School of Engineering and Applied Science (SEAS) Ahmedabad University

BTech(ICT) Semester VI:Digital Signal Processing

Laboratory Assignment-8

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AIM:: LAB8 helps to understand the concept of butterworth filter Using **freq and butter**,**lp2bp** functions. In addition to this, I can use function for finding n,cutoffFreq,numerator and denominator coefficients and after that use of freqz function for plot magnitude and phase .

1. Solution Problem-1 By hand written calculation

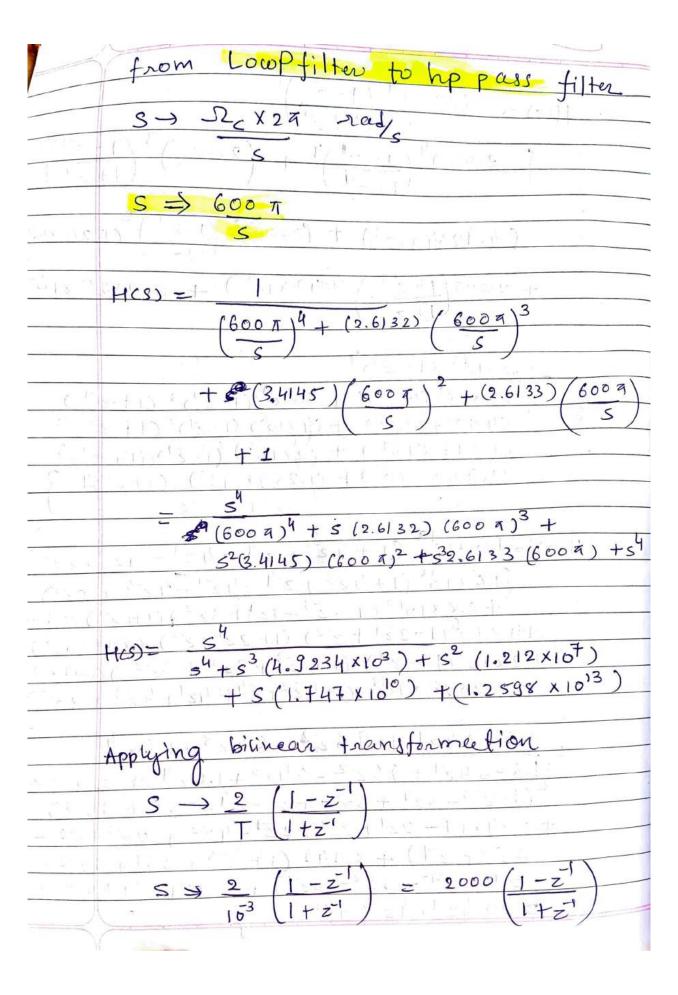
(a) Matlab Script:

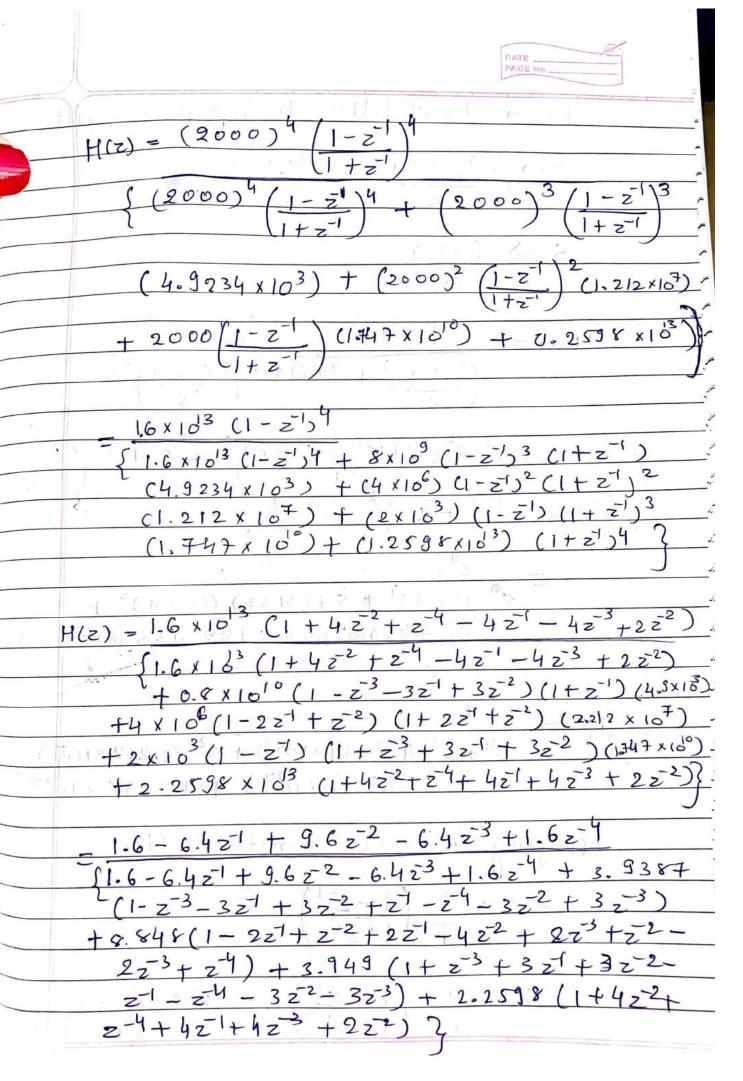
```
1 clc;
   2 close all ;
   4 %impz(b,a,n) with no output arguments plots the impulse response of the digital
                                filter with numerator coefficients b and denominator coefficients a.
   5 %b :: coefficients of numerator part as [...b4(Z^4) b3(Z^3) b1(Z^2) b1(Z^1) b0(Z^4) b1(Z^1) b1(Z^1)
                                 ^0) b(-1)(Z^{-1}) b(-2)(Z^{-2}) b(-3)(Z^{-3}) ...]
    _6 %a :: coefficients of denominator part as [...b4(Z^4) b3(Z^3) b1(Z^2) b1(Z^1) b0(Z^4) b1(Z^5) b1
                                   ^0) b(-1)(Z^{-1}) b(-2)(Z^{-2}) b(-3)(Z^{-3}) ...
   7 b = [0.1067 -0.4267 0.64 -0.4266 0.1067];
   8 a=[1 -0.1467 0.4931 -0.03112 0.018184];
 10 %freqz function : freqz(b,a,n,fs) without output argument,Display the magnitude
                                and phase responses of the filter.
11 %b :: numerator coefficients
 12 %a :: denominator coefficients
13 %(optional)n :: Number of evaluation points, specified as a positive integer
                                 scalar no less than 2. When n is absent, it defaults to 512. For best results,
                                    set n to a value greater than the filter order.
14 %fs :: sampling freq
15 fs=1000;
16 figure (1)
17 freqz(b,a,fs);
18 title('By hand Written')
```

(b) Approach:

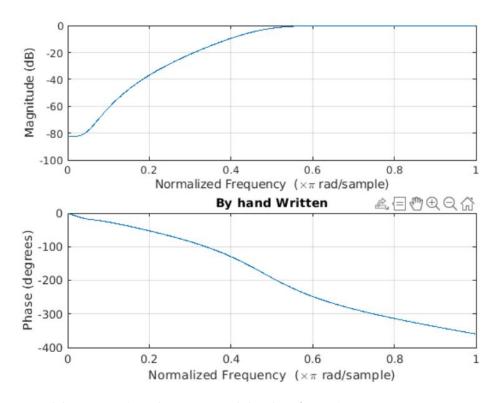
4th order Butterworth highpass filter hewing cut-off freq 300 Hz & Iller Using Bilinear transformer tion $72_{c} = 1 \text{ radys}$ $4s = 1 \text{ KHz} \implies T = 1 \text{ mS}$ Poles at, Sk = Reeilek+N+1) 7/2N 0000 N = 41, k = 0.1.2.3) + (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (5.1.2.1) (= cos(sa/8) + jsin(sa/8) 1+11 6011 31 $S_0 = -0.3827 + j \cdot 0.5239$ $S_1 = e^{j(2+4+1)} \frac{7}{8}$ $S_1 = e^{j(748)} \frac{1}{12} \frac{1}{12$ $S_2 = e^{j(4+h+1)}98$ $= e^{j(998)}$ =-0.9239-j0.3827S3 = e j (6+4+1) 7/8 = e j 117/4 - - 0.3827 - j. 0.9239 Now H(s) = (52) N-1 (S-SK)

```
ACS) = 1/[S+0.3827-j0.9239][S+0.9239-j0.3827]
          [s+0.9239+j0.3827][s+0.3827+j0.9239]
          (S+0.3827)2+(0.9239)2][(S+0.9239)2
                     + (0.3827)
           [52+25(0.3827)+(0.3827)2+(0.9239)27
            52+25(0.9239) + (0.923902 + CO.3827)2
         54 + 253(0.9239) + 52 (0.9239)2 +3(0.3827)28
       + 253 (0.3827) + 452 (0.9239) (0.3827) +
          23 (0.3824) (0.9234)2 + 25 (0.3824)3
       + 52 (0.38 27)2 + 25 (0.9239) (0.3827)2+
           (0.923902 do.3827)2+ 10.3 127 )4
       + 52 (0.9239)2 + 25 (0.9239)3 + (0.9239)9
             + (0.3827)2 (0.9239)2
                                   JU1- 18019 1
       54 + 53 [1.8478+0.7654] + 52 [0.8536+0.1465
         +1.4143 +0.1465 +0.85367 + S[0.6533 +0.1121
        + 0.2706+1,57737+ [0.125+0.0215+
         0.7286 + 0.1257
      H(8) =
              s4+s3 [2.61327+52 [3.41457+8 [2.61337
```





 $= 1.6 - 6.4 z^{-1} + 9.6 z^{-2} - 6.4 z^{-3} + 1.6 z^{-4}$ $15.042 - 2.2067 z^{-1} + 7.41736 z^{-2}$ $- 0.46811 z^{-3} + 0.2735 z^{-4}$ Normalized by 15.042, $0.1067 - 0.4267 z^{-1} + 0.64 z^{-2} = 0.4266 z^{-3}$ $1 - 0.1467 z^{-1} + 0.49311 z^{-2} - 0.03112z^{-3}$ $+ 0.018184z^{-4}$ b = [0.1067 - 0.4267 0.64 - 0.4266 0.1067] q = [1 - 0.1467 0.4931 - 0.03112 0.018184]



2. Solution Problem-1 using butter and lp2hp function

(a) Matlab Script:

```
1 clc;
  2 close all;
  3 clear ;
   4 % Bilinear transformation using fucntions
  5 %high cutoff frequency fc = 300Hz so wc =2*pi*fc => 600*pi and sampling f=1000
  _{6} N=4;% order N = 4
  7 fc=300;
  8 wc=2*pi*fc;
  9 [b,a] = butter (N, 1,"low", 's');
10 % converting from LP filter to HP filter
_{11} % We get high pass analog filter transfer function coefficients bt and at
12 [bt, at] = lp2hp (b, a, wc);
13 fs=10<sup>3</sup>;
14 [bz, az] = bilinear (bt, at, fs);
       %b :: coefficients of numerator part as [...b4(Z^4) b3(Z^3) b1(Z^2) b1(Z^1) b0(Z
                        ^0) b(-1)(Z^-1) b(-2)(Z^-2) b(-3)(Z^-3) ..]
 % a :: coefficients of denominator part as [...b4(Z^4) b3(Z^3) b1(Z^2) b1(Z^1) b0(Z^4) b1(Z^4) b1(Z^5) b1(Z^5
                        ^0) b(-1)(Z^{-1}) b(-2)(Z^{-2}) b(-3)(Z^{-3}) ...
 17 % Plot the zeros and poles
18 figure (1)
19 freqz(bz,az)
20 figure (2)
zplane (bz,az);
```

(b) Approach:

With order 4 ,sampling time =0.001, High pass cutoof frq 300Hz. Using this as arguments in butter function to find transfer function coefficients to lowpass in S domain. Passing this coefficients to lp2bp to get high pass filter's coefficients function ,Passing output of this in bilinear transformation function bilinear to get Z-domain's

coefficients. At the end plotted into freqz and zero and poles.

