

**School of Engineering and Applied Science (SEAS)
Ahmedabad University**

BTech(ICT) Semester VI:Digital Signal Processing

Laboratory Assignment-6

Enrollment No:AU1841131

Name:Mansi Dobariya

AIM :: LAB6 helps to understand the concept of signal and systems. Solving the properties of signal like Z-transform of $X(n)$ and $H(n)$, Inverse Z-transform and plotting Zeros and Poles in plane Using **ztrans,iztrans,zplane,impz** and **syms** functions.

1. Solution Problem-1

(a) Matlab Script:

```
1 clear all;
2 clc;
3 syms n Z; %symbolic variable
4 X1=1;
5 %inbuilt unitStep function in matlab is heaviside(n) + 0.5*delta(n) => 1 here
6 ans1=ztrans(X1,Z); %Ztransform of X1 with transfer variable Z
.
7 display(ans1)
8
9 X2=n;
10 %inbuilt unitStep function in matlab is heaviside(n) + 0.5*delta(n) => 1 here
11 ans2=ztrans(X2,Z); %Ztransform of X2 with transfer variable Z.
12 display(ans2)
13
14 X3=(1+n);
15 %inbuilt unitStep function in matlab is heaviside(n) + 0.5*delta(n) => 1 here
16 ans3=ztrans(X3,Z); %Ztransform of X3 with transfer variable Z.
17 display(ans3)
18
19 syms w; %symbolic variable
20 X4=cos(w.*n);
21 %inbuilt unitStep function in matlab is heaviside(n) + 0.5*delta(n) => 1 here
22 ans4=ztrans(X4,Z); %Ztransform of X4 with transfer variable Z.
23 display(ans4);
24
25 X5=sin(w.*n);
26 %inbuilt unitStep function in matlab is heaviside(n) + 0.5*delta(n) => 1 here
27 ans5=ztrans(X5,Z); %Ztransform of X5 with transfer variable Z.
28 display(ans5);
29
30 syms a; %symbolic variable
31 X6=(a^n).*cos(w.*n);
32 %inbuilt unitStep function in matlab is heaviside(n) + 0.5*delta(n) => 1 here
33 ans6=ztrans(X6,Z); %Ztransform of X6 with transfer variable Z.
34 display(ans6);
35
36 X7=(a^n).*sin(w.*n);
37 %inbuilt unitStep function in matlab is heaviside(n) + 0.5*delta(n) => 1 here
38 ans7=ztrans(X7,Z); %Ztransform of X7 with transfer variable Z.
39 display(ans7);
```

```

40
41 X8=n.*(a^n);
42 %inbuilt unitStep function in matlab is heaviside(n) + 0.5*delta(n) => 1 here
43 ans8=ztrans(X8,Z); %Ztransform of X8 with transfer variable
44 Z.
45 display(ans8);
46
47 X9=-n.*(a^n);
48 %inbuilt unitStep function in matlab is heaviside(n) + 0.5*delta(n) => 1 here
49 ans9=ztrans(X9,Z); %Ztransform of X9 with transfer variable
50 Z.
51 display(ans9);
52
53 X10=n.*((-1)^n);
54 %inbuilt unitStep function in matlab is heaviside(n) + 0.5*delta(n) => 1 here
55 ans10=ztrans(X10,Z); %Ztransform of X10 with transfer
56 variable Z.
57 display(ans10);
58
59 X11=(n^2);
60 %inbuilt unitStep function in matlab is heaviside(n) + 0.5*delta(n) => 1 here
61 ans11=ztrans(X11,Z); %Ztransform of X11 with transfer
62 variable Z.
63 display(ans11);

```

(b) Approach:

`syms` function creates dynamic symbolic variables. Using `syms` function I created `n,Z,w` and `a` as variables.then assigning signal to variables and did Z-transform with the help of `ztrans(f,transformationVar)` ,here transformationVar is `Z`. Display transfer funation in command window.

Command Window

ans1 =

$$z/(z - 1)$$

ans2 =

$$z/(z - 1)^2$$

ans3 =

$$z/(z - 1) + z/(z - 1)^2$$

ans4 =

$$(Z*(Z - \cos(w)))/(Z^2 - 2*\cos(w)*Z + 1)$$

ans5 =

$$(Z*\sin(w))/(Z^2 - 2*\cos(w)*Z + 1)$$

ans6 =

$$-(Z*(\cos(w) - Z/a))/(a*(Z^2/a^2 - (2*Z*\cos(w))/a + 1))$$

ans7 =

$$(Z*\sin(w))/(a*(Z^2/a^2 - (2*Z*\cos(w))/a + 1))$$

ans8 =

$$(Z*a)/(Z - a)^2$$

ans9 =

$$-(Z*a)/(Z - a)^2$$

ans10 =

$$-Z/(Z + 1)^2$$

ans11 =

$$(Z*(Z + 1))/(Z - 1)^3$$

2. Solution Problem-2

(a) Matlab Script:

```
1 clear all;
2 clc;
3
4 z=[0;1/12];
    Zero
5 p=[1/2;-1/3];
    Infinity
6 figure(1);
7 zplane(z,p);
    %plotting Zeros,Poles using zplane()
8 title('Zeros and Poles of X(n)=(1/2)^nu(n) + (-1/3)^nu(n)');
9
10 z=[0];
    %Zeros values where transfer function becomes
        Zero
11 p=[1/2;-1/3];
    Infinity
12 figure(2);
13 zplane(z,p);
    %plotting Zeros,Poles using zplane()
14 title('Zeros and Poles of X(n)=(-1/3)^nu(n) - (1/2)^nu(-n-1)');
15
16 z=[inf];
    Zero
17 p=[1/2];
    Infinity
18 figure(3);
19 zplane(z,p);
    %plotting Zeros,Poles using zplane()
20 title('Zeros and Poles of X(n)=(1/2)^nu(-n)')
21
22 z=[0];
    %Zeros values where transfer function becomes
        Zero
23 p=[1;-1];
    Infinity
24 figure(4);
25 zplane(z,p);
    %plotting Zeros,Poles using zplane()
26 title('Zeros and Poles of X(n)=\{-1,0,-1,0,-1,0,-1,0,...\}')
27
```

(b) Approach:

Answer-2

a)

$$x(n) = \left(\frac{1}{2}\right)^n u(n) + \left(-\frac{1}{3}\right)^n u(n)$$

$$X(z) = \sum_{n=-\infty}^{\infty} x(n) z^{-n}$$

$$= \sum_{n=-\infty}^{\infty} \left[\left(\frac{1}{2}\right)^n u(n) + \left(-\frac{1}{3}\right)^n u(n) \right] z^{-n}$$

$$= \sum_{n=0}^{\infty} \left(\frac{1}{2}\right)^n z^{-n} + \left(-\frac{1}{3}\right)^n z^{-n}$$

$$= \frac{1}{1 - \frac{1}{z}} + \frac{1}{1 + \frac{1}{3z}}$$

$$X(z) = \frac{2z}{2z-1} + \frac{3z}{3z+1}$$

$$z(12z-1)$$

$$(z - \frac{1}{2})(z + \frac{1}{3})$$

$$z > \frac{1}{2} \quad z > -\frac{1}{3}$$

$$\text{ROC} \Rightarrow \boxed{z > \frac{1}{2}}$$

Poles at $\boxed{p = [-\frac{1}{3}, \frac{1}{2}]}$
 Zeros at $\boxed{z = [0, \frac{1}{12}]}$

$$b) (-k_3)^n u(n) - (k_2)^n u(-n-1)$$

$$X(z) = \sum_{n=-\infty}^{\infty} x(n) z^{-n}$$

$$= \sum_{n=-\infty}^{\infty} [(-k_3)^n u(n) - (k_2)^n u(-n-1)] z^{-n}$$

$$= \sum_{n=0}^{\infty} (-k_3)^n z^{-n} - \sum_{n=-\infty}^{-1} (k_2)^n z^{-n}$$

$$= \sum_{n=0}^{\infty} (-k_3)^n z^{-n} - \left[-1 + \sum_{n=0}^{\infty} \left(\frac{1}{2}\right)^{-n} z^{+n} \right]$$

$$= \frac{1}{1 + \frac{z^{-1}}{3}} + 1 - \frac{1}{1 - \frac{z^{+1}}{2^{-1}}}$$

$$= \frac{3z}{3z+1} + 1 - \frac{1}{-1+2z}$$

$$z > -\frac{1}{3} \quad \text{(crossed out)} \quad z > \frac{1}{2}$$

$$\boxed{\text{ROC: } z > \frac{1}{2}} \quad \boxed{\therefore -\frac{1}{3} < z < \frac{1}{2}} \quad \boxed{z > \frac{1}{2}}$$

poles cut, $p = [k_2, -k_3]$

zeros cut, $z^2 = 0$

radius would be +

$$(c) x(n) = \left(\frac{1}{2}\right)^n u(n)$$

$$X(z) = \sum_{n=-\infty}^{\infty} \left(\frac{1}{2}\right)^n u(n) z^{-n} = \sum_{n=-\infty}^{0} \left(\frac{1}{2}\right)^n z^{-n}$$

$$= \sum_{n=0}^{\infty} \left(\frac{1}{2}\right)^{-n} z^n$$

$$X(z) = \frac{1}{1 - \frac{1}{2}z}$$

$$z < \frac{1}{2}$$

$$\text{ROC: } z < \frac{1}{2}$$

poles at, $p = [\frac{1}{2}]$
 zeros at, $z = [0] [\infty]$

$$(d) x(n) = \{-1, 0, -1, 0, -1, 0, \dots\}$$

$$X(z) = \sum_{n=0}^{\infty} x(n) z^{-n}$$

$$= (-1)z^0 + (0)z^{-1} + (-1)z^{-2} + (0)z^{-3} + \dots$$

$$= -1 - \frac{1}{z^2} - \frac{1}{z^4} - \frac{1}{z^6} - \dots$$

$$X(z) = \frac{1}{1 - \frac{1}{z^2}} = \frac{z^2}{z^2 - 1} \in \left(\frac{1}{|z|}\right)$$

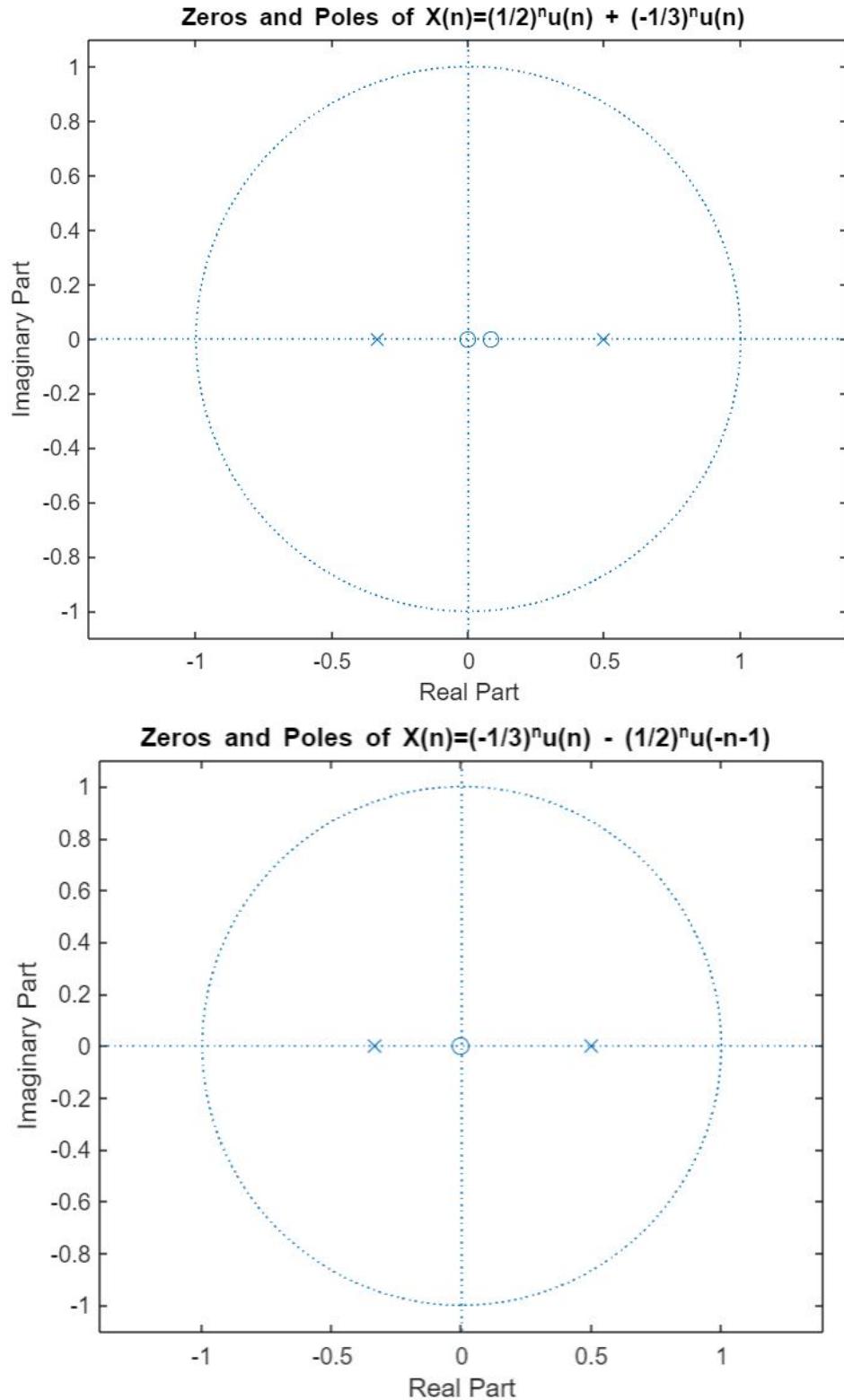
poles at, $p = [+1, -1]$
 zeros at, $z = 0$

$$\text{ROC: } -1 < z < 1$$

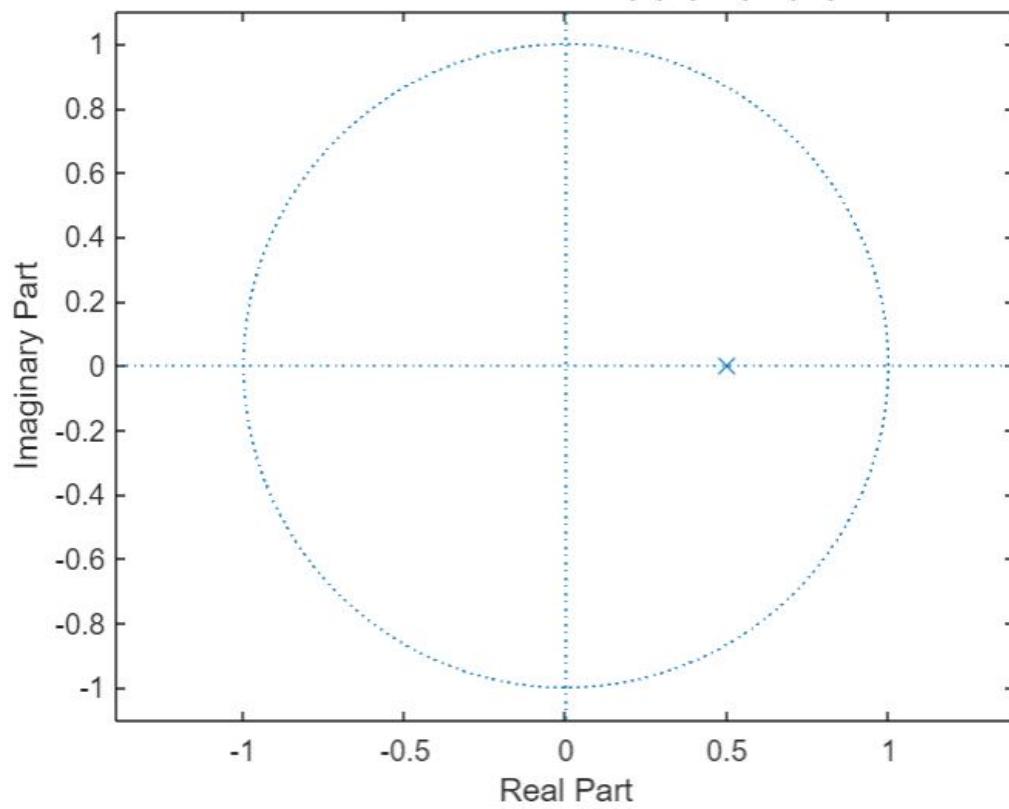
but +ve radius
 ROC $[0 < z < 1]$

I have calculated $X(z)$ on paper and checking where are zeros and poles. After assigning those values to appropriate array \mathbf{z}, \mathbf{p} pass that array to $\text{zplane}(\mathbf{z}, \mathbf{p})$ function which is plot Z and P into plane.

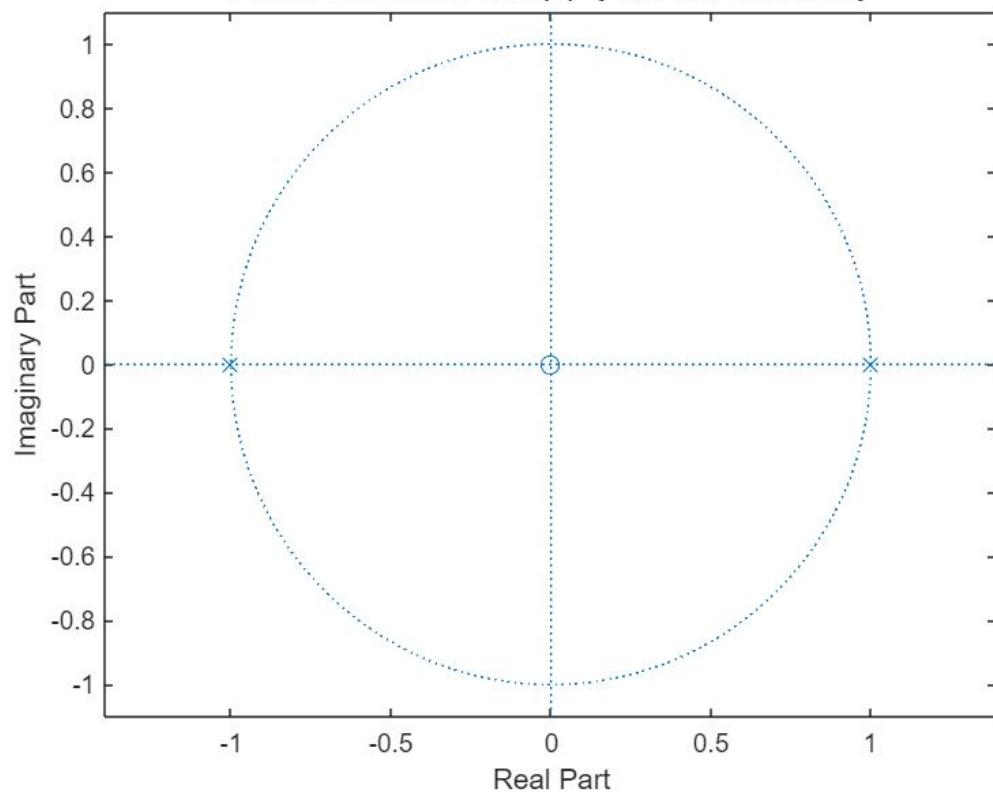
(c) Simulation Output:



Zeros and Poles of $X(n)=(1/2)^n u(-n)$



Zeros and Poles of $X(n)=\{-1,0,-1,0,-1,0,-1,0,\dots\}$



3. Solution Problem-3

(a) Matlab Script:

```
1 clear all;
2 clc;
3 syms n Z;                                     %symbolic variable
4 X1=(1+(3*Z^(-1)) )./(1-(3*Z^(-1)) +(2*Z^(-2)) );
5 ans1=iztrans(X1,n);                           %Inverse Ztransform of X1(z) with transfer
6 variable n
7 display(ans1)
8
9 X2=(1+(2*Z^(-1)) )./(1+(1*Z^(-2)) );
10 ans2=iztrans(X2,n);                          %Inverse Ztransform of X2(z) with transfer
11 variable n
12 display(ans2)
13
14 X3=1./((1 - Z^(-1))^2 * (1 - (2*Z^(-1)) ) );
15 ans3=iztrans(X3,n);                          %Inverse Ztransform of X3(z) with transfer
16 variable n
17 display(ans3)
```

(b) Approach:

Answer-3

$$a) \quad X(z) = \frac{1 + 3z^{-1}}{1 - 3z^{-1} + 2z^{-2}}$$

$$= \frac{(z+3)}{z} \cdot \frac{1}{\frac{z^2 - 3z + 2}{z^2}}$$

$$= \frac{z(z+3)}{z^2 - 3z + 2}$$

$$= \frac{z(z+3)}{(z-2)(z-1)}$$

$$\frac{X(z)}{z} = \frac{z+3}{(z-2)(z-1)}$$

$$z+3 = (z-2)B + A(z-1)$$

$$= \frac{A}{(z-2)} + \frac{B}{(z-1)}$$

$$\begin{aligned} z+3 &= Az - A + Bz \\ z+3 &= z(A+B) - (A+2B) \end{aligned}$$

$$= \frac{5}{(z-2)} + \frac{(-4)}{(z-1)}$$

$$\begin{array}{r} A+B=1 \\ A+2B=-3 \\ \hline -B=4 \end{array}$$

$$\boxed{B = -4}$$

$$F(z) = \frac{5z}{(z-2)} + \frac{(-4)z}{(z-1)}$$

$$= \frac{5}{1 - \frac{2}{z}} - \frac{4}{1 - \frac{1}{z}}$$

$$\boxed{h(n) = 5 \cdot 2^n - 4 \cdot 4^n}$$

$$b) X(z) = \frac{(1 + 2z^{-1})}{(1 + z^{-2})}$$

$$= \frac{(1 + \frac{2}{z})}{(1 + \frac{1}{z^2})}$$

$$= \frac{z(z+2)}{(z^2+1)}$$

$$\frac{X(z)}{z} = \frac{(z+2)}{(z^2+1)}$$

$$\left\{ \begin{array}{l} z^2+1 = (z+j)(z-j) \\ = z^2 + z^2 - zj - (-1) \\ = z^2 + 1 \end{array} \right.$$

$$= \frac{A}{(z+j)} + \frac{B}{(z-j)}$$

$$\left\{ \begin{array}{l} z+2 \\ = A(z-j) + B(z+j) \\ = z(A+B) + 1(Aj+Bj) \end{array} \right.$$

$$= \frac{\left(\frac{-2+j}{2j}\right)}{z+j} + \frac{\left(\frac{j+2}{2j}\right)}{z-j}$$

$$\left\{ \begin{array}{l} A+B = 1 \\ \cancel{Aj+Bj=2} \end{array} \right.$$

$$\left\{ \begin{array}{l} A-B = -\frac{2}{j} \\ - + +j \end{array} \right.$$

$$= \left(\frac{-2+j}{2j}\right)(z+j)^{-1} + \left(\frac{j+2}{2j}\right)(z-j)^{-1}$$

$$\left\{ \begin{array}{l} 2B = 1 + \frac{2}{j} \\ B = \frac{j+2}{2j} \end{array} \right.$$

$$X(z) = \left(\frac{-2+j}{2j}\right) \frac{(z)}{(z+j)} + \left(\frac{j+2}{2j}\right) \frac{(z)}{(z-j)}$$

$$x(n) = \left(\frac{-2+j}{2j}\right) (-j)^n + \left(\frac{j+2}{2j}\right) (j)^n$$

$$x(n) = (-j)^{n-1} \left(1 - j\right)_2 + (j)^{n-1} \left(1 + j\right)_2$$

$$c) x(z) = \frac{1}{(1 - z^{-1})^2 (1 - 2z^{-1})}$$

$$x(z) = \frac{z^3}{(z-1)^2 (z-2)}$$

$$\frac{x(z)}{z} = \frac{z^2}{(z-1)^2 (z-2)}$$

$$= \frac{A}{(z-1)} + \frac{B}{(z-1)^2} + \frac{C}{(z-2)}$$

$$z^2 = A(z-1)(z-2) + B(z-2) + C(z-1)^2$$

$$1 = -B$$

$$4 = C$$

$$0 = 2A - 2B + C \\ = 2A + 2 + 4$$

$$-6 = 2A$$

$$A = -3$$

$$\frac{x(z)}{z} = \frac{-3}{(z-1)} + \frac{-1}{(z-1)^2} + \frac{4}{(z-2)}$$

$$x(z) = \frac{-3z}{(z-1)} + \frac{-z}{(z-1)^2} + \frac{4z}{(z-2)}$$

$$= \frac{-3}{(1-z^{-1})} - \frac{z^{-1}}{(1-z^{-1})^2} + \frac{4}{(1-\frac{2}{z})}$$

$$x(n) = -3u(n) - nu(n) + 4z^n u(n)$$

syms function creates dynamic symbolic variables. Using **syms** function I created n and Z as variables.then assigning signal to variables and did Inverse Z-transform with the help of **iztrans(f,transformationVar)** ,here transformationVar is n. Display transfer funation in command window.

(c) Simulation Output:

```

COMMAND WINDOW

ans1 =
5*2^n - 4

ans2 =
(-1i)^(n - 1)*(1 - 1i/2) + 1i^(n - 1)*(1 + 1i/2)

ans3 =
4*2^n - n - 3

```

4. Solution Problem-4

(a) Matlab Script:

```

1 close all;
2 clear all;
3 clc;
4
5 z=[0]; %Zeros values where transfer function
         becomes Zero
6 p=[1/2;1/4]; %Poles values where transfer function
                 becomes Infinity
7 figure(1); %plotting Zeros,Poles using zplane()
8 zplane(z,p);
9 title('Zeros and Poles of H(Z)= Z^{2}/(Z-0.25)(Z-0.5) ');
10
11 z=[0]; %Zeros values where transfer function
          becomes Zero
12 p=[1]; %Poles values where transfer function
          becomes Infinty
13 figure(2); %plotting Zeros,Poles using zplane()
14 zplane(z,p);
15 title('Zeros and Poles of H(Z)= Z/(Z-1) ');
16
17 z=[-1/sqrt(2);1/sqrt(2)]; %Zeros values where transfer function
                           becomes Zero
18 p=[1/2;1/5]; %Poles values where transfer function
                  becomes Infinity
19 figure(3); %plotting Zeros,Poles using zplane()
20 zplane(z,p);
21 title('Zeros and Poles of H(Z)= (2Z^{2}-1)/(Z-0.5)(Z-0.2) ');
22

```

```

23 %b :: coefficients of nominator part as [...b4(Z^4) b3(Z^3) b1(Z^2) b1(Z^1) b0(Z
24 ^0) b(-1)(Z^-1) b(-2)(Z^-2) b(-3)(Z^-3) ...]
25 %a :: coefficients of denominator part as [...b4(Z^4) b3(Z^3) b1(Z^2) b1(Z^1) b0(Z
26 ^0) b(-1)(Z^-1) b(-2)(Z^-2) b(-3)(Z^-3) ...]
27 b=[1];
28 a=[1 -0.75 0.125];
29 figure(4);
30 impz(b,a,16);
31 %impz is a impulse response of H(z) by b and a coefficient factors and n=16 are
32 title('Impulse Response of H(Z)= 1/( 1-0.75Z^{-1}+0.125Z^{-2} ) ');
33
34 b=[1];
35 a=[1 -1];
36 figure(5);
37 impz(b,a,16);
38 %impz is a impulse response of H(z) by b and a coefficient factors and n=16 are
39 title('Impulse Response of H(Z)= 1/( 1-Z^{-1} ) ');
40
41 b=[2 0 -1];
42 a=[1 -0.7 0.1];
43 figure(6);
44 impz(b,a,16);
45 %impz is a impulse response of H(z) by b and a coefficient factors and n=16 are
46 title('Impulse Response of H(Z)= (2-1Z^{-2})/( 1-0.7Z^{-1}+0.1Z^{-2} ) ');

```

(b) Approach:

Answer-4

$$a) Y(n) = 0.75y(n-1) - 0.125y(n-2) + x(n)$$

$$H(n) = \frac{0.75y(n-1)}{x(n)} - \frac{0.125y(n-2)}{x(n)} + 1$$

→ H(n) would be $\frac{Y(n)}{X(n)}$

and H(z) would be $\frac{Y(z)}{X(z)}$

z-transform property,

$$x(n) \rightarrow X(z)$$

$$x(n-1) \rightarrow z^{-1}X(z)$$

$$\text{so, } Y(z) = 0.75 z^{-1}Y(z) - 0.125 z^{-2}Y(z) + X(z)$$

$$H(z) = \frac{0.75 z^{-1} Y(z)}{X(z)} - \frac{0.125 z^{-2} Y(z)}{X(z)} + 1$$

$$\therefore H(z) = 0.75 z^{-1} H(z) - 0.125 z^{-2} H(z) + 1$$

$$\therefore 1 = 0.125 z^{-2} H(z) - 0.75 z^{-1} H(z) + H(z)$$

$$\therefore 1 = H(z) [1 - 0.75 z^{-1} + 0.125 z^{-2}]$$

$$H(z) = \frac{1}{1 - 0.75z^{-1} + 0.125z^{-2}}$$

--- ①

more expanded for zero and pole values,

$$H(z) = \frac{z^2}{z^2 - 0.75z + 0.125}$$

$$f(z) = \frac{z^2}{(z - 0.25)(z - 0.5)}$$

- ② ROC = ~~0.25 < z < 0.5~~

$$z > 0.25$$

$$z > 0.5$$

ROC, $\{z > 0.5\}$

$$\text{poles} = [0.25, 0.5]$$

$$\text{zeros} = [0]$$

Coefficients for Impulse response
from eq. 1

$$b = [1]$$

\Rightarrow nominator coeff.

$$a = [1 \ -0.75 \ 0.125]$$

\Rightarrow denominator coeff

array value would be form of

[--- (coefficient of z^2) , (coefficient of z) ,

(coefficient of z^0) , (coefficient of z^{-1}) ,

(coefficient of (z^{-2}) , ---)

$$h(z) = \frac{z^2}{(z - 0.25)(z - 0.5)}$$

$$\frac{h(z)}{z} = \frac{z}{(z - \frac{1}{4})(z - \frac{1}{2})}$$

$$= \frac{A}{(z - \frac{1}{4})} + \frac{B}{(z - \frac{1}{2})}$$

$$z = A(z - \frac{1}{2}) + B(z - \frac{1}{4})$$

$$\frac{1}{4} = A(-\frac{1}{4}) \quad \mid \quad \frac{1}{2} = B(\frac{1}{4})$$

$$\boxed{-\frac{1}{4} = A}$$

$$\boxed{B = 2}$$

$$\frac{h(z)}{z} = \frac{-\frac{1}{4}}{(z - \frac{1}{4})} + \frac{2}{(z - \frac{1}{2})}$$

$$h(z) = -\frac{z}{(z - \frac{1}{4})} + \frac{2z}{(z - \frac{1}{2})}$$

$$h(z) = -\frac{1}{(1 - \frac{1}{4}z)} + \frac{2}{(1 - \frac{1}{2}z)}$$

$$\boxed{h(z) = -\left(\frac{1}{4}\right)^n 4(z) + 2\left(\frac{1}{2}\right)^n 4(z)}$$

$$b) Y(n) = Y(n-1) + x(n)$$

$$H(n) = \frac{Y(n)}{X(n)} \Rightarrow \frac{Y(n-1)}{X(n)} + 1$$

$$H(z) = z^{-1} \frac{Y(z)}{X(z)} + 1$$

$$H(z) = z^{-1} H(z) + 1$$

$$\therefore H(z) [1 - z^{-1}] = 1$$

$$H(z) = \frac{1}{1 - z^{-1}}$$

- eq ①

$$z$$

$$H(z) = \frac{z}{z-1}$$

- eq ②

$$\boxed{\text{ROC: } z > 1}$$

poles at, $p = [1]$

zeros at, $z = [0]$

$$b = [1]$$

$$a = [1 \ -1]$$

b)

$$H(z) = \frac{z}{(z^2 - 3)^{z-1}}$$

$$f(z) = \frac{1}{1 - z^{-1}}$$

~~200~~

$$h(n) = u(n)$$

$$c) 0.7(y[n-1]) - 0.1y[n-2] + 2x[n] - x[n-2]$$

$$H(z) = \frac{Y(z)}{X(z)} = \frac{0.7z^{-1} - 0.1z^{-2}}{1 + 2z^{-1} - z^{-2}}$$

$$+ 2 \frac{x[n]}{x[n]} - \frac{x[n-2]}{x[n]}$$

$$H(z) = 0.7z^{-1} H(z) - 0.1z^{-2} H(z) + 2 - z^{-2}$$

$$2 - z^{-2} = H(z) [1 - 0.7z^{-1} + 0.1z^{-2}]$$

$$H(z) = \frac{2 - z^{-2}}{1 - 0.7z^{-1} + 0.1z^{-2}}$$

--- eq ①

$$\therefore H(z) = \frac{2z^2 - 1}{(z - 0.5)(z - 0.2)}$$

--- eq ②

$$\text{poles at } p = [\frac{1}{5}, \frac{1}{2}]$$

$$\text{zeros at } z = [+\frac{1}{\sqrt{2}}, -\frac{1}{\sqrt{2}}]$$

$$b = [2 \ 0 \ -1]$$

$$a = [1 \ -0.7 \ +0.1]$$

$$\text{ROC: } z > 0.5 \quad \& \quad z > 0.2$$

$$\text{so } z > 0.5$$

c) $H(z) = \frac{2z^2 - 1}{(z - \frac{1}{2})(z - \frac{1}{5})}$

$$\frac{H(z)}{z} = \frac{2z - z^{-1}}{(z - \frac{1}{2})(z - \frac{1}{5})}$$

$$= \frac{A}{(z - \frac{1}{5})} + \frac{B}{(z - \frac{1}{2})}$$

$$2z - z^{-1} = A(z - \frac{1}{2}) + B(z - \frac{1}{5})$$

$$\frac{2}{5} - 5 = A \left(\frac{1}{5} - \frac{1}{2} \right)$$

$$-\frac{23}{5} = A \left(-\frac{3}{10} \right)$$

$$A = \frac{46}{3}$$

$$\frac{2}{2} - 2 = B \left(\frac{1}{2} - \frac{1}{5} \right)$$

$$-1 = B \left(\frac{3}{10} \right)$$

$$B = -\frac{10}{3}$$

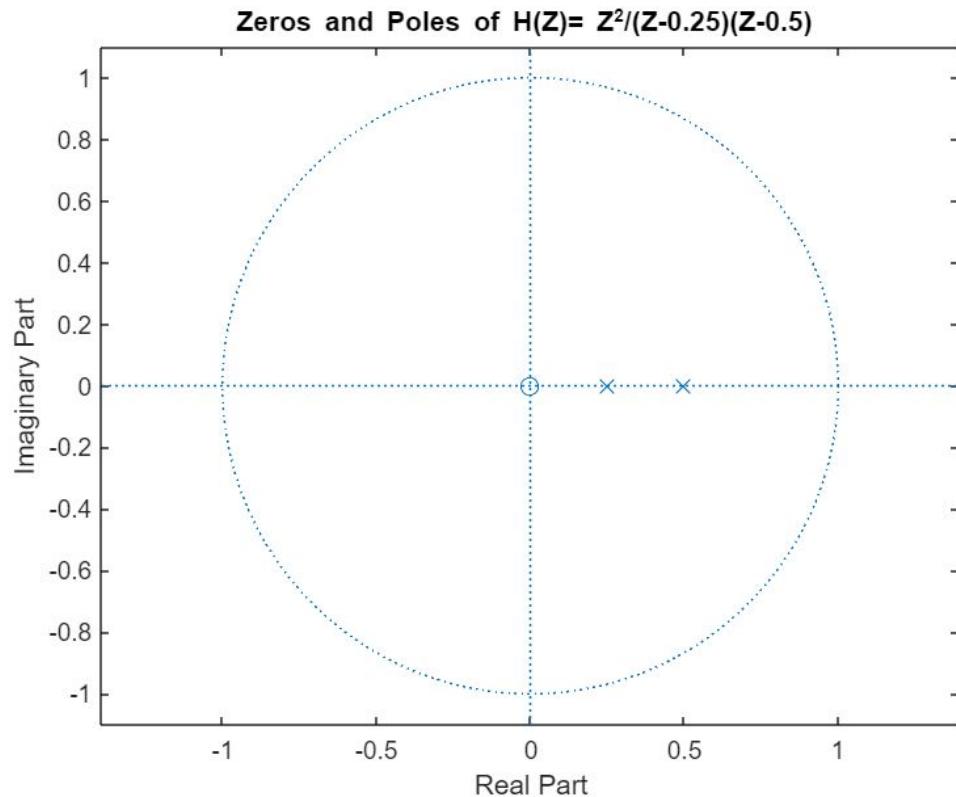
$$\frac{h(z)}{z} = \frac{46}{3} \frac{1}{(z - 1/5)} + \left(-\frac{10}{3} \right) \frac{1}{(z - 1/2)}$$

$$h(z) = \left(\frac{46}{3} \right) \frac{z}{(z - 1/5)} + \left(-\frac{10}{3} \right) \frac{z}{(z - 1/2)}$$

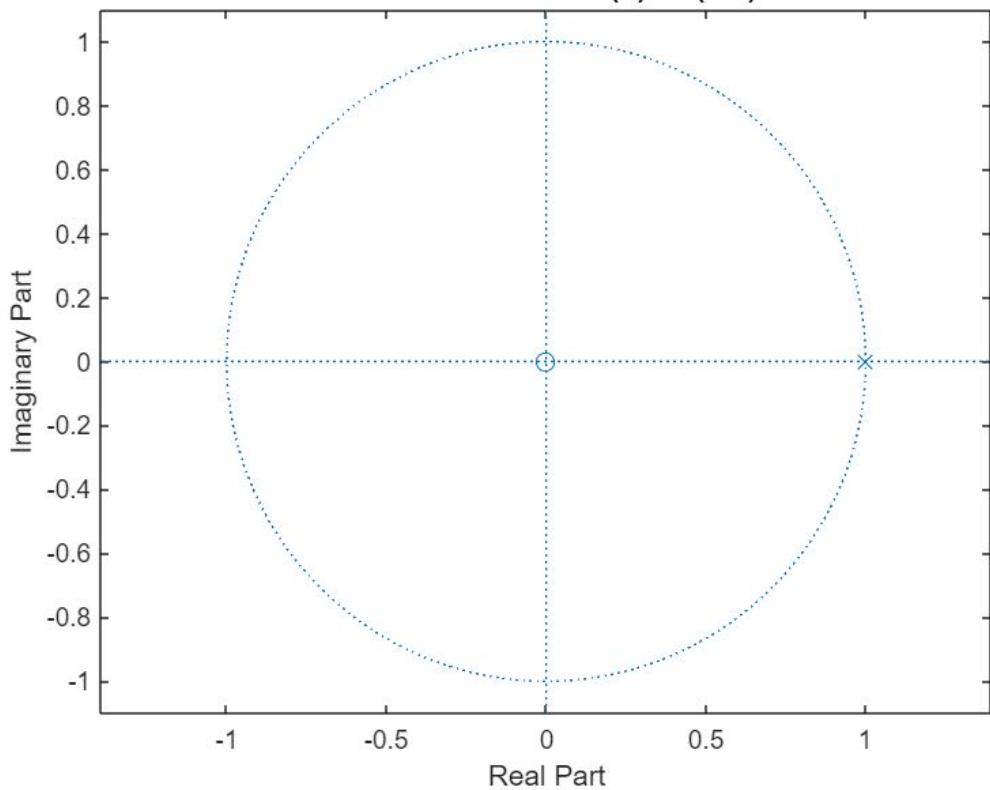
$$h(n) = \frac{46}{3} \left(\frac{1}{5} \right)^n u(n) + \left(-\frac{10}{3} \right) \left(\frac{1}{2} \right)^n u(n)$$

I have calculated $H(z)$ on paper and checking where are zeros and poles. After assigning those values to appropriate array \mathbf{z}, \mathbf{p} pass that array to $\text{zplane}(\mathbf{z}, \mathbf{p})$ function which is plot Z and P into plane. Exploring impz funtion in matlab, which is used to find impulse response of transfer function $\text{impz}(\mathbf{b}, \mathbf{a}, n)$, where \mathbf{b} is array of coefficients of nominator part and \mathbf{a} is array of coefficients of denominator part and $n=16$ are samples in output.

(c) Simulation Output:



Zeros and Poles of $H(Z) = Z/(Z-1)$



Zeros and Poles of $H(Z) = (2Z^2-1)/(Z-0.5)(Z-0.2)$

