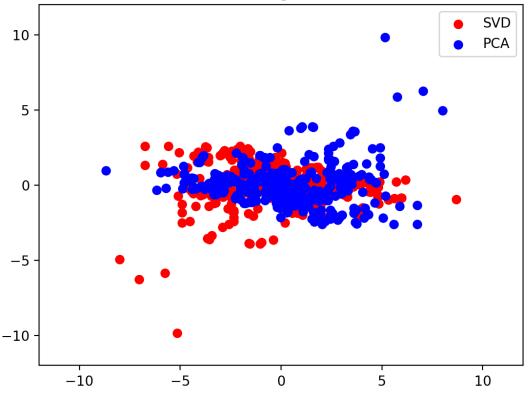
Brandon Luong

2. They are not the same. PCA and SVD are orthogonal to each other. The eigenvalues are flipped, PCA is [x,-y] and SVD is [-x, y]. They both still pick Dealer Price and Retail Price to be the columns with the highest variance.

```
checking if PCA pc are orthogonal: -0.0
checking if SVD pc are orthogonal: 0.0
             PCA
                                           SVD
0.2637504434, 0.4685086975
                                   -0.2637504434, -0.4685086975
0.2623186388, 0.4701465851
                                   -0.2623186388, -0.4701465851
0.347080492, -0.0153471865
                                   -0.347080492, 0.0153471865
0.3341887576, 0.0780320109
                                   -0.3341887576, -0.0780320109
0.3186022585, 0.2922134761
                                   -0.3186022585, -0.2922134761
-0.3104817267, -0.0033659358
                                     0.3104817267, 0.0033659358
-0.3065886386, -0.0109644601
                                     0.3065886386, 0.0109644601
0.3363293669, -0.1674635715
                                   -0.3363293669, 0.1674635715
0.2662100336, -0.418177107
                                   -0.2662100336, 0.418177107
0.2567901877, -0.4084113807
                                    -0.2567901877, 0.4084113807
0.2960545914, -0.3128913502
                                    -0.2960545914, 0.3128913502
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SVD and PCA Using Normalized Data



1.5674430636, -0.4472724582 II -1.5674430636, 0.4472724582 1.6356483399, -0.3397319469 II -1.6356483399, 0.3397319469 1.9066185788, -0.4111386039 II -1.9066185788, 0.4111386039 1.5901986477, 3.862579372 II -1.5901986477, -3.862579372 -2.6547635333, 0.6544513335 II 2.6547635333, -0.6544513335 0.4412425473, 0.0811070504 II -0.4412425473, -0.0811070504 -1.5381110973, 0.0283394434 II 1.5381110973, -0.0283394434 -2.0364083375, -0.0619046098 II 2.0364083375, 0.0619046098 -1.5339429783, 0.2322042074 II 1.5339429783, -0.2322042074 0.1509915682. 0.8018690073 | -0.1509915682. -0.8018690073 -0.4100932632, 0.4709363607 | | 0.4100932632, -0.4709363607 -0.0226164654, 0.5258027755 II 0.0226164654, -0.5258027755 0.0228169406, 0.5685083463 II -0.0228169406, -0.5685083463 0.5221142681, 0.847423195 II -0.5221142681, -0.847423195 0.9057821502, 0.2531061251 II -0.9057821502, -0.2531061251 0.3472865469, -0.1138695036 II -0.3472865469, 0.1138695036 0.9143886432, -0.0180059778 II -0.9143886432, 0.0180059778 0.8087162784, -0.0378180128 II -0.8087162784, 0.0378180128 2.4996408188, 0.7937269531 -2.4996408188, -0.7937269531 Ш 4.3834405911, 0.3932657715 Ш -4.3834405911, -0.3932657715 2.3576130438, 1.7820899045 II -2.3576130438, -1.7820899045 2.391094615, 1.7626644215 II -2.391094615, -1.7626644215 II -4.9143021816, -2.4923783185 4.9143021816, 2.4923783185 -1.9641266413, 1.3607825359 1.9641266413, -1.3607825359 -1.7827214655, 1.6097134844 1.7827214655, -1.6097134844 Ш -0.5642397602, 1.8437583742 Ш 0.5642397602, -1.8437583742 -1.0329412865, 0.2424709697 Ш 1.0329412865, -0.2424709697 -0.9625518, 0.3264677672 II 0.9625518, -0.3264677672 -0.4288061087, 0.5884081644 Ш 0.4288061087, -0.5884081644 -0.7027323085, 0.2729643372 Ш 0.7027323085, -0.2729643372 0.5153103636, -0.3673537396 -0.5153103636, 0.3673537396 Ш -0.4711635052, 0.7935746403 0.4711635052, -0.7935746403 Ш 0.0693272831, 1.0368374632 Ш -0.0693272831, -1.0368374632 -0.5112751123, 0.7220038154 Ш 0.5112751123, -0.7220038154 -0.3155999935, 0.7603590572 Ш 0.3155999935, -0.7603590572 0.3944948228, -0.5048945221 Ш -0.3944948228, 0.5048945221 0.7386390268, -0.1181527087 Ш -0.7386390268, 0.1181527087 2.8880205357, 0.7869098263 -2.8880205357, -0.7869098263 Ш 3.9982220961, 0.6923059597 Ш -3.9982220961, -0.6923059597 4.4517716674, 0.3814809823 -4.4517716674, -0.3814809823 Ш -1.1586810444, -1.5773765097 1.1586810444, 1.5773765097 Ш 1.6123718844, 1.8932200471 II -1.6123718844, -1.8932200471 1.0408344887, -0.0387099227 II -1.0408344887, 0.0387099227 3.4701199756, 0.722935891 II -3.4701199756, -0.722935891 -1.5128949559, 1.4722683208 II 1.5128949559, -1.4722683208 -1.0462434222, 1.9584098339 II 1.0462434222, -1.9584098339

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                           II 2.3485183143, -0.4094291849
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                              -0.0611243689, 0.3076034132
2.3112524996, -0.4070333486 II -2.3112524996, 0.4070333486
```

3. In our case:

```
PC1 PC2
1. [[-725.18054467 -341.57979887]
2. [-721.24380473 -342.77394816]
3. [-954.29610266 11.1893096]
4. [-918.85034246 -56.8914915]
5. [-875.99533986 -213.04667542]
6. [ 853.66797782 2.45403269]
7. [ 842.96395113 7.99395638]
8. [-924.73593721 122.09415405]
9. [-731.94317561 304.88409895]
10. [-706.04335572 297.76411411]
11. [-814.00064035 228.12247676]]
```

The first column representing PC1 has a higher variance for each feature. Therefore all features contributed the most to PC1, and only a small amount to PC2.

It also confirmed when you check the eigen_value/eigensum:

1, 0.65 2, 0.82 3, 0.89 4, 0.93 5, 0.95 6, 0.97 7, 0.97 8, 0.98 9, 0.99 10, 0.99 11, 1.0

Shows that even with only 1 column we are able retain 65% of our original data. From here we can see that:

Feature 1: is strongly negatively correlated to PC1 and PC2
Feature 2: is strongly negatively correlated to PC1 and PC2
Feature 3: is strongly negatively correlated to PC1 and a minimal positive correlation to PC2
Feature 4: is strongly negatively correlated to PC1 and slightly negative correlated PC2
Feature 5: is strongly negatively correlated to PC1 and negative correlated PC2
Feature 6: is strongly positively correlated to PC1 and a minimal positive correlation to PC2
Feature 7: is strongly positively correlated to PC1 and a minimal positive correlation to PC2
Feature 8: is strongly negatively correlated to PC1 and a positive correlation to PC2
Feature 9: is strongly negatively correlated to PC1 and a positive correlation to PC2
Feature 10: is strongly negatively correlated to PC1 and a positive correlation to PC2
Feature 11: is strongly negatively correlated to PC1 and a positive correlation to PC2

Please view output and image if you need more information. I Printed everything