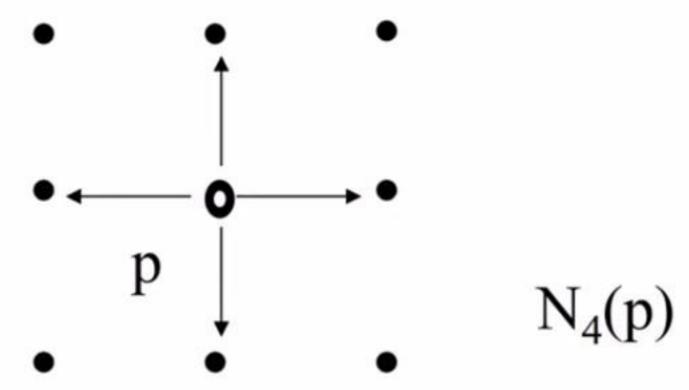
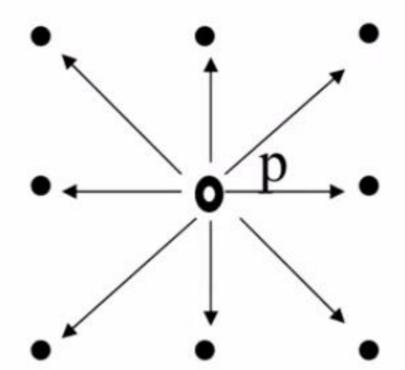
Neighbors of a Pixel

B

The points $N_D(P)$ and $N_4(P)$ are together known as 8-neighbors of the point P, denoted by $N_8(P)$.

• Some of the points in the $N_4(P)$, $N_D(P)$ and $N_8(P)$ may fall outside a finite resolution image when P lies on the border of image.





 $N_8(p)$











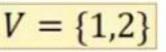


Adjacency

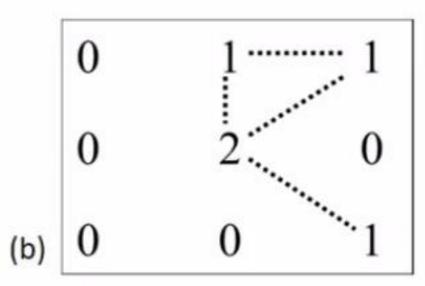
Let V be the set of gray-level values used to define connectivity;

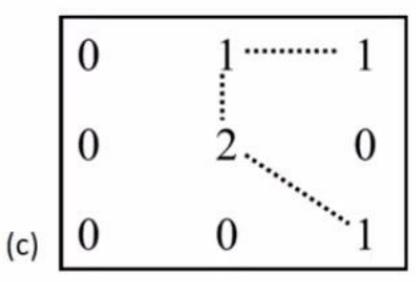
then two pixels p, q that have values from the set V are:

- 4-connected, if q is in the set $N_4(P)$
- b. 8-connected, if q is in the set $N_8(P)$
- c. m-connected, iff
- -q is in $N_4(P)$.
- -q is in $N_D(P)$ and the set $[N_4(P) \cap N_4(Q)]$ is empty (has no pixels whose values are from V)



	0	11	
	0	2	0
(a)	0	0	1





















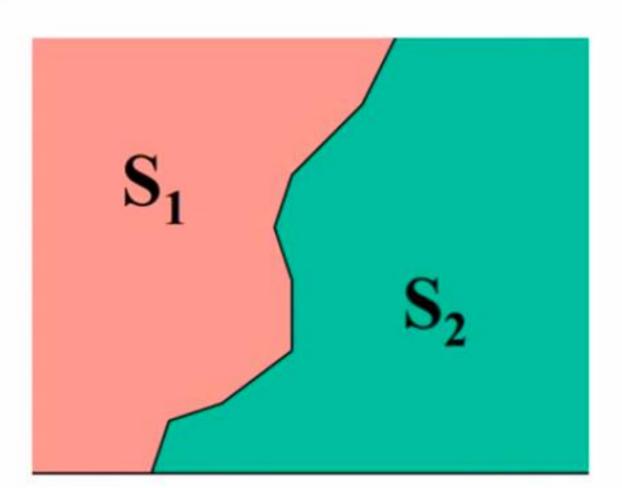






Adjacency

Two image subsets S_1 and S_2 are adjacent if some pixel in S_1 is adjacent to some pixel in S_2

















Paths

A path from pixel p with coordinates (x, y) to pixel q with coordinates (s, t) is a sequence of distinct pixels with coordinates:

$$(x_0, y_0), (x_1, y_1), (x_2, y_2) \dots (x_{n-1}, y_{n-1})$$

where

- $(x_0, y_0) = (x, y)$ $(x_{n-1}, y_{n-1}) = (s, t)$
- (x_i, y_i) is adjacent to (x_{i-1}, y_{i-1}) $1 \le i \le n-1$

Here **n** is the length of the path.

We can define 4-, 8-, and m-paths based on type of adjacency used.











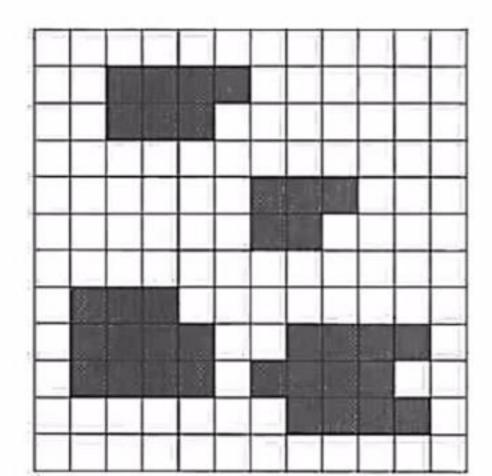


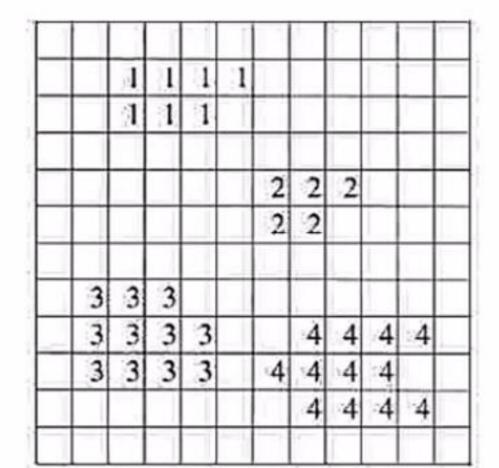




If p and q are pixels of an image subset S then p is connected to q in S if there is a path from p to q consisting entirely of pixels in S.

- For every pixel p in S, the set of pixels in S that are connected to p is called a connected component of S.
- If S has only one connected component then S is called Connected Set.

















Connected Components

Recursive algorithm

- Let is assume that region pixels have the value 0 (black) and that background pixels have the value 255 (white).
 - (1) Scan the image to find an unlabeled 0 (pixel and assign it a new label L.
 - (2) Recursively assign a label to all of its 0 neighbors.
 - (3) Stop if there are no more unlabeled 0 pixels.
 - (4) Go to step 1.

























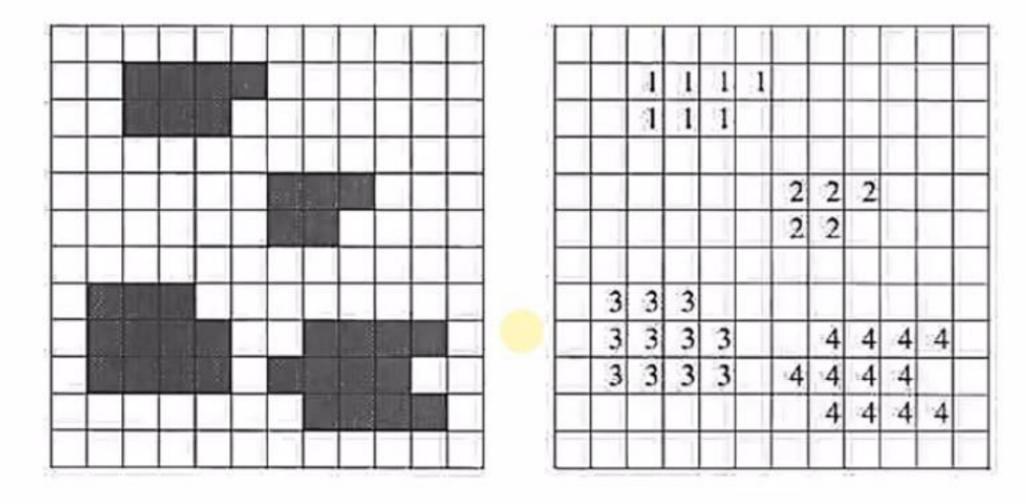




Connected Components

Recursive algorithm

Top to bottom, Left to right

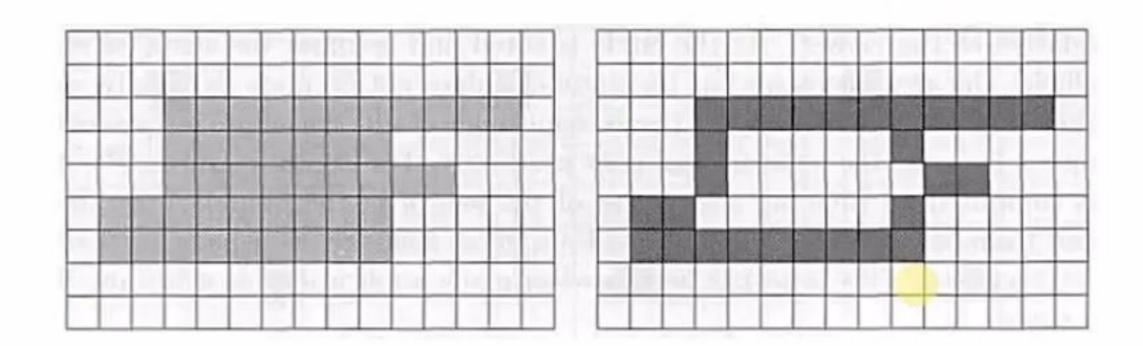


Sequential algorithm

- The sequential algorithm usually requires two passes over the image.
- It works with only two rows of an image at a time.
- (1) Scan the image left to right, top to bottom.
- (2) If the pixel is 0, then:
 - (2.1) If only one of its upper and left neighbors has a label, then copy the label.
 - (2.2) If both have the same label, then copy the label.
- (2.3) If both have different labels, then copy the upper's label and enter the labels in the equivalence table as equivalent labels.
- (2.4) Otherwise assign a new label to this pixel and enter this label in the equivalence table.
- (3) If there are no more pixels to consider, then go to step 2.
- (4) Find the lowest label for each equivalent set in the equivalence table.
- (5) Scan the image. Replace each label by the lowest label in its equivalent set.

Region boundary

- The boundary of a connected component S is the set of pixels of S that are adjacent to background.
- In most applications, one wants to track pixels on the boundary of a region in a particular order (e.g., clockwise).



Distance Measures

Given pixels p, q and z with coordinates (x, y), (s, t), (u, v) respectively, the distance function D has following properties:

- $D(p,q) \ge 0$, [D(p,q) = 0, iff p = q]
- D(p,q) = D(q,p)
- D(p,q) = D(q,p)• $D(p,z) \le D(p,q) + D(q,z)$

Distance Measures

The following are the different Distance measures:

Euclidean Distance:

$$D_e(p,q) = [(x-s)^2 + (y-t)^2]^{1/2}$$

<u>Cityblock Distance</u>:

$$D_4(p,q) = |x-s| + |y-t|$$

Chess-board Distance:

$$D_8(p,q) = max(|x-s|,|y-t|)$$

CONTROL OF THE PROPERTY OF THE		2		
	2	1	2	
2	1	0	1	2
	2	 	2	
10 10 10 10 10 10 10 10 10 10 10 10 10 1		2	******	

Cityblock Distance

2	2	2	2	2
2	1	1	1	2
2	1	0	1	2
2	1	1	1	2
2	2	2	2	2

Chess-board Distance

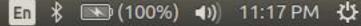




























Distance Measures

The following are the different Distance measures:

Euclidean Distance:

$$D_e(p,q) = [(x-s)^2 + (y-t)^2]^{1/2}$$

Cityblock Distance:

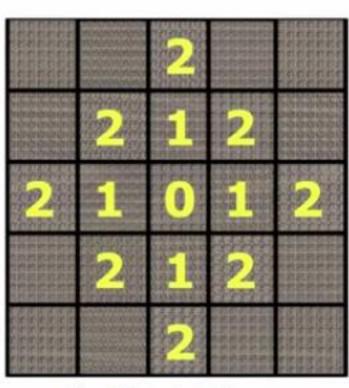
$$l_1$$
 distance

$$D_4(p,q) = |x-s| + |y-t|$$

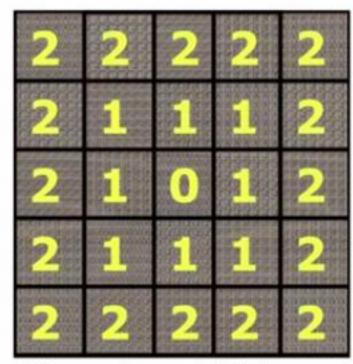
Chess-board Distance:

$$l_{\infty}$$
 distance

$$D_8(p,q) = max(|x-s|,|y-t|)$$



Cityblock Distance



Chess-board Distance

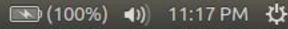




























Arithmetic/Logic Operations:

- Addition : p + q
- Subtraction: p-q
- Multiplication : p*q
- Division : p/q
- AND: pAND q
- -OR:pORq
- Complement: NOT(q)











3









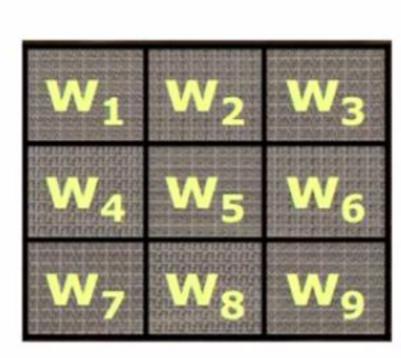




Neighborhood based arithmetic/Logic:

Value assigned to a pixel at position 'e' is a function of its neighbors and a set of window functions.

а	b	C	
d	е	f	••
9	h	Ī	
	•		



$$p = (w_1 a + w_2 b + w_3 c + w_4 d + w_5 e + w_6 f + w_7 g + w_8 h + w_9 i)$$

= $\sum w_1 f_1$

