Merge Sort: Counting Inversions ★

Problem

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In an array, arr, the elements at indices i and j (where i < j) form an inversion if arr[i] > arr[j]. In other words, inverted elements arr[i] and arr[j] are considered to be "out of order". To correct an inversion, we can swap adjacent elements.

Example

$$arr = [2,4,1]$$

To sort the array, we must perform the following two swaps to correct the inversions:

$$\mathit{arr} = [2,4,1] \xrightarrow{\mathit{swap}(\mathit{arr}[1],\mathit{arr}[2]) \rightarrow \mathit{swap}(\mathit{arr}[0],\mathit{arr}[1])} [1,2,4]$$

The sort has two inversions: (4,1) and (2,1).

Given an array *arr*, return the number of inversions to sort the array.

Function Description

Complete the function countInversions in the editor below.

countInversions has the following parameter(s):

• int arr[n]: an array of integers to sort

Returns

• int: the number of inversions

Input Format

The first line contains an integer, d, the number of datasets.

Each of the next **d** pairs of lines is as follows:

- 1. The first line contains an integer, **n**, the number of elements in **arr**.
- 2. The second line contains n space-separated integers, arr[i].

Constraints

- $1 \le d \le 15$
- $1 \le n \le 10^5$
- $1 \le arr[i] \le 10^7$

Sample Input

Sample Output

```
0
4
```

Explanation

We sort the following $oldsymbol{d}=\mathbf{2}$ datasets:

```
1. \mathit{arr} = [1, 1, 1, 2, 2] is already sorted, so there are no inversions for us to correct.
```

2.
$$arr = [2,1,3,1,2] \xrightarrow{\text{1 swap}} [1,2,3,1,2] \xrightarrow{\text{2 swaps}} [1,1,2,3,2] \xrightarrow{\text{1 swap}} [1,1,2,2,3]$$

We performed a total of $\mathbf{1} + \mathbf{2} + \mathbf{1} = \mathbf{4}$ swaps to correct inversions.

```
Change Theme Language C#
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24
          */
25
         public static long countInversions(List<int> arr)
26
27
         {
28
             return MergeSort(arr.ToArray());
29
         }
30
31
         private static long MergeSort(Span<int> arr)
32
             {
33
                 long swaps = 0;
                 var center = arr.Length / 2;
34
35
                 if(arr.Length > 1)
36
37
                     swaps += MergeSort(arr.Slice(0, center));
38
                     swaps += MergeSort(arr.Slice(center));
39
                     swaps += Merge(arr, center);
40
41
                 return swaps;
             }
42
43
             private static long Merge(Span<int> arr, int startOfRightHalf)
44
45
             {
                 long swaps = 0;
46
                 var unsorted = arr.ToArray();
47
                 var lhs = 0;
48
                 var rhs = startOfRightHalf;
49
50
                 var offset = 0;
                                                                                                       Line: 104 Col: 1
                                                                                                       Submit Code
                                                                                         Run Code
Test against custom input
```