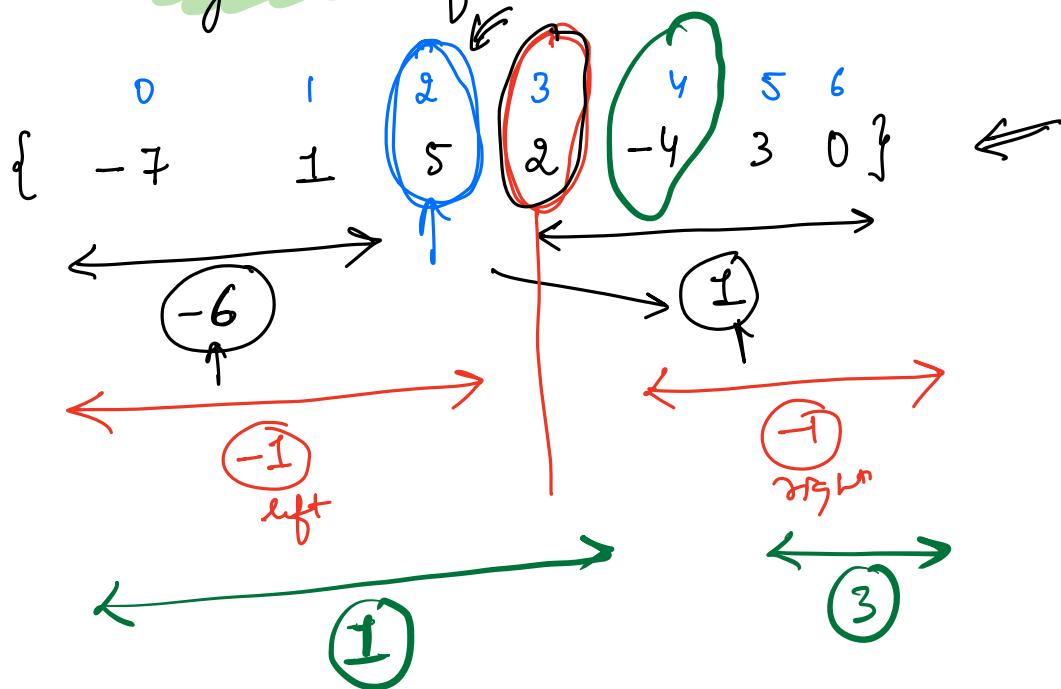




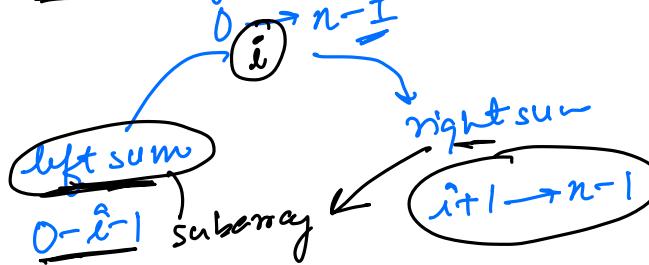
Given array of size N. Find Equilibrium index of the array

Equilibrium index :- an index such that sum of elements on left side of index is equal to sum on right side of index.



Brute force

consider every single index $\rightarrow n$



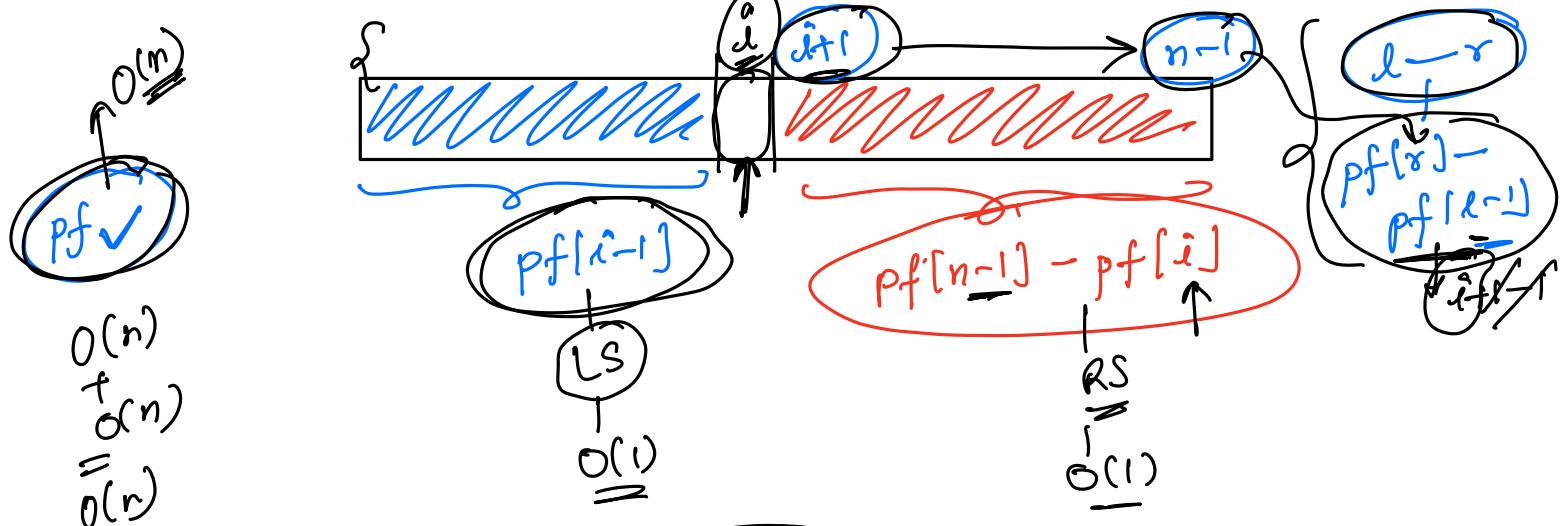
$O(n^2)$

$O(n)$

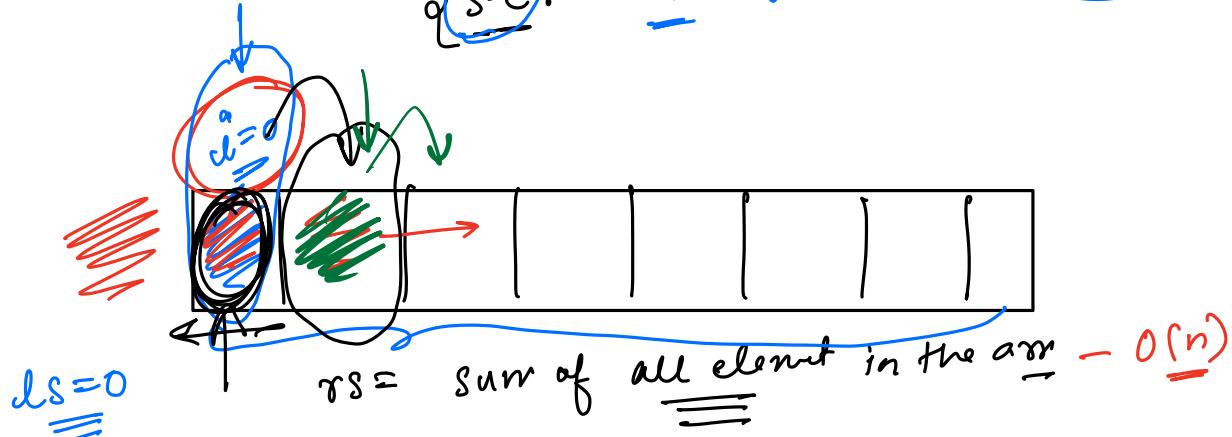
$O(1)$

$O(1)$

\Rightarrow to improve sum calculation
 \rightarrow prefix sum



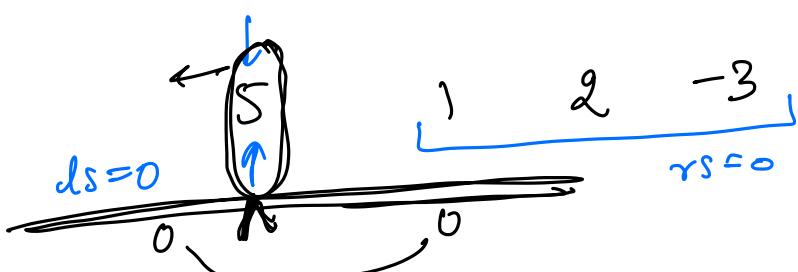
$T.C: O(n)$
 $S.C: O(n)$ $\rightarrow O(1)$ $\{$ pf



$i = 0$
 for $i = 0 \rightarrow n$
 $\{$ $\text{rs} = \text{arr}[i]$
 $\text{if } (\text{ls} == \text{rs})$
 $\text{return } i$

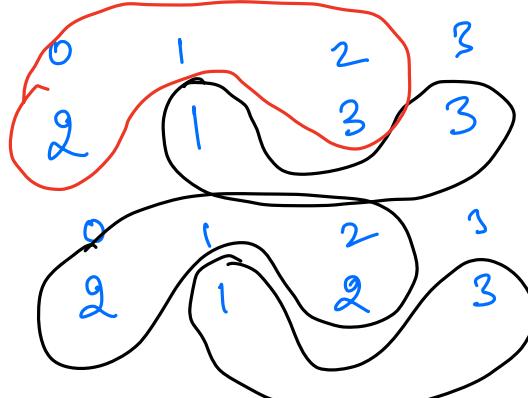
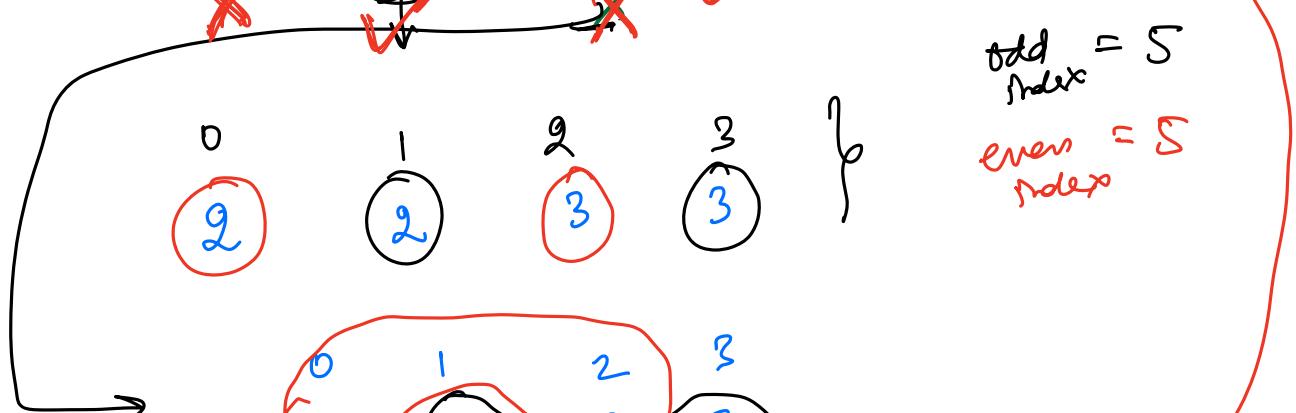
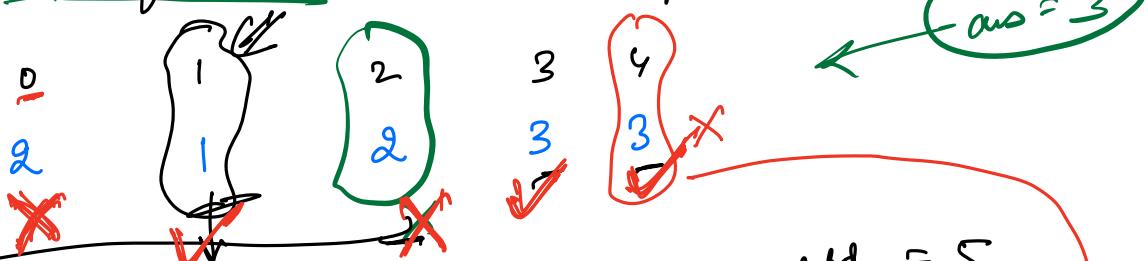
$\text{ls} += \text{arr}[i]$

β



Q Count Special Elements.

An element is special if after removing this element from the array sum of elements at odd position is equal to sum of elements at even position:



LS?

odd \Rightarrow even
even \Rightarrow odd

odd position sum = sum of odd on left
even position sum = sum of even on right

odd position sum = sum of odd on left

even position sum = sum of even on left + sum of even on right



sum of odd on right

B.F

consider every single index $\rightarrow \underline{i}$



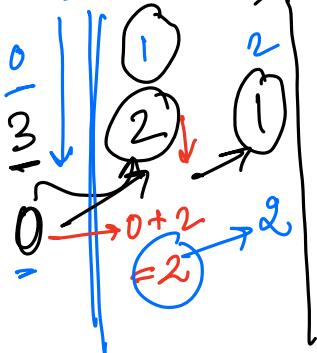
$\left. \begin{array}{l} \text{even right} \\ \text{odd right} \end{array} \right\} n$

$O(n^2)$

$0 - i-1$

$0-i$

$\underline{\text{pfodd}(s)} = \frac{\text{sum of odd pos!}}{\text{from } 0-s}$



$\underline{\text{pfodd}(i)}$
odd position
 $0-i$

$c \quad 2$

$5 \quad 8$

$\underline{\text{pfodd}(i)} = \underline{\cancel{a(i)}} + \underline{\text{pfodd}(i-1)}$

$|i-1| \cdot 2 = 0$

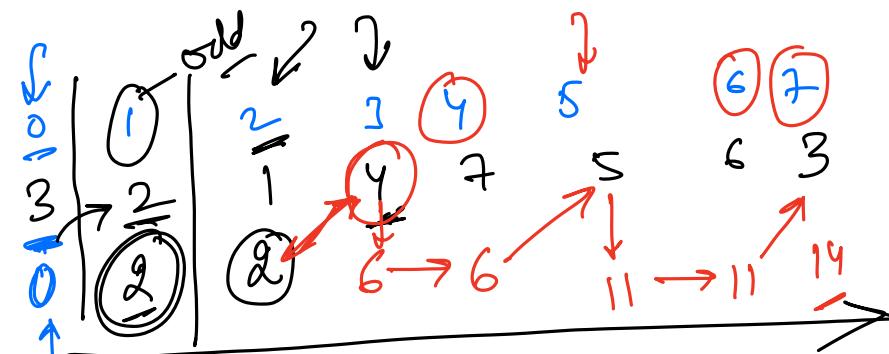
$\underline{\text{pf}}(i) = \underline{a(i)} + \underline{\text{pf}}(i-1)$

$\underline{\text{pfodd}(i)} = \underline{\text{pfodd}(i-1)}$

$\cancel{\text{if } (i-1) \cdot 2 \neq 0}$

$\underline{\text{pfodd}(i)} + \underline{\text{arr}(i)}$

$\underline{\text{pfodd}(i)} = \underline{\text{pfodd}(i)}$

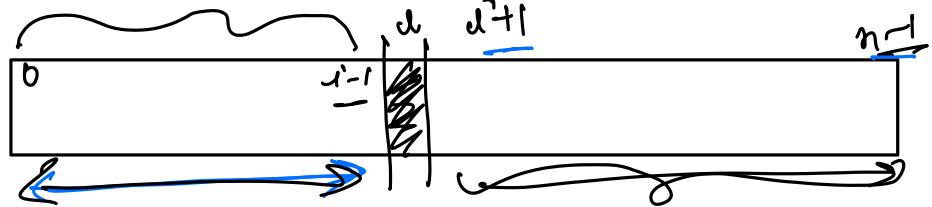


$\underline{\text{pfodd}(i)}$

$\underline{\text{pfeven}(i)}$

$\underline{\text{sumodd}} \stackrel{0-i}{=} \underline{\text{pfodd}}$

$\underline{\text{sumeven}} \stackrel{0-i}{=} \underline{\text{pfeven}}$



$$\left\{ \begin{array}{l} \underline{\text{odd left}} = \underline{\text{pfodd}[i-1]} \\ \underline{\text{even left}} = \underline{\text{pfeven}[i-1]} \end{array} \right. \quad \left. \begin{array}{l} \underline{\text{odd right}} = \underline{\text{pfodd}[n-1]} - \underline{\text{pfodd}[i]} \\ \underline{\text{even right}} = \underline{\text{pfeven}[n-1]} - \underline{\text{pfeven}[i]} \end{array} \right\}$$

$$\begin{aligned} \text{odd left} &= \text{even right} \\ \text{even left} &= \text{odd right} \end{aligned}$$

T.C: O(n)
S.C: O(n)

$$\left\{ \begin{array}{l} l0 = 0 \\ le = 0 \end{array} \right. \quad \left. \begin{array}{l} r0 = \underline{\text{sum of all odd position}} \\ re = \underline{\text{sum of even position}} \end{array} \right\}$$

If calculate $r0$ & re
for $i=0 \rightarrow n$

{ if ($i \% 2 == 0$)

$r0 -= arr[i]$

else
 $re -= arr[i]$

if ($l0 + re == le + r0$)

ans +=;

if ($i \% 2 != 0$)

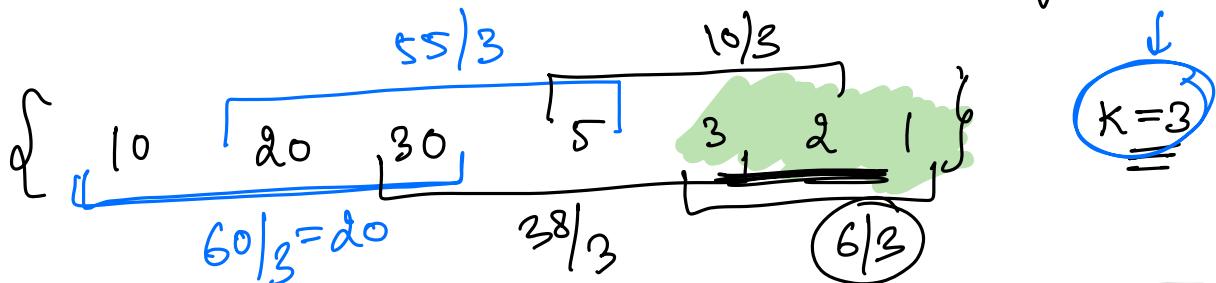
$l0 += arr[i]$

else
 $le += arr[i]$

return ans;

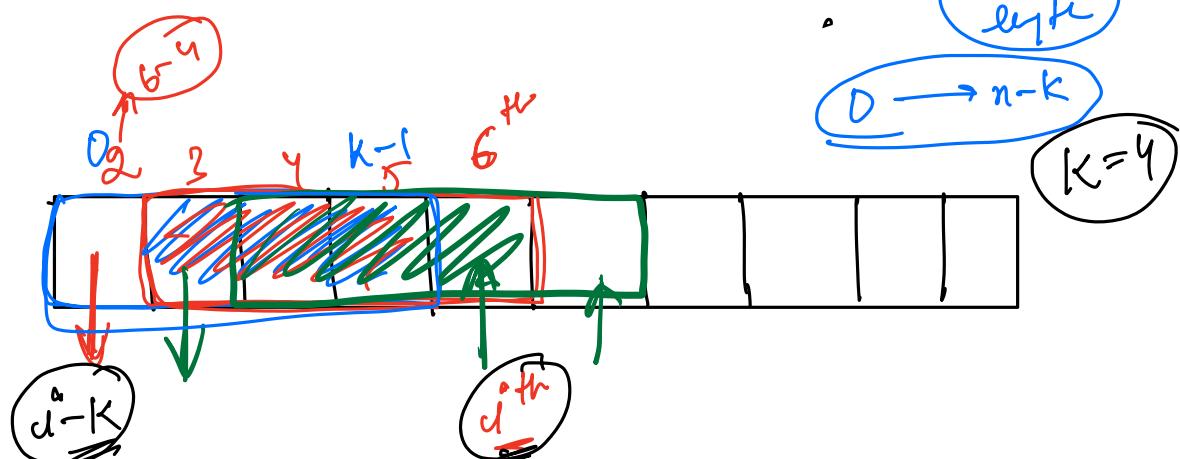
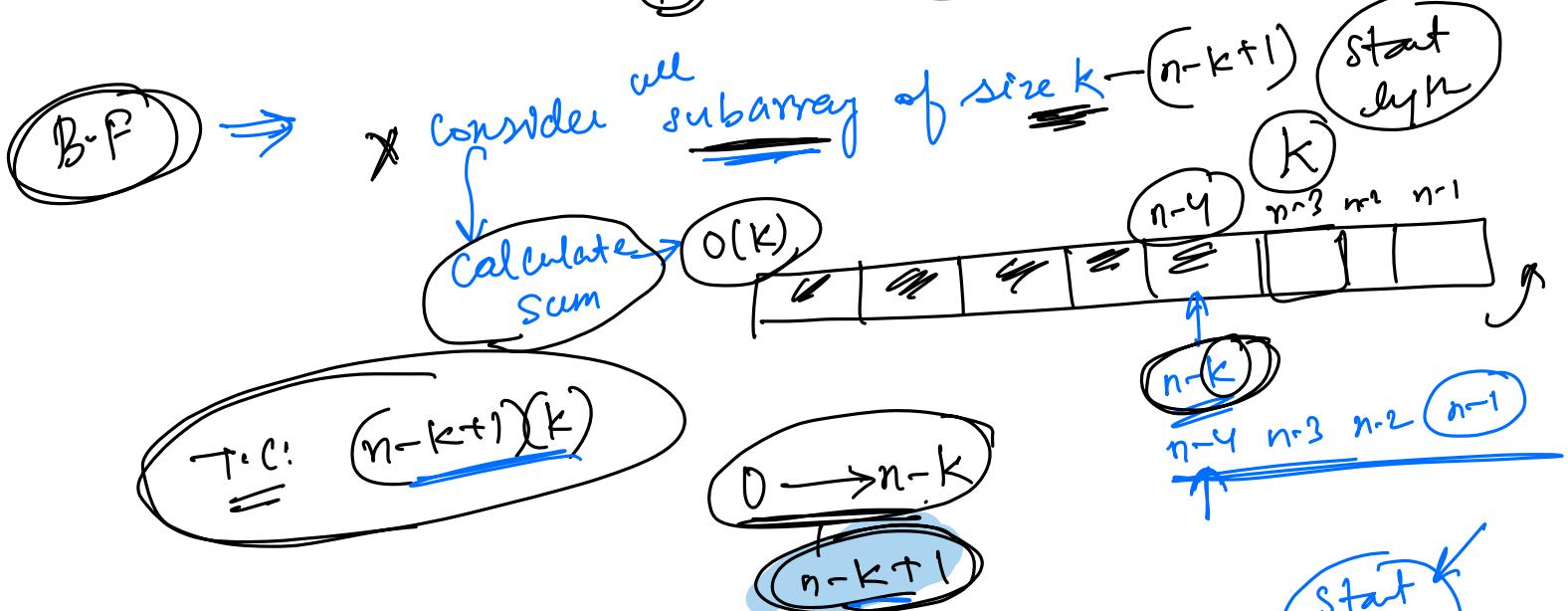
Q Least Average value subarray

Given an array of size N . Find a subarray of size K with least average.



$$\text{average} = \frac{\text{sum}}{K}$$

minimum sum subarray



①

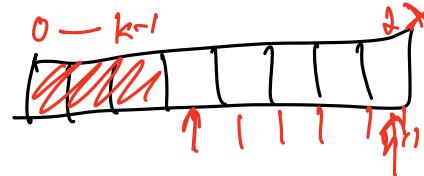
```

int sum = 0           ans = INT-MAX
for i=0 → i<k
    sum += arr[i]
    ans = min(ans, sum);
for j=k → i<n
    sum += arr[i]
    sum -= arr[i-k]
    ans = min(ans, sum)
return ans | K;

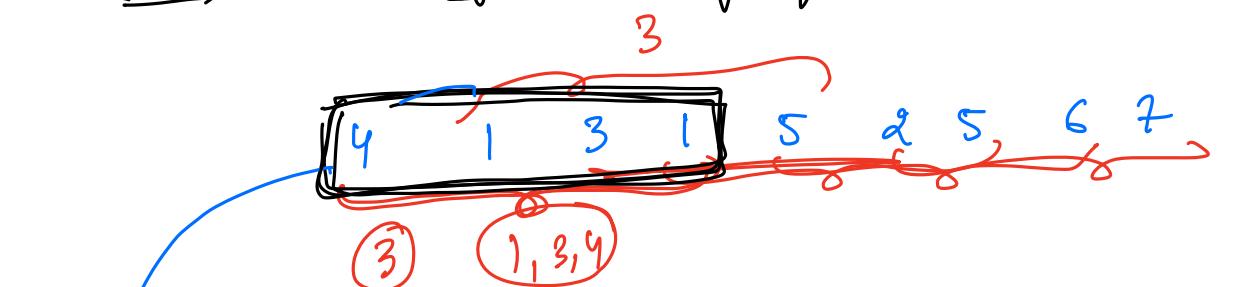
```

 $0 \rightarrow K-1$

~~n-k~~ \Rightarrow $K=3$



Given an array of size N . Find the number of distinct elements in every subarray of size k .

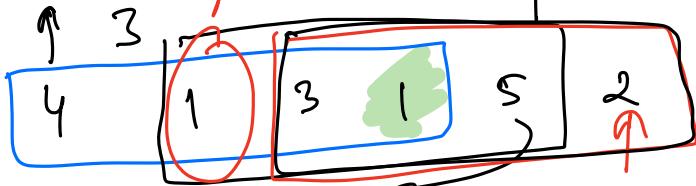
 $K=4$ 

Set? \Rightarrow
Set.size()

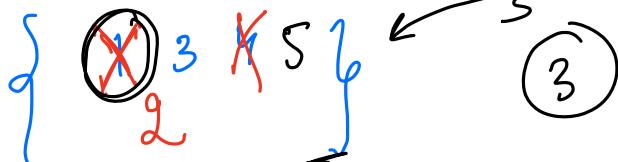
consider every subarray of size k

Set \Leftrightarrow insert my elemt
Set.size()

$O(nrk)$ $\frac{1}{k}$
 $O(n^2)$
For C: $O(k)$



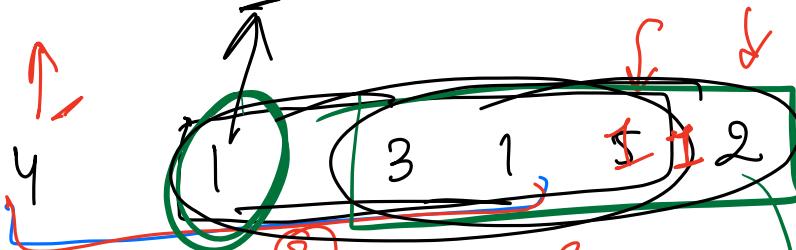
set



~~set~~

freq

map



5 6 7

~~<1, 3>~~
~~(5, 1)~~

~~<1, 2>~~
~~<3, 1>~~
~~<4, 1>~~
~~<5, 1>~~
~~<2, 1>~~

~~<1, 2>~~
~~<2, 1>~~
~~<3, 1>~~

ans = 3

+1
-1

ans = 3

+1
ans = 4

11

map → m <int, int>
int ans = 0;

overli

for i=0 → k
m[arr[i]]++
if(m[arr[i]] == -1)
ans +
1

cout << ans;

T.C: O(n)
S.C: O(n)
O(k)

for i=k → i<n

m[arr[i]]++
arr[i-k] --

if(m[arr[i]] == -1)

ans +

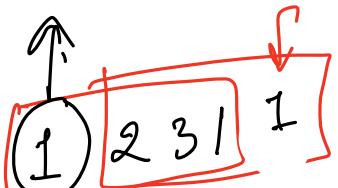
if(m[arr[i-k]] == 0)

ans -

cout << ans;

③ ①

rep. enc



1, 2
2, 1
3, 1

① (1, 2)

1 2 3 4 1

$\omega_0 = \sqrt{g/l}$