School of Engineering and Applied Science (SEAS) Ahmedabad University

BTech(ICT) Semester VI:Digital Signal Processing

Laboratory Assignment-4

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AIM :: LAB4 helps to revise the concept of signal and systems. Solving the properties of signal like Linear Convolution, Circular Convolution, DFT, IDFT, IFFT signal in MATLAB . that's clearly shown in plots to understand better.

1. Solution Problem-1

```
close all;
A = input( 'Enter amplitude:: ');
f = input( 'Enter frequency:: ');
P = input( 'Enter initial phase:: ');

'Enter campling frequency:
                                                          %amplitude
                                                          %frequency
                                                          %phase
 6 fs=input( 'Enter sampling frequency:: ');
                                                          %sampling frequency
 7 cycle=input( 'Enter the number of cycle:: '); %no. periods
9 lower_limit=0;
upper_limit=cycle/f;
t=lower_limit:1/fs:upper_limit;
                                                         %input x(n) signal
x=A*cos((2*pi*f).*t + P);
y_ownFunc=DFT(x);
                                                          \mbox{\ensuremath{\mbox{\scriptsize MDFT}}} on x own function
y_inbuiltFunc=fft(x);
                                                          %DFT on x inbuilt function fft
17 % Magnitude
18 magnitude_ownFunc = abs(y_ownFunc);
magnitude_inbuiltFunc = abs(y_inbuiltFunc);
20
21 % Phase
phase_ownFunc = unwrap(angle(y_ownFunc));
phase_inbuiltFunc = unwrap(angle(y_inbuiltFunc));
25 % vector of freq
26 freq_ownFunc = (0:length(y_ownFunc)-1)*100/length(y_ownFunc);
27 freq_inbuiltFunc = (0:length(y_inbuiltFunc)-1)*100/length(y_inbuiltFunc);
29 % IFFT
30 y_ifft = ifft(y_ownFunc);
32 subplot(3,2,1);
33 stem(t, x,'fill','r');
34 hold on;
35 grid on;
36 title('x(n)');
37 xlabel('n');
38 ylabel('Amplitude');
40 subplot(3,2,2);
stem(1:length(y_ifft), y_ifft,'fill','r');
42 hold on;
43 grid on;
44 title('IFFT of DFT of x(n)');
45 xlabel('n');
46 ylabel('Amplitude');
```

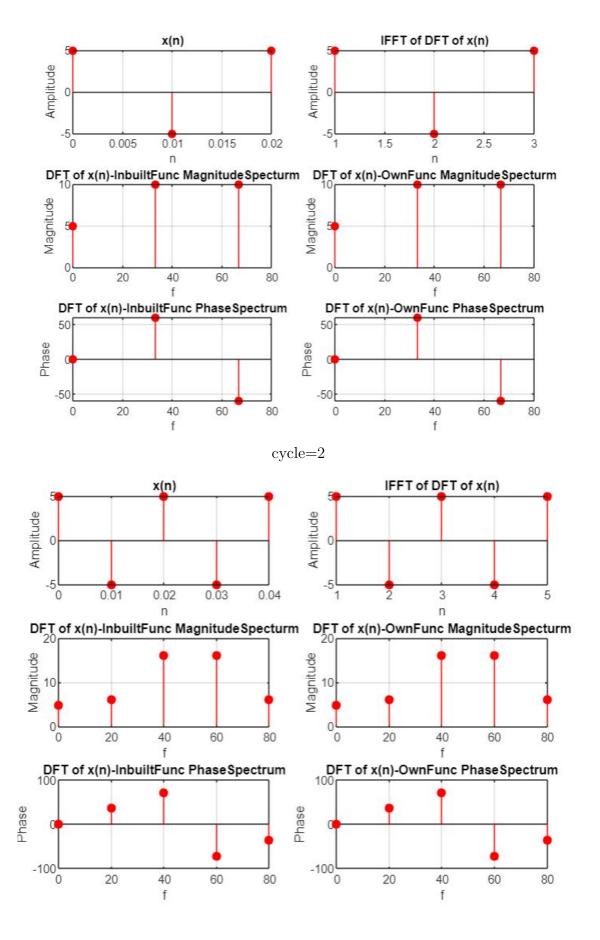
```
48 subplot (3,2,3);
49 stem(freq_inbuiltFunc, magnitude_inbuiltFunc, 'fill','r');
50 hold on;
51 grid on;
52 title('DFT of x(n)-InbuiltFunc MagnitudeSpecturm');
ss xlabel('f');
54 ylabel('Magnitude');
56 subplot (3,2,4);
stem(freq_ownFunc, magnitude_ownFunc, 'fill', 'r');
59 grid on;
title('DFT of x(n)-OwnFunc MagnitudeSpecturm');
61 xlabel('f');
92 ylabel('Magnitude');
64 subplot (3,2,5);
65 stem(freq_inbuiltFunc, phase_inbuiltFunc*180/pi, 'fill', 'r');
66 hold on;
67 grid on;
68 title('DFT of x(n)-InbuiltFunc PhaseSpectrum');
69 xlabel('f');
70 ylabel('Phase');
72 subplot(3,2,6);
73 stem(freq_ownFunc, phase_ownFunc*180/pi,'fill','r');
75 grid on;
76 title('DFT of x(n)-OwnFunc PhaseSpectrum');
77 xlabel('f');
78 ylabel('Phase');
80 %function for DFT of x(n) for N points
81 function y=DFT(x, N)
     if nargin < 2
          N=length(x);
83
84
      end
      y=zeros(1, max(N, length(x)));
85
      %k,n is from 1 to k,N, instead of k,n it be k-1,n-1
86
      for k=1:N
87
          arg = -2*pi*(k-1)/N;
88
          for n=1:min(N, length(x))
89
               ejtheta=exp(arg*(n-1)*1j);
               y(k)=y(k)+(x(n)*ejtheta);
91
           end
92
93
      end
94 end
```

DFT possible for ,N length(x), summing from n=0 to N-1 [x(n)*exp(arg*n*j)] which is equal to y(k); where arg=-2*pi*k/N all k from 0 to N-1,length(y)=N.after Looping from k=1 to N to get y(k). k-1 instead of k; arg=-2*pi*(k-1)/N; n from 1 to min(N, length(x)). finally,y(k)=y(k)+(x(n)*exp(arg*(n-1)*1j)).

(c) Simulation Output:

Inputs for: A=5; f=50; P=0; fs=2*f=100;

cycle=1



2. Solution Problem-2

(a) Matlab Script for 2(a):

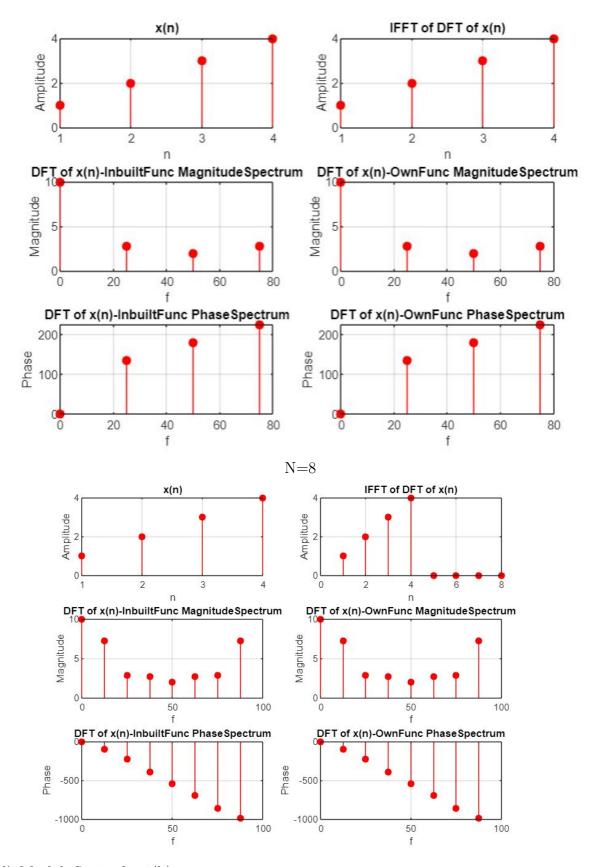
```
1 clc;
close all;
x = [1 \ 2 \ 3 \ 4];
                                       %input signal x(n)
_{4} N=4;
                                       %length of DFT
5 \% N = 8;
                                       %length of DFT
7 y_ownFunc=DFT(x,N);
                                       %DFT on x own function
8 y_inbuiltFunc=fft(x,N);
                                       %DFT on x own function fft
10 %Magnitude
magnitude_ownFunc = abs(y_ownFunc);
magnitude_inbuiltFunc = abs(y_inbuiltFunc);
14 % Phase
phase_ownFunc = unwrap(angle(y_ownFunc));
phase_inbuiltFunc = unwrap(angle(y_inbuiltFunc));
18 % vector of freq
freq_ownFunc = (0:length(y_ownFunc)-1)*100/length(y_ownFunc);
20 freq_inbuiltFunc = (0:length(y_inbuiltFunc)-1)*100/length(y_inbuiltFunc);
21
22 % IFFT
y_ifft = ifft(y_ownFunc,N);
25 subplot(3,2,1);
26 stem(1:length(x), x,'fill','r');
27 hold on;
28 grid on;
29 title('x(n)');
30 xlabel('n');
31 ylabel('Amplitude');
33 subplot (3,2,2);
stem(1:length(y_ifft), y_ifft,'fill','r');
35 hold on;
36 grid on;
title('IFFT of DFT of x(n)');
38 xlabel('n');
39 ylabel('Amplitude');
40
41 subplot(3,2,3);
42 stem(freq_inbuiltFunc, magnitude_inbuiltFunc, 'fill','r');
43 hold on;
44 grid on;
45 title('DFT of x(n)-InbuiltFunc MagnitudeSpectrum');
46 xlabel('f');
47 ylabel('Magnitude');
49 subplot (3,2,4);
50 stem(freq_ownFunc, magnitude_ownFunc,'fill','r');
51 hold on;
52 grid on;
53 title('DFT of x(n)-OwnFunc MagnitudeSpectrum');
54 xlabel('f');
55 ylabel('Magnitude');
57 subplot(3,2,5);
58 stem(freq_inbuiltFunc, phase_inbuiltFunc*180/pi, 'fill','r');
59 hold on;
60 grid on;
fititle('DFT of x(n)-InbuiltFunc PhaseSpectrum');
62 xlabel('f');
63 ylabel('Phase');
65 subplot (3,2,6);
stem(freq_ownFunc, phase_ownFunc*180/pi,'fill','r');
```

```
67 hold on;
68 grid on;
title('DFT of x(n)-OwnFunc PhaseSpectrum');
70 xlabel('f');
71 ylabel('Phase');
73 %function for DFT of x(n) for N points
74 function y=DFT(x, N)
75
       if nargin < 2
            N=length(x);
76
       end
77
78
       y=zeros(1, max(N, length(x)));
        \mbox{\ensuremath{\mbox{\%}}} k\,, n is from 1 to k\,, \mbox{\ensuremath{\mbox{N}}}\,, instead of k\,, n it be k\,-\,1\,, n\,-\,1
79
      for k=1:N
           arg=-2*pi*(k-1)/N;
81
            for n=1:min(N, length(x))
82
                 ejtheta=exp(arg*(n-1)*1j);
83
                 y(k)=y(k)+(x(n)*ejtheta);
84
            end
85
86
        \verb"end"
87 end
```

own function first argument x and second argument (N) a number of points for the transform, which is DFT length. DFT posssible for N length(x), summing from n=0 to N-1 [x(n)*exp(arg*n*j)] which is equal to y(k); where arg=-2*pi*k/N all k from 0 to N-1, length(y)=N. after Looping from k=1 to N to get y(k). k-1 instead of k; arg=-2*pi*(k-1)/N; n from 1 to min(N, length(x)). finally, y(k)=y(k)+(x(n)*exp(arg*(n-1)*1j)).

(c) Simulation Output:

N=4



(d) Matlab Script for 2(b):

1 clc;

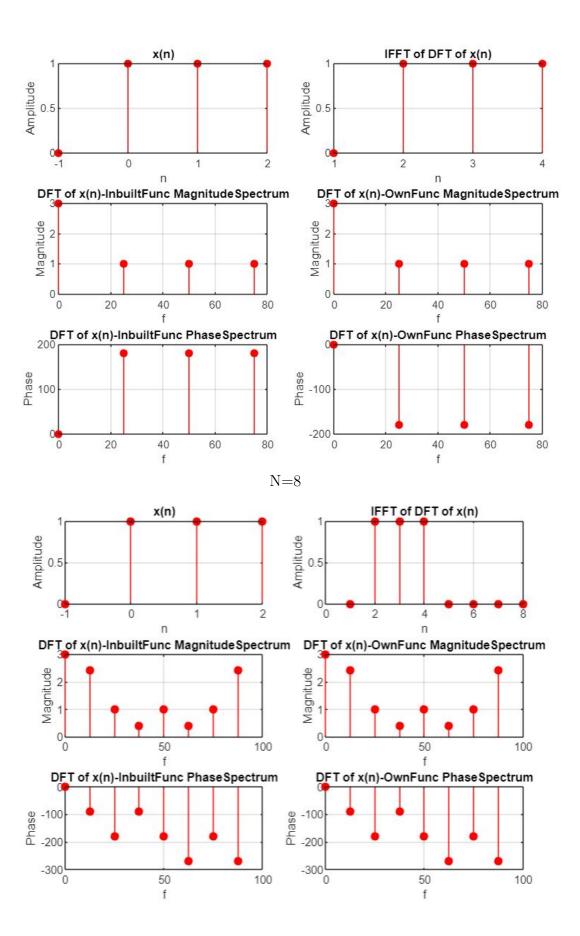
```
close all;
n = -1:1:2;
                                       %input signal
x=u(n)-u(n-3);
6 N = 4;
                                        %length of DFT
7 \% N = 8;
                                        %length of DFT
9 y_ownFunc=DFT(x,N);
                                       %DFT on x own function %DFT on x own function fft
y_inbuiltFunc=fft(x,N);
12 %Magnitude
magnitude_ownFunc = abs(y_ownFunc);
magnitude_inbuiltFunc = abs(y_inbuiltFunc);
16 % Phase
phase_ownFunc = unwrap(angle(y_ownFunc));
phase_inbuiltFunc = unwrap(angle(y_inbuiltFunc));
19
20 % vector of freq
21 freq_ownFunc = (0:length(y_ownFunc)-1)*100/length(y_ownFunc);
freq_inbuiltFunc = (0:length(y_inbuiltFunc)-1)*100/length(y_inbuiltFunc);
24 % IFFT
y_ifft = ifft(y_ownFunc,N);
27 subplot(3,2,1);
28 stem(n, x,'fill','r');
29 hold on;
30 grid on;
31 title('x(n)');
32 xlabel('n');
33 ylabel('Amplitude');
35 subplot (3,2,2);
stem(1:length(y_ifft), y_ifft,'fill','r');
37 hold on;
38 grid on;
39 title('IFFT of DFT of x(n)');
40 xlabel('n');
41 ylabel('Amplitude');
43 subplot (3,2,3);
stem(freq_inbuiltFunc, magnitude_inbuiltFunc, 'fill', 'r');
45 hold on;
46 grid on;
47 title('DFT of x(n)-InbuiltFunc MagnitudeSpectrum');
48 xlabel('f');
49 ylabel('Magnitude');
51 subplot(3,2,4);
52 stem(freq_ownFunc, magnitude_ownFunc,'fill','r');
53 hold on;
54 grid on;
55 title('DFT of x(n)-OwnFunc MagnitudeSpectrum');
s6 xlabel('f');
57 ylabel('Magnitude');
59 subplot(3,2,5);
stem(freq_inbuiltFunc, phase_inbuiltFunc*180/pi, 'fill','r');
62 grid on;
63 title('DFT of x(n)-InbuiltFunc PhaseSpectrum');
64 xlabel('f');
glabel('Phase');
67 subplot (3,2,6);
68 stem(freq_ownFunc, phase_ownFunc*180/pi,'fill','r');
69 hold on;
70 grid on;
71 title('DFT of x(n)-OwnFunc PhaseSpectrum');
```

```
72 xlabel('f');
73 ylabel('Phase');
75 %function for DFT of x(n) for N points
function y=DFT(x, N)
      if nargin < 2
          N=length(x);
78
79
      y=zeros(1, max(N, length(x)));
80
      %k,n is from 1 to k,N, instead of k,n it be k-1,n-1
81
      for k=1:N
82
83
        arg = -2*pi*(k-1)/N;
          for n=1:min(N, length(x))
84
               ejtheta=exp(arg*(n-1)*1j);
               y(k)=y(k)+(x(n)*ejtheta);
86
           end
87
88
89 end
_{90} %function for unit step signal ,If current value is greater than 0,output value=1
      elsewhere 0
91 function y = u(n)
92
      y=zeros(1, length(n));
       for i=1:length(n)
93
           if n(i) >= 0
94
95
               y(i)=1;
96
               y(i)=0;
97
           end
98
       end
99
100 end
```

own function first argument x and second argument (N) a number of points for the transform, which is DFT length. Calculating Unit step function for input sequence and DFT posssible for N length(x), summing from n = 0 to N-1 [x(n)*exp(arg*n*j)] which is equal to y(k); where arg = -2*pi*k/N all k from 0 to N-1, length(y)=N. after Looping from k = 1 to N to get y(k). k-1 instead of k; arg=-2*pi*(k-1)/N; n from 1 to min(N, length(x)). finally, y(k)=y(k)+(x(n)*exp(arg*(n-1)*1j)).

(f) Simulation Output:

N=4



3. Solution Problem-3

```
1 % Case 1
 2 x1=[1 -1 -2 3 -1];
3 x2=[1 2 3];
  _4 %N=length(x1)+length(x2)-1;
 5 % Case 2
 6 \% x1 = [1 2 1 2];
 7 \% x2 = [3 2 1 4];
 8 \% N = length(x1) + length(x2) - 1;
 9 % Case 3
10 % x1=[1 2 3 4];
11 \% x2=u(n)-u(n-3);
12 %N=-1:1:length(x1);
13 clc;
14 close all;
16 %circular convo
N=length(x1)+length(x2)-1;
{\tt 19} \ {\tt cirConvoOwnFunc=cir\_convo\_ownFunc(x1, x2, N);} \ {\tt \%CirculaurConvo} \ {\tt of} \ {\tt x} \ {\tt own} \ {\tt function}
20 cirConvoInbuiltFunc=cconv([x1 zeros(1, max(0,length(x1)-1))],[x2 zeros(1, max(0,
               length(x2)-1))], N); %CirculaurConvo of x inbuilt function
22 %linear convo
linConvoOwnFunc=lin_convo_ownFunc(x1, x2, N); %linearConvo of x own function linConvoInbuiltFunc=conv([x1 zeros(1, max(0,length(x1)-1))], [x2 zeros(1, max(0,length(x1)-1))], [x2 zeros(1, max(0,length(x1)-1))], [x2 zeros(1, max(0,length(x1)-1))], [x3 zeros(1, max(0,length(x1)-1))], [x4 zeros(1, max(0,length(x1)-1))], [x5 zeros(1, max(0,length(x1)-1))], 
                length(x2)-1))], N); %linearConvo of x inbuilt function
26 subplot(3,2,1);
27 stem(1:1:length(x1), x1,'fill','r');
28 hold on;
29 grid on;
30 title('x1(n)');
xlabel('n');
32 ylabel('Amplitude');
34 subplot (3,2,2);
35 stem(1:1:length(x2), x2,'fill','r');
36 hold on;
37 grid on;
38 title('x2(n)');
39 xlabel('n');
40 ylabel('Amplitude');
41
42 subplot(3,2,3);
43 stem(1:1:length(cirConvoInbuiltFunc), cirConvoInbuiltFunc, 'fill', 'r');
44 hold on;
45 grid on;
46 title('Cirular Convo-InbuiltFunc');
47 xlabel('n');
48 ylabel('Amplitude');
50 subplot(3,2,4);
51 stem(1:1:length(cirConvoOwnFunc), cirConvoOwnFunc,'fill','r');
52 hold on;
53 grid on;
54 title('Cirular Convo-OwnFunc');
ss xlabel('n');
56 ylabel('Amplitude');
57
58 subplot(3,2,5);
59 stem(1:1:length(linConvoInbuiltFunc), linConvoInbuiltFunc, 'fill','r');
60 hold on;
61 grid on;
62 title('Linear Convo-InbuiltFunc');
63 xlabel('n');
64 ylabel('Amplitude');
```

```
66 subplot (3,2,6);
67 stem(1:1:length(linConvoOwnFunc), linConvoOwnFunc,'fill','r');
68 hold on;
69 grid on;
70 title('Linear Convo-OwnFunc');
71 xlabel('n');
72 ylabel('Amplitude');
74 %function for DFT of x(n) for N points
75 function y=DFT(x, N)
      if nargin < 2
          N=length(x);
77
       y=zeros(1, max(N, length(x)));
79
       %k,n is from 1 to k,N, instead of k,n it be k-1,n-1
80
      for k=1:N
81
         arg = -2*pi*(k-1)/N;
82
83
           for n=1:min(N, length(x))
84
               ejtheta=exp(arg*(n-1)*1j);
85
               y(k)=y(k)+(x(n)*ejtheta);
           end
86
       end
87
88 end
90 %circular convolution of x(n) using own DFT func
91 function cirConv=cir_convo_ownFunc(x1, x2, N)
       min_n=length(x1)+length(x2)-1;
92
       if nargin < 2
93
           N=min_n;
94
95
       cirConv = ifft(DFT(x1, N).*DFT(x2, N));
96
98
99 %linear convolution of x(n) using own DFT func
function linConv=lin_convo_ownFunc(x1, x2, N)
      min_n = length(x1) + length(x2) - 1;
102
       if nargin < 2
           N=min_n;
103
104
       linConv = ifft(DFT(x1, N).*DFT(x2, N));
105
106 end
107
_{108} %function for unit step signal ,If current value is greater than 0,
      output value=1 elsewhere 0
function y = u(n)
     y=zeros(1, length(n));
110
       for i=1:length(n)
111
          if n(i) >= 0
              y(i)=1;
113
114
               y(i)=0;
115
           end
116
       end
117
118 end
119
```

linear convolution using circular convolution of x1(n) of length L and x2(n) of length M.they should be made of equal length by appending M-1 zeros to x1(n) and L-1 zeros to x2(n).that's why sequences must be made N, Once the zeros are appended, the N point circular convolution of gives the linear convolution of the sequence.DFT possible for ,N length(x), summing from n=0 to N-1 [x(n)*exp(arg*n*j)] which is equal to y(k); where arg=-2*pi*k/N all k from 0 to N-1,length(y)=N.after Looping from k=1 to N to get y(k). k-1 instead of k; arg=-2*pi*(k-1)/N; n from 1 to min(N, length(x)). finally,y(k)=y(k)+(x(n)*exp(arg*(n-1)*1j)).

(c) Simulation Output:

$$\text{case (a) } x1(n) = \{1,-1,-2,3,-1\} \text{ and } x2(n) = \{1,2,3\}$$

$$\text{x1(n)}$$

$$\text{x2(n)}$$

$$\text{x2(n)}$$

$$\text{philder Convo-InbuiltFunc}$$

$$\text{Cirular Convo-OwnFunc}$$

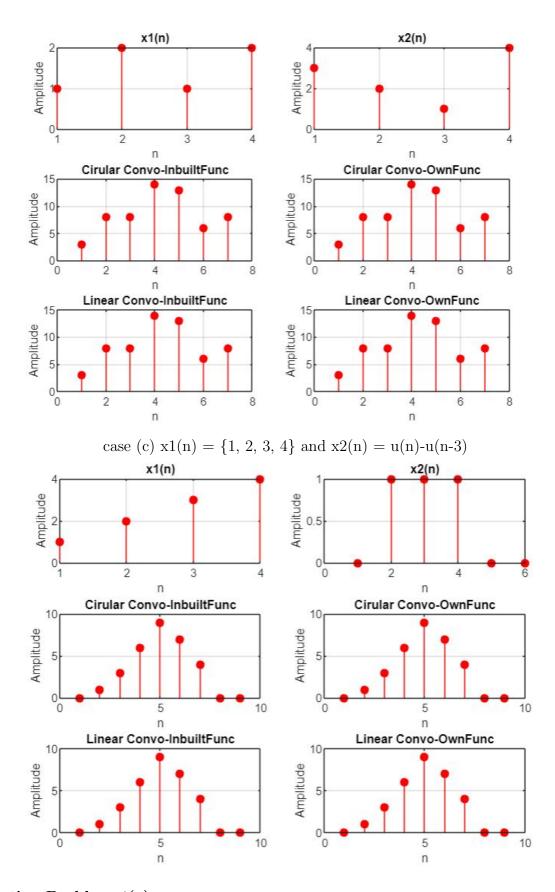
$$\text{Cirular Convo-InbuiltFunc}$$

$$\text{Linear Convo-InbuiltFunc}$$

$$\text{Linear Convo-OwnFunc}$$

$$\text{Linear Convo-OwnFunc}$$

case (b) $x1(n) = \{1, 2, 1, 2\}$ and $x2(n) = \{3,2,1,4\}$



4. Solution Problem-4(a)

- 1.[y,Fs] = audioread(filename) reads data from filename, and returns sampled data(y) and a sample rate for that data (Fs)
- 2.audiowrite(filename,y,Fs) writes a matrix of audio data(y) with sample rate (Fs) to a file called filename.
- 3.y = filter(b,a,x) filters input x using a rational transfer function coefficients b and a.
- 4.y = fftshift(x) does a Fourier transform on x and shifts the zero freq component to the center of the array.
- 5.[b,a] = butter(n,Wn,ftype) designs a diff types of filters lowpass, highpass, bandpass or bandsto.It depends on the value of ftype also number of elements of Wn.

Solution Problem-4(b)

```
1 clc;
close all;
filename="sample_sound.wav";
4 [y, fs]=audioread(filename);
                                               % read the audio file
N = length(y);
                                               % Length of vector y
y_{fft} = fft(y,N);
                                               % Fourier transform of y
7 y_magnitude = abs(y_fft);
                                               % Magnitude of the FFT of y
8 y_phase = unwrap(angle(y_fft));
                                               % Phase of the FFT of y
9 freq_min=0;
                                               % minimum frequency
10 freq_max = (1-1/N)*fs;
                                               % maximum frequency
11 df=fs/N;
12 f = freq_min:df:freq_max;
13 w = 2*pi*f;
                                               % omega
14 freq_normalized = f/freq_max;
                                                % Normalized frequency
t=(0:1:length(y)-1)/fs;
fprintf("\nThe sampling frequency is %d Hz\n ", fs);
fprintf("\nMinimum frequency is %f Hz and Maximum frequency is %f Hz\n", min(y),
      max(y));
18 fprintf("\nNormalized frequency is %f Hz\n", max(freq_normalized) );
19 subplot (3,2,1);
20 plot(t, y,'r');
21 hold on;
22 grid on;
title('Time Domain Signal');
24 xlabel('n');
ylabel('Amplitude');
27 subplot (3,2,2);
28 plot(f, y_magnitude,'r');
29 hold on;
30 grid on;
title('Magnitude Spectrum of Signal');
32 xlabel('f');
33 ylabel('Magnitude');
35 subplot (3,2,3);
36 plot(f, y_phase*180/pi,'r');
37 hold on;
38 grid on;
39 title('Phase Spectrum of Signal');
40 xlabel('f');
ylabel('Phase');
43 subplot (3,2,4);
44 plot(freq_normalized, y_magnitude,'r');
45 hold on;
46 grid on;
47 title('Magnitude Spectrum of Signal');
48 xlabel('Normalized frequency');
49 ylabel('Magnitude');
51 subplot(3,2,5);
52 plot(freq_normalized, y_phase*180/pi,'r');
```

```
hold on;
grid on;
title('Phase Spectrum of Signal');
klabel('Normalized frequency ');
ylabel('Phase');
```

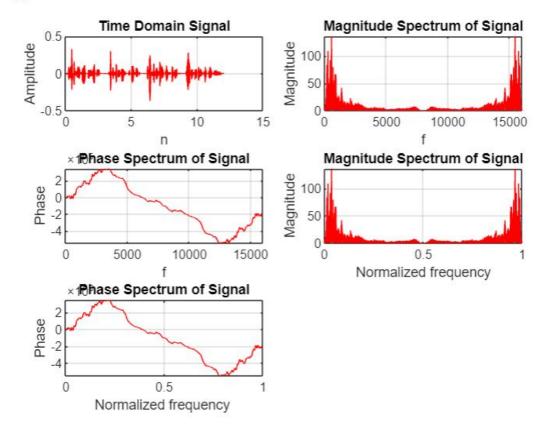
Reading the audio file using audioread function then FFT on file using fft command. Normalized the frequency like f/maxf and getting magnitude and phase spectrum using abs and angle function. Plotting this values in graph

(c) Simulation Output:

The sampling frequency is 16000 Hz

Minimum frequency is -0.366730 Hz and Maximum frequency is 0.328491 Hz

Normalized frequency is 1.000000 Hz >>



Solution Problem-4(c)

```
7 y_magnitude = abs(y_fft);
                                                % Magnitude of the FFT of y
8 y_phase = unwrap(angle(y_fft));
                                                % Phase of the FFT of y
9 freq_min=0;
                                                % minimum frequency
10 freq_max=(1-1/N)*fs;
                                                % maximum frequency
df=fs/N;
12 f = freq_min:df:freq_max;
13 w = 2*pi*f;
                                                % omega
14 freq_normalized = f/freq_max;
                                                % Normalized frequency
15 t=(0:1:length(y)-1)/fs;
16 %Noise
noise=0.5*\cos(2*pi*2*t);
yn=zeros(1, length(y));
19 %Addition of Noise
20 for idx=1:length(t)
      yn(idx)=y(idx)+noise(idx);
21
22 end
23 filename="sample_sound_with_noise_addition.wav";
audiowrite(filename, yn, fs);
                                                % read the noisy file
25 [yn, fsn] = audioread(filename);
26 [b,a] = butter(3, [0.3 0.7], 'bandpass');
_{27} % nth-order bandpass digital Butterworth filter; n = 3
28 y_filteresignal=filter(b, a, yn); % filtering the noisy signal
audiowrite("sample_sound_filtered.wav", y_filteresignal, fsn);
31 fprintf("\nThe sampling frequency is %d Hz\n", fs);
fprintf("\nMinimum frequency is %f Hz and Maximum frequency is %f Hz\n", min(y),
      max(y));
33 subplot (2,2,1);
34 plot(t, y,'r');
35 hold on;
36 grid on;
37 title('Time Domain Signal');
38 xlabel('n');
39 ylabel('Amplitude');
41 subplot(2,2,2);
42 plot(t, noise,'r');
43 hold on;
44 grid on;
45 title('Noise Signal');
46 xlabel('n');
47 ylabel('Amplitude');
49 subplot(2,2,3);
50 plot(t, yn,'r');
51 hold on;
52 grid on;
53 title('Original + noise ');
54 xlabel('n');
55 ylabel('Amplitude');
57 subplot(2,2,4);
plot(t, y_filteresignal,'r');
59 hold on;
60 grid on;
61 title('Signal after filtering');
62 xlabel('n');
63 ylabel('Amplitude');
```

Reading the audio file using audioread function then FFT on file using fft command. Normalized the frequency like f/maxf and getting magnitude and phase spectrum using abs and angle function. Then generate Noisy signal and adding to original signal and take butter filter and filter addition signal . Plotting this values in graph

(c) Simulation Output:

The sampling frequency is 16000 Hz

Minimum frequency is -0.366730 Hz and Maximum frequency is 0.328491 Hz

