

# 1 Thresholds for the assets of the entrant

Derived from the incentive compatibility constraint (IC) of the entrant:

$$R^S = B \quad (1)$$

Derived from the investors' participation (IP) constraint:

$$\pi_E^{t=2} - R^S \geq K - A' \quad (2)$$

Initial assets of the entrant at t=2(i), if the incumbent does not copy:

$$A' = A + \underbrace{\delta(1 - \beta)}_{\pi_E^{t=1}} \quad (3)$$

Initial assets of the entrant at t=2(i), if the incumbent copies:

$$A' = A + \underbrace{0}_{\pi_E^{t=1}} \quad (4)$$

**Calculate  $\underline{A}_S$**

Plug  $\pi_E^{t=2} = \Delta + \delta$ , (1) and (3) into (2):

$$\begin{aligned} \Delta + \delta - B &\geq K - A - \delta(1 - \beta) \\ \implies A &\geq \underline{A}_S = K + B - \Delta - \delta(2 - \beta) \end{aligned} \quad (5)$$

**Calculate  $\underline{A}_C$**

Plug  $\pi_E^{t=2} = 2\delta(1 - \beta)$ , (1) and (3) into (2):

$$\begin{aligned} 2\delta(1 - \beta) - B &\geq K - A - \delta(1 - \beta) \\ \implies A &\geq \underline{A}_C = K + B - 3\delta(1 - \beta) \end{aligned} \quad (6)$$

**Calculate  $\overline{A}_S$**

Plug  $\pi_E^{t=2} = \Delta$ , (1) and (4) into (2):

$$\begin{aligned} \Delta - B &\geq K - A \\ \implies A &\geq \overline{A}_S = K + B - \Delta \end{aligned} \quad (7)$$

**Calculate  $\overline{A}_C$**

Plug  $\pi_E^{t=2} = \delta(1 - \beta)$ , (1) and (4) into (2):

$$\begin{aligned} \delta(1 - \beta) - B &\geq K - A \\ \implies A &\geq \overline{A}_C = K + B - \delta(1 - \beta) \end{aligned} \quad (8)$$

## 2 Thresholds for the fixed costs of the incumbent

Fixed cost threshold, if the entrant invests for sure:

$$F \leq F_{\sigma_E}^{YY} = \pi_I(\sigma_E, \odot, Y) - \pi_I(\sigma_E, \emptyset, Y) \quad (9)$$

Fixed cost threshold, if the incumbent can prevent the entrant to develop its product:

$$F \leq F_{\sigma_E}^{YN} = \pi_I(\sigma_E, \odot, N) - \pi_I(\sigma_E, \emptyset, Y) \quad (10)$$

Benefits of the incument for different choices:

$$\pi_I(S, \odot, Y) = \underbrace{\pi_E(I_P + I_C; E_C)}_{\pi_E^{t=1}} + \underbrace{\pi_E(I_P + I_C; E_C + E_P)}_{\pi_E^{t=2}} = u + \delta \quad (11)$$

$$\pi_I(S, \emptyset, Y) = \underbrace{\pi_E(I_P; E_C)}_{\pi_E^{t=1}} + \underbrace{\pi_E(I_P; E_C + E_P)}_{\pi_E^{t=2}} = u + \delta\beta \quad (12)$$

$$\pi_I(S, \odot, N) = \underbrace{\pi_E(I_P + I_C; E_C)}_{\pi_E^{t=1}} + \underbrace{\pi_E(I_P + I_C; E_C)}_{\pi_E^{t=2}} = 2(u + \delta) \quad (13)$$

$$\pi_I(C, \odot, Y) = \underbrace{\pi_E(I_P + I_C; E_C)}_{\pi_E^{t=1}} + \underbrace{\pi_E(I_P + I_C; E_C + \tilde{E}_C)}_{\pi_E^{t=2}} = 2u + 2\delta + \delta\beta \quad (14)$$

$$\pi_I(C, \emptyset, Y) = \underbrace{\pi_E(I_P; E_C)}_{\pi_E^{t=1}} + \underbrace{\pi_E(I_P; E_C + \tilde{E}_C)}_{\pi_E^{t=2}} = 2u + 3\delta\beta \quad (15)$$

$$\pi_I(C, \odot, N) = \underbrace{\pi_E(I_P + I_C; E_C)}_{\pi_E^{t=1}} + \underbrace{\pi_E(I_P + I_C; E_C)}_{\pi_E^{t=2}} = 2(u + \delta) \quad (16)$$

**Calculate  $F_S^{YY}$**

Plug (11) and (12) into (9):

$$F_S^{YY} = \pi_I(S, \odot, Y) - \pi_I(S, \emptyset, Y) = \delta(1 - \beta) \quad (17)$$

**Calculate  $F_C^{YY}$**

Plug (14) and (15) into (9):

$$F_C^{YY} = \pi_I(C, \odot, Y) - \pi_I(C, \emptyset, Y) = 2\delta(1 - \beta) \quad (18)$$

**Calculate  $F_S^{YN}$**

Plug (13) and (12) into (10):

$$F_S^{YN} = \pi_I(S, \odot, N) - \pi_I(S, \emptyset, Y) = u + \delta(2 - \beta) \quad (19)$$

**Calculate  $F_C^{YN}$**

Plug (16) and (15) into (10):

$$F_C^{YN} = \pi_I(C, \odot, N) - \pi_I(C, \emptyset, Y) = \delta(2 - 3\beta) \quad (20)$$

## 2.1 Additional thresholds for the game with acquisitions

Benefits of the incumbent for different choices with acquisition, if the entrant chooses to develop a substitute (see Proposition 4):

$$\pi_I^{ACQ}(S, \emptyset, Y) = \pi_I(S, \emptyset, Y) + \underbrace{\pi^{ACQ}/2}_{=u/2} = 3/2u + \delta\beta \quad (21)$$

If  $A < \bar{A}_S$ ,  $\pi^{ACQ} = \Delta - K$ :

$$\pi_I^{ACQ}(S, \odot, Y) = \pi_I(S, \odot, N) + \pi^{ACQ}/2 = 2(u + \delta) + \frac{\Delta - K}{2} - F \quad (22)$$

If  $A \geq \bar{A}_S$ ,  $\pi^{ACQ} = u + \delta$ :

$$\pi_I^{ACQ}(S, \odot, Y) = \pi_I(S, \odot, Y) + \pi^{ACQ}/2 = \frac{3(u + \delta)}{2} - F \quad (23)$$

**Calculate  $F_S^{ACQ}$**

If  $A \geq \bar{A}_S$ , plug (23) and (21) into (9):

$$F_S^{ACQ} = \pi_I^{ACQ}(S, \odot, Y) - \pi_I^{ACQ}(S, \emptyset, Y) = \delta(3/2 - \beta) \quad (24)$$

If  $A < \bar{A}_S$ , plug (22) and (21) into (9):

$$F_S^{ACQ} = \pi_I^{ACQ}(S, \odot, Y) - \pi_I^{ACQ}(S, \emptyset, Y) = \frac{\Delta + u - K}{2} + \delta(2 - \beta) \quad (25)$$

Benefits of the incumbent for different choices with acquisition, if the entrant chooses to develop a complement (see Proposition 4):

$$\pi_I^{ACQ}(C, \emptyset, Y) = \pi_I(C, \emptyset, Y) + \underbrace{\pi^{ACQ}/2}_{=0} = 2u + 3\delta\beta \quad (26)$$

If  $A < \overline{A}_C$ ,  $\pi^{ACQ} = \frac{\delta-K}{2}$ :

$$\pi_I^{ACQ}(C, \odot, Y) = \pi_I(C, \odot, N) + \pi^{ACQ}/2 = 2(u + \delta) - F + \frac{\delta - K}{2} \quad (27)$$

If  $A \geq \overline{A}_C$ ,  $\pi^{ACQ} = 0$ :

$$\pi_I^{ACQ}(C, \odot, Y) = \pi_I(C, \odot, Y) = 2u + \delta(2 + \beta) - F \quad (28)$$

**Calculate  $F_C^{ACQ}$**

If  $A \geq \overline{A}_C$ , plug (28) and (26) into (9):

$$F_C^{ACQ} = \pi_I^{ACQ}(C, \odot, Y) - \pi_I^{ACQ}(C, \emptyset, Y) = 2\delta(1 - \beta) \quad (29)$$

If  $A < \overline{A}_C$ , plug (27) and (26) into (9):

$$F_C^{ACQ} = \pi_I^{ACQ}(C, \odot, Y) - \pi_I^{ACQ}(C, \emptyset, Y) = \delta(5/2 - \beta) - K/2 \quad (30)$$