

School of Engineering and Applied Science (SEAS)
Ahmedabad University

BTech(ICT) Semester VI: Digital Signal Processing

Laboratory Assignment-6

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AIM :: Lab6 helps to solve the properties of signal like LTI Systems, DTFT-IDTFT, Sampling Theorem, Digital Frequency signal in MATLAB. The filter's impulse response is a sinc function in the time domain, and its frequency response is a rectangular function

1. Solution Problem-1

(a) Matlab Script:

```
1 clc;
2 close all ;
3
4 fC=1/6; %cut-off freq
5 fL=1/9; %lower edge cut-off freq for Band-Pass and Band-Stop
   Filter
6 fH=1/3; %higher edge cut-off freq for Band-Pass and Band-Stop
   Filter
7 n=linspace(-20, 20); %given interval in Question
8
9 Hn_LowPass=2*fC*sinc(2*fC*n); %impulse response of low pass filter
10 Hn_HighPass=sinc(n)-2*fC*sinc(2*fC*n); %impulse response of high pass filter
11 Hn_BandPass=(2*fH*sinc(2*fH*n))-(2*fL*sinc(2*fL*n)); %impulse response of Band
   Pass filter
12 Hn_BandStop=(2*fL*sinc(2*fL*n))-(2*fH*sinc(2*fH*n)); %impulse response of Band
   Stop filter
13
14 sgtitle('Impulse response of filters ') %main title for figure
15
16 subplot(2,2,1)
17 plot(n, Hn_LowPass);
18 grid on;
19 xlabel('n');
20 ylabel('H(n)');
21 title("Low Pass Filter");
22
23 subplot(2,2,3)
24 plot(n, Hn_HighPass);
25 grid on;
26 xlabel('n');
27 ylabel('H(n)');
28 title("High Pass Filter");
29
30 subplot(2,2,2)
31 plot(n, Hn_BandPass);
32 grid on;
33 xlabel('n');
34 ylabel('H(n)');
35 title("Band Pass Filter");
36
37 subplot(2,2,4)
38 plot(n, Hn_BandStop);
39 grid on;
40 xlabel('n');
41 ylabel('H(n)');
42 title("Band Stop Filter");
```

(b) Approach:

In question, we've been given rectangular function of Low Pass, High Pass, Band Pass and Band Stop filter,

which is **frequency response $H(w)$** of that filter so it's **Rectangular function below :**

f_C = cut-off frequency , f_L =lower band edge and f_H =upper band edge

$$H(w) = \text{rect}\left(\frac{w}{2w_C}\right)$$

$$H(f) = \text{rect}\left(\frac{f}{2f_C}\right)$$

$$\therefore H(f)=1 \quad , \text{for } -f_C \leq f \leq f_C$$

$$\text{so, } -w_C \leq w \leq w_C$$

Next, **impulse response $H(n)$** of that filter which is **Inverse Fourier Transform of frequency response $H(w)$:**

$$H(n) = \mathcal{F}^{-1}(H(f))$$

$$\therefore H(n) = \int_{-f_C}^{f_C} e^{j2\pi f n} df$$

Mentioned in question to adjust $H(n)$ into sinc function ,

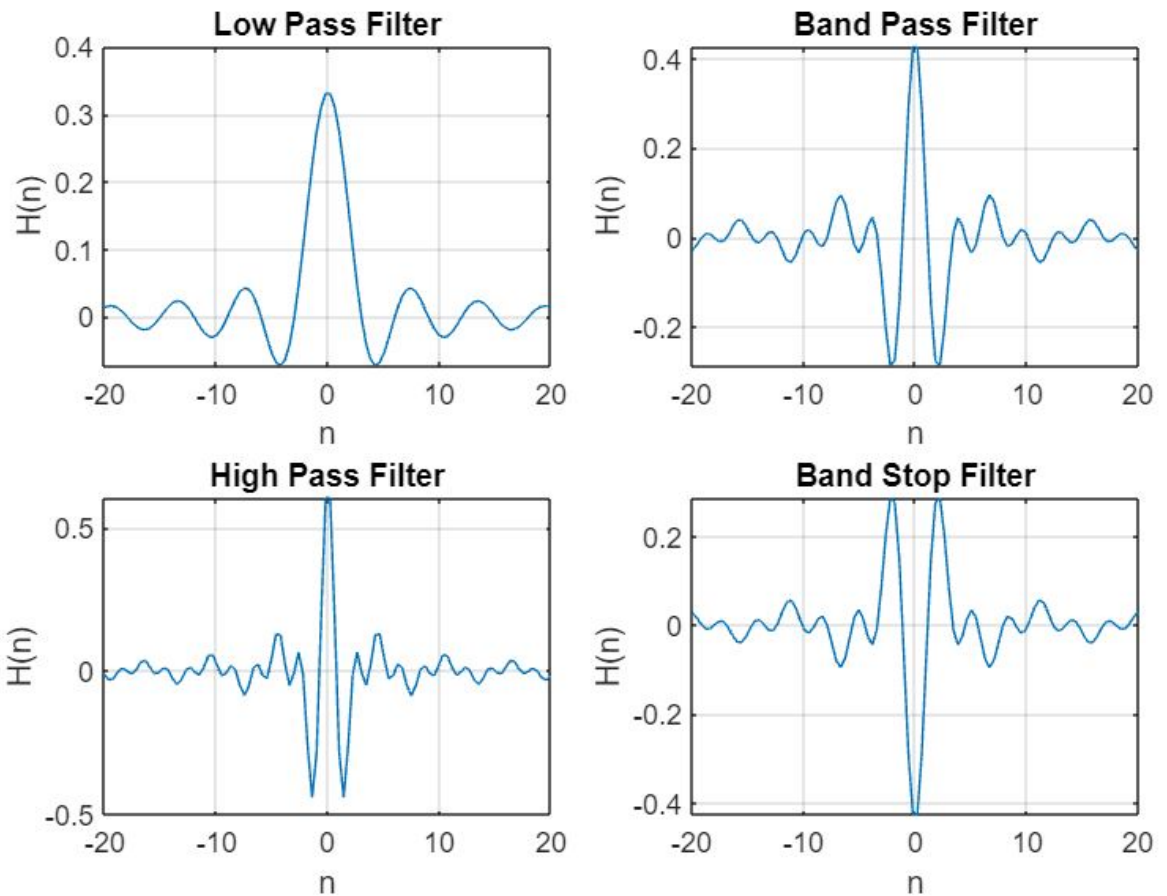
$$\therefore H(n) = \frac{e^{j2\pi f n}}{j2\pi n} \Big|_{-f_C}^{f_C} = \frac{1}{\pi n} \frac{e^{j2\pi f_C n} - e^{-j2\pi f_C n}}{2j} = \frac{1}{\pi n} \sin(2\pi f_C n) = 2f_C \text{sinc}(2f_C n)$$

Using this $H_{LP}(n) = 2f_C \text{sinc}(2f_C n)$ function plotted the graph for Low pass filter. Inverting impulse response or subtract from sinc function of low pass we get High Pass filter's impulse response, $H_{HP}(n) = \text{sinc}(n) - 2f_C \text{sinc}(2f_C n)$

Band Pass filter with lower band edge f_L and upper band edge f_H is just the difference of two such sinc filters if phase is zero, $H_{BP}(n) = 2f_H \text{sinc}(2f_H n) - 2f_L \text{sinc}(2f_L n)$. and Inverting impulse response of Band Pass filter it gives Band Stop filter's impulse response, $H_{BS}(n) = 2f_L \text{sinc}(2f_L n) - 2f_H \text{sinc}(2f_H n)$.

(c) Simulation Output:

Impluse response of filters



2. Solution Problem-2

(a) Matlab Script:

```

1  clc;
2  close all ;
3
4  fC=1/12; %cut-off frequency for filter
5  %if using fc1=1/20 for LP filter and fc2=1/8 for HP filter impulse response it
   gives same output because here i'm using common fc=1/12 which pass low freq in
   low pass filter(1/20) and passes high freq in high pass filter(1/8)
6
7  x_lower_index=input('Enter the lower index signal :');
8  x_upper_index=input('Enter the upper index signal :');
9  dn=0.01;
10 xn=x_lower_index:dn:x_upper_index; %time range of input signal
11
12 %initializing array as zeros
13 Hn_LowPass=zeros(1,length(xn));
14 Hn_HighPass=zeros(1,length(xn));
15 Xn=zeros(1,length(xn));
16
17 %assigning value of signal to array in interval
18 for i=1:length(xn)
19     Hn_LowPass(i)=2*fC*sinc(2*fC*xn(i)); %ideal low pass filter impulse
   response
20     Hn_HighPass(i)=sinc(xn(i))-2*fC*sinc(2*fC*xn(i)); %ideal high pass
   filter impulse response
21     Xn(i)=(10*cos(2*pi*xn(i)/20))+(5*cos(2*pi*xn(i)/8)); %sinusoidal input signal
22 end

```

```

23
24 y_lower_index=2*x_lower_index; %lower index of convolution as y
25 y_upper_index=2*x_upper_index; %upper index of convolution as y
26
27 subplot(3,1,1)
28 plot(xn,Xn,'linewidth' , 2); %x(n) input signal
29 hold on;
30 grid on;
31 title('x(n)=10*cos(2*pi*n/20)+5*cos(2*pi*n/8) signal');
32 xlabel('Time');
33 ylabel('Amplitude');
34 xticks(x_lower_index:1:x_upper_index);
35
36 %low pass Filter-----
37 m=[];
38 y=[];
39 yn=y_lower_index:dn:y_upper_index; %time range of convo output signal
40
41 %Matrix creation
42 %h_lowpass*x(i)
43 for i=1:length(Xn)
44     g=Hn_LowPass.*Xn(i);
45     m=[m;g];%this sequence store array at new row so one matrix will be formed
46 end
47 %summation of diagonal(right) elements an store it into one array
48 %11 12 13 14
49 %21 22 23 24
50 %31 32 33 34
51 %r=3,c=4,k=7,diagonal_index_sum=2(1+1 first element) because max we have sum=k
52 [r c]=size(m);
53 k=r+c;
54 diagonal_index_sum=2;
55 element=0;
56 %column and row wise searching for sum=diagonal_index_sum
57 while(diagonal_index_sum<=k)
58     for i=1:r
59         for j=1:c
60             if((i+j)==diagonal_index_sum)
61                 element=element+m(i,j);
62             end
63         end
64     end
65     diagonal_index_sum=diagonal_index_sum+1; %for next diagonal
66     y=[y element];
67     element=0;
68 end
69 disp(y);
70 subplot(3,1,2)
71 plot(yn,y, 'linewidth' , 2);
72 hold on;
73 grid on;
74 title('y(n)=x(n)*h(n) of low pass Filter');
75 xlabel('Time');
76 ylabel('Amplitude');
77 xticks(y_lower_index:1:y_upper_index);
78
79
80 %high pass Filter-----
81 m=[];
82 y=[];
83 yn=y_lower_index:dn:y_upper_index; %time range of convo output signal
84
85 %Matrix creation
86 %h_highpass*x(i)
87 for i=1:length(Xn)
88     g=Hn_HighPass.*Xn(i);
89     m=[m;g];%this sequence store array at new row so one matrix will be formed
90 end
91 %summation of diagonal(right) elements an store it into one array
92 %11 12 13 14

```

```

93 %21 22 23 24
94 %31 32 33 34
95 %r=3,c=4,k=7,diagonal_index_sum=2(1+1 first element) because max we have sum=k
96 [r c]=size(m);
97 k=r+c;
98 diagonal_index_sum=2;
99 element=0;
100 %column and row wise searching for sum=diagonal_index_sum
101 while(diagonal_index_sum<=k)
102     for i=1:r
103         for j=1:c
104             if((i+j)==diagonal_index_sum)
105                 element=element+m(i,j);
106             end
107         end
108     end
109     diagonal_index_sum=diagonal_index_sum+1;           %for next diagonal
110     y=[y element];
111     element=0;
112 end
113 disp(y);
114 subplot(3,1,3)
115 plot(yn,y, 'linewidth' , 2);
116 hold on;
117 grid on;
118 title('y(n)=x(n)*h(n) of high pass Filter');
119 xlabel('Time');
120 ylabel('Amplitude');
121 xticks(y_lower_index:1:y_upper_index);

```

(b) Approach:

-Using Ideal Low pass and band pass impulse response $H_{LP}(n) = 2f_C \text{sinc}(2f_C n)$ function plotted the graph for Low pass filter. Inverting impulse response of low pass we get High Pass filter's impulse response, $H_{HP}(n) = \text{sinc}(n) - 2f_C \text{sinc}(2f_C n)$
 -With cut-off frequency $= 1/12$ Taking input range from user as -n to n, computing signal using range of interval. Using this discrete signal first $H_{LowPass}(n)$ and $x(n)$, calculated length of convolution array and multiplying one by one element of $x(n)$ with whole array $h(n)$ and storing into one matrix m. Then, I did addition of right diagonal from first element ($m_{1 \times 1}$, where $diagonalIndexSum = 1 + 1 = 2$) to last element ($m_{r \times c}$). Sum of those element which satisfies diagonal index sum (2,3,4,...,r+c).
 -Same as above for $H_{HighPass}(n)$ and $x(n)$, After that plotted the value of y in appropriate range.

if using $fc_1 = 1/20$ for low pass filter and $fc_2 = 1/8$ for high pass filter impulse response it gives same output because here i'm using common $fc = 1/12$ which pass low freq in low pass filter(1/20) and passes high freq in high pass filter(1/8).

(c) Simulation Output:

