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basic education

Department:
Basic Education
REPUBLIC OF SOUTH AFRICA

NATIONAL SENIOR CERTIFICATE

GRADE 12

MATHEMATICS P1

NOVEMBER 2023

MARKS: 150

TIME: 3 hours

This question paper consists of 9 pages and 1 information sheet.

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INSTRUCTIONS AND INFORMATION

Read the following instructions carefully before answering the questions.

- 1. This question paper consists of 10 questions.
- 2. Answer ALL the questions.
- 3. Number the answers correctly according to the numbering system used in this question paper.
- 4. Clearly show ALL calculations, diagrams, graphs, etc. that you have used in determining your answers.
- 5. Answers only will NOT necessarily be awarded full marks.
- 6. You may use an approved scientific calculator (non-programmable and non-graphical), unless stated otherwise.
- 7. If necessary, round off answers to TWO decimal places, unless stated otherwise.
- 8. Diagrams are NOT necessarily drawn to scale.
- 9. An information sheet with formulae is included at the end of the question paper.
- 10. Write neatly and legibly.

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QUESTION 1

1.1 Solve for x:

$$1.1.1 x^2 + x - 12 = 0 (3)$$

1.1.2
$$3x^2 - 2x = 6$$
 (answers correct to TWO decimal places) (4)

$$1.1.3 \sqrt{2x+1} = x-1 (4)$$

$$1.1.4 x^2 - 3 > 2x (4)$$

1.2 Solve for x and y simultaneously:

$$x + 2 = 2y$$
 and $\frac{1}{x} + \frac{1}{y} = 1$ (5)

1.3 Given: $2^{m+1} + 2^m = 3^{n+2} - 3^n$ where m and n are integers.

Determine the value of
$$m + n$$
. (4) [24]

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QUESTION 2

2.1 Given the arithmetic series: $7 + 12 + 17 + \dots$

2.1.1 Determine the value of T_{91} (3)

- 2.1.2 Calculate S_{91} (2)
- 2.1.3 Calculate the value of n for which $T_n = 517$ (3)
- 2.2 The following information is given about a quadratic number pattern:

 $T_1 = 3$, $T_2 - T_1 = 9$ and $T_3 - T_2 = 21$

- 2.2.1 Show that $T_5 = 111$ (2)
- 2.2.2 Show that the general term of the quadratic pattern is $T_n = 6n^2 9n + 6$ (3)
- 2.2.3 Show that the pattern is increasing for all $n \in N$. (3) [16]

QUESTION 3

- 3.1 Given the geometric series: 3+6+12+... to *n* terms.
 - 3.1.1 Write down the general term of this series. (1)
 - 3.1.2 Calculate the value of k such that: $\sum_{p=1}^{k} \frac{3}{2} (2)^p = 98301$ (4)
- 3.2 A geometric sequence and an arithmetic sequence have the same first term.
 - The common ratio of the geometric sequence is $\frac{1}{3}$
 - The common difference of the arithmetic sequence is 3
 - The sum of 22 terms of the arithmetic sequence is 734 more than the sum to infinity of the geometric sequence.

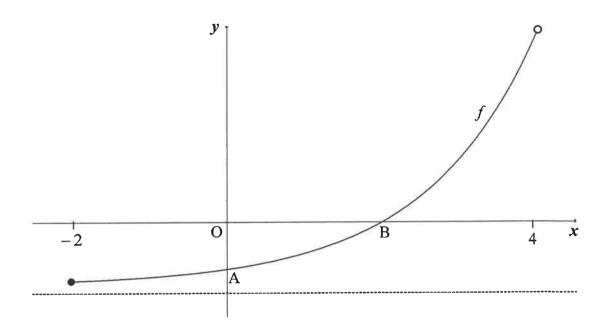
Calculate the value of the first term. (5) [10]

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QUESTION 4

Sketched below is the graph of $f(x) = 2^x - 4$ for $x \in [-2; 4)$.

A and B are respectively the y- and x-intercepts of f.

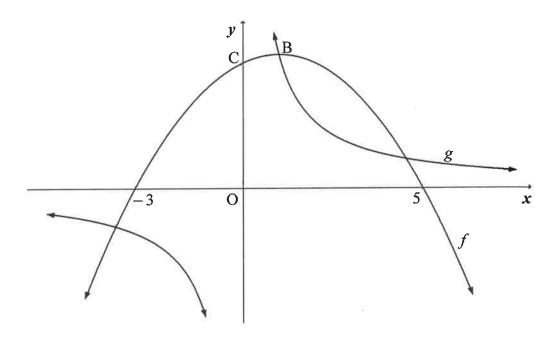


- 4.1 Write down the equation of the asymptote of f. (1)
- 4.2 Determine the coordinates of B. (2)
- Determine the equation of k, a straight line passing through A and B in the form $k(x) = \dots$ (3)
- 4.4 Calculate the vertical distance between k and f at x = 1 (3)
- 4.5 Write down the equation of g if it is given that g(x) = f(x) + 4 (1)
- 4.6 Write down the domain of g^{-1} . (2)
- 4.7 Write down the equation of g^{-1} in the form y = ... (2) [14]

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QUESTION 5

The graphs of $f(x) = -\frac{1}{2}(x-1)^2 + 8$ and $g(x) = \frac{d}{x}$ are drawn below. A point of intersection of f and g is B, the turning point of f. The graph f has x-intercepts at (-3;0) and (5;0)and a y-intercept at C.



- Write down the coordinates of the turning point of f. (2) 5.1
- Calculate the coordinates of C. (2) 5.2
- (1) Calculate the value of d. 5.3
- (1) 5.4 Write down the range of g.
- (3) For which values of x will $f(x).g(x) \le 0$? 5.5
- Calculate the values of k so that h(x) = -2x + k will not intersect the graph of g. (5) 5.6
- h is a tangent to g at R, a point in the first quadrant. Calculate t such that 5.7 y = f(x) + t intersects g at R. (4)

[18]

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OUESTION 6

- Patrick deposited an amount of R18 500 into an account earning r% interest p.a., compounded monthly. After 6 months, his balance was R19 319,48.
 - 6.1.1 Calculate the value of r.

(3)

6.1.2 Calculate the effective interest rate.

(2)

- Kuda bought a laptop for R10 000 on 31 January 2019. He will replace it with a new one in 5 years' time on 31 January 2024.
 - 6.2.1 The value of the old laptop depreciates annually at a rate of 20% p.a. according to the straight-line method. After how many years will the laptop have a value of R0?

(2)

Kuda will buy a laptop that costs R20 000. In order to cover the cost price, he made his first monthly deposit into a savings account on 28 February 2019. He will make his 60th monthly deposit on 31 January 2024. The savings account pays interest at 8,7% p.a., compounded monthly. Calculate Kuda's monthly deposit into this account.

(4)

Tino wins a jackpot of R1 600 000. He invests all of his winnings in a fund that earns interest of 11,2% p.a., compounded monthly. He withdraws R20 000 from the fund at the end of each month. His first withdrawal is exactly 1 month after his initial investment. How many withdrawals of R20 000 will Tino be able to make from this fund?

(5) [**16**]

QUESTION 7

7.1 Determine f'(x) from first principles if $f(x) = -4x^2$

(5)

7.2 Determine:

7.2.1
$$f'(x)$$
 if $f(x) = 2x^3 - 3x$ (2)

7.2.2
$$D_x \left(7.\sqrt[3]{x^2} + 2x^{-5}\right)$$
 (3)

7.3 For which values of x will the tangent to $f(x) = -2x^3 + 8x$ have a positive gradient? (3)

[13]

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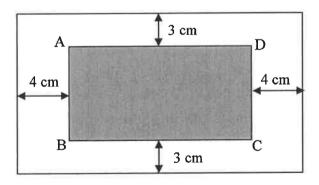
QUESTION 8

Given:
$$f(x) = -x^3 + 6x^2 - 9x + 4 = (x-1)^2(-x+4)$$

- 8.1 Determine the coordinates of the turning points of f. (4)
- 8.2 Draw a sketch graph of f. Clearly label all the intercepts with the axes and any turning points. (4)
- Use the graph to determine the value(s) of k for which $-x^3 + 6x^2 9x + 4 = k$ will have three real and unequal roots. (2)
- 8.4 The line g(x) = ax + b is the tangent to f at the point of inflection of f. Determine the equation of g.
- 8.5 Calculate the value of θ , the acute angle formed between g and the x-axis in the first quadrant. (2) [18]

QUESTION 9

The diagram below represents a printed poster. Rectangle ABCD is the part on which the text is printed. This shaded area ABCD is 432 cm^2 and AD = x cm. ABCD is 4 cm from the left and right edges of the page and 3 cm from the top and bottom of the page.



9.1 Show that the total area of the page is given by:

$$A(x) = \frac{3456}{x} + 6x + 480\tag{3}$$

9.2 Determine the value of x such that the total area of the page is a minimum. (3)

[6]

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QUESTION 10

10.1 A and B are independent events. $P(A) = \frac{1}{3}$ and $P(B) = \frac{3}{4}$ Determine:

10.1.1 P(A and B) (2)

10.1.2 P(at least ONE event occurs) (2)

- The probability that it will snow on the Drakensberg Mountains in June is 5%.
 - When it snows on the mountains, the probability that the minimum temperature in Central South Africa will drop below 0 °C is 72%.
 - If it does not snow on the mountains, the probability that the minimum temperature in Central South Africa will drop below 0 °C is 35%.
 - 10.2.1 Represent the given information on a tree diagram. Clearly indicate the probabilities associated with EACH branch.
 - 10.2.2 Calculate the probability that the temperature in Central South Africa will NOT drop below 0 °C in June 2024. (3)
- Ten learners stand randomly in a line, one behind the other.
 - 10.3.1 In how many different ways can the ten learners stand in the line? (1)
 - 10.3.2 Calculate the probability that there will be 5 learners between the 2 youngest learners in the line.

(3)

(4)

[15]

TOTAL: 150

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INFORMATION SHEET

INFORMATION SHEET

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$A = P(1+ni) \qquad A = P(1-ni) \qquad A = P(1-i)^n \qquad A = P(1+i)^n$$

$$T_n = a + (n-1)d \qquad S_n = \frac{n}{2}[2a + (n-1)d]$$

$$T_n = ar^{n-1} \qquad S_n = \frac{a(r^n - 1)}{r-1} ; r \neq 1 \qquad S_\infty = \frac{a}{1-r}; -1 < r < 1$$

$$F = \frac{x[(1+i)^n - 1]}{i}$$

$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \qquad M\left(\frac{x_1 + x_2}{2}; \frac{y_1 + y_2}{2}\right)$$

$$y = mx + c \qquad y - y_1 = m(x - x_1) \qquad m = \frac{y_2 - y_1}{x_2 - x_1} \qquad m = \tan\theta$$

$$(x - a)^2 + (y - b)^2 = r^2$$

$$In \ \Delta ABC: \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$area \ \Delta ABC = \frac{1}{2}ab \sin C$$

$$\sin(\alpha + \beta) = \sin\alpha .\cos\beta + \cos\alpha .\sin\beta \qquad \sin(\alpha - \beta) = \sin\alpha .\cos\beta - \cos\alpha .\sin\beta$$

$$\cos(\alpha + \beta) = \cos\alpha .\cos\beta + \sin\alpha .\sin\beta \qquad \cos(\alpha - \beta) = \cos\alpha .\cos\beta + \sin\alpha .\sin\beta$$

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