

# Pure Integer Programming

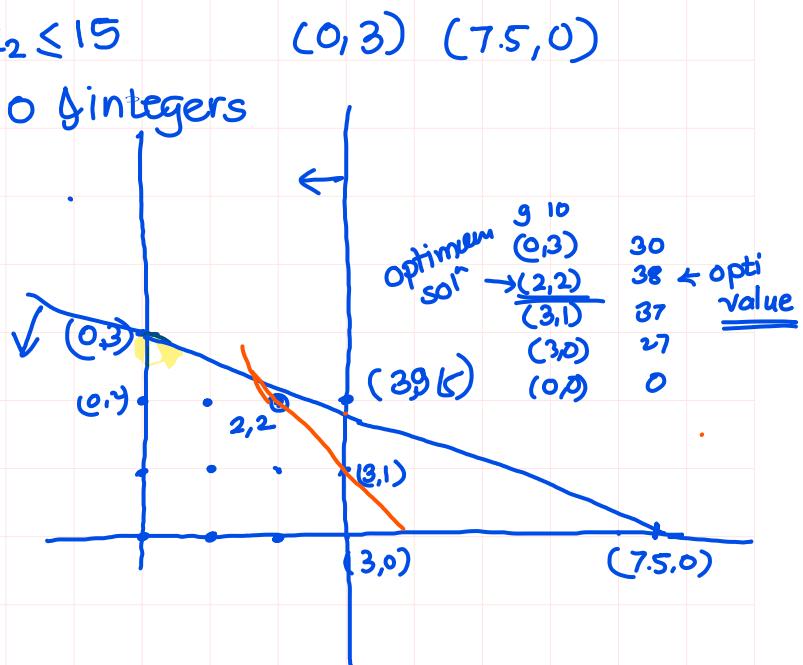
## Gomory's Cutting Plane Method :-

$$\text{Max } Z = 9x_1 + 10x_2$$

$$\text{s.t. } x_1 \leq 3$$

$$2x_1 + 5x_2 \leq 15$$

$x_1, x_2 \geq 0$  & integers



$$\begin{aligned} \text{Max } Z &= 9x_1 + 10x_2 \\ x_1 + x_3 &= 3 \\ 2x_1 + 5x_2 + x_4 &\leq 15 \end{aligned}$$

	$x_1$	$x_2$	$x_3$	$x_4$	b	0
Basic	$x_3$	1	0	1	0	3
0	$x_4$	2	5	0	1	15
Z	0	0	0	0	0	0
$C_j - Z_j$	9	10	0	0		

R <sub>1</sub>	0	$x_3$	1	0	1	0	3	3	→
$\frac{1}{5}R_2$	10	$x_2$	$\frac{2}{5}$	1	0	$\frac{1}{5}$	3	$15/2$	
	Z		4	10	0	2	30		
	$C_j - Z_j$		5	0	0	-2			
	$x_1$	$x_2$	$x_3$	$x_4$					

R <sub>1</sub>	9	$x_4$	1	0	1	0	3	$x_1 = 3, x_2 = 9/5$
$R_2 - \frac{2}{5}R_1$	10	$x_2$	0	1	$-\frac{2}{5}$	$\frac{1}{5}$	$\frac{9}{5}$	$Z = 45$
	Z	9	10	5	2		<u>45</u>	
	$C_j - Z_j$	0	0	-5	-2			

$$0 \cdot x_1 + 1 \cdot x_2 - \frac{2}{5} x_3 + \frac{1}{5} x_4 = \frac{9}{5}$$

$$\leftarrow x_2 = \frac{9}{5} + \frac{2}{5} x_3 - \frac{1}{5} x_4$$

$$u_1 = \underbrace{(-1) + \frac{4}{5}}_{\frac{-1}{5} - (-1)} + \frac{2}{5} x_3 + \frac{4}{5} x_4$$

$$-\frac{2}{5} x_3 - \frac{4}{5} x_4 + u_1 = -\frac{1}{5}$$

		9	10	0	0	0	b
	$x_1$	1	0	1	0	0	3
	$x_2$	0	1	$-\frac{2}{5}$	$\frac{11}{5}$	0	$\frac{9}{5}$
	$u_1$	0	0	$-\frac{2}{5}$	$\boxed{-\frac{4}{5}}$	1	$-\frac{1}{5}$
	$Z$	9	10	5	2	0	
$C_j - Z_j$		0	0	-5	-2	0	
$\theta$		-	-	$2\frac{5}{2}$	$\frac{5}{2}$	-	
	$x_1$	$x_2$	$x_3$	$x_4$	$u_1$	b	

Use dual  
Simplex  
Method

	$x_4$	1	0	1	0	0	b
	$x_2$	0	1	$\boxed{-\frac{1}{2}}$	0	$\frac{1}{4}$	$\frac{7}{4}$
	$x_4$	0	0	$\frac{1}{2}$	1	$-\frac{5}{4}$	$\frac{11}{4}$
	$Z$	9	10	4	0	$\frac{5}{2}$	$\frac{89}{2}$
$C_j - Z_j$		0	0	-4	0	$-\frac{5}{2}$	

Int  
Non-Int  
Non-Int

$$x_4 = \frac{1}{4} - \frac{1}{2} x_3 + \frac{5}{4} u_1$$

$$u_2 = -1 + \frac{1}{4} + \frac{1}{2} x_3 + \frac{1}{4} u_1$$

$$-\frac{1}{2} x_3 - \frac{1}{4} u_1 + u_2 = -\frac{3}{4}$$

		$x_1$	$x_2$	$x_3$	$x_4$	$u_1$	$u_2$	b
9	$x_1$	1	0	1	0	0	0	3
10	$x_2$	0	1	$-\frac{1}{2}$	0	$\frac{1}{4}$	0	$\frac{7}{4}$
0	$x_4$	0	0	$\frac{1}{2}$	1	$-\frac{5}{4}$	0	$\frac{11}{4}$
0	$u_2$	0	0	$(-\frac{1}{2})$	0	$-\frac{1}{4}$	1	$-\frac{3}{4}$
<hr/>								
Z		0	0	4	0	$\frac{5}{2}$	0	
$C_j - Z_j$		0	0	-4	0	$-\frac{5}{2}$		
0		-	-	8 ↑	-	10		
		3	10			0	0	
9	$x_1$	1	0	0	0	$-\frac{1}{2}$	2	$\frac{3}{2}$
10	$x_2$	0	1	0	0	$\frac{1}{2}$	-1	$\frac{5}{2}$
$R_3 - \frac{1}{2}R_4$	$x_4$	0	0	0	1	$[-\frac{3}{2}]$	1	$-\frac{1}{2}$
$-2R_2$	$x_3$	0	0	1	0	$\frac{1}{2}$	-2	$\frac{3}{2}$
	$Z_j$	9	10	0	0	$\frac{1}{2}$	8	$\frac{77}{2}$
	$C_j - Z_j$	0	0	0	0	$-\frac{1}{2}$	-8	
	0	-	-	-	-	$\frac{13}{2}$ ↑	-	

Product	M1	M2	M3	Profit	Vari
1	10	6	8	200	$x_1$
2	5	20	15	300	$x_2$

$$\text{Max } Z = 200x_1 + 300x_2$$

$$10x_1 + 5x_2 \leq 600$$

$$6x_1 + 20x_2 \leq 600$$

$$8x_1 + 15x_2 \leq 600$$

$$x_1, x_2 \geq 0$$

$$\text{Min } Z = 3x_1 + 5x_2$$

$$x_1 + x_2 \geq 200$$

-

$$x_1 \leq 80$$

$$x_2 \geq 60$$

2004, 16, 20, 24, 30, 36, 37, 40, 49, 53, 56

~~2007~~

- ① { 2007  
2008  
2013  
2015  
2017 ·
- ② { 2019 ·  
2028 ·  
2032 ·  
2035 ·
- ③ 2037 ·  
2038 ·
- ④ { 2042 ·  
2045 ·  
2047 ·  
2048 ·
- ⑤ { 2051 ·  
2055 ·

## Dear Students.

I am deeply saddened due to your behaviour today. I think you owe me an explanation for this.

As a punishment,

I have decided to

- subtract 05 marks from your ST-401 Internal Marks
- request you to solve all assignment questions provided in question bank
- request you to prepare a presentation in LaTeX for

- Group & Topics*
- ① BA/BE
  - ② PK Parameters
  - ③ Effect Estimation in 2x2 design
  - ④ ANOVA for 2x2 Crossover design
  - 5 Classical Shortest CI .

Submit by tomorrow 08:00PM

- Manoj

