

MULTI-DIMENSIONAL ARRAYS

$$3 + 3 + 1 + 1$$

$$3 + 3 + 1$$

$A[i][j]$

$A[2][1]$

$int A[5][3];$

7 elements before A

8 including A

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

$$2 * 3$$

$$+ (3 + 1)$$

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	
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$A[i][j]$

$A[i][j]$

$A[5][3]$
↑ rows ↑ columns

$A[i][j]$
↑ row ↑ col

$$3 * i + j$$

base addr

$$+ \text{num-col} * i + j$$

0 1 2 ... j-1

$A[5][3]$

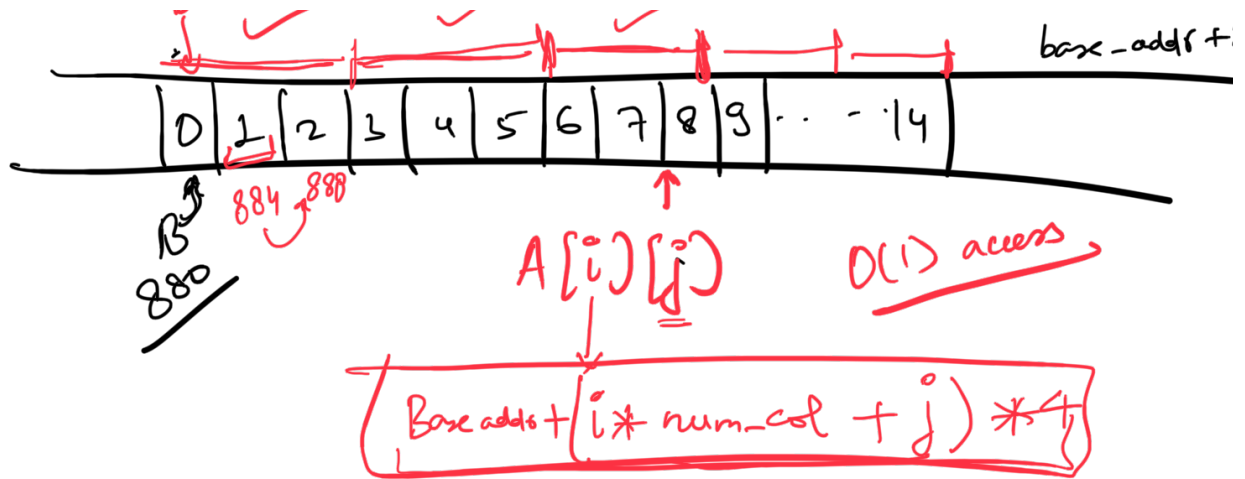
$A[i][j]$
column number
row number

0	1	2
3	4	5
6	7	8
9	10	11
12	13	14

row 0
row 1
row 2

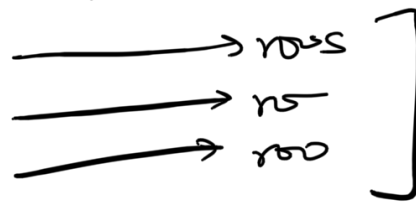
9 10

$A[3][2]$ $A[2]$



Static

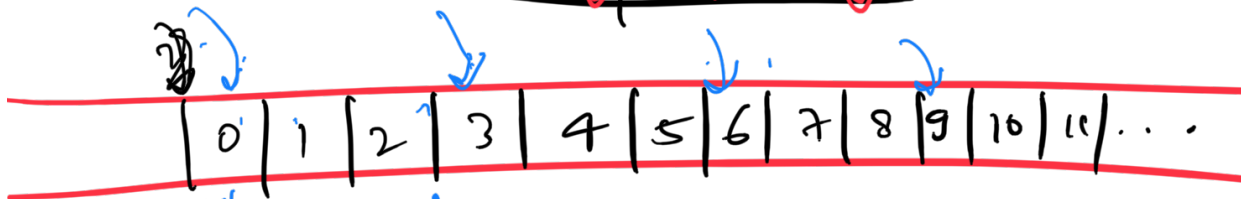
$A[5][3]$



row major
way of storing
numbers

0	1	2
3	4	5
6	7	8
9	10	11
12	13	14

column major



0	0	1	2
1	3	4	5
2	6	7	8
3	9	10	11
4	12	13	14

row major

Code #1

$i \rightarrow 0 \text{ to } 5$
 $j \rightarrow 0 \text{ to } 3$

$j \rightarrow 0 \text{ to } 3$
 $i \rightarrow 0 \text{ to } 5$
print A

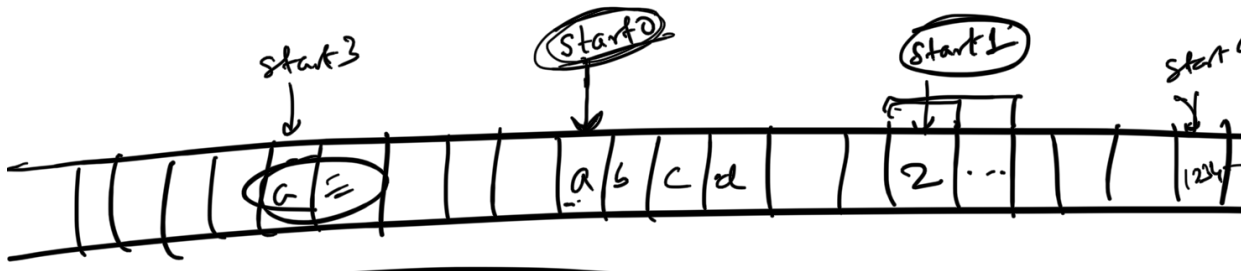
print A[i][j] | 0 3 6 9 12

 0 1 2 3 4 5 6 7 8 ...

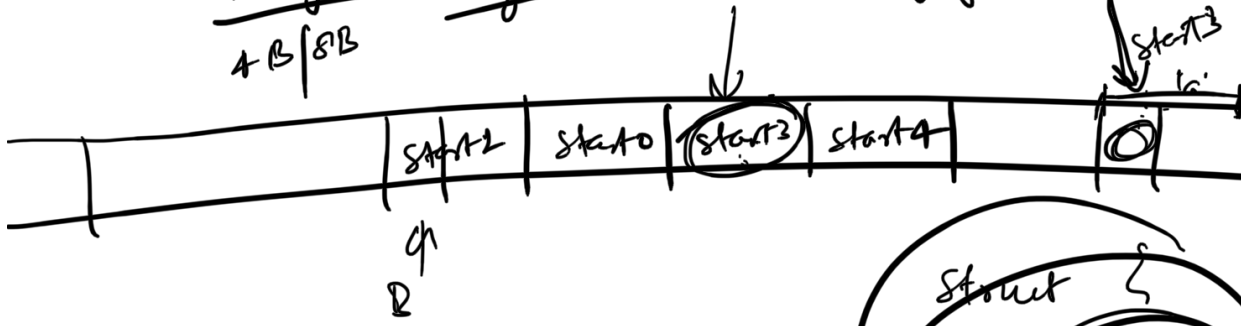
$[\underset{\substack{\uparrow \\ \text{4 bytes}}}{2}, \text{"abcd"}, \text{'a'}, \dots]$
A[i] base-addr + i * size of (A[0])

$[A[i]] \leftarrow O(1)$

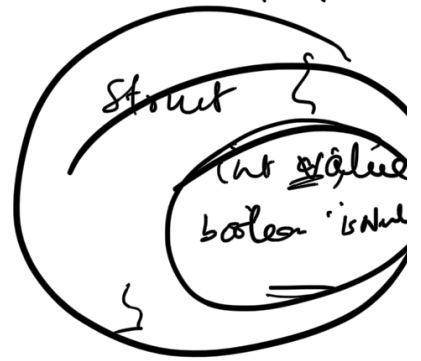
$[\textcircled{2}, \textcircled{\text{"abcd"}}, \textcircled{\text{'a'}}, \textcircled{\text{"234"}}]$ A[2]



$[\text{start0}, \text{start0}, \text{start3}, \text{start4}]$ str = "abcd"
 ↑ ↑
 integer integer
 4B / 8B 4B / 8B



$[\underline{10}, \underline{12}, \underline{13}, \underline{14}]$
 a = "abcde"
 a = "abcd"



$a = 20$
 $a = 40$

immutable

obj. {
 type \leftrightarrow 4 byte
 val \leftrightarrow 4 b

int A[5][3]

15 integers

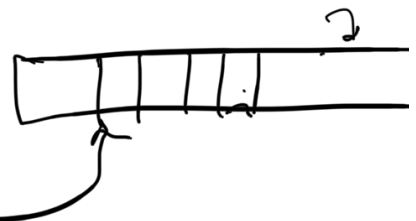
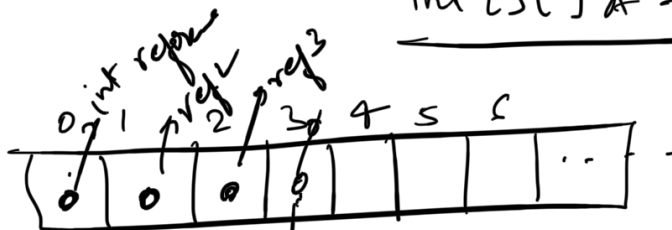
B

vector<int> A[10];

dynamic array



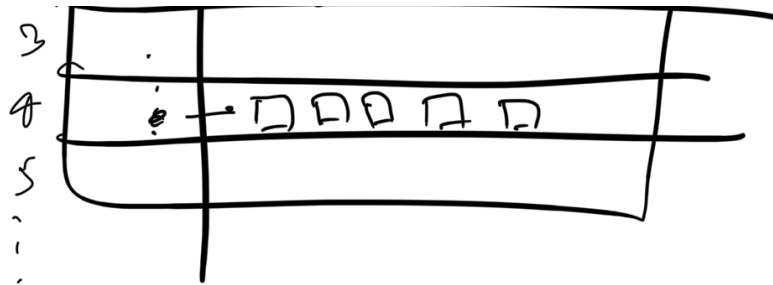
int[][] A = new int[10]



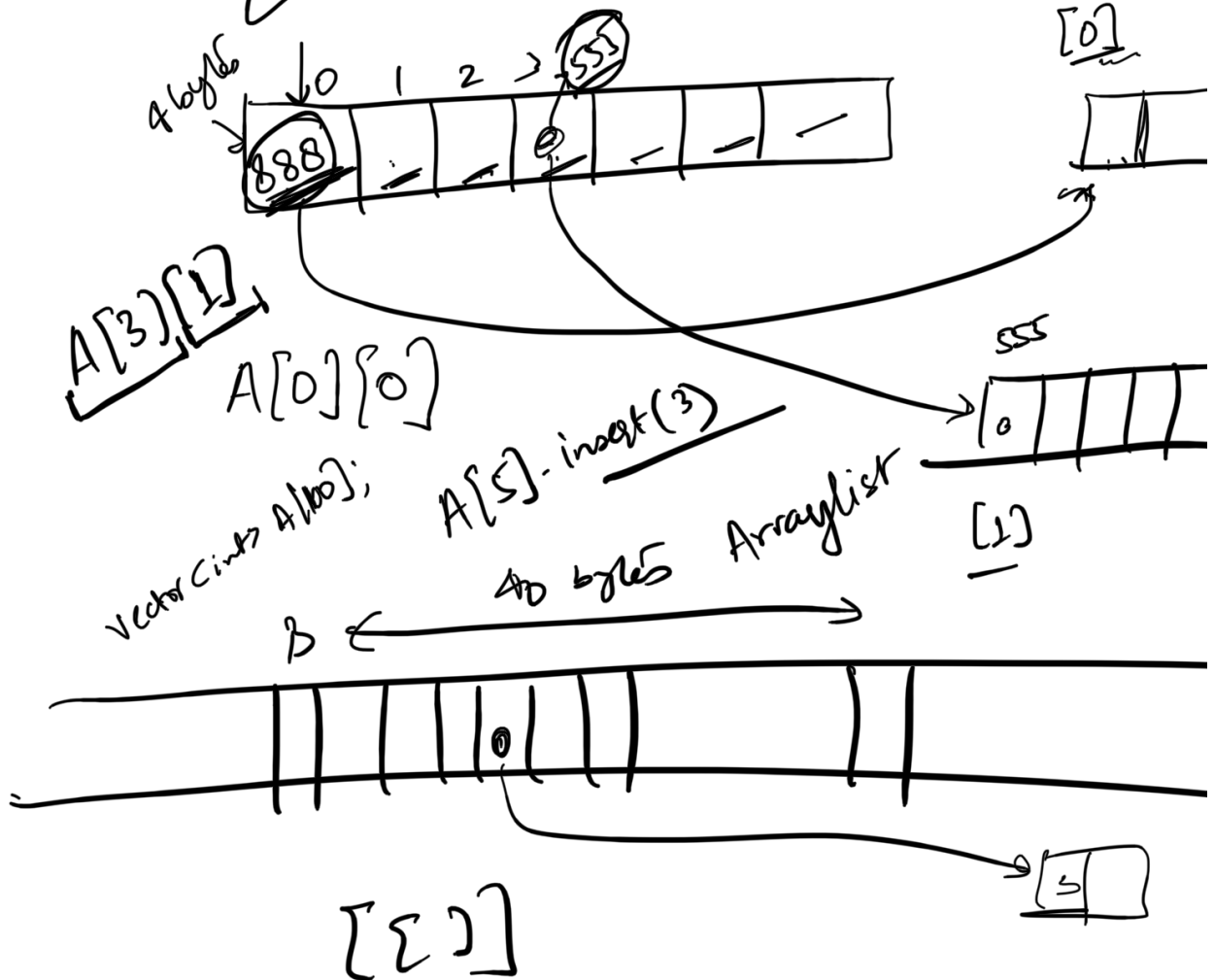
A[10]

→ Static no. of rows.
 Variable no of columns.

0	•	→	2		
1	•	→	2	3	
2	•	→	9	5	6



$\{ \rightarrow \text{Arraylist} < \text{Arraylist} < \text{Integer} > >$
 $\{ \rightarrow \text{vector} < \text{vector} < \text{int} > >$



Arraylist = vector
 = list

C++

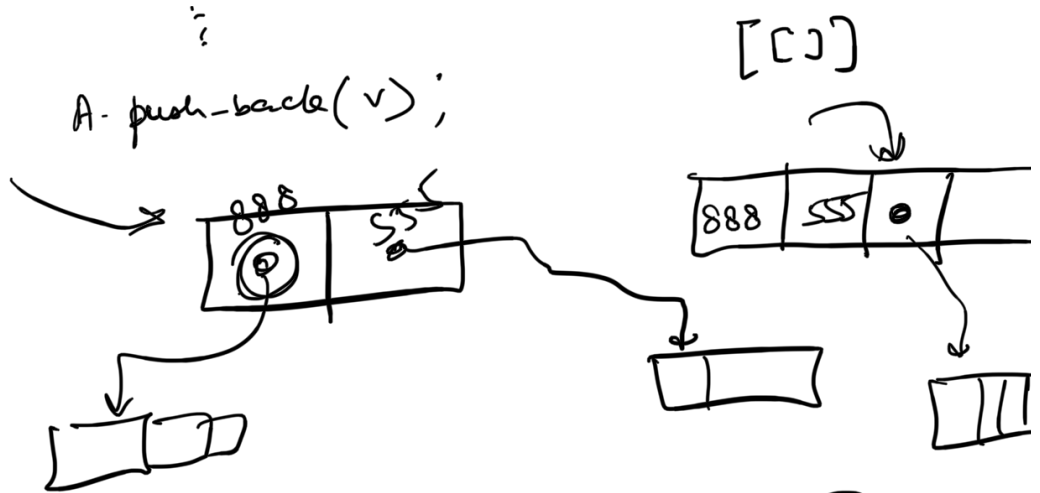
vector<vector<int>> A;

vector<int> v;

JAVA

Arraylist<Arraylist<Integer

Python



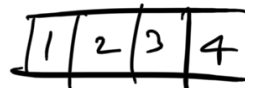
int A[5][3] ← static (15)

Vector c

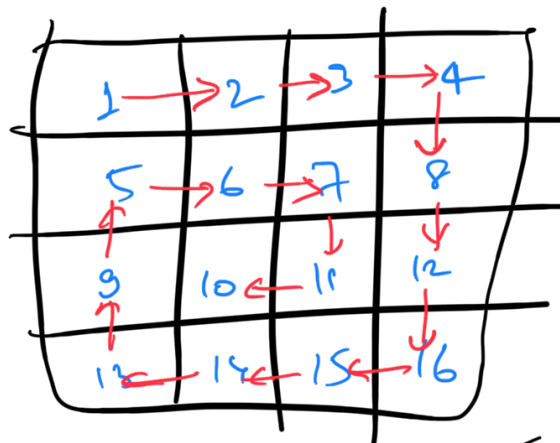
Arraylist Integer > A

A.set(100, 100); A[100]

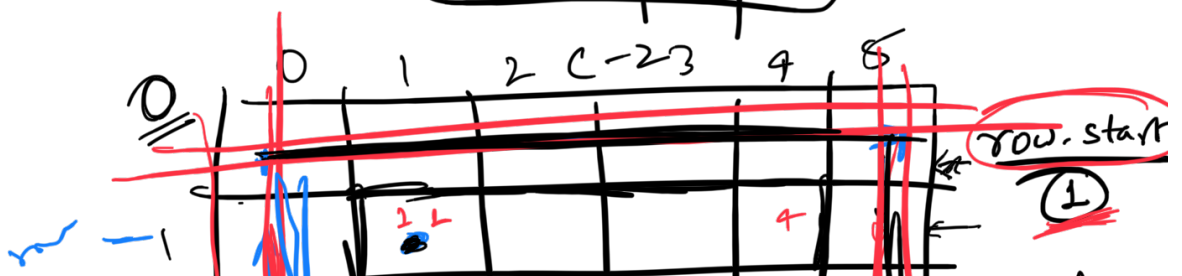
A[1]

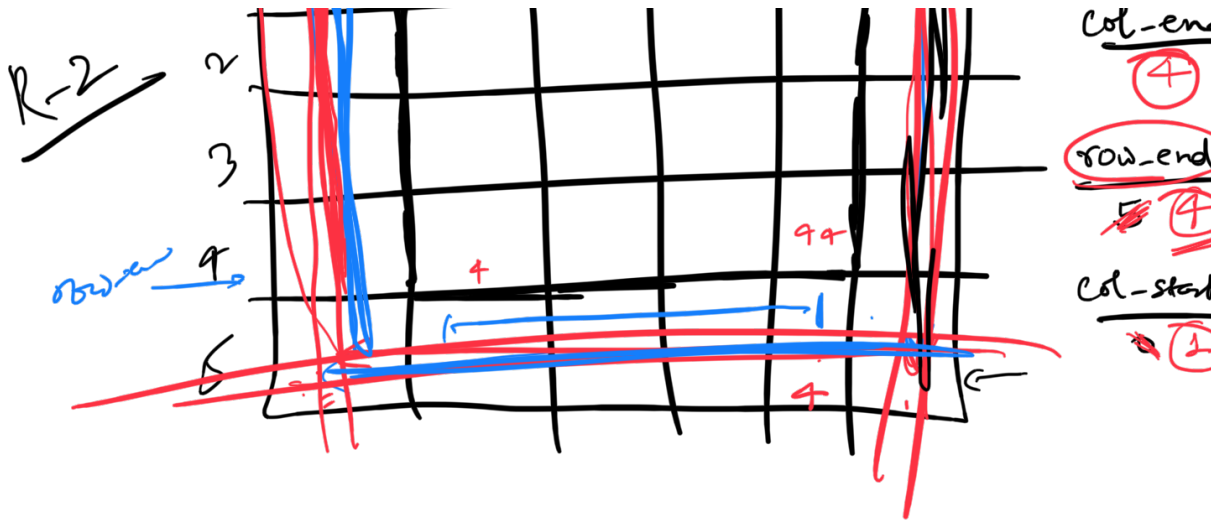


A.insert(1)
A = (1, 3, 4)

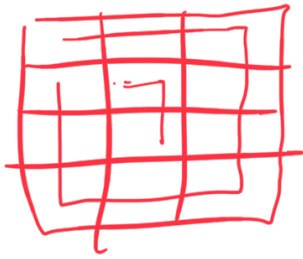


1 2 3 4 8
12 16 15 14
9 5 6 7
10



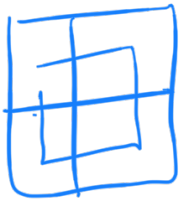


$\text{row_start} = 0$, $\text{row_end} = R-1$, $\text{col_start} = 0$,
 $\text{col_end} = C-1$
 while ($\text{col_start} < \text{col_end}$ & $\text{row_start} < \text{row_end}$) {



printed $\left[\begin{array}{l} \text{C} \rightarrow \text{col_start to col_end} : \\ \text{print } A[\text{row_start}][\text{C}] \\ \text{row_start}++ \end{array} \right.$

print last col $\left[\begin{array}{l} \text{r} \rightarrow \text{row_start to row_end} : \\ \text{print } A[\text{r}][\text{col_end}] \\ \text{col_end}-- \end{array} \right.$



$\text{col_start} = \text{col_end}$
 $\text{row_start} = \text{row_end}$

$\text{C} \rightarrow \text{col_end to col_start} :$
 print $A[\text{row_end}][\text{C}]$

$\text{row_end}--$

$\text{r} \rightarrow \text{row_end to row_start}$
 print $A[\text{r}][\text{col_start}]$

$\text{col_start}++$

$N \leftarrow \text{row}$
 $M \leftarrow \text{col}$
 $O(N \times M)$

$N \times M$ elements

if ($\text{row_start} == \text{row_end}$ & $\text{col_start} == \text{col_end}$)
 print $A[\text{row_start}][\text{col_start}]$

- ① Sum
- ② Column wise

0	0	1	1
0	0	0	1
0	1	1	1
0	0	1	1

Which row
has max
no. of 1