WEEK 6

* Some clarifications;

-Now consider:

$$\frac{(x-x_{1})}{h} = 1 - \frac{1}{h} \left(\frac{x(x_{1+1}-x_{1})}{x(x_{1+1}-x_{1})} + x_{1} - x_{1} \right) \\
= x(x)$$

$$= 1 - x \quad \text{This is } Q_{0}(x) \text{ in } x$$

$$=) \int_{x_{i}}^{x_{i}} Q_{i}(x) dx = \int_{0}^{1} Q_{i}(x(x)) |J| dx \int_{0}^{1} No \text{ need to call}$$
and
$$2Q_{i}(x(x)) = 2Q_{i}(x(x)) \cdot 2x(x)$$

$$2x(x) \cdot 2x \cdot 2x$$

- Also consider

$$\int_{x_{i}}^{K_{i+1}} f(x_{i}x_{i}) dx = \int_{0}^{1} f\left(x_{i}(x_{i+1} - x_{i}) - x_{i}\right) 1 dx$$

$$= T(x_{i}) = x(x_{i})$$

At clarification about transformation using triangles;

$$(0_{1}i) \qquad \zeta^{-1} \qquad P_{2} \qquad Q_{0}(x,q) = 1 - x - q$$

$$(0_{1}i) \qquad P_{0} \qquad Q_{1}(x,q) = x$$

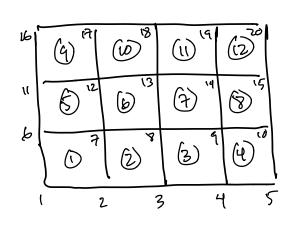
$$(0_{1}i) \qquad P_{1} \qquad Q_{2}(x,q) = q$$

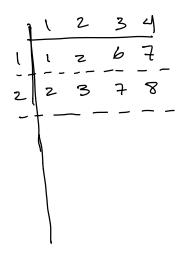
$$Q_{0}(x,q) = 1 - x - q$$

$$Q_{1}(x,q) = x$$

$$Q_{2}(x,q) = q$$

of for connectionty;





weathy:

* Project some function v(x) onto Vn 1

* find un with EVn to the Used = vh(x) on a weak sense

Weak formulabless:

e Lin. algebra:

$$\sum_{j} V_{j} \int_{\Omega} Q_{i}Q_{j} dx = \int_{\Omega} U(x)Q_{i} dx = : F_{i}$$

$$= m_{ij}$$

K See the code in Matlab

* Solve the Poisson equation)

at Linear Plyebra problem:

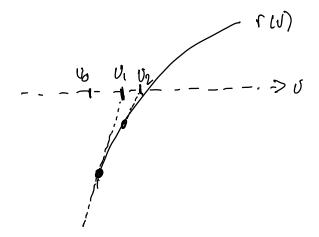
$$\frac{\sum_{i} V_{i} \int_{\mathbb{R}^{2}} \nabla \ell_{i} \cdot \nabla \ell_{j} \, d_{x}}{= \int_{\mathbb{R}^{2}} f(x^{2}) \, \varphi_{i} \, d_{x}} = \int_{\mathbb{R}^{2}} f(x^{2}) \, \varphi_{i} \, d_{x}}{= : F_{t}}$$

Bandary. Then $S_{\bar{i}} = [0...010...0]$

Fi=0 = 2 Boundary value at i-th rude.

of Newtonis method for Northnear Scalar equation !

* fund v* S.I. r(v*)=0



of The (keti)-th Heration 15:

* Newton's method for system of equations

* Example: Given

$$P_{t}(v) = \alpha m_{t}^{r(\sigma)} \left[V_{t} - \tilde{V}_{t} \right] + \left[S_{e} \left(V_{u} \right) \right] \left[V_{un} \right] - 1 \right] e dx$$

$$+ c h \int_{\Sigma} \nabla u_{n} \cdot \nabla e \, dS$$

Where
$$d = 10^{10}$$
, $\tilde{V}_{h} = \frac{2}{3}\tilde{V}_{j}$ & given $c = \frac{1}{2}$
 $\epsilon = 0.1h$

and
$$m_i \Gamma \omega = \int_{\Omega} S_{\epsilon} (r) Q_i dx$$

and
$$S_{\epsilon}(\vec{v}) = 2H_{\epsilon}(\vec{v}) - 1$$

 $S_{\epsilon}(\vec{v}) = H_{\epsilon}(\vec{v})$

$$H_{\varepsilon}(0) = \frac{1}{2} \left[1 + \frac{0}{\varepsilon} + \frac{1}{\pi} S_{\text{IN}} \left(\pi \frac{\hat{v}}{\varepsilon} \right) \right] \quad \text{if} \quad \tilde{v} \leq -\varepsilon$$

$$\frac{1}{2} \left[1 + \frac{0}{\varepsilon} + \frac{1}{\pi} S_{\text{IN}} \left(\pi \frac{\hat{v}}{\varepsilon} \right) \right] \quad \text{if} \quad -\varepsilon \leq \tilde{v} \leq \varepsilon$$

$$\frac{1}{2} \left[1 + \frac{0}{\varepsilon} + \frac{1}{\pi} S_{\text{IN}} \left(\pi \frac{\hat{v}}{\varepsilon} \right) \right] \quad \text{if} \quad \tilde{v} \geq \varepsilon$$

& What is the Jacobian ?

$$J = \frac{2R(v)}{av} - dm_{\tilde{i}} + \frac{2E(v)}{av} + chS$$

where E(v) is a vector whose ith entry is:

& Note that 25/15/20 is a Matrix

* What is the (i,j)-th entry of 2E(v) ?

$$\left(\frac{2E(r)}{2r}\right)_{ij} = \frac{2E_i lr}{2r_j} = \int_{2}^{2} Selon \frac{2|\nabla v_n|}{2r_j} e_i dx$$

* Then,

$$\frac{2 \text{Eilb}}{2 \text{Tj}} = \int_{\mathcal{L}} S_{\text{Elbh}} \frac{(\text{Tuh. Tqj})}{\text{ITuhl}} e_{\text{i}} d_{\text{K}}$$

* Finally,

$$J_{ij}^{(k)} = Am_i^{(k)} + \int_{\mathcal{S}_{\epsilon}} S_{\epsilon} U_h \frac{[\nabla v_h^{(k)} \cdot \nabla v_j] \cdot q_i}{|\nabla v_h^{(k)}|} dx + ch \int_{\mathcal{N}} \nabla v_i \cdot \nabla v_j dx$$

at we need to compute this Matrix. (See the code in Modlab)