

Ratio & proportions

Ans: Given, Ratio of incomes $A:B=3:5$
 \rightarrow Let A's income = $3x$, B's income = $5x$

• Ratio of expenditures $A:B=2:3$
A's expenditure = $2y$, B's expenditure = $3y$

• A saves 20% of his income \rightarrow Savings
 $= 20\% \text{ of } 3x = 0.6x$

\therefore Savings = Income - Expenditure

$$0.6x = 3x - 2y$$

$$\Rightarrow 2y = 3x - 0.6x$$

$$\Rightarrow 2y = 2.4x \Rightarrow y = 1.2x$$

$$B's \text{ expenditure} = 3y = 3 \times 1.2x = 3.6x$$

$$B's \text{ Saving} = 5x - 3.6x = 1.4x$$

$$\text{Percentage} = \frac{1.4x}{5x} \times 100 = 28\%$$

$$\frac{8 \times 7 \times 6}{5 \times 3}$$

$$8 \times 7 \times 6 \times 5$$

2 Ans: - Given,

Milk : Water = 4 : 1

$$\Rightarrow \text{Milk} = 4x, \text{Water} = x$$

10 liters of water is added \rightarrow New water
 $= x + 10$

New ratio becomes 2 : 1

$$\Rightarrow \frac{4x}{x+10} = \frac{2}{1}$$

$$4x = 2(x+10)$$

$$4x = 2x + 20 \Rightarrow 2x = 20 \Rightarrow \boxed{x = 10}$$

\therefore Milk = $4 \times 10 = 40$ litres,

3 Ans: - Given, initial ratio: Boys : Girls = 5 : 3

$$\Rightarrow \text{Boys} = 5x, \text{Girls} = 3x$$

$$\text{After Change: } \frac{5x-4}{3x+2} = \frac{3}{2}$$

$$\Rightarrow 2(5x-4) = 3(3x+2)$$

$$10x - 8 = 9x + 6$$

$$10x - 9x = 6 + 8$$

$$\boxed{x = 14}$$

\therefore Total initial students = $5x + 3x = 8x$
 $= 8 \times 14 = 112 //$

4 Ans: - Ratio : A : B : C = 2 : 3 : 5, Share one $2x, 3x, 5x$

$$\text{Diff} = 5x - 2x = \text{Rs } 1500$$

$$\Rightarrow 3x = 1500 \Rightarrow \boxed{x = 500}$$

$$\text{Total Sum} = 2x + 3x + 5x = 10x = 10 \times 500 = \text{Rs } 5000$$

5Ans:- Given,

Alloy 1: Copper: Zinc = 3:2 \rightarrow Copper fraction = $\frac{3}{5}$

Alloy 2: Copper: Zinc = 4:1 \rightarrow Copper fraction = $\frac{4}{5}$

Desired ratio: 7:3 \rightarrow Copper fraction = $\frac{7}{10}$

Allegation:- $\frac{4}{5} - \frac{7}{10} = \frac{8}{10} - \frac{7}{10} = \frac{1}{10}$

Ratio of mixing = 1:1

6Ans:- Given,

Speed ratio: Fast: Slow = 5:4

Faster train covers 360km in 3hrs
 \rightarrow Speed = $360 \div 3 = 120 \text{ km/h}$

So, slower train's speed = $\frac{4}{5} \times 120 = 96 \text{ km/h}$

Time = $\frac{320}{96} = 3.33 \text{ hrs}$ (taken by slow train to cover 320km)

7Ans:- Initial ratio: A: B: C = 4: 5: 6 \rightarrow Let them be $4x, 5x, 6x$

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Transactions: A gives Rs 200 to B, B gives Rs 300 to C

New amounts:

$$\begin{aligned} A &: 4x - 200 \\ B &: 5x + 200 - 300 = 5x - 100 \\ C &: 6x + 300 \end{aligned}$$

New ratio: $(4x - 200) : (5x - 100) : (6x + 300)$
 $= 3 : 4 : 5$

$$\frac{4x - 200}{3} = \frac{5x - 100}{4}$$

$$\begin{aligned} \Rightarrow 4(4x - 200) &= 3(5x - 100) \\ \Rightarrow 16x - 800 &= 15x - 300 \\ \Rightarrow x &= 500 \end{aligned}$$

\therefore Initial A amt = $4x = 4 \times 500 = \text{Rs } 2000$

8Ans: Initial ratio: $x : y = 7 : 3 \Rightarrow \text{Total} = 7x + 3x = 10x \Rightarrow x = 7x, y = 3x$

20 liters removed \Rightarrow removed $x = \frac{7}{10} \times 20 = 14$ liters

removed $y = \frac{3}{10} \times 20 = 6$ liters

Remainings:

$$x = 7x - 14$$

$$y = 3x - 6 + 20$$

New ratio:

$$\frac{7x - 14}{3x - 6 + 20} = \frac{7}{5}$$

$$\frac{7x-14}{3x+14} = \frac{7}{5} \Rightarrow 5(7x-14) = 7(3x+14)$$

$$\Rightarrow 35x - 70 = 21x + 98$$

$$\Rightarrow 14x = 168 \Rightarrow \boxed{x = 12}$$

$$\therefore \text{Total Capacity} = 10x = 10 \times 12 = 120 \text{ litres}$$

9Ans:- Given,

Current age ratio: A:B:C = 2:3:5

$$\Rightarrow A = 2x, B = 3x, C = 5x$$

After 5 years: $(2x+5):(3x+5):(5x+5)$
 $= 5:7:11$

$$\Rightarrow \frac{2x+5}{5} = \frac{3x+5}{7} \Rightarrow 7(2x+5) = 5(3x+5)$$

$$14x + 35 = 15x + 25$$

$$14x - 15x = 25 - 35$$

$$-x = -10 \Rightarrow \boxed{x = 10}$$

$$A's \text{ Current age} = 2x = 2 \times 10 = 20 \text{ years}$$

10Ans:- Given,

$$A's \text{ Share} = 2 \times B's \text{ Share}$$

$$B's \text{ Share} = 3 \times C's \text{ Share}$$

$$\text{Let } C's \text{ Share} = x$$

$$B's \text{ Share} = 3x$$

$$\Rightarrow A's \text{ Share} = 2 \times 3x = 6x$$

$$T.A = 6x + 3x + x = 1200 \Rightarrow 10x = 1200 \Rightarrow \boxed{x = 120}$$

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$$B's \text{ Share} = 3x = 3 \times 120 = \text{RS } 360 //$$

11Ans: Ratio of Two no - 4:5 $\rightarrow 4x \text{ \& } 5x$

$$LCM = 180$$

LCM of $4x \text{ \& } 5x$ is;

$$LCM = \frac{4x \times 5x}{HCF} = \frac{20x^2}{x} = 20x$$

$$\boxed{HCF = x = 9}$$

12Ans: Rice type mixed in ratio 3:2 \rightarrow Total parts = $3+2 = 5$ parts

price per kg: First type = RS 40, Second type = RS 50

1. Average price per kg:

$$= \frac{(3 \times 40) + (2 \times 50)}{5} = \frac{120 + 100}{5}$$

$$= 44 //$$

13Ans: Initial ratio: Milk (water) 5:2 $\Rightarrow 5x \text{ \& } 2x$

14 litres removed \rightarrow Milk removed

$$= \frac{5}{7} \times 14 = 10 \text{ litres, water removed}$$

$$= \frac{2}{7} \times 14 = 4 \text{ litres}$$

remaining: Milk = $5x - 10$, Water = $2x - 4$
 $+ 6$

New ratio!

$$\frac{5x - 10}{2x - 4 + 6} = \frac{3}{2}$$

$$\Rightarrow 10x - 20 = 6x + 6 \Rightarrow 4x = 26$$

$$\Rightarrow \boxed{x = 6.5}$$

\therefore Initial mixture = $7x = 7 \times 6.5 = 45.5 \text{ litres}$

Ans:- Given,

Initial investment ratio: A: B: C = 3:4:5

Total profit = Rs 4800 \Rightarrow profit sharing
 3:4:5

① Sum of ratio = $3 + 4 + 5 = 12 \text{ parts}$

A's Initial Share = $\frac{3}{12} \times 4800 = 1200$

B's Initial Share = $\frac{4}{12} \times 4800 = 1600$

C's Initial Share = $\frac{5}{12} \times 4800 = 2000$

② Profit is reinvested, invested ratio becomes 4:5:6

Total parts = $4 + 5 + 6 = 15 \text{ parts}$

\therefore A's new Share = $\frac{4}{15} \times 4800 = \text{Rs } 2800 //$