

Assignment Two for FCC 220/520

Total marks: 20 marks.

Due Date: 16/05/2013 (4:00pm)

Requirement: You need to finish this assignment independently.

1. In the process of implementing RSA, exponentiation in modular arithmetic is an important issue in computing

$$M^e \bmod n.$$

Read paragraphs in page 271-272 in the textbook (4th edition) and make sure you fully understand the technical content and implement the Algorithm in Figure 9.7. You are required to do the following:

- You code this algorithm in C/C++ and make sure it can be used to compute $a^b \bmod n$ for positive integer numbers a, b, n with length less than 10 digits. Hand in the hard copy of your code.
 - Use your code to compute $12^{23} \bmod 64$ and print out the final result.
2. In RSA algorithm, if two users are using two public keys (n, e_1) and (n, e_2) with same modular n , where e_1 and e_2 are co-prime. If they encrypt the same message m as following

$$\begin{aligned} c_1 &= m^{e_1} \bmod n \\ c_2 &= m^{e_2} \bmod n \end{aligned}$$

and a cryptanalyst knows the information $\{e_1, e_2, c_1, c_2, n\}$, can he/she recover the information m from $\{e_1, e_2, c_1, c_2, n\}$? With any possible answer you give, explain your justification.

3. Implement the following steps.
 - Select two prime numbers p and q using the algorithm in Question 3 of lab 2. The range of p and q is required to be between 1000 and 10000.
 - Using the Extended Euclidean Algorithm (question 5 in lab 3) to select $\{e, n\}$ with constraint $\gcd(e, \phi(n))=1$.
 - Using the Extended Euclidean Algorithm (question 5 in lab 3) to solve d .
 - Convert each symbol on keyboard to its ASCII code for RSA encryption and decryption.
 - Implement RSA encryption and decryption using the algorithm in Question 1 of this assignment.

- When you finish all steps above, you are required to encrypt and decrypt a text file. In your hard copy, state each step clearly with explanations in your code. The test file will be the same for SDES on the website.