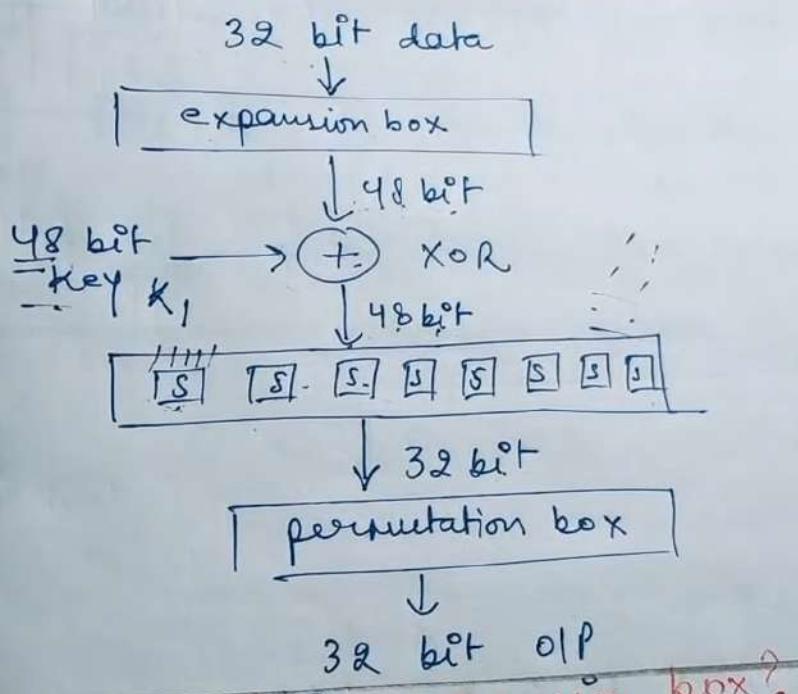
(iv) Final ^{Typing / left} permutation | right swap

Basic structure

inverse initial permutation

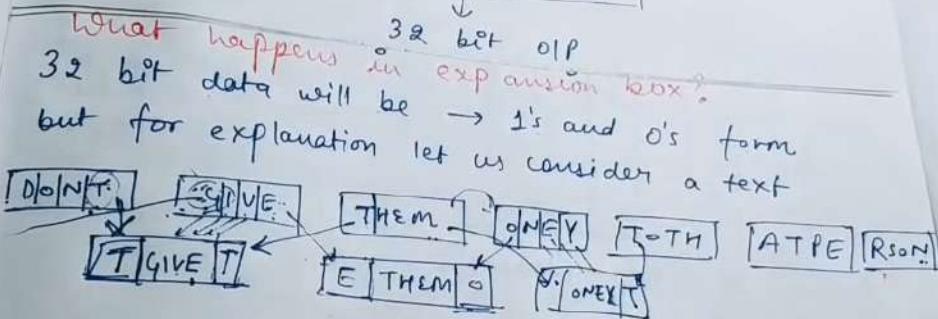
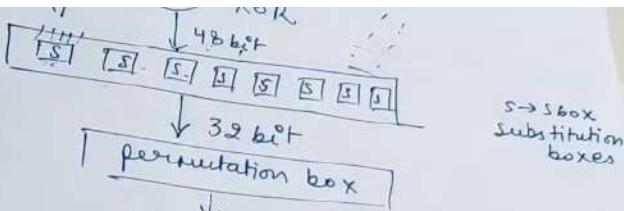


Function definition



S → S box
substitution boxes

What happens in expansion box?



So here every 4 bit block is converted to a 6 bit block

There were 8 blocks of 4 bit each = 32 bit

Now, there are 8 blocks of 6 bit each = 48 bit

Now these 48 bit XOR with 48 bit key

Does what happens in S-boxes?



०११

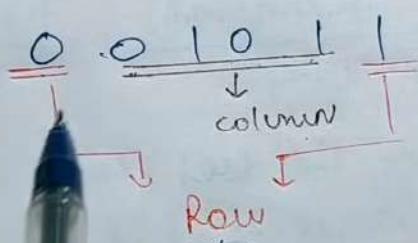
019 → $4 \times 8 = 32$ bits These 32 bits will
go into permutation box.
bit converted to 4 bit?

how 6 bit converted to 4 bit?

→ eg

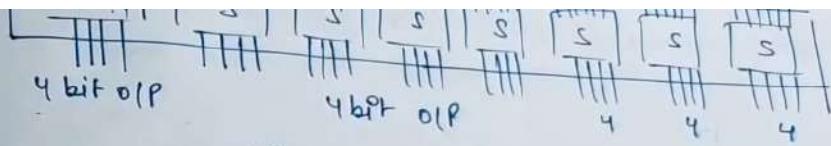
$$0 \mapsto 1$$

0101 → 5.



S₁ box-table 1

| | | | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| 0 | 3 | 5 | 7 | 1 | 4 | - | . | . | . | . | . | . | 1 | 4 | 5 |

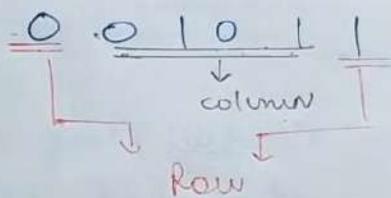


$0111 \quad 01P \rightarrow 4 \times 8 = 32 \text{ bits}$ These 32 bits will go into permutation box.
how 6 bit converted to 4 bit?

eg

$01 \rightarrow 1$

$0101 \rightarrow 5$



S-box - table 1

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
|---|----|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|
| 0 | 3 | 5 | 7 | 0 | 1 | 4 | - | - | - | - | - | - | - | 1 | 4 | 5 |
| 1 | 4 | 2 | 1 | 0 | 9 | 7 | - | - | - | - | - | - | - | 2 | 3 | 6 |
| 2 | 10 | | | | | | | | | | | | | 3 | 4 | 0 |
| 3 | | | | | | | | | | | | | | 11 | 10 | 3 |

$10 \rightarrow 000$

numbers will be filled.

A box will have a diff Table.

DES Weaknesses

• key size

2^{56}

Critics believe that the most serious weakness of DES is its key size of 56 bits.

B/c, with today's technology (like parallel processing and v-powerful processors) it can easily be cracked.

2^{56} keys
(brute force attack)

∴ we use triple DES (3DES) with two keys (112 bits) or triple DES with 3 keys (168 bits).

(ii) Weak Keys → $\boxed{\text{four}}$ out of 2^{56} keys are called weak keys. After the parity drop operation in the one which consists of

completeness
effect

attack

it cipher

S
cipher)

→ we use triple DES (3DES) with 2^{56} keys (brute force attack)
two keys (112 bits) or
triple DES with 3 keys (168 bits).

(iii) Weak Keys → four out of 2^{56} keys are called weak keys.
A weak key is the one which consists of all 0's, all 1's or half 0's and half 1's.

The disadvantage of using a weak key is:

If we encrypt a block with a weak key and subsequently encrypt the result with the same weak key, we get the original block.

The process creates the same original block if we decrypt the block twice.

After 2^{56} deceptions, if the result is the

weak keys. Keys are called weak keys. A weak key is the one which consists of all 0's, all 1's or half 0's and half 1's.

The disadvantage of using a weak key is:

If we encrypt a block with a weak key and subsequently encrypt the result with the same weak key, we get the original block.

The process creates the same original block if we decrypt the block twice.

So, if after 2 decryptions, if the result is the same then, attacker is successful.

(iii) Semi weak keys → six key pairs are called semi-weak keys. (refer book pg 154)

A semi-weak key creates only two different round keys, and thus each of them is repeated 8 times. (show in book pg 155).

(iv) Possible weak keys →⁴⁸ There are 48 keys that are called possible weak keys.

A possible weak key is a key that creates only 4 distinct round keys, in other words, the 16 round keys are divided into 4 groups and each group is made of 4 equal keys.

key $\xrightarrow{K_1}$ but
 $\xrightarrow{K_2}$

(more in book pg 155)

(iv) possible weak keys → 48
There are 48 keys that are called possible weak keys.

A possible weak key is a key that creates only 4 distinct round keys, in other words, the 16 round keys are divided into 4 groups and each group is made of 4 equal keys.

key $\rightarrow k_1$ $\rightarrow k_2$

(v) key clustering
means 2 or more dif keys can create the same ciphertext from the plain text.

Weakness in cipher Design

(i) Two specifically chosen IP's to S-box array can create the same OIP.

... found in design

25
26
27
28

ive root

$$\begin{array}{r} 3 \\ \times 2 \\ \hline 6 \end{array}$$

$$q = 7$$

th of them
eed any
am.
They
Just
use
 x and q .
ch are
een to
all.

$$\begin{array}{r} 17 \\ 7/125 \\ \hline 7 \end{array}$$

$$\begin{array}{r} 55 \\ 99 \\ \hline 6 \end{array}$$

$$625 = 86$$

$$\begin{array}{r} 625 \times 8 \\ \hline 27 \end{array}$$

$$\begin{array}{r} 3125 \\ 7 \end{array} = 446$$

current
ario
diagram)

thus we go to
key concept)
When we are sending a key to receiver, it
can be attacked in b/w.

ALGORITHM

- consider a prime number 'q'
- select α such that it must be the primitive root of q and $\alpha < q$

' α ' is a primitive root of q if

$$\alpha^1 \pmod{q}$$

$$\alpha^2 \pmod{q}$$

$$\alpha^3 \pmod{q}$$

$$\dots \alpha^{q-1} \pmod{q}$$

gives results $\{1, 2, 3, \dots, q-1\}$

i.e. values shouldn't be repeated & we should have all values in the off set from 1 to $q-1$.
(show example).

exchange algorithm

primitive root

$$\begin{array}{l}
 = 3 \\
 = 2 \\
 = 6 \\
 = 4 \\
 = 5 \\
 = 1
 \end{array}
 \quad \alpha = 7$$

$$17 \\ 7/11$$

$$\begin{array}{r}
 125 \\
 7 \\
 \hline
 625 \\
 7 \\
 \hline
 86
 \end{array}$$

Let $q = 7$ (prime)

$\therefore \alpha < q$ i.e. it is a primitive root

Let $\alpha = 5$ we can take any of the two primitive root 3 or 5.

α and $q \rightarrow$ global public elements (known to everyone) key and $X_A < q$

Key generation of person 1

Assume ~~private~~ key $X_A = 3 \quad \because (X_A < q, 3 < 7 \text{ yes})$

calculating public key $Y_A = \alpha^{X_A} \text{ mod } q$

$$Y_A = 5^3 \text{ mod } 7 = 125 \text{ mod } 7$$

$$\boxed{Y_A = 1}$$

Key generation of person 2

Let ~~private~~ key $X_B = 4$

$(X_B < q)$

Both of them
don't need any
info from
anyone. They
just
use
 α and q .

calculating ~~private~~ public key $Y_B = \alpha^{X_B} \text{ mod } q$

$$Y_B = 5^4 \text{ mod } 7 = 625 \text{ mod } 7$$

$$\boxed{Y_B = 1}$$

(show current
scenario
diagram)

Secret key calculation by person 2

M11SH - 3/7/21

\rightarrow private key of user
 \rightarrow public key of user

secret key
will use public

$$K_2 = (Y_A)^{X_B} \text{ mod } q$$

Diffie-Hellman Key Exchange

$x \rightarrow$ private key of users
 $y \rightarrow$ public key of users

(3) assume x_A (private key) and $x_A < q$

calculate
$$Y_A = \alpha^{x_A} \pmod{q}$$

 public key of A

(4) assume x_B (private key of B)

calculate
$$Y_B = \alpha^{x_B} \pmod{q}$$

 public key of B

will calculate secret key

both the secret keys, both the
 users will use public keys.

$\alpha < q$ i.e. it is a primitive root
 let $\alpha = 5$
 we can take any of the two
 α and $q \rightarrow$ global public elements (known to everyone)

Key generation of person 1

Assume ~~private~~ key $x_A = 3$

calculating public key $Y_A = \alpha^{x_A} \pmod{q}$ ($x_A < q$,
 $3 < 7$ yes)

$$Y_A = 5^3 \pmod{7} = 125 \pmod{7}$$

$$\boxed{Y_A = 1}$$

Both
 don't go
 into anyone

Key generation of person 2

let ~~private~~ key $x_B = 4$

calculating ~~private~~ public key $Y_B = \alpha^{x_B} \pmod{q}$,

$$Y_B = 5^4 \pmod{7} = 625 \pmod{7} = 1$$

$$\boxed{Y_B = 1}$$

Both
 don't go
 into anyone

Secret key calculation
 by Alice / person 1

$$x_A = 3$$

$$x_B = 4$$

by person

$$X_A = 3$$

$$X_B = 4$$

$$K = (Y_A)^{x_B}$$

MULTIPLE DES

1. DOUBLE DES
2. TRIPLE DES (2DES)
- (3DES)

Since DES attack was vulnerable to brute force attack, variations of DES called multiple DES were introduced.

abhishek dixit
56

1. Double DES

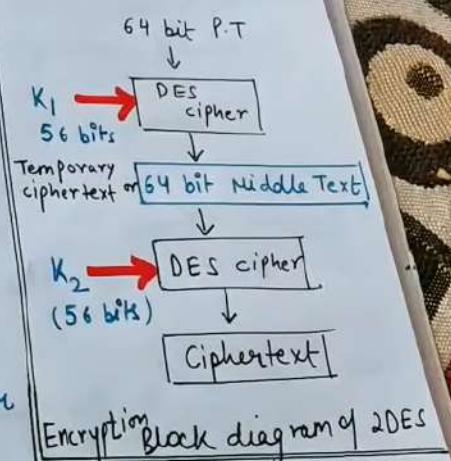
→ uses 2 dif keys
 $(56+56) = 112$ bit key

→ Double encryption occurs
as follows:

$$P \rightarrow E(K_1, P)$$

↓

$$E(K_2, E(K_1, P)) = \text{Cipher}$$



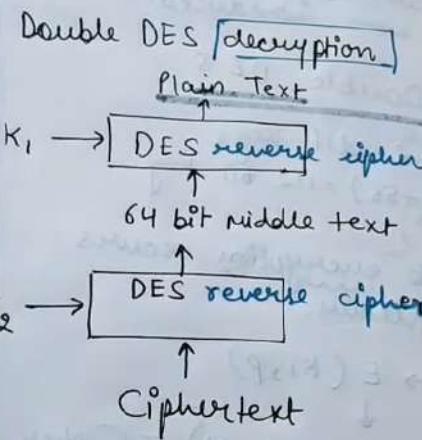
CRYPTOGRAPHY AND NETWORK SECURITY

Behrouz A Forouzan
Debdeep Mukhopadhyay

CRYPTOGRAPHY AND
NETWORK SECURITY

Forouzan
Mukhopadhyay

3e 3e



In decryption, keys are applied in reverse order

$$\text{Plain} = D(K_1, D(K_2, C))$$

1st this will happen

Meet In the Middle Attack

un & ciphertext known



decrypt pairs of
all 2^{56} possible
values of K_2

| Cipher | Middle cipher |
|--------|---------------|
| ≡ | ≡ |
| ≡ | ≡ |
| ≡ | ≡ |

in ~~lot~~ table 1

Drawback of Double DES

Meet-in-the-middle attack

This attack involves encryption from 1 end and decryption from the other end and then "Matching the results in the middle" and hence the name.

Ques Explain drawback of 2DES.

Ques Explain attack on double DES.

Ques Explain Meet-in-the-middle attack or MIM attack

This attack requires knowing (some) plaintext/ciphertext pairs.

Let us assume plaintext = P, ciphertext = C

The attack proceeds as follows:

- (i) encrypt 'P' for all 2^{56} possible values of K_1 and store the results in a table and invert it.

Meet In the Middle Attack

some pairs of
plain text known &

↓
encrypt pairs for
all 2^{56} possible
values of K_1

No. of rows in
Table =

No. of possible
secret keys

| Plain | Cipher | Middle |
|-------|--------|--------|
| ABCD | XWUP | |
| X\$#T | MXMR | |
| = | = | |

sort the results in table 1

ciphertext known
↓

decrypt pairs of
all 2^{56} possible
values of K_2

| Cipher | Middle Cipher |
|--------|---------------|
| | |
| | |

drawback of Double DES
Meet-in-the-middle attack
This attack involves encryption for
decryption from the other end
"Matching the results is hence"

Explain drawback of 2DES
Explain attack on double DES
Explain Meet-in-the-middle attack

This attack requires known
ciphertext pairs.

Let us assume plain
attack proceeds as
encrypt 'P' for
and store the
sort it.

Now, we want

decrypt pairs of
all 2^{56} possible
values of K_2

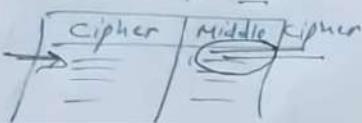


table 1

values

1st Table

Meet-in-the-middle attack

This attack involves encryption from 1 end and decryption from the other end and then "matching the results in the middle" and hence the name.

Explain drawback of 2DES.

Explain attack on double DES.

Explain Meet-in-the-middle attack or MIM attack
This attack requires knowing (some) plaintext/ciphertext pairs.

Let us assume $\text{plaintext} = P$, $\text{ciphertext} = C$

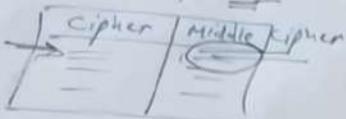
The attack proceeds as follows:

(i) encrypt P for all 2^{56} possible values of K_1 and store the results in a table and sort it.

(ii) Now, decrypt C using all 2^{56} possible values of K_2 . As each result is produced, check against the table for a match.

(iii) When there is a match, we have located a

decrypt pairs of
all 2^{56} possible
values of K_2



in ~~left~~ table 1

these values

1st Table

one
one
one
one

Explain drawback of 2DES.
Explain attack on double DES.

Meet-in-the-middle attack or MIM attack
at some place

This attack requires knowing some plaintext/
ciphertext pairs.

Let us assume plaintext = P, ciphertext = C

The attack proceeds as follows:

- (i) encrypt (P) for all 2^{56} possible values of K_1 and store the results in a table and sort it.
- (ii) Now, decrypt (C) using all 2^{56} possible values of K_2 . As each result is produced, check against the table for a match.

- (iii) When there is a match, we have located a possibly correct pair of keys.

NOTE → Now, more than 1 pair of keys may result in a match, but these no. of pairs will be small. We should try each possible pair of keys.

Euler's Theorem

→ also called Fermat-Euler theorem or Euler's totient theorem
(alc to wikipedia)

Euler's theorem states that if x and n are coprime positive integers, then

$$x^{\phi(n)} \equiv 1 \pmod{n}$$

where $\phi(n) \rightarrow$ Euler's totient function.

Note → It is a generalized version of Fermat's Theorem.

eg let $x = 11, n = 10$ both are coprime

\therefore we can represent them as

$x^{10} \pmod{11}$

where $\phi(n) \rightarrow$ Euler's totient $x^{\phi(n)} \mod n = 1 \mod n$

Note \rightarrow It is a generalized version of Fermat's theorem.

eg let $x = 11, n = 10$ both are coprime
 \therefore we can represent them as

$$11^{\phi(10)} \equiv 1 \mod 10$$

$$11^4 \equiv 1 \mod 10$$

$$14641 \equiv 1 \mod 10 \quad \text{which is true}$$

$$\begin{aligned} \phi(10) &= \phi(2) * \phi(5) & \phi(a * b) &= \phi(a) * \phi(b) \\ &= 1 * 4 & \phi(7) &= 3 \end{aligned}$$

$$11^8 = 214,358,881$$

Note \rightarrow

$$x^{\phi(n)} \equiv 1 \mod n$$

$$11^{\phi(10)} \equiv 1 \pmod{10}$$

$$11^4 \equiv 1 \pmod{10}$$

$$\boxed{11^4 \equiv 1 \pmod{10}}$$

which is true

$$\begin{aligned}\phi(10) &= \phi(2) * \phi(5) \\ &= 1 * 4 \\ &= 4\end{aligned}$$

$$\phi(a * b) = \phi(a) * \phi(b)$$

$$\phi(4) = 2$$

$$\boxed{x^{\phi(n) \cdot a} \equiv 1 \pmod{n}}$$

$$11^8 = 214,358,881$$

$$\text{i.e. } 11^{4*2} \equiv 1 \pmod{10}$$

$$11^{40} \equiv 1 \pmod{10}$$

i.e. any multiple
of $\phi(n)$ will
give the same
result.

Note →

Euler's Totient function

- It is represented using phi as $\phi(n)$ and may also be called Euler's phi function.
- Euler's totient fn is defined as the no. of [+ve integers] less than n that are coprime to n.
 $n \geq 1$

$$\phi(5) = \{1, 2, 3, 4\}$$

$$\phi(6) = \{1, 5\}$$

no. of elements in these sets
is the totient fn.

Note → Two integers a, b are said to be
coprime, mutually prime or
integer factor

$\phi(n)$ is defined as the no. of +ve integers less than n that are coprime to n .

$$\phi(1) = 1 \quad \phi(5) = \{1, 2, 3, 4\} = 4$$

$$\textcircled{1} \quad \begin{matrix} 2 & 3 & 4 & 5 \\ \times & \times & \times & \checkmark \end{matrix} \quad \phi(6) = \{1, 5\} \quad \underbrace{\qquad}_{\text{no. of elements in these sets}} \quad 2$$

is the totient f_n .

Note \rightarrow Two integers a, b are said to be relatively prime, mutually prime or coprime if the only +ve integer/factor that divides both of them is 1.

Now, when $n \rightarrow \text{prime}$ $\phi(n) = n - 1$

eg $\phi(5) = 4$ // we have seen the eg. above

$$\phi(23) = 23 - 1 = 22$$

Now, when $n \rightarrow \text{prime}$ $\phi(n) = n - 1$
eg $\phi(5) = 4$ // we have seen the eg. above
 $\phi(23) = 23 - 1$
 $= 22$

Also, $\phi(a * b) = \phi(a) * \phi(b)$ // a and b
should be coprime
eg $\phi(35) = \phi(7) * \phi(5)$
 $= 6 * 4 = 24$
eg $\phi(12) = \phi(3) * \phi(4) = 2 * 2 = 4$
 $\phi(15) = \phi(3) * \phi(5) = 2 * 4 = 8$
 \downarrow
 $\{1, 2, 4, 5, 7, 8, 11, 13, 14\}$

| n | $\phi(n)$ | nos. coprime to n |
|-----|-----------|---------------------|
| 1 | 1 | 1 |
| 2 | 1 | 1 |
| 3 | 2 | 1, 2 |
| 4 | 2 | 1, 3 |
| 5 | 4 | 1, 2, 3, 4 |
| 6 | 2 | 1, 5 |
| 7 | 6 | 1, 2, 3, 4, 5, 6 |
| 8 | 4 | 1, 3, 5, 7 |
| 9 | 6 | 1, 2, 4, 5, 7, 8 |
| 10 | 4 | 1, 3, 7, 9 |

Euler's
are

where

Note →

eg

Euler's Theorem

→ also called Fermat-Euler theorem or Euler's totient theorem

(acc to wikipedia)

Euler's theorem states that if x and n are coprime positive integers, then

$$x^{\phi(n)} \equiv 1 \pmod{n} \rightarrow x^{\phi(n)} \pmod{n} = 1 \pmod{n}$$

where $\phi(n) \rightarrow$ Euler's totient function.

Note → It is a generalized version of Fermat's Theorem.

eg let $x = 11, n = 10$ both are coprime

∴ we can represent them as

$$11^{\phi(10)} \equiv 1 \pmod{10}$$

$$x^{n-1} \equiv 1 \pmod{n}, \quad x^n \equiv x \pmod{n}$$

[Ques] Verify fermat's theorem for $x = 6$, $n = 7$

$$x^{n-1} \equiv 1 \pmod{n}$$

$$6^{7-1} = 6^6 = 46656 \equiv 1 \pmod{7}$$

$$x^n \equiv x \pmod{n}$$

$$6^7 = 279936$$

$$279936 \equiv 6 \pmod{7}$$

which is true.

not be modified

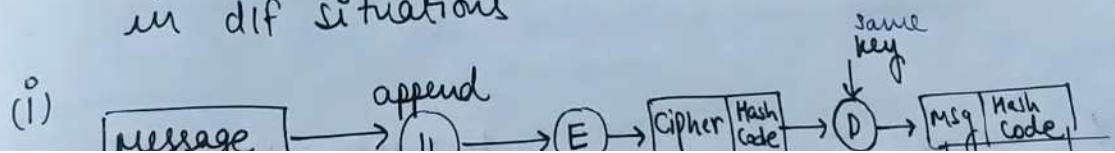
ld be safe

almost be
cryptanalysts

HASH FUNCTIONS

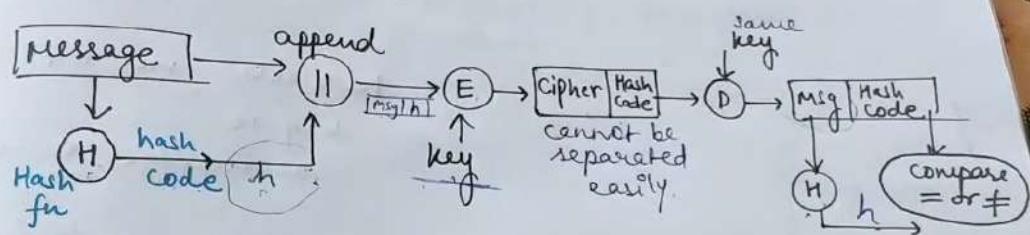
- Similar to MAC (msg. authentication code)
BUT it does not use a key.
 - Takes in variable size message and produce a fixed output.
↓
called Hash Code | Hash value | or
Message Digest
 - The only I/P is the message.
 - A hash value 'h' is generated by a fn H
$$H(M) = \text{fixed length code } 'h'$$

They are also called ~~Variable length~~ ~~Compression~~ Functions.
There are dif methods to provide authentication
in dif situations



They are also called compression functions.
 There are different methods to provide authentication
 in different situations.

(i)



authentication + confidentiality

if both hashcodes
equal in the end

maintained b/c
msg was encrypted
before sending

b/c only A & B share the
secret key, the msg must have
come from A & has not been
altered.

ION

5 principles of security.
authenticity of the msg is imp.
must be there to authenticate

authentication

tion Code (MAC)

MAC (message authentication code)

- We will use a secret key to generate a small fixed size ^{block} of data called MAC or cryptographic checksum.
- It is then appended with the message.
- The communicating parties will share a secret common key.
which will be used to create the MAC

Let A → sender
B → receiver

when A sends a msg to B, it calculates the MAC as a fn of the message and the key.

$$\boxed{MAC = C(K, M)}$$

where
M = input message
C = mac function

AUTHENTICATION

- It is one of the 5 principles of security.
- verifying the authenticity of the msg is imp.
- An authenticator must be there to authenticate the message.

Methods to produce authentication

1. message encryption
2. Message Authentication Code (MAC)
3. Hash functions

MAC (message authentication code)

→ we will use a ~~secret~~
small fixed size.

→ It is then appended
→ The communication

Let A → send
B → receive

when A sends
MAC as a

→ If message is long
be there to authenticate

authentication
cipher text
Code (MAC)
Value

small fixed size of data called MAC or
cryptographic checksum.

- It is then appended with the message.
- The communicating parties will share a secret common key.

~~2MB~~ → ~~2KB~~ which will be used to create the MAC

Let A → sender
B → receiver

when A sends a msg to B, it calculates the
MAC as a fn of the message and the key.

$$\boxed{\text{MAC} = C(K, M)}$$

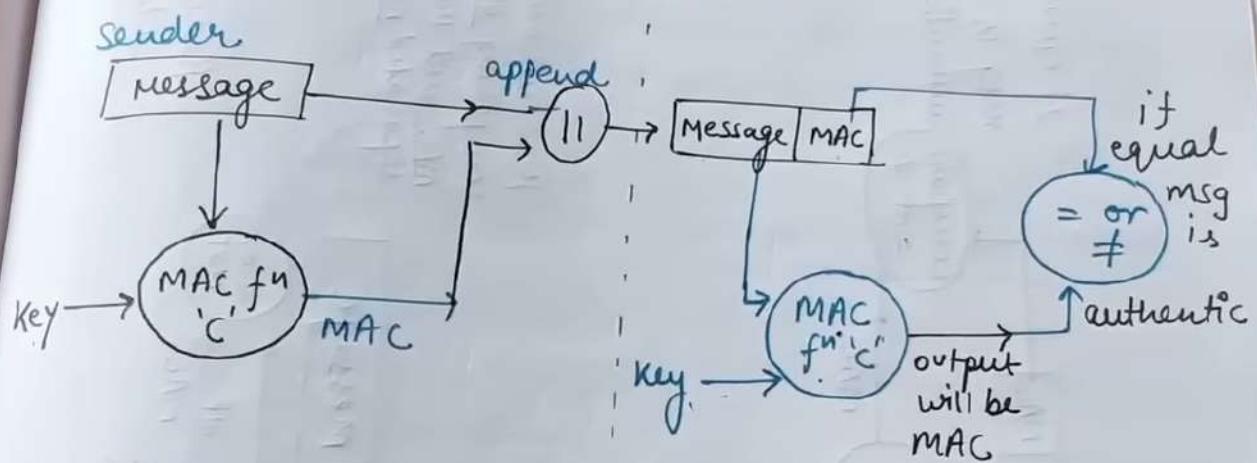
where

M = input message

C = MAC function

K = shared secret key

(i) MAC - for authentication

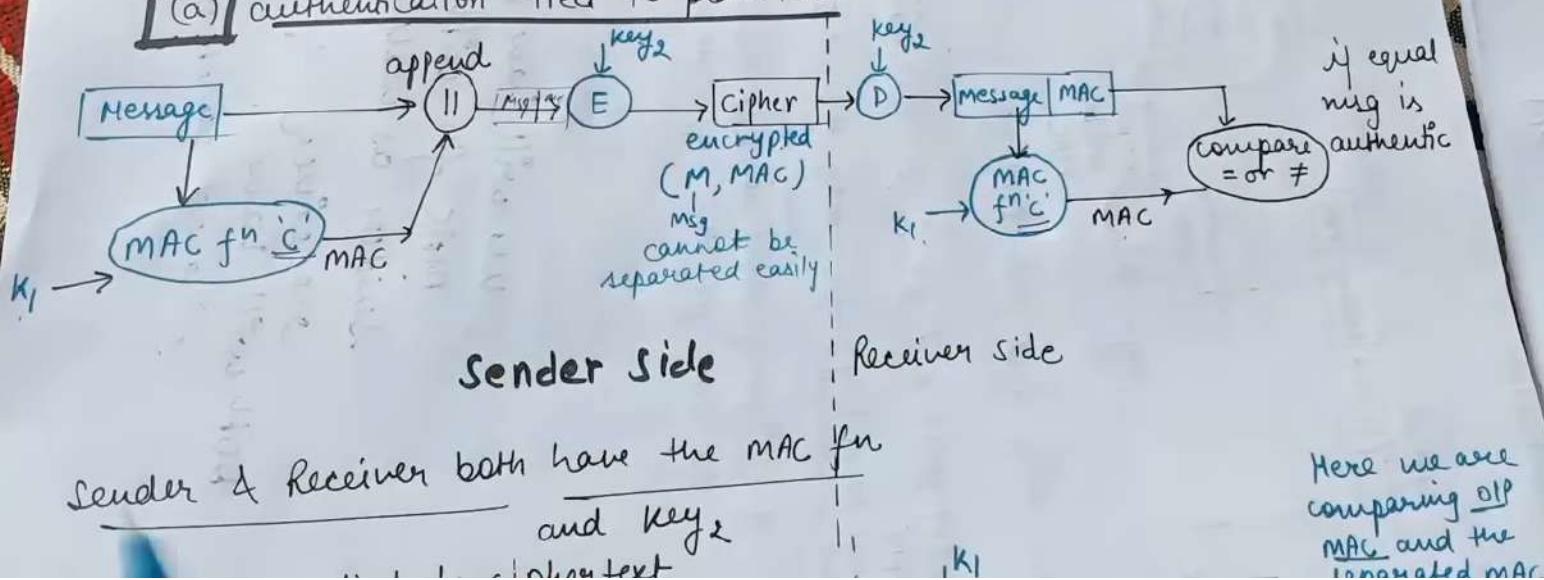


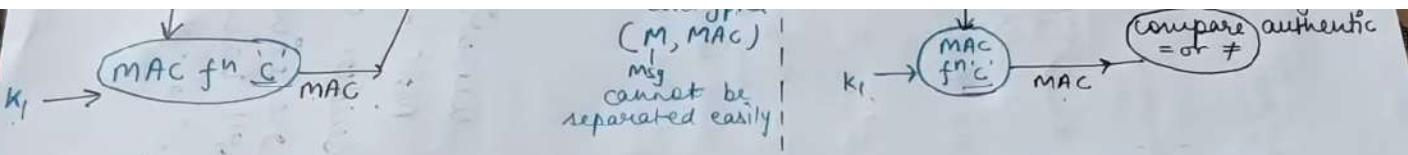
We separate the msg and the MAC

only authentication is achieved
No

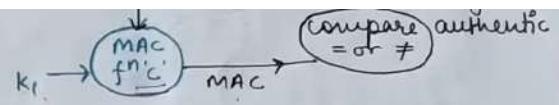
2) MAC - for authentication & confidentiality

(a) authentication tied to plain text





Sender Side

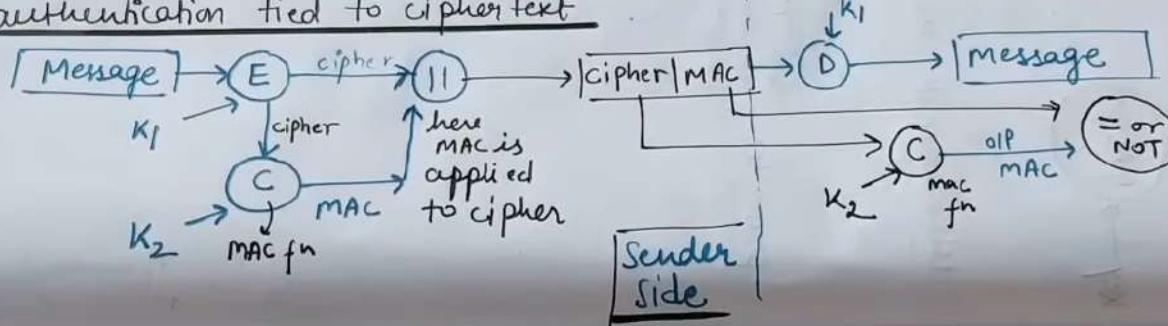


Receiver side

Sender & Receiver both have the MAC fn

and key K_2

b) authentication tied to ciphertext



Here we are comparing oIP MAC and the separated MAC

Receive Side

How is confidentiality achieved?

If the hacker attacks, he will get the

=

auth
has been

Algorithm

Rivest-Shamir-Adleman developed in 1978

- It is an asymmetric cryptographic algo.
(2 keys) ie public and private key concept is used here.
- The acronym RSA is made from the initial letters of the surnames of Ron Rivest, Adi Shamir, and Leonard Adleman.

- Public key → known to all users in N/W
Private key → kept secret, not shareable to all.

If public key of user A is used for encryption, we have to use the private key of same user for decryption.

The RSA scheme is a block cipher in which the plain text and ciphertext are integers b/w 0 and $n-1$ for some value n .

1. Key Generation

- (i) select 2 large prime nos ' p ' and ' q ' for higher security.
- (ii) calculate $n = p * q$
- (iii) calculate $\phi(n) = (p-1) * (q-1)$ // Euler's Totient fn
- (iv) choose value of e
 $1 < e < \phi(n)$ and $\text{gcd}(\phi(n), e) = 1$
- (v) calculate
 $d = e^{-1} \text{ mod } \phi(n)$
ie $ed = 1 \text{ mod } \phi(n)$
- (vi) public key = $\{e, n\}$
- (vii) private key = $\{d, n\}$

2. Encryption

Plaintext = $M < n$ Imp
|| $c \rightarrow \text{ciphertext}$

$$\text{Let } p = 3, q = 11$$

$$n = p \times q = 3 \times 11 = 33$$

$$\phi(n) = (p-1)(q-1) = 2 \times 10 = 20 \quad \therefore \phi(n) = (p-1)(q-1)$$

so, let $\boxed{e=7}$ as $1 < e < 20$ and $\gcd(7, 20) = 1$

$$\text{Now, } d \equiv e^{-1} \pmod{\phi(n)}$$

$$de \equiv 1 \pmod{\phi(n)} \rightarrow de \pmod{\phi(n)} = 1$$

$$7 \times d \equiv 1 \pmod{\phi(n)}$$

$$(7 \times d) \pmod{20} = 1 \quad (\because d=3)$$

multiplicative inverse of 7

and multiples of $\phi(n)$ ie here 20, and just
a no. satisfying a value greater
than ie $(7 \times d)$ should be 21.

using extended euclidean

↓ in next video
(I will use this
method).

Key Generation

select 2 large prime nos p and q → for higher security.

$$n = p \times q$$

$$\phi(n) = (p-1)(q-1) \quad \text{// Euler's Totient fn}$$

choose value of e

$$1 < e < \phi(n) \text{ and } \gcd(\phi(n), e) = 1$$

calculate

$$d \equiv e^{-1} \pmod{\phi(n)}$$

$$ie \quad ed \equiv 1 \pmod{\phi(n)} \rightarrow ed \pmod{\phi(n)} = 1$$

$$\text{public key} = \{e, n\}$$

$$\text{private key} = \{d, n\}$$

Encryption

$$C = M^e \pmod{n}$$

$$\text{Plaintext} = \underline{M} \pmod{n} \quad || \text{Ciphertext}$$

Decryption

$$M = C^d \pmod{n}$$

..... used in encr

$$de \equiv 1 \pmod{\phi(n)} \rightarrow de \pmod{\phi(n)} = 1$$

$$7 \times d \equiv 1 \pmod{\phi(n)}$$

$$(7 \times d) \pmod{20} = 1 \quad (\because d=3)$$

multiplicative inverse of 7

// find multiples of $\phi(n)$ i.e here 20, and just find a no. satisfying a value greater than this i.e $(7 \times d)$ should be 21.

We can solve it using extended euclidean algorithm also

↓ in next video
(I will use this method).

since $e=7, d=3$

$$\begin{aligned}\text{public key } &= \{e, n\} = \{7, 33\} \\ \text{private key } &= \{d, n\} = \{3, 33\}\end{aligned}$$

ENCRYPTION

$$\begin{aligned}C &= M^e \pmod{n} \quad \text{Let } M=31 \\ C &= 31^7 \pmod{33} = 4 \quad \rightarrow \boxed{C=4}\end{aligned}$$

DECRYPTION

$$M = C^d \pmod{n} = 4^3 \pmod{33} = 31 \quad \boxed{M=31}$$

- i) select 2 large prime nos p and q for higher security.
- ii) calculate $n = p \times q$
- iii) calculate $\phi(n) = (p-1) \times (q-1)$ // euler's totient fn
- iv) choose value of e $1 < e < \phi(n)$ and $\gcd(\phi(n), e) = 1$
- v) calculate $d \equiv e^{-1} \pmod{\phi(n)}$
i.e $ed \equiv 1 \pmod{\phi(n)} \rightarrow ed \pmod{\phi(n)} = 1$
- vi) public key $= \{e, n\}$
- vii) private key $= \{d, n\}$

2. Encryption

$$C = M^e \pmod{n} \quad \begin{matrix} \text{Plaintext } \xrightarrow{=} M \\ \text{Ciphertext } \xrightarrow{=} C \end{matrix}$$

3. Decryption

$$M = C^d \pmod{n}$$

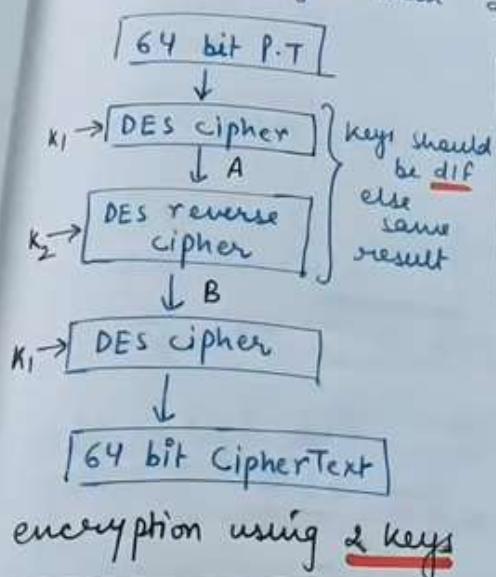
Note → (e, n) is public key used in encryption
 (d, n) → private key used for decryption

ng to break
force.

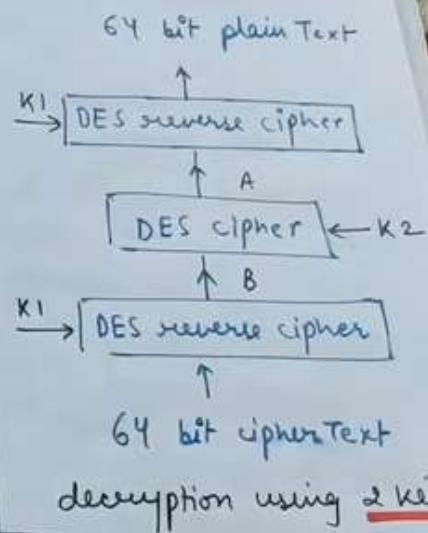
security.

TRIPLE DES

- 2 or 3 keys are used i.e. 3DES
- much stronger than double DES.



encryption using 2 keys



decryption using 2 keys

