

Robot Dynamics & Control

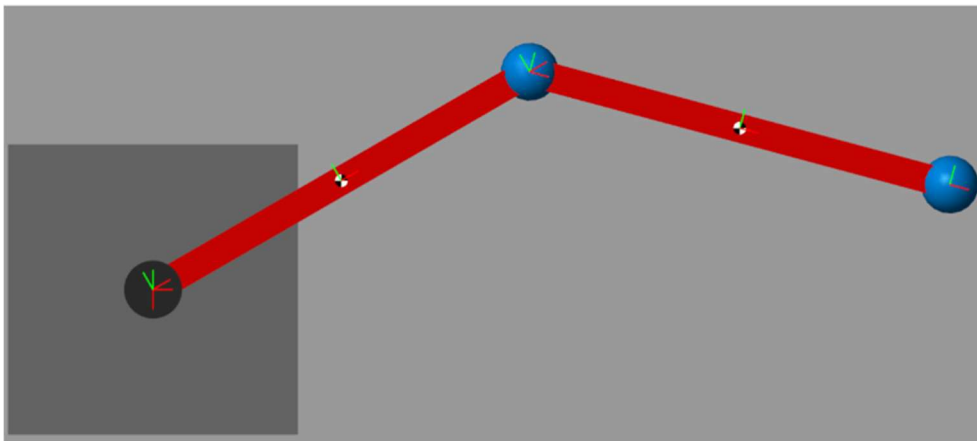
September session - 07/09/2023

Duration - 2:30 h

Important notes:

- It is advised to define the link widths and joint sizes reasonably.
- It is strongly advised to define the manipulator frames according to Denavit-Hartenberg convention. Incorrectly defined frames can lead to grade reduction.
- If the model parameters / joint positions / trajectories do not correspond to those defined in the task, the corresponding task will not be graded.
- If the model uses workspace variables, a *.mat* file or an *.m* script defining them must be included, otherwise the corresponding tasks will not be graded.
- In the tasks using *RigidBodyTree*, a *.mat* file or an *.m* script defining it must be included, otherwise the corresponding tasks will not be graded.

2R Robot



Consider a planar 2R robot with the following set of parameters:

Mass of link 1: 4 Kg

Length of link 1: 35 cm

Mass of link 2: 0.7 Kg

Length of link 2: 17.5 cm

Task 1: Statics

- 1) Set joint positions at $q = [-15^\circ, -65^\circ]$. Implement gravity compensation using the manipulator statics.
- 2) Implement gravity compensation in the same configuration using the manipulator statics

considering a spherical end-effector of mass $M_e = 3$ Kg.

- 3) Implement gravity compensation in the same configuration using the manipulator statics considering a spherical end-effector of mass $M_e = 1$ Kg and two additional masses (modeled as spherical objects): one of 1 Kg placed on link 1 at $1/3$ of its total length, the other one of 0.5 Kg placed on link 2 at $1/2$ of its total length.

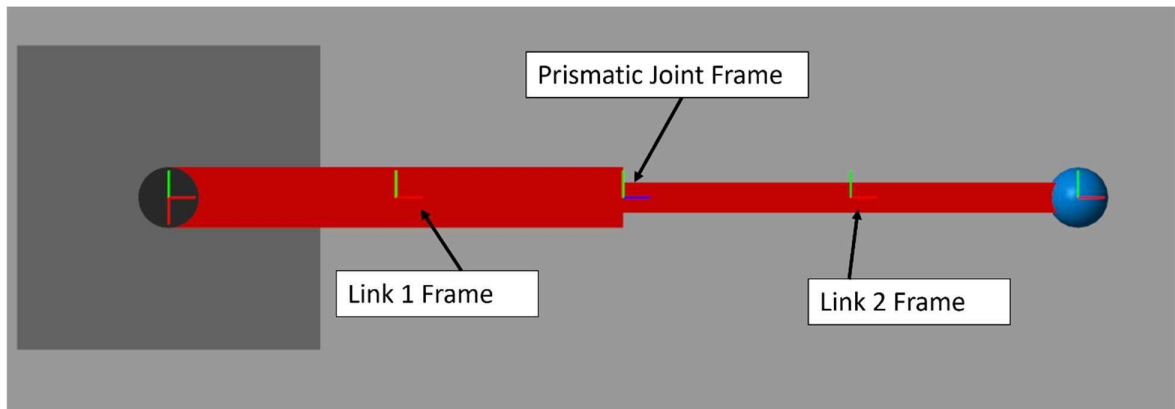
Task 2: Newton-Euler Algorithm

- 1) Implement the Newton-Euler algorithm for recursive inverse dynamics. Generate a cubic polynomial trajectory with the following initial and final configurations: $q_i = [0^\circ, 70^\circ]$, $q_f = [-20^\circ, 90^\circ]$. Consider gravity effect. Do not consider damping in the joints.

Task 3: Control

- 1) Implement the PD controller with gravity compensation term. Given the following initial joint configuration $q_i = [30^\circ, 65^\circ]$ control the robot to reach the final configuration $q_f = [55^\circ, -30^\circ]$.
- 2) Implement the Computed Torque control law using the Robotics System Toolbox blocks. Generate a quintic polynomial trajectory with the following initial and final configurations: $q_i = [10^\circ, 35^\circ]$, $q_f = [95^\circ, 110^\circ]$. Also, the trajectory should pass by an intermediate joint configuration $q = [60^\circ, 85^\circ]$. Also consider gravity action.

RP Robot



Consider a planar RP robot like the one shown in figure (**second joint is a prismatic joint with motion axis along the x-axis of the link**) with the following set of parameters:

Mass of link 1: 2 Kg

Length of link 1: 40 cm

Mass of link 2: 2.5 Kg

Length of link 2: 30 cm

Task 1: Statics

- 1) Joint position $q = [30^\circ, 15 \text{ cm}]$. Implement gravity compensation using the manipulator statics.
- 2) Implement gravity compensation in the same configuration using the manipulator statics considering a spherical end-effector of mass $M_e = 2 \text{ Kg}$.
- 3) Implement gravity compensation in the same configuration using the manipulator statics considering a spherical end-effector of mass $M_e = 1 \text{ Kg}$ and an additional mass of 5 Kg (modeled as a spherical object) placed on link 2 at $2/3$ of its total length.

Task 2: Newton-Euler Algorithm

- 1) Implement the Newton-Euler algorithm for recursive inverse dynamics. Generate a cubic polynomial trajectory with the following initial and final configurations: $q_i = [15^\circ, 0 \text{ cm}]$, $q_f = [65^\circ, 25 \text{ cm}]$. Consider gravity effects. Do not consider damping in the joints.

Task 3: Control

- 1) Implement the PD controller with gravity compensation term. Given the following initial joint configuration $q_i = [30^\circ, 0 \text{ cm}]$, control the robot to reach the final configuration $q_f = [0^\circ; 20\text{cm}]$.
- 2) Implement the Computed Torque control law using the Robotics System Toolbox blocks. Generate a quintic polynomial trajectory with the following initial and final configurations: $q_i = [30^\circ, 0 \text{ cm}]$, $q_f = [-20^\circ; 20\text{cm}]$. Also, the trajectory should pass by an intermediate joint configuration $q = [0^\circ, 10\text{cm}]$. Also consider gravity action.